Homework 2 Applied Mutlivariate Analysis

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1 Workspace

1.1 Packages

```
library(car)
library(knitr)
library(kableExtra)
library(multcomp)
library(lme4)
library(plyr)
library(tidyverse)
```

1.2 data

The file, Set_2.csv, contains data for four variables and four groups.

```
wd <- "https://github.com/emoriebeck/homeworks/raw/master/multivariate/homeworks/homework2"
dat <- sprintf("%s/Set_2(1).csv", wd) %>%
 read_csv() %>%
 mutate(Group = factor(Group))
head(dat)
## # A tibble: 6 x 5
   Group DV1 DV2 DV3 DV4
  <fct> <int> <int> <int> <int>
3
## 5 1
                1 1
                          1
       4 4 1
## 6 1
long_dat <- dat %>%
 mutate(SID = 1:n()) \%
 gather(key = DV, value = value, DV1:DV4)
```

2 Question 1

Conduct a standard ANOVA on each of the measures using aov(). Are the groups different on each of the measures? If so, conduct post-hoc comparisons using Holm correction, indicating the pairs of means that are significantly different.

```
Q1 <- long_dat %>%
 group_by(DV) %>%
 nest() %>%
 mutate(aov = map(data, ~aov(value ~ Group, data = .)),
        tidy = map(aov, broom::tidy))
Q1 %>% unnest(tidy) %>% filter(term == "Group")
## # A tibble: 4 x 7
##
   DV
          term
                  df sumsq meansq statistic p.value
    <chr> <chr> <dbl> <dbl> <dbl> <dbl>
                    3 100.
## 1 DV1
          Group
                             33.4
                                     19.4 6.40e-10
## 2 DV2
          Group
                    3 48.6 16.2
                                      7.14 2.22e- 4
## 3 DV3
                    3 30.9 10.3
                                       6.03 8.33e- 4
          Group
## 4 DV4
          Group
                    3 21.8
                            7.28
                                      3.79 1.28e- 2
```

There are group differences on all DV's.

```
compMat <- rbind(</pre>
  c(1,-1, 0, 0), # 1 v 2
  c(1,0,-1,0), #1 v 3
  c(1, 0, 0, -1), #1 v 4
  c(0,1,-1,0), #2 v 3
  c(0,1,0,-1), #2 v 4
  c(0,0,1,-1) #3 v 4
rownames(compMat) <- c("1 v 2", "1 v 3", "1 v 4",
                    "2 v 3", "2 v 4", "3 v 4")
tab_fun <- function(x){</pre>
  x$confint %>% data.frame %>%
    mutate(Groups = rownames(.)) %>%
    select(Groups, everything())
Q1 <- Q1 %>%
  mutate(comp = map(aov, ~glht(., linfct=compMat, alternative="two.sided",rhs=0)),
         summ = map(comp, ~confint(., adjusted("holm"))),
         tab = map(summ, tab_fun))
Q1 %>% unnest(tab) %>%
  mutate(sign = ifelse(sign(lwr) != sign(upr), "ns", "sig")) %>%
  mutate_at(vars(Estimate:upr), funs(sprintf("%.2f", .))) %>%
  mutate(CI = sprintf("[%s, %s]", lwr, upr)) %>%
  mutate_at(vars(Estimate, CI), funs(ifelse(sign == "sig", sprintf("\\textbf{%s}", .), .))) %>%
  select(-lwr, -upr, -sign, b = Estimate) %>%
  gather(key = est, value = value, b, CI) %>%
  unite(tmp, DV, est, sep = ".") %>%
```

Table 1: Question 1: Pairwise Comparisons

	DV1		$\mathrm{DV}2$		DV3		DV4	
Groups	b	CI	b	CI	b	CI	b	CI
1 v 2	1.68	[0.16, 3.20]	2.60	[0.85, 4.35]	1.96	[0.44, 3.48]	1.64	[0.03, 3.25]
1 v 3	2.08	[0.56,3.60]	2.76	[1.01,4.51]	3.40	[1.88, 4.92]	1.76	[0.15,3.37]
1 v 4	-0.16	[-1.68, 1.36]	1.12	[-0.63, 2.87]	$\bf 2.52$	[1.00,4.04]	2.08	[0.47,3.69]
2 v 3	0.40	[-0.56, 1.36]	0.16	[-0.95, 1.27]	1.44	[0.48, 2.40]	0.12	[-0.90, 1.14]
2 v 4	-1.84	[-2.80, -0.88]	-1.48	[-2.59, -0.37]	0.56	[-0.40, 1.52]	0.44	[-0.58, 1.46]
3 v 4	-2.24	[-3.20, -1.28]	-1.64	[-2.75, -0.53]	-0.88	[-1.84, 0.08]	0.32	[-0.70, 1.34]

3 Question 2

Now combine all of the information for groups and variables into a no-intercept model using lmer. Test the following hypotheses about group differences by constructing an appropriate contrast using glht in the multcomp package.

```
Q2 <- long_dat %>%
  mutate(DV = str_remove(DV, "DV"),
         G1 = mapvalues(Group, 1:4, c(1,0,0,0)),
         G2 = mapvalues(Group, 1:4, c(0,1,0,0)),
         G3 = mapvalues(Group, 1:4, c(0,0,1,0)),
         G4 = mapvalues(Group, 1:4, c(0,0,0,1)),
         DV1 = mapvalues(DV, 1:4, c(1,0,0,0)),
         DV2 = mapvalues(DV, 1:4, c(0,1,0,0)),
         DV3 = mapvalues(DV, 1:4, c(0,0,1,0)),
         DV4 = mapvalues(DV, 1:4, c(0,0,0,1))) \%
  mutate_at(vars(G1:G4, DV1:DV4), funs(as.numeric(as.character(.)))) %>%
  # group_by(DV) %>%
  nest() %>%
  mutate(mod = map(data, ~lme4::lmer(value ~ -1 + G1:DV1 + G1:DV2 + G1:DV3 + G1:DV4 +
                                       G2:DV1 + G2:DV2 + G2:DV3 + G2:DV4 +
                                       G3:DV1 + G3:DV2 + G3:DV3 + G3:DV4 +
                                       G4:DV1 + G4:DV2 + G4:DV3 + G4:DV4 +
                                       (1|SID), data = .)),
         tidy = map(mod, broom::tidy))
Q2 %>% unnest(tidy) %>%
  filter(group == "fixed") %>%
  separate(term, c("DV", "Group"), sep = ":", remove = F) %>%
  mutate(DV = ifelse(DV == "G1", Group, DV),
         Group = ifelse(grepl("G1", term), "G1", Group)) %>%
  mutate_at(vars(estimate:std.error), funs(sprintf("%.2f", .))) %>%
```

Table 2: Question 2: Model Estimated Means

	DV1		DV2		DV3		DV4	
Groups	b	SE	b	SE	b	SE	b	SE
G1	2.44	0.28	2.80	0.28	3.12	0.28	2.84	0.28
G2	3.20	0.28	3.00	0.28	4.28	0.28	4.04	0.28
G3	2.80	0.28	2.84	0.28	2.84	0.28	3.92	0.28
G4	5.04	0.28	4.48	0.28	3.72	0.28	3.60	0.28

Test these hypotheses for each of the four measures: 12contrastsinall, correctusing the Holmmethod.

3.1 Part A

The mean for Group 1 is different from the mean for Group 3

```
C1 <- cbind(diag(1, 4, 4), diag(0, 4, 4), diag(-1, 4, 4), diag(0,4,4))
rownames(C1) <- paste(paste("DV", 1:4, sep = ""), ": 1 v 3", sep = "")
```

3.2 Part B

The mean of Groups 1, 2, and 3 is different from the mean for Group 4

```
C2 <- cbind(diag(1, 4, 4), diag(1, 4, 4), diag(1, 4, 4), diag(-3,4,4))
rownames(C2) <- paste(paste("DV", 1:4, sep = ""), ": 1+2+3 v 4", sep = "")
```

3.3 Part C

The mean of Groups 1 and 2 is different from the mean for Groups 3 and 4

```
C3 <- cbind(diag(1, 4, 4), diag(1, 4, 4), diag(-1, 4, 4), diag(-1,4,4))
rownames(C3) <- paste(paste("DV", 1:4, sep = ""), ": 1+2 v 3+4", sep = "")
```

```
compMat <- rbind(C1, C2, C3)

tab_fun <- function(x){
   x$confint %>% data.frame %>%
    mutate(Groups = rownames(x$confint)) %>%
```

Table 3: Question 2: Group Combinations

DV1		DV2		DV3		DV4		
Groups	b	CI	b	CI	b	CI	b	CI
	-2.20	[-1.45, 0.73] [-3.74, -0.66] [-9.36, -4.00]	-1.52	[-1.13, 1.05] [-3.06, 0.02] [-7.48, -2.12]	0.28 0.84 -0.92	[-0.81, 1.37] [-0.70, 2.38] [-3.60, 1.76]	-0.64	[-2.18, 0.90]

```
select(Groups, everything())
Q2 <- Q2 %>%
 mutate(comp = map(mod, ~glht(., linfct=compMat, alternative="two.sided",rhs=0)),
        summ = map(comp, ~confint(., adjusted("holm"))),
        tab = map(summ, tab_fun))
Q2 %>% unnest(tab) %>%
 mutate(sign = ifelse(sign(lwr) != sign(upr), "ns", "sig")) %>%
 mutate_at(vars(Estimate:upr), funs(sprintf("%.2f", .))) %>%
 mutate(CI = sprintf("[%s, %s]", lwr, upr)) %>%
 select(-lwr, -upr, -sign, b = Estimate) %>%
 separate(Groups, c("DV", "Groups"), sep = ": ") %>%
 gather(key = est, value = value, b, CI) %>%
 unite(tmp, DV, est, sep = ".") %>%
 spread(tmp, value) %>%
 kable(., "latex", booktabs = T, escape = F,
       col.names = c("Groups", rep(c("b", "CI"), times = 4)),
       caption = "Question 2: Group Combinations") %>%
 add_header_above(c(" " = 1, "DV1" = 2, "DV2" = 2, "DV3" = 2, "DV4" = 2))
```

4 Question 3

3. Now construct contrasts for the following hypotheses, ignoring groups (3 contrasts, correct using the Holm method).

4.1 Part A

The mean for DV1 is different from the mean for DV2

```
C1 <- c(1,-1,0,0, 1,-1,0,0, 1,-1,0,0)
```

4.2 Part B

The mean for DV1 and DV2 is different from the mean for DV3 and DV4

```
C2 \leftarrow c(1,1,-1,-1, 1,1,-1,-1, 1,1,-1,-1, 1,1,-1,-1)
```

Table 4: Question 3: Mean Differences Across Variables

Groups	b	CI
DV1 v. DV2	0.36	[-1.04, 1.76]
DV1+DV2 v. $DV3+DV4$	-1.76	[-3.74, 0.22]
$DV1+DV2+DV3 ext{ v } DV4$	-2.64	[-6.07, 0.79]

4.3 Part C

The mean for DV1, DV2, and DV3 is different from the mean for DV4

```
C3 <- c(1,1,1,-3, 1,1,1,-3, 1,1,1,-3)
```

5 Question 4

4. Finally, test each of the hypotheses from Question 3, but combine them with each of the following group questions (a total of 9 contrasts, correct using the Holm method):

5.1 Part A

Just consider Group 1 alone

5.2 Part B

Compare Group 2 to Group 3

```
C2 <- rbind(
    # variable 1 v 2

# (DV1:G2 - DV1:G3 - DV2:G2 + DV2:G3)
    c(0,0,0,0, 1,-1,0,0, -1,1,0,0, 0,0,0,0),

# variable 1+2 v. 3+4

# ((DV1:G2 + DV2:G2) = (DV3:G2 + DV4:G2)) = ((DV1:G3 + DV2:G3) = (DV3:G3 + DV4:G3))

# (DV1:G2 + DV2:G2 - DV3:G2 - DV4:G2 - DV1:G3 - DV2:G3 + DV3:G3 + DV4:G3) = 0

c(0,0,0,0, 1, 1,-1,-1, -1,-1,1,1, 0,0,0,0),

# variable 1+2+3 v 4

# ((DV1:G2 + DV2:G2 + DV3:G2) = DV4:G2) = ((DV1:G3 + DV2:G3 + DV3:G3) + DV4:G3)

# (DV1:G2 + DV2:G2 + DV3:G2 - DV4:G2 - DV1:G3 - DV2:G3 - DV3:G3 + DV4:G3) = 0

c(0,0,0,0, 1,1,1,-3, -1,-1,-1,3, 0,0,0,0)
)

rownames(C2) <- c("DV1vDV2:G2vG3", "DV1+2vDV3+4:G2vG3", "DV1+2+3vDV4:G2vG3")
```

5.3 Part C

Compare Group 1 to the combination of Groups 2, 3, and 4.

```
C3 <- rbind(
    # variable 1 v 2

# (DV1:G1 = (DV1:G2 + DV1:G3 + DV1:G4)) = (DV2:G1 = (DV2:G2 + DV2:G3 + DV2:G4))

# (DV1:G1 - DV1:G2 - DV1:G3 - DV1:G4 - DV2:G1 + DV2:G2 + DV2:G3 + DV2:G4) = 0

c(3,-3,0,0, -1,1,0,0, -1,1,0,0, -1,1,0,0),

# variable 1 + 2 v 3 + 4

# ((DV1:G1 + DV2:G1 - DV3:G1 - DV4:G1)) - DV1:G2 - DV1:G3 - DV1:G4 - DV2:G2 - DV2:G3 - DV2:G4 + DV3:G

c(3,3,-3,-3, -1,-1,1,1, -1,-1,1,1,1,1),

# variable 1 + 2 + 3 v 4

# ((DV1:G1 + DV2:G1 + DV3:G1) = DV4:G1) = ((DV1:G2 + DV2:G2 + DV3:G2 + DV1:G3 + DV2:G3 + DV3:G3 + DV1

# DV1:G1 + DV2:G1 + DV3:G1 - DV4:G1 - DV1:G2 - DV2:G2 - DV3:G2 - DV1:G3 - DV2:G3 - DV3:G3 - DV1:G4 - c(3,3,3,-9, -1,-1,-1,3, -1,-1,-1,3, -1,-1,-1,3)
)

rownames(C3) <- c("DV1vDV2:G1vG2+3+4", "DV1+2vDV3+4:G1vG2+3+4", "DV1+2+3vDV4:G1vG2+3+4")
```

```
(compMat <- rbind(C1,C2,C3))</pre>
##
                     [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## DV1vDV2:G1
                           -1
                                0
                                    0
                                         0
                                             0
                                                  0
## DV1+2vDV3+4:G1
                        1
                            1
                                -1
                                    -1
                                         0
                                             0
                                                  0
                                                      0
                                                          \cap
                                                                \cap
## DV1+2+3vDV4:G1
                           1
                               1
                                    -3
                                           0
                                                          0
                       1
                                            -1
## DV1vDV2:G2vG3
                        0
                           0
                               0
                                    0
                                                    0
                                                        -1
                                         1
                                                 0
                                                                1
                          0
## DV1+2vDV3+4:G2vG3
                       0
                                0
                                     0
                                         1
                                             1
                                                 -1
                                                     -1
                                                          -1
                      0 0 0
## DV1+2+3vDV4:G2vG3
                                   0
                                       1
                                            1 1
                                                     -3 -1
                                                               -1
## DV1vDV2:G1vG2+3+4
                      3 -3
                              0
                                     0
                                       -1
                                             1 0
                                                    0 -1
                                                               1
## DV1+2vDV3+4:G1vG2+3+4 3 3
                                                    1
                              -3
                                        -1
                                            -1
                                                1
                                                         -1
                                                               -1
                                   -3
## DV1+2+3vDV4:G1vG2+3+4
                       3
                           3
                                3
                                   -9
                                        -1
                                            -1 -1
                                                         -1
                                                               -1
##
                     [,11] [,12] [,13] [,14] [,15] [,16]
## DV1vDV2:G1
                         0
                             0
                                   0
                                        0
                         0
                                             0
## DV1+2vDV3+4:G1
                              0
                                   0
                                        0
## DV1+2+3vDV4:G1
                            0
                                0 0 0
```

Table 5: Question 4: Group x DV Combinations

	DV1+2+3 v DV4		V1+	2 v DV3+4	DV1 v DV2	
Groups	b	CI	b	CI	b	CI
G1		[-2.12, 1.80]				
G1vG2+3+4 G2vG3	$\frac{2.00}{1.64}$			[-5.03, 2.79] [-2.60, 0.60]		

```
## DV1vDV2:G2vG3
## DV1+2vDV3+4:G2vG3
                           1
                                 1
                                            0
## DV1+2+3vDV4:G2vG3
                          -1
                                 3
                                      0
                                            0
                          0
                                                        0
## DV1vDV2:G1vG2+3+4
                                0
                                     -1
                                           1
                                                0
## DV1+2vDV3+4:G1vG2+3+4
                          1
                                 1
                                     -1
                                           -1
                                                 1
                                                        1
## DV1+2+3vDV4:G1vG2+3+4
                          -1
                                 3
                                     -1
                                           -1
                                                 -1
                                                        3
Q2 <- Q2 %>%
 mutate(compQ4 = map(mod, ~glht(., linfct=compMat, alternative="two.sided",rhs=0)),
        summQ4 = map(compQ4, ~confint(., adjusted("holm"))),
        tabQ4 = map(summQ4, tab_fun))
```

```
Q2 %>% unnest(tabQ4) %>%
  mutate(sign = ifelse(sign(lwr) != sign(upr), "ns", "sig")) %>%
  mutate_at(vars(Estimate:upr), funs(sprintf("%.2f", .))) %>%
  mutate(CI = sprintf("[%s, %s]", lwr, upr)) %>%
  mutate_at(vars(Estimate, CI), funs(ifelse(sign == "sig", sprintf("\\textbf{%s}", .), .))) %>%
  select(-lwr, -upr, -sign, b = Estimate) %>%
  separate(Groups, c("DV", "Groups"), sep = ":") %>%
  gather(key = est, value = value, b, CI) %>%
  unite(tmp, DV, est, sep = ".") %>%
  spread(tmp, value) %>%
  kable(., "latex", booktabs = T, escape = F,
        col.names = c("Groups", rep(c("b", "CI"), times = 3)),
        caption = "Question 4: Group x DV Combinations") %>%
  add_header_above(c(" " = 1, "DV1+2+3 v DV4" = 2, "V1+2 v DV3+4" = 2, "DV1 v DV2" = 2))
```