

$Y_i = (Y_{i1}, \dots, Y_{it}, \dots, Y_{n_i})$
 $E(Y_{it}) = \mu_{it}$
 $X_i = (x_{i1}, \dots, x_{it}, \dots, x_{in_i})'$ design matrix
 $g(\mu_{it}) = \eta_{it} = x_{it}^T \beta$
 $V(Y_{it}) = \phi a_{it} = \phi a(\mu_{it})$
 ϕ - dispersion parameter
 $V_i = \phi A_i^{1/2} R_i(\alpha) A_i^{1/2}$, where A_i is a diagonal matrix with k th diagonal element a_{ik}
 $D_i = A_i \frac{dg^{-1}(\eta_{ik})}{d\eta_{ik}} X_i$ Generalized estimating equations given by

$$\sum_{i=1}^K D_i^T V_i^{-1} (Y_i - \mu_i) = 0$$

std error = $1/a(\mu)$

Algorithm 1 GEE pseudocode

Initialize β, ϕ, α
while ! convergence **do**
 $\eta = \mathbf{X}\beta$
 $\mu = g^{-1}(\eta)$
 $e_{ik} = (y_{ik} - \mu_{ik})/\sqrt{a_{ik}}$
 $\phi = \frac{1}{(\sum n_i) - p} \sum_{i=1}^K \sum_{j=1}^{n_i} e_{ij}^2$
 Update $\alpha, R(\alpha)$ using ϕ and e_{ik}
 Calculate $R(\alpha)^{-1}$ numerically
 Update β using estimating equations
end while
Calculate sandwich variance estimator
