

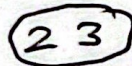
Question 1:

a) 2-3 Tree:

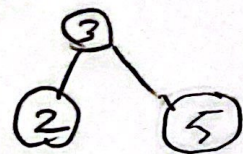
Insert 2:



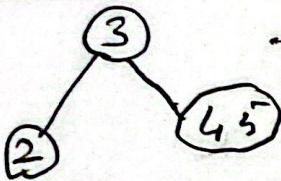
Insert 3:



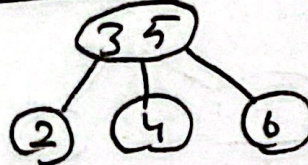
Insert 5:



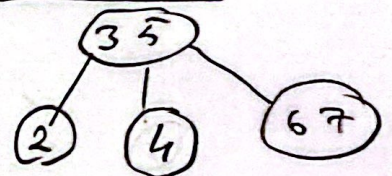
Insert 4:



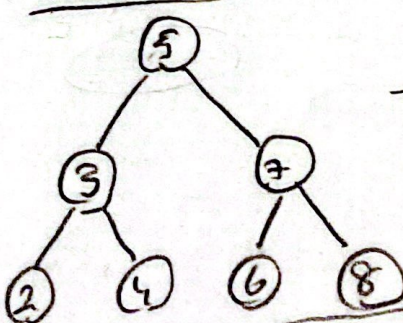
Insert 6:



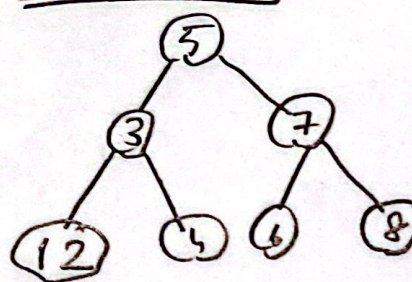
Insert 7:



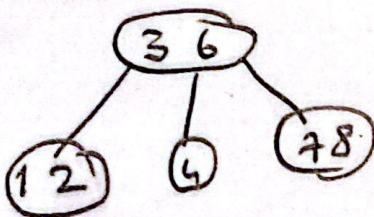
Insert 8:



Insert 1:



Delete 5:



Delete 6:



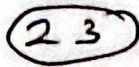


### b) 2-3-4 Tree:

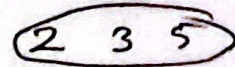
Insert 2:



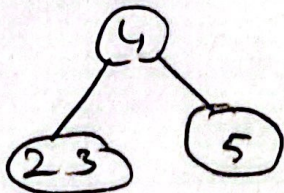
Insert 3:



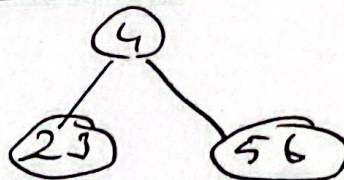
Insert 5:



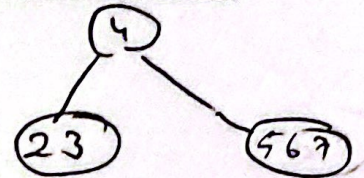
Insert 4:



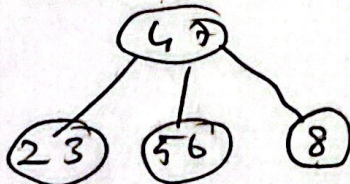
Insert 6:



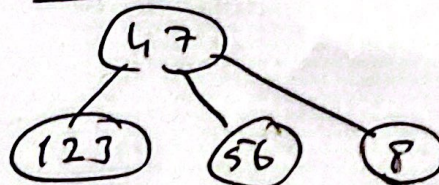
Insert 7:



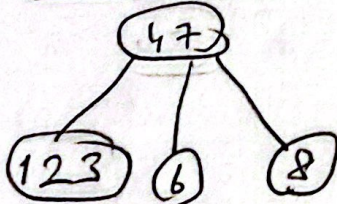
Insert 8:



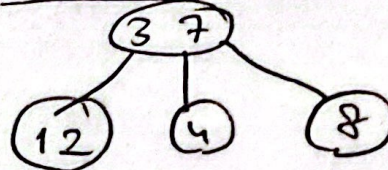
Insert 1:



Delete 5:



Delete 1:

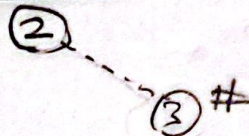


c) Red-Black Tree: Note that Red nodes are represented by #

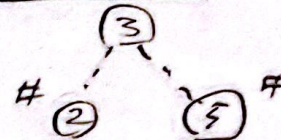
Insert 2:



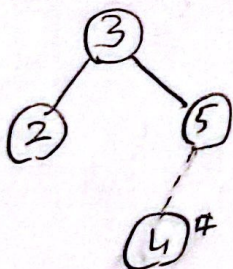
Insert 3:



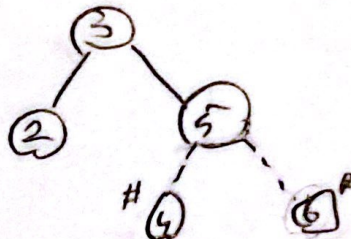
Insert 5:



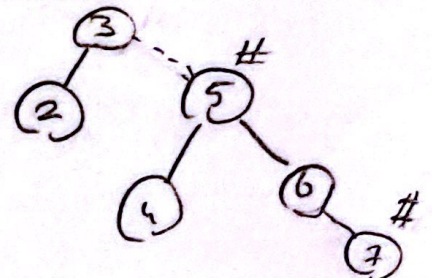
Insert 4:



Insert 6:

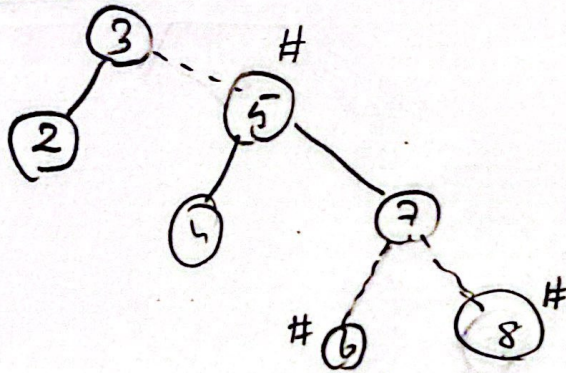


Insert 7:

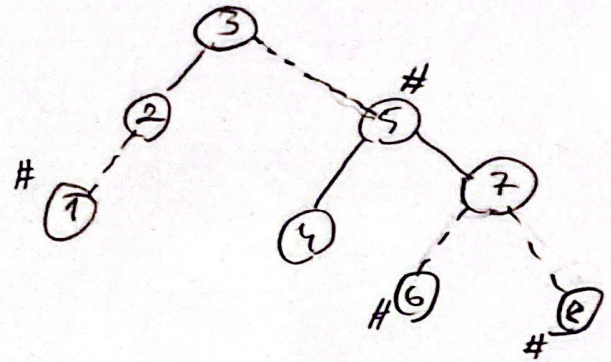




Insert 8:



Insert 1:



Note that → Red pointers are shown with " - - - - - "  
 → Black pointers are shown with " ——— "



## QUESTION 2

a) Table size: 17

### Step 1

$$20 \bmod 17 = 3$$

	0
	1
	2
20	3
	4
	5
	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 2

$$36 \bmod 17 = 2$$

	0
	1
36	2
20	3
	4
	5
	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 3

$$2 \bmod 17 = 2$$

$$2+1, 2+2 = 4 \bmod 17 = 4$$

	0
	1
36	2
20	3
2	4
	5
	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 4

$$19 \bmod 17 = 2$$

$$2+1, 2+2, 2+3 = 5 \bmod 17 = 5$$

	0
	1
36	2
20	3
2	4
19	5
	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 5

$$53 \bmod 17 = 2$$

$$2+1, 2+2, 2+3, 2+4 = 6 \bmod 17 = 6$$

	0
	1
36	2
20	3
2	4
19	5
53	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 6

$$34 \bmod 17 = 0$$

24	0
36	1
20	2
2	3
19	4
53	5
	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16

### Step 7

$$37 \bmod 17 = 3$$

$$3+1, 3+2, 3+3, 3+4 = 7, 11$$

24	0
36	1
20	2
2	3
19	4
53	5
37	6
	7
	8
	9
	10
	11
	12
	13
	14
	15
	16



b) open addressing with quadratic probing

Table size: 17

- ①  $20 \bmod 17 = 3$
- ②  $36 \bmod 17 = 2$
- ③  $2 \bmod 17 = 2$   
 $2 + 1^2, 2 + 2^2 = 6 \bmod 17 = 6$
- ④  $19 \bmod 17 = 2$   
 $2 + 1^2, 2 + 2^2, 2 + 3^2 = 11 \bmod 17 = 11$
- ⑤  $53 \bmod 17 = 2$   
 $2 + 1^2, 2 + 2^2, 2 + 3^2, 2 + 4^2 = 18 \bmod 17 = 1$
- ⑥  $34 \bmod 17 = 0$
- ⑦  $37 \bmod 17 = 3$   
 $3 + 1^2 = 4 \bmod 17 = 4$

0	34	⑥ ←
1	53	⑤ ←
2	36	② ←
3	20	① ←
4	37	⑦ ←
5		
6	2	③ ←
7		
8		
9		
10		
11	19	④ ←
12		
13		
14		
15		
16		

c) Separate chaining

Table size 17. Values: 20, 36, 19, 53, 34, 37  
 for every value  $x \bmod 17$  must be at most 3. Because of  
 that for simplicity, 0, 1, 2, 3 table rows drawn there

