

# Student Information

Name : Emre Geçit  
ID : 2521581

## Question 1

Design a Turing machine which recognizes the language  $L = 0^N 1^N | N \geq 1$ .  
 $\Sigma = \{0, 1, \sqcup\}$ , means that you cannot write any other symbol than these symbols.

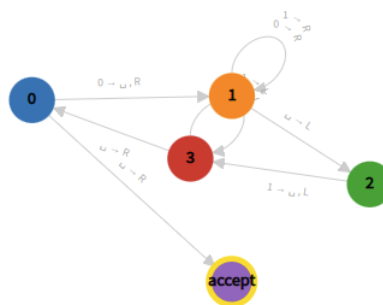
### Solution:

Descriptions for the states:

- State 0 (Initial state): If the tape head is on a 0, changes it with a blank space, moves the tape head to right, and passes to the state 1. If it is on a blank space, passes to the acceptance state.
- State 1: This state's task is finding the right end of the string. After finding the rightmost character in the string, the machine passes to state 2.
- State 2: If the tape head is on a 1, changes it with a blank space, moves the tape head to left, and passes to the state 3. If it is on a blank space, passes to the acceptance state.
- State 3: This state's task is finding the left end of the string. After finding the leftmost character in the string, the machine passes to state 0.

Note that in these descriptions, undefined transistions leads to rejection of the string.

Figure 1: Turing machine which recognizes the language  $L = 0^N 1^N | N \geq 1$



Sample inputs:  
12cm

Figure 2: Input = 000111

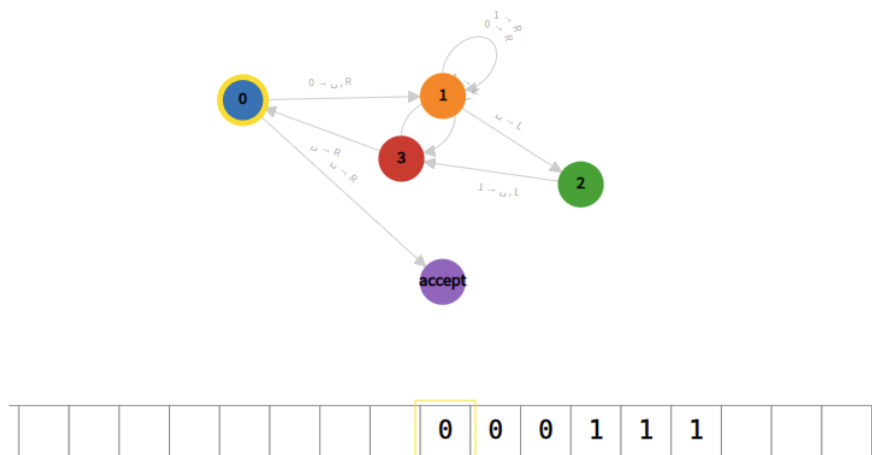


Figure 3: Input = 000111, Output = Accepted

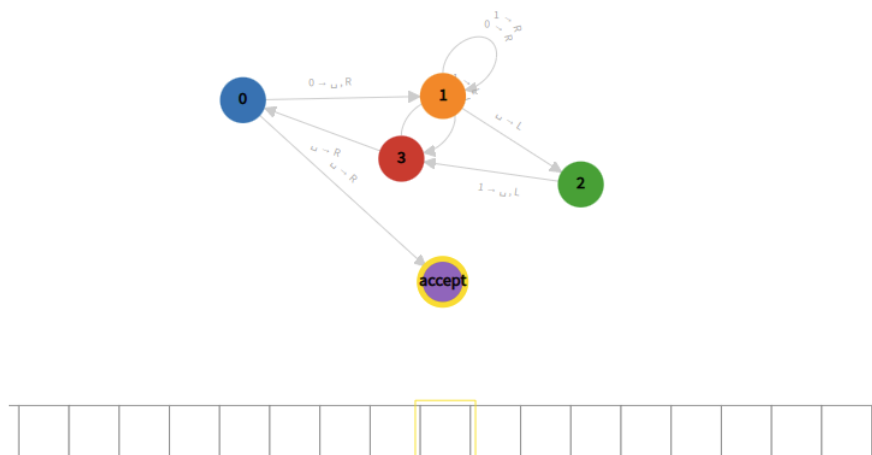


Figure 4: Input = 0000111

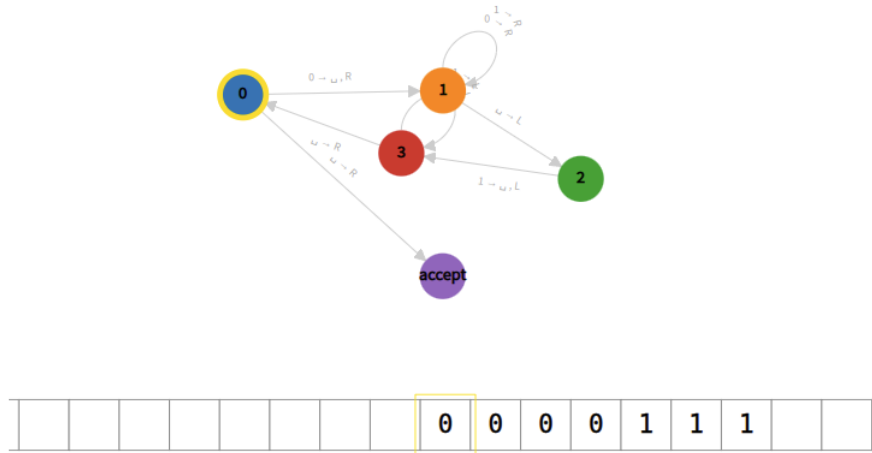


Figure 5: Input = 0000111, Output = Rejected

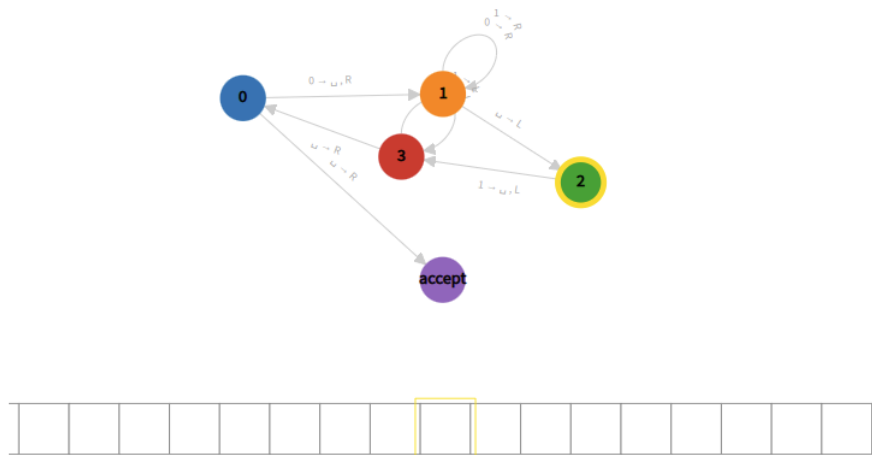


Figure 6: Input = 000011111

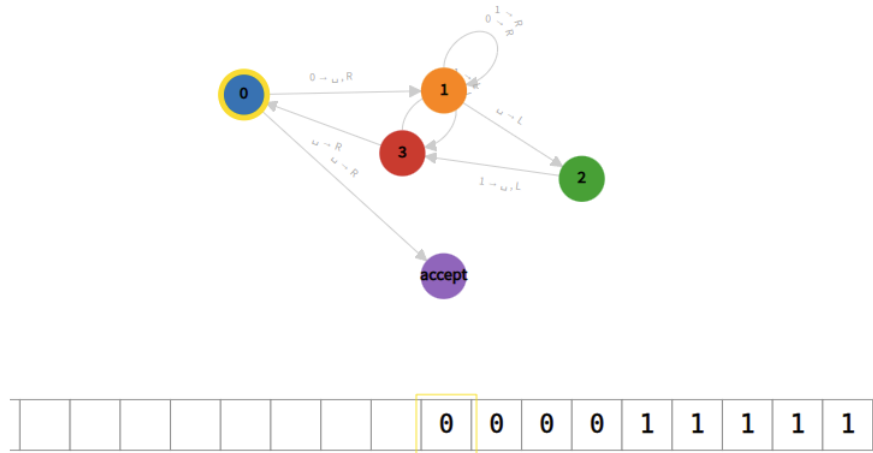


Figure 7: Input = 000011111, Output = Rejected

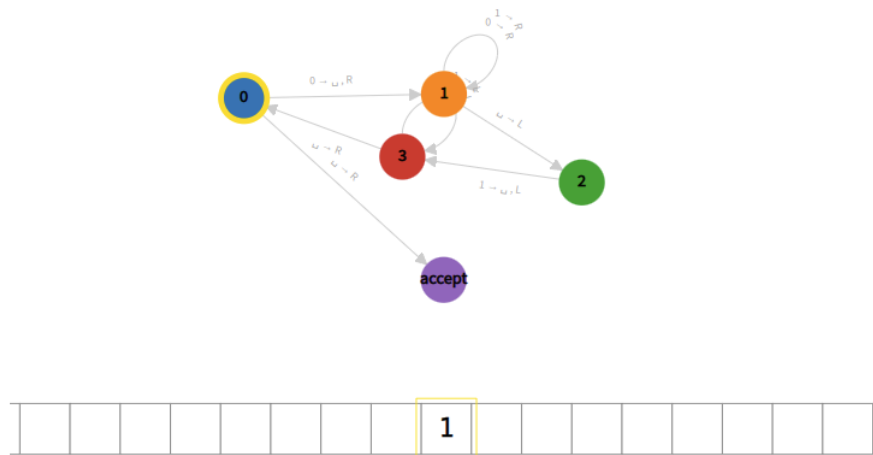


Figure 8: Input = 0001110

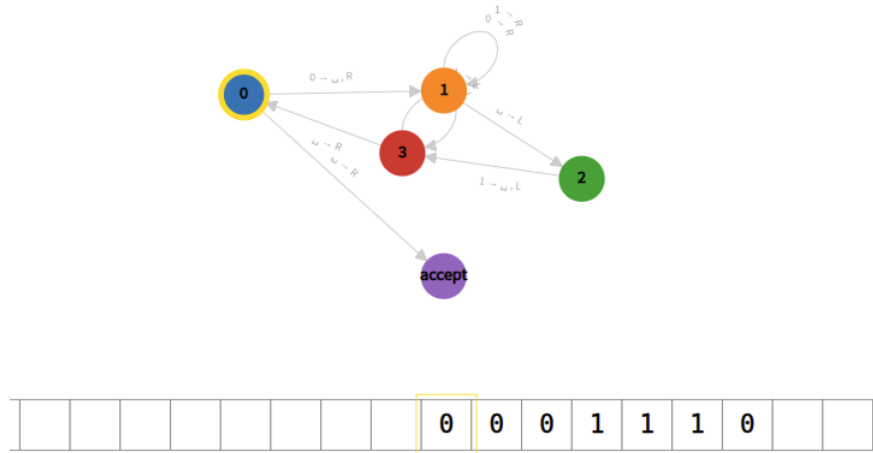


Figure 9: Input = 0001110, Output = Rejected

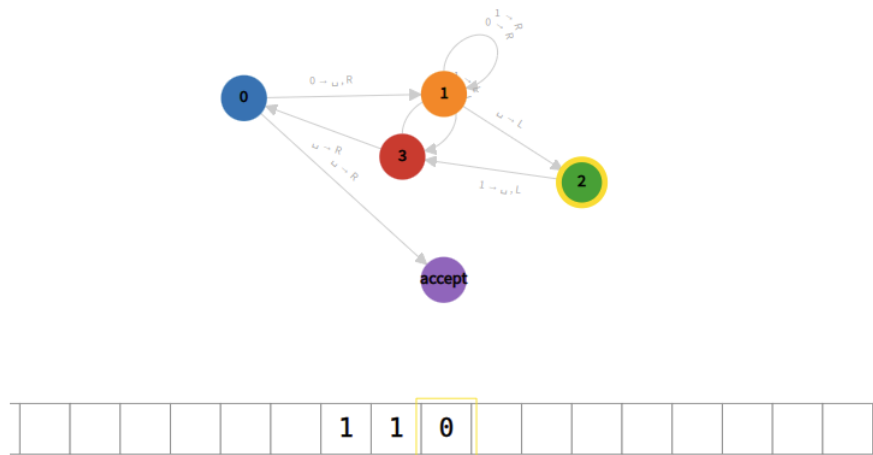


Figure 10: Input = 100011

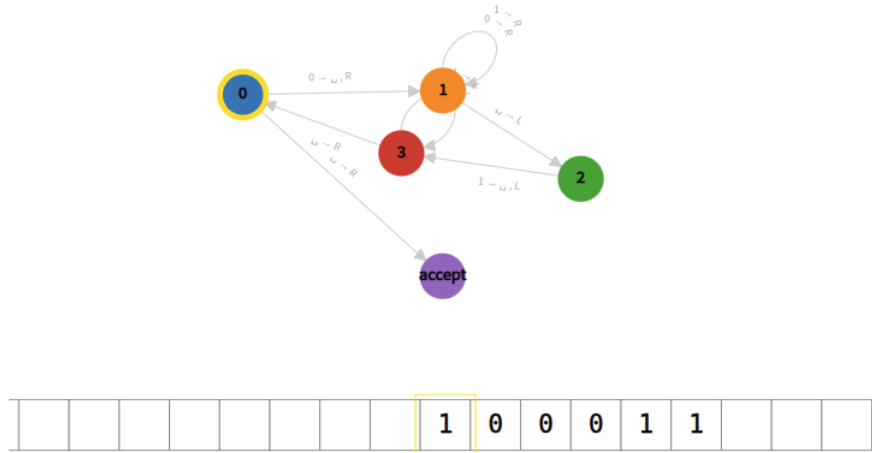
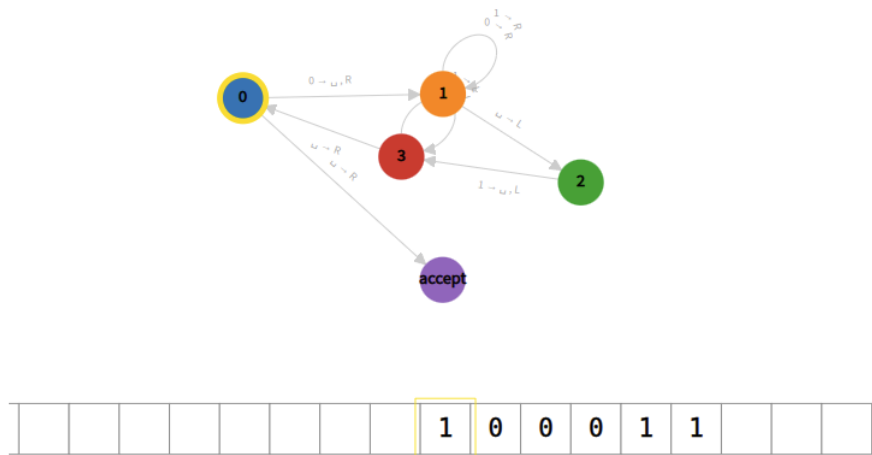


Figure 11: Input = 100011, Output = Rejected



## Question 2

a)

b)

## Question 3

a)

b)