

MONCHI: Multi-scheme Optimization For Collaborative Homomorphic Identification

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ABSTRACT

This paper introduces a novel protocol for privacy-preserving biometric identification, named MONCHI, that combines the use of homomorphic encryption for the computation of the identification score with function secret sharing to obliviously compare this score with a given threshold and finally output the binary result. Given the non-negligible cost of homomorphic encryption, BFV in this solution, we also study and evaluate the integration of two packing solutions that enable the regrouping of multiple templates in one ciphertext to improve efficiency meaningfully. We propose an end-to-end protocol, prove it secure and implement it. Our experimental results attest to MONCHI's applicability to the real-life use case of an airplane boarding scenario with 1000 passengers, where it takes less than one second to authorize/deny access to the plane to each passenger via biometric identification while maintaining the privacy of all passengers.

CCS CONCEPTS

• Security and privacy → Privacy-preserving protocols.

KEYWORDS

Multiparty Homomorphic Encryption, Functional Secret Sharing, Secure Two Party Computation, Masking, Privacy Preserving Technologies, Scalar Product

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1 INTRODUCTION

Biometric identification and authentication are being increasingly adopted in a wide range of applications including law enforcement, banking¹, personal hardware, and airport security². Users are identified based on their unique biological traits (e.g., fingerprint, face, iris), making systems more secure. Biometric systems

usually compute the so-called identification scores through scalar products between a fresh biometric template and templates that were collected in a prior enrollment phase, then stored in a reference database. This score is further compared to a pre-defined threshold and when exceeded, identification is considered successful.

The collection and processing of biometric data raises significant privacy concerns because such data uniquely identifies the individual and cannot be cancelled or re-issued. Therefore, the use of privacy enhancing technologies in such a context is crucial. Privacy-preserving identification systems call for advanced cryptographic techniques such as fully homomorphic encryption (FHE)[12] or multi-party computation[19], that enable computation while data being protected. While this technology ensures that biometric data is never revealed, it still incurs significant overhead and refrains their wide adoption.

In this paper, we study the suitability of FHE for biometric identification in the context of airport applications where passengers are authorized to board the plane only when identification is successful³. As opposed to the use of MPC, FHE does not consume any pre-processing and therefore results in a lighter and one-shot offline phase. To efficiently perform the final comparison operation, similar to [19], we propose that combines the use of FHE, BFV[7, 13] in this application, with function secret sharing[5, 6]. Hence, once the scalar product is computed, masks and splits this score to be distributed among two parties who further collaboratively decrypt the masked score and compare it to the threshold. To improve efficiency even more, we focus on the computation of scalar products and propose to study and evaluate the integration of two packing methods that enable the encoding of multiple templates in one ciphertext and hence increase performance in terms of communication and computation.

By leveraging FHE, MONCHI perfectly fits the airport access control use-case: given that linear operations are carried out without the need for a continuous supply of pre-processing material, and contrary to pure MPC solutions, we reduce the interactions in the offline phase of these linear operations to a one-time setup. This combination yields the best of both worlds, since it removes the otherwise endless supply of pre-processing material required to execute pure MPC protocols while leveraging MPC for non-linear operations that are impractical via FHE.

Our main contributions can be summarized as follows:

- MONCHI is the first protocol that combines the use of FHE with function secret sharing in order not to disclose the identification score but the access decision;
- To improve performance even more, we propose to integrate two packing solutions and study their performance according to different metrics;

¹<https://www.mastercard.com/news/perspectives/2024/biometrics-will-soon-replace-passwords-once-and-for-all/>

²<https://www.fraport.com/en/newsroom/press-releases/2023/q4/using-facial-recognition-sita-and-fraport-enable-a-contactless-.html>

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³<https://www.theguardian.com/world/2024/jan/01/facial-recognition-could-replace-passports-at-uk-airport-e-gates>

- MONCHI is implemented and evaluated through real-life use case scenarios and more specifically to the airport application and demonstrated its feasibility: in an airplane boarding scenario with 1000 passengers, MONCHI takes less than one second to authorize/deny access to the plane.

2 RELATED WORK

There have been multiple solutions that have investigated the use of biometrics (see [32] for a review). These solutions like [2, 22, 31], usually compute the score while the templates are homomorphically encrypted (either using BFV or CKKS). Other solutions like [4, 12] also investigated the use of packing in this context. As opposed to MONCHI, all these solutions decrypt the actual identification score and further compare it to a given threshold. As shown in [14], revealing this identification score is harmful and can help attackers infer and finally disclose biometric templates. In MONCHI, decryption occurs over the masked score and the decryption key is never revealed.

Another noteworthy FHE-based work, Colmade [18], which also employs FHE for distance metric computation in biometrics, addresses this issue by performing vector-matrix multiplication followed by comparison to a threshold in the encrypted domain, and subsequent masking of the result, revealing only its least significant bit. However, performing the comparison in the encrypted domain in Colmade is orders of magnitude more computationally expensive than MONCHI.

Finally, as mentioned in the introduction, an alternative to the use of FHE for scalar products in biometric identification is the use of arithmetic secret sharing in a secure two-party computation (2PC) setting. AriaNN [30] employs arithmetic secret sharing to perform privacy-preserving distance metric computations, followed by a comparison with a threshold with FSS, requiring two rounds of online communication. Subsequently, Funshade [19] improves the communication overhead by employing a novel method for secret-sharing during 2PC called Π -Secret-Sharing (Π -SS). The new Π -SS protocol allows local additions and multiplications with only one round of communication in the online phase, thus outperforming AriaNN. In MONCHI, we chose to replace the 2PC Π -SS building block of Funshade with a distributed implementation of the Brakerski-Fan-Vercauteren (BFV) FHE scheme (together with dedicated packing solutions), and improve its performance keeping the FSS block for subsequent comparison with a fixed threshold. Leveraging BFV for linear operations, we effectively get rid of the associated pre-processing material (typically beaver triples), meaningfully simplifying the continuous operation of a biometric identification system built with MONCHI at the expense of an additional masking to adapt the numerical range of BFV to that of FSS while maintaining the privacy guarantees.

3 PRELIMINARIES

3.0 Notation

We use bold letters to denote matrices/vector (Eg. \mathbf{x}) and non-bold letters for scalars. R_v expresses a polynomial ring with integer coefficients modulo v . $a^{(i)}$ denotes the i -th feature/element/coefficient of a template/vector/polynomial. We use $\langle b \rangle_j$ to refer to share j in an arithmetic modular secret sharing of $b = \sum_{j=1}^K \langle b \rangle_j$. We denote

$[\cdot]_q$ the reduction modulo q , and $\lfloor \cdot \rfloor$, $\lceil \cdot \rceil$ the rounding to the previous and nearest integer respectively. When applied to polynomials, these reductions are performed coefficient-wise. We use $U(X)$ to denote a uniformly random distribution in X , and $\mathcal{N}(\mu, \sigma)$ to denote a Gaussian distribution with mean μ and standard deviation σ . $\mathbf{a} \cdot \mathbf{b} = \mathbf{c}$ to denote the element-wise/coefficient-wise multiplication of two vectors/polynomials where $c^{(i)} = a^{(i)} b^{(i)}$

3.1 BFV

Scheme 1 BFV(t, q, N, w, σ, B)

Input: t, q, N, σ, B : Security Parameters

BFV.SecKeyGen():

$s \leftarrow S_{R_q}$

Output: the secret key $sk = s$

BFV.PubKeyGen(sk):

$p_1 \leftarrow U_{[R_q]}$ and $e \leftarrow \chi_{[R_q]}$

Output: a public key $pk = (p_0, p_1) = (-sk \cdot p_1 + e, p_1)$

BFV.Encrypt(pk, m):

Let $pk = (p_0, p_1)$

$u \leftarrow S_{[R_q]}$ and $e_0, e_1 \leftarrow \chi_{[R_q]}$

$(c_{m_0}, c_{m_1}) = (\Delta m + u \cdot p_0 + e_0, u \cdot p_1 + e_1)$

Output: a ciphertext $c_m = (c_{m_0}, c_{m_1})$

BFV.Add(c_a, c_b):

Let $c_a = (c_{a_0}, c_{a_1}), (c_{b_0}, c_{b_1})$

$c_{add_0} = [c_{a_0} + c_{b_0}]_q$ and $c_{add_1} = [c_{a_1} + c_{b_1}]_q$

Output: the ciphertext $c_{add} = (c_{add_0}, c_{add_1})$

BFV.Mul(c_a, c_b):

Let $c_a = (c_{a_0}, c_{a_1}), (c_{b_0}, c_{b_1})$

$c_{mul_0} = [c_{a_0} \cdot c_{b_0}]_q$ and $c_{mul_1} = [c_{a_1} \cdot c_{b_1}]_q$

Output: the ciphertext $c_{mul} = (c_{mul_0}, c_{mul_1})$

BFV.Decrypt(sk, c_m):

Let $c_m = (c_{m_0}, c_{m_1})$

$m_{res} = \left\lceil \left\lfloor \frac{t}{q} [c_{m_0} + s \cdot c_{m_1}]_q \right\rfloor \right\rceil_t$

Output: the decrypted message m_{res}

The Brakerski-Fan-Vercauteren (BFV) [1, 13, 16] scheme is a privacy-preserving, ring-Learning with Errors (RLWE) homomorphic encryption scheme. The plaintext space is defined by a parameter t . Messages are encoded into the plaintext ring $R_t = \mathbb{Z}[X]/(X^N + 1)$, which defines polynomials of degree at most $N - 1$ with coefficients in \mathbb{Z}_t . Specifically, the coefficients lie in the range $[0, t)$ for non-negative integer and in the symmetric range $[-t/2, t/2)$ for signed integers. The encrypted message will be an element of $R_q = \mathbb{Z}[X]/(X^N + 1)$ with q , a security parameter defining the ciphertext modulus. The coefficients of the encrypted space reside in \mathbb{Z}_q . Typically, $t \ll q$ for security reasons, N is a power of two, and $\Delta = \lceil q/t \rceil$ defines the maximum number of homomorphic operations that can be performed on the ciphertext without affecting the correctness of the decrypted result. q can be decomposed with the Chinese Remainder Theorem (CRT) in small co-prime moduli q_1, \dots, q_v and establishing a ring isomorphism between the spaces \mathbb{Z}_q and $\prod_{i=1}^v \mathbb{Z}_{q_i}$ [16]. Thanks to CRT, arithmetic modulo q can be

replaced by v independent arithmetics in the smaller rings \mathbb{R}_{q_i} enabling Residue Number System (RNS) to accelerate arithmetic in R_q over large integers. .

The BFV scheme defines two uniform distributions: the secret key distribution $S_{R_q} = \mathbb{Z}\{-1, 0, 1\}[X]/(X^N + 1)$, defining ring polynomials of degree at most N with coefficients sampled from a uniform distribution $U\{-1, 0, 1\}$. The error distribution χ_{err} is defined over the ring R_q where coefficients are drawn from a distribution statistically close to a Gaussian with standard deviation σ truncated into $[-B, B]$, where σ and B are two cryptographic parameters. χ_{err} is related to the hardness of the RLWE problem, defined as: given uniformly random a from $U(R_q)$, s from S_{R_q} , and e from χ_{err} , it is computationally hard for an adversary, to distinguish between the distribution of $(sa + e, a)$ and that of (b, a) where b is sampled uniformly from $U(R_q)$. The RLWE problem was introduced in [23] as a version of the Learning-With-Error (LWE) problem [29]. In BFV, noise management is critical for maintaining correctness throughout the decryption process. BFV supports bootstrapping [11], which involves re-encrypting a ciphertext to get a fresh ciphertext of the same message, effectively resetting the noise growth. However, bootstrapping is practically slow, and despite suggested improvements in noise management [8][7], BFV is commonly instantiated with parameters sufficiently large to accommodate noise growth. Scheme 1 outlines several algorithms of the BFV scheme pertinent to our research.

Specifically, the algorithm BFV.Decrypt, which we aim to adapt and use in a distributed setting, involves using the secret key to compute an upscaled plaintext, followed by two rounding processes (first by q , then by t), with a downscaling step between the two rounding operations.

3.2 Multiparty BFV Scheme

Multiparty Homomorphic Encryption (MHE) extends FHE to multiparty settings, facilitating collaborative computation while maintaining the privacy of each party's data. The Distributed Brakerski-Fan-Vercauteren (DBFV) scheme [25], derived from the BFV scheme, permits a pool of M parties to locally secret-share a global secret key and to collaboratively generate a public key using these local shares, as detailed in Scheme 2. The process of computing a common public key (cpk) introduces M additional noise terms, resulting in $\sum_{i=1}^M e_i = \|e_{\text{cpk}}\| < B \cdot M$, where B is the bound on the worst-case norm for an error term drawn from the distribution χ_{err} (see appendix A of [25] for more details). Thus, the worst-case fresh ciphertext noise is linear in the number M of parties. Furthermore, in the decryption phase, each party computes their local decrypted share and then adds in freshly generated noise. This introduction of noise differs from the decryption algorithm used in the single-party BFV scheme and is crucial for addressing the RLWE problem within a distributed setting.

3.3 Plaintext encoding and packing

Despite advances on the efficiency of homomorphic encryption, homomorphic operations remain slow because of the large size of ciphertexts (which is due to the security requirements of the HE scheme). To address this, SIMD (Single Instruction, Multiple Data) instructions were proposed: they consist of packing the encryption

Scheme 2 DBFV(t, q, N, w, σ, B, M)

Input: t, q, N, w, σ, B : Security Parameters; M : Number of parties
DBFV.SecKeyGen() :

Each party P_i :

$s_i \leftarrow S_{R_q}$

Output: $\langle sk \rangle_1 = s_i$. Note $sk = [\sum_{i=1}^M \langle sk \rangle_i]_q$

DBFV.ColPubKeyGen($\langle sk \rangle_1, \dots, \langle sk \rangle_i, \dots, \langle sk \rangle_M$):

Any : $p_1 \leftarrow U(R_q)$. Disclose to all parties.

Each party P_i :

$e_i \leftarrow \chi_{[R_q]}$

$\langle p_0 \rangle_i = -p_1 \cdot \langle sk_i \rangle + e_i$

Any: **Output:** $cpk = (p_0, p_1) = (\sum_i \langle p_0 \rangle_i, p_1)$

DBFV.Encrypt(cpk, m):

Any: **Output:** $c_m = \text{BFV.Encrypt}(cpk, m)$.

DBFV.ColDecrypt($c_m, \langle sk \rangle_1, \dots, \langle sk \rangle_i, \dots, \langle sk \rangle_M$):

Each party P_i :

Let $c_m = (c_{m_0}, c_{m_1})$.

$e_i \leftarrow \chi_{R_q}$

$\langle c_{m_{1s}} \rangle_i = \langle sk \rangle_i \cdot c_{m_1} + e_i$

Any: **Output:** $m_{res} = \left\lceil \left\lfloor \frac{t}{q} [c_{m_0} + \sum_i \langle c_{m_{1s}} \rangle_i]_q \right\rfloor \right\rceil_t$

of multiple values in one ciphertext and further customizing the actual operation, accordingly. For the inner product computation, the literature counts two encoding techniques[3]: (i) packed-matrix encoding, where multiple vectors are encoded within a single polynomial, and (ii) packed-integer encoding, where the same value is cloned to all slots.

We opt to use these two techniques and study their performance in the context of biometric identification, namely, for matching a freshly encrypted live template against an encrypted database of K biometric templates. More specifically, a biometric template is denoted as Y_i and is represented by a vector of dimension l (for l features) as follows:

$$Y_i = \begin{bmatrix} Y_i^{(1)} & Y_i^{(2)} & \dots & Y_i^{(l)} \end{bmatrix}$$

We denote the live template as x :

$$x = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(l)} \end{bmatrix}$$

Packed-Matrix Encoding. This encoding scheme consists of packing multiple plaintext vectors in one ciphertext. Multiple template vectors from the database are packed in a single vector until reaching the size of the ciphertext, i.e., N . Thus, each ciphertexts can encapsulate up to N/l templates. For the sake of clarity, we assume that K is a multiple of N/l and we obtain:

$$Y' = \begin{bmatrix} Y_1 & Y_2 & \dots & Y_{N/l} \\ Y_{(N/l)+1} & Y_{(N/l)+2} & \dots & Y_{2N/l} \\ \vdots & \vdots & \ddots & \vdots \\ Y_{K-(N/l)+1} & Y_{K-(N/l)+2} & \dots & Y_K \end{bmatrix} \in \mathbb{Z}_{\frac{K \cdot l}{N}}^{N \times N}$$

On the other hand, the fresh template x is cloned N/l times

$$X = \begin{bmatrix} x & x & \dots & x \end{bmatrix} \in \mathbb{Z}^N$$

Table 1: Computational Complexity of Matrix-Vector Multiplication in Inner Product Computations (Database of size K , l -dimensional vectors, and Ring Polynomials of Degree N)

Encoding Scheme	Packed-Matrix Encoding	Packed-Integer Encoding	Ratio
Ciphertexts	$\lceil (K \cdot l)/N \rceil$	$\lceil (K/N) \rceil \times l$	1
Multiplications	$\lceil ((K \cdot l)/N) \rceil$	$\lceil (K/N) \rceil \times l$	1
Additions	$\lceil (K \cdot l)/N \rceil \cdot \log_2(l)$	$\lceil (K/N) \rceil \times l$	$\log_2(l)$
Rotations	$\lceil (K \cdot l)/N \rceil \cdot \log_2(l)$	0	N.A.
Decryptions	$\lceil (K \cdot l)/N \rceil$	$\lceil (K/N) \rceil$	1

To encode the entire database, a total of $(K \cdot l)/N$ polynomials would be needed and the operations would be performed by encoding each row of the $Y^{(i)}$ at a time. If Kl is not a multiple of N , the last encoded polynomial will be padded with zero values until the degree of the polynomial is reached. To compute the inner product of each template Y_i from the database with the live template x in the encrypted domain, $(K \cdot l)/N$ multiplications followed by cumulative additions ($\log_2(l)$ rotations and additions per ciphertexts of the encrypted database) will be performed (see appendices for more details).

Packed-Integer Encoding. This packing scheme corresponds to a feature-wise encoding of the database. Instead of concatenating each template vector, we consider a matrix Y'' where each row encapsulates the j^{th} feature from every template in the database:

$$Y'' = [Y_1^T \quad Y_2^T \quad \dots \quad Y_K^T] \in \mathbb{Z}^{l \times K}$$

i.e.

$$Y'' = \begin{bmatrix} Y_1^{(1)} & Y_2^{(1)} & \dots & Y_K^{(1)} \\ Y_1^{(2)} & Y_2^{(2)} & \dots & Y_K^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ Y_1^{(l)} & Y_2^{(l)} & \dots & Y_K^{(l)} \end{bmatrix} \in \mathbb{Z}^{l \times K}$$

On the other hand, the live template will be encoded in a matrix X' by cloning each feature $x^{(j)}$ N times :

$$X' = [x^T \quad x^T \quad \dots \quad x^T] \in \mathbb{Z}^{N \times l}$$

i.e.

$$X' = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(l)} \\ x^{(1)} & x^{(2)} & \dots & x^{(l)} \\ \vdots & \vdots & \ddots & \vdots \\ x^{(1)} & x^{(2)} & \dots & x^{(l)} \end{bmatrix} \in \mathbb{Z}^{N \times l}$$

Each feature from N enrolled templates at a time are encoded across all slots of a single polynomial, thus resulting in l polynomials. If $K > N$ this step will be repeated until all the database is encoded. If, on the other hand, the database size K is less than N , each polynomial is padded with zero values. Regarding the live template, each column of the matrix X' is encoded in a single polynomial resulting in l encodings, each holding N repetitions of the same features of x . To compute the inner product of a subset of N templates Y_i from the database with the live template x in the encrypted domain, l multiplications followed by cumulative additions

will be performed (see appendices for more details). This encoding scheme is not suitable to small databases since the complexity of matrix-vector multiplications in the encrypted domain remains constant (and high).

3.4 FSS

Function Secret Sharing (FSS) was introduced by Boyle et al. in [6]. It is defined for a family of efficiently computable and succinctly described functions $f : \{0, 1\}^n \rightarrow \mathbb{G}$, with \mathbb{G} representing a finite Abelian group. In a semi-honest, two-party setting, FSS enables the splitting of a function $f \in \mathcal{F}$ into two additive shares, denoted as (f_0, f_1) ; Each share, f_j , conceals the secret function f , revealing no information about it. For every input x , the output of the secret function $f(x)$ can be reconstructed by separately computing $f_0(x)$ and $f_1(x)$ by each distinct party, resulting in $f_0(x) + f_1(x) = f(x)$. FSS aims to obtain succinct descriptions of f_0 and f_1 using short keys, k_0 and k_1 , called function keys. This approach leads to a fast online phase with only one round of communication. Besides secret sharing a function f , FSS can also be applied with a secret input, concealed from both parties performing the evaluation. This concealment is achieved by adding a random mask r , with $\hat{x} = x + r$. To maintain correctness during evaluation, the mask r is used in generating the function keys k_0 and k_1 .

A central building block of FSS is the Distributed Comparison Function (DCF)[15], defining a family of comparison functions $f_{\alpha, \beta}^<$ which output β if $x > \alpha$ and 0 otherwise. Interval Containment (IC) gates in an FSS scheme enable to determine whether a secret value x falls within an interval $[p, q]$. Initially built upon two DCF blocks, Boyle et al. introduced a method to construct IC using a single DCF block (as shown in Fig. 3 of Section 4.1 [5]). Setting $p = 0$ and $q = 2^{n-1}$ allows FSS to secretly share a unit step function for n -bit signed integers, denoted as $1_{0 \leq x \leq 2^{n-1}}$.

In our work, we use IC gates in FSS in the context of biometric identification for comparing a secret identification score derived from the scalar product of two templates, with a fixed threshold. We therefore define two algorithms: the key generation process (FSS.Gen^{IC}) and the IC gate evaluation in FSS (FSS.Eval^{IC}). For the sake of clarity, we do not elaborate on the generation and evaluation of DCF calls and refer to the original protocols in Fig. 1 of Section 3 in [5]. FSS.Gen^{IC} generates a pair of function keys containing descriptions of the shares f_0, f_1 of a given secret function f . The evaluation algorithm, given a function key and a masked secret input, evaluates the interval containment gate and outputs an additive share $f_j(\hat{x})$ of the output $f(x) = f_0(\hat{x}) + f_1(\hat{x})$.

Algorithm 1 $\text{FSS.Gen}^{IC}(\lambda, n, r) \rightarrow (k_0, k_1)$

Input: λ, n : Security parameters; r input mask
Output: k_0, k_1 : preprocessing keys

1. Define the interval $[p, q]$ for sign extraction:
 $p \leftarrow 0; q \leftarrow 2^{n-1} - 1$
2. Generate DCF for γ , an arbitrary value above the interval limit:
 $\gamma \leftarrow (2^n - 1) + r$
 $(k_{\gamma 0}, k_{\gamma 1}) \leftarrow \text{Gen}_n^<(\lambda, \gamma, 1, \mathbb{U}_{[2^{2n}]})$
3. Generate the correction terms to fix overflows:
 $c \leftarrow -1_{p+r>q} + r + 1_{q+r+1>p} + r + 2^n - 1_{1+p+r>p} + 1_{p+r=2^n-1}$
 $c_0 \leftarrow \mathbb{U}_{[2^{2n}]}; c_1 \leftarrow c - c_0$
4. Compose the function keys:
 $k_0 \leftarrow (k_{\gamma 0}, c_0); k_1 \leftarrow (k_{\gamma 1}, c_1)$

Scheme 3 $\text{FSS.Eval}^{IC}(j, k_j, \hat{x}) \rightarrow o_j$

Input: j : Party number, $j \in \{0, 1\}$; k_j : Function key for P_j ; \hat{x} : Masked public input $(x + r)$.
Output: o_j : Additive secret share of $1_{x \in [0, 2^{n-1}-1]}$.

1. Define the interval $[p, q]$ for sign extraction:
 $p \leftarrow 0; q \leftarrow 2^{n-1} - 1$
2. Parse the function key and obtain local overflow term η :
 $(k_{\gamma j}, c_j) \leftarrow k_j$
 $\eta \leftarrow 1_{\hat{x}>p} - 1_{\hat{x}>q+1}$
3. Evaluate the DCF with two inputs and compute result:
 $o_j^L \leftarrow \text{Eval}_n^<(j, k_{\gamma j}, 1, \hat{x} - 1)$
 $o_j^R \leftarrow \text{Eval}_n^<(j, k_{\gamma j}, 1, \hat{x} - q)$
 $o_j \leftarrow j \cdot \eta - o_j^L + o_j^R + c_j$

4 OUR SOLUTION

4.1 Idea

We consider an airport biometric access control system use case which aims at authorizing access to the plane to passengers if biometric verification succeeds. Three main entities are involved in the process: a Biometric Identity Provider (BIP), a Gatekeeper (Gate), and a group of passengers (users) seeking plane access. The BIP maintains a database of enrolled users' templates and is responsible for performing biometric identification operations against a live template. The Gate is in charge of extracting a live template from a user seeking access, sending it to the BIP, and making decisions regarding authorizing or denying user access. Additionally, we can include one more entity in our scenario to carry out the prior acquisition of users' templates upon enrollment, which we name Enroller. In this context, storing the database in an unencrypted form poses significant privacy risks.

Motivated by this use case of biometric identification in airports introduced in [18], we combine BFV with FSS to enable third parties to perform biometric identification between a freshly encrypted biometric template and a previously encrypted database of biometric templates. The aim is to make this privacy-preserving identification more efficient and robust thanks to the use of dedicated, preliminary encoding operations before the actual encryption operation. We

propose and study the two packing encoding techniques introduced in section E of [3]: the packed-matrix encoding technique packing several templates in a single polynomial and the packed-integer encoding technique encoding one feature element from enrolled templates in a single polynomial. Further, inspired by [18], the ultimate phase of the protocol, involves two parties collaboratively masking and further decrypting the scores in order to securely transit from BFV to FSS to proceed with an efficient comparison operation.

4.2 MONCHI participants

In line with the scenario presented below, we formalize the four main participants in our protocol based on their roles:

- *Enroller*, responsible for enrollment, i.e, acquiring and encrypting the reference biometric templates of users seeking registration during the setup phase. These encrypted reference templates are then forwarded to the BIP for secure storage and subsequent phases.
- *BIP*, holding the encrypted database of reference templates and responsible for evaluating the scores by computing the scalar product between a freshly encrypted live template and each encrypted template of the database with BFV.
- *Gate*, in charge of capturing the live biometric template of the users requesting access, encrypting the live template, and forwarding them to the BIP during the identification phase. Later on *Gate* receives the final decision on this actual identification and allows or not the user to access the plane.
- P_0 & P_1 , two collaborating parties (e.g., two passengers) who help evaluate the last comparison operation of biometric identification in an efficient manner (through FSS).

Additionally, MONCHI involves a trusted key server responsible for generating the keying and other secret material. This server only plays a role during the setup phase and is considered offline during the actual execution of biometric identification.

4.3 Threat Model

In this scenario, we consider all parties to be semi-honest, namely an adversary follows the protocol correctly but aims at extracting maximum information possible about the input templates and the resulting score. The simplicity and linear nature of distance metric functions yield substantial input leakage. An adversary may leverage this leakage to extract information about the inputs by inverting the used distance metric function [27]. Hence the score also needs strong protection. Our approach minimizes the output information to the least amount of information necessary, yielding a one-bit output that indicates a match or no match against the encrypted database. By employing this technique, we achieve an optimally minimal input leakage.

4.4 MONCHI Overview

MONCHI is defined in two phases and six algorithms. The setup phase consists of the generation and distribution of the keying and security material (Algorithm 1) and the appropriate encryption and storage of the database of biometric templates (Algorithm 2). The identification phase starts with Gate extracting the live template, encrypting, and sending it to BIP. Upon receiving the encrypted live

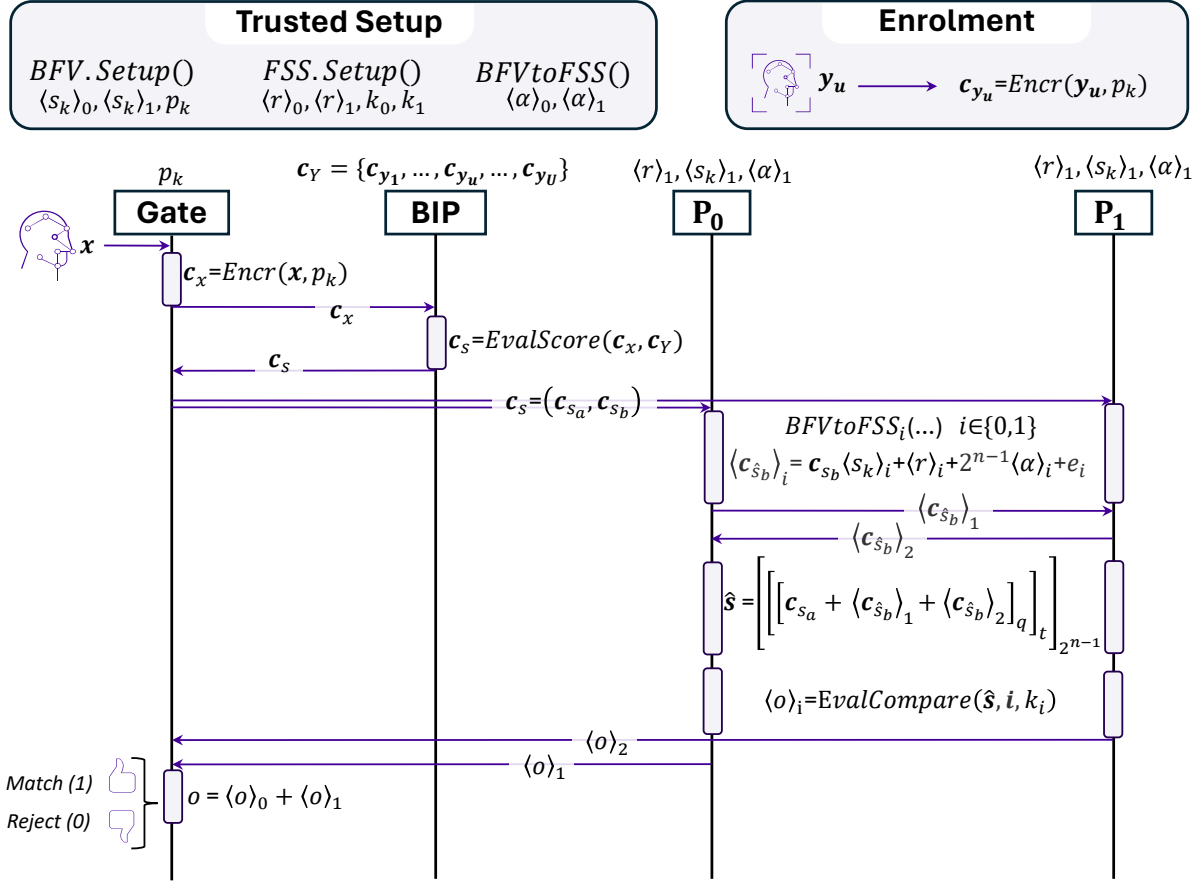


Figure 1: System Diagram of a biometric access control using MONCHI's algorithm.

template, BIP computes the scalar product of this template together with each template of the database (Algorithm 3). The resulting encrypted scores are further sent to P_1 and P_0 who transform these scores through Algorithm 4 in order to apply FSS to perform the secure comparison (Algorithm 5) with the threshold and return the result to Gate. Finally, with Algorithm 6 Gate reconstructs this result.

4.5 MONCHI Algorithms

Algorithm 1: MONCHI.Setup. This algorithm consists of the generation and the distribution of the relevant security and keying materials for BFV, FSS, and the secure transition from BFV to FSS. The key server first generates the encryption key for BFV as well as two shares of the corresponding secret key; For a 1:K biometric identification, K pairs of FSS keys $((k_0, k_1))$ are generated together with K masks r which are secret-shared according to threshold θ . r is used to mask the score before the evaluation of FSS and represent n -bit signed integers uniformly drawn. Finally, to securely transit from BFV to FSS, the key server also generates K random α from $\mathcal{U}[\mathbb{Z}_{2^m}]$ and secret-shares it. α is uniformly drawn from the range -2^{m-1} to 2^{m-1} , where m is defined as the maximum bit size

that ensures both the correctness of the decrypted results and the minimal leakage of private inputs to FSS.

Algorithm 2: MONCHI.Encr. In this algorithm, Enroller first encodes the templates of the database and encrypts this encoded information with BFV using p_k . The encrypted database is then transmitted to BIP. Gate also uses the same algorithm to encode and encrypt the live template.

Algorithm 3: MONCHI.EvalScore. BIP executing this algorithm performs the scalar product between the encrypted live template and each ciphertext in the encrypted database. If the templates are encoded using packed-matrix encoding, the encrypted live template consists of a single ciphertext, encrypting N/l instances of the live template and the encrypted database matrix contains $(K \times l)/N$ ciphertexts. The evaluation involves SIMD multiplications followed by cumulative additions, $(\log_2(l))$ rotations and additions per ciphertext in the encrypted database matrix C_Y . Consequently, the resulting matrix of encrypted scores includes $(K \times l)/N$ ciphertexts, each storing N/l encrypted scores. Conversely, if the templates are packed with packed-integer encoding, the matrix encapsulating the encryption of the live template will be composed of l ciphertexts. Each of these ciphertexts contains N slots, with each slot holding

Protocol 1 MONCHI.Setup($K, pp_{(BFV)}, pp_{(FSS)}, m$)**Players:** Key server**Input:** K : Number of enrolled users; $pp_{(BFV)}(t, q, N, \sigma, B)$: BFV public parameters; $pp_{(FSS)}(\lambda, n, \theta)$: FSS parameters; m Security parameter for BFV to FSS.**Output:** $\langle sk \rangle_0, \langle sk \rangle_1$: DBFV Secret key shares and public key $\langle r \rangle_0, \langle r \rangle_1, k_0, k_1$: Random mask shares and FSS function keys $\langle \alpha \rangle_0, \langle \alpha \rangle_1$: Additional random shares to prevent from leakage when switching from BFV to FSS.

1. Run BFV Setup:

 $\text{BFV.SecKeyGen}() \rightarrow \langle sk \rangle_1, \langle sk \rangle_0$ $\text{BFV.PubKeyGen}(\langle sk \rangle_1 + \langle sk \rangle_0) \rightarrow pk$

2. Run FSS gate setup. For each template in the database, do:

 $r \leftarrow \mathbb{U}_{[\mathbb{Z}_{2^n}^{(n)}]}$ $\text{FSS.Gen}^{IC}(\lambda, n, r) \rightarrow k_0, k_1$ $\langle r \rangle_0, \langle r \rangle_1 \leftarrow r$ and $\langle r \rangle_1 \leftarrow \langle r \rangle_1 - \theta$

3. Run BFVtoFSS setup. For each template in the database, do:

 $\alpha \leftarrow \mathbb{U}_{[\mathbb{Z}_{2^m}^K]}$ $(\langle \alpha \rangle_0, \langle \alpha \rangle_1) \leftarrow \alpha$ **Protocol 2** MONCHI.Encr(pk, V)**Players:** Enroller or Gate**Input:** pk : BFV public key; V : Input vector(s) (either the database of K templates or the freshly extracted live template)**Output:** C_V : Matrix of encrypted template(s). $P_V = \text{BFV.PackEncode}(V)$ $C_V = \text{BFV.Encrypt}(pk, P_V)$

the encryption of the same feature of the live template, having N encryptions of each feature in each ciphertext. The encrypted database matrix will be composed of $(K \times l)/N$ ciphertexts, each containing N features from N templates. Computing the scalar product requires only l multiplications followed by additions for each ciphertext in the encrypted database C_Y . Rotations are no longer required as the coefficients of the ciphertexts are already aligned. As a result, the resulting matrix of encrypted scores contains K/N ciphertexts, with each ciphertext holding N encrypted scores.

Protocol 3 MONCHI.EvalScore(C_Y, C_X)**Players:** BIP**Input:** C_Y : Encrypted Database matrix; C_X Encrypted live template.**Output:** C_S : Encrypted scores matrix. $C_S = \text{BFV.MatMul}(C_Y, C_X)$

Algorithm 4: MONCHI.BFVtoFSS. P_0 and P_1 who have received the encrypted shares of scores first masks them before their decryption. This step is needed for the subsequent comparison step which is executed using FSS. The masking of each score with r is performed via addition. To keep consistency with the FSS-based works [5], the local shares additions needs to be performed modulo 2^{n-1} . Due

to the high computational cost of performing this modulus operation in the encrypted domain, we decide to perform the modulus reduction post-decryption. However, this approach introduces a security vulnerability by potentially exposing information about the results. To mitigate this risk while still performing modulus reduction after decryption, an additional mask α is introduced and secret-shared among the two parties. These shares are multiplied with 2^n to shift them with n bits to the left before being added concurrently with the local shares used for masking during the intermediate decryption. This approach enables the removal of the additional share α via a modulus operation in \mathbb{Z}_2^n post-decryption, while decreasing the probability of leakage associated with modulus reduction performed in cleartext (see Section ?? for more details).

Protocol 4 MONCHI.BFVtoFSS($c_s, \langle sk \rangle_j, \langle r \rangle_j, \langle \alpha \rangle_j$)**Players:** $P_j, j \in \{0, 1\}$ computing parties**Input:** $\langle sk \rangle_j$: Secret key share for BFV $\langle r \rangle_j$: Vector of secret mask shares for FSS $\langle \alpha \rangle_j$: Vector of secret mask shares for BFV to FSS c_s : Matrix of ciphertext of the encrypted scores.**Output:** Masked and randomized decrypted scores \hat{s} .For each ciphertext c_s of the matrix C_S :Let $c_s = (c_{sa}, c_{sb})$ $\langle r \rangle_j \leftarrow \text{BFV.PackEncode}(\langle r \rangle_j)$ $\langle \alpha \rangle_j \leftarrow \text{BFV.PackEncode}(\langle \alpha \rangle_j)$ $e_i \leftarrow \chi R_q$ $\langle c_{sb} \rangle_i = \langle sk \rangle_j c_{sb} + \langle r \rangle_j + \langle \alpha \rangle_j * 2^n + e_i$ $\hat{s} = \left[\left[\frac{t}{q} [(c_{sa} + \langle c_{sb} \rangle_0 + \langle c_{sb} \rangle_1)]_q \right]_t \right]_{2^{n-1}}$

Algorithm 5: MONCHI.EvalCompare. Once the scores are collaboratively decrypted and transformed to become inputs to FSS, the two parties evaluate the interval containment gate to determine whether the scores are below or above the fixed threshold θ .

Protocol 5 MONCHI.EvalCompare(\hat{s}, j, k_j)**Players:** $P_j, j \in \{0, 1\}$ computing parties**Input:** \hat{s} : masked scores; k_j : FSS key.**Output:** o_j : Arithmetic shares.For each masked score \hat{s}_i of \hat{s} : $\langle o \rangle_i \leftarrow \text{FSS.Eval}^{IC}(j, k_{vec}[i], \hat{s}_i)$ $o_j \leftarrow o_j.append(\langle o \rangle_i)$

Algorithm 6: MONCHI.Result. Gate reconstructs the results of the identification from the arithmetic shares, which are derived from the evaluation of the interval containment gate in the FSS scheme, using the decrypted randomized and masked scores.

5 SECURITY ANALYSIS

5.1 Overview

We begin by succinctly analyzing the security of MONCHI.

Protocol 6 MONCHI.Result($\mathbf{o}_0, \mathbf{o}_1$)**Players:** Gate**Input:** ($\mathbf{o}_0, \mathbf{o}_1$): arithmetic shares of the results**Output:** \mathbf{o} : Results of the comparison $f_{\theta,1}^<(\hat{s})$ $\mathbf{o} = \mathbf{o}_0 + \mathbf{o}_1$

Firstly, the security of MONCHI directly derives from the security of BFV and FSS. Nevertheless, since BFV and FSS are not executed in the same rings, during *BFVtoFSS* algorithm, the extra term α_i is added. In *BFVtoFSS*, similar to Funshade, the score is first masked with r before its decryption. At some point during decryption, both P_0 and P_1 obtain $s + r$ without any modular reduction, and, hence, some leakage may appear. Such leakage is mitigated by the introduction of the new α . Considering that s (resp. α) is drawn uniformly at random with n (resp. m) bits, given the sum $s + r + 2^n\alpha$, all values of s can be expected – and an attacker cannot get any information on the score – with a probability of $1 - \frac{2^n - 1}{2^{(n+m)}}$. This term α cancels out during the modular reduction $\bmod 2^n$ which precedes the beginning of the MONCHI.Eval algorithm.

A more detailed formal analysis can be found below.

5.2 Security Proof

We consider security against a Honest-but-Curious adversary \mathcal{A} that corrupts up to one of the parties $\{\text{Enrollment}, \text{BIP}, \text{Gate}, P_0, P_1\}$. We consider a static corruption model where the adversary must choose which participant to corrupt before the execution of the computations. This is a standard security model in previous MPC frameworks [5, 9, 10, 24, 28]. Under this threat model, we define and later prove the privacy and correctness of our constructions. Later, we extend our security to certain combinations of corruptions.

We employ the standard real world - ideal world paradigm, providing a simulator for each party corrupted by the ideal adversary \mathcal{A}' such that the adversary cannot distinguish the simulator-led interactions of \mathcal{A}' from the real-world view of \mathcal{A} with the party/ies he corrupted. The ideal world simulation contains an additional trusted party that receives all the inputs from all parties, computes the ideal functionality correctly and sends the corresponding results back to the corresponding parties. Conversely, the MONCHI protocol is executed in real world in the presence of \mathcal{A} .

Our security proof works in the $(\mathcal{F}_{\text{MONCHI.setup}})$ -hybrid model, that is, grounded on the faithful execution of MONCHI.setup by a trusted party that generates and distributes each piece of setup material to its designated recipient.

Ideal Functionality $\mathcal{F}_{\text{Identif}}$

$\mathcal{F}_{\text{Identif}}$ interacts with *Enrollment*, *BIP*, *Gate*, P_0 , P_1 and the simulator \mathcal{S} , and is parameterized by the inputs to MONCHI.setup and the template length l .

- **Inputs:** $\mathcal{F}_{\text{Identif}}$ receives \mathbf{x} from *Gate* and, \mathbf{Y} from *Enrollment*.
- **Computation:** $\mathcal{F}_{\text{Identif}}$ sets $\mathbf{s} = \{\mathbf{Y}_i \mathbf{x}^T\}_{i \in \{1 \dots K\}}$ and obtains $\mathbf{o} = \{s_i \geq \theta\}_{i \in \{1 \dots K\}}$
- **Output:** Sends \mathbf{o} to *Gate*.

THEOREM 5.1 (SECURITY OF MONCHI). *For each party in $\{\text{BIP}, \text{Enrollment}, \text{Gate}, P_0, P_1\}$, there exists a PPT algorithm \mathcal{S} (simulator) such that $\forall \theta \in \mathbb{Z}_{n+}^*$, $\forall \mathbf{x} \in \mathbb{Z}_n^l$, $\forall \mathbf{Y} \in \mathbb{Z}_n^{l \times K}$, \mathcal{S} realizes the ideal functionality $\mathcal{F}_{\text{Identif}}$, such that its behavior is computationally or statistically indistinguishable from a real world execution of the MONCHI protocol (consisting of the sequential execution of algorithms 4, 5, 6 by the designated players) in the presence of a static semi-honest adversary \mathcal{A} corrupting said party.*

PROOF. We define a simulator \mathcal{S} for each possible corruption during the execution of each sequential step in MONCHI protocol:

- For corrupt *Enrollment*: Since it does not receive any messages from any other party, it suffices for \mathcal{S} to run $C_Y = \{\text{MONCHI.Encr}(pk, Y_i)\}_{i \in \{1 \dots K\}}$ under BFV using pk with the chosen packing technique and give it to \mathcal{A}' , then yield \mathbf{Y} to $\mathcal{F}_{\text{Identif}}$. The adversary cannot distinguish anything, as the valid C_Y is enough to perfectly simulate his view of the protocol.
- For corrupt *BIP*: \mathcal{S} artificially sets $\mathbf{Y}' = \mathbf{0}_{\mathbb{Z}_n^{l \times K}}$ and $\mathbf{x}' = \mathbf{0}_{\mathbb{Z}_n^l}$, encrypts them into $C_{Y'}$ & $C_{x'}$ under BFV using pk with the chosen packing technique and gives both to \mathcal{A}' . It also gives $C_{s'} = \{\text{MONCHI.EvalScore}(C_{Y'}, C_{x'})\}$ to \mathcal{A}' . For all these ciphertexts, any non-negligible advantage to distinguish $C_{s'}$ from C_s , $C_{x'}$ from C_x or $C_{Y'}$ from C_Y would immediately provide a non-negligible advantage to solve the decisional RLWE problem of BFV [13].
- For corrupt *Gate*: \mathcal{S} runs $\text{MONCHI.Encr}(pk, \mathbf{x})$ and gives it to \mathcal{A}' , then it artificially sets $\mathbf{s}' = \mathbf{0}_{\mathbb{Z}_n^K}$, encrypts it under BFV using pk with the chosen packing technique and give it to \mathcal{A}' . Again, any non-negligible advantage to distinguish $C_{s'}$ from C_s would immediately provide a non-negligible advantage to solve the decisional RLWE problem of BFV [13].
- For corrupt P_j with $j \in \{0, 1\}$: \mathcal{S} artificially samples \mathbf{s}' from $\mathcal{U}[\mathbb{Z}_{2^n}^K]$, encrypts it into $C_{s'}$ under BFV using pk and gives it to \mathcal{A}' . \mathcal{S} runs MONCHI.BFVtoFSS to generate share j of \hat{s}' and gives this share to \mathcal{A}' . Then, \mathcal{S} computes the other share $1 - j$ so that their reconstruction yields \hat{s}' and yields it to \mathcal{A}' . Finally, \mathcal{S} runs $\text{MONCHI.EvalCompare}(\hat{s}')$ and gives the output share \mathbf{o}_j to \mathcal{A}' .

Crucially, in the absence of the masking term α , the real-world adversary would receive $\hat{s} = s + r$ without any modular reduction, thus he would have a meaningful advantage at distinguishing between the distributions of \hat{s} and \hat{s}' and thus breaking the simulation. By adding α drawn uniformly at random with m bits, the distributions $s + r + 2^n\alpha$ and $s' + r + 2^n\alpha$ can be distinguished with probability $1 - \frac{2^n - 1}{2^{(n+m)}}$, that is, the probability of obtaining a sampling a value of α that falls under the interval of $[1, 2^n - 1]$. This term α cancels out during the 2^n modular reduction, hence having no impact on the FSS gate evaluation.

For the FSS IC gate, we resort to the simulation-based security of [5, Definition 2] to argue computational indistinguishability of the keys from random strings, hiding the information of r contained in \mathbf{k}_0 and \mathbf{k}_1 from \mathcal{A}/\mathcal{A}' , and thus allowing the addition of this n -bit uniformly random

mask r to perfectly hide the input value s in the signed n -bits interval.

□

THEOREM 5.2 (CORRECTNESS OF MONCHI). *For every threshold $\theta \in \mathbb{Z}_{n+}^*$, every pair of input vectors $\mathbf{x} \in \mathbb{Z}_n^l$, $\mathbf{Y} \in \mathbb{Z}_n^{l \times K}$, and for suitable choices of BFV & FSS parameters, the execution of the MONCHI protocol fulfills:*

$$\Pr[\text{MONCHI}(\mathbf{x}, \mathbf{Y}, \dots) \neq \mathcal{F}_{\text{identif}}(\mathbf{x}, \mathbf{Y})] \leq 1/\text{negl}(pp(\text{BFV}))$$

where $\text{negl}(pp(\text{BFV}))$ is a negligible function for sufficiently large BFV parameters in MONCHI.Setup.

PROOF. To argue the correctness of the BFV-based matrix multiplication we resort to [13, Theorem 1], stating that for an appropriately chosen BFV parameters B , t and q , the BFV scheme supports the evaluation of a circuit of depth L_{BFV} , where $L_{\text{BFV}} = 1$ in our case for the one single multiplication present in the scalar product.

Adding the mask α has no impact on correctness, as this mask is cancelled out when performing reduction modulo 2^n .

Lastly, we focus on the correctness of the FSS gate. Based on [5, Theorem 3], $(\text{FSS.Gen}^{IC}(\lambda, n, r)$ and $\text{FSS.Eval}^{IC}(j, \mathbf{k}_j^{IC}, \hat{z}_\theta)$) constitute an FSS gate realizing $f(s, \theta) = (s \geq \theta)$. Then, following the Correctness definition in [5, Definition 2], we argue that $\Pr[\text{FSS.Eval}^{IC}(0, \mathbf{k}_0^{IC}, \hat{s}_\theta) + \text{FSS.Eval}^{IC}(1, \mathbf{k}_1^{IC}, \hat{s}_\theta) = (s \geq \theta)] = 1$.

□

Beyond this security definition, and due to the lack of direct interactivity between BIP and $\{P_0, P_1\}$, MONCHI also maintains its privacy guarantees if \mathcal{A} corrupts both BIP and one of $\{P_0, P_1\}$. This can be proven straightforwardly combining the simulator for corrupted BIP with that of one corrupted party out of $\{P_0, P_1\}$. A similar argument can be made for the case where \mathcal{A} corrupts both $Enrollment$ and one of $\{P_0, P_1\}$. Finally, $Enrollment$ and BIP may be collapsed into a single party while preserving the privacy of the fresh template and the biometric operations, yet relinquishing the privacy of the reference template database, which is why we presented them as separate entities.

6 PERFORMANCE EVALUATION

In this section, we describe the results of our experimental evaluation of MONCHI.

6.1 Environment setting

We implemented MONCHI with the two packing methods in Golang with efficient C++ blocks and using several cryptography libraries including: Lattigo [26] for MONCHI.Encrypt and MONCHI.BFVtoFSS partially, and Funshade's FSS algorithm for MONCHI.EvalCompare. MONCHI was implemented and executed on an Intel Core i7-7700 CPU, 3600 MHz with 4 physical cores available; To fully leverage the CPU capabilities, multi-threading was used, running the 4 cores in parallel.

Regarding security parameters, the BFV parameters were set as follows: the polynomials degree is set to $N = 8192$, and, the size of the ciphertext modulus to 162. Based on this choice of security parameters, we chose the maximum available plaintext modulus,

and set t to ~ 32 . For FSS we work with $n = 16$ -bit modular arithmetics. Finally, in order to avoid errors while adding α be random m signed bits integers where $m = t - n = 16$. The reason behind the choice of a large plaintext modulus for the BFV scheme is primarily driven by the need to achieve the best performance results while keeping a high security degree and avoid errors during decryption.

To study and evaluate the performance of MONCHI according to the airport use case, we have used the Labeled Faces in the Wild (LFW) dataset [17], the publicly available dataset for face verification. The dataset includes 13,233 facial images of 5,749 individuals. To process these images and extract templates, we used 4 pre-trained neural network models – Swin Transformer [21] – and, obtain templates size of 64, 128, 256, 512 floats. We employ the False Acceptance Rate (FAR) and False Rejection Rate (FRR) as key metrics, as defined in [20], to assess the impact of quantization on our facial recognition model's accuracy.

6.2 Quantization and Accuracy

In this section, we study the level of quantization for minimizing the accuracy impact.

Because BFV deals with integer inputs, the extracted features are further quantized. Given that templates are normalized to unit length and scores are floats ranging between -1 and 1, the quantization factor defines the range of possible scores. Consequently, a larger quantization value expands the score range. Hence, the quantization factor has a direct impact on the accuracy of biometric identification and the security of MONCHI. Given that n is the security parameter for FSS $n = 16$, the scores' range should not exceed $[-2^{n-1}, 2^{n-1} - 1]$. For each template size, the quantization factor has been found to guarantee a degradation lower than 10% rate of FRR at a FAR of 10^{-6} . For the sake of simplicity, we here choose to only keep one quantization factor of a value of 180.

Table 3 presents the False Reject Rate of the original templates, FRR_{org} and the the False Reject Rate of the quantized ones FRR_{qnt} for a fixed $FAR = 10^{-6}$.

As displayed in Table 3, the quantization factor (qf) of 180 results has a small impact on the FRR for templates of size 512.

6.3 Performance evaluation

As previously mentioned, to evaluate the performance of MONCHI and study the effectiveness of the two encoding schemes, we conducted experiments with different database sizes and across various template dimensions.

Table 2 depicts the computational cost of MONCHI's identification phase (i.e. online phase), detailing both the execution time and the total memory required for each of these algorithms. It compares the two encoding schemes for an encrypted database size of 1024, considering templates of various dimensions (64, 128, 256 and 512). The packed-matrix encoding yields a quicker process for the encryption of freshly extracted templates (MONCHI.Encr), around 30 milliseconds (ms) for 512-dimensional templates compared to 0.34 seconds (s) with packed-integer encoding. The computation of the encrypted scores (MONCHI.Evalscore) is also faster, taking around 0.67 s versus 0.90 s with packed-integer encoding. On the other hand, the transformation of scores during the transition from BFV to FHE, involving collective decryption associated

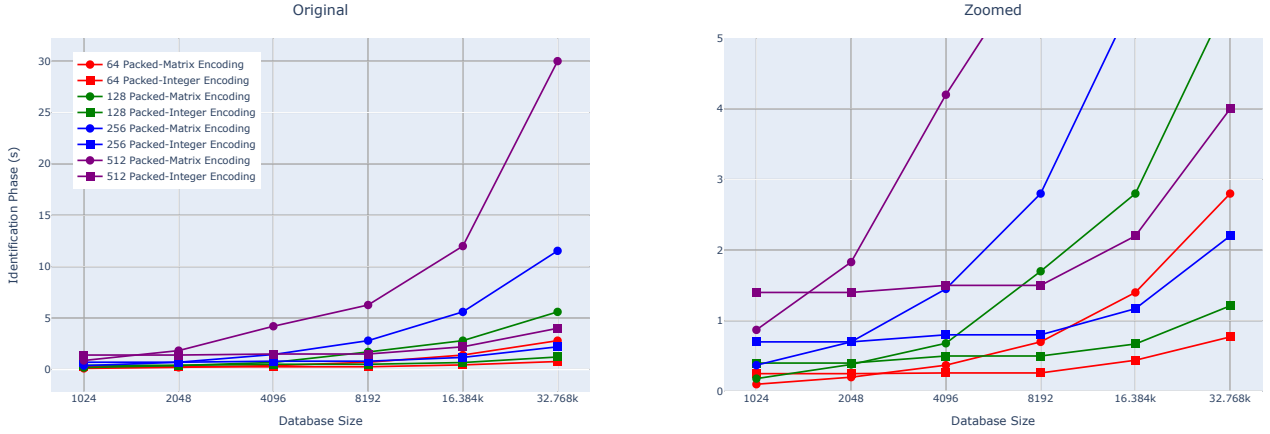


Figure 2: Execution time of 1:K identification with MONCHI for l -dimensional templates using a ring with $N = 8192$

Table 2: Computation overhead of MONCHI (online phase, $N = 8192$, $qf = 180$) running the 4 cores in parallel.

DB Size (K)	Dim (l)	Packed-Matrix Encoding						Packed-Integer Encoding					
		Time (s)				Total	Total	Time(s)				Total	Total
		Enc	EvalScore	BFVtoFSS	EvalCompare	Time (s)		Enc	EvalScore	BFVtoFSS	EvalCompare	Time (s)	
1024	64	0.003	0.09	0.024	0.015	0.132	8	0.06	0.14	0.006	0.015	0.221	52
	128	0.003	0.15	0.055	0.015	0.223	14	0.09	0.27	0.006	0.015	0.381	101
	256	0.003	0.28	0.123	0.015	0.421	26	0.24	0.45	0.006	0.015	0.711	202
	512	0.003	0.67	0.226	0.015	0.914	52	0.34	0.90	0.006	0.015	1.261	403

Table 3: Impact of Template Quantization on Facial Recognition Accuracy at $FAR = 10^{-6}$

(l)	FRR_{org}	FRR_{qnt}
64	0.0187	0.0189
128	0.0089	0.0086
256	0.0025	0.0025
512	0.0031	0.0031

with masking and randomization, is faster when packed-integer encoding is used. MONCHI.BFVtoFSS takes 0.006 s with packed-integer encoding (vs. 0.226s with packed-matrix encoding) thanks to the reduced number of ciphertexts holding the encrypted scores. The processing complexity of evaluating the Interval Containment gate (MONCHI.EvalCompare) remains constant, regardless of the encoding scheme used. This is because there are no encoded inputs anymore. Overall, the identification phase is faster with packed-matrix encoding, requiring 0.914 s with packed-integer encoding for 512-dimensional templates instead of 1.261 s in the case of packet-matrix encoding and the overall memory required is also more efficient with packed-matrix encoding (403 MB vs. 52 MB for 512-dimensional templates).

Figure 2 demonstrates the computational complexity of the online phase for the two encoding schemes, covering a broader range

of database sizes (1024, 2048, 4096, 8192, 16384 and 32768). We observe that, for small database size (typically less than 2048), packed-matrix encoding outperforms packed-integer encoding. However, as the database size exceeds 2048, there is a notable shift in efficiency. Additionally, the computational cost of the online computation remains constant with packed-integer encoding provided that the database size does not exceed $N = 8192$. The reduced efficiency of packed-integer encoding for small databases can be attributed to two factors: the requirement to encode each feature of the live template into a single polynomial, resulting in l ciphertexts encrypting one live template compared to one ciphertext with packed-integer encoding, and the need for padding of each polynomial with $N - K$ zero coefficients, considering that the ring polynomial degree in use is N , K is the database size, and templates are of l -dimension. Furthermore, the better efficiency of packed-integer encoding for larger databases (where $K \geq N$) can be explained with the varying computational demands of the two encoding methods. In packed-matrix encoding, the operations carried out in the encrypted space, involving $\log_2(l)$ cumulative rotations and additions per ciphertext of the encrypted database, become increasingly computationally intensive. Conversely, with packed-integer encoding, the required operations consist of l cumulative additions for each batch of N templates from the database, which is comparatively less demanding on computational resources.

Table 4: Computation and Communication overhead of MONCHI's actors (online phase, $N = 8192$, $qf = 180$)

DB Size (K)	Dim (I)	Packed-Matrix Encoding						Packed-Integer Encoding					
		Time (s)			Bandwidth (MB)			Time(s)			Bandwidth (MB)		
		BIP	Gate	P_j	BIP \longleftrightarrow Gate	Gate $\longleftrightarrow P_j$	$P_{1-j} \longleftrightarrow P_j$	BIP	Gate	P_j	BIP \longleftrightarrow Gate	Gate $\longleftrightarrow P_j$	$P_{1-j} \longleftrightarrow P_j$
1024	64	0.09	0.003	0.039	3.6	3.2	4e-4	0.14	0.06	0.021	26	0.41	5e-5
	128	0.15	0.003	0.070	6.7	6.3	8e-4	0.27	0.09	0.021	51	0.41	5e-5
	256	0.28	0.003	0.14	13	12	1.6e-3	0.45	0.24	0.021	101	0.41	5e-5
	512	0.67	0.003	0.24	26	25	3.2e-3	0.90	0.34	0.021	201	0.41	5e-5

In Table 4, we have also studied the computational costs and the communication bandwidth of the different actors involved in the identification phase. The BIP and the Gate exchanging the encrypted live template (Gate \rightarrow BIP) and the encrypted scores (BIP \rightarrow Gate) results in a communication cost of 26 MB with packed-matrix encoding compared to 201 MB with packed-integer encoding for 512-dimensional templates. Conversely, when considering the communication cost between the Gate and each party involving the exchange of the encrypted scores (Gate $\rightarrow P_j$) and the arithmetic shares of the interval containment gate of FSS ($P_j \rightarrow$ Gate), it is higher with packed-matrix encoding (25 MB vs. 0.41 MB with 512-dimensional templates).

7 CONCLUSION

MONCHI is a novel protocol for privacy-preserving biometric identification. We build our protocol upon BFV, and FSS, for full correctness for decryption and comparison with a fixed threshold, requiring only a single round of communication among the two parties in the identification phase. To ensure leakage resilience, we introduce local shares (α) to securely transition from BFV to FSS. We propose and analyze two packing encoding techniques, packed-matrix encoding and packed-integer encoding. We observe that the primary advantage of packed-integer encoding is its elimination of costly rotational operations during inner product evaluation in the encrypted domain. Conversely, packed-matrix encoding is more suited for operations involving small databases. We analyze practical security aspects of the biometric identification, and implement these protocols on top of the Lattigo library with efficient C++ blocks.

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A PACKED-MATRIX ENCODING

In the context of Section 3.2, this section details the computation of the inner product between a database of K biometric templates and a live template, each of dimension l . We introduce matrices Y' and x , representing the database and the live template, respectively, using packed-matrix encoding. For the sake of clarity, we assume that $K = N/l$, we obtain:

$$Y' = [Y_1 \quad Y_2 \quad \cdots \quad Y_{N/l}] \in \mathbb{Z}^{1 \times N},$$

$$X = [x \quad x \quad \cdots \quad x] \in \mathbb{Z}^N.$$

Encrypting Y' and X yields:

$C_{Y'}$ =

$$\begin{bmatrix} c_{Y_1^{(1)}} & c_{Y_1^{(2)}} & \cdots & c_{Y_1^{(l)}} & \cdots & c_{Y_{N/l}^{(1)}} & \cdots & c_{Y_{N/l}^{(l)}} \end{bmatrix} \in \mathbb{R}_q,$$

$$C_X = [c_{x^{(1)}} \quad c_{x^{(2)}} \quad \cdots \quad c_{x^{(l)}} \quad \cdots \quad c_{x^{(1)}} \quad \cdots \quad c_{x^{(l)}}].$$

First coefficient-wise multiplication (denoted as C_{Mul1}):

$$C_{Mul1} = \begin{bmatrix} c_{x^{(1)}} \cdot c_{Y_1^{(1)}} & \cdots & c_{x^{(1)}} \cdot c_{Y_{N/l}^{(1)}} & \cdots & c_{x^{(l)}} \cdot c_{Y_{N/l}^{(l)}} \end{bmatrix},$$

Left rotation of C_{Mul1} by 1 (denoted as C_{Rot1}):

$$C_{Rot1} = \begin{bmatrix} c_{x^{(2)}} \cdot c_{Y_1^{(2)}} & \cdots & c_{x^{(2)}} \cdot c_{Y_{N/l}^{(2)}} & \cdots & c_{x^{(1)}} \cdot c_{Y_1^{(1)}} \end{bmatrix}.$$

Coefficient-wise addition of C_{Mul1} and C_{Rot1} (denoted as C_{Sum1}):

$$C_{Sum1} =$$

$$\begin{bmatrix} c_{x^{(1)}} \cdot c_{Y_1^{(1)}} + c_{x^{(2)}} \cdot c_{Y_1^{(2)}} & \cdots & c_{x^{(1)}} \cdot c_{Y_{N/l}^{(1)}} + c_{x^{(2)}} \cdot c_{Y_{N/l}^{(2)}} & \cdots \end{bmatrix}.$$

Subsequent left rotation by 3 (denoted as C_{Rot2}):

$C_{Rot2} =$

$$\begin{bmatrix} c_{x^{(3)}} \cdot c_{Y_1^{(3)}} + c_{x^{(4)}} \cdot c_{Y_1^{(4)}} & \cdots & c_{x^{(3)}} \cdot c_{Y_{N/l}^{(3)}} + c_{x^{(4)}} \cdot c_{Y_{N/l}^{(4)}} & \cdots \end{bmatrix}.$$

We recursively repeat the steps of coefficient-wise rotation, and addition $\log_2(l)$ times, culminating in the computation of C_z :

$$C_z = \begin{bmatrix} \sum_{i=1}^l c_{x^{(i)}} \cdot c_{Y_1^{(i)}} & \cdots & \sum_{i=1}^l c_{x^{(i)}} \cdot c_{Y_{N/l}^{(i)}} & \cdots \end{bmatrix}.$$

The coefficients at indices $\{0, N/l, \dots, K - N/l\}$ in C_z contain the encrypted scores for the N/l templates, while other coefficients are disregarded post-decryption.

B PACKED-INTEGER ENCODING

This section introduces a packed-integer encoding scheme for feature-wise representation of a biometric database. Assuming $K = N$ for clarity, we define a matrix Y'' where each row captures the j^{th} feature from every template in the database. The matrix X' comprises l rows, each row containing N replications of each feature of the live template.

$$Y'' = \begin{bmatrix} Y_1^{(1)} & Y_2^{(1)} & \cdots & Y_N^{(1)} \\ Y_1^{(2)} & Y_2^{(2)} & \cdots & Y_N^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ Y_1^{(l)} & Y_2^{(l)} & \cdots & Y_N^{(l)} \end{bmatrix} \in \mathbb{Z}^{l \times N},$$

$$X' = \begin{bmatrix} x^{(1)} & x^{(2)} & \cdots & x^{(l)} \\ x^{(1)} & x^{(2)} & \cdots & x^{(l)} \\ \vdots & \vdots & \ddots & \vdots \\ x^{(1)} & x^{(2)} & \cdots & x^{(l)} \end{bmatrix} \in \mathbb{Z}^{N \times l}.$$

Each row of Y'' and each column of X' are encoded into single polynomials, resulting after the encryption in l ciphertexts for the entire database and l ciphertexts for the live template:

For $i \in \{1, \dots, l\}$, we have:

$$C_{Y^i} = [c_{Y_1^{(i)}} \quad c_{Y_2^{(i)}} \quad \cdots \quad c_{Y_N^{(i)}}],$$

$$C_{X^i} = [c_{x^{(i)}} \quad c_{x^{(i)}} \quad \cdots \quad c_{x^{(i)}}].$$

The computation of the inner product involves l multiplications and cumulative additions.

For each $i \in \{1, \dots, l\}$:

$$C_{mul^{(i)}} = BFV.Mul(C_{Y^i}, C_{X^i}),$$

$$C_z = BFV.Add(C_{mul}^i, C_z).$$

The coefficients in C_z represent encrypted scores, yielding a single ciphertext that encapsulates N encrypted scores.

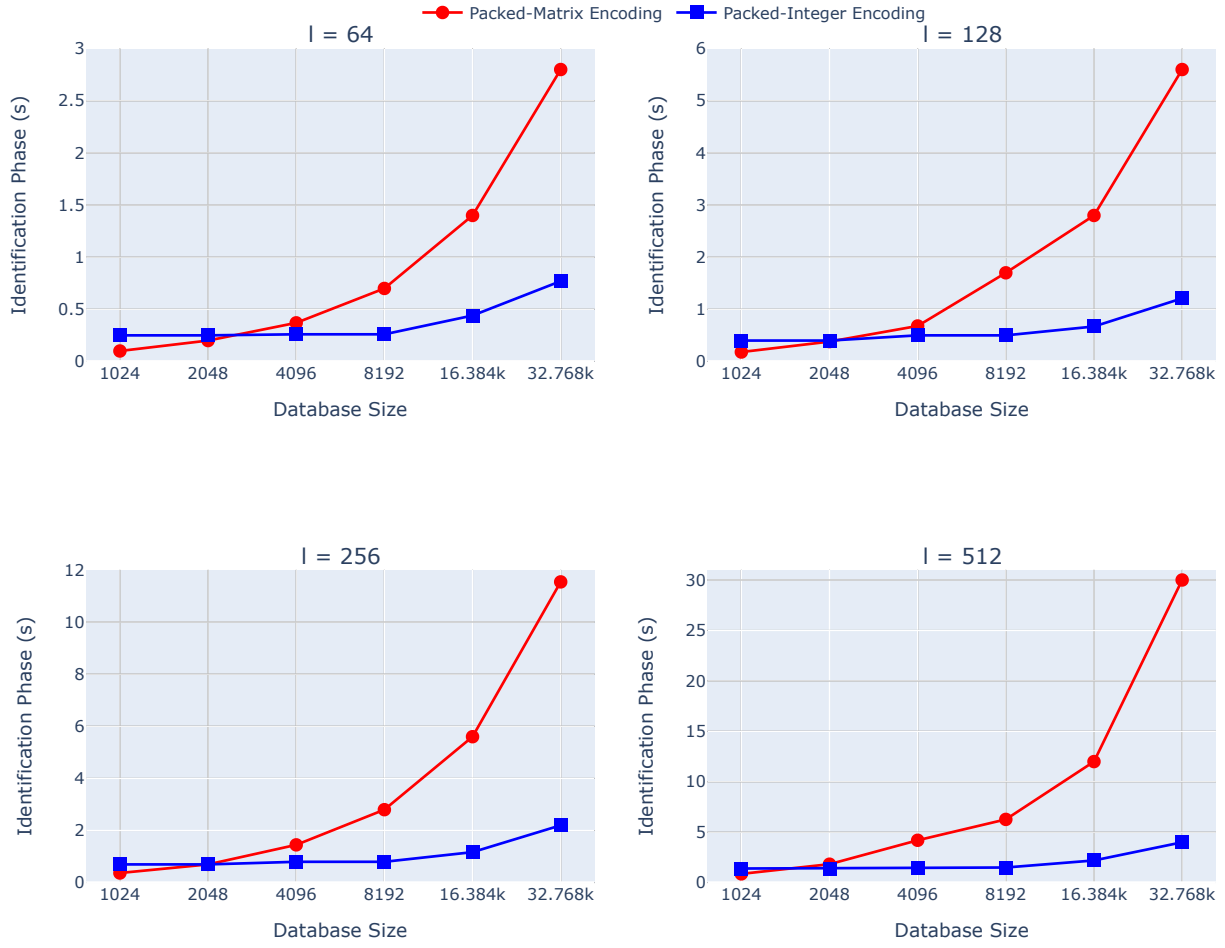


Figure 3: Execution time of 1:K identification with MONCHI for l -dimensional templates using a ring with $N = 8192$