# HMM

### December 8, 2021

```
[1]: import math
     import random
     import numpy
     from collections import *
[2]: class HMM:
         Simple class to represent a Hidden Markov Model.
         def __init__(self, order, initial_distribution, emission_matrix,__
      →transition_matrix):
             self.order = order
             self.initial_distribution = initial_distribution
             self.emission_matrix = emission_matrix
             self.transition_matrix = transition_matrix
[3]: def read_pos_file(filename):
         Parses an input tagged text file.
         Input:
         filename --- the file to parse
         Returns:
         The file represented as a list of tuples, where each tuple
         is of the form (word, POS-tag).
         A list of unique words found in the file.
         A list of unique POS tags found in the file.
         file_representation = []
         unique words = set()
         unique_tags = set()
         f = open(str(filename), "r")
         for line in f:
             if len(line) < 2 or len(line.split("/")) != 2:</pre>
                 continue
             word = line.split("/")[0].replace(" ", "").replace("\t", "").strip()
             tag = line.split("/")[1].replace(" ", "").replace("\t", "").strip()
```

```
file_representation.append( (word, tag) )
            unique_words.add(word)
            unique_tags.add(tag)
        f.close()
        return file_representation, unique_words, unique_tags
[4]: def read_pos_file_modified(training_data_file):
        A modified verysion of read pos that only returns the file representation
        Input: training data file, a text file
        Output: The file represented as a list of tuples, where each tuple
         is of the form (word, POS-tag).
        file_representation = []
        #open file
        f = open(str(training_data_file), "r")
        for line in f:
            if len(line) < 2 or len(line.split("/")) != 2:</pre>
                continue
            #split the string up
            word = line.split("/")[0].replace(" ", "").replace("\t", "").strip()
            tag = line.split("/")[1].replace(" ", "").replace("\t", "").strip()
            file_representation.append( (word, tag) )
        # close the file
        f.close()
        return file_representation
print (read_pos_file_modified("onesentence.txt"))
     #expects The file represented as a list of tuples, where each tuple is of the
     \rightarrow form (word, POS-tag).
     #passes
    [('The', 'DT'), ('New', 'NNP'), ('Deal', 'NNP'), ('was', 'VBD'), ('a', 'DT'),
    ('series', 'NN'), ('of', 'IN'), ('domestic', 'JJ'), ('programs', 'NNS'),
    ('enacted', 'VBN'), ('in', 'IN'), ('the', 'DT'), ('United', 'NNP'), ('States',
    'NNPS'), ('between', 'IN'), ('1933', 'CD'), ('and', 'CC'), ('1936', 'CD'), (',',
    ','), ('and', 'CC'), ('a', 'DT'), ('few', 'JJ'), ('that', 'WDT'), ('came',
    'VBD'), ('later', 'RB'), ('.', '.')]
[6]: def parse_test_file(test_file):
```

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Parses a test file into a list of lists, where the inner lists are sentences
        Input: A testing data file, test_file
        Outputs: a list of words in the file, and a list of lists as described above
        # open the file
        f = open(test_file, "r")
        #split the file into a list
        list_of_words = f.read().split()
        testing_block = []
        L = len(list_of_words)
        count = 0
        while count < L:
            #container for each sentence
            sentence = []
            for word in list_of_words:
                #add word to the sentence
                sentence.append(word)
                count += 1
                if word == ".":
                    # add sentence to the testing block
                   testing_block.append(sentence)
                   sentence = []
        return list_of_words, testing_block
# print (parse_test_file("testdata_untagged.txt"))
    #expect the test data parsed into a list of list
    #passes
[8]: def wrangle_data(training_data_file, percent):
        Inputs: training_data_file, a text file of tagged training data
                percent: a decimal represeting the amount of data you want to build_
     \hookrightarrow a \mod el \ on
        Output: partitioned data, a sequence of (word, tag) tuples
        #read in data
        data = read_pos_file_modified(training_data_file)
```

```
[10]: def get_unique_words_and_tags(data):
            Gets the unique words and tags in a data set
            Input: Data in the representation returned by read pos
            Output: 2 sets, one that holds the unique words and one that holds the unique words and one that holds the unique words and one that holds the unique words are the unique words.
        \hookrightarrow unique tags
            #init empty sets
            unique_words = set([])
            unique_tags = set([])
            for pair in data:
                 #add the word if its not already been seen
                 if pair[0] not in unique_words:
                      unique_words.add(pair[0])
                 #add the tag if its not already been seen
                 if pair[1] not in unique_tags:
                      unique_tags.add(pair[1])
            return unique_words, unique_tags
```

```
#fifty = wrangle data("training.txt", 0.5)
      #print (get_unique_words_and_tags(fifty))
      # expects two sets with unique words and tags, on fifty percent of the training_
      \rightarrow data
      # passes
     fifty = wrangle_data("training.txt", 0.1)
      #print (get_unique_words_and_tags(fifty))
      # expects two sets with unique words and tags, on ten percent of the training
      \rightarrow data
      # passes
[12]: def compute_counts(training_data, order):
         Function that computes different relevant counts about the input file
         Input: Training data, a list of (word, POS-tag) pairs returned by the
      \hookrightarrow function read\_pos\_file,
                Order, the order of the hidden markov model
         Output: If the HMM order is 2, the function returns a tuple consisting of:
                     the number of tokens in training data
                     dictionary that contains that contains C(ti,wi) for every
      →unique tag and unique word (keys correspond to tags)
                         The number of times word wi is tagged with ti
                     a dictionary that contains C(ti)
                         The number of times tag ti appears
                     a dictionary that contains C(ti-1, ti)
                         The number of times the tag sequence ti-1, ti appears
                  If the HMM order is 3, the function returns a tuple consisting of:
                     the number of tokens in training data
                     dictionary that contains that contains C(ti,wi) for every
      →unique tag and unique word (keys correspond to tags)
                     a dictionary that contains C(ti)
                     a dictionary that contains C(ti-1, ti)
                     a dictionary that contains C(ti-2, ti-1, ti)
                         The number of times the tag sequence ti-2, ti-1, ti appears
          11 II II
         # get the number of tokens in the training set
         numtokens = len(training_data)
         # counts the number of times word wi is taked with tag ti
         word2tag_dict = defaultdict(lambda: defaultdict(int))
```

```
# counts the number of times tag ti appears
   tag_count_dict = defaultdict(int)
   # counts the number of times the tag sequence ti-1, ti appears
   bigramdict = defaultdict(lambda: defaultdict(int))
   # counts the number of times the tag sequence ti-2, ti-1, ti appears
   trigramdict = defaultdict(lambda: defaultdict(lambda: defaultdict(int)))
   for i in range(0, numtokens):
       #increment the tag_count_dict
       tag_count_dict[training_data[i][1]] += 1
       #increment the word2tag_dict
       word2tag_dict[training_data[i][1]][training_data[i][0]]+=1
       if i > 0:
           if training_data[i-1][1] != ".":
               #increment the bigram dict
               bigramdict[training_data[i-1][1]][training_data[i][1]] += 1
       if order > 2:
           if i > 1:
               if (training_data[i-2][1] != ".") and (training_data[i-1][1] !=__
→"."):
                   #increment the trigram dict

→trigramdict[training_data[i-2][1]][training_data[i-1][1]][training_data[i][1]]

→+= 1
   if order == 2:
       return(numtokens, word2tag_dict, tag_count_dict, bigramdict)
       return(numtokens, word2tag_dict, tag_count_dict, bigramdict,__
→trigramdict)
```

```
#print(tinydata[0])
      #Order 2 test on a single sentence
      print(compute_counts(tinydata[0], 2)[0])
      print(dict(compute_counts(tinydata[0], 2)[1]))
      print(dict(compute_counts(tinydata[0], 2)[2]))
      #expect a dictionary with the correct amount of words in the sentence
      #passes
      # Order 3 test on a single sentence
      #print(dict(compute counts(tinydata[0], 3)))
      # expect a dictionary with the correct amount of words in the sentence
      # passes
     26
     {'DT': defaultdict(<class 'int'>, {'The': 1, 'a': 2, 'the': 1}), 'NNP':
     defaultdict(<class 'int'>, {'New': 1, 'Deal': 1, 'United': 1}), 'VBD':
     defaultdict(<class 'int'>, {'was': 1, 'came': 1}), 'NN': defaultdict(<class</pre>
     'int'>, {'series': 1}), 'IN': defaultdict(<class 'int'>, {'of': 1, 'in': 1,
     'between': 1}), 'JJ': defaultdict(<class 'int'>, {'domestic': 1, 'few': 1}),
     'NNS': defaultdict(<class 'int'>, {'programs': 1}), 'VBN': defaultdict(<class
     'int'>, {'enacted': 1}), 'NNPS': defaultdict(<class 'int'>, {'States': 1}),
     'CD': defaultdict(<class 'int'>, {'1933': 1, '1936': 1}), 'CC':
     defaultdict(<class 'int'>, {'and': 2}), ',': defaultdict(<class 'int'>, {',':
     1}), 'WDT': defaultdict(<class 'int'>, {'that': 1}), 'RB': defaultdict(<class
     'int'>, {'later': 1}), '.': defaultdict(<class 'int'>, {'.': 1})}
     {'DT': 4, 'NNP': 3, 'VBD': 2, 'NN': 1, 'IN': 3, 'JJ': 2, 'NNS': 1, 'VBN': 1,
     'NNPS': 1, 'CD': 2, 'CC': 2, ',': 1, 'WDT': 1, 'RB': 1, '.': 1}
[14]: def compute_initial_distribution(training_data, order):
          n n n
          Function that computes the intitial distributions of words, pi 1 and pi 2
          Input: Training data, a list of (word, POS-tag) pairs returned by the ⊔
       \hookrightarrow function read\_pos\_file,
                 Order, the order of the hidden markov model
          Output: If order = 2:
                      Returns a one dim dictionary pi_1, that maps a tag to its_
       \hookrightarrow emission probability
                      Returns a 2 dim dictionary pi_2, that maps a bigram to its_{\sqcup}
       \rightarrow emmission probability
```

```
numtokens = len(training_data)
   # initialize the pi dictionaries
   pi_1 = defaultdict(int)
   pi_2 = defaultdict(lambda: defaultdict(int))
   if order==2:
       # the first tag is the second element of the first tuple
       first_tag = training_data[0][1]
       # increment the total count by 1
       pi_1[first_tag] += 1
   else:
       # aceess the first and second tags
       first_tag = training_data[0][1]
       second_tag = training_data[1][1]
       # increment the dictionary
       pi_2[first_tag][second_tag] += 1
   # set the total counts to be 1, we will normalize later
   order2count = 1
   order3count = 1
   for i in range(order -1, numtokens - order + 1):
       if order == 2:
           #if we encounter a period, we know we have the beginning of a_{\sqcup}
\rightarrowsentence
           if training_data[i-1][1] == ".":
               # increment the count by 1
               pi_1[training_data[i][1]] += 1
               order2count += 1
       if order == 3:
           # if two words ago was a period, then we have a bigram that is at \Box
→ the begining of a word
           # will fail for 1 word sentences
           if training_data[i-2][1] == ".":
               pi_2[training_data[i-1][1]][training_data[i][1]] += 1
```

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order3count +=1
         if order == 2:
             for key, value in pi_1.items():
                 #normalize by the order 2 count
                 pi_1[key] = float(float(value)/float(order2count))
             return pi_1
         else:
             # iterate through the keys and values
             for key, value in pi_2.items():
                 # value is a dict, whose "values" are counts
                 for tag, count in value.items():
                     #normalize by the order 3 count
                    pi_2[key][tag] = float(float(count)/float(order3count))
             return pi_2
littledata = read_pos_file('littledata.txt')
     print(compute_initial_distribution(littledata[0], 3))
     #expect DT-JJ to be 1/2 and NNP-NNPS to be 1/2
     #passes
     littledata = read_pos_file('littledata.txt')
     print(compute_initial_distribution(littledata[0], 2))
     # #expect DT to be 1/2 and NNP to be 1/2
     # #passes
     defaultdict(<function compute_initial_distribution.<locals>.<lambda> at
     0x7fd19bed9700>, {'DT': defaultdict(<class 'int'>, {'JJ': 0.5}), 'NNP':
     defaultdict(<class 'int'>, {'NNPS': 0.5})})
     defaultdict(<class 'int'>, {'DT': 0.5, 'NNP': 0.5})
[16]: def compute_emission_probabilities(unique_words, unique_tags, W, C):
         Function computes the emmission matrix for different parts of speech given_
      \hookrightarrow training data
         Input: unique_words: a set of unique words returned by the read_pos function
                unique_tags : a set of unique tags returned by the read_pos function
```

```
W: the C(ti, wi) dictionary returned by the function compute_counts
C: the C(ti) dictionary returned by the function compute_counts

Output: emission matrix, a 2d dict where the keys are parts of speech

"""

#initialize the emission matrix
emission_matrix = defaultdict(lambda: defaultdict(int))

# tags are keys in the emission matrix
for tag in unique_tags:
    for word in W[tag].keys():

        #caluculate emission prob
        emission_matrix[tag][word] = float(float(W[tag][word])/

infloat(C[tag]))

return emission_matrix
```

```
→#######################
     tinydata = read_pos_file('onesentence.txt')
     unique words2 = tinydata[1]
     unique tags2 = tinydata[2]
     w1 = compute counts(tinydata[0], 2)[1]
     C1 = compute_counts(tinydata[0], 2)[2]
     print(compute_emission_probabilities(unique_words2, unique_tags2, w1, C1))
     # expect a dict with each word corresponding to its emmission prob
     # passes
     onethousand = read_pos_file("onethousandlines.txt")
     unique_tags = onethousand[2]
     unique_words = onethousand[1]
     c1 = compute_counts(onethousand[0], 3)[1]
     c2 = compute_counts(onethousand[0], 3)[2]
     # print(compute_emission_probabilities(unique_words, unique_tags, c1, c2))
     # # expect a dict with each word corresponding to its emmission prob
     # # passes
```

```
defaultdict(<function compute_emission_probabilities.<locals>.<lambda> at
0x7fd1a441b160>, {'VBN': defaultdict(<class 'int'>, {'enacted': 1.0}), 'CD':
defaultdict(<class 'int'>, {'1933': 0.5, '1936': 0.5}), 'VBD':
defaultdict(<class 'int'>, {'was': 0.5, 'came': 0.5}), 'NN': defaultdict(<class
'int'>, {'series': 1.0}), 'JJ': defaultdict(<class 'int'>, {'domestic': 0.5,
'few': 0.5}), ',': defaultdict(<class 'int'>, {',': 1.0}), 'NNS':
```

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0.333333333333333), '.': defaultdict(<class 'int'>, {'.': 1.0}), 'CC':
     defaultdict(<class 'int'>, {'and': 1.0}), 'IN': defaultdict(<class 'int'>,
     0.333333333333333), 'RB': defaultdict(<class 'int'>, {'later': 1.0}), 'DT':
     defaultdict(<class 'int'>, {'The': 0.25, 'a': 0.5, 'the': 0.25}), 'WDT':
     defaultdict(<class 'int'>, {'that': 1.0}), 'NNPS': defaultdict(<class 'int'>,
     {'States': 1.0})})
[18]: def compute_lambdas(unique_tags, num_tokens, C1, C2, C3, order):
         Function implements the Algorithm Compute_Lambdas
         Inputs: unique tags: a set of unique tags returned by the read pos function
                 numtokens: number of words in the training corpus
                 C1: C(ti), The number of times tag ti appears
                 C2: C(ti-1, ti), the Number of times the sequence ti-1, ti appears
                 C3: C(ti-2, ti-1, ti) the number of times the sequence ti-2, ti-1, \sqcup
      \hookrightarrow ti appears
         Outputs: A list that contains lambda1, lambda2, lambda2
          11 II II
         lambdas = [0.0, 0.0, 0.0]
         counter = 0
         # only if order is 3 do we consider trigrams
         if order == 3:
             # access ti -2
             for timinus2, value in C3.items():
                 # access ti-1
                 for timinus1, value2 in value.items():
                     # access ti
                     for ti, count in value2.items():
                         counter += 1
                         # initialize the argmax
                         argmax = 0
                         max_alpha = 0
                         # calculate the alpha scores
                         for i in range(3):
```

defaultdict(<class 'int'>, {'programs': 1.0}), 'NNP': defaultdict(<class 'int'>,

```
if i == 0:
                           if float(num_tokens) == 0:
                               alpha = 0
                               alpha = float(float(C1[ti] - 1)/
→float(num_tokens))
                       if i == 1:
                           if float(C1[timinus1] - 1) == 0:
                               alpha = 0
                           else:
                               #print "hey", C2[timinus1][ti]
                               #print C1[timinus1]
                               alpha = float(float(C2[timinus1][ti] - 1)/
→float(C1[timinus1] - 1))
                       if i == 2:
                           if float(C2[timinus2][timinus1] - 1) == 0:
                               alpha = 0
                           else:
                               alpha = float(float(C3[timinus2][timinus1][ti]_u
→ 1)/float(C2[timinus2][timinus1] - 1))
                       # find the biggest alpha
                       if alpha > max_alpha:
                           max_alpha = alpha
                           argmax = i
                   # increment alpha
                   lambdas[argmax] += C3[timinus2][timinus1][ti]
       # calculate the lambda values
       lambdas_sum = sum(lambdas)
       for i in range(order):
           lambdas[i] = float(float(lambdas[i])/float(lambdas_sum))
       return lambdas
   # if order is equal to 2
   else:
       \#access\ ti-\ 1 and ti
       for timinus1, value2 in C2.items():
           for ti, count in value2.items():
               argmax = 0
```

```
max_alpha = 0
               #calculate alpha scores
               for i in range(2):
                   if i == 0:
                       if float(num_tokens) == 0:
                            alpha = 0
                       else:
                           alpha = float(float(C1[ti] - 1)/float(num_tokens))
                   if i == 1:
                       if float(C1[timinus1] - 1) == 0:
                           alpha = 0
                       else:
                            alpha = float(float(C2[timinus1][ti] - 1)/
→float(C1[timinus1] - 1))
                   if alpha > max_alpha:
                       max_alpha = alpha
                       argmax = i
               # increment lambda
               lambdas[argmax] += C2[timinus1][ti]
       # calculate the final lambda values
       lambdas_sum = sum(lambdas)
       for i in range(order):
           lambdas[i] = float(float(lambdas[i])/float(lambdas_sum))
       return lambdas
```

```
# expect 2 lambda values that are not 0 that sum to 1
# passes
```

[0.20472736536501893, 0.7952726346349811, 0.0] [0.9583333333333334, 0.04166666666666664, 0.0]

```
[20]: def compute_transition_matrix(training_data, unique_tags, order, use_smoothing):
           HHHH
           Input: training_data, a file containing training data,
               unique tags, a set of unique tags in the data,
               order, the order of the HMM
               use smoothing: a boolean paramater
          \mathit{Output}: \mathit{transistion} \mathit{matrix}: a \mathit{matrix} that \mathit{contains} the \mathit{transistion}
       \hookrightarrow probabiility between states
           11 11 11
           # order
          if order == 2:
               # get the counts
               # counts = compute counts(training data, 2)
               counts_trigram = compute_counts(training_data, 3)
               # get the number of tokens
               num_tokens = counts_trigram[0]
               # if smoothing is true, compute the appropriate lambda values
               if use_smoothing == True:
                   lambdas = compute_lambdas(unique_tags, num_tokens,_
       →counts_trigram[2], counts_trigram[3], counts_trigram[4], order)
               else:
                   lambdas = [0, 1, 0]
               # compute the transition matrix
               transition_matrix = defaultdict(lambda: defaultdict(int))
               # obtain ti - 1
               for timinus1 in unique_tags:
                   # obtain ti
                   for ti in unique_tags:
                       term1 =
       →(float(lambdas[1])*float(counts_trigram[3][timinus1][ti])/
       →float(counts_trigram[2][timinus1]))
                       term2 = (float(lambdas[0])*float(counts trigram[2][ti])/
       →float(num_tokens))
```

```
transition_matrix[timinus1][ti] = float(term1) + float(term2)
      return transition_matrix
  else:
      #get your counts
      counts_trigram = compute_counts(training_data, 3)
      # get the number of tokens
      num_tokens = counts_trigram[0]
      # if smoothing is true, compute the appropriate lambda values
      if use_smoothing == True:
          lambdas = compute_lambdas(unique_tags, num_tokens,_
else:
          lambdas = [0.0, 0.0, 1.0]
      # compute the transition matrix
      transition_matrix = defaultdict(lambda: defaultdict(lambda:__
→defaultdict(int)))
      for timinus2 in unique_tags:
          # obtain ti - 1
          for timinus1 in unique_tags:
              # obtain ti
              for ti in unique_tags:
                  # calculate term 1 of the equation
                  if float(counts_trigram[3][timinus2][timinus1]) == 0:
                     term1 = 0
                  else:
                     term1 =
→(float(lambdas[2])*float(counts_trigram[4][timinus2][timinus1][ti]))/
→float(counts_trigram[3][timinus2][timinus1])
                  #caluculate term 2 of the equations
                  if float(counts_trigram[2][timinus1]) == 0:
                     term2 = 0
                  else:
                      term2 =
→(float(lambdas[1])*float(counts_trigram[3][timinus1][ti])/
→float(counts_trigram[2][timinus1]))
```

defaultdict(<function compute\_transition\_matrix.<locals>.<lambda> at 0x7fd1803628b0>, {'VBN': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 1.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'CD': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.5, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.5, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'VBD': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 0.0, 'RB': 0.5, 'DT': 0.5, 'WDT': 0.0, 'NNPS': 0.0}), 'NN': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 1.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'JJ': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.5, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.5, 'NNPS': 0.0}), ',': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 1.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'NNS': defaultdict(<class 'int'>, {'VBN': 1.0, 'CD': 0.0, 'VBD':

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0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'NNP':
    'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.3333333333333333, '.': 0.0,
    'CC': 0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS':
    'VBD': 0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0,
    'CC': 0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'CC':
    defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.5, 'VBD': 0.0, 'NN': 0.0, 'JJ':
    0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 0.0, 'RB':
    0.0, 'DT': 0.5, 'WDT': 0.0, 'NNPS': 0.0}), 'IN': defaultdict(<class 'int'>,
    0.0, 'RB': 0.0, 'DT': 0.333333333333333, 'WDT': 0.0, 'NNPS': 0.0}), 'RB':
    defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ':
    0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 1.0, 'CC': 0.0, 'IN': 0.0, 'RB':
    0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'DT': defaultdict(<class 'int'>,
    {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.25, 'JJ': 0.25, ',': 0.0, 'NNS':
    0.0, 'NNP': 0.5, '.': 0.0, 'CC': 0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT':
    0.0, 'NNPS': 0.0}), 'WDT': defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0,
    'VBD': 1.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0,
    'CC': 0.0, 'IN': 0.0, 'RB': 0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0}), 'NNPS':
    defaultdict(<class 'int'>, {'VBN': 0.0, 'CD': 0.0, 'VBD': 0.0, 'NN': 0.0, 'JJ':
    0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC': 0.0, 'IN': 1.0, 'RB':
    0.0, 'DT': 0.0, 'WDT': 0.0, 'NNPS': 0.0})})
[22]: def build_hmm(training_data, unique_tags, unique_words, order, use_smoothing):
        Creates a fully trained Hidden Markov Model
        Inputs: training data: a full training corpus,
                unique tags: a set of parts of speech found in the training corpus
               unique_words : a set of words found in the training corpus
                order: the order of the markov chain
               Use_smoothing : a boolean parameter
        Outputs: a fully trained HMM object
         11 11 11
        # build an order 2 markov model
        counts = compute_counts(training_data, order)
        #compute the initial distribution
        initial_distribution = compute_initial_distribution(training data, order)
         #compute the emission matrix
```

0.0, 'NN': 0.0, 'JJ': 0.0, ',': 0.0, 'NNS': 0.0, 'NNP': 0.0, '.': 0.0, 'CC':

```
W_dict = counts[1]
  C_dict = counts[2]
  emission_matrix = compute_emission_probabilities(unique_words, unique_tags, unique_tags,
```

```
onethousand = read_pos_file("onethousandlines.txt")
     unique_tags = onethousand[2]
     unique_words = onethousand[1]
     #print(build hmm(onethousand[0], unique tags, unique words, 2, True))
     #expect am HMM object
     #passes
     tinydata = read_pos_file('onesentence.txt')
     unique_tags = tinydata[2]
     unique_words = tinydata[1]
     model = build_hmm(tinydata[0], unique_tags, unique_words, 3, False)
     #Expect an HMM Object
     #View the HMM Attributes
     #print( "Order", model.order)
     #print( "Intial Dist", model.initial distribution)
     #print( "Emmission Matrix", model.emission_matrix)
     #print( "trans mat", model.transition_matrix)
     # pass
```

```
[24]: def update_hmm(hmm, sentence):
    """

Function updates HMM based on new words it encounters

Input: an hmm object and a sentence, a list of strings ending with a period

Output: An updated hmm object

"""

#get the attributes of the hidden markov model

order = hmm.order

initial_distribution = hmm.initial_distribution

emission_matrix = hmm.emission_matrix
```

```
transition_matrix = hmm.transition_matrix
   # get all the words
   unique_words = []
   for pos in emission_matrix:
       for word in emission_matrix[pos]:
           # add each word that the model has seen into unique words
           unique_words.append(word)
   #bool flag for if any new words were encountered
   new_word = False
   for word in sentence:
       # if the word is new, we want to add update the HMM
       if word not in unique_words:
           # if we get to this line, we have a new word
           new word = True
           for part_of_speech in emission_matrix:
               for seen_word in emission_matrix[part_of_speech]:
                   # increment the each word by the same amount
                   emission_matrix[part_of_speech][seen_word] += 0.00001
               # add the new word to each part of speech with a small_
\rightarrowprobability
               emission_matrix[part_of_speech][word] = 0.00001
   if new_word == True:
       #begin the normalization process
       for tag in emission_matrix:
           # find the normalizing term
           normalizer = sum(emission_matrix[tag].values())
```

```
# normalize each word
                for finalword in emission_matrix[tag]:
                    emission_matrix[tag][finalword] = [
      →float(emission_matrix[tag][finalword])/float(normalizer)
             # updated model = HMM(order, initial distribution, emission matrix, ____
      \hookrightarrow transition_matrix)
         return HMM(order, initial distribution, emission matrix, transition matrix)
\hookrightarrow HMM
     alldata = read_pos_file("training.txt")
     unique_tags = alldata[2]
     unique words = alldata[1]
     hiddenmarkovmodel = build_hmm(alldata[0], unique_tags, unique_words, 2, False)
     print (hiddenmarkovmodel.order)
     #expect a new hmm of order 2
     #passes
```

hiddenmarkovmodel = build\_hmm(alldata[0], unique\_tags, unique\_words, 3, False)

2

#passes

alldata = read\_pos\_file("training.txt")

unique\_tags = alldata[2]
unique\_words = alldata[1]

print (hiddenmarkovmodel.order)
#expect a new hmm of order 3

```
[26]: def log(number):
    """
    Caluculates the Logarithm of a number, and returns -inf in the number is 0
    Inputs : number, a real number
    Output : The log of a number, whihe is a real number of -inf
    """

# log of 0 is negative infinity

if number == 0:
    return float("-inf")
    else:
    return float(math.log(number))
```

#### -inf

# 4.23410650459726

```
[27]: def bigram_viterbi(hmm, sentence):
          Implements the Viterbi algorithm for the bigram model on an input HMM and a_{\sqcup}
       ⇒sentence (a list of words and the period at the end).
          Input: HMM, an HMM object, and sentence, a list of words with a period at_{\sqcup}
       \hookrightarrow the end
          Output: Tagged Words : a list of words and their tags
          #get the data from the HMM object
          {\tt initial\_distribution} \ = \ {\tt hmm.initial\_distribution}
          emission_matrix = hmm.emission_matrix
          transition_matrix = hmm.transition_matrix
          # init V and BP
          V = defaultdict(lambda: defaultdict(int))
          bp = defaultdict(lambda: defaultdict(int))
          # length of the input sentence.
          L = len(sentence)
          # init the first column of the V matrix
          for pos in emission_matrix:
               #caluclate the first column of the matrix
              pi_sub_l = log(initial_distribution[pos])
               emissison_prob_x0 = log(emission_matrix[pos][sentence[0]])
              V[pos][0] = pi_sub_l + emissison_prob_x0
          for i in range(1, L):
               # l is a part of speech, more generally, a markov state
```

```
for l in emission_matrix:
           max_prob = -float("inf")
           argmax = None
           # find the different l_prime values that can be take, then_
\rightarrow determine the argmax and the max
           for l_prime in emission_matrix:
               transition_probability = log(transition_matrix[l_prime][l])
               previous_prob = V[l_prime][i-1]
               possible_max = transition_probability + previous_prob
               #update l prime
               if possible_max > max_prob:
                   max_prob = possible_max
                   argmax = l_prime
           # if none
           if argmax == None:
               for l_prime in emission_matrix.keys():
                   if V[l_prime][i-1]>= max_prob:
                       max_prob = V[l_prime][i-1]
                       argmax = l_prime
           emission_prob = log(emission_matrix[l][sentence[i]])
           #update V and BP
           V[1][i] = emission_prob + max_prob
           bp[1][i] = argmax
   # begin traceback
   argmax2 = None
   max_val_holder = -float("inf")
   #access the first element in the Sequence
   for l_prime_pos in emission_matrix:
       v_mat_entry = V[l_prime_pos][L-1]
       #get highest entry
       if v_mat_entry > max_val_holder:
           max_val_holder = v_mat_entry
           argmax2 = 1_prime_pos
   sentence[L-1] = (sentence[L-1], argmax2)
```

```
for i in range(L-2, -1, -1):
             zi = bp[sentence[i+1][1]][i+1]
             sentence[i] = (sentence[i], zi)
         return sentence
\hookrightarrow VITERBI
     alldata = read_pos_file("training.txt")
     unique_tags = alldata[2]
     unique words = alldata[1]
     hiddenmarkovmodel = build_hmm(alldata[0], unique_tags, unique_words, 2, False)
     print (bigram_viterbi(hiddenmarkovmodel, ["My", "hips", "do", "not", "lie", ".
     # Expect Possesive, noun, verb, negator, verb, period
      # Passes
     alldata = read_pos_file("training.txt")
     unique tags = alldata[2]
     unique words = alldata[1]
     hiddenmarkovmodel = build hmm(alldata[0], unique tags, unique words, 2, False)
     print (bigram_viterbi(hiddenmarkovmodel, ["I", "hope", "I", "pass", "this", __
      # Expect Pronoun, verb, Pronoun, verb, determiner, noun, perios
     # Passes
     [('My', 'PRP$'), ('hips', 'NNS'), ('do', 'VBP'), ('not', 'RB'), ('lie', 'VB'),
     ('.', '.')]
     [('I', 'PRP'), ('hope', 'VBP'), ('I', 'PRP'), ('pass', 'VBP'), ('this', 'DT'),
     ('class', 'NN'), ('.', '.')]
[29]: def trigram_viterbi(hmm, sentence):
         Implements the Viterbi algorithm for the treigram model on an input HMM and \sqcup
      \rightarrowa sentence (a list of words and the period at the end).
         Input: HMM, an HMM object, and sentence, a list of words with a period at_{\sqcup}
      \hookrightarrow the end
         Output: Tagged Words : a list of words and their tags
         #get the data from the HMM object
         initial_distribution = hmm.initial_distribution
         emission_matrix = hmm.emission_matrix
```

#traceback

```
transition_matrix = hmm.transition_matrix
   # init V and BP
   V = defaultdict(lambda: defaultdict(lambda: defaultdict(int)))
   bp = defaultdict(lambda: defaultdict(lambda: defaultdict(int)))
   # length of the input sentence.
   L = len(sentence)
   #being building the V matrix
   # init the l prime of the V matrix
   for pos_l_prime in emission_matrix:
       #init the l state
       for pos_l in emission_matrix:
           #caucluate the first column/plane in the 3d matrix
           pi_sub_lprime_l = log(initial_distribution[pos_l_prime][pos_l])
           emissison_prob_x0 = log(emission_matrix[pos_l_prime][sentence[0]])
           emissison_prob_x1 = log(emission_matrix[pos_1][sentence[1]])
           # put the entry in the matrix
           V[pos_l_prime][pos_l][1] = pi_sub_lprime_l + emissison_prob_x0 + 
→emissison_prob_x1
   for i in range(2, L):
       # l is a part of speech, more generally, a markov state
       for l_prime in emission_matrix:
           # find the different l_prime values that can be take, then_
\rightarrow determine the argmax and the max
           for l in emission_matrix:
               bestmax = -float("inf")
               argmax = None
               for l_double_prime in emission_matrix:
                   #calculate possible entries
                   transition_probability =_
→log(transition_matrix[l_double_prime][l_prime][l])
                   previous_prob = V[l_double_prime][l_prime][i-1]
                   possible_max = transition_probability + previous_prob
```

```
# update l double prime
                if possible_max > bestmax:
                    bestmax = possible_max
                    argmax = l_double_prime
            #if none in matrix
            if argmax == None:
                for l_double_prime in emission_matrix.keys():
                    if V[l_double_prime][l_prime][i-1] >= bestmax:
                        bestmax = V[l_double_prime][l_prime][i-1]
                        argmax = l_double_prime
            emission_prob = log(emission_matrix[l][sentence[i]])
            #update V and BP
            V[l_prime][l][i] = emission_prob + bestmax
            bp[l_prime][l][i] = argmax
# begin traceback
ZL_minus_1 = None
ZL minus 2 = None
max_val_holder= -float("inf")
#access the first element in the Sequence
for state_1 in emission_matrix:
    for state_2 in emission_matrix:
        v_mat_entry = V[state_1][state_2][L-1]
        #qet highest entry
        if v_mat_entry > max_val_holder:
            max_val_holder = v_mat_entry
            ZL_minus_1 = state_2
            ZL_minus_2 = state_1
#init last Z values
sentence[L-1] = (sentence[L-1], ZL_minus_1)
sentence[L-2] = (sentence[L-2], ZL_minus_2)
#traceback
for i in range(L-3, -1, -1):
    zi = bp[sentence[i+1][1]][sentence[i+2][1]][i+2]
    sentence[i] = (sentence[i], zi)
return sentence
```

```
[('I', 'PRP'), ('am', 'VBP'), ('the', 'DT'), ('machine', 'NN'), ('.', '.')]
[('I', 'PRP'), ('am', 'VBP'), ('happy', 'JJ'), ('.', '.')]
```

# 0.1 ANALYSIS CODE

```
a = ["a", "a", "a", "a"]
     b = ["a", "b", "a", "a"]
     print (compute_accuracy(a,b))
     # expect .75
     #passes
     a = ["a", "a", "a", "a"]
     b = ["a", "a", "a", "a"]
     print (compute_accuracy(a,b))
     # expect 1.0
     #passes
     0.75
     1.0
[33]: def bigram_validate(training_data, percent, testdata_untagged, testdata_tagged,__
      →order, use_smoothing):
         Computes the out of sample accuracy of the POS tagging algorithm for bigram ...
      \hookrightarrow HMM
         Inputs: a file training data, a percentage of data, untagged test data, u
      ⇒tagged test data, the order of the markov chain,
                 a boolean parameter use smoothing
         Output: Accuracy, a real number between 0 and 1
         11 11 11
         #wrangle the data
         my_data = wrangle_data(training_data, percent)
         unique_words, unique_tags = get_unique_words_and_tags(my_data)
         #build an HMM
         old_hmm = build_hmm(my_data, unique_tags, unique_words, order,_
      →use_smoothing)
         list_of_words, test_data_parsed = parse_test_file(testdata_untagged)
         #update the HMM if need be
         new_hmm = update_hmm(old_hmm, list_of_words)
         # put the predidted tags into a master list
         full_results = []
         for sentence in test_data_parsed:
             results = bigram_viterbi(new_hmm, sentence)
             for tup in results:
                 full_results.append(tup)
```

```
# read in the validation data
validation_data = read_pos_file_modified(testdata_tagged)

#get the final accuracy
return compute_accuracy(validation_data, full_results)
```

- 0.7587268993839835
- 0.6919917864476386

```
[35]: def trigram_validate(training_data, percent, testdata_untagged,__
       →testdata_tagged, order, use_smoothing):
          Computes the out of sample accuracy of the POS tagging algorithm for bigram,
       \hookrightarrow HMM
          Inputs: a file training data, a percentage of data, untagged test data,\sqcup
       \hookrightarrow tagged test data,
                   the order of the markov chain, a boolean parameter use smoothing
          Output: Accuracy, a real number between 0 and 1
          #wrangle the data
          my_data = wrangle_data(training_data, percent)
          unique words, unique tags = get unique words and tags(my data)
          #build an hmm
          old_hmm = build_hmm(my_data, unique_tags, unique_words, order,_
       →use_smoothing)
          list_of_words, test_data_parsed = parse_test_file(testdata_untagged)
          #update the HMM if any new words are encountered
          new_hmm = update_hmm(old_hmm, list_of_words)
          # put the algorithm's predictions into a master list
          full results = []
          for sentence in test_data_parsed:
```

```
results = trigram_viterbi(new_hmm, sentence)
for tup in results:
    full_results.append(tup)

#read in the validation data
validation_data = read_pos_file_modified(testdata_tagged)

#get an accuracy value
return compute_accuracy(validation_data, full_results)
```

- 0.7453798767967146
- 0.6468172484599589

#### 0.2 EXPERIMENT CODE

```
In experiment one, we build seven bigram HMMs on the first 1%, 5%, 10%, 25\%, _{\square}
     \hookrightarrow 50%,
    75%, and 100% of the training corpus without smoothing and obtain 7 accuracy,
    \hookrightarrow values
    onepercent_1 = bigram_validate("training.txt", 0.01, "testdata_untagged.txt", u
     fivepercent_1 = bigram_validate("training.txt", 0.05, "testdata_untagged.txt", u
     tenpercent_1 = bigram_validate("training.txt", 0.1, "testdata_untagged.txt", u
     twentyfivepercent_1 = bigram_validate("training.txt", 0.25, "testdata_untagged.
    fiftypercent_1 = bigram_validate("training.txt", 0.5, "testdata_untagged.txt", u
     seventyfivepercent_1 = bigram_validate("training.txt", 0.75, "testdata_untagged.
     →txt", "testdata_tagged.txt", 2, False)
```

```
onehundopercent_1 = bigram_validate("training.txt", 1, "testdata_untagged.txt", \( \)

→"testdata_tagged.txt", 2, False)

experiment_1_results = [onepercent_1, fivepercent_1, tenpercent_1, twentyfivepercent_1, fiftypercent_1, \( \)

→seventyfivepercent_1, onehundopercent_1]

print(experiment_1_results)

"""

[0.6919917864476386, 0.8275154004106776, 0.8696098562628337, 0. \( \)

→9055441478439425, 0.9271047227926078, 0.9496919917864476, 0.9579055441478439]

"""
```

[0.6919917864476386, 0.8275154004106776, 0.8696098562628337, 0.9055441478439425, 0.9271047227926078, 0.9496919917864476, 0.9579055441478439]

[37]: '\n[0.6919917864476386, 0.8275154004106776, 0.8696098562628337, 0.9055441478439425, 0.9271047227926078, 0.9496919917864476, 0.9579055441478439]\n'

```
In experiment 2, we build 7 trigram HMMs on the first 1%, 5%, 10%, 25%, 50%,
     75%, and 100% of the training corpus without smoothing and obtain 7 accuracy _{\sqcup}
     \rightarrow values
     . . .
     onepercent_2 = trigram_validate("training.txt", 0.01, "testdata_untagged.txt", u

¬"testdata_tagged.txt", 3, False)
     fivepercent_2 = trigram_validate("training.txt", 0.05, "testdata_untagged.txt", u
     tenpercent_2 = trigram_validate("training.txt", 0.1, "testdata_untagged.txt", u
     twentyfivepercent_2 = trigram_validate("training.txt", 0.25, "testdata_untagged.
     →txt", "testdata tagged.txt", 3, False)
     fiftypercent_2 = trigram_validate("training.txt", 0.5, "testdata_untagged.txt", u
     seventyfivepercent_2 = trigram_validate("training.txt", 0.75, __
     →"testdata_untagged.txt", "testdata_tagged.txt", 3, False)
     onehundopercent_2 = trigram_validate("training.txt", 1, "testdata_untagged.
     →txt", "testdata_tagged.txt", 3, False)
     experiment 2 results = [onepercent 2, fivepercent 2, tenpercent 2, ...
     →twentyfivepercent_2, fiftypercent_2, seventyfivepercent_2, onehundopercent_2]
     print(experiment_2_results)
     111
```

```
[0.6468172484599589, 0.7905544147843943, 0.8357289527720739, 0.

→8593429158110883, 0.8952772073921971, 0.917864476386037, 0.9322381930184805]
```

[0.6468172484599589, 0.7905544147843943, 0.8357289527720739, 0.8593429158110883, 0.8952772073921971, 0.917864476386037, 0.9322381930184805]

[38]: '\n[0.6468172484599589, 0.7905544147843943, 0.8357289527720739, 0.8593429158110883, 0.8952772073921971, 0.917864476386037, 0.9322381930184805]\n\n'

```
In experiment three, we build seven bigram HMMs on the first 1%, 5%, 10%, 25\%, \Box
     \hookrightarrow 50%.
     75%, and 100% of the training corpus with smoothing and obtain 7 accuracy values
     onepercent_3 = bigram_validate("training.txt", 0.01, "testdata_untagged.txt", u
     fivepercent_3 = bigram_validate("training.txt", 0.05, "testdata_untagged.txt", u

¬"testdata_tagged.txt", 2, True)

     tenpercent_3 = bigram_validate("training.txt", 0.1, "testdata_untagged.txt", u
     twentyfivepercent_3 = bigram_validate("training.txt", 0.25, "testdata_untagged.
     ⇔txt", "testdata_tagged.txt", 2, True)
     fiftypercent 3 = bigram validate("training.txt", 0.5, "testdata untagged.txt", 11
     seventyfivepercent_3 = bigram_validate("training.txt", 0.75, "testdata_untagged.
     →txt", "testdata_tagged.txt", 2, True)
     onehundopercent_3 = bigram_validate("training.txt", 1, "testdata_untagged.txt", u
     →"testdata_tagged.txt", 2, True)
     experiment_3_results = [onepercent_3, fivepercent_3, tenpercent_3,_u
     twentyfivepercent_3, fiftypercent_3, seventyfivepercent_3, onehundopercent_3]
     print (experiment_3_results)
     111
     \hookrightarrow 0.9394250513347022, 0.9548254620123203, 0.9599589322381931
     111
```

[0.7587268993839835, 0.8603696098562629, 0.8901437371663244, 0.919917864476386, 0.9394250513347022, 0.9548254620123203, 0.9599589322381931]

```
[39]: '\n[0.7587268993839835, 0.8603696098562629, 0.8901437371663244, 0.919917864476386, 0.9394250513347022, 0.9548254620123203, 0.9599589322381931]\n\n'
```

```
In experiment 2, we build 7 trigram HMMs on the first 1%, 5%, 10%, 25%, 50%,
     75%, and 100% of the training corpus with smoothing and obtain 7 accuracy values
    onepercent_4 = trigram_validate("training.txt", 0.01, "testdata_untagged.txt", u
     fivepercent_4 = trigram_validate("training.txt", 0.05, "testdata_untagged.txt", |

¬"testdata_tagged.txt", 3, True)

    tenpercent 4 = trigram validate("training.txt", 0.1, "testdata untagged.txt", |
     twentyfivepercent_4 = trigram_validate("training.txt", 0.25, "testdata_untagged.
     →txt", "testdata_tagged.txt", 3, True)
    fiftypercent_4 = trigram_validate("training.txt", 0.5, "testdata_untagged.txt", u
     seventyfivepercent_4 = trigram_validate("training.txt", 0.75,
     onehundopercent_4 = trigram_validate("training.txt", 1, "testdata_untagged.
     experiment_4 results = [onepercent_4, fivepercent_4, tenpercent_4,__
     -twentyfivepercent_4, fiftypercent_4, seventyfivepercent_4, onehundopercent_4]
    print(experiment_4_results)
     [0.7453798767967146, 0.86652977412731, 0.8993839835728953, 0.9281314168377823,,,]
     \rightarrow 0.9496919917864476, 0.9640657084188912, 0.9691991786447639]
     111
```

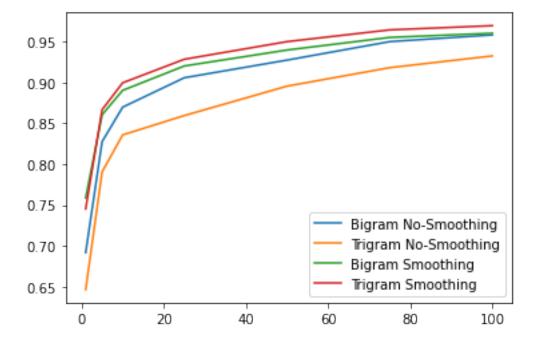
[0.7453798767967146, 0.86652977412731, 0.8993839835728953, 0.9281314168377823, 0.9496919917864476, 0.9640657084188912, 0.9691991786447639]

[40]: '\n[0.7453798767967146, 0.86652977412731, 0.8993839835728953, 0.9281314168377823, 0.9496919917864476, 0.9640657084188912, 0.9691991786447639]\n\n'

```
[41]: # importing package
import matplotlib.pyplot as plt

# create data
x = [1,5,10,25,50, 75, 100]
y1 = experiment_1_results
```

```
y2 = experiment_2_results
y3 = experiment_3_results
y4 = experiment_4_results
# plot lines
plt.plot(x, y1, label = "Bigram No-Smoothing")
plt.plot(x, y2, label = "Trigram No-Smoothing")
plt.plot(x, y3, label = "Bigram Smoothing")
plt.plot(x, y4, label = "Trigram Smoothing")
plt.plot(x, y4, label = "Trigram Smoothing")
```



[]: