CodeBook MU_Resplendence

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Part 1 ⇒ Number Theory

1.1: BigMod

```
11 BigMod(ll a, ll b, ll m) {
    if(!b) {
        return 1 % m;
    }
    ll x = BigMod(a, b / 2, m);
    x = (x * x) % m;
    if(b & 1) {
        x = (x * a) % m;
    } return x;
}
```

1.2: Modular Inverse

```
pll extendedEuclid(ll a, ll b) { // returns x, y | ax + by = gcd(a,b)
    if(b == 0) {
        return pll(1LL, 0LL);
    }
    else {
        pll d = extendedEuclid(b, a % b);
        return pll(d.second, d.first - d.second * (a / b));
    }
}

ll modularInverse(ll a, ll n) {
    pair<ll, ll> ret = extendedEuclid(a, n);
    return ((ret.first % n) + n) % n;
}
```

1.3: Sieve

```
bool isPrime[1000101];

void sieve() {
   int MAX = 1000100, sq = sqrt(MAX);
   memset(isPrime, true, sizeof isPrime);
   for(int i = 4; i <= MAX; i += 2) {
        isPrime[i] = 0;
   }
}</pre>
```

```
}
    for(int i = 3; i \le sq; i += 2) {
        if(isPrime[i]) {
            for(int j = i * i; j <= MAX; j += i) {
                 isPrime[j] = 0;
            }
        }
    }
    isPrime[1] = 0;
    isPrime[0] = 0;
}
1.4: nCr
11 f[Max], inv[Max];
11 BigMod(ll a, int e) {
    if(e == -1) {
        e = Mod - 2;
    11 r = 1;
    while(e) {
        if(e & 1) {
            r *= a, r %= Mod;
        a *= a, a %= Mod, e >>= 1;
    return r;
}
11 nCr(int x, int y) {
    if(x < 0 \text{ or } y < 0 \text{ or } x < y) {
        return 0;
    }
    return f[x] * (inv[y] * inv[x - y] % Mod) % Mod;
}
void init() {
    f[0] = 1;
    for(int i = 1; i < Max; ++i) {</pre>
        f[i] = i * 1LL * f[i - 1] % Mod;
    }
    inv[Max - 1] = BigMod(f[Max - 1], -1);
    for(int i = Max - 1; i; --i) {
        inv[i - 1] = i * 1LL * inv[i] % Mod;
    }
}
```

1.5: nCr with DP

```
11 nCr[Max][Max];

11 rec(ll n, ll r) {
    if(n == r) {
        return 1;
    }
    if(r == 1) {
        return n;
    }
    ll &ret = nCr[n][r];
    if(~ret) {
        return ret;
    }
    ret = rec(n - 1, r) + rec(n - 1, r - 1);
    return ret;
}
```

1.6: Phi Function

```
11 phi[Max];
void phigen(int n) {
    for(int i = 1; i <= n; i++) {
        phi[i] = i;
    }
    for(int p = 2; p <= n; p++) {
        if(phi[p] == p) {
            phi[p] = p - 1;
            for(int i = 2 * p; i <= n; i += p) {
                 phi[i] = (phi[i] / p) * (p - 1);
            }
        }
     }
}</pre>
```

1.7: Divisor Count

```
11 divcnt[Max];
void DivisorCount(ll n) {
    for(int i = 1; i <= n; i++) {
        for(int j = i; j <= n; j += i) {</pre>
```

```
divcnt[j]++;
}
}
```

1.8: Sum of Divisors in a range

```
ll triangle(ll a, ll b) {
    return (a + b + 1) * (b - a) / 2;
}
11 divSum(ll a, ll b) { // Sum of divisors between a to b
    11 n = sqrt(b);
    11 \text{ sum} = 0;
    for(ll i = 1; i <= n; i++) {
        sum += i * (b / i - a / i) + triangle(max(n, a / i), max(n, b / i));
    }
    return sum;
}
int main() {
    ll a, b;
    cin >> a >> b;
    ll ans = divSum(a - 1, b);
    cout << ans << endl;</pre>
    return 0;
}
```

1.9: Divisors of a Factorial

```
vector <ull> vec;
bool isPrime[1000101];

void sieve() {
   int MAX = 1000100, sq = sqrt(MAX);
   memset(isPrime, true, sizeof isPrime);
   for(int i = 4; i <= MAX; i += 2) {
      isPrime[i] = 0;
   }
   for(int i = 3; i <= sq; i += 2) {
      if(isPrime[i]) {
        for(int j = i * i; j <= MAX; j += i) {</pre>
```

```
isPrime[j] = 0;
            }
        }
    }
    isPrime[1] = 0;
    isPrime[0] = 0;
    for(int p = 2; p < MAX; p++) {
        if(isPrime[p]) {
            vec.push_back(p);
        }
    }
}
ull factorialDivisors(ull n) {
    ull res = 1;
    for(ull x : vec) {
        ull p = x;
        ull exp = 0;
        while(p <= n) {
            exp = exp + (n / p);
            p = p * x;
        res = res * (exp + 1);
    }
    return res;
}
int main() {
    sieve();
    cout << factorialDivisors(6) << endl;</pre>
    return 0;
}
```

1.10: Bitwise Sieve

```
#include <bits/stdc++.h>
using namespace std;

bool Check(int n, int pos) {
    return (bool)(n & (1 << pos));
}</pre>
```

```
void Set(int &n, int pos) {
    n = n \mid (1 << pos);
}
const int Max = 1e8 + 5;
int prime[(Max >> 5) + 2];
vector <int> primes;
void sieve() {
    int lim = sqrt(Max);
    for(int i = 3; i <= lim; i += 2) {
        if(!Check(prime[i >> 5], i & 31)) {
            for(int j = i * i; j <= Max; j += (i << 1)) {
                Set(prime[j >> 5], j & 31);
            }
        }
    }
    primes.push_back(2);
    for(int i = 3; i \leftarrow Max; i += 2) {
        if(!Check(prime[i >> 5], i & 31)) {
            primes.push_back(i);
        }
    }
}
int main() {
    sieve();
    return 0;
}
```

1.11: Miller Rabin Primality Test

```
inline bool miller(ll p, int iter = 20) {
   if(p == 3 || p == 2 || p == 5) {
      return true;
   }
   if(p % 2 == 0) {
      return false;
   }
   if(p < 3) {
      return false;
   }
   mt19937_64 rnd(chrono::steady_clock::now().time_since_epoch().count());
   for(int i = 0; i < iter; i++) {
      ll a = (rnd()) % (p - 4) + 2;
   }
}</pre>
```

```
ll s = p - 1;
        while(s \% 2 == 0) {
            s /= 2;
        }
        11 mod = bigmod(a, s, p);
        if(mod == 1 || mod == p - 1) {
            continue;
        }
        bool flag = 0;
        s *= 2;
        while(s != p - 1) {
            mod = mulmod(mod, mod, p);
            if(mod == p - 1) {
                flag = 1;
                break;
            }
            s *= 2;
        }
        if(flag == 0) {
           return 0;
        }
    }
    return 1;
}
```

Part 2 ⇒ Data Structure

2.1: Merge Sort Tree

```
vector <int> tree[4 * Max];
int ar[Max];
int inp[Max];
void build(int node, int 1, int r) {
    if(1 == r) {
        tree[node].push_back(ar[1]);
        return;
    }
    int mid = (1 + r) >> 1;
    int lf = node * 2;
    int rt = node * 2 + 1;
    build(lf, 1, mid);
    build(rt, mid + 1, r);
    merge(tree[lf].begin(), tree[lf].end(), tree[rt].begin(), tree[rt].end(),
back_inserter(tree[node]));
}
int query(int node, int 1, int r, int L, int R, int val) {
    if(L > r || 1 > R) {
        return 0;
    }
    if(L <= 1 \&\& r <= R) {
        return lower_bound(tree[node].begin(), tree[node].end(), val) -
tree[node].begin();
    int mid = (1 + r) >> 1;
    int lf = node * 2;
    int rt = node * 2 + 1;
    int u = query(lf, 1, mid, L, R, val);
    int v = query(rt, mid + 1, r, L, R, val);
    return u + v;
}
```

2.2: MO's Algorithm

```
const int Max = 1e5 + 10;
int BLOCK_SIZE, cnt;
int mp[Max];
int ar[Max];
int ans[Max];
```

```
struct Node {
    int l, r, id;
   Node() {};
   Node(int l_, int r_, int id_) {
        1 = 1_{;}
        r = r_{;}
        id = id_;
    }
    bool operator<(const Node &b) const {</pre>
        int block_a = 1 / BLOCK_SIZE;
        int block_b = b.1 / BLOCK_SIZE;
        if(block_a != block_b) {
            return block_a < block_b;</pre>
        }
        return r < b.r;
    }
} qr[Max];
void add(int x) {
void del(int x) {
}
int main() {
    int n, m, l, r;
    scanf("%d %d", &n, &m);
    BLOCK_SIZE = sqrt(n);
   memset(mp, 0, sizeof mp);
    cnt = 0;
    for(int i = 1; i <= n; i++) {
        scanf("%d", &ar[i]);
    }
    for(int i = 1; i <= m; i++) {
        scanf("%d %d", &l, &r);
        qr[i] = Node(l, r, i);
    }
   sort(qr + 1, qr + m + 1);
    int L = 1, R = 0;
```

```
for(int i = 1; i <= m; i++) {
        int l = qr[i].l;
        int r = qr[i].r;
        while(R < r) {
            R++;
            add(ar[R]);
        }
        while(R > r) {
            del(ar[R]);
            R--;
        }
        while(L < 1) {
            del(ar[L]);
            L++;
        }
        while(L > 1) {
            L--;
            add(ar[L]);
        }
        ans[qr[i].id] = cnt;
    }
    for(int i = 1; i <= m; i++) {
        printf("%lld\n", ans[i]);
    return 0;
}
```

2.3: Segment Tree

```
const int Max = 1e5 + 10;
int ar[Max];
int seg[Max * 4];

void build(int node, int 1, int r) {
    if(1 == r) {
        seg[node] = ar[1];
        return;
    }
    int mid = (1 + r) >> 1;
    int lf = node * 2;
    int rt = node * 2 + 1;
    build(lf, 1, mid);
```

```
build(rt, mid + 1, r);
    seg[node] = seg[lf] + seg[rt];
}
int update(int node, int 1, int r, int idx, int val) {
    if(1 == r) {
        seg[node] = val;
        return seg[node];
    }
    int mid = (1 + r) >> 1, u = seg[node * 2], v = seg[node * 2 + 1];
    if(mid >= idx) {
        u = update(2 * node, 1, mid, idx, val);
    }
    else {
       v = update(2 * node + 1, mid + 1, r, idx, val);
    return seg[node] = u + v;
}
int query(int node, int 1, int r, int L, int R) {
    if(R < 1 || L > r) {
        return 0;
    if(L <= 1 && r <= R) {
        return seg[node];
    }
    int mid = (1 + r) >> 1;
    int u = query(node * 2, 1, mid, L, R);
    int v = query(node * 2 + 1, mid + 1, r, L, R);
    return u + v;
}
```

2.4: Sqrt Decomposition

```
const int Max = 1e5 + 10;

ll BLOCK_SIZE;
ll BLOCK[1001];
ll ar[100001];

ll getID(ll idx) {
    ll id = idx / BLOCK_SIZE;
    return id;
}

ll calc() {
    for(int i = 1; i < 1000; i++) {</pre>
```

```
BLOCK[i] = 0;
    }
}
void del(int idx) {
    int id = getID(idx);
    BLOCK[id] -= ar[idx];
    ar[idx] = 0;
}
void add(int idx, ll val) {
    int id = getID(idx);
    BLOCK[id] += val;
}
11 query(int 1, int r) {
    int lf = getID(1);
    int rt = getID(r);
    11 ret = 0;
    if(lf == rt) {
        for(int i = 1; i <= r; i++) {
            ret += ar[i];
        return ret;
    }
    for(int i = 1; i < (lf + 1) * BLOCK_SIZE; i++) {</pre>
        ret += ar[i];
    }
    for(int i = lf + 1; i < rt; i++) {
        ret += BLOCK[i];
    }
    for(int i = rt * BLOCK_SIZE; i <= r; i++) {</pre>
        ret += ar[i];
    }
    return ret;
}
int main() {
    int t, n, m;
    scanf("%d", &t);
    int tc = 1;
   while(t--) {
```

```
scanf("%d %d", &n, &m);
        BLOCK_SIZE = sqrt(n);
        calc();
        for(int i = 1; i <= n; i++) {
            scanf("%lld", &ar[i]);
            add(i, ar[i]);
        }
        printf("Case %d:\n", tc++);
        int type, l, r, val;
        while(m--) {
            scanf("%d", &type);
            if(type == 1) {
                scanf("%d", &1);
                1++;
                printf("%lld\n", ar[1]);
                del(1);
            }
            else if(type == 2) {
                scanf("%d %d", &l, &val);
                1++;
                add(1, val);
                ar[1] += val;
            }
            else {
                scanf("%d %d", &l, &r);
                1++;
                r++;
                printf("%lld\n", query(l, r));
            }
        }
    }
    return 0;
}
```

2.5: Disjoint Set

```
int par[Max];
int cnt[Max];
int rnk[Max];

void make_set() {
    for(int i = 0; i < n; i++) {
        par[i] = i;
        cnt[i] = 1;
}</pre>
```

```
rnk[i] = 0;
    }
}
int find_rep(int x) {
    if(x != par[x]) {
        par[x] = find_rep(par[x]);
    return par[x];
}
int union_(int u, int v) {
    if((u = find_rep(u)) != (v = find_rep(v))) {
        if(rnk[u] < rnk[v]) {
            cnt[v] += cnt[u];
            par[u] = par[v];
            return cnt[v];
        }
        else {
            rnk[u] = max(rnk[u], rnk[v] + 1);
            cnt[u] += cnt[v];
            par[v] = par[u];
        }
    }
    return cnt[u];
}
```

2.6: Range Minimum Query Using Sparse Table

```
const int Max = 1e5;
int ar[Max];
int tr[Max][18];
int n;
void Read() {
   for(int i = 0; i < n; i++) {
        scanf("%d", &ar[i]);
    }
}
void Build() {
   for(int i = 0; i < n; i++) {
        tr[i][0] = ar[i];
    for(int j = 1; (1 << j) <= n; j++) {
        for(int i = 0; i + (1 << j) - 1 < n; i++) {
            tr[i][j] = max(tr[i][j - 1], tr[i + (1 << (j - 1))][j - 1]);
        }
```

```
}
}
int Query(int 1, int r) {
   int k = log2(r - 1 + 1);
   return max(tr[1][k], tr[r - (1 << k) + 1][k]);
}</pre>
```

2.7: Binary Indexed Tree

```
const int Max = 1e5 + 10;
int ar[Max], n;
11 BIT[Max];
void update(int idx, int val) {
   while(idx <= n) {
        BIT[idx] += val;
        idx += idx \& -idx;
    }
}
ll query(int idx) {
    11 \text{ ret} = 0;
   while(idx > 0) {
        ret += BIT[idx];
        idx -= idx & -idx;
    }
    return ret;
}
11 query(int 1, int r) {
    return query(r) - query(l - 1);
}
void build() {
    for(int i = 1; i <= n; i++) {
        update(i, ar[i]);
    }
}
int main() {
    int q, 1, r;
    scanf("%d %d", &n, &q);
    for(int i = 1; i <= n; i++) {
        scanf("%d", &ar[i]);
    }
```

```
build();
while(q--) {
    scanf("%d %d", &l, &r);
    printf("%lld\n", query(l, r));
}
return 0;
}
```

2.8: Lazy Propagation

```
const int Max = 1e5 + 10;
11 ar[Max];
struct Node {
    11 prop, sum;
} seg[Max * 4];
void build(ll node, ll l, ll r) {
    if(1 == r) {
        seg[node].sum = ar[1];
        return;
    }
    11 1f = node * 2;
    11 rt = node * 2 + 1;
    11 \text{ mid} = (1 + r) / 2;
    build(lf, 1, mid);
    build(rt, mid + 1, r);
    seg[node].sum = seg[lf].sum + seg[rt].sum;
    seg[node].prop = 0;
}
11 query(11 node, 11 1, 11 r, 11 L, 11 R, 11 cary = 0) {
    if(L > r || R < 1) {
        return 0;
    }
    if(1 >= L and r <= R) {
        return seg[node].sum + cary * (r - 1 + 1);
    }
    11 1f = node << 1;</pre>
    11 \text{ rt} = (\text{node} << 1) + 1;
    11 \text{ mid} = (1 + r) >> 1;
    11 u = query(1f, 1, mid, L, R, cary + seg[node].prop);
    11 v = query(rt, mid + 1, r, L, R, cary + seg[node].prop);
```

```
return u + v;
}
void update(ll node, ll l, ll r, ll L, ll R, ll val) {
    if(L > r || R < 1) {
        return;
    if(1 >= L \&\& r <= R) {
        seg[node].sum += ((r - l + 1) * val);
        seg[node].prop += val;
        return;
    }
    11 1f = node * 2;
    11 \text{ rt} = (\text{node} * 2) + 1;
    11 \text{ mid} = (1 + r) / 2;
    update(lf, l, mid, L, R, val);
    update(rt, mid + 1, r, L, R, val);
    seg[node].sum = seg[lf].sum + seg[rt].sum + (r - l + 1) * seg[node].prop;
}
```

2.9: Kth Element in Segment

```
int findkth(int node, int 1, int r, int k) {
    if(1 >= r) {
        return 1;
    }

    int mid = (1 + r) >> 1;

    if(seg[node * 2] >= k) {
        return findkth(node * 2, 1, mid, k);
    }
    else {
        return findkth(node * 2 + 1, mid + 1, r, k - seg[node * 2]);
    }
}
```

2.10: Lowest Common Ancestor

```
int L[Max];
int P[Max][22];
int T[Max];
vector <int> G[Max];
```

```
void dfs(int u, int par, int dep) {
    T[u] = par;
    L[u] = dep;
    for(int v : G[u]) {
        if(v == par) {
            continue;
        }
        dfs(v, u, dep + 1);
    }
}
int lca_query(int p, int q) {
    if(L[p] < L[q]) {
        swap(p, q);
    }
    int lg = 1;
   while(1) {
        int nxt = lg + 1;
        if((1 << nxt) > L[p]) {
            break;
        }
        lg++;
    for(int i = lg; i >= 0; i--) {
        if(L[p] - (1 << i) >= L[q]) {
            p = P[p][i];
        }
    }
    if(p == q) {
        return p;
    for(int i = lg; i >= 0; i--) {
        if(P[p][i] != -1 && P[p][i] != P[q][i]) {
            p = P[p][i], q = P[q][i];
        }
    return T[p];
}
void lca_init(int n) {
    memset(P, -1, sizeof(P));
    for(int i = 0; i < n; i++) {
        P[i][0] = T[i];
    }
   for(int j = 1; 1 << j < n; j++) {
```

```
for(int i = 0; i < n; i++) {
            if(P[i][j - 1] != -1) {
                P[i][j] = P[P[i][j - 1]][j - 1];
            }
        }
    }
}
int main() {
    int n, u, v, q;
    scanf("%d", &n);
    for(int i = 1; i < n; i++) {
        scanf("%d %d", &u, &v);
        G[u].push_back(v);
        G[v].push_back(u);
    }
    dfs(0, 0, 0);
    lca_init(n);
    scanf("%d", &q);
   while(q--) {
        scanf("%d %d", &u, &v);
        printf("%d\n", lca_query(u, v));
    return 0;
}
    Be careful about indexing for lca_init()
2.10: BIT in Grid
int BIT[Max][Max];
void update(int x, int y) {
    for(int i = x; i < Max; i += i & -i) {
        for(int j = y; j < Max; j += j & -j) {
            BIT[i][j]++;
        }
    }
}
int query(int x, int y) {
    int ret = 0;
```

for(int i = x; i > 0; i -= i & -i) {

```
for(int j = y; j > 0; j -= j & -j) {
     ret += BIT[i][j];
   }
}
return ret;
}
```

2.11: Next Greater Element

```
// O(n)
vector<int> nextGreaterElement(vector<int> &arr) {
    int n = arr.size();
    stack<int> s;
    vector<int> ret(n + 1, n);
    for(int i = n - 1; i >= 0; i--) {
        while(!s.empty() && arr[s.top()] <= arr[i]) {</pre>
            s.pop();
        }
        if(!s.empty()) {
            ret[i] = s.top();
        }
        s.push(i);
    }
    return ret;
}
```

2.12: Sliding RMQ

```
//O(n)
vector<int> slidingRMQ(vector<int> &arr, int k) {
    vector<int> ret(arr.size(), 1e9); // ret[i] = minimum of arr[i, i+k-1]
    deque<int> Q;

for(int i = 0; i < arr.size(); i++) {
    while(!Q.empty() && Q.back() > arr[i]) {
        Q.pop_back();
    }

    Q.push_back(arr[i]);
```

```
if(i >= k && arr[i - k] == Q.front()) {
        Q.pop_front();
}

if(i >= k - 1) {
        ret[i - k + 1] = Q.front();
    }
} return ret;
}
```

2.13: Heavy Light Decomposition

```
#include <bits/stdc++.h>
using namespace std;
typedef long long int 11;
typedef pair <ll, 11> pll;
const int Max = 3e4 + 10;
const int Mod = 1e9 + 7;
const 11 Inf = 1LL << 62;</pre>
vector <int> G[Max];
int ar[Max];
int inp[Max];
int seg[Max * 6];
int cur, chainNo, pos[Max];
int L[Max];
int P[Max][22];
int T[Max];
int sub[Max];
int chainInd[Max];
int chainHead[Max];
void build(int node, int 1, int r) {
    if(1 == r) {
        seg[node] = ar[1];
        return;
    int mid = (1 + r) >> 1;
    int lf = node * 2;
    int rt = lf + 1;
    build(lf, 1, mid);
    build(rt, mid + 1, r);
    seg[node] = seg[lf] + seg[rt];
}
```

```
int update(int node, int l, int r, int idx, int val) {
    if(1 == r) {
        seg[node] = val;
       return seg[node];
    int mid = (1 + r) >> 1, u = seg[node * 2], v = seg[node * 2 + 1];
    if(mid >= idx) {
        u = update(2 * node, 1, mid, idx, val);
    }
    else {
       v = update(2 * node + 1, mid + 1, r, idx, val);
    return seg[node] = u + v;
}
int query(int node, int 1, int r, int L, int R) {
    if(R < 1 || L > r) {
        return 0;
    }
    if(L <= 1 && r <= R) {
        return seg[node];
    }
    int mid = (1 + r) >> 1;
    int u = query(node * 2, 1, mid, L, R);
    int v = query(node * 2 + 1, mid + 1, r, L, R);
    return u + v;
}
int query_up(int u, int v) {
    int uchain;
    int vchain = chainInd[v];
    int ans = 0;
   while(true) {
        uchain = chainInd[u];
        if(uchain == vchain) {
            ans += query(1, 0, cur - 1, pos[v], pos[u]);
            break;
        ans += query(1, 0, cur - 1, pos[chainHead[uchain]], pos[u]);
        u = chainHead[uchain];
        u = P[u][0];
    }
    return ans;
}
int lca_query(int p, int q) {
```

```
}
void lca_init(int n) {
}
int query(int u, int v) {
    int lca = lca_query(u, v);
    return query_up(u, lca) + query_up(v, lca) - ar[pos[lca]];
}
void update(int idx, int val) {
    ar[pos[idx]] = val;
    update(1, 0, cur - 1, pos[idx], val);
}
void HLD(int u, int prev) {
    if(chainHead[chainNo] == -1) {
        chainHead[chainNo] = u;
    }
    chainInd[u] = chainNo;
    pos[u] = cur;
    ar[cur++] = inp[u];
    int sc = -1, mx = -1;
    for(int i = 0; i < G[u].size(); i++) {</pre>
        int v = G[u][i];
        if(prev == v) {
            continue;
        }
        if(sub[v] > mx) {
            mx = sub[v];
            sc = v;
        }
    }
    if(sc != -1) {
        HLD(sc, u);
    for(int i = 0; i < G[u].size(); i++) {</pre>
        int v = G[u][i];
        if(v != prev && v != sc) {
            chainNo++;
            HLD(v, u);
        }
    }
}
void dfs(int u, int par, int dep) {
    T[u] = par;
```

```
L[u] = dep;
    sub[u] = 1;
    for(int i = 0; i < G[u].size(); i++) {</pre>
        int v = G[u][i];
        if(v == par) {
            continue;
        }
        dfs(v, u, dep + 1);
        sub[u] += sub[v];
    }
}
void Clear() {
    for(int i = 0; i < Max; i++) {
        G[i].clear();
    }
    cur = chainNo = 0;
    memset(chainHead, -1, sizeof chainHead);
}
int main() {
#ifdef Mr_Emrul
    freopen("inputf.in", "r", stdin);
#endif /// Mr Emrul
    int t, n, q, u, v, ty, idx, val;
    scanf("%d", &t);
    for(int tc = 1; tc <= t; tc++) {
        Clear();
        scanf("%d", &n);
        for(int i = 0; i < n; i++) {
            scanf("%d", &inp[i]);
        }
        for(int i = 1; i < n; i++) {
            scanf("%d %d", &u, &v);
            G[u].push_back(v);
            G[v].push_back(u);
        }
        dfs(0, -1, 0);
        HLD(0, -1);
        lca_init(n);
        build(1, 0, cur - 1);
        printf("Case %d:\n", tc);
        scanf("%d", &q);
        while(q--) {
            scanf("%d", &ty);
            if(ty == 0) {
                scanf("%d %d", &u, &v);
```

```
printf("%d\n", query(u, v));
            }
            else {
                scanf("%d %d", &idx, &val);
                update(idx, val);
            }
        }
    }
    return 0;
}
2.14: Trie
struct Node {
      bool endmark;
      int cnt;
      Node *nxt[26 + 1];
      Node() {
            endmark = false;
            cnt = 0;
            for(int i = 0; i < 26; i++) {
                   nxt[i] = NULL;
            }
      }
} *root;
void insert(char *str, int len) {
      Node *cur = root;
      for(int i = 0; i < len; i++) {
            int id = str[i] - 'a';
            if(cur->nxt[id] == NULL) {
                   cur->nxt[id] = new Node();
            }
            cur = cur->nxt[id];
            cur->cnt++;
      cur->endmark = true;
}
bool search(char *str, int len) {
      Node *cur = root;
      for(int i = 0; i < len; i++) {
            int id = str[i] - 'a';
            if(cur->nxt[id] == NULL) {
                   return false;
```

}

```
cur = cur->nxt[id];
      }
      return cur->endmark;
}
int query(char *str, int len) {
      int ans = 0;
      Node *cur = root;
      for(int i = 0; i < len; i++) {
            int id = str[i] - 'a';
            if(cur->nxt[id] == NULL) {
                   return false;
            }
            cur = cur->nxt[id];
            ans = max(ans, (i + 1) * cur->cnt);
      }
      return ans;
}
void del(Node *cur) {
      for(int i = 0; i < 26; i++) {
            if(cur->nxt[i]) {
                   del(cur->nxt[i]);
            }
      delete(cur);
}
```

2.15: 2D Segment Tree

```
const int Max = 2001;
int seg[4 * Max][4 * Max], n, m, ar[Max][Max];

void buildY(int ndx, int lx, int rx, int ndy, int ly, int ry) {
    if(ly == ry) {
        if(lx == rx) {
            seg[ndx][ndy] = ar[lx][ly];
        }
        else {
            seg[ndx][ndy] = seg[ndx * 2][ndy] + seg[ndx * 2 + 1][ndy];
        }
        return;
    }
    int mid = ly + ry >> 1;
    buildY(ndx, lx, rx, ndy * 2, ly, mid);
    buildY(ndx, lx, rx, ndy * 2 + 1, mid + 1, ry);
```

```
seg[ndx][ndy] = seg[ndx][ndy * 2] + seg[ndx][ndy * 2 + 1];
}
void buildX(int ndx, int lx, int rx) {
    if(lx != rx) {
        int mid = lx + rx >> 1;
        buildX(ndx * 2, lx, mid);
        buildX(ndx * 2 + 1, mid + 1, rx);
    }
    buildY(ndx, lx, rx, 1, 0, m - 1);
}
void updateY(int ndx, int lx, int rx, int ndy, int ly, int ry, int y, int val)
{
    if(ly == ry) {
        if(lx == rx) {
            seg[ndx][ndy] = val;
        }
        else {
            seg[ndx][ndy] = seg[ndx * 2][ndy] + seg[ndx * 2 + 1][ndy];
        return;
    }
    int mid = ly + ry >> 1;
    if(y <= mid) {
        updateY(ndx, lx, rx, ndy * 2, ly, mid, y, val);
    }
    else {
        updateY(ndx, lx, rx, ndy * 2 + 1, mid + 1, ry, y, val);
    seg[ndx][ndy] = seg[ndx][ndy * 2] + seg[ndx][ndy * 2 + 1];
}
void updateX(int ndx, int lx, int rx, int x, int y, int val) {
    if(lx != rx) {
        int mid = lx + rx >> 1;
        if(x <= mid) {
            updateX(ndx * 2, lx, mid, x, y, val);
        }
        else {
            updateX(ndx * 2 + 1, mid + 1, rx, x, y, val);
        }
    updateY(ndx, lx, rx, 1, 0, m - 1, y, val);
}
int queryY(int ndx, int ndy, int ly, int ry, int y1, int y2) {
    if(ry < y1 || 1y > y2) {
```

```
return 0;
    }
    if(y1 <= ly && ry <= y2) {
        return seg[ndx][ndy];
    }
    int mid = ly + ry >> 1;
    return queryY(ndx, ndy * 2, ly, mid, y1, y2) +
           queryY(ndx, ndy * 2 + 1, mid + 1, ry, y1, y2);
}
int queryX(int ndx, int lx, int rx, int x1, int y1, int x2, int y2) {
    if(rx < x1 || 1x > x2) {
        return 0;
    if(x1 \le 1x \&\& rx \le x2) {
        return queryY(ndx, 1, 0, m - 1, y1, y2);
    }
    int mid = lx + rx >> 1;
    return queryX(ndx * 2, 1x, mid, x1, y1, x2, y2) +
           queryX(ndx * 2 + 1, mid + 1, rx, x1, y1, x2, y2);
}
```

2.16: Maximum Histrogram

```
ll histro(vector<ll> &hist) {
    stack <int> st;
    ll res = 0;
    for(int i = 0; i <= hist.size(); i++) {
        ll h = (i == n ? 0 : hist[i]);
        if(st.empty() || h >= hist[st.top()]) {
            st.push(i++);
        }
        else {
            int x = st.top();
            st.pop();
            res = max(res, hist[x] * (st.empty() ? i : i - 1 - st.top()));
        }
    }
    return res;
}
```

2.17: MO's Algo with Update

/*

Tested Problem:

```
You are given an array a. You have to answer the following queries:
        1. You are given two integers 1 and r. Let c[i] be the number of
occurrences of i in a[l: r], where a[l: r] is the subarray of a from l-th
element to r-th inclusive. Find the Mex of \{c[0], c[1], ..., c[10^9]\}
        2. You are given two integers p to x. Change a[p] to x.
The Mex of a multiset of numbers is the smallest non-negative integer not in
the set.
*/
const int Max = 1e5 + 10;
inline void read(int &res) {
    char c;
    while(c = getchar(), c <= ' ');</pre>
    res = c - '0';
   while(c = getchar(), c >= '0' \&\& c <= '9') {
        res = res * 10 + (c - '0');
    }
}
int n, m, ar[Max], prv[Max], ans[Max];
int block, sz;
struct query {
    int l, r, id, t, blcl, blcr;
    query(int _a, int _b, int _c, int _d) {
        1 = _a, r = _b;
        id = _c, t = _d;
        blcl = 1 / block;
        blcr = r / block;
    }
    bool operator < (const query &p) const {</pre>
        if(blcl != p.blcl) {
            return 1 < p.1;
        }
        if(blcr != p.blcr) {
            return r < p.r;
        return t < p.t;
    }
};
vector <query> q;
struct update {
```

```
int pos, pre, now;
};
vector <update> u;
struct MEX {
    int cnt[555], freq[Max * 2];
    MEX() {
        memset(cnt, 0, sizeof cnt);
        memset(freq, 0, sizeof freq);
    void add(int x) {
        if(!freq[x]) {
            ++cnt[x / sz];
        }
        ++freq[x];
    }
    void remove(int x) {
        if(freq[x] == 1) {
            --cnt[x / sz];
        }
        --freq[x];
    }
    int get() {
        for(int i = 0; i <= sz; i++) {
            if(cnt[i] < sz) {</pre>
                for(int j = i * sz, ed = j + sz; j < ed; j++) {
                     if(!freq[j]) {
                         return j;
                     }
                }
            }
        }
    }
} ds;
int 1, r, t;
int cnt[Max * 2];
void add(int x) {
    x = ar[x];
    int &c = cnt[x];
    if(c) {
        ds.remove(c);
    }
    ++c;
    ds.add(c);
}
```

```
void remove(int x) {
    x = ar[x];
    int &c = cnt[x];
   ds.remove(c);
    --c;
    if(c) {
       ds.add(c);
    }
}
void apply(int i, int x) {
    if(1 <= i && i <= r) {
        remove(i);
        ar[i] = x;
        add(i);
    }
    else {
        ar[i] = x;
    }
}
int main() {
   vector <int> v;
    read(n);
    read(m);
    for(int i = 0; i < n; ++i) {
        read(ar[i]);
        v.push_back(ar[i]);
    }
    block = pow(n, 0.667);
    int T[m], L[m], R[m];
    for(int i = 0; i < m; ++i) {
        read(T[i]);
        read(L[i]);
        read(R[i]);
        if(T[i] == 2) {
            v.push_back(R[i]);
        }
    }
    sort(v.begin(), v.end());
    v.erase(unique(v.begin(), v.end());
   map<int, int> mp;
    for(int i = 0; i < v.size(); i++) {
        mp[v[i]] = i + 1;
    }
    for(int i = 0; i < n; i++) {
        ar[i] = prv[i] = mp[ar[i]];
    }
```

```
for(int i = 0; i < m; i++) {
    if(T[i] == 2) {
        R[i] = mp[R[i]];
    }
}
sz = sqrt((double)v.size()) + 2;
u.push_back({-1, -1, -1});
for(int i = 0; i < m; ++i) {
    int t = T[i], l = --L[i], r = R[i];
    if(t == 1) {
        q.push_back(query(l, r, q.size(), u.size() - 1));
    }
    else {
        u.push_back({1, prv[1], r});
        prv[1] = r;
    }
}
sort(q.begin(), q.end());
l = 0, r = -1, t = 0;
ds.add(0);
for(int i = 0; i < q.size(); i++) {
    while(t < q[i].t) {
        ++t, apply(u[t].pos, u[t].now);
    while(t > q[i].t) {
        apply(u[t].pos, u[t].pre), --t;
    }
    while(r < q[i].r) {
        add(++r);
    }
    while(l > q[i].1) {
        add(--1);
    }
    while(r > q[i].r) {
        remove(r--);
    }
    while(l < q[i].l) {
        remove(1++);
    ans[q[i].id] = ds.get();
for(int i = 0; i < q.size(); i++) {
    printf("%d\n", ans[i]);
}
return 0;
```

}

2.18: Persistent Segment Tree

2.18.1: Version in Segment Tree

```
const int Max = 1e5 + 10;
struct Node {
    int 1, r, sum;
} seg[Max * 20];
int root[Max], ar[Max], n, q, idx;
void build(int nd, int 1, int r) {
    if(1 == r) {
        seg[nd].sum = ar[1];
        return;
    int mid = (1 + r) >> 1;
    build(seg[nd].1 = ++idx, 1, mid);
    build(seg[nd].r = ++idx, mid + 1, r);
    seg[nd].sum = seg[seg[nd].1].sum + seg[seg[nd].r].sum;
}
void update(int &nd, int 1, int r, int &i, int &val) {
    seg[++idx] = seg[nd];
    seg[nd = idx].sum += val;
    if(1 == r) {
        return;
    }
    int mid = (1 + r) >> 1;
    if(i <= mid) {
        update(seg[nd].1, 1, mid, i, val);
    }
    else {
        update(seg[nd].r, mid + 1, r, i, val);
    }
}
int query(int nd, int l, int r, int &i, int &j) {
    if(r < i || 1 > j) {
```

```
return 0;
    }
    if(i <= 1 && r <= j) {
        return seg[nd].sum;
    int mid = (1 + r) >> 1;
    return query(seg[nd].l, l, mid, i, j) + query(seg[nd].r, mid + 1, r, i,
j);
}
int main() {
    scanf("%d", &n);
    for(int i = 1; i <= n; i++) {
        scanf("%d", &ar[i]);
    }
    build(root[0], 1, n);
    scanf("%d", &q);
    int ver = 0;
    while(q--) {
        int ty, idx, l, r, pos, v;
        scanf("%d", &ty);
        if(ty == 1) {
            scanf("%d %d %d", &idx, &pos, &v);
            update(root[++ver] = root[idx], 1, n, pos, v);
        }
        else {
            scanf("%d %d %d", &idx, &l, &r);
            printf("%d\n", query(root[idx], 1, n, l, r));
        }
    }
    return 0;
}
```

2.18.2: Less than or k in a Range

```
const int Max = 1e5 + 10;

struct Node {
    int l, r, sum;
} seg[Max * 20];
int root[Max], ar[Max], n, q, idx, M = 1e5; /* M = Number of unique elements
*/

void update(int &nd, int l, int r, int &i) {
    seg[++idx] = seg[nd];
    ++seg[nd = idx].sum;
    if(l == r) {
```

```
return;
    }
    int mid = (1 + r) >> 1;
    if(i <= mid) {
        update(seg[nd].1, 1, mid, i);
    }
   else {
        update(seg[nd].r, mid + 1, r, i);
    }
}
int lesscnt(int a, int b, int l, int r, int k) {
    if(r <= k) {
        return seg[a].sum - seg[b].sum;
    }
    int mid = (1 + r) >> 1;
    if(k <= mid) {
        return lesscnt(seg[a].l, seg[b].l, l, mid, k);
    else return lesscnt(seg[a].1, seg[b].1, 1, mid, k) +
                    lesscnt(seg[a].r, seg[b].r, mid + 1, r, k);
}
void init() {
    seg[0].1 = seg[0].r = seg[0].sum = 0;
    for(int i = 1; i <= n; ++i) {
        update(root[i] = root[i - 1], 0, M, ar[i]);
    }
}
2.18.3: Kth Number in a Range
/// update(), init() is as like as 2.18.1
int kthnum(int a, int b, int l, int r, int k) {
    if(1 == r) {
        return 1;
    int cnt = seg[seg[a].1].sum - seg[seg[b].1].sum;
    int mid = (1 + r) >> 1;
    if(cnt >= k) {
        return kthnum(seg[a].1, seg[b].1, 1, mid, k);
    }
    else {
        return kthnum(seg[a].r, seg[b].r, mid + 1, r, k - cnt);
    }
}
```

Part 3 ⇒ Utilities

3.1: Bit Manipulation

```
11 Set(11 num, 11 pos) {
    return num | (1LL << pos);
}

11 Clear(11 num, 11 pos) {
    return num & ~(1LL << pos);
}

11 Toggle(11 num, 11 pos) {
    return num ^ (1LL << pos);
}

bool Check(11 num, 11 pos) {
    return (bool)(num & (1LL << pos));
}</pre>
```

3.2: Policy Based Data Structure

```
#include <bits/stdc++.h>
#include <ext/pb ds/assoc container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
template <typename T> using
                                 Set = tree<T, null_type,</pre>
                                 less<T>, rb_tree_tag,
                                 tree_order_statistics_node_update>;
Set <int> st;
int main() {
    st.insert(5); //Insert
    st.erase(5); //Delete
    st.insert(1);
    st.insert(2);
    st.insert(9);
    cout << *st.find_by_order(0) << endl; //Find value by rank</pre>
    cout << st.order_of_key(9) << endl; //Find value's rank</pre>
    /* For multiple same element, use pair, store index in second of pair */
    return 0;
}
```

3.3: Direction Array

```
int dx4[] = {0, 0, -1, 1};
int dy4[] = {1, -1, 0, 0};

int dx8[] = {1, 1, 1, 0, 0, -1, -1, -1};
int dy8[] = {1, 0, -1, 1, -1, 1, 0, -1};

int dx_horse[] = {1, 1, -1, -1, 2, 2, -2, -2}
Int dy_horse[] = {2, -2, 2, -2, 1, -1, 1, -1}
```

3.4: Big Integer Template

```
#include <cstdio>
#include <string>
#include <algorithm>
#include <iostream>
using namespace std;
struct Bigint {
 // representations and structures
 string a; // to store the digits
 int sign; // sign = -1 for negative numbers, sign = 1 otherwise
 // constructors
 Bigint() {} // default constructor
 Bigint(string b) {
    (*this) = b; // constructor for string
 }
 // some helpful methods
  int size() { // returns number of digits
    return a.size();
 Bigint inverseSign() { // changes the sign
    sign *= -1;
    return (*this);
 Bigint normalize(int newSign) { // removes leading 0, fixes sign
   for(int i = a.size() - 1; i > 0 && a[i] == '0'; i--) {
     a.erase(a.begin() + i);
    sign = (a.size() == 1 && a[0] == '0') ? 1 : newSign;
   return (*this);
  }
```

```
// assignment operator
 void operator = (string b) { // assigns a string to Bigint
   a = b[0] == '-' ? b.substr(1) : b;
   reverse(a.begin(), a.end());
   this->normalize(b[0] == '-' ? -1 : 1);
 }
 // conditional operators
 bool operator < (const Bigint &b) const { // less than operator</pre>
   if(sign != b.sign) {
     return sign < b.sign;</pre>
   }
   if(a.size() != b.a.size()) {
     return sign == 1 ? a.size() < b.a.size() : a.size() > b.a.size();
   for(int i = a.size() - 1; i >= 0; i--) if(a[i] != b.a[i]) {
       return sign == 1 ? a[i] < b.a[i] : a[i] > b.a[i];
     }
   return false;
 bool operator == (const Bigint &b) const { // operator for equality
   return a == b.a && sign == b.sign;
 }
 // mathematical operators
 Bigint operator + (Bigint b) { // addition operator overloading
   if(sign != b.sign) {
     return (*this) - b.inverseSign();
   }
   Bigint c;
   for(int i = 0, carry = 0; i < a.size() || i < b.size() || carry; <math>i++) {
     carry += (i < a.size() ? a[i] - 48 : 0) + (i < b.a.size() ? b.a[i] - 48</pre>
: 0);
     c.a += (carry % 10 + 48);
     carry /= 10;
   }
   return c.normalize(sign);
 Bigint operator - (Bigint b) { // subtraction operator overloading
   if(sign != b.sign) {
     return (*this) + b.inverseSign();
   }
   int s = sign;
   sign = b.sign = 1;
   if((*this) < b) {
     return ((b - (*this)).inverseSign()).normalize(-s);
   }
```

```
Bigint c;
  for(int i = 0, borrow = 0; i < a.size(); i++) {
    borrow = a[i] - borrow - (i < b.size() ? b.a[i] : 48);
   c.a += borrow >= 0? borrow + 48 : borrow + 58;
   borrow = borrow >= 0 ? 0 : 1;
  }
 return c.normalize(s);
}
Bigint operator * (Bigint b) { // multiplication operator overloading
  Bigint c("0");
 for(int i = 0, k = a[i] - 48; i < a.size(); i++, k = a[i] - 48) {
   while(k--) {
      c = c + b;
                  // ith digit is k, so, we add k times
   b.a.insert(b.a.begin(), '0'); // multiplied by 10
  return c.normalize(sign * b.sign);
Bigint operator / (Bigint b) { // division operator overloading
  if(b.size() == 1 && b.a[0] == '0') {
   b.a[0] /= (b.a[0] - 48);
  Bigint c("0"), d;
  for(int j = 0; j < a.size(); j++) {
    d.a += "0";
  }
  int dSign = sign * b.sign;
  b.sign = 1;
 for(int i = a.size() - 1; i >= 0; i--) {
   c.a.insert(c.a.begin(), '0');
   c = c + a.substr(i, 1);
   while(!(c < b)) {
      c = c - b, d.a[i]++;
   }
  }
  return d.normalize(dSign);
Bigint operator % (Bigint b) { // modulo operator overloading
  if(b.size() == 1 && b.a[0] == '0') {
    b.a[0] /= (b.a[0] - 48);
  }
  Bigint c("0");
  b.sign = 1;
 for(int i = a.size() - 1; i >= 0; i--) {
   c.a.insert(c.a.begin(), '0');
   c = c + a.substr(i, 1);
   while(!(c < b)) {
      c = c - b;
```

```
}
   }
   return c.normalize(sign);
 }
 // output method
 void print() {
   if(sign == -1) {
     putchar('-');
   for(int i = a.size() - 1; i >= 0; i--) {
     putchar(a[i]);
   }
 }
};
int main() {
   Bigint a, b, c; // declared some Bigint variables
   // taking Bigint input //
   string input; // string to take input
   cin >> input; // take the Big integer as string
   a = input; // assign the string to Bigint a
   cin >> input; // take the Big integer as string
   b = input; // assign the string to Bigint b
   // Using mathematical operators //
   c = a + b; // adding a and b
   c.print(); // printing the Bigint
   puts(""); // newline
   c = a - b; // subtracting b from a
   c.print(); // printing the Bigint
   puts(""); // newline
   c = a * b; // multiplying a and b
   c.print(); // printing the Bigint
   puts(""); // newline
   c = a / b; // dividing a by b
   c.print(); // printing the Bigint
```

```
puts(""); // newline
   c = a \% b; // a modulo b
   c.print(); // printing the Bigint
   puts(""); // newline
   // Using conditional operators //
   if(a == b) {
      puts("equal"); // checking equality
   }
   else {
      puts("not equal");
   }
   if(a < b) {
      puts("a is smaller than b"); // checking less than operator
   }
   return 0;
}
```

3.4: Character Wise I/O Method

```
#define gc getchar_unlocked
#define pc putchar_unlocked
inline void Cin(int &num) {
    num = 0;
    char c = gc();
    int flag = 0;
   while(!((c >= '0' & c <= '9') || c == '-')) {
        c = gc();
    }
    if(c == '-') {
        flag = 1;
        c = gc();
    }
   while(c >= '0' && c <= '9') \{
        num = (num << 1) + (num << 3) + c - '0';
        c = gc();
```

```
}
    if(flag == 1) {
        num = 0 - num;
    }
}
inline void Cout(int n) {
    int NN = n, rev, count = 0;
    rev = NN;
    if(NN == 0) {
        pc('0');
        return;
   while((rev % 10) == 0) {
        count++;
        rev /= 10;
    }
    rev = 0;
   while(NN != 0) {
        rev = (rev << 3) + (rev << 1) + NN % 10;
        NN /= 10;
   while(rev != 0) {
        pc(rev % 10 + '0');
        rev /= 10;
   while(count--) {
        pc('0');
    }
}
```

Part 4 ⇒ String

4.1: Hashing

```
const int base = 331;
const int Max = 2e6 + 10;
const int Mod = 1e9 + 7;
const ll Inf = 1LL << 62;</pre>
11 pw[Max];
11 Hash[Max];
void pre_power() {
    pw[0] = 1;
    for(int i = 1; i < Max; i++) {</pre>
        pw[i] = (pw[i - 1] * base) % Mod;
    }
}
void Hashing(string str, int len) {
    11 \text{ hash val} = 0;
    for(int i = 0; i < len; i++) {
        hash_val = (hash_val * base + str[i]) % Mod;
        Hash[i + 1] = hash_val;
    }
}
11 SubstringHash(int 1, int r) {
    return (Hash[r] - (Hash[l - 1] * pw[r - l + 1]) % Mod + Mod) % Mod;
}
```

4.2: Z Algorithm

```
}
                   Z[i] = R - L;
                   R--;
             }
             else {
                   k = i - L;
                   if(Z[k] < R - i + 1) {
                          Z[i] = Z[k];
                    }
                   else {
                          L = i;
                          while(R < n \&\& S[R - L] == S[R]) {
                                 R++;
                          Z[i] = R - L;
                          R--;
                   }
             }
      }
}
int main() {
    scanf("%s", S);
    compute z function(strlen(S));
    for(int i = 0; i < strlen(S); i++) {</pre>
        printf("%d ", Z[i]);
    return 0;
}
```

4.3: KMP

```
int kmp(const string &T, const string &P) {
    if (P.empty()) return 0;

vector<int> pi(P.size(), 0);
for (int i = 1, k = 0; i < P.size(); ++i) {
      while (k && P[k] != P[i]) k = pi[k - 1];
      if (P[k] == P[i]) ++k;
      pi[i] = k;
}

for (int i = 0, k = 0; i < T.size(); ++i) {
      while (k && P[k] != T[i]) k = pi[k - 1];
      if (P[k] == T[i]) ++k;
      if (k == P.size()) return i - k + 1;</pre>
```

```
}
return -1;
}
```

4.4: Suffix Array

```
const int Max = 1e5 + 10;
char str[Max];
int n, len;
int sa[Max], pos[Max], tmp[Max], lcp[Max];
bool sufCmp(int i, int j) {
    if(pos[i] != pos[j]) {
        return pos[i] < pos[j];</pre>
    }
    i += len;
    j += len;
    return (i < n \&\& j < n) ? pos[i] < pos[j] : i > j;
}
void buildSA() {
    memset(sa, 0, sizeof sa);
    memset(pos, 0, sizeof pos);
    memset(lcp, 0, sizeof lcp);
    memset(tmp, 0, sizeof tmp);
    n = strlen(str);
    for(int i = 0; i < n; i++) {
        sa[i] = i, pos[i] = str[i];
    }
    for(len = 1;; len *= 2) {
        sort(sa, sa + n, sufCmp);
        for(int i = 0; i < n - 1; i++) {
            tmp[i + 1] = tmp[i] + sufCmp(sa[i], sa[i + 1]);
        for(int i = 0; i < n; i++) {
            pos[sa[i]] = tmp[i];
        }
        if(tmp[n - 1] == n - 1) {
            break;
        }
    }
}
```

```
void buildLCP() {
    for(int i = 0, k = 0; i < n; i++) {
        if(pos[i] != n - 1) {
            for(int j = sa[pos[i] + 1]; str[i + k] == str[j + k];) {
                k++;
            }
            lcp[pos[i]] = k;
            if(k) {
                k--;
            }
        }
    for(int i = n - 1; i > 0; i--) {
        lcp[i] = lcp[i - 1];
    }
    lcp[0] = 0;
}
```

4.5: Aho Corasick Algorithm

```
/*
   Algo: Given a string inp and some pattern strings s[i], Count of s[i] for
every i as substring in inp
*/
#include <bits/stdc++.h>
using namespace std;
const int sz = 1e6 + 10;
const int Max = 505 * 505 + 100;
char inp[sz], s[505][505];
int cnt[505];
struct AhoCorasick {
    vector < int > mark[Max + 7];
    int state, failure[Max + 7];
    int trie[Max + 7][26];
   AhoCorasick() {
        init();
    }
   void init() {
        mark[0].clear();
        fill(trie[0], trie[0] + 26, -1);
        state = 0;
```

```
}
int value(char c) {
    return c - 'a';
}
/*
    Adding s[t] in trie
*/
void add(char *s, int t) {
    int root = 0, id;
    for(int i = 0; s[i]; i++) {
        id = value(s[i]);
        if(trie[root][id] == -1) {
            trie[root][id] = ++state;
            mark[state].clear();
            fill(trie[state], trie[state + 1] + 26, - 1);
        }
        root = trie[root][id];
    }
    mark[root].push_back(t);
}
/*
    Failure function
*/
void computeFailure() {
    queue < int > Q;
    failure[0] = 0;
    for(int i = 0; i < 26; i++) {
        if(trie[0][i] != -1) {
            failure[trie[0][i]] = 0;
            Q.push(trie[0][i]);
        }
        else {
            trie[0][i] = 0;
        }
    while(!Q.empty()) {
        int u = Q.front();
        Q.pop();
        for(int v : mark[failure[u]]) {
            mark[u].push_back(v);
        for(int i = 0; i < 26; i++) {
            if(trie[u][i] != -1) {
                failure[trie[u][i]] = trie[failure[u]][i];
                Q.push(trie[u][i]);
```

```
}
                else {
                    trie[u][i] = trie[failure[u]][i];
                }
            }
        }
    }
} automata;
void countFreq() {
    for(int i = 0, root = 0, id; inp[i]; i++) {
        id = automata.value(inp[i]);
        root = automata.trie[root][id];
        if(root == 0) {
            continue;
        }
        for(int v : automata.mark[root]) {
            cnt[v]++;
        }
    }
}
int main() {
    int t, n, m;
    scanf("%d", &t);
    for(int tc = 1; tc <= t; tc++) {
        scanf("%d", &n);
        scanf("%s", inp);
        automata.init();
        memset(cnt, 0, sizeof cnt);
        for(int i = 0; i < n; i++) {
            scanf("%s", s[i]);
            automata.add(s[i], i);
        }
        automata.computeFailure();
        countFreq();
        printf("Case %d:\n", tc);
        for(int i = 0; i < n; i++) {
            printf("%d\n", cnt[i]);
        }
    }
}
```

4.6: Palindrome Tree

```
Palindrome tree. Useful structure to deal with palindromes in strings.
O(N)
   This code counts number of palindrome substrings of the string.
#include <bits/stdc++.h>
using namespace std;
const int Max = 105000;
struct node {
    int next[26];
    int len;
    int sufflink;
    int num;
};
int len;
char s[Max];
node tree[Max];
int num;
                  // node 1 - root with len -1, node 2 - root with len 0
int suff;
                  // max suffix palindrome
long long ans;
bool addLetter(int pos) {
    int cur = suff, curlen = 0;
    int let = s[pos] - 'a';
   while(true) {
        curlen = tree[cur].len;
        if(pos - 1 - curlen) = 0 \& s[pos - 1 - curlen] == s[pos]) {
            break;
        }
        cur = tree[cur].sufflink;
    if(tree[cur].next[let]) {
        suff = tree[cur].next[let];
        return false;
    }
    num++;
    suff = num;
   tree[num].len = tree[cur].len + 2;
   tree[cur].next[let] = num;
```

```
if(tree[num].len == 1) {
        tree[num].sufflink = 2;
        tree[num].num = 1;
        return true;
    }
   while(true) {
        cur = tree[cur].sufflink;
        curlen = tree[cur].len;
        if(pos - 1 - curlen) = 0 && s[pos - 1 - curlen] == s[pos]) {
            tree[num].sufflink = tree[cur].next[let];
            break;
        }
    }
    tree[num].num = 1 + tree[tree[num].sufflink].num;
    return true;
}
void initTree() {
    num = 2;
    suff = 2;
    tree[1].len = -1;
    tree[1].sufflink = 1;
   tree[2].len = 0;
   tree[2].sufflink = 1;
}
int main() {
    scanf("%s", s);
    len = strlen(s);
    initTree();
    for(int i = 0; i < len; i++) {
        addLetter(i);
        ans += tree[suff].num;
    printf("%lld\n", ans);
    return 0;
}
```


5.1: Geometry formulas

5.1.1: Perimeter

Perimeter of a square: s + s + s + s + s s:length of one side

Perimeter of a rectangle: l + w + l + w l: length w: width

Perimeter of a triangle: a + b + c a, b, and c: lengths of the 3 sides

5.1.2: Агеа

Area of a square: s × s s: length of one side

Area of a rectangle: l × w l: length w: width

Area of a triangle: (b × h)/2 b: length of base h: length of height

Area of a trapezoid: $(b_1 + b_2) \times h/2$ b_1 and b_2 : parallel sides or the bases h: length of height

5.1.3: Volume

Volume of a cube: $s \times s \times s$ s: length of one side

Volume of a box: l × w × h
l: length
w: width
h: height

Volume of a sphere: $(4/3) \times pi \times r^3$

```
pi: 3.14 r: radius of sphere
```

Volume of a triangular prism: area of triangle \times Height = (1/2 base \times height) \times Height

base: length of the base of the triangle

height: height of the triangle

Height: height of the triangular prism

Volume of a cylinder: pi \times Γ^2 \times Height

pi: 3.14

r: radius of the circle of the base Height: height of the cylinder

5.2: Geometry Template

```
#include<bits/stdc++.h>
using namespace std;
#define PI acos(-1)
const double INF = 1e4;
const double EPS = 1e-10;
struct Point {
    double x, y;
    Point() {}
    Point(double x, double y): x(x), y(y) {}
    Point(const Point &p): x(p.x), y(p.y) {}
   void input() {
        scanf("%lf%lf", &x, &y);
    }
    Point operator + (const Point &p) const {
        return Point(x + p.x, y + p.y);
    }
    Point operator - (const Point &p) const {
        return Point(x - p.x, y - p.y);
    }
    Point operator * (double c) const {
        return Point(x * c, y * c);
    }
```

```
Point operator / (double c) const {
        return Point(x / c, y / c);
    }
};
vector<Point>polygon;
double getClockwiseAngle(Point p) {
    return -1 * atan2(p.x, -1 * p.y);
}
//compare function to compare clockwise
bool comparePoints(Point p1, Point p2) {
    return getClockwiseAngle(p1) < getClockwiseAngle(p2);</pre>
}
// rotate 90 degrees counter clockwise
Point RotateCCW90(Point p) {
    return Point(-p.y, p.x);
}
// rotate 90 degrees clockwise
Point RotateCW90(Point p) {
    return Point(p.y, -p.x);
}
Point RotateCCW(Point p, double t) {
    return Point(p.x * cos(t) - p.y * sin(t), p.x * sin(t) + p.y * cos(t));
}
Point RotateCW(Point p, double t) {
    return Point(p.x * cos(t) + p.y * sin(t), -p.x * sin(t) + p.y * cos(t));
}
double dot(Point A, Point B) {
    return A.x * B.x + A.y * B.y;
}
double cross(Point A, Point B) {
    return A.x * B.y - A.y * B.x;
double dist2(Point A, Point B) {
    return dot(A - B, A - B);
}
// returns distance between two points
double dist(Point A, Point B) {
    return sqrt(dot(A - B, A - B));
```

```
}
// Distance between point A and B
double distBetweenPoint(Point A, Point B) {
    return sqrt(dot(A - B, A - B));
}
// project point c onto line AB (A!=B)
Point ProjectPointLine(Point A, Point B, Point C) {
    return A + (B - A) * dot(C - A, B - A) / dot(B - A, B - A);
}
// Determine if Line AB and CD are parallel or collinear
bool LinesParallel(Point A, Point B, Point C, Point D) {
    return fabs(cross(B - A, C - D)) < EPS;</pre>
}
// Determine if Line AB and CD are collinear
bool LinesCollinear(Point A, Point B, Point C, Point D) {
    return LinesParallel(A, B, C, D) && fabs(cross(A - B, A - C)) < EPS &&
fabs(cross(C - D, C - A)) < EPS;</pre>
}
// checks if AB intersect with CD
bool SegmentIntersect(Point A, Point B, Point C, Point D) {
    if(LinesCollinear(A, B, C, D)) {
        if(dist2(A, C) < EPS || dist2(A, D) < EPS || dist2(B, C) < EPS ||
dist2(B, D) < EPS) {
            return true;
        if(dot(C - A, C - B) > 0 && dot(D - A, D - B) > 0 && dot(C - B, D - B)
> 0) {
            return false;
        }
        return true;
    if(cross(D - A, B - A) * cross(C - A, B - A) > 0) {
        return false;
    if(cross(A - C, D - C) * cross(B - C, D - C) > 0) {
        return false;
    }
    return true;
}
// Compute the coordinates where AB and CD intersect
Point ComputeLineIntersection(Point A, Point B, Point C, Point D) {
    double a1, b1, c1, a2, b2, c2;
```

```
a1 = A.y - B.y;
    b1 = B.x - A.x;
    c1 = cross(A, B);
    a2 = C.y - D.y;
    b2 = D.x - C.x;
    c2 = cross(C, D);
    double Dist = a1 * b2 - a2 * b1;
    return Point((b1 * c2 - b2 * c1) / Dist, (c1 * a2 - c2 * a1) / Dist);
}
//Project point C onto line segment AB -- return the Point from AB which is
the closest to C --
Point ProjectPointSegment(Point A, Point B, Point C) {
    double r = dot(B - A, B - A);
    if(fabs(r) < EPS) {</pre>
        return A;
    }
    r = dot(C - A, B - A) / r;
    if(r < 0) {
       return A;
    }
    if(r > 1) {
        return B;
    return A + (B - A) * r;
}
// return the minimum distance from a point C to a line AB
double DistancePointSegment(Point A, Point B, Point C) {
    return distBetweenPoint(C, ProjectPointSegment(A, B, C));
}
// return distance between P and a point where p is perpendicular on AB. AB er
upore p jei point e lombo shei point theke p er distance
double distToLine(Point p, Point a, Point b) {
    pair<double, double>c;
    double scale = (double)(dot(p - a, b - a)) / (dot(b - a, b - a));
    c.first = a.x + scale * (b.x - a.x);
    c.second = a.y + scale * (b.y - a.y);
    double dx = (double)p.x - c.first, dy = (double)p.y - c.second;
    return sqrt(dx * dx + dy * dy);
}
long long orientation(Point p, Point q, Point r) {
    long long val = (q.y - p.y) * (r.x - q.x) - (q.x - p.x) * (r.y - q.y);
    if(val > 0) {
        return 1;
    }
```

```
if(val < 0) {
        return 2;
    }
    else {
        return val;
    }
}
// Given three colinear points p, q, r, the function checks if
// point q lies on line segment 'pr'
bool onSegment(Point p, Point q, Point r) {
    if(q.x \le max(p.x, r.x) \&\& q.x \ge min(p.x, r.x) \&\& q.y \le max(p.y, r.y) \&\&
q.y >= min(p.y, r.y)) {
        return true;
    }
    return false;
}
//checks if Point P is inside of polygon or not
bool isInside(int n, Point p) {
    if(n < 3) {
        return false;
    }
    Point extreme = Point(INF, p.y); // here INF=1e4
    int count = 0, i = 0;
    do {
        int next = (i + 1) \% n;
        if(SegmentIntersect(polygon[i], polygon[next], p, extreme)) {
            if(orientation(polygon[i], p, polygon[next]) == 0) {
                return onSegment(polygon[i], p, polygon[next]);
            }
            count++;
        }
        i = next;
    } while(i != 0);
    return count & 1;
}
// returns the perimeter of a polygon
double polygonPerimeter(int n) {
    double perimeter = 0.0;
    for(int i = 0; i < n - 1; i++) { //polygon vector holds the corner points
of the given polygon
        perimeter += dist(polygon[i], polygon[i + 1]);
    }
    perimeter += dist(polygon[0], polygon[n - 1]);
    return perimeter;
```

```
}
// returns the area of a polygon
double polygonArea(int n) {
    double area = 0.0;
    int j = n - 1;
    for(int i = 0; i < n; i++) {
        area += (polygon[j].x + polygon[i].x) * (polygon[j].y - polygon[i].y);
    return fabs(area) * 0.5;
}
double getTriangleArea(Point a, Point b, Point c) {
    return fabs(cross(b - a, c - a));
}
bool compareConvex(Point X, Point Y) {
    long long ret = orientation(points[0], X, Y);
    if(ret == 0) {
        long long dist11 = dist2(points[0], X);
        long long dist22 = dist2(points[0], Y);
        return dist11 < dist22;</pre>
    }
    else if(ret == 2) {
        return true;
    }
    else {
        return false;
    }
}
Point nextToTop(stack<Point> &S) {
    Point p = S.top();
    S.pop();
    Point res = S.top();
    S.push(p);
    return res;
}
// make a minimum area polygon
stack<Point> convexHull(int N) {
    int ymin = points[0].y, index = 0;
    for(int i = 1; i < N; i++) {
        if(points[i].y < ymin || (points[i].y == ymin && points[i].x <</pre>
points[index].x)) {
            ymin = points[i].y ;
            index = i;
```

```
}
    }
    stack<Point>S;
    swap(points[0], points[index]);
    sort(&points[1], &points[N], compareConvex);
    S.push(points[0]);
    for(int i = 1; i < N; i++) {
        while(S.size() > 1 && orientation(nextToTop(S), S.top(), points[i]) !=
2) {
            S.pop();
        S.push(points[i]);
    }
    return S;
}
// Angle between Line AB and AC in degree
double angle(Point B, Point A, Point C) {
    double c = dist(A, B);
    double a = dist(B, C);
    double b = dist(A, C);
    double ans = acos((b * b + c * c - a * a) / (2 * b * c));
    return (ans * 180) / acos(-1);
}
// returns number of vertices on boundary of a polygon
long long picks theorem boundary count() {
    int sz = polygon.size(), i;
    long long res = \_gcd((long long)abs(polygon[0].x - polygon[sz - 1].x),
(long long)abs(polygon[0].y - polygon[sz - 1].y));
    for(i = 0; i < sz - 1; i++) {
        res += __gcd((long long)abs(polygon[i].x - polygon[i + 1].x), (long
long)abs(polygon[i].y - polygon[i + 1].y));
    }
    return res;
}
// picks theorem
// Polygon area= inside points + boundary points/2 -1
// return inside points counts
long long lattice_points_inside_polygon() {
    long long ar = polygonArea(n);
    long long b = picks_theorem_boundary_count();
    long long tot = ar + 1 - b / 2;
    return tot;
}
```

5.3: Number Theory Template

```
#define ll long long
#define ull unsigned long long
ll num[50], rem[50];
vector<ll>parts
char s[100005];
// generate pairwise coprime divisors of N.
void computeCoprimeDivisor() {
   for(int i = 2; i < MX; i++) {
       if(prime[i] == 0) {
          // pr vector holds the divisor of i which is pairwise coprime
          pr[i].push_back(i);
          {
              for(int j = i + i; j < MX; j += i) {
                 prime[j] = 1;
                 pr[j].push_back(fnc(j, i));
             }
          }
      }
   }
   primes[0] = 2;
   int k = 1;
   for(int i = 3; i < MX; i += 2) { // storing primes
       if(prime[i] == 0) {
          primes[k++] = i;
       }
   }
   for(int i = 0; i < k; i++) { // computing perfect powers
       int x = primes[i];
      for(ll j = (ll)x * (ll)x ; j <= 100000; j *= x) {
          perf[j] = 1;
       }
   }
   }
// divides the actual string into several integer parts of 9 digits.
// used in efficient numerical string modulo x
void divide(int len) {
   // len= actual numerical string size
   parts.clear();
```

```
11 \text{ total} = 0;
    int po = 0;
    for(int i = len - 1; i >= 0; i--) {
        11 add = s[i] - '0'; // s is the actual string
        add *= power[po];
        total += add;
        if(po == 9 || i == 0) {
            parts.push_back(total);
            po = 0;
            total = 0;
        }
        else {
            po++;
        }
    }
    reverse(parts.begin(), parts.end());
}
// calculates string modulo x efficiently
11 modulo(11 x) {
    11 \mod = 0;
    for(int i = 0; i < parts.size(); i++) {</pre>
        mod = mod * power[10];
        mod \%= x;
        mod += parts[i];
        mod \%= x;
    }
    return mod;
}
// returns 5 % X where S is a numerical string.
11 stringModx(ll x) {
    divide(strlen(s));
    return modulo(x);
}
// returns inverse(a)%m
ll inv(ll a, ll m) {
    11 m0 = m, t, q;
    11 \times 0 = 0, \times 1 = 1;
    if(m == 1) {
        return 0;
    }
    while(a > 1) {
        q = a / m;
```

```
t = m;
        m = a \% m, a = t;
        t = x0;
        x0 = x1 - q * x0;
        x1 = t;
    }
    if(x1 < 0) {
        x1 += m0;
    }
    return x1;
}
// Sum of NOD
int SNOD(int n) {
    int res = 0;
    int u = sqrt(n);
    for(int i = 1; i <= u; i++) {
        res += (n / i) - i;
    }
    res *= 2;
    res += u;
    return res;
}
int SOD(int n) {
    int res = 1;
    int sqrtn = sqrt(n);
    for(int i = 0; i < prime.size() && prime[i] <= sqrtn; i++) {</pre>
        if(n % prime[i] == 0) {
            // Contains value of (p^0+p^1+...p^a)
            int tempSum = 1;
            int p = 1;
            while(n % prime[i] == 0) {
                n /= prime[i];
                p *= prime[i];
                tempSum += p;
            }
            sqrtn = sqrt(n);
            res *= tempSum;
        }
    }
    if(n != 1) {
        res *= (n + 1); // Need to multiply (p^0+p^1)
    }
    return res;
}
```

```
// given some numbers num[] and reminders rem[] find
// smallest x such that x%num[i]=rem[i] for all i from 0 to k
11 ChineseRemainder(int k) {
    11 \text{ prod} = 1;
    for(int i = 0; i < k; i++) {
        prod = prod * 1LL * num[i];
    }
    11 \text{ result} = 0;
    for(int i = 0; i < k; i++) {
        11 pp = prod / num[i];
        result += rem[i] * inv(pp, num[i]) * pp;
    return result % prod;
}
// Legendre's formula.. returns largest power of P that divides n!
ll largestPower(ll n, ll p) {
    11 \times = 0;
    // Calculate x = n/p + n/(p^2) + n/(p^3) + ....
    while(n) {
        n /= p;
        x += n;
    }
    return x;
}
11 trailing_Zeroes_of_N_Factorial_in_base_b(ll n, ll b) {
    11 \text{ ans} = (11)1e18;
    for(int i = 2; i <= sqrt(b); i++) {
        11 cnt = 0;
        while(b % i == 0) {
            b /= i;
            cnt++;
        }
        if(cnt) {
            ans = min(ans, largestPower(n, i) / cnt);
        }
    }
    if(b != 1) {
        ans = min(ans, largestPower(n, b));
    }
    return ans;
}
// returns nTh catalan number
11 catalan_number(ll n) {
    11 c = nCr(2 * n, n);
    return c / (n + 1);
```

- /* Application of catalan numbers
- 1. Number of possible Binary Search Trees with n keys.
- 2. Number of expressions containing n pairs of parentheses which are correctly matched. For n = 3, possible expressions are ((())), (()()), (()()).
- 3. Number of ways a convex polygon of n+2 sides can split into triangles by connecting vertices.
- 4. Number of full binary trees (A rooted binary tree is full if every vertex has either two children or no children) with n+1 leaves.
 - 5. Number of different Unlabeled Binary Trees can be there with n nodes.
- 6. The number of paths with 2n steps on a rectangular grid from bottom left, i.e., (n-1, 0) to top right (0, n-1) that do not cross above the main diagonal.
- 7. Number of ways to insert n pairs of parentheses in a word of n+1 letters, e.g., for n=2 there are 2 ways: ((ab)c) or (a(bc)). For n=3 there are 5 ways, ((ab)(cd)), (((ab)c)d), ((a(bc))d), (a((bc)d)), (a(b(cd))).
- 8. Number of Dyck words of length 2n. A Dyck word is a string consisting of n X's and n Y's such that no initial segment of the string has more Y's than X's. For example, the following are the Dyck words of length 6: XXXYYY XYXXYY XXYXXYY XXYXXYY.
- 9. Number of ways to form a "mountain ranges" with n upstrokes and n down-strokes that all stay above the original line. The mountain range interpretation is that the mountains will never go below the horizon.
- 10. Number of stack-sortable permutations of $\{1, ..., n\}$. A permutation w is called stack-sortable if S(w) = (1, ..., n), where S(w) is defined recursively as follows: write w = unv where n is the largest element in w and u and v are shorter sequences, and set S(w) = S(u)S(v)n, with S being the identity for one-element sequences.
- 11. Number of permutations of $\{1, ..., n\}$ that avoid the pattern 123 (or any of the other patterns of length 3); that is, the number of permutations with no three-term increasing subsequence. For n=3, these permutations are 132, 213, 231, 312 and 321. For n=4, they are 1432, 2143, 2413, 2431, 3142, 3214, 3241, 3412, 3421, 4132, 4213, 4231, 4312 and 4321

```
}

ull mul(ull a, ull b) {
    ull res = 0;
    while(b) {
        if(b & 1LL) {
            res = (res + a);
        }
        if(res >= n) {
                return 0;
        }
        a = (a << 1LL);
        b >>= 1LL;
    }
}
```

*/

```
return res;
}
int p, primes[] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 51, }
53, 59, 61, 67, 71};
void backtrack(int i, int lim, ull val, ull r) {
    if(r > res) {
        res = r;
    }
    if(i == p) {
        return;
    }
    int d;
    ull x = val;
    for(d = 1; d <= lim; d++) {
        x = mul(x, primes[i]);
        if(x == 0) {
            return;
        backtrack(i + 1, d, x, r * (d + 1));
}
ull maximum_NOD_of_any_number_less_than_N(ull n) {
    p = sizeof(primes) / sizeof(int);
    res = 0;
    backtrack(0, 100, 1, 1);
    return res;
}
```


6.1: Kruskal

```
const int Max = 15e3 + 10;
struct Node {
    int u, v, w;
} g[Max];
bool less(Node a, Node b) {
    return a.w < b.w;
}
bool more(Node a, Node b) {
    return a.w > b.w;
}
int node, edge, parent[Max];
int Find_parent(int n) {
   //cout << ": " << n << " " << parent[n] << endl;
    if(parent[n] == n) {
        return n;
    }
    return Find_parent(parent[n]);
}
void graph() {
   for(int i = 1; ; i++) {
        cin >> g[i].u >> g[i].v >> g[i].w;
        edge++;
    }
}
int kruskal() {
    int sum = 0;
   for(int i = 0; i <= node; i++) {
        parent[i] = i;
    }
   for(int i = 1; i <= edge; i++) {
        int u = Find_parent(g[i].u), v = Find_parent(g[i].v);
        //cout << u << " " << v << endl;
        if(u != v) {
            //printf("The cost from %d to %d is : %d\n", s1[i], s2[i], w[i]);
            parent[u] = v;
```

```
sum += g[i].w;
        }
    }
    return sum;
}
int main() {
    int t; cin >> t;
    for(int tc = 1; tc <= t; tc++) {
        cin >> node;
        edge = 0;
        graph();
        // Minimus
        sort(g + 1, g + edge + 1, less);
        cout << kruskal() << endl;</pre>
        // Maximum
        sort(g + 1, g + edge + 1, more);
        cout << kruskal() << endl;</pre>
    }
    return 0;
}
```

6.2: Dijkstra

```
struct Node {
    int at, cost;
    Node(int _at, int _cost) {
        at = _at;
        cost = _cost;
    }
};

bool operator<(Node a, Node b) {
    return a.cost > b.cost;
}

struct Edge {
    int v, w;
    Edge(int _v, int _w) {
        v = _v;
        w = _w;
    }
}
```

```
}
};
vector <Edge> G[10001];
priority_queue <Node> pq;
int dist[10001];
int n, m, s;
void dijsktra(int src) {
    for(int i = 1; i <= n; i++) {
        dist[i] = 1e9;
    }
    dist[src] = 0;
    pq.push(Node(src, 0));
   while(!pq.empty()) {
        Node u = pq.top();
        pq.pop();
        if(u.cost != dist[u.at]) {
            continue;
        for(int i = 0; i < G[u.at].size(); i++) {</pre>
            Edge e = G[u.at][i];
            if(dist[e.v] > u.cost + e.w) {
                dist[e.v] = u.cost + e.w;
                pq.push(Node(e.v, dist[e.v]));
            }
        }
    }
}
```

6.3: Dijkstra with Set

```
#include<bits/stdc++.h>
#define MX 100005
#define INF 2000100100105
#define LL long long
#define pb push_back
#define mp make_pair
using namespace std;
vector<pair<LL, LL> > v[MX];
vector<pair<LL, LL> > ::iterator vt;
int edge, node, path[MX];
LL dist[MX];
```

```
void graph() {
    LL a, b, w;
    for(int i = 1; i <= node; i++) {
        dist[i] = INF;
    for(int i = 1; i <= edge; i++) {
        cin >> a >> b >> w;
        v[a].pb(mp(b, w));
        v[b].pb(mp(a, w));
}
void dijkstra(int src) {
    set<pair<LL, LL> > s;
    set<pair<LL, LL> > ::iterator it;
    dist[src] = 0;
    s.insert(mp(0, src));
    while(s.size()) {
        it = s.begin();
        int u = it->second;
        s.erase(it);
        for(vt = v[u].begin(); vt != v[u].end(); vt++) {
            if(dist[u] + vt->second < dist[vt->first]) {
                if(dist[vt->first] != INF) {
                    s.erase(s.find(make_pair(dist[vt->first], vt->first)));
                }
                dist[vt->first] = dist[u] + vt->second;
                s.insert(mp(dist[vt->first], vt->first));
                path[vt->first] = u;
            }
        }
    }
}
void print_path(int src) {
    if(src == 0) {
        return;
    print_path(path[src]);
    cout << src << " ";
}
int main() {
    ios_base::sync_with_stdio(false);
    cin >> node >> edge;
    graph();
    dijkstra(1);
```

```
//cout << dist[node] << endl;
if(dist[node] != INF) {
    print_path(node);
    cout << endl;
}
else {
    cout << -1 << endl;
}
return 0;
}</pre>
```

6.4: Dinic Maxflow

```
///V^2*E Complexity
///number of augment path * (V+E)
///Base doesn't matter
const int INF = 2000000000;
const int MAXN = 100;///total nodes
const int MAXM = 10000;///total edges
int N, edges;
int last[MAXN], Prev[MAXM], head[MAXM];
int Cap[MAXM], Flow[MAXM];
int dist[MAXN];
int nextEdge[MAXN];///used for keeping track of next edge of ith node
queue<int> Q;
void init(int N) {
    edges = 0;
   memset(last, -1, sizeof(int)*N);
}
//cap=capacity of edges , flow = initial flow
inline void addEdge(int u, int v, int cap, int flow) {
    head[edges] = v;
    Prev[edges] = last[u];
   Cap[edges] = cap;
    Flow[edges] = flow;
    last[u] = edges++;
   head[edges] = u;
    Prev[edges] = last[v];
   Cap[edges] = 0;
    Flow[edges] = 0;
    last[v] = edges++;
```

```
}
inline bool dinicBfs(int S, int E, int N) {
    int from = S, to, cap, flow;
    memset(dist, 0, sizeof(int)*N);
    dist[from] = 1;
   while(!Q.empty()) {
        Q.pop();
    }
   Q.push(from);
   while(!Q.empty()) {
        from = Q.front(); Q.pop();
        for(int e = last[from]; e >= 0; e = Prev[e]) {
            to = head[e];
            cap = Cap[e];
            flow = Flow[e];
            if(!dist[to] && cap > flow) {
                dist[to] = dist[from] + 1;
                Q.push(to);
            }
        }
    return (dist[E] != 0);
}
inline int dfs(int from, int minEdge, int E) {
    if(!minEdge) {
        return 0;
    }
    if(from == E) {
        return minEdge;
    }
    int to, e, cap, flow, ret;
    for(; nextEdge[from] >= 0; nextEdge[from] = Prev[e]) {
        e = nextEdge[from];
        to = head[e];
        cap = Cap[e];
        flow = Flow[e];
```

```
if(dist[to] != dist[from] + 1) {
            continue;
        }
        ret = dfs(to, min(minEdge, cap - flow), E);
        if(ret) {
            Flow[e] += ret;
            Flow[e ^ 1] -= ret;
            return ret;
        }
    }
    return 0;
}
int dinicUpdate(int S, int E) {
    int flow = 0;
   while(int minEdge = dfs(S, INF, E)) {
        if(minEdge == 0) {
            break;
        }
        flow += minEdge;
    }
    return flow;
}
int maxFlow(int S, int E, int N) {
    int totFlow = 0;
   while(dinicBfs(S, E, N)) {
        for(int i = 0; i <= N; i++) {
            nextEdge[i] = last[i]; /// update last edge of ith node
        }
        totFlow += dinicUpdate(S, E);
    }
    return totFlow;
}
```

6.5: HopcroftKarp

```
//Esqrt(V) Complexity
//0 Based
//Edge from set a to set b
const int MAXN1 = 50010; //nodes in set a
const int MAXN2 = 50010; //nodes in set b
const int MAXM = 150010; //number of edges
int n1, n2, edges, last[MAXN1], prev[MAXM], head[MAXM];
int matching[MAXN2], dist[MAXN1], Q[MAXN1];
bool used[MAXN1], vis[MAXN1]; //vis is cleared in each dfs
// n1 = number of nodes in set a, n2 = number of nodes in set b
void init(int _n1, int _n2) {
    n1 = _n1;
    n2 = _n2;
    edges = 0;
    fill(last, last + n1, -1);
}
void addEdge(int u, int v) {
    head[edges] = v;
    prev[edges] = last[u];
    last[u] = edges++;
}
void bfs() {
    fill(dist, dist + n1, -1);
    int sizeQ = 0;
    for(int u = 0; u < n1; ++u) {
        if(!used[u]) {
            Q[sizeQ++] = u;
            dist[u] = 0;
        }
    }
    for(int i = 0; i < sizeQ; i++) {
        int u1 = Q[i];
        for(int e = last[u1]; e >= 0; e = prev[e]) {
            int u2 = matching[head[e]];
            if(u2 >= 0 \&\& dist[u2] < 0) {
                dist[u2] = dist[u1] + 1;
                Q[sizeQ++] = u2;
            }
        }
    }
```

```
}
bool dfs(int u1) {
   vis[u1] = true;
    for(int e = last[u1]; e >= 0; e = prev[e]) {
        int v = head[e];
        int u2 = matching[v];
        if(u2 < 0 \mid | (!vis[u2] \&\& dist[u2] == dist[u1] + 1 \&\& dfs(u2))) {
            matching[v] = u1;
            used[u1] = true;
            return true;
        }
    }
    return false;
}
int augmentPath() {
    bfs();
    fill(vis, vis + n1, false);
    int f = 0;
    for(int u = 0; u < n1; ++u)
        if(!used[u] && dfs(u)) {
            ++f;
        }
    return f;
}
```

6.6: Articulation Bridge

```
void ArticulationBridge(int u) {
    low[u] = dist[u] = ++cur;
    vist[u] = 1;
    for(int i = 0; i < G[u].size(); i++) {
        int v = G[u][i];
        if(vist[v]) {
             if(v != par[u]) {
                  low[u] = min(low[u], dist[v]);
             }
        }
        else {
             par[v] = u;
             ArticulationBridge(v);</pre>
```

6.7: Articulation Point

```
void ArticulationPoint(int u) {
    low[u] = dist[u] = ++cur;
    vist[u] = 1;
    int tot = 0;
    for(int i = 0; i < G[u].size(); i++) {</pre>
        int v = G[u][i];
        tot++;
        if(vist[v]) {
            if(v != par[u]) {
                low[u] = min(low[u], dist[v]);
            }
        }
        else {
            par[v] = u;
            ArticulationPoint(v);
            low[u] = min(low[u], low[v]);
            if(tot > 1 and par[u] == -1) {
                st.insert(u);
            }
            if(par[u] != -1 and low[v] >= dist[u]) {
                st.insert(u);
            }
        }
    }
}
```

6.8: Bellman Ford

```
struct edge {
    int u, v, w;
    edge(int _u, int _v, int _w) {
        u = _u;
        v = v;
        W = W;
};
const int MAX = 1e5 + 7, INF = 1e7 + 7;
vector < edge > adj;
long long dist[MAX];
int par[MAX];
int V, E;
void bellman_ford(int src) {
    for(int i = 1; i <= V; i++) {
        dist[i] = INF;
    }
    dist[src] = 0;
    par[src] = -1;
    for(int i = 1; i < V; i++) {
        int flag = 0;
        for(auto j : adj) {
            if(dist[j.v] > dist[j.u] + j.w) {
                dist[j.v] = dist[j.u] + j.w;
                par[j.v] = j.u;
                flag = 1;
            }
        }
        if(!flag) {
            break;
        }
    }
}
void print_path(int src, int node) {
    vector < int > path;
    int i = node;
    while(i != -1) {
        path.push_back(i);
        i = par[i];
    for(i = path.size() - 1; i >= 0; i--) {
        cout << path[i] << " ";
    }
```

```
cout << endl;</pre>
}
bool negetive_cycle(int src) {
    bellman_ford(src);
    for(auto i : adj) {
        if(dist[i.v] > dist[i.u] + i.w) {
            return true;
        }
    }
    return false;
}
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    int uu, vv, ww;
    cin >> V >> E;
    for(int i = 0; i < E; i++) {
        cin >> uu >> vv >> ww;
        adj.push_back(edge(uu, vv, ww));
    }
    if(negetive_cycle(1)) {
        cout << "Negetive Cycle is found!!\n";</pre>
    else if(dist[V] < INF) {</pre>
        print_path(1, V);
    }
    else {
        cout << -1 << endl;
    }
}
```

6.9: Strongly Connected Component

```
const int MAX = 1e3 + 10;
vector <int> graph[MAX], reverseGraph[MAX], components[MAX];
bool vis[MAX];
int scc[MAX], compCount;
stack<int>nodes;

void DFS(int src) {
   vis[src] = 1;
   for(auto i : graph[src]) {
      if(!vis[i]) {
```

```
DFS(i);
        }
    }
    nodes.push(src);
}
void DFS2(int src) {
    vis[src] = 1;
    for(auto i : reverseGraph[src]) {
        if(!vis[i]) {
            DFS2(i);
        }
    }
    components[compCount].push_back(src);
    scc[src] = compCount;
}
void init() {
    compCount = 1;
    for(int i = 1; i < MAX; i++) {</pre>
        graph[i].clear(), reverseGraph[i].clear(), components[i].clear();
    }
}
void addEdge(int u, int v) {
    graph[u].push_back(v);
    reverseGraph[v].push_back(u);
}
void kosaraju_SCC(int n) {
    memset(vis, 0, sizeof vis);
    for(int i = 1; i <= n; i++) {
        if(!vis[i]) {
            DFS(i);
        }
    memset(vis, 0, sizeof vis);
   while(nodes.size()) {
        int top = nodes.top();
        nodes.pop();
        if(!vis[top]) {
            DFS2(top);
            compCount++;
        }
    }
}
void print_SCCs() {
```

```
for(int i = 1; i < compCount; i++) {</pre>
        cout << "Component " << i << ":\n";</pre>
        for(auto j : components[i]) {
            cout << j << " -> ";
        cout << endl;</pre>
    }
}
int main() {
    int n, m, u, v;
    init();
    cin >> n >> m;
    for(int i = 0; i < m; i++) {
        cin >> u >> v;
        addEdge(u, v);
    kosaraju_SCC(n);
    print_SCCs();
}
```

6.10: Ford Fulkerson for Max Flow

```
const int MAXN = 1050;
const int INF = (int) 1e9;
struct edge {
    int from, to, f, cap;
};
int n, m;
vector <edge> e;
vector <int> g[MAXN];
bool used[MAXN];
int s, t;
long long ans;
void init() {
    e.clear();
    for(int i=0;i<MAXN;i++)</pre>
        g[i].clear();
   memset(used,0,sizeof(used));
    ans=0;
}
void addEdge(int from, int to, int cap) {
```

```
edge ed;
    ed.from = from; ed.to = to; ed.f = 0; ed.cap = cap;
    e.push_back(ed);
    g[from].push_back((int) e.size() - 1);
    ed.from = to; ed.to = from; ed.f = cap; ed.cap = cap;
    e.push_back(ed);
    g[to].push_back((int) e.size() - 1);
}
long long pushFlow(int v, long long flow = INF) {
    used[v] = true;
    if (v == t)
        return flow;
    for (int i = 0; i < (int) g[v].size(); i++) {
        int ind = g[v][i];
        int to = e[ind].to;
        int f = e[ind].f;
        int cap = e[ind].cap;
        if (used[to] || cap - f == 0)
            continue;
        long long pushed = pushFlow(to, min(flow, (long long)cap - f));
        if (pushed > 0) {
            e[ind].f += pushed;
            e[ind ^ 1].f -= pushed;
            return pushed;
        }
    }
    return 0;
}
```

6.11: Directed MST (Edmond's Algorithm)

```
/* Algo
    1 . For each node find the minimum incoming edge except root
    2 . Look for cycle if there is no cycle its MST
    3 . If cycle then consider one cycle as a one single vertex , give
every vertex a new indx and again recalculate the every edge
    4 . goto step 2
*/
// Directed MST (Edmond's Algo) Template Credit https://github.com/shakilaust
```

```
// Tested On LightOJ 1380
#include<bits/stdc++.h>
using namespace std;
#define INF 1e9
const int Maxn = 1005 ; // Highest Vertex
struct edge {
    int u, v, w;
    edge() {}
    edge(int _u, int _v, int _w) {
       u = _u, v = _v, w = _w;
    }
};
int nodes, edges, root; // nV = number of vertex , nE = number of edge ,
root is root
int vis[Maxn], parnt[Maxn]; // vis[] will store from which cycle it belogs ,
pre[] store its parnt
int Idx[Maxn] ; // will store new indxing Id
int dis[Maxn]; // store the lowest incoming edge of a root
vector < edge > vec ;
int DMST() {
    int ans = 0, i, u, v, w;
    while(true) {
        int i ;
        for(i = 0; i < nodes; i++) {
            dis[i] = INF ;
            vis[i] = -1;
            Idx[i] = -1;
        for(i = 0; i < vec.size(); i++) {
            u = vec[i].u;
            v = vec[i].v;
            w = vec[i].w;
            if(u != v && dis[v] > w) { // lowest Incoming Edge
                parnt[v] = u;
                dis[v] = w;
            }
        }
        parnt[root] = root;
        dis[root] = 0;
        for(i = 0; i < nodes; i++) {
            if(dis[i] == INF) {
               return -1; // its not possible to reach
            }
            ans += dis[i];
```

```
}
        int idx = 0;
        // cycle detection
        for(i = 0; i < nodes; i++) {
            if(vis[i] == -1) { // not yet visited
                int cur = i ;
                while(vis[cur] == -1) {
                    vis[cur] = i ;
                    cur = parnt[cur] ;
                if(cur == root || vis[cur] != i) {
                    continue;
                                 // not cycle
                Idx[cur] = idx ; // new indexing
                for(u = parnt[cur] ; cur != u ; u = parnt[u]) {
                    Idx[u] = idx;
                }
                idx++;
            }
        }
        if(idx == 0) {
            break; // no cycle
        }
        for(i = 0; i < nodes; i++) {
            if(Idx[i] == -1) { // yet not find any grp}
                Idx[i] = idx++;
            }
        }
        for(i = 0; i < vec.size(); i++) {
            vec[i].w -= dis[vec[i].v];
            vec[i].u = Idx[vec[i].u];
            vec[i].v = Idx[vec[i].v];
        }
        nodes = idx++;
        root = Idx[root];
    }
    return ans;
}
```

6.12: Prim's Algorithm for finding MST

```
#include <bits/stdc++.h>
using namespace std;

typedef long long int 11;
```

```
typedef pair <11, 11> pll;
const int Max = 1e5 + 10;
const int Mod = 1e9 + 7;
const ll Inf = 1LL << 62;</pre>
bool vist[Max];
vector <pll> G[Max];
ll prim(int src) {
    priority_queue <pll, vector<pll>, greater<pll>> q;
    11 \, mn = 0;
    q.push(make_pair(0, src));
    while(!q.empty()) {
        pll p = q.top();
        q.pop();
        int u = p.second;
        if(vist[u] == true) {
            continue;
        }
        mn += p.first;
        vist[u] = true;
        for(pll v : G[u]) {
            if(vist[v.second] == false) {
                q.push(v);
            }
        }
    }
    return mn;
}
int main() {
    int n, m, u, v;
    11 w, mn;
    cin >> n >> m;
    for(int i = 1; i <= m; i++) {
        cin >> u >> v >> w;
        G[u].push_back(make_pair(w, v));
        G[v].push_back(make_pair(w, u));
    }
    mn = prim(1);
    cout << mn << endl;</pre>
    return 0;
}
```

6.13: Centroid Decomposition

```
/*
Tested Problem:
 Each node has a color, white or black. All the nodes are black initially.
 We will ask you to perfrom some instructions of the following form:
   0 i : change the color of i-th node(from black to white, or from white to
black).
    1 \ v: ask for the minimum dist(u, v), node u must be white(u can be equal
to v). Obviously, as long as node v is white, the result will always be 0.
const int Max = 2e5 + 10;
int L[Max];
int P[Max][22];
int T[Max];
int ans[Max];
vector <int> G[Max];
void dfs(int u, int par, int dep) {
   T[u] = par;
    L[u] = dep;
    for(int v : G[u]) {
        if(v == par) {
            continue;
        dfs(v, u, dep + 1);
    }
}
int lca_query(int p, int q) {
}
void lca_init(int n) {
}
struct CentriodDecomposition {
    bool vist[Max];
    int sub[Max];
    int path[Max];
   CentriodDecomposition() {
```

```
memset(vist, 0, sizeof vist);
        memset(sub, 0, sizeof sub);
        memset(path, 0, sizeof path);
    }
    int centroid(int u, int par, int sz) {
        for(int v : G[u]) {
            if(v == par) {
                continue;
            }
            if(!vist[v]) {
                if(sub[v] > sz) {
                    return centroid(v, u, sz);
                }
            }
        }
        return u;
    }
    void calc(int u, int par) {
        sub[u] = 1;
        for(int v : G[u]) {
            if(v == par) {
                continue;
            }
            if(!vist[v]) {
                calc(v, u);
                sub[u] += sub[v];
            }
        }
    }
    void decompose(int u, int par) {
        calc(u, par);
        int c = centroid(u, -1, sub[u] / 2);
        vist[c] = 1;
        path[c] = par;
        for(int v : G[c]) {
            if(!vist[v]) {
                decompose(v, c);
            }
        }
    }
} tree;
int dist(int u, int v) {
    int lca = lca_query(u, v);
    return L[u] + L[v] - 2 * L[lca];
```

```
}
int cnt[Max];
multiset <int> st[Max];
struct UpdateQuery {
    UpdateQuery() {
        for(int i = 0; i < Max; i++) {
            ans[i] = 1e9;
        }
    }
    int query(int u) {
        int ret = 1e9;
        for(int v = u; v + 1 > 0; v = tree.path[v]) {
            if(st[v].size()) {
                ret = min(ret, *st[v].begin() + dist(u, v));
            }
        }
        if(ret == 1e9) {
            ret = -1;
        }
        return ret;
    }
    void update(int u) {
        for(int v = u; v + 1 > 0; v = tree.path[v]) {
            if(cnt[u] & 1) {
                st[v].insert(dist(u, v));
            }
            else {
                st[v].erase(st[v].find(dist(u, v)));
            }
        }
    }
} ds;
int main() {
    int n, q, ty, u, v;
    scanf("%d", &n);
    for(int i = 1; i < n; i++) {
        scanf("%d %d", &u, &v);
        G[u].push_back(v);
        G[v].push_back(u);
    }
    dfs(1, -1, 0);
    lca_init(n);
    tree.decompose(1, -1);
```

```
scanf("%d", &q);
while(q--) {
    scanf("%d %d", &ty, &u);
    if(ty == 0) {
        cnt[u]++;
        ds.update(u);
    }
    else {
        printf("%d\n", ds.query(u));
    }
}
return 0;
}
```

6.14: Stable Marriage Problem

```
const int Max = 1e3 + 10;
int n, pref[2 * Max][Max];
bool freeMan[Max];
int wPartner[Max];
bool wPreferM_M1(int w, int m, int m1) {
    for(int i = 1; i <= n; i++) {
        if(pref[w][i] == m) {
            return true;
        }
        if(pref[w][i] == m1) {
            return false;
        }
    }
}
void stableMarriage() {
    memset(freeMan, 0, sizeof freeMan);
    memset(wPartner, -1, sizeof wPartner);
    int rem = n;
    while(rem) {
        int m;
        for(int i = 1; i <= n; i++) {
            if(freeMan[i] == 0) {
                m = i;
                break;
            }
        }
```

```
for(int i = 1; i <= n && freeMan[m] == 0; i++) {
            int w = pref[m][i];
            if(wPartner[w - n] == -1) {
                freeMan[m] = 1;
                wPartner[w - n] = m;
                rem--;
            }
            else {
                int m1 = wPartner[w - n];
                if(wPreferM_M1(w, m, m1)) {
                    freeMan[m1] = 0;
                    freeMan[m] = 1;
                    wPartner[w - n] = m;
                }
            }
        }
    }
    for(int i = 1; i <= n; i++) {
        printf(" (%d %d)", wPartner[i], i + n);
    }
    printf("\n");
}
```

6.15: Floyd Warshall

```
const int Max = 205;
const int inf = 1e9 + 10;
int n, m;
int adj[Max][Max], path[Max][Max];
int dist[Max][Max], minimax[Max][Max], maximin[Max][Max], prob[Max][Max];
bool hasPath[Max][Max];
/// Calculates shortest path for all pairs in dist[][] variable
void floydWarsh() {
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= n; j++) {
            dist[i][j] = adj[i][j];
        }
    }
    for(int via = 1; via <= n; via++) {</pre>
        for(int from = 1; from <= n; from++) {</pre>
            for(int to = 1; to <= n; to++) {
                if(dist[from][via] + dist[via][to] < dist[from][to]) {</pre>
                    dist[from][to] = dist[from][via] + dist[via][to];
                    path[from][to] = path[via][to];
```

```
}
            }
        }
    }
}
/// finding a path between two nodes that minimizes the maximum edge cost in
the path
void mini_max() {
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= n; j++) {
            minimax[i][j] = adj[i][j];
        }
    }
    for(int via = 1; via <= n; via++) {</pre>
        for(int from = 1; from <= n; from++) {</pre>
            for(int to = 1; to <= n; to++) {
                minimax[from][to] = min(minimax[from][to],
max(minimax[from][via], minimax[via][to]));
        }
    }
}
/// finding a path between two nodes that maximizes the minimum edge cost in
the path
void maxi min() {
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= n; j++) {
            maximin[i][j] = (adj[i][j] == inf) ? 0 : adj[i][j];
        }
    }
    for(int via = 1; via <= n; via++) {</pre>
        for(int from = 1; from <= n; from++) {</pre>
            for(int to = 1; to <= n; to++) {
                maximin[from][to] = max(maximin[from][to],
min(maximin[from][via], maximin[via][to]));
        }
    }
}
/// Calculates if a path exits between two nodes for all pairs in directed
graph
void transitiveClosure() {
    for(int i = 1; i <= n; i++) {
```

```
for(int j = 1; j <= n; j++) {
            hasPath[i][j] = (adj[i][j] == inf) ? 0 : adj[i][j];
        }
    }
    for(int via = 1; via <= n; via++) {</pre>
        for(int from = 1; from <= n; from++) {</pre>
            for(int to = 1; to <= n; to++) {
                hasPath[from][to] |= (hasPath[from][via] & hasPath[via][to]);
            }
        }
    }
}
/// Safest path variant of Floyd-Warshall example
/// input: p is an probability matrix (probability of survival) for n nodes
        e.g. p[i][j] is the probability of survival moving directly from i to
///
j.
///
        the probability from a node to itself e.g. p[i][i] should be
initialized to 1
/// output: p[i][j] will contain the probability of survival using the safest
path from i to j.
void safest_path() {
    for(int via = 1; via <= n; via++) {</pre>
        for(int from = 1; from <= n; from++) {</pre>
            for(int to = 1; to <= n; to++) {
                prob[from][to] = max(prob[from][to], prob[from][via] *
prob[via][to]);
            }
        }
    }
}
/// Check if the graph contains negative cycle in connected graph
/// Distance from any node to itself should always be 0
/// For disconnected graph, check whether the distance is 0 for all node
bool negativeCycle() {
    floydWarsh();
    return dist[0][0] < 0;
}
/// Finds the path from i to j
void findPath(int i, int j) {
    cout << i << endl;</pre>
    if(i != j) {
        findPath(path[i][j], j);
    }
}
```

```
/// initializes adjacency matrix and path
void init() {
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= n; j++) {
            adj[i][j] = inf;
        }
    }
    for(int i = 1; i <= n; i++) {
        adj[i][i] = 0, path[i][i] = i;
    }
}</pre>
```

Part 7 ⇒ Dynamic Programming

7.1: LCS

```
const int Max = 1000 + 5;
int dp[Max][Max];
bool vist[Max][Max];
string s, t;
int n, m;
int lcs(int i, int j) {
    if(i >= n \text{ or } j >= m) {
        return 0;
    int &ret = dp[i][j];
    bool &vis = vist[i][j];
    if(vis) {
        return ret;
    vis = 1;
    int res = 0;
    if(s[i] == t[j]) {
        res = 1 + lcs(i + 1, j + 1);
    }
    else {
        res = \max(lcs(i + 1, j), lcs(i, j + 1));
    return ret = res;
}
string ans;
void solution(int i, int j) {
    if(i >= n \text{ or } j >= m) {
        return;
    if(s[i] == t[j]) {
        ans += s[i];
        solution(i + 1, j + 1);
    }
    else {
        if(lcs(i + 1, j) > lcs(i, j + 1)) {
            solution(i + 1, j);
        }
        else {
            solution(i, j + 1);
        }
```

```
}
}
int main() {
    int T;
    cin >> T;
    for(int tc = 1; tc <= T; tc++) {
        cin >> s >> t;
        n = s.size();
        m = t.size();
        memset(vist, 0, sizeof vist);
        int maxlen = lcs(0, 0);
        ans = "";
        solution(0, 0);
        cout << ans << '\n';</pre>
    }
}
```

7.2: Longest Increasing Subsequence (nlogn)

```
#include<bits/stdc++.h>
using namespace std;
int main() {
    int n, t;
    vector<int> v;
    vector<int> LIS;
    scanf("%d", &n);
    for(int i = 1; i <= n; i++) {
        scanf("%d", &t);
        v.push_back(t);
        vector<int> ::iterator it;
        it = lower_bound(LIS.begin(), LIS.end(), t);
        if(it != LIS.end()) {
            *it = t;
        }
        else {
            LIS.push_back(t);
        }
    }
    cout << LIS.size() << endl;</pre>
    return 0;
}
```

7.3: Coin Change

In a strange shop there are **n** types of coins of value A_n , A_2 ... A_n . You have to find the number of ways you can make **K** using the coins. You can use any coin at most **K** times.

For example, suppose there are three coins 1, 2, 5. Then if K = 5 the possible ways are:

```
11111
1112
122
So, 5 can be made in 4 ways.
Solution:
11 ar[Max];
int main() {
    11 t, n, k;
    while(scanf("%11d", &t) == 1) {
        int tc = 1;
        while(t--) {
            scanf("%11d %11d", &n, &k);
            11 dp[k + 1];
            memset(dp, 0, sizeof dp);
            dp[0] = 1;
            for(int i = 1; i <= n; i++) {
                 scanf("%lld", &ar[i]);
            }
            for(int i = 1; i <= n; i++) {
                 for(int j = 1; j <= k; j++) {
                     if(ar[i] <= j) {
                         dp[j] = dp[j] \% Mod + dp[j - ar[i]] \% Mod;
                         dp[j] %= Mod;
                     }
                 }
            }
            printf("Case %d: %lld\n", tc, dp[k]);
            tc++;
        }
    }
    return 0;
}
```

7.4: SOS DP

```
for(int i = 0; i < (1 << N); ++i) {
    F[i] = A[i];
}

for(int i = 0; i < N; ++i) {
    for(int mask = 0; mask < (1 << N); ++mask) {
        if(mask & (1 << i)) {
            F[mask] += F[mask ^ (1 << i)];
        }
    }
}</pre>
```

Part 8 ⇒ Matrix

8.1: Matrix Exponentiation

```
#include <bits/stdc++.h>
using namespace std;
typedef long long int 11;
typedef pair <ll, ll> pll;
const int Max = 2e6 + 10;
const int Mod = 1e4 + 7;
const ll Inf = 1LL << 62;
struct Matrix {
    int n, m;
    vector <vector <int>> mat;
   Matrix() {}
   Matrix(int _n, int _m) {
        n = _n, m = _m;
        mat = vector <vector <int>> (n, vector <int> (m));
    }
    void print() {
        for(int i = 0; i < n; i++) {
            for(int j = 0; j < m; j++) {
                printf("%d", mat[i][j]);
                if(j == m - 1) {
                    printf("\n");
                }
                else {
                    printf(" ");
                }
            }
        }
    }
};
Matrix Multiply(Matrix a, Matrix b, int Mod) {
   Matrix c = Matrix(a.n, b.m);
    for(int i = 0; i < a.n; i++) {
        for(int j = 0; j < b.m; j++) {
            c.mat[i][j] = 0;
            for(int k = 0; k < a.m; k++) {
                c.mat[i][j] += (1LL * a.mat[i][k] * b.mat[k][j]) % Mod;
                c.mat[i][j] %= Mod;
            }
```

```
}
    }
    return c;
}
Matrix Add(Matrix a, Matrix b, int Mod) {
   Matrix c = Matrix(a.n, a.n);
    for(int i = 0; i < a.n; i++) {
        for(int j = 0; j < a.n; j++) {
            c.mat[i][j] = a.mat[i][j] + b.mat[i][j];
            c.mat[i][j] %= Mod;
        }
    }
    return c;
}
Matrix Pow(Matrix a, ll p, int Mod) {
    if(p == 1) {
        return a;
    }
   Matrix x = Pow(a, p / 2, Mod);
    x = Multiply(x, x, Mod);
    if(p & 1) {
        x = Multiply(x, a, Mod);
    return x;
}
int main() {
#ifdef Mr_Emrul
    freopen("inputf.in", "r", stdin);
#endif /// Mr_Emrul
    int t, n, a, b, c;
    scanf("%d", &t);
    for(int tc = 1; tc <= t; tc++) {
        scanf("%d %d %d %d", &n, &a, &b, &c);
        if(n <= 2) {
            printf("Case %d: 0\n", tc);
            continue;
        }
        Matrix M = Matrix(4, 4);
        M.mat[0][0] = a;
        M.mat[0][2] = b;
        M.mat[0][3] = c;
        M.mat[1][0] = 1;
        M.mat[2][1] = 1;
        M.mat[3][3] = 1;
```

```
Matrix A = Matrix(4, 1);
A.mat[3][0] = 1;
M = Pow(M, n - 2, Mod);
A = Multiply(M, A, Mod);
//A.print();
printf("Case %d: %d\n", tc, A.mat[0][0]);
}
return 0;
}
```

8.2: Matrix Power Sum

```
Matrix solveBinary(const Matrix &a, int n) {
    if(n == 1) {
        return a;
    }
   Matrix answer = new_matrix;
   Matrix tmp = new_matrix;
    answer = solveBinary(a, n / 2);
    if(n & 1) {
        tmp = mod_pow(a, n / 2 + 1);
        answer = Add(answer, multiply(tmp, answer));
        answer = Add(tmp, answer);
    }
    else {
        tmp = mod_pow(a, n / 2);
        answer = Add(answer, multiply(tmp, answer));
    return answer;
}
/*
      We know that the matrix A^x can be solved quickly by the matrix fast
      power. We must consider how to reduce the computation is S = A + A ^ 2
      + A ^ 3 + ... A ^ k + during the addition of this time-consuming
      operation. Below we consider matrix A as a normal number A.
      For S(10) we have:
      S(10) = A + A^2 + A^3 + A^4 + A^5 + A^5 * (A + A^2 + A^3 + A^4 + A^5)
      For S(5) we have:
      S(5) = A + A^2 + A^3 + A^3 * (A + A^2)
      For S(2) we have:
      S(2) = A + A * (A)
      The value of A has been given in the question, then we can get the
      value of S(2) by recursive backtracking, and find the value of A^3,
      then we can get the value of S(5) by the above formula, and then get S(5)
```

The value of (10). Then for each S(k) we can do this two-way recursive solution. Note that S(n) here requires an additional value of $A^{(n/2+1)}$ when n is odd (for example, S(5) above). Finally, add the matrix's fast power and addition operations.

*/