Centre No.				Paper Reference			Surname	Initial(s)			
Candidate No.			6	6	6	9	/	0	1	Signature	

Paper Reference(s)

## 6669/01

# **Edexcel GCE**

# **Further Pure Mathematics FP3** Advanced/Advanced Subsidiary

Monday 23 June 2014 – Morning

Time: 1 hour 30 minutes

Materials required for examination	Items included with question paper
Mathematical Formulae (Pink)	Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

#### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 32 pages in this question paper. Any blank pages are indicated.

### Advice to Candidates

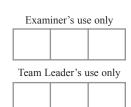
You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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Turn over

**Total** 

**PEARSON** 

1.	The line $l$ passes through the point $P(2,1,3)$ and is perpendicular to the plane $\Pi$ whose						
	vector equation is $\mathbf{r}.(\mathbf{i} - 2\mathbf{j} - \mathbf{k}) = 3$						
	Find						
	(a) a vector equation of the line <i>l</i> ,						
		(2)					
	(b) the position vector of the point where $l$ meets $\Pi$ .	(4)					
	(c) Hence find the perpendicular distance of $P$ from $\Pi$ .						
		(2)					



2.

$$\mathbf{M} = \begin{pmatrix} 1 & 0 & 2 \\ 0 & 4 & 1 \\ 0 & 5 & 0 \end{pmatrix}$$

(a) Show that matrix **M** is not orthogonal.

**(2)** 

(b) Using algebra, show that 1 is an eigenvalue of  $\mathbf{M}$  and find the other two eigenvalues of  $\mathbf{M}$ .

**(5)** 

(c) Find an eigenvector of  $\mathbf{M}$  which corresponds to the eigenvalue 1

**(2)** 

The transformation  $M: \mathbb{R}^3 \to \mathbb{R}^3$  is represented by the matrix **M**.

(d) Find a cartesian equation of the image, under this transformation, of the line

$$x = \frac{y}{2} = \frac{z}{-1}$$

**(4)** 



estion 2 continued		

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3. Using calculus, find the exact value of

(a)	<sup>2</sup> _	1	dx
(a)	$\int_{1}^{1}$	$\sqrt{(x^2-2x+3)}$	· u.i

(4)

(b)	$\int_{0}^{1} e^{2x}$	sinh x	dχ
(-)	<b>J</b> 0 -		

**(4)** 




nestion 3 continued	



1. Using the definitions of hyperbolic functions in terms of exponentials,						
(a)	show that	$\operatorname{sech}^2 x = 1 - \tanh^2 x$	(3)			
(b)	solve the equation	$4\sinh x - 3\cosh x = 3$	(4)			



5. Given that  $y = \operatorname{artanh} \frac{x}{\sqrt{1 + x^2}}$ 

show that	$dy_{\perp}$	1
Show that	$\frac{1}{\mathrm{d}x}$	$\sqrt{(1+x^2)}$

**(4)** 



**6.** [In this question you may use the appropriate trigonometric identities on page 6 of the pink Mathematical Formulae and Statistical Tables.]

The points  $P(3\cos\alpha, 2\sin\alpha)$  and  $Q(3\cos\beta, 2\sin\beta)$ , where  $\alpha \neq \beta$ , lie on the ellipse with equation

$$\frac{x^2}{9} + \frac{y^2}{4} = 1$$

(a) Show the equation of the chord PQ is

$$\frac{x}{3}\cos\frac{(\alpha+\beta)}{2} + \frac{y}{2}\sin\frac{(\alpha+\beta)}{2} = \cos\frac{(\alpha-\beta)}{2}$$

**(4)** 

(b) Write down the coordinates of the mid-point of PQ.

**(1)** 

Given that the gradient, m, of the chord PQ is a constant,

(c) show that the centre of the chord lies on a line

$$y = -kx$$

expressing k in terms of m.

**(5)** 



uestion 6 continued		



7. A circle C with centre O and radius r has cartesian equation  $x^2 + y^2 = r^2$  where r is a constant.

(a) Show that  $1 + \left(\frac{dy}{dx}\right)^2 = \frac{r^2}{r^2 - x^2}$  (3)

(b) Show that the surface area of the sphere generated by rotating C through  $\pi$  radians about the x-axis is  $4\pi r^2$ .

**(5)** 

(c) Write down the length of the arc of the curve  $y = \sqrt{1 - x^2}$  from x = 0 to x = 1

(1)



estion 7 continued	



**8.** The position vectors of the points A, B and C from a fixed origin O are

$$a = i - j$$
,  $b = i + j + k$ ,  $c = 2j + k$ 

respectively.

(a) Using vector products, find the area of the triangle ABC.

**(4)** 

(b) Show that  $\frac{1}{6}\mathbf{a}.(\mathbf{b} \times \mathbf{c}) = 0$ 

**(3)** 

(c) Hence or otherwise, state what can be deduced about the vectors a, b and c.

(1)



uestion 8 continued		



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$$I_n = \int (x^2 + 1)^{-n} \, \mathrm{d}x, \quad n > 0$$

(a) Show that, for n > 0

$$I_{n+1} = \frac{x(x^2+1)^{-n}}{2n} + \frac{2n-1}{2n}I_n$$

**(5)** 

(b)	Find	$I_2$
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**(3)** 






Question 9 continued		
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		<b>Q9</b>
	(Total 8 marks)	
	TOTAL FOR PAPER: 75 MARKS	
END	TOTAL FUN FAFEN: /5 MAKKS	