

Mark Scheme (Final)

January 2008

GCE

GCE Mathematics (6684/01)

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL

190 High Holborn London WC1V 7BH

January 2008

Advanced Subsidiary/Advanced Level

General Certificate of Education

Subject: **Statistics 2**

Paper: S2

Question Number	Marks	Scheme	
1. (a)	A census is when <u>every member</u> of the <u>population</u> is investigated.	B1	
(b)	There would be no cookers left to sell.	B1	
(c)	A list of the unique identification numbers of the cookers.	B1	
(d)	A cooker	B1	
			(4)
Notes			
1. (a)	B1 Need one word from each group (1) <u>Every member /all items / entire /oe</u> (2) <u>population/collection of individuals/sampling frame/oe</u> enumerating the population on its own gets B0		
(b)	B1 Idea of Tests to destruction. Do not accept cheap or quick		
(c)	B1 Idea of list/ register/database of cookers/serial numbers		
(d)	B1 cooker(s) / serial number(s) The sample of 5 cookers or every 400 th cooker gets B1		

2. (a)	<p>Let X be the random variable the number of faulty bolts</p> $P(X \leq 2) - P(X \leq 1) = 0.0355 - 0.0076 \quad \text{or} \quad (0.3)^2 (0.7)^{18} \frac{20!}{18!2!}$ $= 0.0279 \quad \quad \quad = 0.0278$	<p>M1</p> <p>A1</p> <p>(2)</p>
(b)	$1 - P(X \leq 3) = 1 - 0.1071$ $= 0.8929$ <p>or $1 - (0.3)^3 (0.7)^{17} \frac{20!}{17!3!} - (0.3)^2 (0.7)^{18} \frac{20!}{18!2!} - (0.3)(0.7)^{19} \frac{20!}{19!1!} - (0.7)^{20}$</p>	<p>M1</p> <p>A1</p> <p>(2)</p>
(c)	$\frac{10!}{4!6!} (0.8929)^6 (0.1071)^4 = 0.0140.$	<p>M1A1√A1</p> <p>(3)</p>
Notes		
2. (a)	<p>M1 Either attempting to use $P(X \leq 2) - P(X \leq 1)$</p> <p>or attempt to use binomial and find $p(X = 2)$. Must have $(p)^2 (1 - p)^{18} \frac{20!}{18!2!}$, with a value of p</p> <p>A1 awrt 0.0278 or 0.0279.</p>	
(b)	<p>M1 Attempting to find $1 - P(X \leq 3)$</p> <p>A1 awrt 0.893</p>	
(c)	<p>M1 for $k (p)^6 (1 - p)^4$. They may use any value for p and k can be any number or ${}^nC_6 p^6 (1 - p)^{n-6}$</p> <p>A1√ $\frac{10!}{4!6!} (their\ part\ b)^6 (1 - their\ part\ b)^4$ may write ${}^{10}C_6$ or ${}^{10}C_4$</p> <p>A1 awrt 0.014</p>	

3. (a)	<p><u>Events</u> occur at a constant rate. any two of the 3</p> <p><u>Events</u> occur independently or randomly.</p> <p><u>Events</u> occur singly.</p>	B1 B1 (2)
(b)	Let X be the random variable the number of cars passing the observation point.	
(i)	<p>Po(6)</p> $P(X \leq 4) - P(X \leq 3) = 0.2851 - 0.1512 \quad \text{or} \quad \frac{e^{-6} 6^4}{4!}$ $= 0.1339$	B1 M1 A1
(ii)	$1 - P(X \leq 4) = 1 - 0.2851 \quad \text{or} \quad 1 - e^{-6} \left(\frac{6^4}{4!} + \frac{6^3}{3!} + \frac{6^2}{2!} + \frac{6}{1!} + 1 \right)$ $= 0.7149$	M1 A1
(c)	<p>P (0 car and 1 others) + P (1 cars and 0 other)</p> $= e^{-1} \times 2e^{-2} + 1e^{-1} \times e^{-2}$ $= 0.3679 \times 0.2707 + 0.3674 \times 0.1353$ $= 0.0996 + 0.0498$ $= 0.149$ <p><u>alternative</u></p> $P_o(1+2) = P_o(3) \quad \text{B1}$ $P(X=1) = 3e^{-3} \quad \text{M1 A1}$ $= 0.149 \quad \text{A1}$	B1 M1 A1 A1 (5) (4)
Notes 3(a)	<p>B1 B1 Need the word events at least once. Independently and randomly are the same reason. Award the first B1 if they only gain 1 mark Special case. If they have 2 of the 3 lines without the word events they get B0 B1</p>	
(b) (i)	<p>B1 Using Po(6) in (i) or (ii)</p> <p>M1 Attempting to find $P(X \leq 4) - P(X \leq 3)$ or $\frac{e^{-\lambda} \lambda^4}{4!}$</p> <p>A1 awrt 0.134</p>	
(ii)	<p>M1 Attempting to find $1 - P(X \leq 4)$</p> <p>A1 awrt 0.715</p>	

(c)	<p>B1 Attempting to find both possibilities. May be implied by doing $e^{-\lambda_1} \times \lambda_2 e^{-\lambda_2} + e^{-\lambda_2} \times \lambda_1 e^{-\lambda_1}$ any values of λ_1 and λ_2</p> <p>M1 finding one pair of form $e^{-\lambda_1} \times \lambda_2 e^{-\lambda_2}$ any values of λ_1 and λ_2</p> <p>A1 one pair correct</p> <p>A1 awrt 0.149</p> <p>Alternative.</p> <p>B1 for Po(3)</p> <p>M1 for attempting to find $P(X=1)$ with Po(3)</p> <p>A1 $3e^{-3}$</p> <p>A1 awrt 0.149</p>	
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4. (a)	$K(2^4 + 2^2 - 2) = 1$ $K = 1/18$	M1 A1 (2)
(b)	$1 - F(1.5) = 1 - \frac{1}{18}(1.5^4 + 1.5^2 - 2)$ $= 0.705 \quad \text{or} \quad \frac{203}{288}$	M1 A1 (2)
(c)	$f(y) = \begin{cases} \frac{1}{9}(2y^3 + y) & 1 \leq y \leq 2 \\ 0 & \text{otherwise} \end{cases}$	M1 A1 B1 (3)
Notes		
4. (a)	<p>M1 putting $F(2) = 1$ or $F(2) - F(1) = 1$</p> <p>A1 cso. Must show substituting $y = 2$ and the $1/18$</p>	
(b)	<p>M1 either attempting to find $1 - F(1.5)$ may write and use $F(2) - F(1.5)$</p> <p>A1 awrt 0.705</p>	
(c)	<p>M1 attempting to differentiate. Must see either a $y^n \rightarrow y^{n-1}$ at least once</p> <p>A1 for getting $\frac{1}{9}(2y^3 + y)$ o.e and $1 \leq y \leq 2$ allow $1 < y < 2$</p> <p>B1 for the 0 otherwise. Allow 0 for $y < 1$ and 0 for $y > 2$</p> <p>Allow them to use any letter</p>	

5	<p>$H_0 : p = 0.3; H_1 : p > 0.3$</p> <p>Let X represent the number of tomatoes greater than 4 cm : $X \sim B(40, 0.3)$</p> <p> $P(X \geq 18) = 1 - P(X \leq 17)$ $= 0.0320$ </p> <p> $P(X \geq 18) = 1 - P(X \leq 17) = 0.0320$ $P(X \geq 17) = 1 - P(X \leq 16) = 0.0633$ CR $X \geq 18$ </p> <p>$0.0320 < 0.05$ $18 \geq 18$ or 18 in the critical region</p> <p>no evidence to Reject H_0 or it is significant</p> <p>New fertiliser has <u>increased</u> the probability of a <u>tomato</u> being greater than 4 cm Or Dhriti's claim is true</p>	<p>B1 B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>B1d cao (7)</p>
5	<p>B1 for correct H_0 . must use p or pi</p> <p>B1 for correct H_1 must use p and be one tail.</p> <p>B1 using $B(40, 0.3)$. This may be implied by their calculation</p> <p>M1 attempt to find $1 - P(X \leq 17)$ or get a correct probability. For CR method must attempt to find $P(X \geq 18)$ or give the correct critical region</p> <p>A1 awrt 0.032 or correct CR.</p> <p>M1 correct statement based on their probability , H_1 and 0.05 or a correct contextualised statement that implies that.</p> <p>B1 this is not a follow through .conclusion in context. Must use the words increased, tomato and some reference to size or diameter. This is dependent on them getting the previous M1</p> <p>If they do a two tail test they may get B1 B0 B1 M1 A1 M1 B0 For the second M1 they must have accept H_0 or it is not significant or a correct contextualised statement that implies that.</p>	

b)	<p>A1 award for either $\frac{13.5-10}{\sqrt{7.5}}$ or awrt 1.28</p> <p>M1 Finding the correct area. Following on from their 7.5 and 13.5. Need to do a Prob >0.5 – prob <0.5 or prob <0.5 + prob < 0.5</p> <p>A1 awrt 0.718 or 0.719 only. Dependent on them getting all three method marks.</p> <p>No working but correct answer will gain all the marks</p> <p>first B1 normal</p> <p>second B1 p close to half, or mean \neq variance or np and nq both > 5. They may use a number bigger than 5 or they may work out the exact value 0.7148 using the binomial distribution.</p> <p>Do not allow np > 5 and npq > 5</p> <p>A hypothesis test is a mathematical procedure to <u>examine a value of</u></p>	
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7 ai)	<u>a population parameter proposed by the null hypothesis compared with an alternative hypothesis.</u>	B1
ii)	The critical region is the <u>range of values or a test statistic or region where the test is significant</u> that would lead <u>to the rejection of H_0</u> .	B1g B1h (3)
(b)	Let X represent the number of incoming calls : $X \sim \text{Po}(9)$ From table $P(X \geq 16) = 0.0220$ $P(x \leq 3) = 0.0212$ Critical region ($x \leq 3$ or $x \geq 16$)	B1 M1 A1 A1 B1 (5)
(c)	Significance level = $0.0220 + 0.0212$ = 0.0432 or 4.32%	B1 (1)
(d)	$H_0 : \lambda = 0.45$; $H_1 : \lambda < 0.45$ (accept : $H_0 : \lambda = 4.5$; $H_1 : \lambda < 4.5$) Using $X \sim \text{Po}(4.5)$ $P(X \leq 1) = 0.0611$ CR $X \leq 0$ awrt 0.0611 $0.0611 > 0.05$. $1 \geq 0$ or 1 not in the critical region There is evidence to Accept H_0 or it is not significant There is no evidence that there are less calls during school holidays.	B1 M1 A1 M1 B1cao (5)
Notes 7 ai)	B1 Method for deciding between 2 hypothesis.	
ii)	B1 range of values. This may be implied by other words. Not region on its own B1 which lead you to <u>reject H_0</u> Give the first B1 if only one mark awarded.	
(b)	B1 using $P_o(9)$	

	<p>M1 attempting to find $P(X \geq 16)$ or $P(x \leq 3)$</p> <p>A1 0.0220 or $P(X \geq 16)$ A1 0.0212 or $P(x \leq 3)$ These 3 marks may be gained by seeing the numbers in part c</p> <p>B1 correct critical region</p> <p>A completely correct critical region will get all 5 marks. Half of the correct critical region eg $x \leq 3$ or $x \geq 17$ say would get B1 M1 A0 A1 B0 if the M1 A1 A1 not already awarded.</p>	
(c)	<p>B1 cao awrt 0.0432</p>	
(d)	<p>B1 may use λ or μ. Needs both H_0 and H_1</p> <p>M1 using $P_o(4.5)$</p> <p>A1 correct probability or CR only</p> <p>M1 correct statement based on their probability, H_1 and 0.05 or a correct contextualised statement that implies that.</p> <p>B1 this is not a follow through. Conclusion in context. Must see the word calls in conclusion</p> <p>If they get the correct CR with no evidence of using $P_o(4.5)$ they will get M0 A0</p> <p>SC If they get the critical region $X \leq 1$ they score M1 for rejecting H_0 and B1 for concluding the rate of calls in the holiday is lower.</p>	

8. a)	<div data-bbox="300 331 1037 857"> </div> <div data-bbox="1059 353 1318 465"> <p>Max height of 2 labelled and goes through (2,0)</p> </div> <div data-bbox="1059 499 1302 712"> <p>shape must be between 2 and 3 and no other lines drawn (accept patios drawn)</p> </div> <div data-bbox="1091 723 1264 824"> <p>correct shape</p> </div>	<p>B1</p> <p>B1</p> <p>B1</p>
b)	3	<p>(3)</p> <p>B1</p>
c)	$\int_2^3 2x(x-2) dx = \left[\frac{2x^3}{3} - 2x^2 \right]_2^3$ $= 2\frac{2}{3}$	<p>M1A1</p> <p>A1</p> <p>(3)</p>
d)	$\int_2^m 2(x-2) dx = 0.5$ $\left[x^2 - 4x \right]_2^m = 0.5$ $m^2 - 4m + 4 = 0.5$ $m^2 - 4m + 3.5 = 0$ $m = \frac{4 \pm \sqrt{2}}{2}$ $m = 2.71$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(4)</p>
e)	<p>Negative skew. mean < median < mode .</p>	<p>B1</p> <p>B1dep</p> <p>(2)</p>

Notes 8.		
(a)	<p>B1 the graph must have a maximum of 2 which must be labelled</p> <p>B1 the line must be between 2 and 3 with not other line drawn except patios. They can get this mark even if the patio cannot be seen.</p> <p>B1 the line must be straight and the right shape.</p>	
(b)	<p>B1 Only accept 3</p>	
(c)	<p>M1 attempt to find $\int xf(x)dx$ for attempt we need to see $x^n \rightarrow x^{n+1}$. ignore limits</p> <p>A1 correct integration ignore limits</p> <p>A1 accept $2\frac{2}{3}$ or awrt 2.67 or $2.\dot{6}$</p>	
(d)	<p>M1 using $\int f(x)dx=0.5$</p> <p>A1 $m^2 - 4m + 4 = 0.5$ oe</p> <p>M1 attempting to solve quadratic.</p> <p>A1 awrt 2.71 or $\frac{4 + \sqrt{2}}{2}$ or $2 + \frac{\sqrt{2}}{2}$ oe</p>	
(e)	<p>First B1 for negative</p> <p>Second B1 for mean < median < mode. Need all 3 or may explain using diagram.</p>	