

Mark Scheme (Results) January 2010

GCE

GCE Core Mathematics C4 (6666/01)



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January 2010
Publications Code UA022713
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January 2010 6666 Core Mathematics C4 Mark Scheme

Question Number	Scheme	Marks	
Q1	(a) $(1-8x)^{\frac{1}{2}} = 1 + (\frac{1}{2})(-8x) + \frac{(\frac{1}{2})(-\frac{1}{2})}{2}(-8x)^2 + \frac{(\frac{1}{2})(-\frac{1}{2})(-\frac{3}{2})}{3!}(-8x)^3 + \dots$ = $1-4x-8x^2; -32x^3 - \dots$	M1 A1 A1; A1	(4)
	(b) $\sqrt{(1-8x)} = \sqrt{(1-\frac{8}{100})}$ = $\sqrt{\frac{92}{100}} = \sqrt{\frac{23}{25}} = \frac{\sqrt{23}}{5}$ * cso	M1 A1	(2)
	$\sqrt{100} \sqrt{25} 5$ (c) $1-4x-8x^2-32x^3=1-4(0.01)-8(0.01)^2-32(0.01)^3$ $=1-0.04-0.0008-0.000032=0.959168$	M1	, ,
	$\sqrt{23} = 5 \times 0.959168$ = 4.795 84 cao	M1 A1	(3) [9]

Question Number	Scheme	Marks	
Q2	(a) 1.386, 2.291 awrt 1.386, 2.291	B1 B1 (2))
	(b) $A \approx \frac{1}{2} \times 0.5$ ()	B1	
	$= \dots \left(0 + 2\left(0.608 + 1.386 + 2.291 + 3.296 + 4.385\right) + 5.545\right)$	M1	
	= 0.25(0+2(0.608+1.386+2.291+3.296+4.385)+5.545) ft their (a)	A1ft	
	$=0.25 \times 29.477 \dots \approx 7.37$ cao	A1 (4	1)
	(c)(i) $\int x \ln x dx = \frac{x^2}{2} \ln x - \int \frac{x^2}{2} \times \frac{1}{x} dx$ $= \frac{x^2}{2} \ln x - \int \frac{x}{2} dx$	M1 A1	
	$= \frac{x^2}{2} \ln x - \frac{x^2}{4} \ (+C)$	M1 A1	
	(ii) $\left[\frac{x^2}{2}\ln x - \frac{x^2}{4}\right]_1^4 = \left(8\ln 4 - 4\right) - \left(-\frac{1}{4}\right)$	M1	
	$=8\ln 4 - \frac{15}{4}$		
	$=8(2\ln 2)-\frac{15}{4} \qquad \ln 4 = 2\ln 2 \text{ seen or implied}$	M1	
	$= \frac{1}{4} (64 \ln 2 - 15) \qquad a = 64, b = -15$	A1 (7	7)
	4	[13	3]

Question Number	Scheme	Marks	
Q3	(a) $-2\sin 2x - 3\sin 3y \frac{dy}{dx} = 0$ $\frac{dy}{dx} = -\frac{2\sin 2x}{3\sin 3y}$ Accept $\frac{2\sin 2x}{-3\sin 3y}$, $\frac{-2\sin 2x}{3\sin 3y}$	M1 A1	(3)
	(b) At $x = \frac{\pi}{6}$, $\cos\left(\frac{2\pi}{6}\right) + \cos 3y = 1$ $\cos 3y = \frac{1}{2}$ $3y = \frac{\pi}{3} \Rightarrow y = \frac{\pi}{9}$ awrt 0.349	M1 A1 A1	(3)
	(c) At $\left(\frac{\pi}{6}, \frac{\pi}{9}\right)$, $\frac{dy}{dx} = -\frac{2\sin 2\left(\frac{\pi}{6}\right)}{3\sin 3\left(\frac{\pi}{9}\right)} = -\frac{2\sin \frac{\pi}{3}}{3\sin \frac{\pi}{3}} = -\frac{2}{3}$ $y - \frac{\pi}{9} = -\frac{2}{3}\left(x - \frac{\pi}{6}\right)$ Leading to $6x + 9y - 2\pi = 0$		(3) [9]

Question Number	Scheme	Marks	
Q4	(a) $A: (-6, 4, -1)$ Accept vector forms	B1 (1	1)
	(b) $\begin{pmatrix} 4 \\ -1 \\ 3 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ -4 \\ 1 \end{pmatrix} = 12 + 4 + 3 = \sqrt{4^2 + (-1)^2 + 3^2} \sqrt{3^2 + (-4)^2 + 1^2} \cos \theta$	M1 A1	
	$\cos \theta = \frac{19}{26}$ awrt 0.73	A1 (3	3)
	(c) X : $(10, 0, 11)$ Accept vector forms	B1 (1	1)
	(d) $\overrightarrow{AX} = \begin{pmatrix} 10\\0\\11 \end{pmatrix} - \begin{pmatrix} -6\\4\\-1 \end{pmatrix}$ Either order	M1	
	$= \begin{pmatrix} 16 \\ -4 \\ 12 \end{pmatrix} $ cao	A1 (2	2)
	(e) $ \overrightarrow{AX} = \sqrt{16^2 + (-4)^2 + 12^2}$	M1	
	$= \sqrt{416} = \sqrt{16 \times 26} = 4\sqrt{26} * \text{Do not penalise if consistent incorrect signs in (d)}$	A1 (2	2)
	(f) $ \frac{4\sqrt{26}}{A} = \cos \theta $ Use of correct right angled triangle $ \frac{ \overrightarrow{AX} }{d} = \cos \theta $ $ d = \frac{4\sqrt{26}}{\frac{19}{26}} \approx 27.9 \text{awrt } 27.9 $	M1 M1 A1 (3	

Question Number	Scheme	Marks	
Q5	(a) $\int \frac{9x+6}{x} dx = \int \left(9 + \frac{6}{x}\right) dx$ $= 9x + 6 \ln x \ (+C)$	M1 A1	(2)
	(b) $\int \frac{1}{y^{\frac{1}{3}}} dy = \int \frac{9x+6}{x} dx$ Integral signs not necessary	B1	
	$\int y^{-\frac{1}{3}} dy = \int \frac{9x+6}{x} dx$ $\frac{y^{\frac{2}{3}}}{\frac{2}{3}} = 9x + 6\ln x \ (+C)$ $\pm ky^{\frac{2}{3}} = \text{their (a)}$	M1	
	$\frac{3}{2}y^{\frac{2}{3}} = 9x + 6\ln x \ (+C)$ ft their (a)	A1ft	
	$\frac{3}{2}8^{\frac{2}{3}} = 9 + 6\ln 1 + C$	M1	
	$C = -3$ $y^{\frac{2}{3}} = \frac{2}{3} (9x + 6 \ln x - 3)$	A1	
	$y^{2} = (6x + 4\ln x - 2)^{3} \left(= 8(3x + 2\ln x - 1)^{3} \right)$	A1	(6) [8]

Question Number	Scheme	Marks
Q6	$\frac{\mathrm{d}A}{\mathrm{d}t} = 1.5$	B1
	$A = \pi r^2 \implies \frac{\mathrm{d}A}{\mathrm{d}r} = 2\pi r$	B1
	When $A = 2$	
	$2 = \pi r^2 \implies r = \sqrt{\frac{2}{\pi}} \ (= 0.797 \ 884 \dots)$	M1
	$\frac{\mathrm{d}A}{\mathrm{d}t} = \frac{\mathrm{d}A}{\mathrm{d}r} \times \frac{\mathrm{d}r}{\mathrm{d}t}$	
	$1.5 = 2\pi r \frac{\mathrm{d}r}{\mathrm{d}t}$	M1
	$\frac{\mathrm{d}r}{\mathrm{d}t} = \frac{1.5}{2\pi\sqrt{\frac{2}{\pi}}} \approx 0.299$ awrt 0.299	A1
		[5]

Question Number	Scheme	Marks	
Q7	(a) $y = 0 \Rightarrow t(9-t^2) = t(3-t)(3+t) = 0$ t = 0, 3, -3 Any one correct value At $t = 0$, $x = 5(0)^2 - 4 = -4$ Method for finding one value of x At $t = 3$, $x = 5(3)^2 - 4 = 41$	B1 M1	
	(At $t = -3$, $x = 5(-3)^2 - 4 = 41$) At A , $x = -4$; at B , $x = 41$ Both (b) $\frac{dx}{dt} = 10t$ Seen or implied	A1 B1	(3)
	$\int y dx = \int y \frac{dx}{dt} dt = \int t \left(9 - t^2\right) 10t dt$ $= \int \left(90t^2 - 10t^4\right) dt$	M1 A1	
	$= \frac{90t^3}{3} - \frac{10t^5}{5} (+C) \qquad (=30t^3 - 2t^5 (+C))$	A1	
	$\left[\frac{90t^3}{3} - \frac{10t^5}{5}\right]_0^3 = 30 \times 3^3 - 2 \times 3^5 (=324)$	M1	
	$A = 2\int y \mathrm{d}x = 648 \left(\mathrm{units}^2\right)$		(6) [9]

Question Number	Scheme	Marks
Q8	(a) $\frac{\mathrm{d}x}{\mathrm{d}u} = -2\sin u$	B1
	$\int \frac{1}{x^2 \sqrt{4 - x^2}} dx = \int \frac{1}{(2\cos u)^2 \sqrt{4 - (2\cos u)^2}} \times -2\sin u du$	M1
	$= \int \frac{-2\sin u}{4\cos^2 u \sqrt{4\sin^2 u}} du \qquad \text{Use of } 1 - \cos^2 u = \sin^2 u$	M1
	$= -\frac{1}{4} \int \frac{1}{\cos^2 u} du \qquad \pm k \int \frac{1}{\cos^2 u} du$	M1
	$= -\frac{1}{4} \tan u \ \left(+C\right) \qquad \qquad \pm k \tan u$	M1
	$x = \sqrt{2} \implies \sqrt{2} = 2\cos u \implies u = \frac{\pi}{4}$	
	$x=1 \implies 1=2\cos u \implies u=\frac{\pi}{3}$	M1
	$\left[-\frac{1}{4} \tan u \right]_{\frac{\pi}{3}}^{\frac{\pi}{4}} = -\frac{1}{4} \left(\tan \frac{\pi}{4} - \tan \frac{\pi}{3} \right)$	
	$=-\frac{1}{4}\left(1-\sqrt{3}\right) \left(=\frac{\sqrt{3}-1}{4}\right)$	A1 (7)
	(b) $V = \pi \int_{1}^{\sqrt{2}} \left(\frac{4}{x(4-x^2)^{\frac{1}{4}}} \right)^2 dx$	M1
	$=16\pi \int_{1}^{\sqrt{2}} \frac{1}{x^2 \sqrt{4-x^2}} dx$ 16\pi \text{ integral in (a)}	M1
	$=16\pi\left(\frac{\sqrt{3}-1}{4}\right)$ 16\pi \text{ their answer to part (a)}	A1ft (3)
		[10]

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Order Code UA022713 January 2010

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