

TR29124 C++ Special Math Functions

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Chapter 1

Mathematical Special Functions

1.1 Introduction and History

The first significant library upgrade on the road to C++2011, [TR1](#), included a set of 23 mathematical functions that significantly extended the standard transcendental functions inherited from C and declared in `<cmath>`.

Although most components from TR1 were eventually adopted for C++11 these math functions were left behind out of concern for implementability. The math functions were published as a separate international standard [IS 29124 - Extensions to the C++ Library to Support Mathematical Special Functions](#).

For C++17 these functions were incorporated into the main standard.

1.2 Contents

The following functions are implemented in namespace `std`:

- [assoc_laguerre](#) - Associated Laguerre functions
- [assoc_legendre](#) - Associated Legendre functions
- [beta](#) - Beta functions
- [comp_ellint_1](#) - Complete elliptic functions of the first kind
- [comp_ellint_2](#) - Complete elliptic functions of the second kind
- [comp_ellint_3](#) - Complete elliptic functions of the third kind
- [cyl_bessel_i](#) - Regular modified cylindrical Bessel functions
- [cyl_bessel_j](#) - Cylindrical Bessel functions of the first kind
- [cyl_bessel_k](#) - Irregular modified cylindrical Bessel functions
- [cyl_neumann](#) - Cylindrical Neumann functions or Cylindrical Bessel functions of the second kind
- [ellint_1](#) - Incomplete elliptic functions of the first kind

- [ellint_2](#) - Incomplete elliptic functions of the second kind
- [ellint_3](#) - Incomplete elliptic functions of the third kind
- [expint](#) - The exponential integral
- [hermite](#) - Hermite polynomials
- [laguerre](#) - Laguerre functions
- [legendre](#) - Legendre polynomials
- [riemann_zeta](#) - The Riemann zeta function
- [sph_bessel](#) - Spherical Bessel functions
- [sph_legendre](#) - Spherical Legendre functions
- [sph_neumann](#) - Spherical Neumann functions

The hypergeometric functions were stricken from the TR29124 and C++17 versions of this math library because of implementation concerns. However, since they were in the TR1 version and since they are popular we kept them as an extension in namespace `__gnu_cxx`:

- [conf_hyperg](#) - Confluent hypergeometric functions
- [hyperg](#) - Hypergeometric functions

In addition a large number of new functions are added as extensions:

- [airy_ai](#) - Airy functions of the first kind
- [airy_bi](#) - Airy functions of the second kind
- [bincoef](#) - Binomial coefficients
- [bose_einstein](#) - Bose-Einstein integrals
- [chebyshev_t](#) - Chebyshev polynomials of the first kind
- [chebyshev_u](#) - Chebyshev polynomials of the second kind
- [chebyshev_v](#) - Chebyshev polynomials of the third kind
- [chebyshev_w](#) - Chebyshev polynomials of the fourth kind
- [clausen](#) - Clausen integrals
- [clausen_c](#) - Clausen cosine integrals
- [clausen_s](#) - Clausen sine integrals
- [comp_ellint_d](#) - Incomplete Legendre D elliptic integral
- [conf_hyperg_lim](#) - Confluent hypergeometric limit functions
- [cos_pi](#) - Reperiodized cosine function.
- [cosh_pi](#) - Reperiodized hyperbolic cosine function.
- [coshint](#) - Hyperbolic cosine integral

- [cosint](#) - Cosine integral
- [cyl_hankel_1](#) - Cylindrical Hankel functions of the first kind
- [cyl_hankel_2](#) - Cylindrical Hankel functions of the second kind
- [dawson](#) - Dawson integrals
- [dilog](#) - Dilogarithm functions
- [dirichlet_beta](#) - Dirichlet beta function
- [dirichlet_eta](#) - Dirichlet beta function
- [dirichlet_lambda](#) - Dirichlet lambda function
- [double_factorial](#) -
- [ellint_d](#) - Legendre D elliptic integrals
- [ellint_rc](#) - Carlson elliptic functions R_C
- [ellint_rd](#) - Carlson elliptic functions R_D
- [ellint_rf](#) - Carlson elliptic functions R_F
- [ellint_rg](#) - Carlson elliptic functions R_G
- [ellint_rj](#) - Carlson elliptic functions R_J
- [ellnome](#) - Elliptic nome
- [expint](#) - Exponential integrals
- [factorial](#) - Factorials
- [fermi_dirac](#) - Fermi-Dirac integrals
- [fresnel_c](#) - Fresnel cosine integrals
- [fresnel_s](#) - Fresnel sine integrals
- [gegenbauer](#) - Gegenbauer polynomials
- [heuman_lambda](#) - Heuman lambda functions
- [hurwitz_zeta](#) - Hurwitz zeta functions
- [ibeta](#) - Regularized incomplete beta functions
- [jacobi](#) - Jacobi polynomials
- [jacobi_sn](#) - Jacobi sine amplitude functions
- [jacobi_cn](#) - Jacobi cosine amplitude functions
- [jacobi_dn](#) - Jacobi delta amplitude functions
- [jacobi_zeta](#) - Jacobi zeta functions
- [lbincoef](#) - Log binomial coefficients
- [ldouble_factorial](#) - Log double factorials
- [legendre_q](#) - Legendre functions of the second kind

- `lfactorial` - Log factorials
- `lgamma` - Log gamma for complex arguments
- `lpochhammer_lower` - Log lower Pochhammer functions
- `lpochhammer` - Log upper Pochhammer functions
- `owens_t` - Owens T functions
- `pgamma` - Regularized lower incomplete gamma functions
- `pochhammer_lower` - Lower Pochhammer functions
- `pochhammer` - Upper Pochhammer functions
- `psi` - Psi or digamma function
- `qgamma` - Regularized upper incomplete gamma functions
- `radpoly` - Radial polynomials
- `sinhc` - Hyperbolic sinus cardinal function
- `sinhc_pi` -
- `sinc` - Normalized sinus cardinal function
- `sincos` - Sine + cosine function
- `sincos_pi` - Reperiodized sine + cosine function
- `sin_pi` - Reperiodized sine function.
- `sinh_pi` - Reperiodized hyperbolic sine function.
- `sinc_pi` - Sinus cardinal function
- `sinhint` - Hyperbolic sine integral
- `sinint` - Sine integral
- `sph_bessel_i` - Spherical regular modified Bessel functions
- `sph_bessel_k` - Spherical irregular modified Bessel functions
- `sph_hankel_1` - Spherical Hankel functions of the first kind
- `sph_hankel_2` - Spherical Hankel functions of the first kind
- `sph_harmonic` - Spherical
- `tan_pi` - Reperiodized tangent function.
- `tanh_pi` - Reperiodized hyperbolic tangent function.
- `tgamma` - Gamma for complex arguments
- `tgamma` - Upper incomplete gamma functions
- `tgamma_lower` - Lower incomplete gamma functions
- `theta_1` - Exponential theta function 1
- `theta_2` - Exponential theta function 2
- `theta_3` - Exponential theta function 3
- `theta_4` - Exponential theta function 4
- `zernike` - Zernike polynomials

1.3 General Features

1.3.1 Argument Promotion

The arguments supplied to the non-suffixed functions will be promoted according to the following rules:

1. If any argument intended to be floating point is given an integral value That integral value is promoted to double.
2. All floating point arguments are promoted up to the largest floating point precision among them.

1.3.2 NaN Arguments

If any of the floating point arguments supplied to these functions is invalid or NaN (`std::numeric_limits<Tp>::quiet_NaN`), the value NaN is returned.

1.4 Implementation

We strive to implement the underlying math with type generic algorithms to the greatest extent possible. In practice, the functions are thin wrappers that dispatch to function templates. Type dependence is controlled with `std::numeric_limits` and functions thereof.

We don't promote `float` to `double` or `double` to `long double` reflexively. The goal is for `float` functions to operate more quickly, at the cost of `float` accuracy and possibly a smaller domain of validity. Similarly, `long double` should give you more dynamic range and slightly more precision than `double` on many systems.

1.5 Testing

These functions have been tested against equivalent implementations from the [Gnu Scientific Library](http://www.gnu.org/software/scientific/), [GSL](http://www.boost.org/doc/libs/1_60_0/libs/math/doc/html/index.html) and [Boost](http://www.boost.org/doc/libs/1_60_0/libs/math/doc/html/index.html) and the ratio

$$\frac{|f - f_{test}|}{|f_{test}|}$$

is generally found to be within 10^{-15} for 64-bit double on linux-x86_64 systems over most of the ranges of validity.

Todo Provide accuracy comparisons on a per-function basis for a small number of targets.

1.6 General Bibliography

See also

Abramowitz and Stegun: Handbook of Mathematical Functions, with Formulas, Graphs, and Mathematical Tables
Edited by Milton Abramowitz and Irene A. Stegun, National Bureau of Standards Applied Mathematics Series - 55
Issued June 1964, Tenth Printing, December 1972, with corrections Electronic versions of A&S abound including
both pdf and navigable html.

for example <http://people.math.sfu.ca/~cbm/aands/>

The old A&S has been redone as the NIST Digital Library of Mathematical Functions: <http://dlmf.nist.gov/>↵
This version is far more navigable and includes more recent work.

An Atlas of Functions: with Equator, the Atlas Function Calculator 2nd Edition, by Oldham, Keith B., Myland, Jan,
Spanier, Jerome

Asymptotics and Special Functions by Frank W. J. Olver, Academic Press, 1974

Numerical Recipes in C, The Art of Scientific Computing, by William H. Press, Second Ed., Saul A. Teukolsky,
William T. Vetterling, and Brian P. Flannery, Cambridge University Press, 1992

The Special Functions and Their Approximations: Volumes 1 and 2, by Yudell L. Luke, Academic Press, 1969

Chapter 2

Todo List

page [Mathematical Special Functions](#)

Provide accuracy comparisons on a per-function basis for a small number of targets.

Member [std::__detail::__dawson_cont_frac](#) ([_Tp __x](#))

this needs some compile-time construction!

Member [std::__detail::__expint](#) ([unsigned int __n](#), [_Tp __x](#))

Study arbitrary switch to large-n $E_n(x)$.

Find a good asymptotic switch point in $E_n(x)$.

Find a good asymptotic switch point in $E_n(x)$.

Member [std::__detail::__expint_E1](#) ([_Tp __x](#))

Find a good asymptotic switch point in $E_1(x)$.

Member [std::__detail::__expint_En_recursion](#) ([unsigned int __n](#), [_Tp __x](#))

Find a principled starting number for the $E_n(x)$ downward recursion.

Member [std::__detail::__hurwitz_zeta_polylog](#) ([_Tp __s](#), [std::complex<_Tp> __a](#))

This [__hurwitz_zeta_polylog](#) prefactor is prone to overflow. positive integer orders s?

Member [std::__detail::__Airy_asymp<_Tp>::__S_absarg_lt_pio3](#) ([_Cmplx __z](#)) const

Revisit these numbers of terms for the Airy asymptotic expansions.

Member [std::__detail::__Airy_series<_Tp>::__S_Scorer](#) ([_Cmplx __t](#))

Find out what is wrong with the $H_i = f_{ai} + g_{ai} + h_{ai}$ scorer function.

Chapter 3

Module Index

3.1 Modules

Here is a list of all modules:

C++ Mathematical Special Functions	19
C++17/IS29124 Mathematical Special Functions	20
GNU Extended Mathematical Special Functions	45

Chapter 4

Namespace Index

4.1 Namespace List

Here is a list of all namespaces with brief descriptions:

__gnu_cxx	145
std	154
std::__detail	156

Chapter 5

Hierarchical Index

5.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

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<code>std::__detail::__gamma_lanczos_data< _Tp ></code>	298
<code>std::__detail::__gamma_lanczos_data< double ></code>	298
<code>std::__detail::__gamma_lanczos_data< float ></code>	299
<code>std::__detail::__gamma_lanczos_data< long double ></code>	300
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Chapter 6

Class Index

6.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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std::__detail::__gamma_lanczos_data< _Tp >	298
std::__detail::__gamma_lanczos_data< double >	298
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std::__detail::__AiryAuxilliaryState< _Tp >	323
std::__detail::__AiryState< _Tp >	324
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Chapter 7

File Index

7.1 File List

Here is a list of all files with brief descriptions:

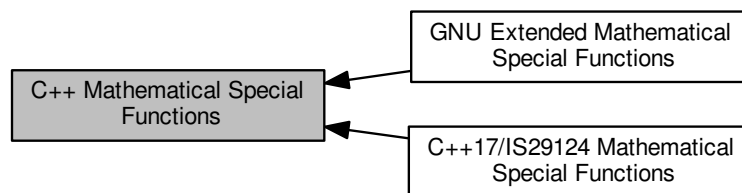
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bits/sf_cardinal.tcc	335
bits/sf_chebyshev.tcc	337
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bits/sf_ellint.tcc	342
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Chapter 8

Module Documentation

8.1 C++ Mathematical Special Functions

Collaboration diagram for C++ Mathematical Special Functions:



Modules

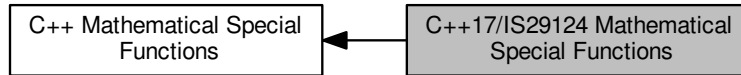
- [C++17/IS29124 Mathematical Special Functions](#)
- [GNU Extended Mathematical Special Functions](#)

8.1.1 Detailed Description

A collection of advanced mathematical special functions.

8.2 C++17/IS29124 Mathematical Special Functions

Collaboration diagram for C++17/IS29124 Mathematical Special Functions:



Functions

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::assoc_laguerre` (unsigned int __n, unsigned int __m, _Tp __x)
- `float std::assoc_laguerref` (unsigned int __n, unsigned int __m, float __x)
- `long double std::assoc_laguerrel` (unsigned int __n, unsigned int __m, long double __x)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::assoc_legendre` (unsigned int __l, unsigned int __m, _Tp __x)
- `float std::assoc_legendref` (unsigned int __l, unsigned int __m, float __x)
- `long double std::assoc_legendrel` (unsigned int __l, unsigned int __m, long double __x)
- `template<typename _Tpa, typename _Tpb >`
`__gnu_cxx::__promote_fp_t< _Tpa, _Tpb > std::beta` (_Tpa __a, _Tpb __b)
- `float std::betaf` (float __a, float __b)
- `long double std::betal` (long double __a, long double __b)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::comp_ellint_1` (_Tp __k)
- `float std::comp_ellint_1f` (float __k)
- `long double std::comp_ellint_1l` (long double __k)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::comp_ellint_2` (_Tp __k)
- `float std::comp_ellint_2f` (float __k)
- `long double std::comp_ellint_2l` (long double __k)
- `template<typename _Tp, typename _Tpn >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpn > std::comp_ellint_3` (_Tp __k, _Tpn __nu)
- `float std::comp_ellint_3f` (float __k, float __nu)
- *Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for float modulus k .*
- `long double std::comp_ellint_3l` (long double __k, long double __nu)
- *Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for long double modulus k .*
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_i` (_Tpnu __nu, _Tp __x)
- `float std::cyl_bessel_if` (float __nu, float __x)
- `long double std::cyl_bessel_il` (long double __nu, long double __x)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_j` (_Tpnu __nu, _Tp __x)
- `float std::cyl_bessel_jf` (float __nu, float __x)
- `long double std::cyl_bessel_jl` (long double __nu, long double __x)

- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_k (_Tpnu __nu, _Tp __x)`
- `float std::cyl_bessel_kf (float __nu, float __x)`
- `long double std::cyl_bessel_kl (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_neumann (_Tpnu __nu, _Tp __x)`
- `float std::cyl_neumannf (float __nu, float __x)`
- `long double std::cyl_neumannl (long double __nu, long double __x)`
- `template<typename _Tp, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpp > std::ellint_1 (_Tp __k, _Tpp __phi)`
- `float std::ellint_1f (float __k, float __phi)`
- `long double std::ellint_1l (long double __k, long double __phi)`
- `template<typename _Tp, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpp > std::ellint_2 (_Tp __k, _Tpp __phi)`
- `float std::ellint_2f (float __k, float __phi)`
Return the incomplete elliptic integral of the second kind $E(k, \phi)$ for float argument.
- `long double std::ellint_2l (long double __k, long double __phi)`
Return the incomplete elliptic integral of the second kind $E(k, \phi)$.
- `template<typename _Tp, typename _Tpn, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpn, _Tpp > std::ellint_3 (_Tp __k, _Tpn __nu, _Tpp __phi)`
Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.
- `float std::ellint_3f (float __k, float __nu, float __phi)`
Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ for float argument.
- `long double std::ellint_3l (long double __k, long double __nu, long double __phi)`
Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::expint (_Tp __x)`
- `float std::expintf (float __x)`
- `long double std::expintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::hermite (unsigned int __n, _Tp __x)`
- `float std::hermitef (unsigned int __n, float __x)`
- `long double std::hermitel (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::laguerre (unsigned int __n, _Tp __x)`
- `float std::laguerref (unsigned int __n, float __x)`
- `long double std::laguerrel (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::legendre (unsigned int __l, _Tp __x)`
- `float std::legendref (unsigned int __l, float __x)`
- `long double std::legendrel (unsigned int __l, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::riemann_zeta (_Tp __s)`
- `float std::riemann_zetaf (float __s)`
- `long double std::riemann_zetal (long double __s)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::sph_bessel (unsigned int __n, _Tp __x)`
- `float std::sph_besself (unsigned int __n, float __x)`
- `long double std::sph_bessell (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta)`

- float [std::sph_legendref](#) (unsigned int __l, unsigned int __m, float __theta)
- long double [std::sph_legendrel](#) (unsigned int __l, unsigned int __m, long double __theta)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t<_Tp> [std::sph_neumann](#) (unsigned int __n, _Tp __x)
- float [std::sph_neumannf](#) (unsigned int __n, float __x)
- long double [std::sph_neumannl](#) (unsigned int __n, long double __x)

8.2.1 Detailed Description

A collection of advanced mathematical special functions for C++17 and IS29124.

8.2.2 Function Documentation

8.2.2.1 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::assoc_laguerre (unsigned int __n, unsigned int __m, _Tp __x) [inline]`

Return the associated Laguerre polynomial $L_n^m(x)$ of nonnegative order n , nonnegative degree m and real argument x .

The associated Laguerre function of real degree α , $L_n^\alpha(x)$, is defined by

$$L_n^\alpha(x) = \frac{(\alpha+1)_n}{n!} {}_1F_1(-n; \alpha+1; x)$$

where $(\alpha)_n$ is the Pochhammer symbol and ${}_1F_1(a; c; x)$ is the confluent hypergeometric function.

The associated Laguerre polynomial is defined for integral degree $\alpha = m$ by:

$$L_n^m(x) = (-1)^m \frac{d^m}{dx^m} L_{n+m}(x)$$

where the Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

and $x \geq 0$.

See also

[laguerre](#) for details of the Laguerre function of degree n

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

\leftrightarrow __n	The order of the Laguerre function, __n >= 0.
\leftrightarrow __m	The degree of the Laguerre function, __m >= 0.
\leftrightarrow __x	The argument of the Laguerre function, __x >= 0.

Exceptions

<code>std::domain_error</code>	if __x < 0.
--------------------------------	-------------

Definition at line 390 of file specfun.h.

8.2.2.2 `float std::assoc_laguerref (unsigned int __n, unsigned int __m, float __x) [inline]`

Return the associated Laguerre polynomial $L_n^m(x)$ of order n , degree m , and `float` argument x .

See also

[assoc_laguerre](#) for more details.

Definition at line 342 of file specfun.h.

8.2.2.3 `long double std::assoc_laguerrel (unsigned int __n, unsigned int __m, long double __x) [inline]`

Return the associated Laguerre polynomial $L_n^m(x)$ of order n , degree m and `long double` argument x .

See also

[assoc_laguerre](#) for more details.

Definition at line 353 of file specfun.h.

8.2.2.4 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::assoc_legendre (unsigned int __l, unsigned int __m, _Tp __x) [inline]`

Return the associated Legendre function $P_l^m(x)$ of degree l , order m , and real argument x .

The associated Legendre function is derived from the Legendre function $P_l(x)$ by the Rodrigues formula:

$$P_l^m(x) = (1 - x^2)^{m/2} \frac{d^m}{dx^m} P_l(x)$$

See also

[legendre](#) for details of the Legendre function of degree 1

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__l</code>	The degree <code>__l >= 0</code> .
<code>__m</code>	The order <code>__m <= 1</code> .
<code>__x</code>	The argument, <code>abs (__x) <= 1</code> .

Exceptions

<code>std::domain_error</code>	if <code>abs (__x) > 1</code> .
--------------------------------	------------------------------------

Definition at line 438 of file `specfun.h`.

8.2.2.5 `float std::assoc_legendref (unsigned int __l, unsigned int __m, float __x) [inline]`

Return the associated Legendre function $P_l^m(x)$ of degree l , order m , and `float` argument x .

See also

[assoc_legendre](#) for more details.

Definition at line 405 of file `specfun.h`.

8.2.2.6 `long double std::assoc_legendrel (unsigned int __l, unsigned int __m, long double __x) [inline]`

Return the associated Legendre function $P_l^m(x)$ of degree l , order m , and `long double` argument x .

See also

[assoc_legendre](#) for more details.

Definition at line 416 of file `specfun.h`.

8.2.2.7 `template<typename _Tpa, typename _Tpb> __gnu_cxx::__promote_fp_t<_Tpa, _Tpb> std::beta (_Tpa __a, _Tpb __b) [inline]`

Return the beta function, $B(a, b)$, for real parameters a, b .

The beta function is defined by

$$B(a, b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$$

where $a > 0$ and $b > 0$

Template Parameters

<code>_Tpa</code>	The floating-point type of the parameter <code>__a</code> .
<code>_Tpb</code>	The floating-point type of the parameter <code>__b</code> .

Parameters

<code>__a</code>	The first argument of the beta function, <code>__a > 0</code> .
<code>__b</code>	The second argument of the beta function, <code>__b > 0</code> .

Exceptions

<code>std::domain_error</code>	if <code>__a < 0</code> or <code>__b < 0</code> .
--------------------------------	---

Definition at line 483 of file `specfun.h`.

8.2.2.8 `float std::betaf (float __a, float __b) [inline]`

Return the beta function, $B(a, b)$, for `float` parameters a, b .

See also

[beta](#) for more details.

Definition at line 452 of file `specfun.h`.

8.2.2.9 `long double std::betal (long double __a, long double __b) [inline]`

Return the beta function, $B(a, b)$, for long double parameters a, b .

See also

[beta](#) for more details.

Definition at line 462 of file `specfun.h`.

8.2.2.10 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::comp_ellint_1 (_Tp __k) [inline]`

Return the complete elliptic integral of the first kind $K(k)$ for real modulus k .

The complete elliptic integral of the first kind is defined as

$$K(k) = F(k, \pi/2) = \int_0^{\pi/2} \frac{d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

where $F(k, \phi)$ is the incomplete elliptic integral of the first kind and the modulus $|k| \leq 1$.

See also

[ellint_1](#) for details of the incomplete elliptic function of the first kind.

Template Parameters

<code>_Tp</code>	The floating-point type of the modulus <code>__k</code> .
------------------	---

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
------------------	---

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 531 of file `specfun.h`.

8.2.2.11 `float std::comp_ellint_1f (float __k) [inline]`

Return the complete elliptic integral of the first kind $E(k)$ for `float` modulus k .

See also

[comp_ellint_1](#) for details.

Definition at line 498 of file `specfun.h`.

8.2.2.12 `long double std::comp_ellint_1l (long double __k) [inline]`

Return the complete elliptic integral of the first kind $E(k)$ for `long double` modulus k .

See also

[comp_ellint_1](#) for details.

Definition at line 508 of file `specfun.h`.

8.2.2.13 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::comp_ellint_2 (_Tp __k) [inline]`

Return the complete elliptic integral of the second kind $E(k)$ for real modulus k .

The complete elliptic integral of the second kind is defined as

$$E(k) = E(k, \pi/2) = \int_0^{\pi/2} \sqrt{1 - k^2 \sin^2 \theta} d\theta$$

where $E(k, \phi)$ is the incomplete elliptic integral of the second kind and the modulus $|k| \leq 1$.

See also

[ellint_2](#) for details of the incomplete elliptic function of the second kind.

Template Parameters

<code>_Tp</code>	The floating-point type of the modulus <code>__k</code> .
------------------	---

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
------------------	---

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 578 of file `specfun.h`.

8.2.2.14 `float std::comp_ellint_2f (float __k) [inline]`

Return the complete elliptic integral of the second kind $E(k)$ for `float` modulus k .

See also

[comp_ellint_2](#) for details.

Definition at line 546 of file `specfun.h`.

8.2.2.15 `long double std::comp_ellint_2l (long double __k) [inline]`

Return the complete elliptic integral of the second kind $E(k)$ for `long double` modulus k .

See also

[comp_ellint_2](#) for details.

Definition at line 556 of file `specfun.h`.

8.2.2.16 `template<typename _Tp, typename _Tpn> __gnu_cxx::__promote_fp_t<_Tp, _Tpn> std::comp_ellint_3 (_Tp __k, _Tpn __nu) [inline]`

Return the complete elliptic integral of the third kind $\Pi(k, \nu) = \Pi(k, \nu, \pi/2)$ for real modulus k .

The complete elliptic integral of the third kind is defined as

$$\Pi(k, \nu) = \Pi(k, \nu, \pi/2) = \int_0^{\pi/2} \frac{d\theta}{(1 - \nu \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}}$$

where $\Pi(k, \nu, \phi)$ is the incomplete elliptic integral of the second kind and the modulus $|k| \leq 1$.

See also

[ellint_3](#) for details of the incomplete elliptic function of the third kind.

Template Parameters

<code>_Tp</code>	The floating-point type of the modulus <code>__k</code> .
<code>_Tpnu</code>	The floating-point type of the argument <code>__nu</code> .

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
<code>__nu</code>	The argument

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 629 of file `specfun.h`.

8.2.2.17 `float std::comp_ellint_3f (float __k, float __nu) [inline]`

Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for `float` modulus `k`.

See also

[comp_ellint_3](#) for details.

Definition at line 593 of file `specfun.h`.

8.2.2.18 `long double std::comp_ellint_3l (long double __k, long double __nu) [inline]`

Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for `long double` modulus `k`.

See also

[comp_ellint_3](#) for details.

Definition at line 603 of file `specfun.h`.

8.2.2.19 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> std::cyl_bessel_i (_Tpnu __nu, _Tp __x) [inline]`

Return the regular modified Bessel function $I_\nu(x)$ for real order ν and argument $x \geq 0$.

The regular modified cylindrical Bessel function is:

$$I_\nu(x) = i^{-\nu} J_\nu(ix) = \sum_{k=0}^{\infty} \frac{(x/2)^{\nu+2k}}{k! \Gamma(\nu + k + 1)}$$

Template Parameters

<code>_Tpnu</code>	The floating-point type of the order <code>__nu</code> .
<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .

Parameters

<code>__nu</code>	The order
<code>__x</code>	The argument, <code>__x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 675 of file `specfun.h`.

8.2.2.20 `float std::cyl_bessel_if (float __nu, float __x) [inline]`

Return the regular modified Bessel function $I_\nu(x)$ for `float` order ν and argument $x \geq 0$.

See also

[cyl_bessel_i](#) for setails.

Definition at line 644 of file `specfun.h`.

8.2.2.21 `long double std::cyl_bessel_il (long double __nu, long double __x) [inline]`

Return the regular modified Bessel function $I_\nu(x)$ for `long double` order ν and argument $x \geq 0$.

See also

[cyl_bessel_i](#) for setails.

Definition at line 654 of file `specfun.h`.

8.2.2.22 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> std::cyl_bessel_j (_Tpnu __nu, _Tp __x) [inline]`

Return the Bessel function $J_\nu(x)$ of real order ν and argument $x \geq 0$.

The cylindrical Bessel function is:

$$J_\nu(x) = \sum_{k=0}^{\infty} \frac{(-1)^k (x/2)^{\nu+2k}}{k! \Gamma(\nu + k + 1)}$$

Template Parameters

<code>_Tpnu</code>	The floating-point type of the order <code>__nu</code> .
<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .

Parameters

<code>__nu</code>	The order
<code>__x</code>	The argument, <code>__x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 721 of file `specfun.h`.

8.2.2.23 `float std::cyl_bessel_jf(float __nu, float __x) [inline]`

Return the Bessel function of the first kind $J_\nu(x)$ for `float` order ν and argument $x \geq 0$.

See also

[cyl_bessel_j](#) for setails.

Definition at line 690 of file `specfun.h`.

8.2.2.24 `long double std::cyl_bessel_jl(long double __nu, long double __x) [inline]`

Return the Bessel function of the first kind $J_\nu(x)$ for `long double` order ν and argument $x \geq 0$.

See also

[cyl_bessel_j](#) for setails.

Definition at line 700 of file `specfun.h`.

8.2.2.25 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> std::cyl_bessel_k(_Tpnu __nu, _Tp __x) [inline]`

Return the irregular modified Bessel function $K_\nu(x)$ of real order ν and argument x .

The irregular modified Bessel function is defined by:

$$K_\nu(x) = \frac{\pi I_{-\nu}(x) - I_\nu(x)}{2 \sin \nu \pi}$$

where for integral $\nu = n$ a limit is taken: $\lim_{\nu \rightarrow n}$. For negative argument we have simply:

$$K_{-\nu}(x) = K_\nu(x)$$

Template Parameters

<code>_Tpnu</code>	The floating-point type of the order <code>__nu</code> .
<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .

Parameters

<code>__nu</code>	The order
<code>__x</code>	The argument, <code>__x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 773 of file `specfun.h`.

8.2.2.26 `float std::cyl_bessel_kf(float __nu, float __x) [inline]`

Return the irregular modified Bessel function $K_\nu(x)$ for `float` order ν and argument $x \geq 0$.

See also

[cyl_bessel_k](#) for details.

Definition at line 736 of file `specfun.h`.

8.2.2.27 `long double std::cyl_bessel_kl(long double __nu, long double __x) [inline]`

Return the irregular modified Bessel function $K_\nu(x)$ for `long double` order ν and argument $x \geq 0$.

See also

[cyl_bessel_k](#) for details.

Definition at line 746 of file `specfun.h`.

8.2.2.28 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> std::cyl_neumann(_Tpnu __nu, _Tp __x) [inline]`

Return the Neumann function $N_\nu(x)$ of real order ν and argument $x \geq 0$.

The Neumann function is defined by:

$$N_\nu(x) = \frac{J_\nu(x) \cos \nu\pi - J_{-\nu}(x)}{\sin \nu\pi}$$

where $x \geq 0$ and for integral order $\nu = n$ a limit is taken: $\lim_{\nu \rightarrow n}$.

Template Parameters

<code>_Tpnu</code>	The floating-point type of the order <code>__nu</code> .
<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .

Parameters

<code>__nu</code>	The order
<code>__x</code>	The argument, <code>__x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 821 of file `specfun.h`.

8.2.2.29 `float std::cyl_neumannf (float __nu, float __x) [inline]`

Return the Neumann function $N_\nu(x)$ of `float` order ν and argument x .

See also

[cyl_neumann](#) for setails.

Definition at line 788 of file `specfun.h`.

8.2.2.30 `long double std::cyl_neumannl (long double __nu, long double __x) [inline]`

Return the Neumann function $N_\nu(x)$ of `long double` order ν and argument x .

See also

[cyl_neumann](#) for setails.

Definition at line 798 of file `specfun.h`.

8.2.2.31 `template<typename _Tp, typename _Tpp> __gnu_cxx::__promote_fp_t<_Tp, _Tpp> std::ellint_1 (_Tp __k, _Tpp __phi) [inline]`

Return the incomplete elliptic integral of the first kind $F(k, \phi)$ for `real` modulus k and angle ϕ .

The incomplete elliptic integral of the first kind is defined as

$$F(k, \phi) = \int_0^\phi \frac{d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

For $\phi = \pi/2$ this becomes the complete elliptic integral of the first kind, $K(k)$.

See also

[comp_ellint_1](#).

Template Parameters

<code>_Tp</code>	The floating-point type of the modulus <code>__k</code> .
<code>_Tpp</code>	The floating-point type of the angle <code>__phi</code> .

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
<code>__phi</code>	The integral limit argument in radians

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 869 of file `specfun.h`.

8.2.2.32 `float std::ellint_1f (float __k, float __phi) [inline]`

Return the incomplete elliptic integral of the first kind $E(k, \phi)$ for `float` modulus k and angle ϕ .

See also

[ellint_1](#) for details.

Definition at line 836 of file `specfun.h`.

8.2.2.33 `long double std::ellint_1l (long double __k, long double __phi) [inline]`

Return the incomplete elliptic integral of the first kind $E(k, \phi)$ for `long double` modulus k and angle ϕ .

See also

[ellint_1](#) for details.

Definition at line 846 of file `specfun.h`.

8.2.2.34 `template<typename _Tp, typename _Tpp> __gnu_cxx::__promote_fp_t<_Tp, _Tpp> std::ellint_2 (_Tp __k, _Tpp __phi) [inline]`

Return the incomplete elliptic integral of the second kind $E(k, \phi)$.

The incomplete elliptic integral of the second kind is defined as

$$E(k, \phi) = \int_0^\phi \sqrt{1 - k^2 \sin^2 \theta}$$

For $\phi = \pi/2$ this becomes the complete elliptic integral of the second kind, $E(k)$.

See also

[comp_ellint_2](#).

Template Parameters

<code>__Tp</code>	The floating-point type of the modulus <code>__k</code> .
<code>__Tpp</code>	The floating-point type of the angle <code>__phi</code> .

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
<code>__phi</code>	The integral limit argument in radians

Returns

The elliptic function of the second kind.

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 917 of file `specfun.h`.

8.2.2.35 `float std::ellint_2f (float __k, float __phi)` `[inline]`

Return the incomplete elliptic integral of the second kind $E(k, \phi)$ for `float` argument.

See also

[ellint_2](#) for details.

Definition at line 884 of file `specfun.h`.

8.2.2.36 `long double std::ellint_2l (long double __k, long double __phi)` `[inline]`

Return the incomplete elliptic integral of the second kind $E(k, \phi)$.

See also

[ellint_2](#) for details.

Definition at line 894 of file `specfun.h`.

8.2.2.37 `template<typename _Tp, typename _Tpn, typename _Tpp> __gnu_cxx::__promote_fp_t<_Tp, _Tpn, _Tpp> std::ellint_3 (_Tp __k, _Tpn __nu, _Tpp __phi) [inline]`

Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.

The incomplete elliptic integral of the third kind is defined by:

$$\Pi(k, \nu, \phi) = \int_0^\phi \frac{d\theta}{(1 - \nu \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}}$$

For $\phi = \pi/2$ this becomes the complete elliptic integral of the third kind, $\Pi(k, \nu)$.

See also

[comp_ellint_3](#).

Template Parameters

<code>_Tp</code>	The floating-point type of the modulus <code>__k</code> .
<code>_Tpn</code>	The floating-point type of the argument <code>__nu</code> .
<code>_Tpp</code>	The floating-point type of the angle <code>__phi</code> .

Parameters

<code>__k</code>	The modulus, <code>abs (__k) <= 1</code>
<code>__nu</code>	The second argument
<code>__phi</code>	The integral limit argument in radians

Returns

The elliptic function of the third kind.

Exceptions

<code>std::domain_error</code>	if <code>abs (__k) > 1</code> .
--------------------------------	------------------------------------

Definition at line 970 of file `specfun.h`.

8.2.2.38 `float std::ellint_3f (float __k, float __nu, float __phi) [inline]`

Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ for `float` argument.

See also

[ellint_3](#) for details.

Definition at line 932 of file `specfun.h`.

8.2.2.39 `long double std::ellint_3l (long double __k, long double __nu, long double __phi) [inline]`

Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.

See also

[ellint_3](#) for details.

Definition at line 942 of file specfun.h.

8.2.2.40 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::expint (_Tp __x) [inline]`

Return the exponential integral $Ei(x)$ for `real` argument x .

The exponential integral is given by

$$Ei(x) = - \int_{-x}^{\infty} \frac{e^t}{t} dt$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__x</code>	The argument of the exponential integral function.
------------------	--

Definition at line 1010 of file specfun.h.

8.2.2.41 `float std::expintf (float __x) [inline]`

Return the exponential integral $Ei(x)$ for `float` argument x .

See also

[expint](#) for details.

Definition at line 984 of file specfun.h.

8.2.2.42 `long double std::expintl (long double __x) [inline]`

Return the exponential integral $Ei(x)$ for `long double` argument x .

See also

[expint](#) for details.

Definition at line 994 of file specfun.h.

8.2.2.43 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::hermite (unsigned int __n, _Tp __x) [inline]`

Return the Hermite polynomial $H_n(x)$ of order `n` and `real` argument x .

The Hermite polynomial is defined by:

$$H_n(x) = (-1)^n e^{x^2} \frac{d^n}{dx^n} e^{-x^2}$$

The Hermite polynomial obeys a reflection formula:

$$H_n(-x) = (-1)^n H_n(x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__n</code>	The order
<code>__x</code>	The argument

Definition at line 1058 of file `specfun.h`.

8.2.2.44 `float std::hermitef (unsigned int __n, float __x) [inline]`

Return the Hermite polynomial $H_n(x)$ of nonnegative order `n` and `float` argument x .

See also

[hermite](#) for details.

Definition at line 1025 of file `specfun.h`.

8.2.2.45 `long double std::hermitel (unsigned int __n, long double __x) [inline]`

Return the Hermite polynomial $H_n(x)$ of nonnegative order `n` and `long double` argument x .

See also

[hermite](#) for details.

Definition at line 1035 of file `specfun.h`.

8.2.2.46 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::laguerre (unsigned int __n, _Tp __x) [inline]`

Returns the Laguerre polynomial $L_n(x)$ of nonnegative degree n and real argument $x \geq 0$.

The Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__n</code>	The nonnegative order
<code>__x</code>	The argument <code>__x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
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Definition at line 1102 of file `specfun.h`.

8.2.2.47 `float std::laguerref (unsigned int __n, float __x) [inline]`

Returns the Laguerre polynomial $L_n(x)$ of nonnegative degree `n` and `float` argument $x \geq 0$.

See also

[laguerre](#) for more details.

Definition at line 1073 of file `specfun.h`.

8.2.2.48 `long double std::laguerrel (unsigned int __n, long double __x) [inline]`

Returns the Laguerre polynomial $L_n(x)$ of nonnegative degree `n` and `long double` argument $x \geq 0$.

See also

[laguerre](#) for more details.

Definition at line 1083 of file `specfun.h`.

8.2.2.49 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::legendre (unsigned int __l, _Tp __x) [inline]`

Return the Legendre polynomial $P_l(x)$ of nonnegative degree l and real argument $|x| \leq 0$.

The Legendre function of order l and argument x , $P_l(x)$, is defined by:

$$P_l(x) = \frac{1}{2^l l!} \frac{d^l}{dx^l} (x^2 - 1)^l$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__l</code>	The degree $l \geq 0$
<code>__x</code>	The argument $\text{abs}(\text{__x}) \leq 1$

Exceptions

<code>std::domain_error</code>	if $\text{abs}(\text{__x}) > 1$
--------------------------------	---------------------------------

Definition at line 1147 of file `specfun.h`.

8.2.2.50 `float std::legendref (unsigned int __l, float __x) [inline]`

Return the Legendre polynomial $P_l(x)$ of nonnegative degree l and `float` argument $|x| \leq 1$.

See also

[legendre](#) for more details.

Definition at line 1117 of file `specfun.h`.

8.2.2.51 `long double std::legendrel (unsigned int __l, long double __x) [inline]`

Return the Legendre polynomial $P_l(x)$ of nonnegative degree l and `long double` argument $|x| \leq 1$.

See also

[legendre](#) for more details.

Definition at line 1127 of file `specfun.h`.

8.2.2.52 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::riemann_zeta (_Tp __s) [inline]`

Return the Riemann zeta function $\zeta(s)$ for real argument s .

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} k^{-s} \text{ for } s > 1$$

and

$$\zeta(s) = \frac{1}{1 - 2^{1-s}} \sum_{k=1}^{\infty} (-1)^{k-1} k^{-s} \text{ for } 0 < s < 1$$

For $s < 1$ use the reflection formula:

$$\zeta(s) = 2^s \pi^{s-1} \sin\left(\frac{\pi s}{2}\right) \Gamma(1-s) \zeta(1-s)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__s</code> .
------------------	--

Parameters

<code>__s</code>	The argument $s \neq 1$
------------------	-------------------------

Definition at line 1198 of file `specfun.h`.

8.2.2.53 `float std::riemann_zetaf (float __s) [inline]`

Return the Riemann zeta function $\zeta(s)$ for `float` argument s .

See also

[riemann_zeta](#) for more details.

Definition at line 1162 of file `specfun.h`.

8.2.2.54 `long double std::riemann_zetal (long double __s) [inline]`

Return the Riemann zeta function $\zeta(s)$ for `long double` argument s .

See also

[riemann_zeta](#) for more details.

Definition at line 1172 of file `specfun.h`.

8.2.2.55 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::sph_bessel (unsigned int __n, _Tp __x) [inline]`

Return the spherical Bessel function $j_n(x)$ of nonnegative order n and real argument $x \geq 0$.

The spherical Bessel function is defined by:

$$j_n(x) = \left(\frac{\pi}{2x}\right)^{1/2} J_{n+1/2}(x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__n</code>	The integral order <code>n >= 0</code>
<code>__x</code>	The real argument <code>x >= 0</code>

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
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Definition at line 1242 of file `specfun.h`.

8.2.2.56 `float std::sph_besself (unsigned int __n, float __x) [inline]`

Return the spherical Bessel function $j_n(x)$ of nonnegative order `n` and `float` argument $x \geq 0$.

See also

[sph_bessel](#) for more details.

Definition at line 1213 of file `specfun.h`.

8.2.2.57 `long double std::sph_bessell (unsigned int __n, long double __x) [inline]`

Return the spherical Bessel function $j_n(x)$ of nonnegative order `n` and `long double` argument $x \geq 0$.

See also

[sph_bessel](#) for more details.

Definition at line 1223 of file `specfun.h`.

8.2.2.58 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta) [inline]`

Return the spherical Legendre function of nonnegative integral degree l and order m and real angle θ in radians.

The spherical Legendre function is defined by

$$Y_l^m(\theta, \phi) = (-1)^m \left[\frac{(2l+1)}{4\pi} \frac{(l-m)!}{(l+m)!} \right] P_l^m(\cos \theta) \exp^{im\phi}$$

Template Parameters

<code>_Tp</code>	The floating-point type of the angle <code>__theta</code> .
------------------	---

Parameters

<code>__l</code>	The order <code>__l >= 0</code>
<code>__m</code>	The degree <code>__m >= 0</code> and <code>__m <= __l</code>
<code>__theta</code>	The radian polar angle argument

Definition at line 1289 of file `specfun.h`.

8.2.2.59 `float std::sph_legendref (unsigned int __l, unsigned int __m, float __theta) [inline]`

Return the spherical Legendre function of nonnegative integral degree l and order m and float angle θ in radians.

See also

[sph_legendre](#) for details.

Definition at line 1257 of file `specfun.h`.

8.2.2.60 `long double std::sph_legendrel (unsigned int __l, unsigned int __m, long double __theta) [inline]`

Return the spherical Legendre function of nonnegative integral degree l and order m and long double angle θ in radians.

See also

[sph_legendre](#) for details.

Definition at line 1268 of file `specfun.h`.

8.2.2.61 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::sph_neumann (unsigned int __n, _Tp __x) [inline]`

Return the spherical Neumann function of integral order $n \geq 0$ and real argument $x \geq 0$.

The spherical Neumann function is defined by

$$n_n(x) = \left(\frac{\pi}{2x}\right)^{1/2} N_{n+1/2}(x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__n</code>	The integral order $n \geq 0$
<code>__x</code>	The real argument $x \geq 0$

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
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Definition at line 1333 of file `specfun.h`.

8.2.2.62 `float std::sph_neumannf (unsigned int __n, float __x) [inline]`

Return the spherical Neumann function of integral order $n \geq 0$ and `float` argument $x \geq 0$.

See also

[sph_neumann](#) for details.

Definition at line 1304 of file `specfun.h`.

8.2.2.63 `long double std::sph_neumannl (unsigned int __n, long double __x) [inline]`

Return the spherical Neumann function of integral order $n \geq 0$ and `long double` $x \geq 0$.

See also

[sph_neumann](#) for details.

Definition at line 1314 of file `specfun.h`.

8.3 GNU Extended Mathematical Special Functions

Collaboration diagram for GNU Extended Mathematical Special Functions:



Enumerations

- enum { [__gnu_cxx::__GLIBCXX_JACOBI_SN](#), [__gnu_cxx::__GLIBCXX_JACOBI_CN](#), [__gnu_cxx::__GLIBCXX_JACOBI_DN](#) }

Functions

- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::airy_ai](#) (_Tp __x)
- template<typename _Tp >
std::complex< [__gnu_cxx::__promote_fp_t<_Tp>](#) > [__gnu_cxx::airy_ai](#) (std::complex<_Tp> __x)
- float [__gnu_cxx::airy_aif](#) (float __x)
- long double [__gnu_cxx::airy_ail](#) (long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::airy_bi](#) (_Tp __x)
- template<typename _Tp >
std::complex< [__gnu_cxx::__promote_fp_t<_Tp>](#) > [__gnu_cxx::airy_bi](#) (std::complex<_Tp> __x)
- float [__gnu_cxx::airy_bif](#) (float __x)
- long double [__gnu_cxx::airy_bil](#) (long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::bernoulli](#) (unsigned int __n)
- float [__gnu_cxx::bernoullif](#) (unsigned int __n)
- long double [__gnu_cxx::bernoullil](#) (unsigned int __n)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::bincoef](#) (unsigned int __n, unsigned int __k)
- float [__gnu_cxx::bincoeff](#) (unsigned int __n, unsigned int __k)
- long double [__gnu_cxx::bincoefl](#) (unsigned int __n, unsigned int __k)
- template<typename _Tps, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tps, _Tp>](#) [__gnu_cxx::bose_einstein](#) (_Tps __s, _Tp __x)
- float [__gnu_cxx::bose_einsteinf](#) (float __s, float __x)
- long double [__gnu_cxx::bose_einsteinl](#) (long double __s, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::chebyshev_t](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::chebyshev_tf](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::chebyshev_tl](#) (unsigned int __n, long double __x)

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_u (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::chebyshev_uf (unsigned int __n, float __x)`
- `long double __gnu_cxx::chebyshev_ul (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_v (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::chebyshev_vf (unsigned int __n, float __x)`
- `long double __gnu_cxx::chebyshev_vl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_w (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::chebyshev_wf (unsigned int __n, float __x)`
- `long double __gnu_cxx::chebyshev_wl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen (unsigned int __m, _Tp __w)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::clausen (unsigned int __m, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen_c (unsigned int __m, _Tp __w)`
- `float __gnu_cxx::clausen_cf (unsigned int __m, float __w)`
- `long double __gnu_cxx::clausen_cl (unsigned int __m, long double __w)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen_s (unsigned int __m, _Tp __w)`
- `float __gnu_cxx::clausen_sf (unsigned int __m, float __w)`
- `long double __gnu_cxx::clausen_sl (unsigned int __m, long double __w)`
- `float __gnu_cxx::clausenf (unsigned int __m, float __w)`
- `std::complex< float > __gnu_cxx::clausenf (unsigned int __m, std::complex< float > __w)`
- `long double __gnu_cxx::clausenl (unsigned int __m, long double __w)`
- `std::complex< long double > __gnu_cxx::clausenl (unsigned int __m, std::complex< long double > __w)`
- `template<typename _Tk >`
`__gnu_cxx::__promote_fp_t< _Tk > __gnu_cxx::comp_ellint_d (_Tk __k)`
- `float __gnu_cxx::comp_ellint_df (float __k)`
- `long double __gnu_cxx::comp_ellint_dl (long double __k)`
- `float __gnu_cxx::comp_ellint_rf (float __x, float __y)`
- `long double __gnu_cxx::comp_ellint_rf (long double __x, long double __y)`
- `template<typename _Tx, typename _Ty >`
`__gnu_cxx::__promote_fp_t< _Tx, _Ty > __gnu_cxx::comp_ellint_rf (_Tx __x, _Ty __y)`
- `float __gnu_cxx::comp_ellint_rg (float __x, float __y)`
- `long double __gnu_cxx::comp_ellint_rg (long double __x, long double __y)`
- `template<typename _Tx, typename _Ty >`
`__gnu_cxx::__promote_fp_t< _Tx, _Ty > __gnu_cxx::comp_ellint_rg (_Tx __x, _Ty __y)`
- `template<typename _Tpa, typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpa, _Tpc, _Tp > __gnu_cxx::conf_hyperg (_Tpa __a, _Tpc __c, _Tp __x)`
- `template<typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_2< _Tpc, _Tp >::type __gnu_cxx::conf_hyperg_lim (_Tpc __c, _Tp __x)`
- `float __gnu_cxx::conf_hyperg_limf (float __c, float __x)`
- `long double __gnu_cxx::conf_hyperg_liml (long double __c, long double __x)`
- `float __gnu_cxx::conf_hypergf (float __a, float __c, float __x)`
- `long double __gnu_cxx::conf_hypergl (long double __a, long double __c, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::cos_pi (_Tp __x)`
- `float __gnu_cxx::cos_pif (float __x)`

- long double [__gnu_cxx::cos_pil](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::cosh_pi](#) (_Tp __x)
- float [__gnu_cxx::cosh_pif](#) (float __x)
- long double [__gnu_cxx::cosh_pil](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::coshint](#) (_Tp __x)
- float [__gnu_cxx::coshintf](#) (float __x)
- long double [__gnu_cxx::coshintl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::cosint](#) (_Tp __x)
- float [__gnu_cxx::cosintf](#) (float __x)
- long double [__gnu_cxx::cosintl](#) (long double __x)
- template<typename _Tpnu, typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>](#) > [__gnu_cxx::cyl_hankel_1](#) (_Tpnu __nu, _Tp __z)
- template<typename _Tpnu, typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>](#) > [__gnu_cxx::cyl_hankel_1](#) (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)
- std::complex< float > [__gnu_cxx::cyl_hankel_1f](#) (float __nu, float __z)
- std::complex< float > [__gnu_cxx::cyl_hankel_1f](#) (std::complex< float > __nu, std::complex< float > __x)
- std::complex< long double > [__gnu_cxx::cyl_hankel_1l](#) (long double __nu, long double __z)
- std::complex< long double > [__gnu_cxx::cyl_hankel_1l](#) (std::complex< long double > __nu, std::complex< long double > __x)
- template<typename _Tpnu, typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>](#) > [__gnu_cxx::cyl_hankel_2](#) (_Tpnu __nu, _Tp __z)
- template<typename _Tpnu, typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>](#) > [__gnu_cxx::cyl_hankel_2](#) (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)
- std::complex< float > [__gnu_cxx::cyl_hankel_2f](#) (float __nu, float __z)
- std::complex< float > [__gnu_cxx::cyl_hankel_2f](#) (std::complex< float > __nu, std::complex< float > __x)
- std::complex< long double > [__gnu_cxx::cyl_hankel_2l](#) (long double __nu, long double __z)
- std::complex< long double > [__gnu_cxx::cyl_hankel_2l](#) (std::complex< long double > __nu, std::complex< long double > __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::dawson](#) (_Tp __x)
- float [__gnu_cxx::dawsonf](#) (float __x)
- long double [__gnu_cxx::dawsonl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp>](#) [__gnu_cxx::dilog](#) (_Tp __x)
- float [__gnu_cxx::dilogf](#) (float __x)
- long double [__gnu_cxx::dilogl](#) (long double __x)
- template<typename _Tp >
 _Tp [__gnu_cxx::dirichlet_beta](#) (_Tp __s)
- float [__gnu_cxx::dirichlet_betaf](#) (float __s)
- long double [__gnu_cxx::dirichlet_betall](#) (long double __s)
- template<typename _Tp >
 _Tp [__gnu_cxx::dirichlet_eta](#) (_Tp __s)
- float [__gnu_cxx::dirichlet_etaf](#) (float __s)
- long double [__gnu_cxx::dirichlet_etall](#) (long double __s)
- template<typename _Tp >
 _Tp [__gnu_cxx::dirichlet_lambda](#) (_Tp __s)
- float [__gnu_cxx::dirichlet_lambdaf](#) (float __s)

- long double [__gnu_cxx::dirichlet_lambdal](#) (long double __s)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::double_factorial](#) (int __n)
- float [__gnu_cxx::double_factorialf](#) (int __n)
- long double [__gnu_cxx::double_factoriall](#) (int __n)
- template<typename _Tk, typename _Tp, typename _Ta, typename _Tb >
 [__gnu_cxx::__promote_fp_t](#)< _Tk, _Tp, _Ta, _Tb > [__gnu_cxx::ellint_cel](#) (_Tk __k_c, _Tp __p, _Ta __a, _Tb __b)
- float [__gnu_cxx::ellint_celf](#) (float __k_c, float __p, float __a, float __b)
- long double [__gnu_cxx::ellint_cell](#) (long double __k_c, long double __p, long double __a, long double __b)
- template<typename _Tk, typename _Tphi >
 [__gnu_cxx::__promote_fp_t](#)< _Tk, _Tphi > [__gnu_cxx::ellint_d](#) (_Tk __k, _Tphi __phi)
- float [__gnu_cxx::ellint_df](#) (float __k, float __phi)
- long double [__gnu_cxx::ellint_dl](#) (long double __k, long double __phi)
- template<typename _Tp, typename _Tk >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Tk > [__gnu_cxx::ellint_el1](#) (_Tp __x, _Tk __k_c)
- float [__gnu_cxx::ellint_el1f](#) (float __x, float __k_c)
- long double [__gnu_cxx::ellint_el1l](#) (long double __x, long double __k_c)
- template<typename _Tp, typename _Tk, typename _Ta, typename _Tb >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Tk, _Ta, _Tb > [__gnu_cxx::ellint_el2](#) (_Tp __x, _Tk __k_c, _Ta __a, _Tb __b)
- float [__gnu_cxx::ellint_el2f](#) (float __x, float __k_c, float __a, float __b)
- long double [__gnu_cxx::ellint_el2l](#) (long double __x, long double __k_c, long double __a, long double __b)
- template<typename _Tx, typename _Tk, typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tx, _Tk, _Tp > [__gnu_cxx::ellint_el3](#) (_Tx __x, _Tk __k_c, _Tp __p)
- float [__gnu_cxx::ellint_el3f](#) (float __x, float __k_c, float __p)
- long double [__gnu_cxx::ellint_el3l](#) (long double __x, long double __k_c, long double __p)
- template<typename _Tp, typename _Up >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Up > [__gnu_cxx::ellint_rc](#) (_Tp __x, _Up __y)
- float [__gnu_cxx::ellint_rcf](#) (float __x, float __y)
- long double [__gnu_cxx::ellint_rcl](#) (long double __x, long double __y)
- template<typename _Tp, typename _Up, typename _Vp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Up, _Vp > [__gnu_cxx::ellint_rd](#) (_Tp __x, _Up __y, _Vp __z)
- float [__gnu_cxx::ellint_rdf](#) (float __x, float __y, float __z)
- long double [__gnu_cxx::ellint_rdl](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Up, _Vp > [__gnu_cxx::ellint_rf](#) (_Tp __x, _Up __y, _Vp __z)
- float [__gnu_cxx::ellint_rff](#) (float __x, float __y, float __z)
- long double [__gnu_cxx::ellint_rfl](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Up, _Vp > [__gnu_cxx::ellint_rg](#) (_Tp __x, _Up __y, _Vp __z)
- float [__gnu_cxx::ellint_rgf](#) (float __x, float __y, float __z)
- long double [__gnu_cxx::ellint_rgl](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp, typename _Wp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp, _Up, _Vp, _Wp > [__gnu_cxx::ellint_rj](#) (_Tp __x, _Up __y, _Vp __z, _Wp __p)
- float [__gnu_cxx::ellint_rjf](#) (float __x, float __y, float __z, float __p)
- long double [__gnu_cxx::ellint_rjl](#) (long double __x, long double __y, long double __z, long double __p)
- template<typename _Tp >
 _Tp [__gnu_cxx::ellnome](#) (_Tp __k)
- float [__gnu_cxx::ellnomef](#) (float __k)
- long double [__gnu_cxx::ellnomel](#) (long double __k)

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::expint (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::expintf (unsigned int __n, float __x)`
- `long double __gnu_cxx::expintl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::factorial (unsigned int __n)`
- `float __gnu_cxx::factorialf (unsigned int __n)`
- `long double __gnu_cxx::factoriall (unsigned int __n)`
- `template<typename _Tps, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tps, _Tp > __gnu_cxx::fermi_dirac (_Tps __s, _Tp __x)`
- `float __gnu_cxx::fermi_diracf (float __s, float __x)`
- `long double __gnu_cxx::fermi_diracl (long double __s, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::fresnel_c (_Tp __x)`
- `float __gnu_cxx::fresnel_cf (float __x)`
- `long double __gnu_cxx::fresnel_cl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::fresnel_s (_Tp __x)`
- `float __gnu_cxx::fresnel_sf (float __x)`
- `long double __gnu_cxx::fresnel_sl (long double __x)`
- `template<typename _Talpha, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Talpha, _Tp > __gnu_cxx::gegenbauer (unsigned int __n, _Talpha __alpha, _Tp __x)`
- `float __gnu_cxx::gegenbauerf (unsigned int __n, float __alpha, float __x)`
- `long double __gnu_cxx::gegenbauerl (unsigned int __n, long double __alpha, long double __x)`
- `template<typename _Tk, typename _Tphi >`
`__gnu_cxx::__promote_fp_t< _Tk, _Tphi > __gnu_cxx::heuman_lambda (_Tk __k, _Tphi __phi)`
- `float __gnu_cxx::heuman_lambdaf (float __k, float __phi)`
- `long double __gnu_cxx::heuman_lambdal (long double __k, long double __phi)`
- `template<typename _Tp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up > __gnu_cxx::hurwitz_zeta (_Tp __s, _Up __a)`
- `template<typename _Tp, typename _Up >`
`std::complex< _Tp > __gnu_cxx::hurwitz_zeta (_Tp __s, std::complex< _Up > __a)`
- `float __gnu_cxx::hurwitz_zetaf (float __s, float __a)`
- `long double __gnu_cxx::hurwitz_zetal (long double __s, long double __a)`
- `template<typename _Tpa, typename _Tpb, typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpa, _Tpb, _Tpc, _Tp > __gnu_cxx::hyperg (_Tpa __a, _Tpb __b, _Tpc __c, _Tp __x)`
- `float __gnu_cxx::hyperg (float __a, float __b, float __c, float __x)`
- `long double __gnu_cxx::hypergl (long double __a, long double __b, long double __c, long double __x)`
- `template<typename _Ta, typename _Tb, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tb, _Tp > __gnu_cxx::ibeta (_Ta __a, _Tb __b, _Tp __x)`
- `template<typename _Ta, typename _Tb, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tb, _Tp > __gnu_cxx::ibetac (_Ta __a, _Tb __b, _Tp __x)`
- `float __gnu_cxx::ibetacf (float __a, float __b, float __x)`
- `long double __gnu_cxx::ibetacl (long double __a, long double __b, long double __x)`
- `float __gnu_cxx::ibetaf (float __a, float __b, float __x)`
- `long double __gnu_cxx::ibetal (long double __a, long double __b, long double __x)`
- `template<typename _Talpha, typename _Tbeta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Talpha, _Tbeta, _Tp > __gnu_cxx::jacobi (unsigned __n, _Talpha __alpha, _Tbeta __beta, _Tp __x)`

- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_cn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_cnf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_cnl (long double __k, long double __u)`
- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_dn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_dnf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_dnl (long double __k, long double __u)`
- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_sn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_snf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_snl (long double __k, long double __u)`
- `template<typename _Tk, typename _Tphi >`
`__gnu_cxx::__promote_fp_t< _Tk, _Tphi > __gnu_cxx::jacobi_zeta (_Tk __k, _Tphi __phi)`
- `float __gnu_cxx::jacobi_zetaf (float __k, float __phi)`
- `long double __gnu_cxx::jacobi_zetal (long double __k, long double __phi)`
- `float __gnu_cxx::jacobi_f (unsigned __n, float __alpha, float __beta, float __x)`
- `long double __gnu_cxx::jacobi_l (unsigned __n, long double __alpha, long double __beta, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::lbincoef (unsigned int __n, unsigned int __k)`
- `float __gnu_cxx::lbincoeff (unsigned int __n, unsigned int __k)`
- `long double __gnu_cxx::lbincoefl (unsigned int __n, unsigned int __k)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::ldouble_factorial (int __n)`
- `float __gnu_cxx::ldouble_factorialf (int __n)`
- `long double __gnu_cxx::ldouble_factoriall (int __n)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::legendre_q (unsigned int __l, _Tp __x)`
- `float __gnu_cxx::legendre_qf (unsigned int __l, float __x)`
- `long double __gnu_cxx::legendre_ql (unsigned int __l, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::lfactorial (unsigned int __n)`
- `float __gnu_cxx::lfactorialf (unsigned int __n)`
- `long double __gnu_cxx::lfactoriall (unsigned int __n)`
- `template<typename _Ta >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ta > > __gnu_cxx::lgamma (std::complex< _Ta > __a)`
- `std::complex< float > __gnu_cxx::lgammaf (std::complex< float > __a)`
- `std::complex< long double > __gnu_cxx::lgammal (std::complex< long double > __a)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::logint (_Tp __x)`
- `float __gnu_cxx::logintf (float __x)`
- `long double __gnu_cxx::logintl (long double __x)`
- `template<typename _Tp, typename _Tn >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::lpochhammer (_Tp __a, _Tn __n)`
- `template<typename _Tp, typename _Tn >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::lpochhammer_lower (_Tp __a, _Tn __n)`
- `float __gnu_cxx::lpochhammer_lowerf (float __a, float __n)`
- `long double __gnu_cxx::lpochhammer_lowerl (long double __a, long double __n)`
- `float __gnu_cxx::lpochhammerf (float __a, float __n)`
- `long double __gnu_cxx::lpochhammerl (long double __a, long double __n)`
- `template<typename _Tph, typename _Tpa >`
`__gnu_cxx::__promote_fp_t< _Tph, _Tpa > __gnu_cxx::owens_t (_Tph __h, _Tpa __a)`

- float `__gnu_cxx::owens_tf` (float __h, float __a)
- long double `__gnu_cxx::owens_tl` (long double __h, long double __a)
- template<typename _Ta, typename _Tp >
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::pgamma` (_Ta __a, _Tp __x)
- float `__gnu_cxx::pgammaf` (float __a, float __x)
- long double `__gnu_cxx::pgammal` (long double __a, long double __x)
- template<typename _Tp, typename _Tn >
`__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::pochhammer` (_Tp __a, _Tn __n)
- template<typename _Tp, typename _Tn >
`__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::pochhammer_lower` (_Tp __a, _Tn __n)
- float `__gnu_cxx::pochhammer_lowerf` (float __a, float __n)
- long double `__gnu_cxx::pochhammer_lowerl` (long double __a, long double __n)
- float `__gnu_cxx::pochhammerf` (float __a, float __n)
- long double `__gnu_cxx::pochhammerl` (long double __a, long double __n)
- template<typename _Tp, typename _Wp >
`__gnu_cxx::__promote_fp_t< _Tp, _Wp > __gnu_cxx::polylog` (_Tp __s, _Wp __w)
- template<typename _Tp, typename _Wp >
`std::complex< __gnu_cxx::__promote_fp_t< _Tp, _Wp > > __gnu_cxx::polylog` (_Tp __s, std::complex< _Tp > __w)
- float `__gnu_cxx::polylogf` (float __s, float __w)
- std::complex< float > `__gnu_cxx::polylogf` (float __s, std::complex< float > __w)
- long double `__gnu_cxx::polylogl` (long double __s, long double __w)
- std::complex< long double > `__gnu_cxx::polylogl` (long double __s, std::complex< long double > __w)
- template<typename _Tp >
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::psi` (_Tp __x)
- float `__gnu_cxx::psif` (float __x)
- long double `__gnu_cxx::psil` (long double __x)
- template<typename _Ta, typename _Tp >
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::qgamma` (_Ta __a, _Tp __x)
- float `__gnu_cxx::qgammaf` (float __a, float __x)
- long double `__gnu_cxx::qgammal` (long double __a, long double __x)
- template<typename _Tp >
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::radpoly` (unsigned int __n, unsigned int __m, _Tp __rho)
- float `__gnu_cxx::radpolyf` (unsigned int __n, unsigned int __m, float __rho)
- long double `__gnu_cxx::radpolyl` (unsigned int __n, unsigned int __m, long double __rho)
- template<typename _Tp >
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::sin_pi` (_Tp __x)
- float `__gnu_cxx::sin_pif` (float __x)
- long double `__gnu_cxx::sin_pil` (long double __x)
- template<typename _Tp >
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::sinc` (_Tp __x)
- template<typename _Tp >
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::sinc_pi` (_Tp __x)
- float `__gnu_cxx::sinc_pif` (float __x)
- long double `__gnu_cxx::sinc_pil` (long double __x)
- float `__gnu_cxx::sincf` (float __x)
- long double `__gnu_cxx::sincl` (long double __x)
- `__gnu_cxx::__sincos_t< double > __gnu_cxx::sincos` (double __x)
- template<typename _Tp >
`__gnu_cxx::__sincos_t< _Tp > __gnu_cxx::sincos` (_Tp __x)
- template<typename _Tp >
`__gnu_cxx::__sincos_t< _Tp > __gnu_cxx::sincos_pi` (_Tp __x)

- [__gnu_cxx::__sincos_t](#)< float > [__gnu_cxx::sincos_pif](#) (float __x)
- [__gnu_cxx::__sincos_t](#)< long double > [__gnu_cxx::sincos_pil](#) (long double __x)
- [__gnu_cxx::__sincos_t](#)< float > [__gnu_cxx::sincosf](#) (float __x)
- [__gnu_cxx::__sincos_t](#)< long double > [__gnu_cxx::sincosl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sinh_pi](#) (_Tp __x)
- float [__gnu_cxx::sinh_pif](#) (float __x)
- long double [__gnu_cxx::sinh_pil](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sinhc](#) (_Tp __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sinhc_pi](#) (_Tp __x)
- float [__gnu_cxx::sinhc_pif](#) (float __x)
- long double [__gnu_cxx::sinhc_pil](#) (long double __x)
- float [__gnu_cxx::sinhcf](#) (float __x)
- long double [__gnu_cxx::sinhcl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sinhint](#) (_Tp __x)
- float [__gnu_cxx::sinhintf](#) (float __x)
- long double [__gnu_cxx::sinhintl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sinint](#) (_Tp __x)
- float [__gnu_cxx::sinintf](#) (float __x)
- long double [__gnu_cxx::sinintl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sph_bessel_i](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::sph_bessel_if](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::sph_bessel_il](#) (unsigned int __n, long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t](#)< _Tp > [__gnu_cxx::sph_bessel_k](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::sph_bessel_kf](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::sph_bessel_kl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t](#)< _Tp > > [__gnu_cxx::sph_hankel_1](#) (unsigned int __n, _Tp __z)
- template<typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t](#)< _Tp > > [__gnu_cxx::sph_hankel_1](#) (unsigned int __n, std::complex< _Tp > __x)
- std::complex< float > [__gnu_cxx::sph_hankel_1f](#) (unsigned int __n, float __z)
- std::complex< float > [__gnu_cxx::sph_hankel_1f](#) (unsigned int __n, std::complex< float > __x)
- std::complex< long double > [__gnu_cxx::sph_hankel_1l](#) (unsigned int __n, long double __z)
- std::complex< long double > [__gnu_cxx::sph_hankel_1l](#) (unsigned int __n, std::complex< long double > __x)
- template<typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t](#)< _Tp > > [__gnu_cxx::sph_hankel_2](#) (unsigned int __n, _Tp __z)
- template<typename _Tp >
 std::complex< [__gnu_cxx::__promote_fp_t](#)< _Tp > > [__gnu_cxx::sph_hankel_2](#) (unsigned int __n, std::complex< _Tp > __x)
- std::complex< float > [__gnu_cxx::sph_hankel_2f](#) (unsigned int __n, float __z)
- std::complex< float > [__gnu_cxx::sph_hankel_2f](#) (unsigned int __n, std::complex< float > __x)
- std::complex< long double > [__gnu_cxx::sph_hankel_2l](#) (unsigned int __n, long double __z)
- std::complex< long double > [__gnu_cxx::sph_hankel_2l](#) (unsigned int __n, std::complex< long double > __x)

- `template<typename _Ttheta, typename _Tphi >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ttheta, _Tphi > > __gnu_cxx::sph_harmonic` (unsigned int __l,
int __m, _Ttheta __theta, _Tphi __phi)
- `std::complex< float > __gnu_cxx::sph_harmonicf` (unsigned int __l, int __m, float __theta, float __phi)
- `std::complex< long double > __gnu_cxx::sph_harmonicl` (unsigned int __l, int __m, long double __theta, long
double __phi)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::tan_pi` (_Tp __x)
- `float __gnu_cxx::tan_pif` (float __x)
- `long double __gnu_cxx::tan_pil` (long double __x)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::tanh_pi` (_Tp __x)
- `float __gnu_cxx::tanh_pif` (float __x)
- `long double __gnu_cxx::tanh_pil` (long double __x)
- `template<typename _Ta >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ta > > __gnu_cxx::tgamma` (std::complex< _Ta > __a)
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::tgamma` (_Ta __a, _Tp __x)
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::tgamma_lower` (_Ta __a, _Tp __x)
- `float __gnu_cxx::tgamma_lowerf` (float __a, float __x)
- `long double __gnu_cxx::tgamma_lowerl` (long double __a, long double __x)
- `std::complex< float > __gnu_cxx::tgammaf` (std::complex< float > __a)
- `float __gnu_cxx::tgammaf` (float __a, float __x)
- `std::complex< long double > __gnu_cxx::tgammal` (std::complex< long double > __a)
- `long double __gnu_cxx::tgammal` (long double __a, long double __x)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_1` (_Tpnu __nu, _Tp __x)
- `float __gnu_cxx::theta_1f` (float __nu, float __x)
- `long double __gnu_cxx::theta_1l` (long double __nu, long double __x)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_2` (_Tpnu __nu, _Tp __x)
- `float __gnu_cxx::theta_2f` (float __nu, float __x)
- `long double __gnu_cxx::theta_2l` (long double __nu, long double __x)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_3` (_Tpnu __nu, _Tp __x)
- `float __gnu_cxx::theta_3f` (float __nu, float __x)
- `long double __gnu_cxx::theta_3l` (long double __nu, long double __x)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_4` (_Tpnu __nu, _Tp __x)
- `float __gnu_cxx::theta_4f` (float __nu, float __x)
- `long double __gnu_cxx::theta_4l` (long double __nu, long double __x)
- `template<typename _Tp_k, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp_k, _Tp > __gnu_cxx::theta_c` (_Tp_k __k, _Tp __x)
- `float __gnu_cxx::theta_cf` (float __k, float __x)
- `long double __gnu_cxx::theta_cl` (long double __k, long double __x)
- `template<typename _Tp_k, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp_k, _Tp > __gnu_cxx::theta_d` (_Tp_k __k, _Tp __x)
- `float __gnu_cxx::theta_df` (float __k, float __x)
- `long double __gnu_cxx::theta_dl` (long double __k, long double __x)
- `template<typename _Tp_k, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp_k, _Tp > __gnu_cxx::theta_n` (_Tp_k __k, _Tp __x)

- float `__gnu_cxx::theta_nf` (float `__k`, float `__x`)
- long double `__gnu_cxx::theta_nl` (long double `__k`, long double `__x`)
- template<typename `_Tpk`, typename `_Tp` >
`__gnu_cxx::__promote_fp_t<_Tpk, _Tp>` `__gnu_cxx::theta_s` (`_Tpk` `__k`, `_Tp` `__x`)
- float `__gnu_cxx::theta_sf` (float `__k`, float `__x`)
- long double `__gnu_cxx::theta_sl` (long double `__k`, long double `__x`)
- template<typename `_Trho`, typename `_Tphi` >
`__gnu_cxx::__promote_fp_t<_Trho, _Tphi>` `__gnu_cxx::zernike` (unsigned int `__n`, int `__m`, `_Trho` `__rho`, `_Tphi` `__phi`)
- float `__gnu_cxx::zernikef` (unsigned int `__n`, int `__m`, float `__rho`, float `__phi`)
- long double `__gnu_cxx::zernikel` (unsigned int `__n`, int `__m`, long double `__rho`, long double `__phi`)

8.3.1 Detailed Description

An extended collection of advanced mathematical special functions for GNU.

8.3.2 Enumeration Type Documentation

8.3.2.1 anonymous enum

Enumerator

`__GLIBCXX_JACOBI_SN`
`__GLIBCXX_JACOBI_CN`
`__GLIBCXX_JACOBI_DN`

Definition at line 1782 of file specfun.h.

8.3.3 Function Documentation

8.3.3.1 template<typename `_Tp` > `__gnu_cxx::__promote_fp_t<_Tp>` `__gnu_cxx::airy_ai` (`_Tp` `__x`) `[inline]`

Return the Airy function $Ai(x)$ of real argument x .

The Airy function is defined by:

$$Ai(x) = \frac{1}{\pi} \int_0^{\infty} \cos\left(\frac{t^3}{3} + xt\right) dt$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>_↔</code> <code>_x</code>	The argument
------------------------------------	--------------

Definition at line 2730 of file specfun.h.

```
8.3.3.2  template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::airy_ai ( std::complex<_Tp>
        >_x )  [inline]
```

Return the Airy function $Ai(x)$ of complex argument x .

The Airy function is defined by:

$$Ai(x) = \frac{1}{\pi} \int_0^\infty \cos\left(\frac{t^3}{3} + xt\right) dt$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>_↔</code> <code>_x</code>	The complex argument
------------------------------------	----------------------

Definition at line 2750 of file specfun.h.

```
8.3.3.3  float __gnu_cxx::airy_aif ( float _x )  [inline]
```

Return the Airy function $Ai(x)$ for `float` argument x .

See also

[airy_ai](#) for details.

Definition at line 2703 of file specfun.h.

```
8.3.3.4  long double __gnu_cxx::airy_ail ( long double _x )  [inline]
```

Return the Airy function $Ai(x)$ for `long double` argument x .

See also

[airy_ai](#) for details.

Definition at line 2713 of file specfun.h.

8.3.3.5 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::airy_bi (_Tp __x) [inline]`

Return the Airy function $Bi(x)$ of real argument x .

The Airy function is defined by:

$$Bi(x) = \frac{1}{\pi} \int_0^\infty \left[\exp\left(-\frac{t^3}{3} + xt\right) + \sin\left(\frac{t^3}{3} + xt\right) \right] dt$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↔ _x</code>	The argument
-----------------------	--------------

Definition at line 2792 of file specfun.h.

8.3.3.6 `template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::airy_bi (std::complex<_Tp> __x) [inline]`

Return the Airy function $Bi(x)$ of complex argument x .

The Airy function is defined by:

$$Bi(x) = \frac{1}{\pi} \int_0^\infty \left[\exp\left(-\frac{t^3}{3} + xt\right) + \sin\left(\frac{t^3}{3} + xt\right) \right] dt$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↔ _x</code>	The complex argument
-----------------------	----------------------

Definition at line 2813 of file specfun.h.

8.3.3.7 `float __gnu_cxx::airy_bif (float __x) [inline]`

Return the Airy function $Bi(x)$ for `float` argument x .

See also

[airy_bi](#) for details.

Definition at line 2764 of file specfun.h.

8.3.3.8 `long double __gnu_cxx::airy_bil (long double __x) [inline]`

Return the Airy function $Bi(x)$ for `long double` argument x .

See also

[airy_bi](#) for details.

Definition at line 2774 of file specfun.h.

8.3.3.9 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::bernoulli (unsigned int __n) [inline]`

Return the Bernoulli number of integer order n .

The Bernoulli numbers are defined by

Parameters

<code>__n</code>	The order.
------------------	------------

Definition at line 3886 of file specfun.h.

8.3.3.10 `float __gnu_cxx::bernoullif (unsigned int __n) [inline]`

Return the Bernoulli number of integer order n as a `float`.

See also

[bernoulli](#) for details.

Definition at line 3861 of file specfun.h.

8.3.3.11 `long double __gnu_cxx::bernoullil (unsigned int __n) [inline]`

Return the Bernoulli number of integer order n as a `long double`.

See also

[bernoulli](#) for details.

Definition at line 3871 of file specfun.h.

8.3.3.12 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::bincoef (unsigned int __n, unsigned int __k)`
`[inline]`

Definition at line 3826 of file specfun.h.

8.3.3.13 `float __gnu_cxx::bincoeff (unsigned int __n, unsigned int __k)` `[inline]`

Definition at line 3814 of file specfun.h.

8.3.3.14 `long double __gnu_cxx::bincoefl (unsigned int __n, unsigned int __k)` `[inline]`

Definition at line 3818 of file specfun.h.

8.3.3.15 `template<typename _Tps, typename _Tp> __gnu_cxx::__promote_fp_t<_Tps, _Tp> __gnu_cxx::bose_einstein (_Tps __s, _Tp __x)` `[inline]`

Definition at line 5402 of file specfun.h.

8.3.3.16 `float __gnu_cxx::bose_einsteinf (float __s, float __x)` `[inline]`

Definition at line 5393 of file specfun.h.

8.3.3.17 `long double __gnu_cxx::bose_einsteinl (long double __s, long double __x)` `[inline]`

Definition at line 5397 of file specfun.h.

8.3.3.18 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::chebyshev_t (unsigned int __n, _Tp __x)`
`[inline]`

Return the Chebyshev polynomial of the first kind $T_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the first kind is defined by:

$$T_n(x) = \cos(n\theta)$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

\leftrightarrow __n	The non-negative integral order
\leftrightarrow __x	The real argument $-1 \leq x \leq +1$

Definition at line 1983 of file specfun.h.

8.3.3.19 `float __gnu_cxx::chebyshev_tf (unsigned int __n, float __x) [inline]`

Return the Chebyshev polynomials of the first kind $T_n(x)$ of non-negative order n and `float` argument x .

See also

[chebyshev_t](#) for details.

Definition at line 1954 of file specfun.h.

8.3.3.20 `long double __gnu_cxx::chebyshev_tl (unsigned int __n, long double __x) [inline]`

Return the Chebyshev polynomials of the first kind $T_n(x)$ of non-negative order n and real argument x .

See also

[chebyshev_t](#) for details.

Definition at line 1964 of file specfun.h.

8.3.3.21 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::chebyshev_u (unsigned int __n, _Tp __x) [inline]`

Return the Chebyshev polynomial of the second kind $U_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the second kind is defined by:

$$U_n(x) = \frac{\sin[(n+1)\theta]}{\sin(\theta)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

__Tp	The real type of the argument
------	-------------------------------

Parameters

\leftrightarrow __n	The non-negative integral order
\leftrightarrow __x	The real argument $-1 \leq x \leq +1$

Definition at line 2027 of file specfun.h.

8.3.3.22 `float __gnu_cxx::chebyshev_uf (unsigned int __n, float __x) [inline]`

Return the Chebyshev polynomials of the second kind $U_n(x)$ of non-negative order n and `float` argument x .

See also

[chebyshev_u](#) for details.

Definition at line 1998 of file specfun.h.

8.3.3.23 `long double __gnu_cxx::chebyshev_ul (unsigned int __n, long double __x) [inline]`

Return the Chebyshev polynomials of the second kind $U_n(x)$ of non-negative order n and real argument x .

See also

[chebyshev_u](#) for details.

Definition at line 2008 of file specfun.h.

8.3.3.24 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::chebyshev_v (unsigned int __n, _Tp __x) [inline]`

Return the Chebyshev polynomial of the third kind $V_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the third kind is defined by:

$$V_n(x) = \frac{\cos \left[\left(n + \frac{1}{2} \right) \theta \right]}{\cos \left(\frac{\theta}{2} \right)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

\leftrightarrow __n	The non-negative integral order
\leftrightarrow __x	The real argument $-1 \leq x \leq +1$

Definition at line 2072 of file specfun.h.

8.3.3.25 `float __gnu_cxx::chebyshev_vf (unsigned int __n, float __x) [inline]`

Return the Chebyshev polynomials of the third kind $V_n(x)$ of non-negative order n and `float` argument x .

See also

[chebyshev_v](#) for details.

Definition at line 2042 of file specfun.h.

8.3.3.26 `long double __gnu_cxx::chebyshev_vl (unsigned int __n, long double __x) [inline]`

Return the Chebyshev polynomials of the third kind $V_n(x)$ of non-negative order n and real argument x .

See also

[chebyshev_v](#) for details.

Definition at line 2052 of file specfun.h.

8.3.3.27 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::chebyshev_w (unsigned int __n, _Tp __x) [inline]`

Return the Chebyshev polynomial of the fourth kind $W_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the fourth kind is defined by:

$$W_n(x) = \frac{\sin \left[\left(n + \frac{1}{2} \right) \theta \right]}{\sin \left(\frac{\theta}{2} \right)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

__Tp	The real type of the argument
------	-------------------------------

Parameters

\leftrightarrow __n	The non-negative integral order
\leftrightarrow __x	The real argument $-1 \leq x \leq +1$

Definition at line 2117 of file specfun.h.

8.3.3.28 `float __gnu_cxx::chebyshev_wf (unsigned int __n, float __x) [inline]`

Return the Chebyshev polynomials of the fourth kind $W_n(x)$ of non-negative order n and `float` argument x .

See also

[chebyshev_w](#) for details.

Definition at line 2087 of file specfun.h.

8.3.3.29 `long double __gnu_cxx::chebyshev_wl (unsigned int __n, long double __x) [inline]`

Return the Chebyshev polynomials of the fourth kind $W_n(x)$ of non-negative order n and real argument x .

See also

[chebyshev_w](#) for details.

Definition at line 2097 of file specfun.h.

8.3.3.30 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::clausen (unsigned int __m, _Tp __w) [inline]`

Return the Clausen function $Cl_n(w)$ of integer order m and real argument w .

The Clausen function is defined by

$$Cl_n(w) = S_n(w) = \sum_{k=1}^{\infty} \frac{\sin(kx)}{k^n} \text{ for even } m = C_n(w) = \sum_{k=1}^{\infty} \frac{\cos(kx)}{k^n} \text{ for odd } m$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

$_m$	The integral order
$_w$	The complex argument

Definition at line 4897 of file specfun.h.

```
8.3.3.31 template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::clausen ( unsigned int __m,
std::complex<_Tp> __w ) [inline]
```

Return the Clausen function $Cl_n(w)$ of integer order m and complex argument w .

The Clausen function is defined by

$$Cl_n(w) = S_n(w) = \sum_{k=1}^{\infty} \frac{\sin(kx)}{k^n} \text{ for even } m = C_n(w) = \sum_{k=1}^{\infty} \frac{\cos(kx)}{k^n} \text{ for odd } m$$

Template Parameters

$_Tp$	The real type of the complex components
--------	---

Parameters

$_m$	The integral order
$_w$	The complex argument

Definition at line 4941 of file specfun.h.

```
8.3.3.32 template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::clausen_c ( unsigned int __m, _Tp __w )
[inline]
```

Return the Clausen cosine function $C_n(w)$ of order m and real argument w .

The Clausen cosine function is defined by

$$C_n(w) = \sum_{k=1}^{\infty} \frac{\cos(kx)}{k^n}$$

Template Parameters

$_Tp$	The real type of the argument
--------	-------------------------------

Parameters

\leftrightarrow <code>__m</code>	The unsigned integer order
\leftrightarrow <code>__w</code>	The real argument

Definition at line 4853 of file specfun.h.

8.3.3.33 `float __gnu_cxx::clausen_cf (unsigned int __m, float __w) [inline]`

Return the Clausen cosine function $C_n(w)$ of order m and `float` argument w .

See also

[clausen_c](#) for details.

Definition at line 4825 of file specfun.h.

8.3.3.34 `long double __gnu_cxx::clausen_cl (unsigned int __m, long double __w) [inline]`

Return the Clausen cosine function $C_n(w)$ of order m and `long double` argument w .

See also

[clausen_c](#) for details.

Definition at line 4835 of file specfun.h.

8.3.3.35 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::clausen_s (unsigned int __m, _Tp __w) [inline]`

Return the Clausen sine function $S_n(w)$ of order m and real argument w .

The Clausen sine function is defined by

$$S_n(w) = \sum_{k=1}^{\infty} \frac{\sin(kx)}{k^n}$$

Template Parameters

<code>__Tp</code>	The real type of the argument
-------------------	-------------------------------

Parameters

\leftrightarrow _m	The unsigned integer order
\leftrightarrow _w	The real argument

Definition at line 4810 of file specfun.h.

8.3.3.36 `float __gnu_cxx::clausen_sf (unsigned int __m, float __w) [inline]`

Return the Clausen sine function $S_n(w)$ of order m and `float` argument w .

See also

[clausen_s](#) for details.

Definition at line 4782 of file specfun.h.

8.3.3.37 `long double __gnu_cxx::clausen_sl (unsigned int __m, long double __w) [inline]`

Return the Clausen sine function $S_n(w)$ of order m and `long double` argument w .

See also

[clausen_s](#) for details.

Definition at line 4792 of file specfun.h.

8.3.3.38 `float __gnu_cxx::clausenf (unsigned int __m, float __w) [inline]`

Return the Clausen function $Cl_n(w)$ of integer order m and `float` argument w .

See also

[clausen](#) for details.

Definition at line 4868 of file specfun.h.

8.3.3.39 `std::complex<float> __gnu_cxx::clausenf (unsigned int __m, std::complex< float > __w) [inline]`

Return the Clausen function $Cl_n(w)$ of integer order m and `std::complex<float>` argument w .

See also

[clausen](#) for details.

Definition at line 4912 of file `specfun.h`.

8.3.3.40 `long double __gnu_cxx::clausenl (unsigned int __m, long double __w) [inline]`

Return the Clausen function $Cl_n(w)$ of integer order m and `long double` argument w .

See also

[clausen](#) for details.

Definition at line 4878 of file `specfun.h`.

8.3.3.41 `std::complex<long double> __gnu_cxx::clausenl (unsigned int __m, std::complex< long double > __w) [inline]`

Return the Clausen function $Cl_n(w)$ of integer order m and `std::complex<long double>` argument w .

See also

[clausen](#) for details.

Definition at line 4922 of file `specfun.h`.

8.3.3.42 `template<typename _Tk> __gnu_cxx::__promote_fp_t<_Tk> __gnu_cxx::comp_ellint_d (_Tk __k) [inline]`

Return the complete Legendre elliptic integral $D(k)$ of real modulus k .

The complete Legendre elliptic integral D is defined by

$$D(k) = \int_0^{\pi/2} \frac{\sin^2 \theta d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

Template Parameters

<code>_Tk</code>	The type of the modulus k
------------------	-----------------------------

Parameters

\leftrightarrow _k	The modulus $-1 \leq _k \leq +1$
-------------------------	-----------------------------------

Definition at line 4088 of file specfun.h.

8.3.3.43 `float __gnu_cxx::comp_ellint_df(float __k) [inline]`

Return the complete Legendre elliptic integral $D(k)$ of float modulus k .

See also

[comp_ellint_d](#) for details.

Definition at line 4061 of file specfun.h.

8.3.3.44 `long double __gnu_cxx::comp_ellint_dl(long double __k) [inline]`

Return the complete Legendre elliptic integral $D(k)$ of long double modulus k .

See also

[comp_ellint_d](#) for details.

Definition at line 4071 of file specfun.h.

8.3.3.45 `float __gnu_cxx::comp_ellint_rf(float __x, float __y) [inline]`

Return the complete Carlson elliptic function $R_F(x, y, z)$ for float arguments.

See also

[comp_ellint_rf](#) for details.

Definition at line 3008 of file specfun.h.

8.3.3.46 `long double __gnu_cxx::comp_ellint_rf(long double __x, long double __y) [inline]`

Return the complete Carlson elliptic function $R_F(x, y)$ for long double arguments.

See also

[comp_ellint_rf](#) for details.

Definition at line 3018 of file specfun.h.

8.3.3.47 `template<typename _Tx, typename _Ty> __gnu_cxx::__promote_fp_t<_Tx, _Ty> __gnu_cxx::comp_ellint_rf(_Tx __x, _Ty __y) [inline]`

Return the complete Carlson elliptic function $R_F(x, y)$ for real arguments.

The complete Carlson elliptic function of the first kind is defined by:

$$R_F(x, y) = R_F(x, y, y) = \frac{1}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)}$$

Parameters

\leftrightarrow __x	The first argument.
\leftrightarrow __y	The second argument.

Definition at line 3036 of file specfun.h.

8.3.3.48 `float __gnu_cxx::comp_ellint_rg (float __x, float __y) [inline]`

Return the Carlson complementary elliptic function $R_G(x, y)$.

See also

[comp_ellint_rg](#) for details.

Definition at line 3241 of file specfun.h.

8.3.3.49 `long double __gnu_cxx::comp_ellint_rg (long double __x, long double __y) [inline]`

Return the Carlson complementary elliptic function $R_G(x, y)$.

See also

[comp_ellint_rg](#) for details.

Definition at line 3250 of file specfun.h.

8.3.3.50 `template<typename _Tx, typename _Ty> __gnu_cxx::__promote_fp_t<_Tx, _Ty> __gnu_cxx::comp_ellint_rg (_Tx __x, _Ty __y) [inline]`

Return the complete Carlson elliptic function $R_G(x, y)$ for real arguments.

The complete Carlson elliptic function is defined by:

$$R_G(x, y) = R_G(x, y, y) = \frac{1}{4} \int_0^\infty dt t (t+x)^{-1/2} (t+y)^{-1} \left(\frac{x}{t+x} + \frac{2y}{t+y} \right)$$

Parameters

\leftrightarrow __x	The first argument.
\leftrightarrow __y	The second argument.

Definition at line 3269 of file specfun.h.

```
8.3.3.51 template<typename _Tpa , typename _Tpc , typename _Tp > __gnu_cxx::__promote_fp_t<_Tpa, _Tpc, _Tp>
        __gnu_cxx::conf_hyperg ( _Tpa __a, _Tpc __c, _Tp __x )  [inline]
```

Return the confluent hypergeometric function ${}_1F_1(a; c; x)$ of real numeratorial parameter a , denominatorial parameter c , and argument x .

The confluent hypergeometric function is defined by

$${}_1F_1(a; c; x) = \sum_{n=0}^{\infty} \frac{(a)_n x^n}{(c)_n n!}$$

where the Pochhammer symbol is $(x)_k = (x)(x+1)\dots(x+k-1)$, $(x)_0 = 1$

Parameters

\hookleftarrow _a	The numeratorial parameter
\hookleftarrow _c	The denominatorial parameter
\hookleftarrow _x	The argument

Definition at line 1398 of file specfun.h.

```
8.3.3.52 template<typename _Tpc , typename _Tp > __gnu_cxx::__promote_2<_Tpc, _Tp>::__type __gnu_cxx::conf_hyperg_lim (
        _Tpc __c, _Tp __x )  [inline]
```

Return the confluent hypergeometric limit function ${}_0F_1(; c; x)$ of real numeratorial parameter c and argument x .

The confluent hypergeometric limit function is defined by

$${}_0F_1(; c; x) = \sum_{n=0}^{\infty} \frac{x^n}{(c)_n n!}$$

where the Pochhammer symbol is $(x)_k = (x)(x+1)\dots(x+k-1)$, $(x)_0 = 1$

Parameters

\hookleftarrow _c	The denominatorial parameter
\hookleftarrow _x	The argument

Definition at line 1493 of file specfun.h.

8.3.3.53 `float __gnu_cxx::conf_hyperg_limf (float __c, float __x) [inline]`

Return the confluent hypergeometric limit function ${}_0F_1(; c; x)$ of `float` numeratorial parameter c and argument x .

See also

[conf_hyperg_lim](#) for details.

Definition at line 1464 of file `specfun.h`.

8.3.3.54 `long double __gnu_cxx::conf_hyperg_liml (long double __c, long double __x) [inline]`

Return the confluent hypergeometric limit function ${}_0F_1(; c; x)$ of `long double` numeratorial parameter c and argument x .

See also

[conf_hyperg_lim](#) for details.

Definition at line 1474 of file `specfun.h`.

8.3.3.55 `float __gnu_cxx::conf_hypergf (float __a, float __c, float __x) [inline]`

Return the confluent hypergeometric function ${}_1F_1(a; c; x)$ of `float` numeratorial parameter a , denominatorial parameter c , and argument x .

See also

[conf_hyperg](#) for details.

Definition at line 1366 of file `specfun.h`.

8.3.3.56 `long double __gnu_cxx::conf_hypergl (long double __a, long double __c, long double __x) [inline]`

Return the confluent hypergeometric function ${}_1F_1(a; c; x)$ of `long double` numeratorial parameter a , denominatorial parameter c , and argument x .

See also

[conf_hyperg](#) for details.

Definition at line 1377 of file `specfun.h`.

8.3.3.57 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::cos_pi (_Tp __x) [inline]`

Return the reperiodized cosine function $\cos_\pi(x)$ for real argument x .

The reperiodized cosine function is defined by:

$$\cos_\pi(x) = \cos(\pi x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 5528 of file `specfun.h`.

8.3.3.58 `float __gnu_cxx::cos_pif (float __x) [inline]`

Return the reperiodized cosine function $\cos_{\pi}(x)$ for `float` argument x .

See also

[cos_pi](#) for more details.

Definition at line 5501 of file `specfun.h`.

8.3.3.59 `long double __gnu_cxx::cos_pil (long double __x) [inline]`

Return the reperiodized cosine function $\cos_{\pi}(x)$ for `long double` argument x .

See also

[cos_pi](#) for more details.

Definition at line 5511 of file `specfun.h`.

8.3.3.60 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::cosh_pi (_Tp __x) [inline]`

Return the reperiodized hyperbolic cosine function $\cosh_{\pi}(x)$ for real argument x .

The reperiodized hyperbolic cosine function is defined by:

$$\cosh_{\pi}(x) = \cosh(\pi x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>_↔</code>	The argument
<code>_x</code>	

Definition at line 5570 of file specfun.h.

8.3.3.61 `float __gnu_cxx::cosh_pif (float __x) [inline]`

Return the reperiodized hyperbolic cosine function $\cosh_{\pi}(x)$ for `float` argument x .

See also

[cosh_pi](#) for more details.

Definition at line 5543 of file specfun.h.

8.3.3.62 `long double __gnu_cxx::cosh_pil (long double __x) [inline]`

Return the reperiodized hyperbolic cosine function $\cosh_{\pi}(x)$ for `long double` argument x .

See also

[cosh_pi](#) for more details.

Definition at line 5553 of file specfun.h.

8.3.3.63 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::coshint (_Tp __x) [inline]`

Return the hyperbolic cosine integral $Chi(x)$ of real argument x .

The hyperbolic cosine integral is defined by

$$Chi(x) = - \int_x^{\infty} \frac{\cosh(t)}{t} dt = \gamma_E + \ln(x) + \int_0^x \frac{\cosh(t) - 1}{t} dt$$

Template Parameters

<code>_Tp</code>	The type of the real argument
------------------	-------------------------------

Parameters

<code>_↔</code>	The real argument
<code>_x</code>	

Definition at line 1775 of file specfun.h.

8.3.3.64 `float __gnu_cxx::coshintf (float _x) [inline]`

Return the hyperbolic cosine integral of `float` argument x .

See also

[coshint](#) for details.

Definition at line 1747 of file specfun.h.

8.3.3.65 `long double __gnu_cxx::coshintl (long double _x) [inline]`

Return the hyperbolic cosine integral $Chi(x)$ of `long double` argument x .

See also

[coshint](#) for details.

Definition at line 1757 of file specfun.h.

8.3.3.66 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::cosint (_Tp _x) [inline]`

Return the cosine integral $Ci(x)$ of real argument x .

The cosine integral is defined by

$$Ci(x) = - \int_x^\infty \frac{\cos(t)}{t} dt = \gamma_E + \ln(x) + \int_0^x \frac{\cos(t) - 1}{t} dt$$

Parameters

<code>_↔</code>	The real upper integration limit
<code>_x</code>	

Definition at line 1692 of file specfun.h.

8.3.3.67 `float __gnu_cxx::cosintf (float __x) [inline]`

Return the cosine integral $Ci(x)$ of `float` argument x .

See also

[cosint](#) for details.

Definition at line 1666 of file `specfun.h`.

8.3.3.68 `long double __gnu_cxx::cosintl (long double __x) [inline]`

Return the cosine integral $Ci(x)$ of `long double` argument x .

See also

[cosint](#) for details.

Definition at line 1676 of file `specfun.h`.

8.3.3.69 `template<typename _Tpnu , typename _Tp > std::complex<__gnu_cxx::__promote_fp_t<_Tpnu, _Tp> > __gnu_cxx::cyl_hankel_1 (_Tpnu __nu, _Tp __z) [inline]`

Return the cylindrical Hankel function of the first kind $H_n^{(1)}(x)$ of real order ν and argument $x \geq 0$.

The cylindrical Hankel function of the first kind is defined by:

$$H_\nu^{(1)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} [J_{n+1/2}(x) + iN_{n+1/2}(x)]$$

where $J_\nu(x)$ and $N_\nu(x)$ are the cylindrical Bessel and Neumann functions respectively (

See also

`cyl_bessel` and `cyl_neumann`).

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__nu</code>	The real order
<code>__z</code>	The real argument

Definition at line 2466 of file specfun.h.

```
8.3.3.70  template<typename _Tpnu , typename _Tp > std::complex<__gnu_cxx::__promote_fp_t<_Tpnu, _Tp> >
          __gnu_cxx::cyl_hankel_1 ( std::complex<_Tpnu > __nu, std::complex<_Tp> __x )  [inline]
```

Return the complex cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$ of complex order ν and argument x .

The cylindrical Hankel function of the first kind is defined by

$$H_\nu^{(1)}(x) = J_\nu(x) + iN_\nu(x)$$

Template Parameters

<code>_Tpnu</code>	The complex type of the order
<code>_Tp</code>	The complex type of the argument

Parameters

<code>__nu</code>	The complex order
<code>__x</code>	The complex argument

Definition at line 4365 of file specfun.h.

```
8.3.3.71  std::complex<float> __gnu_cxx::cyl_hankel_1f ( float __nu, float __z )  [inline]
```

Return the cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$ of `float` order ν and argument $x \geq 0$.

See also

[cyl_hankel_1](#) for details.

Definition at line 2433 of file specfun.h.

```
8.3.3.72  std::complex<float> __gnu_cxx::cyl_hankel_1f ( std::complex<float> __nu, std::complex<float> __x )
          [inline]
```

Return the complex cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$ of `std::complex<float>` order ν and argument x .

See also

[cyl_hankel_1](#) for more details.

Definition at line 4334 of file specfun.h.

8.3.3.73 `std::complex<long double> __gnu_cxx::cyl_hankel_1l(long double __nu, long double __z)` `[inline]`

Return the cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$ of `long double` order ν and argument $x \geq 0$.

See also

[cyl_hankel_1](#) for details.

Definition at line 2444 of file `specfun.h`.

8.3.3.74 `std::complex<long double> __gnu_cxx::cyl_hankel_1l(std::complex< long double > __nu, std::complex< long double > __x)` `[inline]`

Return the complex cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$ of `std::complex<long double>` order ν and argument x .

See also

[cyl_hankel_1](#) for more details.

Definition at line 4345 of file `specfun.h`.

8.3.3.75 `template<typename _Tpnu, typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>> __gnu_cxx::cyl_hankel_2(_Tpnu __nu, _Tp __z)` `[inline]`

Return the cylindrical Hankel function of the second kind $H_n^{(2)}(x)$ of real order ν and argument $x \geq 0$.

The cylindrical Hankel function of the second kind is defined by:

$$H_\nu^{(2)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} [J_{n+1/2}(x) - iN_{n+1/2}(x)]$$

where $J_\nu(x)$ and $N_\nu(x)$ are the cylindrical Bessel and Neumann functions respectively (

See also

`cyl_bessel` and `cyl_neumann`).

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__nu</code>	The real order
<code>__z</code>	The real argument

Definition at line 2515 of file specfun.h.

8.3.3.76 `template<typename _Tpnu, typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tpnu, _Tp>> __gnu_cxx::cyl_hankel_2 (std::complex<_Tpnu> __nu, std::complex<_Tp> __x) [inline]`

Return the complex cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$ of complex order ν and argument x .

The cylindrical Hankel function of the second kind is defined by

$$H_\nu^{(2)}(x) = J_\nu(x) - iN_\nu(x)$$

Template Parameters

<code>_Tpnu</code>	The complex type of the order
<code>_Tp</code>	The complex type of the argument

Parameters

<code>__nu</code>	The complex order
<code>__x</code>	The complex argument

Definition at line 4412 of file specfun.h.

8.3.3.77 `std::complex<float> __gnu_cxx::cyl_hankel_2f (float __nu, float __z) [inline]`

Return the cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$ of `float` order ν and argument $x \geq 0$.

See also

[cyl_hankel_2](#) for details.

Definition at line 2482 of file specfun.h.

8.3.3.78 `std::complex<float> __gnu_cxx::cyl_hankel_2f (std::complex<float> __nu, std::complex<float> __x) [inline]`

Return the complex cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$ of `std::complex<float>` order ν and argument x .

See also

[cyl_hankel_2](#) for more details.

Definition at line 4381 of file specfun.h.

8.3.3.79 `std::complex<long double> __gnu_cxx::cyl_hankel_2l(long double __nu, long double __z)` `[inline]`

Return the cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$ of `long double` order ν and argument $x \geq 0$.

See also

[cyl_hankel_2](#) for details.

Definition at line 2493 of file `specfun.h`.

8.3.3.80 `std::complex<long double> __gnu_cxx::cyl_hankel_2l(std::complex< long double > __nu, std::complex< long double > __x)` `[inline]`

Return the complex cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$ of `std::complex<long double>` order ν and argument x .

See also

[cyl_hankel_2](#) for more details.

Definition at line 4392 of file `specfun.h`.

8.3.3.81 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::dawson(_Tp __x)` `[inline]`

Return the Dawson integral, $F(x)$, for real argument x .

The Dawson integral is defined by:

$$F(x) = e^{-x^2} \int_0^x e^{y^2} dy$$

and it's derivative is:

$$F'(x) = 1 - 2xF(x)$$

Parameters

<code>__x</code>	The argument $-inf < x < inf$.
------------------	---------------------------------

Definition at line 3591 of file `specfun.h`.

8.3.3.82 `float __gnu_cxx::dawsonf(float __x)` `[inline]`

Return the Dawson integral, $F(x)$, for `float` argument x .

See also

[dawson](#) for details.

Definition at line 3563 of file specfun.h.

8.3.3.83 `long double __gnu_cxx::dawsonl (long double __x) [inline]`

Return the Dawson integral, $F(x)$, for `long double` argument x .

See also

[dawson](#) for details.

Definition at line 3572 of file specfun.h.

8.3.3.84 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::dilog (_Tp __x) [inline]`

Return the dilogarithm function $\psi(z)$ for real argument.

The dilogarithm is defined by:

$$Li_2(x) = \sum_{k=1}^{\infty} \frac{x^k}{k^2}$$

Parameters

<code>__x</code>	The argument.
------------------	---------------

Definition at line 2993 of file specfun.h.

8.3.3.85 `float __gnu_cxx::dilogf (float __x) [inline]`

Return the dilogarithm function $\psi(z)$ for `float` argument.

See also

[dilog](#) for details.

Definition at line 2967 of file specfun.h.

8.3.3.86 `long double __gnu_cxx::dilog(long double __x)` `[inline]`

Return the dilogarithm function $\psi(z)$ for `long double` argument.

See also

[dilog](#) for details.

Definition at line 2977 of file `specfun.h`.

8.3.3.87 `template<typename _Tp> _Tp __gnu_cxx::dirichlet_beta (_Tp __s)` `[inline]`

Return the Dirichlet beta function of real argument s .

The Dirichlet beta function is defined by:

$$\beta(s) = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)^s}$$

An important reflection formula is:

$$\beta(1-s) = \left(\frac{2}{\pi}\right)^s \sin\left(\frac{\pi s}{2}\right) \Gamma(s) \beta(s)$$

Parameters

<code>__s</code>	
------------------	--

Definition at line 4728 of file `specfun.h`.

8.3.3.88 `float __gnu_cxx::dirichlet_betaf (float __s)` `[inline]`

Return the Dirichlet beta function of real argument s .

See also

[dirichlet_beta](#) for details.

Definition at line 4699 of file `specfun.h`.

8.3.3.89 `long double __gnu_cxx::dirichlet_betal (long double __s)` `[inline]`

Return the Dirichlet beta function of real argument s .

See also

[dirichlet_beta](#) for details.

Definition at line 4708 of file `specfun.h`.

8.3.3.90 `template<typename _Tp> _Tp __gnu_cxx::dirichlet_eta (_Tp __s) [inline]`

Return the Dirichlet eta function of real argument s .

The Dirichlet eta function is defined by

$$\eta(s) = \sum_{k=1}^{\infty} \frac{(-1)^k}{k^s} = (1 - 2^{1-s}) \zeta(s)$$

An important reflection formula is:

$$\eta(-s) = 2 \frac{1 - 2^{-s-1}}{1 - 2^{-s}} \pi^{-s-1} s \sin\left(\frac{\pi s}{2}\right) \Gamma(s) \eta(s+1)$$

Parameters

\leftarrow	
s	

Definition at line 4685 of file specfun.h.

8.3.3.91 `float __gnu_cxx::dirichlet_etaf (float __s) [inline]`

Return the Dirichlet eta function of real argument s .

See also

[dirichlet_eta](#) for details.

Definition at line 4655 of file specfun.h.

8.3.3.92 `long double __gnu_cxx::dirichlet_etalf (long double __s) [inline]`

Return the Dirichlet eta function of real argument s .

See also

[dirichlet_eta](#) for details.

Definition at line 4664 of file specfun.h.

8.3.3.93 `template<typename _Tp> _Tp __gnu_cxx::dirichlet_lambda (_Tp __s) [inline]`

Return the Dirichlet lambda function of real argument s .

The Dirichlet lambda function is defined by

$$\lambda(s) = \sum_{k=0}^{\infty} \frac{1}{(2k+1)^s} = (1 - 2^{-s}) \zeta(s)$$

Parameters

\longleftrightarrow	
s	

Definition at line 4767 of file specfun.h.

8.3.3.94 `float __gnu_cxx::dirichlet_lambdaf (float s)` `[inline]`

Return the Dirichlet lambda function of real argument s .

See also

[dirichlet_lambda](#) for details.

Definition at line 4742 of file specfun.h.

8.3.3.95 `long double __gnu_cxx::dirichlet_lambdal (long double s)` `[inline]`

Return the Dirichlet lambda function of real argument s .

See also

[dirichlet_lambda](#) for details.

Definition at line 4751 of file specfun.h.

8.3.3.96 `template<typename T_p > __gnu_cxx::__promote_fp_t< T_p > __gnu_cxx::double_factorial (int n)` `[inline]`

Definition at line 3763 of file specfun.h.

8.3.3.97 `float __gnu_cxx::double_factorialf (int n)` `[inline]`

Definition at line 3751 of file specfun.h.

8.3.3.98 `long double __gnu_cxx::double_factoriall (int n)` `[inline]`

Definition at line 3755 of file specfun.h.

8.3.3.99 `template<typename T_k , typename T_p , typename T_a , typename T_b > __gnu_cxx::__promote_fp_t< T_k , T_p , T_a , T_b > __gnu_cxx::ellint_cel (T_k k_c , T_p p , T_a a , T_b b)` `[inline]`

Return the Bulirsch complete elliptic integral $cel(k_c, p, a, b)$ of real complementary modulus k_c , and parameters p , a , and b .

The Bulirsch complete elliptic integral is defined by

$$cel(k_c, p, a, b) = \int_0^{\pi/2} \frac{a \cos^2 \theta + b \sin^2 \theta}{\cos^2 \theta + p \sin^2 \theta} \frac{d\theta}{\sqrt{\cos^2 \theta + k_c^2 \sin^2 \theta}}$$

Parameters

<code>__k↔ __c</code>	The complementary modulus $k_c = \sqrt{1 - k^2}$
<code>__p</code>	The parameter
<code>__a</code>	The parameter
<code>__b</code>	The parameter

Definition at line 4318 of file specfun.h.

8.3.3.100 `float __gnu_cxx::ellint_celf (float __k_c, float __p, float __a, float __b) [inline]`

Return the Bulirsch complete elliptic integral $cel(k_c, p, a, b)$ of real complementary modulus k_c , and parameters p , a , and b .

See also

[ellint_cel](#) for details.

Definition at line 4286 of file specfun.h.

8.3.3.101 `long double __gnu_cxx::ellint_cell (long double __k_c, long double __p, long double __a, long double __b) [inline]`

Return the Bulirsch complete elliptic integral $cel(k_c, p, a, b)$.

See also

[ellint_cel](#) for details.

Definition at line 4295 of file specfun.h.

8.3.3.102 `template<typename _Tk, typename _Tphi> __gnu_cxx::__promote_fp_t<_Tk, _Tphi> __gnu_cxx::ellint_d (_Tk __k, _Tphi __phi) [inline]`

Return the incomplete Legendre elliptic integral $D(k, \phi)$ of real modulus k and angular limit ϕ .

The Legendre elliptic integral D is defined by

$$D(k, \phi) = \int_0^\phi \frac{\sin^2 \theta d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

Parameters

<code>__k</code>	The modulus $-1 \leq \text{__k} \leq +1$
<code>__phi</code>	The angle

Definition at line 4131 of file `specfun.h`.

8.3.3.103 `float __gnu_cxx::ellint_df (float __k, float __phi) [inline]`

Return the incomplete Legendre elliptic integral $D(k, \phi)$ of `float` modulus k and angular limit ϕ .

See also

[ellint_d](#) for details.

Definition at line 4103 of file `specfun.h`.

8.3.3.104 `long double __gnu_cxx::ellint_dl (long double __k, long double __phi) [inline]`

Return the incomplete Legendre elliptic integral $D(k, \phi)$ of `long double` modulus k and angular limit ϕ .

See also

[ellint_d](#) for details.

Definition at line 4113 of file `specfun.h`.

8.3.3.105 `template<typename _Tp, typename _Tk> __gnu_cxx::__promote_fp_t<_Tp, _Tk> __gnu_cxx::ellint_el1 (_Tp __x, _Tk __k_c) [inline]`

Return the Bulirsch elliptic integral $el1(x, k_c)$ of the first kind of real tangent limit x and complementary modulus k_c .

The Bulirsch elliptic integral of the first kind is defined by

$$el1(x, k_c) = el2(x, k_c, 1, 1) = \int_0^{\arctan x} \frac{1 + \tan^2 \theta}{\sqrt{(1 + \tan^2 \theta)(1 + k_c^2 \tan^2 \theta)}} d\theta$$

Parameters

<code>__x</code>	The tangent of the angular integration limit
<code>__k_c</code>	The complementary modulus $k_c = \sqrt{1 - k^2}$

Definition at line 4177 of file specfun.h.

8.3.3.106 `float __gnu_cxx::ellint_el1f (float __x, float __k_c) [inline]`

Return the Bulirsch elliptic integral $el1(x, k_c)$ of the first kind of `float` tangent limit x and complementary modulus k_c .

See also

[ellint_el1](#) for details.

Definition at line 4147 of file specfun.h.

8.3.3.107 `long double __gnu_cxx::ellint_el1l (long double __x, long double __k_c) [inline]`

Return the Bulirsch elliptic integral $el1(x, k_c)$ of the first kind of real tangent limit x and complementary modulus k_c .

See also

[ellint_el1](#) for details.

Definition at line 4158 of file specfun.h.

8.3.3.108 `template<typename _Tp, typename _Tk, typename _Ta, typename _Tb> __gnu_cxx::__promote_fp_t<_Tp, _Tk, _Ta, _Tb> __gnu_cxx::ellint_el2 (_Tp __x, _Tk __k_c, _Ta __a, _Tb __b) [inline]`

Return the Bulirsch elliptic integral of the second kind $el2(x, k_c, a, b)$.

The Bulirsch elliptic integral of the second kind is defined by

$$el2(x, k_c, a, b) = \int_0^{\arctan x} \frac{a + b \tan^2 \theta}{\sqrt{(1 + \tan^2 \theta)(1 + k_c^2 \tan^2 \theta)}} d\theta$$

Parameters

<code>__x</code>	The tangent of the angular integration limit
<code>__k_c</code>	The complementary modulus $k_c = \sqrt{1 - k^2}$
<code>__a</code>	The parameter
<code>__b</code>	The parameter

Definition at line 4223 of file specfun.h.

8.3.3.109 `float __gnu_cxx::ellint_el2f (float __x, float __k_c, float __a, float __b) [inline]`

Return the Bulirsch elliptic integral of the second kind $el2(x, k_c, a, b)$.

See also

[ellint_el2](#) for details.

Definition at line 4192 of file specfun.h.

8.3.3.110 `long double __gnu_cxx::ellint_el2l (long double __x, long double __k_c, long double __a, long double __b) [inline]`

Return the Bulirsch elliptic integral of the second kind $el2(x, k_c, a, b)$.

See also

[ellint_el2](#) for details.

Definition at line 4202 of file specfun.h.

8.3.3.111 `template<typename _Tx, typename _Tk, typename _Tp> __gnu_cxx::__promote_fp_t<_Tx, _Tk, _Tp> __gnu_cxx::ellint_el3 (_Tx __x, _Tk __k_c, _Tp __p) [inline]`

Return the Bulirsch elliptic integral of the third kind $el3(x, k_c, p)$ of real tangent limit x , complementary modulus k_c , and parameter p .

The Bulirsch elliptic integral of the third kind is defined by

$$el3(x, k_c, p) = \int_0^{\arctan x} \frac{d\theta}{(\cos^2 \theta + p \sin^2 \theta) \sqrt{\cos^2 \theta + k_c^2 \sin^2 \theta}}$$

Parameters

<code>__x</code>	The tangent of the angular integration limit
<code>__k_c</code>	The complementary modulus $k_c = \sqrt{1 - k^2}$
<code>__p</code>	The parameter

Definition at line 4270 of file specfun.h.

8.3.3.112 `float __gnu_cxx::ellint_el3f (float __x, float __k_c, float __p) [inline]`

Return the Bulirsch elliptic integral of the third kind $el3(x, k_c, p)$ of `float` tangent limit x , complementary modulus k_c , and parameter p .

See also

[ellint_el3](#) for details.

Definition at line 4239 of file `specfun.h`.

8.3.3.113 `long double __gnu_cxx::ellint_el3l (long double __x, long double __k_c, long double __p) [inline]`

Return the Bulirsch elliptic integral of the third kind $el3(x, k_c, p)$ of `long double` tangent limit x , complementary modulus k_c , and parameter p .

See also

[ellint_el3](#) for details.

Definition at line 4250 of file `specfun.h`.

8.3.3.114 `template<typename _Tp, typename _Up> __gnu_cxx::__promote_fp_t<_Tp, _Up> __gnu_cxx::ellint_rc (_Tp __x, _Up __y) [inline]`

Return the Carlson elliptic function $R_C(x, y) = R_F(x, y, y)$ where $R_F(x, y, z)$ is the Carlson elliptic function of the first kind.

The Carlson elliptic function is defined by:

$$R_C(x, y) = \frac{1}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first argument.
<code>__y</code>	The second argument.

Definition at line 3128 of file specfun.h.

8.3.3.115 `float __gnu_cxx::ellint_rcf (float __x, float __y) [inline]`

Return the Carlson elliptic function $R_C(x, y)$.

See also

[ellint_rc](#) for details.

Definition at line 3094 of file specfun.h.

8.3.3.116 `long double __gnu_cxx::ellint_rcl (long double __x, long double __y) [inline]`

Return the Carlson elliptic function $R_C(x, y)$.

See also

[ellint_rc](#) for details.

Definition at line 3103 of file specfun.h.

8.3.3.117 `template<typename _Tp, typename _Up, typename _Vp> __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp> __gnu_cxx::ellint_rd (_Tp __x, _Up __y, _Vp __z) [inline]`

Return the Carlson elliptic function of the second kind $R_D(x, y, z) = R_J(x, y, z, z)$ where $R_J(x, y, z, p)$ is the Carlson elliptic function of the third kind.

The Carlson elliptic function of the second kind is defined by:

$$R_D(x, y, z) = \frac{3}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{3/2}}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first of two symmetric arguments.
<code>__y</code>	The second of two symmetric arguments.
<code>__z</code>	The third argument.

Definition at line 3227 of file specfun.h.

8.3.3.118 `float __gnu_cxx::ellint_rdf (float __x, float __y, float __z) [inline]`

Return the Carlson elliptic function $R_D(x, y, z)$.

See also

[ellint_rd](#) for details.

Definition at line 3191 of file specfun.h.

8.3.3.119 `long double __gnu_cxx::ellint_rdl (long double __x, long double __y, long double __z) [inline]`

Return the Carlson elliptic function $R_D(x, y, z)$.

See also

[ellint_rd](#) for details.

Definition at line 3200 of file specfun.h.

8.3.3.120 `template<typename _Tp, typename _Up, typename _Vp> __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp> __gnu_cxx::ellint_rf (_Tp __x, _Up __y, _Vp __z) [inline]`

Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind for real arguments.

The Carlson elliptic function of the first kind is defined by:

$$R_F(x, y, z) = \frac{1}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{1/2}}$$

Parameters

<code>__x</code>	The first of three symmetric arguments.
<code>__y</code>	The second of three symmetric arguments.
<code>__z</code>	The third of three symmetric arguments.

Definition at line 3080 of file specfun.h.

8.3.3.121 `float __gnu_cxx::ellint_rff (float __x, float __y, float __z) [inline]`

Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind for `float` arguments.

See also

[ellint_rf](#) for details.

Definition at line 3051 of file `specfun.h`.

8.3.3.122 `long double __gnu_cxx::ellint_rfl (long double __x, long double __y, long double __z) [inline]`

Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind for `long double` arguments.

See also

[ellint_rf](#) for details.

Definition at line 3061 of file `specfun.h`.

8.3.3.123 `template<typename _Tp, typename _Up, typename _Vp> __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp> __gnu_cxx::ellint_rg (_Tp __x, _Up __y, _Vp __z) [inline]`

Return the symmetric Carlson elliptic function of the second kind $R_G(x, y, z)$.

The Carlson symmetric elliptic function of the second kind is defined by:

$$R_G(x, y, z) = \frac{1}{4} \int_0^\infty dt [(t+x)(t+y)(t+z)]^{-1/2} \left(\frac{x}{t+x} + \frac{y}{t+y} + \frac{z}{t+z} \right)$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first of three symmetric arguments.
<code>__y</code>	The second of three symmetric arguments.
<code>__z</code>	The third of three symmetric arguments.

Definition at line 3318 of file specfun.h.

8.3.3.124 `float __gnu_cxx::ellint_rgf (float __x, float __y, float __z) [inline]`

Return the Carlson elliptic function $R_G(x, y)$.

See also

[ellint_rg](#) for details.

Definition at line 3283 of file specfun.h.

8.3.3.125 `long double __gnu_cxx::ellint_rgl (long double __x, long double __y, long double __z) [inline]`

Return the Carlson elliptic function $R_G(x, y)$.

See also

[ellint_rg](#) for details.

Definition at line 3292 of file specfun.h.

8.3.3.126 `template<typename _Tp, typename _Up, typename _Vp, typename _Wp> __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp, _Wp> __gnu_cxx::ellint_rj (_Tp __x, _Up __y, _Vp __z, _Wp __p) [inline]`

Return the Carlson elliptic function $R_J(x, y, z, p)$ of the third kind.

The Carlson elliptic function of the third kind is defined by:

$$R_J(x, y, z, p) = \frac{3}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{1/2}(t+p)}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first of three symmetric arguments.
<code>__y</code>	The second of three symmetric arguments.
<code>__z</code>	The third of three symmetric arguments.
<code>__p</code>	The fourth argument.

Definition at line 3177 of file specfun.h.

8.3.3.127 `float __gnu_cxx::ellint_rjf (float __x, float __y, float __z, float __p) [inline]`

Return the Carlson elliptic function $R_J(x, y, z, p)$.

See also

[ellint_rj](#) for details.

Definition at line 3142 of file specfun.h.

8.3.3.128 `long double __gnu_cxx::ellint_rjl (long double __x, long double __y, long double __z, long double __p) [inline]`

Return the Carlson elliptic function $R_J(x, y, z, p)$.

See also

[ellint_rj](#) for details.

Definition at line 3151 of file specfun.h.

8.3.3.129 `template<typename _Tp> _Tp __gnu_cxx::ellnome (_Tp __k) [inline]`

Return the elliptic nome function $q(k)$ of modulus k .

The elliptic nome function is defined by

$$q(k) = \exp \left(-\pi \frac{K(k)}{K(\sqrt{1-k^2})} \right)$$

where $K(k)$ is the complete elliptic function of the first kind.

Template Parameters

<code>_Tp</code>	The real type of the modulus
------------------	------------------------------

Parameters

<code>↵ _k</code>	The modulus $-1 \leq k \leq +1$
-----------------------	---------------------------------

Definition at line 5155 of file specfun.h.

8.3.3.130 `float __gnu_cxx::ellnomef (float __k) [inline]`

Return the elliptic nome function $q(k)$ of modulus k .

See also

[ellnome](#) for details.

Definition at line 5128 of file specfun.h.

8.3.3.131 `long double __gnu_cxx::ellnomel (long double __k) [inline]`

Return the elliptic nome function $q(k)$ of long double modulus k .

See also

[ellnome](#) for details.

Definition at line 5138 of file specfun.h.

8.3.3.132 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::expint (unsigned int __n, _Tp __x) [inline]`

Return the exponential integral $E_n(x)$ of integral order n and real argument x . The exponential integral is defined by:

$$E_n(x) = \int_1^\infty \frac{e^{-tx}}{t^n} dt$$

In particular

$$E_1(x) = \int_1^\infty \frac{e^{-tx}}{t} dt = -Ei(-x)$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__n</code>	The integral order
<code>__x</code>	The real argument

Definition at line 3637 of file specfun.h.

8.3.3.133 `float __gnu_cxx::expintf (unsigned int __n, float __x) [inline]`

Return the exponential integral $E_n(x)$ for integral order n and `float` argument x .

See also

[expint](#) for details.

Definition at line 3606 of file `specfun.h`.

8.3.3.134 `long double __gnu_cxx::expintl (unsigned int __n, long double __x) [inline]`

Return the exponential integral $E_n(x)$ for integral order n and `long double` argument x .

See also

[expint](#) for details.

Definition at line 3616 of file `specfun.h`.

8.3.3.135 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::factorial (unsigned int __n) [inline]`

Definition at line 3742 of file `specfun.h`.

8.3.3.136 `float __gnu_cxx::factorialf (unsigned int __n) [inline]`

Definition at line 3730 of file `specfun.h`.

8.3.3.137 `long double __gnu_cxx::factoriall (unsigned int __n) [inline]`

Definition at line 3734 of file `specfun.h`.

8.3.3.138 `template<typename _Tps, typename _Tp> __gnu_cxx::__promote_fp_t<_Tps, _Tp> __gnu_cxx::fermi_dirac (_Tps __s, _Tp __x) [inline]`

Definition at line 5384 of file `specfun.h`.

8.3.3.139 `float __gnu_cxx::fermi_diracf (float __s, float __x) [inline]`

Definition at line 5375 of file `specfun.h`.

8.3.3.140 `long double __gnu_cxx::fermi_diracl (long double __s, long double __x) [inline]`

Definition at line 5379 of file `specfun.h`.

8.3.3.141 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::fresnel_c (_Tp __x) [inline]`

Return the Fresnel cosine integral of argument x .

The Fresnel cosine integral is defined by

$$C(x) = \int_0^x \cos\left(\frac{\pi}{2}t^2\right)dt$$

Parameters

\leftrightarrow	The argument
x	

Definition at line 3549 of file specfun.h.

8.3.3.142 `float __gnu_cxx::fresnel_cf (float x) [inline]`

Definition at line 3530 of file specfun.h.

8.3.3.143 `long double __gnu_cxx::fresnel_cl (long double x) [inline]`

Definition at line 3534 of file specfun.h.

8.3.3.144 `template<typename T_p > __gnu_cxx::__promote_fp_t< T_p > __gnu_cxx::fresnel_s (T_p x) [inline]`

Return the Fresnel sine integral of argument x .

The Fresnel sine integral is defined by

$$S(x) = \int_0^x \sin\left(\frac{\pi}{2}t^2\right)dt$$

Parameters

\leftrightarrow	The argument
x	

Definition at line 3521 of file specfun.h.

8.3.3.145 `float __gnu_cxx::fresnel_sf (float x) [inline]`

Definition at line 3502 of file specfun.h.

8.3.3.146 `long double __gnu_cxx::fresnel_sl (long double x) [inline]`

Definition at line 3506 of file specfun.h.

8.3.3.147 `template<typename _Talpha, typename _Tp> __gnu_cxx::__promote_fp_t<_Talpha, _Tp> __gnu_cxx::gegenbauer (unsigned int __n, _Talpha __alpha, _Tp __x) [inline]`

Return the Gegenbauer polynomial $C_n^\alpha(x)$ of degree n and real order $\alpha > -1/2, \alpha \neq 0$ and argument x .

The Gegenbauer polynomials are generated by a three-term recursion relation:

$$C_n^\alpha(x) = \frac{1}{n} [2x(n + \alpha - 1)C_{n-1}^\alpha(x) - (n + 2\alpha - 2)C_{n-2}^\alpha(x)]$$

and $C_0^\alpha(x) = 1, C_1^\alpha(x) = 2\alpha x$.

Template Parameters

<code>_Talpha</code>	The real type of the order
<code>_Tp</code>	The real type of the argument

Parameters

<code>__n</code>	The non-negative integral degree
<code>__alpha</code>	The real order
<code>__x</code>	The real argument

Definition at line 2225 of file `specfun.h`.

8.3.3.148 `float __gnu_cxx::gegenbauerf (unsigned int __n, float __alpha, float __x) [inline]`

Return the Gegenbauer polynomial $C_n^\alpha(x)$ of degree n and `float` order $\alpha > -1/2, \alpha \neq 0$ and argument x .

See also

[gegenbauer](#) for details.

Definition at line 2192 of file `specfun.h`.

8.3.3.149 `long double __gnu_cxx::gegenbauerl (unsigned int __n, long double __alpha, long double __x) [inline]`

Return the Gegenbauer polynomial $C_n^\alpha(x)$ of degree n and `long double` order $\alpha > -1/2, \alpha \neq 0$ and argument x .

See also

[gegenbauer](#) for details.

Definition at line 2203 of file `specfun.h`.


```
8.3.3.150 template<typename _Tk, typename _Tphi> __gnu_cxx::__promote_fp_t<_Tk, _Tphi> __gnu_cxx::heuman_lambda (
    _Tk __k, _Tphi __phi ) [inline]
```

Return the Heuman lambda function $\Lambda(k, \phi)$ of modulus k and angular limit ϕ .

The complete Heuman lambda function is defined by

$$\Lambda(k, \phi) = \frac{F(1-m, \phi)}{K(1-m)} + \frac{2}{\pi} K(m) Z(1-m, \phi)$$

where $m = k^2$, $K(k)$ is the complete elliptic function of the first kind, and $Z(k, \phi)$ is the Jacobi zeta function.

Template Parameters

<code>_Tk</code>	the floating-point type of the modulus
<code>_Tphi</code>	the floating-point type of the angular limit argument

Parameters

<code>__k</code>	The modulus
<code>__phi</code>	The angle

Definition at line 4046 of file specfun.h.

```
8.3.3.151 float __gnu_cxx::heuman_lambdaf ( float __k, float __phi ) [inline]
```

Definition at line 4020 of file specfun.h.

```
8.3.3.152 long double __gnu_cxx::heuman_lambdal ( long double __k, long double __phi ) [inline]
```

Definition at line 4024 of file specfun.h.

```
8.3.3.153 template<typename _Tp, typename _Up> __gnu_cxx::__promote_fp_t<_Tp, _Up> __gnu_cxx::hurwitz_zeta ( _Tp __s,
    _Up __a ) [inline]
```

Return the Hurwitz zeta function of real argument s , and parameter a .

The the Hurwitz zeta function is defined by

$$\zeta(s, a) = \sum_{n=0}^{\infty} \frac{1}{(a+n)^s}$$

Parameters

\leftrightarrow _s	The argument
\leftrightarrow _a	The parameter

Definition at line 3359 of file specfun.h.

```
8.3.3.154 template<typename _Tp, typename _Up> std::complex<_Tp> __gnu_cxx::hurwitz_zeta ( _Tp __s, std::complex<_Up> __a )
```

Return the Hurwitz zeta function of real argument s , and complex parameter a .

See also

[hurwitz_zeta](#) for details.

Definition at line 3373 of file specfun.h.

```
8.3.3.155 float __gnu_cxx::hurwitz_zetaf ( float __s, float __a ) [inline]
```

Return the Hurwitz zeta function of `float` argument s , and parameter a .

See also

[hurwitz_zeta](#) for details.

Definition at line 3333 of file specfun.h.

```
8.3.3.156 long double __gnu_cxx::hurwitz_zetal ( long double __s, long double __a ) [inline]
```

Return the Hurwitz zeta function of `long double` argument s , and parameter a .

See also

[hurwitz_zeta](#) for details.

Definition at line 3343 of file specfun.h.

```
8.3.3.157 template<typename _Tpa, typename _Tpb, typename _Tpc, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpa, _Tpb, _Tpc, _Tp> __gnu_cxx::hyperg ( _Tpa __a, _Tpb __b, _Tpc __c, _Tp __x ) [inline]
```

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ of real numeratorial parameters a and b , denominatorial parameter c , and argument x .

The hypergeometric function is defined by

$${}_2F_1(a, b; c; x) = \sum_{n=0}^{\infty} \frac{(a)_n (b)_n x^n}{(c)_n n!}$$

where the Pochhammer symbol is $(x)_k = (x)(x+1)\dots(x+k-1)$, $(x)_0 = 1$

Parameters

\leftrightarrow _a	The first numeratorial parameter
\leftrightarrow _b	The second numeratorial parameter
\leftrightarrow _c	The denominatorial parameter
\leftrightarrow _x	The argument

Definition at line 1447 of file specfun.h.

8.3.3.158 `float __gnu_cxx::hypergf (float __a, float __b, float __c, float __x) [inline]`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ of @ float numeratorial parameters a and b , denominatorial parameter c , and argument x .

See also

[hyperg](#) for details.

Definition at line 1414 of file specfun.h.

8.3.3.159 `long double __gnu_cxx::hypergl (long double __a, long double __b, long double __c, long double __x) [inline]`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ of long double numeratorial parameters a and b , denominatorial parameter c , and argument x .

See also

[hyperg](#) for details.

Definition at line 1425 of file specfun.h.

8.3.3.160 `template<typename _Ta, typename _Tb, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp> __gnu_cxx::ibeta (_Ta __a, _Tb __b, _Tp __x) [inline]`

Return the regularized incomplete beta function of parameters a , b , and argument x .

The regularized incomplete beta function is defined by

$$I_x(a, b) = \frac{B_x(a, b)}{B(a, b)}$$

where

$$B_x(a, b) = \int_0^x t^{a-1} (1-t)^{b-1} dt$$

is the non-regularized incomplete beta function and $B(a, b)$ is the usual beta function.

Parameters

\leftrightarrow _a	The first parameter
\leftrightarrow _b	The second parameter
\leftrightarrow _x	The argument

Definition at line 3462 of file specfun.h.

```
8.3.3.161  template<typename _Ta, typename _Tb, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp>
           __gnu_cxx::ibetac ( _Ta __a, _Tb __b, _Tp __x )  [inline]
```

Return the regularized complementary incomplete beta function of parameters a , b , and argument x .

The regularized complementary incomplete beta function is defined by

$$I_x(a, b) = I_x(a, b)$$

Parameters

\leftrightarrow _a	The parameter
\leftrightarrow _b	The parameter
\leftrightarrow _x	The argument

Definition at line 3493 of file specfun.h.

```
8.3.3.162  float __gnu_cxx::ibetacf ( float __a, float __b, float __x )  [inline]
```

Definition at line 3471 of file specfun.h.

References `__gnu_cxx::ibetaf()`.

```
8.3.3.163  long double __gnu_cxx::ibetacl ( long double __a, long double __b, long double __x )  [inline]
```

Definition at line 3475 of file specfun.h.

References `__gnu_cxx::ibetal()`.

8.3.3.164 `float __gnu_cxx::ibetaf (float __a, float __b, float __x) [inline]`

Return the regularized incomplete beta function of parameters a , b , and argument x .

See `ibeta` for details.

Definition at line 3428 of file `specfun.h`.

Referenced by `__gnu_cxx::ibetaf()`.

8.3.3.165 `long double __gnu_cxx::ibetal (long double __a, long double __b, long double __x) [inline]`

Return the regularized incomplete beta function of parameters a , b , and argument x .

See `ibeta` for details.

Definition at line 3438 of file `specfun.h`.

Referenced by `__gnu_cxx::ibetac()`.

8.3.3.166 `template<typename _Talpha, typename _Tbeta, typename _Tp> __gnu_cxx::__promote_fp_t<_Talpha, _Tbeta, _Tp> __gnu_cxx::jacobi (unsigned __n, _Talpha __alpha, _Tbeta __beta, _Tp __x) [inline]`

Return the Jacobi polynomial $P_n^{(\alpha, \beta)}(x)$ of degree n and `float` orders $\alpha, \beta > -1$ and argument x .

The Jacobi polynomials are generated by a three-term recursion relation:

$$2n(\alpha + \beta + n)(\alpha + \beta + 2n - 2)P_n^{(\alpha, \beta)}(x) = (\alpha + \beta + 2n - 1)((\alpha^2 - \beta^2) + x(\alpha + \beta + 2n - 2)(\alpha + \beta + 2n))P_{n-1}^{(\alpha, \beta)}(x) - 2(\alpha + n - 1)(\beta + n - 1)(\alpha + \beta + 2n - 2)P_{n-2}^{(\alpha, \beta)}(x)$$

where $P_0^{(\alpha, \beta)}(x) = 1$ and $P_1^{(\alpha, \beta)}(x) = ((\alpha - \beta) + (2 + (\alpha + \beta)) * x) / 2$.

Template Parameters

<code>_Talpha</code>	The real type of the order α
<code>_Tbeta</code>	The real type of the order β
<code>_Tp</code>	The real type of the argument

Parameters

<code>__n</code>	The non-negative integral degree
<code>__alpha</code>	The real order
<code>__beta</code>	The real order
<code>__x</code>	The real argument

Definition at line 2177 of file `specfun.h`.

References `std::__detail::__beta()`.

```
8.3.3.167 template<typename _Kp, typename _Up> __gnu_cxx::__promote_fp_t<_Kp, _Up> __gnu_cxx::jacobi_cn ( _Kp __k,
    _Up __u ) [inline]
```

Return the Jacobi elliptic $cn(k, u)$ integral of real modulus k and argument u .

The Jacobi elliptic cn integral is defined by

$$\cos(\phi) = cn(k, F(k, \phi))$$

where $F(k, \phi)$ is the elliptic integral of the first kind.

Template Parameters

<code>_Kp</code>	The type of the real modulus
<code>_Up</code>	The type of the real argument

Parameters

<code>↔ _k</code>	The real modulus
<code>↔ _u</code>	The real argument

Definition at line 1886 of file `specfun.h`.

```
8.3.3.168 float __gnu_cxx::jacobi_cnf ( float __k, float __u ) [inline]
```

Return the Jacobi elliptic $cn(k, u)$ integral of `float` modulus k and argument u .

See also

[jacobi_cn](#) for details.

Definition at line 1850 of file `specfun.h`.

```
8.3.3.169 long double __gnu_cxx::jacobi_cnl ( long double __k, long double __u ) [inline]
```

Return the Jacobi elliptic $cn(k, u)$ integral of `long double` modulus k and argument u .

See also

[jacobi_cn](#) for details.

Definition at line 1863 of file `specfun.h`.

8.3.3.170 `template<typename _Kp, typename _Up> __gnu_cxx::__promote_fp_t<_Kp, _Up> __gnu_cxx::jacobi_dn (_Kp __k, _Up __u) [inline]`

Return the Jacobi elliptic $dn(k, u)$ integral of real modulus k and argument u .

The Jacobi elliptic dn integral is defined by

$$\sqrt{1 - k^2 \sin(\phi)} = dn(k, F(k, \phi))$$

where $F(k, \phi)$ is the elliptic integral of the first kind.

Template Parameters

<code>_Kp</code>	The type of the real modulus
<code>_Up</code>	The type of the real argument

Parameters

<code>↔ _k</code>	The real modulus
<code>↔ _u</code>	The real argument

Definition at line 1938 of file `specfun.h`.

8.3.3.171 `float __gnu_cxx::jacobi_dnf (float __k, float __u) [inline]`

Return the Jacobi elliptic $dn(k, u)$ integral of `float` modulus k and argument u .

See also

[jacobi_dn](#) for details.

Definition at line 1902 of file `specfun.h`.

8.3.3.172 `long double __gnu_cxx::jacobi_dnl (long double __k, long double __u) [inline]`

Return the Jacobi elliptic $dn(k, u)$ integral of `long double` modulus k and argument u .

See also

[jacobi_dn](#) for details.

Definition at line 1915 of file `specfun.h`.

8.3.3.173 `template<typename _Kp, typename _Up> __gnu_cxx::__promote_fp_t<_Kp, _Up> __gnu_cxx::jacobi_sn (_Kp __k, _Up __u) [inline]`

Return the Jacobi elliptic $sn(k, u)$ integral of real modulus k and argument u .

The Jacobi elliptic `sn` integral is defined by

$$\sin(\phi) = sn(k, F(k, \phi))$$

where $F(k, \phi)$ is the elliptic integral of the first kind.

Template Parameters

<code>_Kp</code>	The type of the real modulus
<code>_Up</code>	The type of the real argument

Parameters

<code>↔ _k</code>	The real modulus
<code>↔ _u</code>	The real argument

Definition at line 1834 of file `specfun.h`.

8.3.3.174 `float __gnu_cxx::jacobi_snf (float __k, float __u) [inline]`

Return the Jacobi elliptic $sn(k, u)$ integral of `float` modulus k and argument u .

See also

[jacobi_sn](#) for details.

Definition at line 1798 of file `specfun.h`.

8.3.3.175 `long double __gnu_cxx::jacobi_snl (long double __k, long double __u) [inline]`

Return the Jacobi elliptic $sn(k, u)$ integral of `long double` modulus k and argument u .

See also

[jacobi_sn](#) for details.

Definition at line 1811 of file `specfun.h`.

8.3.3.176 `template<typename _Tk, typename _Tphi> __gnu_cxx::__promote_fp_t<_Tk, _Tphi> __gnu_cxx::jacobi_zeta (_Tk __k, _Tphi __phi) [inline]`

Return the Jacobi zeta function of k and ϕ .

The Jacobi zeta function is defined by

$$Z(m, \phi) = E(m, \phi) - \frac{E(m)F(m, \phi)}{K(m)}$$

where $E(m, \phi)$ is the elliptic function of the second kind, $E(m)$ is the complete elliptic function of the second kind, and $F(m, \phi)$ is the elliptic function of the first kind.

Template Parameters

<code>_Tk</code>	the real type of the modulus
<code>_Tphi</code>	the real type of the angle limit

Parameters

<code>__k</code>	The modulus
<code>__phi</code>	The angle

Definition at line 4011 of file `specfun.h`.

8.3.3.177 `float __gnu_cxx::jacobi_zetaf (float __k, float __phi) [inline]`

Definition at line 3986 of file `specfun.h`.

8.3.3.178 `long double __gnu_cxx::jacobi_zetal (long double __k, long double __phi) [inline]`

Definition at line 3990 of file `specfun.h`.

8.3.3.179 `float __gnu_cxx::jacobi (unsigned __n, float __alpha, float __beta, float __x) [inline]`

Return the Jacobi polynomial $P_n^{(\alpha, \beta)}(x)$ of degree n and `float` orders $\alpha, \beta > -1$ and argument x .

See also

[jacobi](#) for details.

Definition at line 2133 of file `specfun.h`.

References `std::__detail::__beta()`.

8.3.3.180 `long double __gnu_cxx::jacobi (unsigned __n, long double __alpha, long double __beta, long double __x)`
`[inline]`

Return the Jacobi polynomial $P_n^{(\alpha, \beta)}(x)$ of degree n and long double orders $\alpha, \beta > -1$ and argument x .

See also

[jacobi](#) for details.

Definition at line 2144 of file specfun.h.

References `std::__detail::__beta()`.

8.3.3.181 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::lbincoef (unsigned int __n, unsigned int __k)`
`[inline]`

Definition at line 3847 of file specfun.h.

8.3.3.182 `float __gnu_cxx::lbincoeff (unsigned int __n, unsigned int __k)` `[inline]`

Definition at line 3835 of file specfun.h.

8.3.3.183 `long double __gnu_cxx::lbincoefl (unsigned int __n, unsigned int __k)` `[inline]`

Definition at line 3839 of file specfun.h.

8.3.3.184 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::ldouble_factorial (int __n)` `[inline]`

Definition at line 3805 of file specfun.h.

8.3.3.185 `float __gnu_cxx::ldouble_factorialf (int __n)` `[inline]`

Definition at line 3793 of file specfun.h.

8.3.3.186 `long double __gnu_cxx::ldouble_factoriall (int __n)` `[inline]`

Definition at line 3797 of file specfun.h.

8.3.3.187 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::legendre_q (unsigned int __l, _Tp __x)`
`[inline]`

Return the Legendre function of the second kind $Q_l(x)$ of nonnegative degree l and real argument $|x| \leq 0$.

The Legendre function of the second kind of order l and argument x , $Q_l(x)$, is defined by:

$$Q_l(x) = \frac{1}{2} \log \frac{x+1}{x-1} P_l(x) - \sum_{k=0}^{l-1} \frac{(l+k)!}{(l-k)!(k!)^2 s^k} [\psi(l+1) - \psi(k+1)] (x-1)^k$$

where $P_l(x)$ is the Legendre polynomial of degree l and $\psi(x)$ is the psi or dilogarithm function.

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__l</code>	The degree $l \geq 0$
<code>__x</code>	The argument $\text{abs}(\text{__x}) \leq 1$

Exceptions

<code>std::domain_error</code>	if $\text{abs}(\text{__x}) > 1$
--------------------------------	---------------------------------

Definition at line 3935 of file `specfun.h`.

8.3.3.188 `float __gnu_cxx::legendre_qf (unsigned int __l, float __x) [inline]`

Return the Legendre function of the second kind $Q_l(x)$ of nonnegative degree l and `float` argument.

See also

[legendre_q](#) for details.

Definition at line 3901 of file `specfun.h`.

8.3.3.189 `long double __gnu_cxx::legendre_ql (unsigned int __l, long double __x) [inline]`

Return the Legendre function of the second kind $Q_l(x)$ of nonnegative degree l and `long double` argument.

See also

[legendre_q](#) for details.

Definition at line 3911 of file `specfun.h`.

8.3.3.190 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::lfactorial (unsigned int __n) [inline]`

Definition at line 3784 of file `specfun.h`.

8.3.3.191 `float __gnu_cxx::lfactorialf (unsigned int __n) [inline]`

Definition at line 3772 of file specfun.h.

8.3.3.192 `long double __gnu_cxx::lfactoriall (unsigned int __n) [inline]`

Definition at line 3776 of file specfun.h.

8.3.3.193 `template<typename _Ta> std::complex<__gnu_cxx::__promote_fp_t<_Ta>> __gnu_cxx::lgamma (std::complex<_Ta> __a) [inline]`

Return the logarithm of the gamma function for complex argument.

Definition at line 2846 of file specfun.h.

8.3.3.194 `std::complex<float> __gnu_cxx::lgammaf (std::complex<float> __a) [inline]`

Return the logarithm of the gamma function for `std::complex<float>` argument.

See also

[lgamma](#) for details.

Definition at line 2828 of file specfun.h.

8.3.3.195 `std::complex<long double> __gnu_cxx::lgammal (std::complex<long double> __a) [inline]`

Return the logarithm of the gamma function for `std::complex<long double>` argument.

See also

[lgamma](#) for details.

Definition at line 2838 of file specfun.h.

8.3.3.196 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::logint (_Tp __x) [inline]`

Return the logarithmic integral of argument x .

The logarithmic integral is defined by

$$li(x) = \int_0^x \frac{dt}{\ln(t)}$$

Parameters

$_x$	The real upper integration limit
-------	----------------------------------

Definition at line 1613 of file specfun.h.

8.3.3.197 `float __gnu_cxx::logintf (float __x) [inline]`

Return the logarithmic integral of argument x .

See also

[logint](#) for details.

Definition at line 1589 of file specfun.h.

8.3.3.198 `long double __gnu_cxx::logintl (long double __x) [inline]`

Return the logarithmic integral of argument x .

See also

[logint](#) for details.

Definition at line 1598 of file specfun.h.

8.3.3.199 `template<typename _Tp, typename _Tn> __gnu_cxx::__promote_fp_t<_Tp, _Tn> __gnu_cxx::lpochhammer (_Tp __a, _Tn __n) [inline]`

Definition at line 3658 of file specfun.h.

8.3.3.200 `template<typename _Tp, typename _Tn> __gnu_cxx::__promote_fp_t<_Tp, _Tn> __gnu_cxx::lpochhammer_lower (_Tp __a, _Tn __n) [inline]`

Definition at line 3679 of file specfun.h.

8.3.3.201 `float __gnu_cxx::lpochhammer_lowerf (float __a, float __n) [inline]`

Definition at line 3667 of file specfun.h.

8.3.3.202 `long double __gnu_cxx::lpochhammer_lowerl (long double __a, long double __n) [inline]`

Definition at line 3671 of file specfun.h.

8.3.3.203 `float __gnu_cxx::lpochhammerf (float __a, float __n) [inline]`

Definition at line 3646 of file specfun.h.

8.3.3.204 `long double __gnu_cxx::lpochhammerl (long double __a, long double __n) [inline]`

Definition at line 3650 of file specfun.h.

8.3.3.205 `template<typename _Tph, typename _Tpa> __gnu_cxx::__promote_fp_t<_Tph, _Tpa> __gnu_cxx::owens_t (_Tph __h, _Tpa __a) [inline]`

Return the Owens T function $T(h, a)$ of shape factor h and integration limit a .

The Owens T function is defined by

$$T(h, a) = \frac{1}{2\pi} \int_0^a \frac{\exp\left[-\frac{1}{2}h^2(1+x^2)\right]}{1+x^2} dx$$

Parameters

\leftrightarrow __h	The shape factor
\leftrightarrow __a	The integration limit

Definition at line 5366 of file specfun.h.

8.3.3.206 `float __gnu_cxx::owens_tf (float __h, float __a) [inline]`

Return the Owens T function $T(h, a)$ of shape factor h and integration limit a .

See also

[owens_t](#) for details.

Definition at line 5338 of file specfun.h.

8.3.3.207 `long double __gnu_cxx::owens_tl (long double __h, long double __a) [inline]`

Return the Owens T function $T(h, a)$ of `long double` shape factor h and integration limit a .

See also

[owens_t](#) for details.

Definition at line 5348 of file `specfun.h`.

8.3.3.208 `template<typename _Ta, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tp> __gnu_cxx::pgamma (_Ta __a, _Tp __x) [inline]`

Definition at line 3956 of file `specfun.h`.

8.3.3.209 `float __gnu_cxx::pgammaf (float __a, float __x) [inline]`

Definition at line 3944 of file `specfun.h`.

8.3.3.210 `long double __gnu_cxx::pgammal (long double __a, long double __x) [inline]`

Definition at line 3948 of file `specfun.h`.

8.3.3.211 `template<typename _Tp, typename _Tn> __gnu_cxx::__promote_fp_t<_Tp, _Tn> __gnu_cxx::pochhammer (_Tp __a, _Tn __n) [inline]`

Definition at line 3700 of file `specfun.h`.

8.3.3.212 `template<typename _Tp, typename _Tn> __gnu_cxx::__promote_fp_t<_Tp, _Tn> __gnu_cxx::pochhammer_lower (_Tp __a, _Tn __n) [inline]`

Definition at line 3721 of file `specfun.h`.

8.3.3.213 `float __gnu_cxx::pochhammer_lowerf (float __a, float __n) [inline]`

Definition at line 3709 of file `specfun.h`.

8.3.3.214 `long double __gnu_cxx::pochhammer_lowerl (long double __a, long double __n) [inline]`

Definition at line 3713 of file `specfun.h`.

8.3.3.215 `float __gnu_cxx::pochhammerf (float __a, float __n) [inline]`

Definition at line 3688 of file specfun.h.

8.3.3.216 `long double __gnu_cxx::pochhammerl (long double __a, long double __n) [inline]`

Definition at line 3692 of file specfun.h.

8.3.3.217 `template<typename _Tp, typename _Wp> __gnu_cxx::__promote_fp_t<_Tp, _Wp> __gnu_cxx::polylog (_Tp __s, _Wp __w) [inline]`

Return the complex polylogarithm function of real thing s and complex argument w .

The polylogarithm function is defined by

Parameters

\leftarrow __s	
\leftarrow __w	

Definition at line 4601 of file specfun.h.

8.3.3.218 `template<typename _Tp, typename _Wp> std::complex<__gnu_cxx::__promote_fp_t<_Tp, _Wp>> __gnu_cxx::polylog (_Tp __s, std::complex<_Tp> __w) [inline]`

Return the complex polylogarithm function of real thing s and complex argument w .

The polylogarithm function is defined by

Parameters

\leftarrow __s	
\leftarrow __w	

Definition at line 4641 of file specfun.h.

8.3.3.219 `float __gnu_cxx::polylogf (float __s, float __w) [inline]`

Return the real polylogarithm function of real thing s and real argument w .

See also

[polylog](#) for details.

Definition at line 4574 of file `specfun.h`.

8.3.3.220 `std::complex<float> __gnu_cxx::polylogf (float __s, std::complex<float> __w) [inline]`

Return the complex polylogarithm function of real thing s and complex argument w .

See also

[polylog](#) for details.

Definition at line 4614 of file `specfun.h`.

8.3.3.221 `long double __gnu_cxx::polylogl (long double __s, long double __w) [inline]`

Return the complex polylogarithm function of real thing s and complex argument w .

See also

[polylog](#) for details.

Definition at line 4584 of file `specfun.h`.

8.3.3.222 `std::complex<long double> __gnu_cxx::polylogl (long double __s, std::complex<long double> __w) [inline]`

Return the complex polylogarithm function of real thing s and complex argument w .

See also

[polylog](#) for details.

Definition at line 4624 of file `specfun.h`.

8.3.3.223 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::psi (_Tp __x) [inline]`

Return the psi or digamma function of argument x .

The the psi or digamma function is defined by

$$\psi(x) = \frac{d}{dx} \log(\Gamma(x)) = \frac{\Gamma'(x)}{\Gamma(x)}$$

Parameters

\leftrightarrow	The parameter
x	

Definition at line 3413 of file specfun.h.

8.3.3.224 `float __gnu_cxx::psif (float __x) [inline]`

Return the psi or digamma function of `float` argument x .

See also

[psi](#) for details.

Definition at line 3387 of file specfun.h.

8.3.3.225 `long double __gnu_cxx::psil (long double __x) [inline]`

Return the psi or digamma function of `long double` argument x .

See also

[psi](#) for details.

Definition at line 3397 of file specfun.h.

8.3.3.226 `template<typename _Ta, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tp> __gnu_cxx::qgamma (_Ta __a, _Tp __x) [inline]`

Definition at line 3977 of file specfun.h.

8.3.3.227 `float __gnu_cxx::qgammaf (float __a, float __x) [inline]`

Definition at line 3965 of file specfun.h.

8.3.3.228 `long double __gnu_cxx::qgamma (long double __a, long double __x) [inline]`

Definition at line 3969 of file specfun.h.

8.3.3.229 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::radpoly (unsigned int __n, unsigned int __m, _Tp __rho) [inline]`

Return the radial polynomial $R_n^m(\rho)$ for non-negative degree n , order $m \leq n$, and real radial argument ρ .

The radial polynomials are defined by

$$R_n^m(\rho) = \sum_{k=0}^{\frac{n-m}{2}} \frac{(-1)^k (n-k)!}{k! \left(\frac{n+m}{2} - k\right)! \left(\frac{n-m}{2} - k\right)!} \rho^{n-2k}$$

for $n - m$ even and identically 0 for $n - m$ odd. The radial polynomials can be related to the Jacobi polynomials:

$$R_n^m(\rho) =$$

See also

[jacobi](#) for details on the Jacobi polynomials.

Template Parameters

<code>_Tp</code>	The real type of the radial coordinate
------------------	--

Parameters

<code>__n</code>	The non-negative degree.
<code>__m</code>	The non-negative azimuthal order
<code>__rho</code>	The radial argument

Definition at line 2335 of file `specfun.h`.

8.3.3.230 `float __gnu_cxx::radpolyf (unsigned int __n, unsigned int __m, float __rho) [inline]`

Return the radial polynomial $R_n^m(\rho)$ for non-negative degree n , order $m \leq n$, and `float` radial argument ρ .

See also

[radpoly](#) for details.

Definition at line 2296 of file `specfun.h`.

References `std::__detail::__poly_radial_jacobi()`.

8.3.3.231 `long double __gnu_cxx::radpolyl (unsigned int __n, unsigned int __m, long double __rho) [inline]`

Return the radial polynomial $R_n^m(\rho)$ for non-negative degree n , order $m \leq n$, and long double radial argument ρ .

See also

[radpoly](#) for details.

Definition at line 2307 of file specfun.h.

References `std::__detail::__poly_radial_jacobi()`.

8.3.3.232 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sin_pi (_Tp __x) [inline]`

Return the reperiodized sine function $\sin_\pi(x)$ for real argument x .

The reperiodized sine function is defined by:

$$\sin_\pi(x) = \sin(\pi x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 5444 of file specfun.h.

8.3.3.233 `float __gnu_cxx::sin_pif (float __x) [inline]`

Return the reperiodized sine function $\sin_\pi(x)$ for float argument x .

See also

[sin_pi](#) for more details.

Definition at line 5417 of file specfun.h.

8.3.3.234 `long double __gnu_cxx::sin_pi (long double __x) [inline]`

Return the reperiodized sine function $\sin_{\pi}(x)$ for `long double` argument x .

See also

[sin_pi](#) for more details.

Definition at line 5427 of file `specfun.h`.

8.3.3.235 `template<typename _Tp> __gnu_cxx::_promote_fp_t<_Tp> __gnu_cxx::sinc (_Tp __x) [inline]`

Return the sinus cardinal function $\text{sinc}_{\pi}(x)$ for real argument `__x`. The sinus cardinal function is defined by:

$$\text{sinc}(x) = \frac{\sin(x)}{x}$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 1534 of file `specfun.h`.

8.3.3.236 `template<typename _Tp> __gnu_cxx::_promote_fp_t<_Tp> __gnu_cxx::sinc_pi (_Tp __x) [inline]`

Return the reperiodized sinus cardinal function $\text{sinc}(x)$ for real argument `__x`. The normalized sinus cardinal function is defined by:

$$\text{sinc}_{\pi}(x) = \frac{\sin(\pi x)}{\pi x}$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 1575 of file specfun.h.

8.3.3.237 `float __gnu_cxx::sinc_pif (float __x) [inline]`

Return the reperiodized sinus cardinal function $\text{sinc}(x)$ for `float` argument `__x`.

See also

[sinc](#) for details.

Definition at line 1549 of file specfun.h.

8.3.3.238 `long double __gnu_cxx::sinc_pil (long double __x) [inline]`

Return the reperiodized sinus cardinal function $\text{sinc}(x)$ for `long double` argument `__x`.

See also

[sinc](#) for details.

Definition at line 1559 of file specfun.h.

8.3.3.239 `float __gnu_cxx::sincf (float __x) [inline]`

Return the sinus cardinal function $\text{sinc}_\pi(x)$ for `float` argument `__x`.

See also

[sinc_pi](#) for details.

Definition at line 1508 of file specfun.h.

8.3.3.240 `long double __gnu_cxx::sincl (long double __x) [inline]`

Return the sinus cardinal function $\text{sinc}_\pi(x)$ for `long double` argument `__x`.

See also

[sinc_pi](#) for details.

Definition at line 1518 of file specfun.h.

8.3.3.241 `__gnu_cxx::__sincos_t<double> __gnu_cxx::sincos (double __x) [inline]`

Return both the sine and the cosine of a `double` argument.

See also

[sincos](#) for details.

Definition at line 5682 of file `specfun.h`.

8.3.3.242 `template<typename _Tp> __gnu_cxx::__sincos_t<_Tp> __gnu_cxx::sincos (_Tp __x) [inline]`

Return both the sine and the cosine of a reperiodized argument.

$$\text{sincos}(x) = \sin(x), \cos(x)$$

Definition at line 5693 of file `specfun.h`.

8.3.3.243 `template<typename _Tp> __gnu_cxx::__sincos_t<_Tp> __gnu_cxx::sincos_pi (_Tp __x) [inline]`

Return both the sine and the cosine of a reperiodized real argument.

$$\text{sincos}_\pi(x) = \sin(\pi x), \cos(\pi x)$$

Definition at line 5727 of file `specfun.h`.

8.3.3.244 `__gnu_cxx::__sincos_t<float> __gnu_cxx::sincos_pif (float __x) [inline]`

Return both the sine and the cosine of a reperiodized `float` argument.

See also

[sincos_pi](#) for details.

Definition at line 5705 of file `specfun.h`.

8.3.3.245 `__gnu_cxx::__sincos_t<long double> __gnu_cxx::sincos_pil (long double __x) [inline]`

Return both the sine and the cosine of a reperiodized `long double` argument.

See also

[sincos_pi](#) for details.

Definition at line 5715 of file `specfun.h`.

8.3.3.246 `__gnu_cxx::__sincos_t<float> __gnu_cxx::sincosf (float __x)` `[inline]`

Return both the sine and the cosine of a `float` argument.

Definition at line 5664 of file `specfun.h`.

8.3.3.247 `__gnu_cxx::__sincos_t<long double> __gnu_cxx::sincosl (long double __x)` `[inline]`

Return both the sine and the cosine of a `long double` argument.

See also

[sincos](#) for details.

Definition at line 5673 of file `specfun.h`.

8.3.3.248 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinh_pi (_Tp __x)` `[inline]`

Return the reperiodized hyperbolic sine function $\sinh_{\pi}(x)$ for real argument x .

The reperiodized hyperbolic sine function is defined by:

$$\sinh_{\pi}(x) = \sinh(\pi x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 5486 of file `specfun.h`.

8.3.3.249 `float __gnu_cxx::sinh_pif (float __x)` `[inline]`

Return the reperiodized hyperbolic sine function $\sinh_{\pi}(x)$ for `float` argument x .

See also

[sinh_pi](#) for more details.

Definition at line 5459 of file `specfun.h`.

8.3.3.250 `long double __gnu_cxx::sinh_pi (long double __x) [inline]`

Return the reperiodized hyperbolic sine function $\sinh_{\pi}(x)$ for `long double` argument x .

See also

[sinh_pi](#) for more details.

Definition at line 5469 of file `specfun.h`.

8.3.3.251 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhc (_Tp __x) [inline]`

Return the normalized hyperbolic sinus cardinal function $\operatorname{sinhc}(x)$ for real argument `__x`. The normalized hyperbolic sinus cardinal function is defined by:

$$\operatorname{sinhc}(x) = \frac{\sinh(\pi x)}{\pi x}$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 2417 of file `specfun.h`.

8.3.3.252 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhc_pi (_Tp __x) [inline]`

Return the hyperbolic sinus cardinal function $\operatorname{sinhc}_{\pi}(x)$ for real argument `__x`. The sinus cardinal function is defined by:

$$\operatorname{sinhc}_{\pi}(x) = \frac{\sinh(x)}{x}$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>__x</code>	The argument
------------------	--------------

Definition at line 2376 of file specfun.h.

8.3.3.253 `float __gnu_cxx::sinhc_pif (float __x) [inline]`

Return the hyperbolic sinus cardinal function $\operatorname{sinhc}_{\pi}(x)$ for `float` argument `__x`.

See also

[sinhc_pi](#) for details.

Definition at line 2350 of file specfun.h.

8.3.3.254 `long double __gnu_cxx::sinhc_pil (long double __x) [inline]`

Return the hyperbolic sinus cardinal function $\operatorname{sinhc}_{\pi}(x)$ for `long double` argument `__x`.

See also

[sinhc_pi](#) for details.

Definition at line 2360 of file specfun.h.

8.3.3.255 `float __gnu_cxx::sinhcf (float __x) [inline]`

Return the normalized hyperbolic sinus cardinal function $\operatorname{sinhc}(x)$ for `float` argument `__x`.

See also

[sinhc](#) for details.

Definition at line 2391 of file specfun.h.

8.3.3.256 `long double __gnu_cxx::sinhcl (long double __x) [inline]`

Return the normalized hyperbolic sinus cardinal function $\operatorname{sinhc}(x)$ for `long double` argument `__x`.

See also

[sinhc](#) for details.

Definition at line 2401 of file specfun.h.

8.3.3.257 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhint (_Tp __x) [inline]`

Return the hyperbolic sine integral $\operatorname{Shi}(x)$ of real argument x .

The hyperbolic sine integral is defined by

$$\operatorname{Shi}(x) = \int_0^x \frac{\sinh(t)}{t} dt$$

Template Parameters

<code>_Tp</code>	The type of the real argument
------------------	-------------------------------

Parameters

<code>↔</code> <code>_x</code>	The argument
-----------------------------------	--------------

Definition at line 1733 of file `specfun.h`.

8.3.3.258 `float __gnu_cxx::sinhintf (float __x) [inline]`

Return the hyperbolic sine integral of `float` argument x .

See also

[sinhint](#) for details.

Definition at line 1706 of file `specfun.h`.

8.3.3.259 `long double __gnu_cxx::sinhintl (long double __x) [inline]`

Return the hyperbolic sine integral $Shi(x)$ of `long double` argument x .

See also

[sinhint](#) for details.

Definition at line 1716 of file `specfun.h`.

8.3.3.260 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinint (_Tp __x) [inline]`

Return the sine integral $Si(x)$ of real argument x .

The sine integral is defined by

$$Si(x) = \int_0^x \frac{\sin(t)}{t} dt$$

Parameters

<code>↔</code> <code>_x</code>	The real upper integration limit
-----------------------------------	----------------------------------

Definition at line 1652 of file specfun.h.

8.3.3.261 `float __gnu_cxx::sinintf (float __x) [inline]`

Return the sine integral $Si(x)$ of `float` argument x .

See also

[sinint](#) for details.

Definition at line 1627 of file specfun.h.

8.3.3.262 `long double __gnu_cxx::sinintl (long double __x) [inline]`

Return the sine integral $Si(x)$ of `long double` argument x .

See also

[sinint](#) for details.

Definition at line 1637 of file specfun.h.

8.3.3.263 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sph_bessel_i (unsigned int __n, _Tp __x) [inline]`

Return the regular modified spherical Bessel function $i_n(x)$ of nonnegative order n and real argument $x \geq 0$.

The spherical Bessel function is defined by:

$$i_n(x) = \left(\frac{\pi}{2x}\right)^{1/2} I_{n+1/2}(x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

<code>↔ _n</code>	The integral order $n \geq 0$
<code>↔ _x</code>	The real argument $x \geq 0$

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 2645 of file `specfun.h`.

8.3.3.264 `float __gnu_cxx::sph_bessel_if (unsigned int __n, float __x) [inline]`

Return the regular modified spherical Bessel function $i_n(x)$ of nonnegative order `n` and `float` argument $x \geq 0$.

See also

[sph_bessel_i](#) for details.

Definition at line 2616 of file `specfun.h`.

8.3.3.265 `long double __gnu_cxx::sph_bessel_il (unsigned int __n, long double __x) [inline]`

Return the regular modified spherical Bessel function $i_n(x)$ of nonnegative order `n` and `long double` argument $x \geq 0$.

See also

[sph_bessel_i](#) for details.

Definition at line 2626 of file `specfun.h`.

8.3.3.266 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sph_bessel_k (unsigned int __n, _Tp __x) [inline]`

Return the irregular modified spherical Bessel function $k_n(x)$ of nonnegative order `n` and real argument $x \geq 0$.

The spherical Bessel function is defined by:

$$k_n(x) = \left(\frac{\pi}{2x}\right)^{1/2} K_{n+1/2}(x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

\leftrightarrow __n	The integral order $n \geq 0$
\leftrightarrow __x	The real argument $x \geq 0$

Exceptions

<code>std::domain_error</code>	if <code>__x < 0</code> .
--------------------------------	------------------------------

Definition at line 2689 of file `specfun.h`.

8.3.3.267 `float __gnu_cxx::sph_bessel_kf(unsigned int __n, float __x) [inline]`

Return the irregular modified spherical Bessel function $k_n(x)$ of nonnegative order n and `float` argument $x \geq 0$.

See also

[sph_bessel_k](#) for more details.

Definition at line 2660 of file `specfun.h`.

8.3.3.268 `long double __gnu_cxx::sph_bessel_kl(unsigned int __n, long double __x) [inline]`

Return the irregular modified spherical Bessel function $k_n(x)$ of nonnegative order n and `long double` argument $x \geq 0$.

See also

[sph_bessel_k](#) for more details.

Definition at line 2670 of file `specfun.h`.

8.3.3.269 `template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::sph_hankel_1(unsigned int __n, _Tp __z) [inline]`

Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$ of nonnegative order n and real argument $x \geq 0$.

The spherical Hankel function of the first kind is defined by:

$$h_n^{(1)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} H_{n+1/2}^{(1)}(x)$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>_↔ _n</code>	The non-negative order
<code>_↔ _z</code>	The real argument

Definition at line 2558 of file `specfun.h`.

```
8.3.3.270  template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::sph_hankel_1 ( unsigned
            int __n, std::complex<_Tp> __x )  [inline]
```

Return the complex spherical Hankel function of the first kind $h_n^{(1)}(x)$ of non-negative integral n and complex argument x .

The spherical Hankel function of the first kind is defined by

$$h_n^{(1)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} H_{n+1/2}^{(1)}(x) = j_n(x) + in_n(x)$$

where $j_n(x)$ and $n_n(x)$ are the spherical Bessel and Neumann functions respectively.

Parameters

<code>_↔ _n</code>	The integral order ≥ 0
<code>_↔ _x</code>	The complex argument

Definition at line 4460 of file `specfun.h`.

```
8.3.3.271  std::complex<float> __gnu_cxx::sph_hankel_1f ( unsigned int __n, float __z )  [inline]
```

Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$ of nonnegative order n and `float` argument $x \geq 0$.

See also

[sph_hankel_1](#) for details.

Definition at line 2530 of file `specfun.h`.

8.3.3.272 `std::complex<float> __gnu_cxx::sph_hankel_1f(unsigned int __n, std::complex< float > __x) [inline]`

Return the complex spherical Hankel function of the first kind $h_n^{(1)}(x)$ of non-negative integral n and `std::complex<float>` argument x .

See also

[sph_hankel_1](#) for more details.

Definition at line 4428 of file `specfun.h`.

8.3.3.273 `std::complex<long double> __gnu_cxx::sph_hankel_1l(unsigned int __n, long double __z) [inline]`

Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$ of nonnegative order n and `long double` argument $x \geq 0$.

See also

[sph_hankel_1](#) for details.

Definition at line 2540 of file `specfun.h`.

8.3.3.274 `std::complex<long double> __gnu_cxx::sph_hankel_1l(unsigned int __n, std::complex< long double > __x) [inline]`

Return the complex spherical Hankel function of the first kind $h_n^{(1)}(x)$ of non-negative integral n and `std::complex<long double>` argument x .

See also

[sph_hankel_1](#) for more details.

Definition at line 4439 of file `specfun.h`.

8.3.3.275 `template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::sph_hankel_2(unsigned int __n, _Tp __z) [inline]`

Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$ of nonnegative order n and real argument $x \geq 0$.

The spherical Hankel function of the second kind is defined by:

$$h_n^{(2)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} H_{n+1/2}^{(2)}(x)$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>_↔ _n</code>	The non-negative order
<code>_↔ _z</code>	The real argument

Definition at line 2601 of file `specfun.h`.

```
8.3.3.276  template<typename _Tp> std::complex<__gnu_cxx::__promote_fp_t<_Tp>> __gnu_cxx::sph_hankel_2 ( unsigned
            int __n, std::complex<_Tp> __x )  [inline]
```

Return the complex spherical Hankel function of the second kind $h_n^{(2)}(x)$ of nonnegative order n and complex argument x .

The spherical Hankel function of the second kind is defined by

$$h_n^{(2)}(x) = \left(\frac{\pi}{2x}\right)^{1/2} H_{n+1/2}^{(2)}(x) = j_n(x) - in_n(x)$$

where $j_n(x)$ and $n_n(x)$ are the spherical Bessel and Neumann functions respectively.

Parameters

<code>_↔ _n</code>	The integral order ≥ 0
<code>_↔ _x</code>	The complex argument

Definition at line 4508 of file `specfun.h`.

```
8.3.3.277  std::complex<float> __gnu_cxx::sph_hankel_2f ( unsigned int __n, float __z )  [inline]
```

Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$ of nonnegative order n and `float` argument $x \geq 0$.

See also

[sph_hankel_2](#) for details.

Definition at line 2573 of file `specfun.h`.

8.3.3.278 `std::complex<float> __gnu_cxx::sph_hankel_2f (unsigned int __n, std::complex< float > __x) [inline]`

Return the complex spherical Hankel function of the second kind $h_n^{(2)}(x)$ of non-negative integral n and `std::complex<float>` argument x .

See also

[sph_hankel_2](#) for more details.

Definition at line 4476 of file `specfun.h`.

8.3.3.279 `std::complex<long double> __gnu_cxx::sph_hankel_2l (unsigned int __n, long double __z) [inline]`

Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$ of nonnegative order n and `long double` argument $x \geq 0$.

See also

[sph_hankel_2](#) for details.

Definition at line 2583 of file `specfun.h`.

8.3.3.280 `std::complex<long double> __gnu_cxx::sph_hankel_2l (unsigned int __n, std::complex< long double > __x) [inline]`

Return the complex spherical Hankel function of the second kind $h_n^{(2)}(x)$ of non-negative integral n and `std::complex<long double>` argument x .

See also

[sph_hankel_2](#) for more details.

Definition at line 4487 of file `specfun.h`.

8.3.3.281 `template<typename _Ttheta , typename _Tphi > std::complex<__gnu_cxx::__promote_fp_t<_Ttheta, _Tphi> > __gnu_cxx::sph_harmonic (unsigned int __l, int __m, _Ttheta __theta, _Tphi __phi) [inline]`

Return the complex spherical harmonic function of degree l , order m , and real zenith angle θ , and azimuth angle ϕ .

The spherical harmonic function is defined by:

$$Y_l^m(\theta, \phi) = (-1)^m \left[\frac{(2l+1)}{4\pi} \frac{(l-m)!}{(l+m)!} \right] P_l^{|m|}(\cos \theta) \exp^{im\phi}$$

Parameters

<code>__l</code>	The order
<code>__m</code>	The degree
<code>__theta</code>	The zenith angle in radians
<code>__phi</code>	The azimuth angle in radians

Definition at line 4559 of file `specfun.h`.

8.3.3.282 `std::complex<float> __gnu_cxx::sph_harmonic(unsigned int __l, int __m, float __theta, float __phi)` `[inline]`

Return the complex spherical harmonic function of degree l , order m , and `float` zenith angle θ , and azimuth angle ϕ .

See also

[sph_harmonic](#) for details.

Definition at line 4523 of file `specfun.h`.

8.3.3.283 `std::complex<long double> __gnu_cxx::sph_harmonic(unsigned int __l, int __m, long double __theta, long double __phi)` `[inline]`

Return the complex spherical harmonic function of degree l , order m , and `long double` zenith angle θ , and azimuth angle ϕ .

See also

[sph_harmonic](#) for details.

Definition at line 4535 of file `specfun.h`.

8.3.3.284 `template<typename _Tp> __gnu_cxx::promote_fp_t<_Tp> __gnu_cxx::tan_pi(_Tp __x)` `[inline]`

Return the reperiodized tangent function $\tan_{\pi}(x)$ for real argument x .

The reperiodized tangent function is defined by:

$$\tan_{\pi}(x) = \tan(\pi x)$$

Template Parameters

<code>_Tp</code>	The floating-point type of the argument <code>__x</code> .
------------------	--

Parameters

\leftrightarrow	The argument
x	

Definition at line 5612 of file specfun.h.

8.3.3.285 `float __gnu_cxx::tan_pif (float x)` `[inline]`

Return the reperiodized tangent function $\tan_{\pi}(x)$ for `float` argument x .

See also

[tan_pi](#) for more details.

Definition at line 5585 of file specfun.h.

8.3.3.286 `long double __gnu_cxx::tan_pil (long double x)` `[inline]`

Return the reperiodized tangent function $\tan_{\pi}(x)$ for `long double` argument x .

See also

[tan_pi](#) for more details.

Definition at line 5595 of file specfun.h.

8.3.3.287 `template<typename Tp > __gnu_cxx::__promote_fp_t< Tp > __gnu_cxx::tanh_pi (Tp x)` `[inline]`

Return the reperiodized hyperbolic tangent function $\tanh_{\pi}(x)$ for real argument x .

The reperiodized hyperbolic tangent function is defined by:

$$\tanh_{\pi}(x) = \tanh(\pi x)$$

Template Parameters

Tp	The floating-point type of the argument x .
------	---

Parameters

\leftrightarrow	The argument
x	

Definition at line 5654 of file specfun.h.

8.3.3.288 `float __gnu_cxx::tanh_pif (float __x) [inline]`

Return the reperiodized hyperbolic tangent function $\tanh_{\pi}(x)$ for `float` argument x .

See also

[tanh_pi](#) for more details.

Definition at line 5627 of file specfun.h.

8.3.3.289 `long double __gnu_cxx::tanh_pil (long double __x) [inline]`

Return the reperiodized hyperbolic tangent function $\tanh_{\pi}(x)$ for `long double` argument x .

See also

[tanh_pi](#) for more details.

Definition at line 5637 of file specfun.h.

8.3.3.290 `template<typename _Ta> std::complex<__gnu_cxx::__promote_fp_t<_Ta>> __gnu_cxx::tgamma (std::complex<_Ta> __a) [inline]`

Return the gamma function for complex argument.

Definition at line 2878 of file specfun.h.

8.3.3.291 `template<typename _Ta, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tp> __gnu_cxx::tgamma (_Ta __a, _Tp __x) [inline]`

Return the upper incomplete gamma function $\Gamma(a, x)$. The (upper) incomplete gamma function is defined by

$$\Gamma(a, x) = \int_x^{\infty} t^{a-1} e^{-t} dt$$

Definition at line 2915 of file specfun.h.

8.3.3.292 `template<typename _Ta, typename _Tp> __gnu_cxx::__promote_fp_t<_Ta, _Tp> __gnu_cxx::tgamma_lower (_Ta __a, _Tp __x) [inline]`

Return the lower incomplete gamma function $\gamma(a, x)$. The lower incomplete gamma function is defined by

$$\gamma(a, x) = \int_0^x t^{a-1} e^{-t} dt$$

Definition at line 2952 of file `specfun.h`.

8.3.3.293 `float __gnu_cxx::tgamma_lowerf (float __a, float __x) [inline]`

Return the lower incomplete gamma function $\gamma(a, x)$ for `float` argument.

See also

[tgamma_lower](#) for details.

Definition at line 2930 of file `specfun.h`.

8.3.3.294 `long double __gnu_cxx::tgamma_lowerl (long double __a, long double __x) [inline]`

Return the lower incomplete gamma function $\gamma(a, x)$ for `long double` argument.

See also

[tgamma_lower](#) for details.

Definition at line 2940 of file `specfun.h`.

8.3.3.295 `std::complex<float> __gnu_cxx::tgammaf (std::complex<float> __a) [inline]`

Return the gamma function for `std::complex<float>` argument.

See also

[lgamma](#) for details.

Definition at line 2860 of file `specfun.h`.

8.3.3.296 `float __gnu_cxx::tgammaf (float __a, float __x) [inline]`

Return the upper incomplete gamma function $\Gamma(a, x)$ for `float` argument.

See also

[tgamma](#) for details.

Definition at line 2893 of file `specfun.h`.

8.3.3.297 `std::complex<long double> __gnu_cxx::tgamma (std::complex< long double > __a) [inline]`

Return the gamma function for `std::complex<long double>` argument.

See also

[lgamma](#) for details.

Definition at line 2870 of file `specfun.h`.

8.3.3.298 `long double __gnu_cxx::tgamma (long double __a, long double __x) [inline]`

Return the upper incomplete gamma function $\Gamma(a, x)$ for `long double` argument.

See also

[tgamma](#) for details.

Definition at line 2903 of file `specfun.h`.

8.3.3.299 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> __gnu_cxx::theta_1 (_Tpnu __nu, _Tp __x) [inline]`

Return the exponential theta-1 function $\theta_1(\nu, x)$ of period nu and argument x .

The Neville theta-1 function is defined by

$$\theta_1(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} (-1)^j \exp\left(\frac{-(\nu + j - 1/2)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 2) argument
<code>__x</code>	The argument

Definition at line 4984 of file specfun.h.

8.3.3.300 `float __gnu_cxx::theta_1f(float __nu, float __x) [inline]`

Return the exponential theta-1 function $\theta_1(\nu, x)$ of period nu and argument x .

See also

[theta_1](#) for details.

Definition at line 4956 of file specfun.h.

8.3.3.301 `long double __gnu_cxx::theta_1l(long double __nu, long double __x) [inline]`

Return the exponential theta-1 function $\theta_1(\nu, x)$ of period nu and argument x .

See also

[theta_1](#) for details.

Definition at line 4966 of file specfun.h.

8.3.3.302 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> __gnu_cxx::theta_2(_Tpnu __nu, _Tp __x) [inline]`

Return the exponential theta-2 function $\theta_2(\nu, x)$ of period nu and argument x .

The exponential theta-2 function is defined by

$$\theta_2(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} (-1)^j \exp\left(\frac{-(\nu + j)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 2) argument
<code>__x</code>	The argument

Definition at line 5027 of file specfun.h.

8.3.3.303 `float __gnu_cxx::theta_2f(float __nu, float __x) [inline]`

Return the exponential theta-2 function $\theta_2(\nu, x)$ of period nu and argument x .

See also

[theta_2](#) for details.

Definition at line 4999 of file specfun.h.

```
8.3.3.304 long double __gnu_cxx::theta_2l( long double __nu, long double __x ) [inline]
```

Return the exponential theta-2 function $\theta_2(\nu, x)$ of period nu and argument x .

See also

[theta_2](#) for details.

Definition at line 5009 of file specfun.h.

```
8.3.3.305 template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> __gnu_cxx::theta_3( _Tpnu
__nu, _Tp __x ) [inline]
```

Return the exponential theta-3 function $\theta_3(\nu, x)$ of period nu and argument x .

The exponential theta-3 function is defined by

$$\theta_3(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} \exp\left(\frac{-(\nu + j)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 1) argument
<code>__x</code>	The argument

Definition at line 5070 of file specfun.h.

```
8.3.3.306 float __gnu_cxx::theta_3f( float __nu, float __x ) [inline]
```

Return the exponential theta-3 function $\theta_3(\nu, x)$ of period nu and argument x .

See also

[theta_3](#) for details.

Definition at line 5042 of file specfun.h.

8.3.3.307 `long double __gnu_cxx::theta_3l (long double __nu, long double __x)` `[inline]`

Return the exponential theta-3 function $\theta_3(\nu, x)$ of period nu and argument x .

See also

[theta_3](#) for details.

Definition at line 5052 of file specfun.h.

8.3.3.308 `template<typename _Tpnu, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpnu, _Tp> __gnu_cxx::theta_4 (_Tpnu __nu, _Tp __x)` `[inline]`

Return the exponential theta-4 function $\theta_4(\nu, x)$ of period nu and argument x .

The exponential theta-4 function is defined by

$$\theta_4(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} \exp\left(\frac{-(\nu + j + 1/2)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 1) argument
<code>__x</code>	The argument

Definition at line 5113 of file specfun.h.

8.3.3.309 `float __gnu_cxx::theta_4f (float __nu, float __x)` `[inline]`

Return the exponential theta-4 function $\theta_4(\nu, x)$ of period nu and argument x .

See also

[theta_4](#) for details.

Definition at line 5085 of file specfun.h.

8.3.3.310 `long double __gnu_cxx::theta_4l (long double __nu, long double __x)` `[inline]`

Return the exponential theta-4 function $\theta_4(\nu, x)$ of period nu and argument x .

See also

[theta_4](#) for details.

Definition at line 5095 of file specfun.h.

8.3.3.311 `template<typename _Tpk, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpk, _Tp> __gnu_cxx::theta_c (_Tpk __k, _Tp __x) [inline]`

Return the Neville theta-c function $\theta_c(k, x)$ of modulus k and argument x .

The Neville theta-c function is defined by

Parameters

\leftrightarrow __k	The modulus $-1 \leq k \leq +1$
\leftrightarrow __x	The argument

Definition at line 5239 of file specfun.h.

8.3.3.312 `float __gnu_cxx::theta_cf (float __k, float __x) [inline]`

Return the Neville theta-c function $\theta_c(k, x)$ of modulus k and argument x .

See also

[theta_c](#) for details.

Definition at line 5212 of file specfun.h.

8.3.3.313 `long double __gnu_cxx::theta_cl (long double __k, long double __x) [inline]`

Return the Neville theta-c function $\theta_c(k, x)$ of long double modulus k and argument x .

See also

[theta_c](#) for details.

Definition at line 5222 of file specfun.h.

8.3.3.314 `template<typename _Tpk, typename _Tp> __gnu_cxx::__promote_fp_t<_Tpk, _Tp> __gnu_cxx::theta_d (_Tpk __k, _Tp __x) [inline]`

Return the Neville theta-d function $\theta_d(k, x)$ of modulus k and argument x .

The Neville theta-d function is defined by

$$\theta_d(k, x) =$$

Parameters

\leftrightarrow __k	The modulus $-1 \leq k \leq +1$
\leftrightarrow __x	The argument

Definition at line 5281 of file specfun.h.

8.3.3.315 `float __gnu_cxx::theta_df (float __k, float __x) [inline]`

Return the Neville theta-d function $\theta_d(k, x)$ of modulus k and argument x .

See also

[theta_d](#) for details.

Definition at line 5254 of file specfun.h.

8.3.3.316 `long double __gnu_cxx::theta_dl (long double __k, long double __x) [inline]`

Return the Neville theta-d function $\theta_d(k, x)$ of long double modulus k and argument x .

See also

[theta_d](#) for details.

Definition at line 5264 of file specfun.h.

8.3.3.317 `template<typename _Tp, typename _Tp> __gnu_cxx::__promote_fp_t<_Tp, _Tp> __gnu_cxx::theta_n (_Tp __k, _Tp __x) [inline]`

Return the Neville theta-n function $\theta_n(k, x)$ of modulus k and argument x .

The Neville theta-n function is defined by

$$\theta_n(k, x) =$$

Parameters

\leftrightarrow __k	The modulus $-1 \leq k \leq +1$
\leftrightarrow __x	The argument

Definition at line 5323 of file specfun.h.

8.3.3.318 `float __gnu_cxx::theta_nf (float __k, float __x) [inline]`

Return the Neville theta-n function $\theta_n(k, x)$ of modulus k and argument x .

See also

[theta_n](#) for details.

Definition at line 5296 of file specfun.h.

8.3.3.319 `long double __gnu_cxx::theta_nl (long double __k, long double __x) [inline]`

Return the Neville theta-n function $\theta_n(k, x)$ of `long double` modulus k and argument x .

See also

[theta_n](#) for details.

Definition at line 5306 of file specfun.h.

8.3.3.320 `template<typename _Tp, typename _Tp> __gnu_cxx::__promote_fp_t<_Tp, _Tp> __gnu_cxx::theta_s (_Tp __k, _Tp __x) [inline]`

Return the Neville theta-s function $\theta_s(k, x)$ of modulus k and argument x .

The Neville theta-s function is defined by

Parameters

\leftrightarrow __k	The modulus $-1 \leq k \leq +1$
\leftrightarrow __x	The argument

Definition at line 5197 of file specfun.h.

8.3.3.321 `float __gnu_cxx::theta_sf (float __k, float __x) [inline]`

Return the Neville theta-s function $\theta_s(k, x)$ of modulus k and argument x .

See also

[theta_s](#) for details.

Definition at line 5170 of file specfun.h.

8.3.3.322 `long double __gnu_cxx::theta_sl (long double __k, long double __x) [inline]`

Return the Neville theta-s function $\theta_s(k, x)$ of `long double` modulus k and argument x .

See also

[theta_s](#) for details.

Definition at line 5180 of file specfun.h.

8.3.3.323 `template<typename _Trho, typename _Tphi> __gnu_cxx::__promote_fp_t<_Trho, _Tphi> __gnu_cxx::zernike (unsigned int __n, int __m, _Trho __rho, _Tphi __phi) [inline]`

Return the Zernicke polynomial $Z_n^m(\rho, \phi)$ for non-negative degree n , signed order m , and real radial argument ρ and azimuthal angle ϕ .

The even Zernicke polynomials are defined by:

$$Z_n^m(\rho, \phi) = R_n^m(\rho) \cos(m\phi)$$

and the odd Zernicke polynomials are defined by:

$$Z_n^{-m}(\rho, \phi) = R_n^m(\rho) \sin(m\phi)$$

for non-negative degree m and $m \leq n$ and where $R_n^m(\rho)$ is the radial polynomial (

See also

[radpoly](#)).

Template Parameters

<code>_Trho</code>	The real type of the radial coordinate
<code>_Tphi</code>	The real type of the azimuthal angle

Parameters

<code>__n</code>	The non-negative degree.
<code>__m</code>	The (signed) azimuthal order
<code>__rho</code>	The radial coordinate
<code>__phi</code>	The azimuthal angle

Definition at line 2280 of file specfun.h.

8.3.3.324 `float __gnu_cxx::zernikef (unsigned int __n, int __m, float __rho, float __phi) [inline]`

Return the Zernicke polynomial $Z_n^m(\rho, \phi)$ for non-negative degree n , signed order m , and real radial argument ρ and azimuthal angle ϕ .

See also

[zernike](#) for details.

Definition at line 2241 of file specfun.h.

8.3.3.325 `long double __gnu_cxx::zernikel (unsigned int __n, int __m, long double __rho, long double __phi) [inline]`

Return the Zernicke polynomial $Z_n^m(\rho, \phi)$ for non-negative degree n , signed order m , and real radial argument ρ and azimuthal angle ϕ .

See also

[zernike](#) for details.

Definition at line 2252 of file specfun.h.

Chapter 9

Namespace Documentation

9.1 `__gnu_cxx` Namespace Reference

Classes

- struct [__sincos_t](#)

Enumerations

- enum { [_GLIBCXX_JACOBI_SN](#), [_GLIBCXX_JACOBI_CN](#), [_GLIBCXX_JACOBI_DN](#) }

Functions

- template<typename `_Tp` >
 `__gnu_cxx::__promote_fp_t<_Tp>` [airy_ai](#) (`_Tp __x`)
- template<typename `_Tp` >
 `std::complex<__gnu_cxx::__promote_fp_t<_Tp>>` [airy_ai](#) (`std::complex<_Tp> __x`)
- float [airy_aif](#) (float `__x`)
- long double [airy_ail](#) (long double `__x`)
- template<typename `_Tp` >
 `__gnu_cxx::__promote_fp_t<_Tp>` [airy_bi](#) (`_Tp __x`)
- template<typename `_Tp` >
 `std::complex<__gnu_cxx::__promote_fp_t<_Tp>>` [airy_bi](#) (`std::complex<_Tp> __x`)
- float [airy_bif](#) (float `__x`)
- long double [airy_bil](#) (long double `__x`)
- template<typename `_Tp` >
 `__gnu_cxx::__promote_fp_t<_Tp>` [bernoulli](#) (unsigned int `__n`)
- float [bernoullif](#) (unsigned int `__n`)
- long double [bernoullil](#) (unsigned int `__n`)
- template<typename `_Tp` >
 `__gnu_cxx::__promote_fp_t<_Tp>` [bincoef](#) (unsigned int `__n`, unsigned int `__k`)
- float [bincoeff](#) (unsigned int `__n`, unsigned int `__k`)

- long double [bincoefl](#) (unsigned int __n, unsigned int __k)
- template<typename _Tps, typename _Tp >
__gnu_cxx::__promote_fp_t< _Tps, _Tp > [bose_einstein](#) (_Tps __s, _Tp __x)
- float [bose_einsteinf](#) (float __s, float __x)
- long double [bose_einsteinl](#) (long double __s, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [chebyshev_t](#) (unsigned int __n, _Tp __x)
- float [chebyshev_tf](#) (unsigned int __n, float __x)
- long double [chebyshev_tl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [chebyshev_u](#) (unsigned int __n, _Tp __x)
- float [chebyshev_uf](#) (unsigned int __n, float __x)
- long double [chebyshev_ul](#) (unsigned int __n, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [chebyshev_v](#) (unsigned int __n, _Tp __x)
- float [chebyshev_vf](#) (unsigned int __n, float __x)
- long double [chebyshev_vl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [chebyshev_w](#) (unsigned int __n, _Tp __x)
- float [chebyshev_wf](#) (unsigned int __n, float __x)
- long double [chebyshev_wl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [clausen](#) (unsigned int __m, _Tp __w)
- template<typename _Tp >
std::complex< __gnu_cxx::__promote_fp_t< _Tp > > [clausen](#) (unsigned int __m, std::complex< _Tp > __w)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [clausen_c](#) (unsigned int __m, _Tp __w)
- float [clausen_cf](#) (unsigned int __m, float __w)
- long double [clausen_cl](#) (unsigned int __m, long double __w)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [clausen_s](#) (unsigned int __m, _Tp __w)
- float [clausen_sf](#) (unsigned int __m, float __w)
- long double [clausen_sl](#) (unsigned int __m, long double __w)
- float [clausenf](#) (unsigned int __m, float __w)
- std::complex< float > [clausenf](#) (unsigned int __m, std::complex< float > __w)
- long double [clausenl](#) (unsigned int __m, long double __w)
- std::complex< long double > [clausenl](#) (unsigned int __m, std::complex< long double > __w)
- template<typename _Tk >
__gnu_cxx::__promote_fp_t< _Tk > [comp_ellint_d](#) (_Tk __k)
- float [comp_ellint_df](#) (float __k)
- long double [comp_ellint_dl](#) (long double __k)
- float [comp_ellint_rf](#) (float __x, float __y)
- long double [comp_ellint_rf](#) (long double __x, long double __y)
- template<typename _Tx, typename _Ty >
__gnu_cxx::__promote_fp_t< _Tx, _Ty > [comp_ellint_rf](#) (_Tx __x, _Ty __y)
- float [comp_ellint_rg](#) (float __x, float __y)
- long double [comp_ellint_rg](#) (long double __x, long double __y)
- template<typename _Tx, typename _Ty >
__gnu_cxx::__promote_fp_t< _Tx, _Ty > [comp_ellint_rg](#) (_Tx __x, _Ty __y)
- template<typename _Tpa, typename _Tpc, typename _Tp >
__gnu_cxx::__promote_fp_t< _Tpa, _Tpc, _Tp > [conf_hyperg](#) (_Tpa __a, _Tpc __c, _Tp __x)

- `template<typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_2< _Tpc, _Tp >::__type conf_hyperg_lim (_Tpc __c, _Tp __x)`
- `float conf_hyperg_limf (float __c, float __x)`
- `long double conf_hyperg_liml (long double __c, long double __x)`
- `float conf_hypergf (float __a, float __c, float __x)`
- `long double conf_hypergl (long double __a, long double __c, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > cos_pi (_Tp __x)`
- `float cos_pif (float __x)`
- `long double cos_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > cosh_pi (_Tp __x)`
- `float cosh_pif (float __x)`
- `long double cosh_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > coshint (_Tp __x)`
- `float coshintf (float __x)`
- `long double coshintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > cosint (_Tp __x)`
- `float cosintf (float __x)`
- `long double cosintl (long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > cyl_hankel_1 (_Tpnu __nu, _Tp __z)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > cyl_hankel_1 (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)`
- `std::complex< float > cyl_hankel_1f (float __nu, float __z)`
- `std::complex< float > cyl_hankel_1f (std::complex< float > __nu, std::complex< float > __x)`
- `std::complex< long double > cyl_hankel_1l (long double __nu, long double __z)`
- `std::complex< long double > cyl_hankel_1l (std::complex< long double > __nu, std::complex< long double > __x)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > cyl_hankel_2 (_Tpnu __nu, _Tp __z)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > cyl_hankel_2 (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)`
- `std::complex< float > cyl_hankel_2f (float __nu, float __z)`
- `std::complex< float > cyl_hankel_2f (std::complex< float > __nu, std::complex< float > __x)`
- `std::complex< long double > cyl_hankel_2l (long double __nu, long double __z)`
- `std::complex< long double > cyl_hankel_2l (std::complex< long double > __nu, std::complex< long double > __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > dawson (_Tp __x)`
- `float dawsonf (float __x)`
- `long double dawsonl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > dilog (_Tp __x)`
- `float dilogf (float __x)`
- `long double dilogl (long double __x)`
- `template<typename _Tp >`
`_Tp dirichlet_beta (_Tp __s)`

- float [dirichlet_betal](#) (float __s)
- long double [dirichlet_betal](#) (long double __s)
- template<typename _Tp >
 _Tp [dirichlet_eta](#) (_Tp __s)
- float [dirichlet_etaf](#) (float __s)
- long double [dirichlet_etaf](#) (long double __s)
- template<typename _Tp >
 _Tp [dirichlet_lambda](#) (_Tp __s)
- float [dirichlet_lambdaf](#) (float __s)
- long double [dirichlet_lambdaf](#) (long double __s)
- template<typename _Tp >
 __gnu_cxx::__promote_fp_t<_Tp > [double_factorial](#) (int __n)
- float [double_factorialf](#) (int __n)
- long double [double_factorialf](#) (int __n)
- template<typename _Tk, typename _Tp, typename _Ta, typename _Tb >
 __gnu_cxx::__promote_fp_t<_Tk, _Tp, _Ta, _Tb > [ellint_cel](#) (_Tk __k_c, _Tp __p, _Ta __a, _Tb __b)
- float [ellint_celf](#) (float __k_c, float __p, float __a, float __b)
- long double [ellint_celf](#) (long double __k_c, long double __p, long double __a, long double __b)
- template<typename _Tk, typename _Tphi >
 __gnu_cxx::__promote_fp_t<_Tk, _Tphi > [ellint_d](#) (_Tk __k, _Tphi __phi)
- float [ellint_df](#) (float __k, float __phi)
- long double [ellint_df](#) (long double __k, long double __phi)
- template<typename _Tp, typename _Tk >
 __gnu_cxx::__promote_fp_t<_Tp, _Tk > [ellint_el1](#) (_Tp __x, _Tk __k_c)
- float [ellint_el1f](#) (float __x, float __k_c)
- long double [ellint_el1f](#) (long double __x, long double __k_c)
- template<typename _Tp, typename _Tk, typename _Ta, typename _Tb >
 __gnu_cxx::__promote_fp_t<_Tp, _Tk, _Ta, _Tb > [ellint_el2](#) (_Tp __x, _Tk __k_c, _Ta __a, _Tb __b)
- float [ellint_el2f](#) (float __x, float __k_c, float __a, float __b)
- long double [ellint_el2f](#) (long double __x, long double __k_c, long double __a, long double __b)
- template<typename _Tx, typename _Tk, typename _Tp >
 __gnu_cxx::__promote_fp_t<_Tx, _Tk, _Tp > [ellint_el3](#) (_Tx __x, _Tk __k_c, _Tp __p)
- float [ellint_el3f](#) (float __x, float __k_c, float __p)
- long double [ellint_el3f](#) (long double __x, long double __k_c, long double __p)
- template<typename _Tp, typename _Up >
 __gnu_cxx::__promote_fp_t<_Tp, _Up > [ellint_rc](#) (_Tp __x, _Up __y)
- float [ellint_rcf](#) (float __x, float __y)
- long double [ellint_rcf](#) (long double __x, long double __y)
- template<typename _Tp, typename _Up, typename _Vp >
 __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp > [ellint_rd](#) (_Tp __x, _Up __y, _Vp __z)
- float [ellint_rdf](#) (float __x, float __y, float __z)
- long double [ellint_rdf](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp >
 __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp > [ellint_rf](#) (_Tp __x, _Up __y, _Vp __z)
- float [ellint_rff](#) (float __x, float __y, float __z)
- long double [ellint_rff](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp >
 __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp > [ellint_rg](#) (_Tp __x, _Up __y, _Vp __z)
- float [ellint_rgf](#) (float __x, float __y, float __z)
- long double [ellint_rgf](#) (long double __x, long double __y, long double __z)
- template<typename _Tp, typename _Up, typename _Vp, typename _Wp >
 __gnu_cxx::__promote_fp_t<_Tp, _Up, _Vp, _Wp > [ellint_rj](#) (_Tp __x, _Up __y, _Vp __z, _Wp __p)

- float [ellint_rjf](#) (float __x, float __y, float __z, float __p)
- long double [ellint_rjl](#) (long double __x, long double __y, long double __z, long double __p)
- template<typename _Tp >
 [_Tp ellnome](#) (_Tp __k)
- float [ellnomef](#) (float __k)
- long double [ellnomel](#) (long double __k)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp > expint](#) (unsigned int __n, _Tp __x)
- float [expintf](#) (unsigned int __n, float __x)
- long double [expintl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp > factorial](#) (unsigned int __n)
- float [factorialf](#) (unsigned int __n)
- long double [factoriall](#) (unsigned int __n)
- template<typename _Tps, typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tps, _Tp > fermi_dirac](#) (_Tps __s, _Tp __x)
- float [fermi_diracf](#) (float __s, float __x)
- long double [fermi_diracl](#) (long double __s, long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp > fresnel_c](#) (_Tp __x)
- float [fresnel_cf](#) (float __x)
- long double [fresnel_cl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp > fresnel_s](#) (_Tp __x)
- float [fresnel_sf](#) (float __x)
- long double [fresnel_sl](#) (long double __x)
- template<typename _Talpha, typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Talpha, _Tp > gegenbauer](#) (unsigned int __n, _Talpha __alpha, _Tp __x)
- float [gegenbauerf](#) (unsigned int __n, float __alpha, float __x)
- long double [gegenbauerl](#) (unsigned int __n, long double __alpha, long double __x)
- template<typename _Tk, typename _Tphi >
 [__gnu_cxx::__promote_fp_t<_Tk, _Tphi > heuman_lambda](#) (_Tk __k, _Tphi __phi)
- float [heuman_lambdaf](#) (float __k, float __phi)
- long double [heuman_lambdal](#) (long double __k, long double __phi)
- template<typename _Tp, typename _Up >
 [__gnu_cxx::__promote_fp_t<_Tp, _Up > hurwitz_zeta](#) (_Tp __s, _Up __a)
- template<typename _Tp, typename _Up >
 [std::complex<_Tp > hurwitz_zeta](#) (_Tp __s, std::complex<_Up > __a)
- float [hurwitz_zetaf](#) (float __s, float __a)
- long double [hurwitz_zetal](#) (long double __s, long double __a)
- template<typename _Tpa, typename _Tpb, typename _Tpc, typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tpa, _Tpb, _Tpc, _Tp > hyperg](#) (_Tpa __a, _Tpb __b, _Tpc __c, _Tp __x)
- float [hypergff](#) (float __a, float __b, float __c, float __x)
- long double [hypergfl](#) (long double __a, long double __b, long double __c, long double __x)
- template<typename _Ta, typename _Tb, typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp > ibeta](#) (_Ta __a, _Tb __b, _Tp __x)
- template<typename _Ta, typename _Tb, typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp > ibetac](#) (_Ta __a, _Tb __b, _Tp __x)
- float [ibetaacf](#) (float __a, float __b, float __x)
- long double [ibetaacl](#) (long double __a, long double __b, long double __x)
- float [ibetaf](#) (float __a, float __b, float __x)

- long double [ibetal](#) (long double __a, long double __b, long double __x)
- template<typename _Talpha, typename _Tbeta, typename _Tp >
__gnu_cxx::__promote_fp_t< _Talpha, _Tbeta, _Tp > [jacobi](#) (unsigned __n, _Talpha __alpha, _Tbeta __beta, _Tp __x)
- template<typename _Kp, typename _Up >
__gnu_cxx::__promote_fp_t< _Kp, _Up > [jacobi_cn](#) (_Kp __k, _Up __u)
- float [jacobi_cnf](#) (float __k, float __u)
- long double [jacobi_cnl](#) (long double __k, long double __u)
- template<typename _Kp, typename _Up >
__gnu_cxx::__promote_fp_t< _Kp, _Up > [jacobi_dn](#) (_Kp __k, _Up __u)
- float [jacobi_dnf](#) (float __k, float __u)
- long double [jacobi_dnl](#) (long double __k, long double __u)
- template<typename _Kp, typename _Up >
__gnu_cxx::__promote_fp_t< _Kp, _Up > [jacobi_sn](#) (_Kp __k, _Up __u)
- float [jacobi_snf](#) (float __k, float __u)
- long double [jacobi_snl](#) (long double __k, long double __u)
- template<typename _Tk, typename _Tphi >
__gnu_cxx::__promote_fp_t< _Tk, _Tphi > [jacobi_zeta](#) (_Tk __k, _Tphi __phi)
- float [jacobi_zetaf](#) (float __k, float __phi)
- long double [jacobi_zetal](#) (long double __k, long double __phi)
- float [jacobif](#) (unsigned __n, float __alpha, float __beta, float __x)
- long double [jacobil](#) (unsigned __n, long double __alpha, long double __beta, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [lbincoef](#) (unsigned int __n, unsigned int __k)
- float [lbincoeff](#) (unsigned int __n, unsigned int __k)
- long double [lbincoefl](#) (unsigned int __n, unsigned int __k)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [ldouble_factorial](#) (int __n)
- float [ldouble_factorialf](#) (int __n)
- long double [ldouble_factoriall](#) (int __n)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [legendre_q](#) (unsigned int __l, _Tp __x)
- float [legendre_qf](#) (unsigned int __l, float __x)
- long double [legendre_ql](#) (unsigned int __l, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [lfactorial](#) (unsigned int __n)
- float [lfactorialf](#) (unsigned int __n)
- long double [lfactoriall](#) (unsigned int __n)
- template<typename _Ta >
std::complex< __gnu_cxx::__promote_fp_t< _Ta > > [lgamma](#) (std::complex< _Ta > __a)
- std::complex< float > [lgammaf](#) (std::complex< float > __a)
- std::complex< long double > [lgammal](#) (std::complex< long double > __a)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [logint](#) (_Tp __x)
- float [logintf](#) (float __x)
- long double [logintl](#) (long double __x)
- template<typename _Tp, typename _Tn >
__gnu_cxx::__promote_fp_t< _Tp, _Tn > [lpochhammer](#) (_Tp __a, _Tn __n)
- template<typename _Tp, typename _Tn >
__gnu_cxx::__promote_fp_t< _Tp, _Tn > [lpochhammer_lower](#) (_Tp __a, _Tn __n)
- float [lpochhammer_lowerf](#) (float __a, float __n)
- long double [lpochhammer_lowerl](#) (long double __a, long double __n)

- float [lpochhammerf](#) (float __a, float __n)
- long double [lpochhammerl](#) (long double __a, long double __n)
- template<typename _Tph, typename _Tpa >
__gnu_cxx::__promote_fp_t< _Tph, _Tpa > [owens_t](#) (_Tph __h, _Tpa __a)
- float [owens_tf](#) (float __h, float __a)
- long double [owens_tl](#) (long double __h, long double __a)
- template<typename _Ta, typename _Tp >
__gnu_cxx::__promote_fp_t< _Ta, _Tp > [pgamma](#) (_Ta __a, _Tp __x)
- float [pgammaf](#) (float __a, float __x)
- long double [pgammal](#) (long double __a, long double __x)
- template<typename _Tp, typename _Tn >
__gnu_cxx::__promote_fp_t< _Tp, _Tn > [pochhammer](#) (_Tp __a, _Tn __n)
- template<typename _Tp, typename _Tn >
__gnu_cxx::__promote_fp_t< _Tp, _Tn > [pochhammer_lower](#) (_Tp __a, _Tn __n)
- float [pochhammer_lowerf](#) (float __a, float __n)
- long double [pochhammer_lowerl](#) (long double __a, long double __n)
- float [pochhammerf](#) (float __a, float __n)
- long double [pochhammerl](#) (long double __a, long double __n)
- template<typename _Tp, typename _Wp >
__gnu_cxx::__promote_fp_t< _Tp, _Wp > [polylog](#) (_Tp __s, _Wp __w)
- template<typename _Tp, typename _Wp >
std::complex< __gnu_cxx::__promote_fp_t< _Tp, _Wp > > [polylog](#) (_Tp __s, std::complex< _Tp > __w)
- float [polylogf](#) (float __s, float __w)
- std::complex< float > [polylogf](#) (float __s, std::complex< float > __w)
- long double [polylogl](#) (long double __s, long double __w)
- std::complex< long double > [polylogl](#) (long double __s, std::complex< long double > __w)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [psi](#) (_Tp __x)
- float [psif](#) (float __x)
- long double [psil](#) (long double __x)
- template<typename _Ta, typename _Tp >
__gnu_cxx::__promote_fp_t< _Ta, _Tp > [qgamma](#) (_Ta __a, _Tp __x)
- float [qgammaf](#) (float __a, float __x)
- long double [qgammal](#) (long double __a, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [radpoly](#) (unsigned int __n, unsigned int __m, _Tp __rho)
- float [radpolyf](#) (unsigned int __n, unsigned int __m, float __rho)
- long double [radpolyl](#) (unsigned int __n, unsigned int __m, long double __rho)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sin_pi](#) (_Tp __x)
- float [sin_pif](#) (float __x)
- long double [sin_pil](#) (long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sinc](#) (_Tp __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sinc_pi](#) (_Tp __x)
- float [sinc_pif](#) (float __x)
- long double [sinc_pil](#) (long double __x)
- float [sincf](#) (float __x)
- long double [sincl](#) (long double __x)
- __gnu_cxx::__sincos_t< double > [sincos](#) (double __x)

- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > sincos (_Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > sincos_pi (_Tp __x)`
- `__gnu_cxx::__sincos_t< float > sincos_pif (float __x)`
- `__gnu_cxx::__sincos_t< long double > sincos_pil (long double __x)`
- `__gnu_cxx::__sincos_t< float > sincosf (float __x)`
- `__gnu_cxx::__sincos_t< long double > sincosl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sinh_pi (_Tp __x)`
- `float sinh_pif (float __x)`
- `long double sinh_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sinhc (_Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sinhc_pi (_Tp __x)`
- `float sinhc_pif (float __x)`
- `long double sinhc_pil (long double __x)`
- `float sinhcf (float __x)`
- `long double sinhcl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sinhint (_Tp __x)`
- `float sinhintf (float __x)`
- `long double sinhintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sinint (_Tp __x)`
- `float sinintf (float __x)`
- `long double sinintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sph_bessel_i (unsigned int __n, _Tp __x)`
- `float sph_bessel_if (unsigned int __n, float __x)`
- `long double sph_bessel_il (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > sph_bessel_k (unsigned int __n, _Tp __x)`
- `float sph_bessel_kf (unsigned int __n, float __x)`
- `long double sph_bessel_kl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > sph_hankel_1 (unsigned int __n, _Tp __z)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > sph_hankel_1 (unsigned int __n, std::complex< _Tp > __x)`
- `std::complex< float > sph_hankel_1f (unsigned int __n, float __z)`
- `std::complex< float > sph_hankel_1f (unsigned int __n, std::complex< float > __x)`
- `std::complex< long double > sph_hankel_1l (unsigned int __n, long double __z)`
- `std::complex< long double > sph_hankel_1l (unsigned int __n, std::complex< long double > __x)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > sph_hankel_2 (unsigned int __n, _Tp __z)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > sph_hankel_2 (unsigned int __n, std::complex< _Tp > __x)`
- `std::complex< float > sph_hankel_2f (unsigned int __n, float __z)`
- `std::complex< float > sph_hankel_2f (unsigned int __n, std::complex< float > __x)`

- `std::complex< long double > sph_hankel_2l` (unsigned int `__n`, long double `__z`)
- `std::complex< long double > sph_hankel_2l` (unsigned int `__n`, `std::complex< long double > __x`)
- `template<typename _Ttheta, typename _Tphi >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ttheta, _Tphi > > sph_harmonic` (unsigned int `__l`, int `__m`, `__Ttheta __theta`, `__Tphi __phi`)
- `std::complex< float > sph_harmonicf` (unsigned int `__l`, int `__m`, float `__theta`, float `__phi`)
- `std::complex< long double > sph_harmonicl` (unsigned int `__l`, int `__m`, long double `__theta`, long double `__phi`)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > tan_pi` (`_Tp __x`)
- float `tan_pif` (float `__x`)
- long double `tan_pil` (long double `__x`)
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > tanh_pi` (`_Tp __x`)
- float `tanh_pif` (float `__x`)
- long double `tanh_pil` (long double `__x`)
- `template<typename _Ta >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ta > > tgamma` (`std::complex< _Ta > __a`)
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > tgamma` (`_Ta __a`, `_Tp __x`)
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > tgamma_lower` (`_Ta __a`, `_Tp __x`)
- float `tgamma_lowerf` (float `__a`, float `__x`)
- long double `tgamma_lowerl` (long double `__a`, long double `__x`)
- `std::complex< float > tgammaf` (`std::complex< float > __a`)
- float `tgammaf` (float `__a`, float `__x`)
- `std::complex< long double > tgamma` (`std::complex< long double > __a`)
- long double `tgamma` (long double `__a`, long double `__x`)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > theta_1` (`_Tpnu __nu`, `_Tp __x`)
- float `theta_1f` (float `__nu`, float `__x`)
- long double `theta_1l` (long double `__nu`, long double `__x`)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > theta_2` (`_Tpnu __nu`, `_Tp __x`)
- float `theta_2f` (float `__nu`, float `__x`)
- long double `theta_2l` (long double `__nu`, long double `__x`)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > theta_3` (`_Tpnu __nu`, `_Tp __x`)
- float `theta_3f` (float `__nu`, float `__x`)
- long double `theta_3l` (long double `__nu`, long double `__x`)
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > theta_4` (`_Tpnu __nu`, `_Tp __x`)
- float `theta_4f` (float `__nu`, float `__x`)
- long double `theta_4l` (long double `__nu`, long double `__x`)
- `template<typename _Tpk, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpk, _Tp > theta_c` (`_Tpk __k`, `_Tp __x`)
- float `theta_cf` (float `__k`, float `__x`)
- long double `theta_cl` (long double `__k`, long double `__x`)
- `template<typename _Tpk, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpk, _Tp > theta_d` (`_Tpk __k`, `_Tp __x`)
- float `theta_df` (float `__k`, float `__x`)
- long double `theta_dl` (long double `__k`, long double `__x`)

- `template<typename _Tpk, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpk, _Tp > theta_n (_Tpk __k, _Tp __x)`
- `float theta_nf (float __k, float __x)`
- `long double theta_nl (long double __k, long double __x)`
- `template<typename _Tpk, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpk, _Tp > theta_s (_Tpk __k, _Tp __x)`
- `float theta_sf (float __k, float __x)`
- `long double theta_sl (long double __k, long double __x)`
- `template<typename _Trho, typename _Tphi >`
`__gnu_cxx::__promote_fp_t< _Trho, _Tphi > zernike (unsigned int __n, int __m, _Trho __rho, _Tphi __phi)`
- `float zernikef (unsigned int __n, int __m, float __rho, float __phi)`
- `long double zernikel (unsigned int __n, int __m, long double __rho, long double __phi)`

9.2 std Namespace Reference

Namespaces

- [__detail](#)

Functions

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > assoc_laguerre (unsigned int __n, unsigned int __m, _Tp __x)`
- `float assoc_laguerref (unsigned int __n, unsigned int __m, float __x)`
- `long double assoc_laguerrel (unsigned int __n, unsigned int __m, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > assoc_legendre (unsigned int __l, unsigned int __m, _Tp __x)`
- `float assoc_legendref (unsigned int __l, unsigned int __m, float __x)`
- `long double assoc_legendrel (unsigned int __l, unsigned int __m, long double __x)`
- `template<typename _Tpa, typename _Tpb >`
`__gnu_cxx::__promote_fp_t< _Tpa, _Tpb > beta (_Tpa __a, _Tpb __b)`
- `float betaf (float __a, float __b)`
- `long double betal (long double __a, long double __b)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > comp_ellint_1 (_Tp __k)`
- `float comp_ellint_1f (float __k)`
- `long double comp_ellint_1l (long double __k)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > comp_ellint_2 (_Tp __k)`
- `float comp_ellint_2f (float __k)`
- `long double comp_ellint_2l (long double __k)`
- `template<typename _Tp, typename _Tpn >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpn > comp_ellint_3 (_Tp __k, _Tpn __nu)`
- `float comp_ellint_3f (float __k, float __nu)`

Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for float modulus k .

- `long double comp_ellint_3l (long double __k, long double __nu)`

Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for long double modulus k .

- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > cyl_bessel_i (_Tpnu __nu, _Tp __x)`
- `float cyl_bessel_if (float __nu, float __x)`
- `long double cyl_bessel_il (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > cyl_bessel_j (_Tpnu __nu, _Tp __x)`
- `float cyl_bessel_jf (float __nu, float __x)`
- `long double cyl_bessel_jl (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > cyl_bessel_k (_Tpnu __nu, _Tp __x)`
- `float cyl_bessel_kf (float __nu, float __x)`
- `long double cyl_bessel_kl (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > cyl_neumann (_Tpnu __nu, _Tp __x)`
- `float cyl_neumannf (float __nu, float __x)`
- `long double cyl_neumannl (long double __nu, long double __x)`
- `template<typename _Tp, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpp > ellint_1 (_Tp __k, _Tpp __phi)`
- `float ellint_1f (float __k, float __phi)`
- `long double ellint_1l (long double __k, long double __phi)`
- `template<typename _Tp, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpp > ellint_2 (_Tp __k, _Tpp __phi)`
- `float ellint_2f (float __k, float __phi)`
- Return the incomplete elliptic integral of the second kind $E(k, \phi)$ for float argument.*
- `long double ellint_2l (long double __k, long double __phi)`
- Return the incomplete elliptic integral of the second kind $E(k, \phi)$.*
- `template<typename _Tp, typename _Tpn, typename _Tpp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpn, _Tpp > ellint_3 (_Tp __k, _Tpn __nu, _Tpp __phi)`
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.*
- `float ellint_3f (float __k, float __nu, float __phi)`
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ for float argument.*
- `long double ellint_3l (long double __k, long double __nu, long double __phi)`
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.*
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > expint (_Tp __x)`
- `float expintf (float __x)`
- `long double expintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > hermite (unsigned int __n, _Tp __x)`
- `float hermitef (unsigned int __n, float __x)`
- `long double hermitel (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > laguerre (unsigned int __n, _Tp __x)`
- `float laguerref (unsigned int __n, float __x)`
- `long double laguerrel (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > legendre (unsigned int __l, _Tp __x)`
- `float legendref (unsigned int __l, float __x)`
- `long double legendrel (unsigned int __l, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > riemann_zeta (_Tp __s)`

- float [riemann_zetaf](#) (float __s)
- long double [riemann_zetal](#) (long double __s)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sph_bessel](#) (unsigned int __n, _Tp __x)
- float [sph_besself](#) (unsigned int __n, float __x)
- long double [sph_bessell](#) (unsigned int __n, long double __x)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sph_legendre](#) (unsigned int __l, unsigned int __m, _Tp __theta)
- float [sph_legendref](#) (unsigned int __l, unsigned int __m, float __theta)
- long double [sph_legendrel](#) (unsigned int __l, unsigned int __m, long double __theta)
- template<typename _Tp >
__gnu_cxx::__promote_fp_t< _Tp > [sph_neumann](#) (unsigned int __n, _Tp __x)
- float [sph_neumannf](#) (unsigned int __n, float __x)
- long double [sph_neumannl](#) (unsigned int __n, long double __x)

9.3 std::__detail Namespace Reference

Classes

- struct [__gamma_lanczos_data](#)
- struct [__gamma_lanczos_data< double >](#)
- struct [__gamma_lanczos_data< float >](#)
- struct [__gamma_lanczos_data< long double >](#)
- struct [__gamma_spouge_data](#)
- struct [__gamma_spouge_data< double >](#)
- struct [__gamma_spouge_data< float >](#)
- struct [__gamma_spouge_data< long double >](#)
- class [_Airy](#)
- class [_Airy_asymp](#)
- struct [_Airy_asymp_data](#)
- struct [_Airy_asymp_data< double >](#)
- struct [_Airy_asymp_data< float >](#)
- struct [_Airy_asymp_data< long double >](#)
- class [_Airy_asymp_series](#)
- struct [_Airy_default_radii](#)
- struct [_Airy_default_radii< double >](#)
- struct [_Airy_default_radii< float >](#)
- struct [_Airy_default_radii< long double >](#)
- class [_Airy_series](#)
- struct [_AiryAuxilliaryState](#)
- struct [_AiryState](#)
- struct [_Factorial_table](#)

Functions

- `template<typename _Tp >`
`__gnu_cxx::__airy_t< _Tp, _Tp > __airy (_Tp __z)`
Compute the Airy functions $Ai(x)$ and $Bi(x)$ and their first derivatives $Ai'(x)$ and $Bi'(x)$ respectively.
- `template<typename _Tp >`
`std::complex< _Tp > __airy_ai (std::complex< _Tp > __z)`
Return the complex Airy Ai function.
- `template<typename _Tp >`
`void __airy_arg (std::complex< _Tp > __num2d3, std::complex< _Tp > __zeta, std::complex< _Tp > &__argp, std::complex< _Tp > &__argm)`
Compute the arguments for the Airy function evaluations carefully to prevent premature overflow. Note that the major work here is in `safe_div`. A faster, but less safe implementation can be obtained without use of `safe_div`.
- `template<typename _Tp >`
`std::complex< _Tp > __airy_bi (std::complex< _Tp > __z)`
Return the complex Airy Bi function.
- `template<typename _Tp >`
`_Tp __assoc_laguerre (unsigned int __n, unsigned int __m, _Tp __x)`
This routine returns the associated Laguerre polynomial of order n , degree m : $L_n^m(x)$.
- `template<typename _Tp >`
`_Tp __assoc_legendre_p (unsigned int __l, unsigned int __m, _Tp __x)`
Return the associated Legendre function by recursion on l and downward recursion on m .
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __bernoulli (int __n)`
This returns Bernoulli number B_n .
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __bernoulli_2n (int __n)`
This returns Bernoulli number B_{2n} at even integer arguments $2n$.
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __bernoulli_series (unsigned int __n)`
This returns Bernoulli numbers from a table or by summation for larger values.
- `template<typename _Tp >`
`_Tp __beta (_Tp __a, _Tp __b)`
Return the beta function $B(a, b)$.
- `template<typename _Tp >`
`_Tp __beta_gamma (_Tp __a, _Tp __b)`
Return the beta function: $B(a, b)$.
- `template<typename _Tp >`
`_Tp __beta_inc (_Tp __a, _Tp __b, _Tp __x)`
- `template<typename _Tp >`
`_Tp __beta_lgamma (_Tp __a, _Tp __b)`
Return the beta function $B(a, b)$ using the log gamma functions.
- `template<typename _Tp >`
`_Tp __beta_product (_Tp __a, _Tp __b)`
Return the beta function $B(x, y)$ using the product form.
- `template<typename _Tp >`
`_Tp __bincoef (unsigned int __n, unsigned int __k)`

Return the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

- `template<typename _Tp >`
`_Tp __bincoef (_Tp __nu, unsigned int __k)`

Return the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- `template<typename _Tp >`
`_Tp __binomial_cdf (_Tp __p, unsigned int __n, unsigned int __k)`
Return the binomial cumulative distribution function.
- `template<typename _Tp >`
`_Tp __binomial_cdfc (_Tp __p, unsigned int __n, unsigned int __k)`
Return the complementary binomial cumulative distribution function.
- `template<typename _Tp >`
`_Tp __binomial_pdf (_Tp __p, unsigned int __n, unsigned int __k)`
Return the binomial probability mass function.
- `template<typename _Sp, typename _Tp >`
`_Tp __bose_einstein (_Sp __s, _Tp __x)`
- `template<typename _Tp >`
`_Tp __chebyshev_recur (unsigned int __n, _Tp __x, _Tp __C0, _Tp __C1)`
- `template<typename _Tp >`
`_Tp __chebyshev_t (unsigned int __n, _Tp __x)`
- `template<typename _Tp >`
`_Tp __chebyshev_u (unsigned int __n, _Tp __x)`
- `template<typename _Tp >`
`_Tp __chebyshev_v (unsigned int __n, _Tp __x)`
- `template<typename _Tp >`
`_Tp __chebyshev_w (unsigned int __n, _Tp __x)`
- `template<typename _Tp >`
`_Tp __chi_squared_pdf (_Tp __chi2, unsigned int __nu)`

Return the chi-squared propability function. This returns the probability that the observed chi-squared for a correct model is less than the value χ^2 .

- `template<typename _Tp >`
`_Tp __chi_squared_pdfc (_Tp __chi2, unsigned int __nu)`

Return the complementary chi-squared propability function. This returns the probability that the observed chi-squared for a correct model is greater than the value χ^2 .

- `template<typename _Tp >`
`std::pair< _Tp, _Tp > __chshint (_Tp __x, _Tp &__Chi, _Tp &__Shi)`

This function returns the hyperbolic cosine $Ci(x)$ and hyperbolic sine $Si(x)$ integrals as a pair.

- `template<typename _Tp >`
`void __chshint_cont_frac (_Tp __t, _Tp &_Chi, _Tp &_Shi)`
This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by continued fraction for positive argument.
- `template<typename _Tp >`
`void __chshint_series (_Tp __t, _Tp &_Chi, _Tp &_Shi)`
This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by series summation for positive argument.
- `template<typename _Tp >`
`std::complex< _Tp > __clamp_0_m2pi (std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > __clamp_pi (std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > __clausen (unsigned int __m, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp __clausen (unsigned int __m, _Tp __w)`
- `template<typename _Tp >`
`_Tp __clausen_c (unsigned int __m, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp __clausen_c (unsigned int __m, _Tp __w)`
- `template<typename _Tp >`
`_Tp __clausen_s (unsigned int __m, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp __clausen_s (unsigned int __m, _Tp __w)`
- `template<typename _Tp >`
`_Tp __comp_ellint_1 (_Tp __k)`
Return the complete elliptic integral of the first kind $K(k)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __comp_ellint_2 (_Tp __k)`
Return the complete elliptic integral of the second kind $E(k)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __comp_ellint_3 (_Tp __k, _Tp __nu)`
Return the complete elliptic integral of the third kind $\Pi(k, \nu) = \Pi(k, \nu, \pi/2)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __comp_ellint_d (_Tp __k)`
- `template<typename _Tp >`
`_Tp __comp_ellint_rf (_Tp __x, _Tp __y)`
- `template<typename _Tp >`
`_Tp __comp_ellint_rg (_Tp __x, _Tp __y)`
- `template<typename _Tp >`
`_Tp __conf_hyperg (_Tp __a, _Tp __c, _Tp __x)`
Return the confluent hypergeometric function ${}_1F_1(a; c; x)$.
- `template<typename _Tp >`
`_Tp __conf_hyperg_lim (_Tp __c, _Tp __x)`
Return the confluent hypergeometric limit function ${}_0F_1(-; c; x)$.
- `template<typename _Tp >`
`_Tp __conf_hyperg_lim_series (_Tp __c, _Tp __x)`
This routine returns the confluent hypergeometric limit function by series expansion.
- `template<typename _Tp >`
`_Tp __conf_hyperg_luke (_Tp __a, _Tp __c, _Tp __xin)`

Return the hypergeometric function ${}_1F_1(a; c; x)$ by an iterative procedure described in Luke, *Algorithms for the Computation of Mathematical Functions*.

- `template<typename _Tp >`
`_Tp __conf_hyperg_series (_Tp __a, _Tp __c, _Tp __x)`

This routine returns the confluent hypergeometric function by series expansion.

- `template<typename _Tp >`
`_Tp __cos_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __cos_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp __cosh_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __cosh_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp __coshint (const _Tp __x)`

Return the hyperbolic cosine integral $Chi(x)$.

- `template<typename _Tp >`
`std::complex< _Tp > __cyl_bessel (std::complex< _Tp > __nu, std::complex< _Tp > __z)`

Return the complex cylindrical Bessel function.

- `template<typename _Tp >`
`_Tp __cyl_bessel_i (_Tp __nu, _Tp __x)`

Return the regular modified Bessel function of order ν : $I_\nu(x)$.

- `template<typename _Tp >`
`_Tp __cyl_bessel_ij_series (_Tp __nu, _Tp __x, _Tp __sgn, unsigned int __max_iter)`

This routine returns the cylindrical Bessel functions of order ν : J_ν or I_ν by series expansion.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_ik (_Tp __nu, _Tp __x)`

Return the modified cylindrical Bessel functions and their derivatives of order ν by various means.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_ik_asymp (_Tp __nu, _Tp __x)`

This routine computes the asymptotic modified cylindrical Bessel and functions of order ν : $I_\nu(x)$, $N_\nu(x)$. Use this for $x \gg nu^2 + 1$.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_ik_steel (_Tp __nu, _Tp __x)`

Compute the modified Bessel functions $I_\nu(x)$ and $K_\nu(x)$ and their first derivatives $I'_\nu(x)$ and $K'_\nu(x)$ respectively. These four functions are computed together for numerical stability.

- `template<typename _Tp >`
`_Tp __cyl_bessel_j (_Tp __nu, _Tp __x)`

Return the Bessel function of order ν : $J_\nu(x)$.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_jn (_Tp __nu, _Tp __x)`

Return the cylindrical Bessel functions and their derivatives of order ν by various means.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_jn_asymp (_Tp __nu, _Tp __x)`

This routine computes the asymptotic cylindrical Bessel and Neumann functions of order ν : $J_\nu(x)$, $N_\nu(x)$. Use this for $x \gg nu^2 + 1$.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, std::complex< _Tp > > __cyl_bessel_jn_neg_arg (_Tp __nu, _Tp __x)`

Return the cylindrical Bessel functions and their derivatives of order ν and argument $x < 0$.

- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > __cyl_bessel_jn_steel (_Tp __nu, _Tp __x)`

Compute the Bessel $J_\nu(x)$ and Neumann $N_\nu(x)$ functions and their first derivatives $J'_\nu(x)$ and $N'_\nu(x)$ respectively. These four functions are computed together for numerical stability.

- `template<typename _Tp >`
`_Tp __cyl_bessel_k (_Tp __nu, _Tp __x)`
 Return the irregular modified Bessel function $K_\nu(x)$ of order ν .
- `template<typename _Tp >`
`std::complex< _Tp > __cyl_hankel_1 (_Tp __nu, _Tp __x)`
 Return the cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > __cyl_hankel_1 (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
 Return the complex cylindrical Hankel function of the first kind.
- `template<typename _Tp >`
`std::complex< _Tp > __cyl_hankel_2 (_Tp __nu, _Tp __x)`
 Return the cylindrical Hankel function of the second kind $H_\nu^{(2)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > __cyl_hankel_2 (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
 Return the complex cylindrical Hankel function of the second kind.
- `template<typename _Tp >`
`std::complex< _Tp > __cyl_neumann (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
 Return the complex cylindrical Neumann function.
- `template<typename _Tp >`
`_Tp __cyl_neumann_n (_Tp __nu, _Tp __x)`
 Return the Neumann function of order ν : $N_\nu(x)$.
- `template<typename _Tp >`
`_Tp __dawson (_Tp __x)`
 Return the Dawson integral, $F(x)$, for real argument x .
- `template<typename _Tp >`
`_Tp __dawson_cont_frac (_Tp __x)`
 Compute the Dawson integral using a sampling theorem representation.
- `template<typename _Tp >`
`_Tp __dawson_series (_Tp __x)`
 Compute the Dawson integral using the series expansion.
- `template<typename _Tp >`
`void __debye_region (std::complex< _Tp > __alpha, int &__indexr, char &__aorb)`
- `template<typename _Tp >`
`_Tp __dilog (_Tp __x)`
 Compute the dilogarithm function $Li_2(x)$ by summation for $x \leq 1$.
- `template<typename _Tp >`
`_Tp __dirichlet_beta (std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp __dirichlet_beta (_Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > __dirichlet_eta (std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp __dirichlet_eta (_Tp __w)`
- `template<typename _Tp >`
`_Tp __dirichlet_lambda (_Tp __w)`
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __double_factorial (int __n)`
 Return the double factorial of the integer n .

- `template<typename _Tp >`
`_Tp __ellint_1 (_Tp __k, _Tp __phi)`
Return the incomplete elliptic integral of the first kind $F(k, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __ellint_2 (_Tp __k, _Tp __phi)`
Return the incomplete elliptic integral of the second kind $E(k, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __ellint_3 (_Tp __k, _Tp __nu, _Tp __phi)`
Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp __ellint_cel (_Tp __k_c, _Tp __p, _Tp __a, _Tp __b)`
- `template<typename _Tp >`
`_Tp __ellint_d (_Tp __k, _Tp __phi)`
- `template<typename _Tp >`
`_Tp __ellint_el1 (_Tp __x, _Tp __k_c)`
- `template<typename _Tp >`
`_Tp __ellint_el2 (_Tp __x, _Tp __k_c, _Tp __a, _Tp __b)`
- `template<typename _Tp >`
`_Tp __ellint_el3 (_Tp __x, _Tp __k_c, _Tp __p)`
- `template<typename _Tp >`
`_Tp __ellint_rc (_Tp __x, _Tp __y)`
Return the Carlson elliptic function $R_C(x, y) = R_F(x, y, y)$ where $R_F(x, y, z)$ is the Carlson elliptic function of the first kind.
- `template<typename _Tp >`
`_Tp __ellint_rd (_Tp __x, _Tp __y, _Tp __z)`
Return the Carlson elliptic function of the second kind $R_D(x, y, z) = R_J(x, y, z, z)$ where $R_J(x, y, z, p)$ is the Carlson elliptic function of the third kind.
- `template<typename _Tp >`
`_Tp __ellint_rf (_Tp __x, _Tp __y, _Tp __z)`
Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind.
- `template<typename _Tp >`
`_Tp __ellint_rg (_Tp __x, _Tp __y, _Tp __z)`
Return the symmetric Carlson elliptic function of the second kind $R_G(x, y, z)$.
- `template<typename _Tp >`
`_Tp __ellint_rj (_Tp __x, _Tp __y, _Tp __z, _Tp __p)`
Return the Carlson elliptic function $R_J(x, y, z, p)$ of the third kind.
- `template<typename _Tp >`
`_Tp __ellnome (_Tp __k)`
- `template<typename _Tp >`
`_Tp __ellnome_k (_Tp __k)`
- `template<typename _Tp >`
`_Tp __ellnome_series (_Tp __k)`
- `template<typename _Tp >`
`_Tp __expint (unsigned int __n, _Tp __x)`
Return the exponential integral $E_n(x)$.
- `template<typename _Tp >`
`_Tp __expint (_Tp __x)`
Return the exponential integral $Ei(x)$.
- `template<typename _Tp >`
`_Tp __expint_E1 (_Tp __x)`

Return the exponential integral $E_1(x)$.

- `template<typename _Tp >`
`_Tp __expint_E1_asymp (_Tp __x)`

Return the exponential integral $E_1(x)$ by asymptotic expansion.

- `template<typename _Tp >`
`_Tp __expint_E1_series (_Tp __x)`

Return the exponential integral $E_1(x)$ by series summation. This should be good for $x < 1$.

- `template<typename _Tp >`
`_Tp __expint_Ei (_Tp __x)`

Return the exponential integral $Ei(x)$.

- `template<typename _Tp >`
`_Tp __expint_Ei_asymp (_Tp __x)`

Return the exponential integral $Ei(x)$ by asymptotic expansion.

- `template<typename _Tp >`
`_Tp __expint_Ei_series (_Tp __x)`

Return the exponential integral $Ei(x)$ by series summation.

- `template<typename _Tp >`
`_Tp __expint_En_asymp (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ for large argument.

- `template<typename _Tp >`
`_Tp __expint_En_cont_frac (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by continued fractions.

- `template<typename _Tp >`
`_Tp __expint_En_large_n (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ for large order.

- `template<typename _Tp >`
`_Tp __expint_En_recursion (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by recursion. Use upward recursion for $x < n$ and downward recursion (Miller's algorithm) otherwise.

- `template<typename _Tp >`
`_Tp __expint_En_series (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by series summation.

- `template<typename _Tp >`
`_Tp __exponential_cdf (_Tp __lambda, _Tp __x)`

Return the exponential cumulative probability density function.

- `template<typename _Tp >`
`_Tp __exponential_cdfc (_Tp __lambda, _Tp __x)`

Return the complement of the exponential cumulative probability density function.

- `template<typename _Tp >`
`_Tp __exponential_pdf (_Tp __lambda, _Tp __x)`

Return the exponential probability density function.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __factorial (unsigned int __n)`

Return the factorial of the integer n .

- `template<typename _Sp, typename _Tp >`
`_Tp __fermi_dirac (_Sp __s, _Tp __x)`

- `template<typename _Tp >`
`_Tp __fisher_f_cdf (_Tp __F, unsigned int __nu1, unsigned int __nu2)`

Return the F -distribution probability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .

- `template<typename _Tp >`
`_Tp __fisher_f_cdfc (_Tp __F, unsigned int __nu1, unsigned int __nu2)`
Return the F-distribution propability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .
- `template<typename _Tp >`
`__gnu_cxx::__fock_airy_t< _Tp, std::complex< _Tp > > __fock_airy (_Tp __x)`
Compute the Fock-type Airy functions $w_1(x)$ and $w_2(x)$ and their first derivatives $w'_1(x)$ and $w'_2(x)$ respectively.

$$w_1(x) = \sqrt{\pi}(Ai(x) + iBi(x))$$

$$w_2(x) = \sqrt{\pi}(Ai(x) - iBi(x))$$
- `template<typename _Tp >`
`std::complex< _Tp > __fresnel (const _Tp __x)`
Return the Fresnel cosine and sine integrals as a complex number $f[C(x) + iS(x)]$.
- `template<typename _Tp >`
`void __fresnel_cont_frac (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`
This function computes the Fresnel cosine and sine integrals by continued fractions for positive argument.
- `template<typename _Tp >`
`void __fresnel_series (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`
This function returns the Fresnel cosine and sine integrals as a pair by series expansion for positive argument.
- `template<typename _Tp >`
`_Tp __gamma (_Tp __a)`
Return the gamma function $\Gamma(a)$. The gamma function is defined by:

$$\Gamma(a) = \int_0^{\infty} e^{-t} t^{a-1} dt (a > 0)$$
- `template<typename _Tp >`
`_Tp __gamma_cdf (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma cumulative propability distribution function.
- `template<typename _Tp >`
`_Tp __gamma_cdfc (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma complementary cumulative propability distribution function.
- `template<typename _Tp >`
`std::pair< _Tp, _Tp > __gamma_cont_frac (_Tp __a, _Tp __x)`
Return the incomplete gamma function by continued fraction.
- `template<typename _Tp >`
`_Tp __gamma_pdf (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma propability distribution function.
- `template<typename _Tp >`
`_Tp __gamma_reciprocal_series (_Tp __a)`
- `template<typename _Tp >`
`std::pair< _Tp, _Tp > __gamma_series (_Tp __a, _Tp __x)`
Return the incomplete gamma function by series summation.

$$\gamma(a, x) = x^a e^{-x} \sum_{k=1}^{\infty} \frac{x^k}{(a)_k}$$
- `template<typename _Tp >`
`__gnu_cxx::__gamma_temme_t< _Tp > __gamma_temme (_Tp __mu)`

Compute the gamma functions required by the Temme series expansions of $N_\nu(x)$ and $K_\nu(x)$.

$$\Gamma_1 = \frac{1}{2\mu} \left[\frac{1}{\Gamma(1-\mu)} - \frac{1}{\Gamma(1+\mu)} \right]$$

and

$$\Gamma_2 = \frac{1}{2} \left[\frac{1}{\Gamma(1-\mu)} + \frac{1}{\Gamma(1+\mu)} \right]$$

where $-1/2 \leq \mu \leq 1/2$ is $\mu = \nu - N$ and N is the nearest integer to ν . The values of $\Gamma(1+\mu)$ and $\Gamma(1-\mu)$ are returned as well.

- `template<typename _Tp >`
`_Tp __gauss(_Tp __x)`
- `template<typename _Tp >`
`_Tp __gegenbauer_poly(unsigned int __n, _Tp __alpha, _Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > __hankel`
`(std::complex< _Tp > __nu, std::complex< _Tp > __z)`
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > __hankel←`
`__debye(std::complex< _Tp > __nu, std::complex< _Tp > __z, std::complex< _Tp > __alpha, int __indexr, char`
`& __aorb, int __morn)`
- `template<typename _Tp >`
`void __hankel_params(std::complex< _Tp > __nu, std::complex< _Tp > __zhat, std::complex< _Tp > & __p,`
`std::complex< _Tp > & __p2, std::complex< _Tp > & __nup2, std::complex< _Tp > & __num2, std::complex<`
`_Tp > & __num1d3, std::complex< _Tp > & __num2d3, std::complex< _Tp > & __num4d3, std::complex< ←`
`_Tp > & __zeta, std::complex< _Tp > & __zetaphf, std::complex< _Tp > & __zetamhf, std::complex< _Tp >`
`& __zetam3hf, std::complex< _Tp > & __zetrat)`

Compute parameters depending on z and nu that appear in the uniform asymptotic expansions of the Hankel functions and their derivatives, except the arguments to the Airy functions.

- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > __hankel←`
`__uniform(std::complex< _Tp > __nu, std::complex< _Tp > __z)`
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > __hankel←`
`__uniform_olver(std::complex< _Tp > __nu, std::complex< _Tp > __z)`

This routine computes the uniform asymptotic approximations of the Hankel functions and their derivatives including a patch for the case when the order equals or nearly equals the argument. At such points, Olver's expressions have zero denominators (and numerators) resulting in numerical problems. This routine averages results from four surrounding points in the complex plane to obtain the result in such cases.

- `template<typename _Tp >`
`void __hankel_uniform_outer(std::complex< _Tp > __nu, std::complex< _Tp > __z, _Tp __eps, std::complex<`
`_Tp > & __zhat, std::complex< _Tp > & __1dnsq, std::complex< _Tp > & __num1d3, std::complex< _Tp >`
`& __num2d3, std::complex< _Tp > & __p, std::complex< _Tp > & __p2, std::complex< _Tp > & __etm3h, std←`
`::complex< _Tp > & __etrat, std::complex< _Tp > & __Aip, std::complex< _Tp > & __o4dp, std::complex< _Tp`
`> & __Aim, std::complex< _Tp > & __o4dm, std::complex< _Tp > & __od2p, std::complex< _Tp > & __od0dp,`
`std::complex< _Tp > & __od2m, std::complex< _Tp > & __od0dm)`

Compute outer factors and associated functions of z and nu appearing in Olver's uniform asymptotic expansions of the Hankel functions of the first and second kinds and their derivatives. The various functions of z and nu returned by `hankel_uniform_outer` are available for use in computing further terms in the expansions.

- `template<typename _Tp >`
`void __hankel_uniform_sum(std::complex< _Tp > __p, std::complex< _Tp > __p2, std::complex< _Tp > ←`
`__num2, std::complex< _Tp > __zetam3hf, std::complex< _Tp > __Aip, std::complex< _Tp > __o4dp, std←`
`::complex< _Tp > __Aim, std::complex< _Tp > __o4dm, std::complex< _Tp > __od2p, std::complex< _Tp >`

`__od0dp, std::complex< _Tp > __od2m, std::complex< _Tp > __od0dm, _Tp __eps, std::complex< _Tp > &__H1sum, std::complex< _Tp > &__H1psum, std::complex< _Tp > &__H2sum, std::complex< _Tp > &__H2psum)`

Compute the sums in appropriate linear combinations appearing in Olver's uniform asymptotic expansions for the Hankel functions of the first and second kinds and their derivatives, using up to nterms (less than 5) to achieve relative error eps.

- `template<typename _Tp >`
`_Tp __harmonic_number (unsigned int __n)`
- `template<typename _Tp >`
`_Tp __heuman_lambda (_Tp __k, _Tp __phi)`
- `template<typename _Tp >`
`_Tp __hurwitz_zeta (_Tp __s, _Tp __a)`
Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.
- `template<typename _Tp >`
`_Tp __hurwitz_zeta_euler_maclaurin (_Tp __s, _Tp __a)`
Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.
- `template<typename _Tp >`
`std::complex< _Tp > __hurwitz_zeta_polylog (_Tp __s, std::complex< _Tp > __a)`
- `template<typename _Tp >`
`std::complex< _Tp > __hydrogen (unsigned int __n, unsigned int __l, unsigned int __m, _Tp __Z, _Tp __r, _Tp __theta, _Tp __phi)`
- `template<typename _Tp >`
`_Tp __hyperg (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$.
- `template<typename _Tp >`
`_Tp __hyperg_luke (_Tp __a, _Tp __b, _Tp __c, _Tp __xin)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by an iterative procedure described in Luke, Algorithms for the Computation of Mathematical Functions.
- `template<typename _Tp >`
`_Tp __hyperg_reflect (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by the reflection formulae in Abramowitz & Stegun formula 15.3.6 for $d = c - a - b$ not integral and formula 15.3.11 for $d = c - a - b$ integral. This assumes $a, b, c \neq$ negative integer.
- `template<typename _Tp >`
`_Tp __hyperg_series (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by series expansion.
- `template<typename _Tp >`
`_Tp __ibeta_cont_frac (_Tp __a, _Tp __b, _Tp __x)`
- `template<typename _Tp >`
`std::tuple< _Tp, _Tp, _Tp > __jacobi_sncndn (_Tp __k, _Tp __u)`
- `template<typename _Tp >`
`_Tp __jacobi_zeta (_Tp __k, _Tp __phi)`
- `template<typename _Tp >`
`_Tp __laguerre (unsigned int __n, _Tp __x)`
This routine returns the Laguerre polynomial of order n: $L_n(x)$.
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __lanczos_binet1p (_Tp __z)`
Return the Binet function $J(1 + z)$ by the Lanczos method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^(z))$ defined by*

$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

- template<typename _Tp >
_GLIBCXX14_CONSTEXPR _Tp __lanczos_log_gamma1p (_Tp __z)
Return the logarithm of the gamma function $\log(\Gamma(1+z))$ by the Lanczos method.
- template<typename _Tp >
_Tp __legendre_q (unsigned int __l, _Tp __x)
Return the Legendre function of the second kind by upward recursion on order l .
- template<typename _Tp >
_Tp __log_bincoef (unsigned int __n, unsigned int __k)
Return the logarithm of the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

- template<typename _Tp >
_Tp __log_bincoef (_Tp __nu, unsigned int __k)
Return the logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- template<typename _Tp >
_Tp __log_bincoef_sign (_Tp __nu, unsigned int __k)
Return the sign of the exponentiated logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- template<typename _Tp >
std::complex< _Tp > __log_bincoef_sign (std::complex< _Tp > __nu, unsigned int __k)
- template<typename _Tp >
_GLIBCXX14_CONSTEXPR _Tp __log_double_factorial (_Tp __x)
- template<typename _Tp >
_GLIBCXX14_CONSTEXPR _Tp __log_double_factorial (int __n)
Return the logarithm of the double factorial of the integer n .
- template<typename _Tp >
_GLIBCXX14_CONSTEXPR _Tp __log_factorial (unsigned int __n)
Return the logarithm of the factorial of the integer n .
- template<typename _Tp >
_Tp __log_gamma (_Tp __a)
Return $\log(|\Gamma(a)|)$. This will return values even for $a < 0$. To recover the sign of $\Gamma(a)$ for any argument use __log_gamma_sign.

- `template<typename _Tp >`
`std::complex< _Tp > __log_gamma (std::complex< _Tp > __a)`
Return $\log(\Gamma(a))$ for complex argument.
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __log_gamma_bernoulli (_Tp __x)`
Return $\log(\Gamma(x))$ by asymptotic expansion with Bernoulli number coefficients. This is like Sterling's approximation.
- `template<typename _Tp >`
`_Tp __log_gamma_sign (_Tp __a)`
Return the sign of $\Gamma(x)$. At nonpositive integers zero is returned indicating $\Gamma(x)$ is undefined.
- `template<typename _Tp >`
`std::complex< _Tp > __log_gamma_sign (std::complex< _Tp > __a)`
- `template<typename _Tp >`
`_Tp __log_pochhammer (_Tp __a, _Tp __nu)`
Return the logarithm of the (upper) Pochhammer symbol or the rising factorial function. The Pochhammer symbol is defined for integer order by

$$(a)_\nu = \Gamma(a + \nu) / \Gamma(a) = \prod_{k=0}^{\nu-1} (a + k), (a)_0 = 1$$

Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a + \nu)] - \ln[\Gamma(a)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp __log_pochhammer_lower (_Tp __a, _Tp __nu)`
Return the logarithm of the lower Pochhammer symbol or the falling factorial function. The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + 1) / \Gamma(a - \nu + 1) = \prod_{k=0}^{\nu-1} (a - k), (a)_0 = 1$$

In particular, $(n)_n = n!$. Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a + 1)] - \ln[\Gamma(a - \nu + 1)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\underline{n}}$$

,

$$\left\{ \begin{matrix} a \\ n \end{matrix} \right\}$$

, and others.

- `template<typename _Tp >`
`_Tp __logint (const _Tp __x)`
Return the logarithmic integral $li(x)$.
- `template<typename _Tp >`
`_Tp __lognormal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`
Return the lognormal cumulative probability density function.
- `template<typename _Tp >`
`_Tp __lognormal_pdf (_Tp __mu, _Tp __sigma, _Tp __x)`
Return the lognormal probability density function.
- `template<typename _Tp >`
`_Tp __normal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`

Return the normal cumulative probability density function.

- `template<typename _Tp >`
`_Tp __normal_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the normal probability density function.

- `template<typename _Tp >`
`_Tp __owens_t (_Tp __h, _Tp __a)`
- `template<typename _Tp >`
`_Tp __pgamma (_Tp __a, _Tp __x)`

Return the regularized lower incomplete gamma function. The regularized lower incomplete gamma function is defined by

$$P(a, x) = \frac{\gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

is the lower incomplete gamma function.

- `template<typename _Tp >`
`_Tp __pochhammer (_Tp __a, int __n)`

Return the (upper) Pochhammer function or the rising factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + \nu) / \Gamma(a), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp __pochhammer_lower (_Tp __a, int __n)`

Return the (lower) Pochhammer function or the falling factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a) / \Gamma(a - \nu), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp __pochhammer_lower_lower (_Tp __a, int __n)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and integral order n . The lower Pochhammer symbol is defined by

$$(a)_n = \prod_{k=0}^{n-1} (a - k), (a)_0 = 1 = \Gamma(a + 1) / \Gamma(a - n + 1)$$

In particular, $(n)_n = n!$.

- `template<typename _Tp >`
`_Tp __pochhammer_lower_lower_lower (_Tp __a, _Tp __nu)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and order ν . The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a+1)/\Gamma(a-\nu+1) = \prod_{k=0}^{\nu-1} (a-k), (a)_0 = 1, \nu = n$$

In particular, $(n)_n = n!$.

- `template<typename _Tp >`
`std::complex< _Tp > __polar_pi (_Tp __rho, _Tp __phi_pi)`
- `template<typename _Tp >`
`_Tp __poly_hermite (unsigned int __n, _Tp __x)`
This routine returns the Hermite polynomial of order n : $H_n(x)$.
- `template<typename _Tp >`
`_Tp __poly_hermite_asymp (unsigned int __n, _Tp __x)`
This routine returns the Hermite polynomial of large order n : $H_n(x)$. We assume here that $x \geq 0$.
- `template<typename _Tp >`
`_Tp __poly_hermite_recursion (unsigned int __n, _Tp __x)`
This routine returns the Hermite polynomial of order n : $H_n(x)$ by recursion on n .
- `template<typename _Tp >`
`_Tp __poly_jacobi (unsigned int __n, _Tp __alpha, _Tp __beta, _Tp __x)`
- `template<typename _Tpa, typename _Tp >`
`_Tp __poly_laguerre (unsigned int __n, _Tpa __alpha1, _Tp __x)`
This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^\alpha(x)$.
- `template<typename _Tpa, typename _Tp >`
`_Tp __poly_laguerre_hyperg (unsigned int __n, _Tpa __alpha1, _Tp __x)`
Evaluate the polynomial based on the confluent hypergeometric function in a safe way, with no restriction on the arguments.
- `template<typename _Tpa, typename _Tp >`
`_Tp __poly_laguerre_large_n (unsigned __n, _Tpa __alpha1, _Tp __x)`
This routine returns the associated Laguerre polynomial of order n , degree $\alpha > -1$ for large n . Abramowitz & Stegun, 13.5.21.
- `template<typename _Tpa, typename _Tp >`
`_Tp __poly_laguerre_recursion (unsigned int __n, _Tpa __alpha1, _Tp __x)`
This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^\alpha(x)$ by recursion.
- `template<typename _Tp >`
`_Tp __poly_legendre_p (unsigned int __l, _Tp __x)`
Return the Legendre polynomial by upward recursion on order l .
- `template<typename _Tp >`
`_Tp __poly_prob_hermite_recursion (unsigned int __n, _Tp __x)`
This routine returns the Probabilists Hermite polynomial of order n : $He_n(x)$ by recursion on n .
- `template<typename _Tp >`
`_Tp __poly_radial_jacobi (unsigned int __n, unsigned int __m, _Tp __rho)`
- `template<typename _Tp >`
`_Tp __polylog (_Tp __s, _Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __polylog (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp, typename ArgType >`
`__gnu_cxx::__promote_fp_t< std::complex< _Tp >, ArgType > __polylog_exp (_Tp __s, ArgType __w)`
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_asymp (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_int_neg (int __s, std::complex< _Tp > __w)`

- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_int_neg` (const int __s, _Tp __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_int_pos` (unsigned int __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_int_pos` (unsigned int __s, _Tp __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_neg` (_Tp __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_neg` (int __s, std::complex< _Tp > __w)
- `template<typename _Tp, int __sigma>`
`std::complex< _Tp > __polylog_exp_neg_even` (unsigned int __n, std::complex< _Tp > __w)
- `template<typename _Tp, int __sigma>`
`std::complex< _Tp > __polylog_exp_neg_odd` (unsigned int __n, std::complex< _Tp > __w)
- `template<typename _PowTp, typename _Tp >`
`_Tp __polylog_exp_negative_real_part` (_PowTp __s, _Tp __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_pos` (unsigned int __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_pos` (unsigned int __s, _Tp __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_pos` (_Tp __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_real_neg` (_Tp __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_real_neg` (_Tp __s, _Tp __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_real_pos` (_Tp __s, std::complex< _Tp > __w)
- `template<typename _Tp >`
`std::complex< _Tp > __polylog_exp_real_pos` (_Tp __s, _Tp __w)
- `template<typename _Tp >`
`_Tp __psi` (unsigned int __n)

Return the digamma function of integral argument. The digamma or $\psi(x)$ function is defined as the logarithmic derivative of the gamma function:

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

The digamma series for integral argument is given by:

$$\psi(n) = -\gamma_E + \sum_{k=1}^{\infty} \frac{1}{k}$$

The latter sum is called the harmonic number, H_n .

- `template<typename _Tp >`
`_Tp __psi` (_Tp __x)

Return the digamma function. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

For negative argument the reflection formula is used:

$$\psi(x) = \psi(1-x) - \pi \cot(\pi x)$$

- `template<typename _Tp >`
`_Tp __psi (unsigned int __n, _Tp __x)`
Return the polygamma function $\psi^{(n)}(x)$.

- `template<typename _Tp >`
`_Tp __psi_asymp (_Tp __x)`
Return the digamma function for large argument. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

- `template<typename _Tp >`
`_Tp __psi_series (_Tp __x)`
Return the digamma function by series expansion. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

- `template<typename _Tp >`
`_Tp __qgamma (_Tp __a, _Tp __x)`
Return the regularized upper incomplete gamma function. The regularized upper incomplete gamma function is defined by

$$Q(a, x) = \frac{\Gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\Gamma(a, x) = \int_x^\infty e^{-t} t^{a-1} dt (a > 0)$$

is the upper incomplete gamma function.

- `template<typename _Tp >`
`_Tp __rice_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`
Return the Rice probability density function.

- `template<typename _Tp >`
`_Tp __riemann_zeta (_Tp __s)`
Return the Riemann zeta function $\zeta(s)$.

- `template<typename _Tp >`
`_Tp __riemann_zeta_alt (_Tp __s)`
Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.

- `template<typename _Tp >`
`_Tp __riemann_zeta_euler_maclaurin (_Tp __s)`
Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.

- `template<typename _Tp >`
`_Tp __riemann_zeta_glob (_Tp __s)`
Evaluate the Riemann zeta function by series for all $s \neq 1$. Convergence is great until largish negative numbers. Then the convergence of the > 0 sum gets better.

- `template<typename _Tp >`
`_Tp __riemann_zeta_m_1 (_Tp __s)`
Return the Riemann zeta function $\zeta(s) - 1$.

- `template<typename _Tp >`
`_Tp __riemann_zeta_m_1_sum (_Tp __s)`
Return the Riemann zeta function $\zeta(s) - 1$ by summation for $s > 1$. This is a small remainder for large s .

- `template<typename _Tp >`
`_Tp __riemann_zeta_product (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ using the product over prime factors.

- `template<typename _Tp >`
`_Tp __riemann_zeta_sum (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ by summation for $s > 1$.

- `template<typename _Tp >`
`_Tp __sin_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __sin_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __sinc (_Tp __x)`

Return the sinus cardinal function

$$\text{sinc}(x) = \frac{\sin(x)}{x}$$

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __sinc_pi (_Tp __x)`

Return the reperiodized sinus cardinal function

$$\text{sinc}_{\pi}(x) = \frac{\sin(\pi x)}{\pi x}$$

- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > __sincos (_Tp __x)`
- `template<>`
`__gnu_cxx::__sincos_t< float > __sincos (float __x)`
- `template<>`
`__gnu_cxx::__sincos_t< double > __sincos (double __x)`
- `template<>`
`__gnu_cxx::__sincos_t< long double > __sincos (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > __sincos_pi (_Tp __x)`
- `template<typename _Tp >`
`std::pair< _Tp, _Tp > __sincosint (_Tp __x)`

This function returns the sine $Si(x)$ and cosine $Ci(x)$ integrals as a pair.

- `template<typename _Tp >`
`void __sincosint_asymp (_Tp __t, _Tp &_Si, _Tp &_Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by asymptotic series summation for positive argument.

- `template<typename _Tp >`
`void __sincosint_cont_frac (_Tp __t, _Tp &_Si, _Tp &_Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by continued fraction for positive argument.

- `template<typename _Tp >`
`void __sincosint_series (_Tp __t, _Tp &_Si, _Tp &_Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by series summation for positive argument.

- `template<typename _Tp >`
`_Tp __sinh_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __sinh_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __sinhc (_Tp __x)`

Return the hyperbolic sinus cardinal function

$$\text{sinhc}(x) = \frac{\sinh(x)}{x}$$

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __sinhc_pi (_Tp __x)`
Return the reperiodized hyperbolic sinus cardinal function

$$\operatorname{sinhc}_{\pi}(x) = \frac{\sinh(\pi x)}{\pi x}$$
- `template<typename _Tp >`
`_Tp __sinhint (const _Tp __x)`
Return the hyperbolic sine integral $\operatorname{Shi}(x)$.
- `template<typename _Tp >`
`_Tp __sph_bessel (unsigned int __n, _Tp __x)`
Return the spherical Bessel function $j_n(x)$ of order n and non-negative real argument x .
- `template<typename _Tp >`
`std::complex< _Tp > __sph_bessel (unsigned int __n, std::complex< _Tp > __z)`
Return the complex spherical Bessel function.
- `template<typename _Tp >`
`__gnu_cxx::__sph_mod_bessel_t< unsigned int, _Tp, _Tp > __sph_bessel_ik (unsigned int __n, _Tp __x)`
Compute the spherical modified Bessel functions $i_n(x)$ and $k_n(x)$ and their first derivatives $i'_n(x)$ and $k'_n(x)$ respectively.
- `template<typename _Tp >`
`__gnu_cxx::__sph_bessel_t< unsigned int, _Tp, _Tp > __sph_bessel_jn (unsigned int __n, _Tp __x)`
Compute the spherical Bessel $j_n(x)$ and Neumann $n_n(x)$ functions and their first derivatives $j'_n(x)$ and $n'_n(x)$ respectively.
- `template<typename _Tp >`
`__gnu_cxx::__sph_bessel_t< unsigned int, _Tp, std::complex< _Tp > > __sph_bessel_jn_neg_arg (unsigned int __n, _Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__sph_hankel_t< unsigned int, std::complex< _Tp >, std::complex< _Tp > > __sph_hankel (unsigned int __n, std::complex< _Tp > __z)`
Helper to compute complex spherical Hankel functions and their derivatives.
- `template<typename _Tp >`
`std::complex< _Tp > __sph_hankel_1 (unsigned int __n, _Tp __x)`
Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > __sph_hankel_1 (unsigned int __n, std::complex< _Tp > __z)`
Return the complex spherical Hankel function of the first kind.
- `template<typename _Tp >`
`std::complex< _Tp > __sph_hankel_2 (unsigned int __n, _Tp __x)`
Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > __sph_hankel_2 (unsigned int __n, std::complex< _Tp > __z)`
Return the complex spherical Hankel function of the second kind.
- `template<typename _Tp >`
`std::complex< _Tp > __sph_harmonic (unsigned int __l, int __m, _Tp __theta, _Tp __phi)`
Return the spherical harmonic function.
- `template<typename _Tp >`
`_Tp __sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta)`
Return the spherical associated Legendre function.
- `template<typename _Tp >`
`_Tp __sph_neumann (unsigned int __n, _Tp __x)`

Return the spherical Neumann function $n_n(x)$ of order n and non-negative real argument x .

- `template<typename _Tp >`
`std::complex< _Tp > __sph_neumann (unsigned int __n, std::complex< _Tp > __z)`

Return the complex spherical Neumann function.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __spouge_binet1p (_Tp __z)`

Return the Binet function $J(1+z)$ by the Spouge method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^*(z))$ defined by

$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp __spouge_log_gamma1p (_Tp __z)`

Return the logarithm of the gamma function $\log(\Gamma(1+z))$ by the Spouge algorithm:

$$\Gamma(z+1) = (z+a)^{z+1/2} e^{-z-a} \left[\sqrt{2\pi} + \sum_{k=1}^{\lceil a \rceil + 1} \frac{c_k(a)}{z+k} \right]$$

where

$$c_k(a) = \frac{(-1)^{k-1}}{(k-1)!} (a-k)^{k-1/2} e^{a-k}$$

and the error is bounded by

$$\epsilon(a) < a^{-1/2} (2\pi)^{-a-1/2}$$

- `template<typename _Tp >`
`_Tp __student_t_cdf (_Tp __t, unsigned int __nu)`
Return the Students T probability function.
- `template<typename _Tp >`
`_Tp __student_t_cdfc (_Tp __t, unsigned int __nu)`
Return the complement of the Students T probability function.
- `template<typename _Tp >`
`_Tp __tan_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __tan_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp __tanh_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > __tanh_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp __tgamma (_Tp __a, _Tp __x)`

Return the upper incomplete gamma function. The lower incomplete gamma function is defined by

$$\Gamma(a, x) = \int_x^\infty e^{-t} t^{a-1} dt (a > 0)$$

- `template<typename _Tp >`
`_Tp __tgamma_lower (_Tp __a, _Tp __x)`

Return the lower incomplete gamma function. The lower incomplete gamma function is defined by

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

- `template<typename _Tp >`
`_Tp __theta_1 (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_2 (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_2_asymp (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_2_sum (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_3 (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_3_asymp (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_3_sum (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_4 (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_c (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_d (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_n (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp __theta_s (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp __weibull_cdf (_Tp __a, _Tp __b, _Tp __x)`
Return the Weibull cumulative probability density function.
- `template<typename _Tp >`
`_Tp __weibull_pdf (_Tp __a, _Tp __b, _Tp __x)`
Return the Weibull probability density function.
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __zernike (unsigned int __n, int __m, _Tp __rho, _Tp __phi)`
- `template<typename _Tp >`
`_Tp __znorm1 (_Tp __x)`
- `template<typename _Tp >`
`_Tp __znorm2 (_Tp __x)`
- `template<typename _Tp = double>`
`_Tp evenzeta (unsigned int __k)`

Variables

- `template<typename _Tp >`
`constexpr int __max_FGH = _Airy_series<_Tp>::_N_FGH`
- `template<>`
`constexpr int __max_FGH< double > = 79`
- `template<>`
`constexpr int __max_FGH< float > = 15`
- `constexpr size_t _Num_Euler_Maclaurin_zeta = 100`
- `constexpr _Factorial_table< long double > _S_double_factorial_table [301]`
- `constexpr long double _S_Euler_Maclaurin_zeta [_Num_Euler_Maclaurin_zeta]`
- `constexpr _Factorial_table< long double > _S_factorial_table [171]`

- constexpr unsigned long long [_S_harmonic_denom](#) [[_S_num_harmonic_number](#)]
- constexpr unsigned long long [_S_harmonic_number](#) [[_S_num_harmonic_number](#)]
- constexpr [_Factorial_table](#)< long double > [_S_neg_double_factorial_table](#) [999]
- template<typename [_Tp](#) >
constexpr std::size_t [_S_num_double_factorials](#) = 0
- template<>
constexpr std::size_t [_S_num_double_factorials](#)< double > = 301
- template<>
constexpr std::size_t [_S_num_double_factorials](#)< float > = 57
- template<>
constexpr std::size_t [_S_num_double_factorials](#)< long double > = 301
- template<typename [_Tp](#) >
constexpr std::size_t [_S_num_factorials](#) = 0
- template<>
constexpr std::size_t [_S_num_factorials](#)< double > = 171
- template<>
constexpr std::size_t [_S_num_factorials](#)< float > = 35
- template<>
constexpr std::size_t [_S_num_factorials](#)< long double > = 171
- constexpr unsigned long long [_S_num_harmonic_number](#) = 29
- template<typename [_Tp](#) >
constexpr std::size_t [_S_num_neg_double_factorials](#) = 0
- template<>
constexpr std::size_t [_S_num_neg_double_factorials](#)< double > = 150
- template<>
constexpr std::size_t [_S_num_neg_double_factorials](#)< float > = 27
- template<>
constexpr std::size_t [_S_num_neg_double_factorials](#)< long double > = 999
- constexpr size_t [_S_num_zetam1](#) = 41
- constexpr long double [_S_zetam1](#) [[_S_num_zetam1](#)]

9.3.1 Function Documentation

9.3.1.1 template<typename [_Tp](#) > [__gnu_cxx::__airy_t](#)<[_Tp](#), [_Tp](#)> std::__detail::__airy ([_Tp](#) [_z](#))

Compute the Airy functions $Ai(x)$ and $Bi(x)$ and their first derivatives $Ai'(x)$ and $Bi'(x)$ respectively.

Parameters

_z	The argument of the Airy functions.
--------------------	-------------------------------------

Returns

A struct containing the Airy functions of the first and second kinds and their derivatives.

Definition at line 458 of file [sf_mod_bessel.tcc](#).

References [__cyl_bessel_ik\(\)](#), and [__cyl_bessel_jn\(\)](#).

Referenced by [__airy_ai\(\)](#), [__airy_bi\(\)](#), [__fock_airy\(\)](#), and [__poly_hermite_asymp\(\)](#).

9.3.1.2 `template<typename _Tp> std::complex<_Tp> std::__detail::__airy_ai (std::complex<_Tp> __z)`

Return the complex Airy Ai function.

Definition at line 2622 of file `sf_airy.tcc`.

References `__airy()`.

9.3.1.3 `template<typename _Tp> void std::__detail::__airy_arg (std::complex<_Tp> __num2d3, std::complex<_Tp> __zeta, std::complex<_Tp> &__argp, std::complex<_Tp> &__argm)`

Compute the arguments for the Airy function evaluations carefully to prevent premature overflow. Note that the major work here is in `safe_div`. A faster, but less safe implementation can be obtained without use of `safe_div`.

Parameters

in	<code>__num2d3</code>	$\nu^{-2/3}$ - output from <code>hankel_params</code>
in	<code>__zeta</code>	zeta in the uniform asymptotic expansions - output from <code>hankel_params</code>
out	<code>__argp</code>	$e^{+i2\pi/3}\nu^{2/3}\zeta$
out	<code>__argm</code>	$e^{-i2\pi/3}\nu^{2/3}\zeta$

Exceptions

<code>std::runtime_error</code>	if unable to compute Airy function arguments
---------------------------------	--

Definition at line 215 of file `sf_hankel.tcc`.

Referenced by `__hankel_uniform_outer()`.

9.3.1.4 `template<typename _Tp> std::complex<_Tp> std::__detail::__airy_bi (std::complex<_Tp> __z)`

Return the complex Airy Bi function.

Definition at line 2634 of file `sf_airy.tcc`.

References `__airy()`.

9.3.1.5 `template<typename _Tp> _Tp std::__detail::__assoc_laguerre (unsigned int __n, unsigned int __m, _Tp __x)`

This routine returns the associated Laguerre polynomial of order n , degree m : $L_n^m(x)$.

The associated Laguerre polynomial is defined for integral $\alpha = m$ by:

$$L_n^m(x) = (-1)^m \frac{d^m}{dx^m} L_{n+m}(x)$$

where the Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

Template Parameters

$_Tp$	The type of the parameter
--------	---------------------------

Parameters

$_n$	The order
$_m$	The degree
$_x$	The argument

Returns

The value of the associated Laguerre polynomial of order n , degree m , and argument x .

Definition at line 300 of file sf_laguerre.tcc.

Referenced by __hydrogen().

9.3.1.6 `template<typename _Tp> _Tp std::__detail::__assoc_legendre_p (unsigned int $_l$, unsigned int $_m$, $_Tp$ $_x$)`

Return the associated Legendre function by recursion on l and downward recursion on m .

The associated Legendre function is derived from the Legendre function $P_l(x)$ by the Rodrigues formula:

$$P_l^m(x) = (1 - x^2)^{m/2} \frac{d^m}{dx^m} P_l(x)$$

Parameters

$_l$	The order of the associated Legendre function. $l \geq 0$.
$_m$	The order of the associated Legendre function. $m \leq l$.
$_x$	The argument of the associated Legendre function.

Definition at line 177 of file sf_legendre.tcc.

References __poly_legendre_p().

9.3.1.7 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli (int $_n$)`

This returns Bernoulli number B_n .

Parameters

\leftrightarrow	the order n of the Bernoulli number.
n	

Returns

The Bernoulli number of order n .

Definition at line 1799 of file sf_gamma.tcc.

References `std::__detail::_Factorial_table<_Tp>::__n`.

9.3.1.8 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli_2n (int __n)`

This returns Bernoulli number B_{2n} at even integer arguments $2n$.

Parameters

\leftrightarrow	the half-order n of the Bernoulli number.
n	

Returns

The Bernoulli number of order $2n$.

Definition at line 1812 of file sf_gamma.tcc.

References `std::__detail::_Factorial_table<_Tp>::__n`.

9.3.1.9 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli_series (unsigned int __n)`

This returns Bernoulli numbers from a table or by summation for larger values.

Upward recursion is unstable.

Parameters

\leftrightarrow	the order n of the Bernoulli number.
n	

Returns

The Bernoulli number of order n .

Definition at line 1736 of file sf_gamma.tcc.

References std::__detail::_Factorial_table<_Tp>::_n.

9.3.1.10 `template<typename _Tp> _Tp std::__detail::__beta (_Tp __a, _Tp __b)`

Return the beta function $B(a, b)$.

The beta function is defined by

$$B(a, b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$$

Parameters

\leftrightarrow __a	The first argument of the beta function.
\leftrightarrow __b	The second argument of the beta function.

Returns

The beta function.

Definition at line 215 of file sf_beta.tcc.

References __beta_gamma(), and __beta_lgamma().

Referenced by __poly_jacobi(), __gnu_cxx::jacobi(), __gnu_cxx::jacobi(), __gnu_cxx::jacobi(), and std::__detail::__Airy<_Tp>::operator()().

9.3.1.11 `template<typename _Tp> _Tp std::__detail::__beta_gamma (_Tp __a, _Tp __b)`

Return the beta function: $B(a, b)$.

The beta function is defined by

$$B(a, b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$$

Parameters

\leftrightarrow __a	The first argument of the beta function.
\leftrightarrow __b	The second argument of the beta function.

Returns

The beta function.

Definition at line 77 of file sf_beta.tcc.

References `__gamma()`.

Referenced by `__beta()`.

9.3.1.12 `template<typename _Tp> _Tp std::__detail::__beta_inc (_Tp __a, _Tp __b, _Tp __x)`

Return the regularized incomplete beta function, $I_x(a, b)$, of arguments `a`, `b`, and `x`.

The regularized incomplete beta function is defined by:

$$I_x(a, b) = \frac{B_x(a, b)}{B(a, b)}$$

where

$$B_x(a, b) = \int_0^x t^{a-1} (1-t)^{b-1} dt$$

is the non-regularized beta function and $B(a, b)$ is the usual beta function.

Parameters

<code>__a</code>	The first parameter
<code>__b</code>	The second parameter
<code>__x</code>	The argument

Definition at line 311 of file sf_beta.tcc.

References `__ibeta_cont_frac()`, `__log_gamma()`, and `__log_gamma_sign()`.

Referenced by `__binomial_cdf()`, `__binomial_cdfc()`, `__fisher_f_cdf()`, `__fisher_f_cdfc()`, `__student_t_cdf()`, and `__student_t_cdfc()`.

9.3.1.13 `template<typename _Tp> _Tp std::__detail::__beta_lgamma (_Tp __a, _Tp __b)`

Return the beta function $B(a, b)$ using the log gamma functions.

The beta function is defined by

$$B(a, b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$$

Parameters

\leftrightarrow _a	The first argument of the beta function.
\leftrightarrow _b	The second argument of the beta function.

Returns

The beta function.

Definition at line 125 of file sf_beta.tcc.

References `__log_gamma()`, and `__log_gamma_sign()`.

Referenced by `__beta()`.

9.3.1.14 `template<typename _Tp> _Tp std::__detail::__beta_product (_Tp __a, _Tp __b)`

Return the beta function $B(x, y)$ using the product form.

The beta function is defined by

$$B(a, b) = \int_0^1 t^{a-1} (1-t)^{b-1} dt = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$$

Here, we employ the product form:

$$B(a, b) = \frac{a+b}{ab} \prod_{k=1}^{\infty} \frac{1 + (a+b)/k}{(1+a/k)(1+b/k)} = \frac{a+b}{ab} \prod_{k=1}^{\infty} \left[1 - \frac{ab}{(a+k)(b+k)} \right]$$

Parameters

\leftrightarrow _a	The first argument of the beta function.
\leftrightarrow _b	The second argument of the beta function.

Returns

The beta function.

Definition at line 179 of file sf_beta.tcc.

9.3.1.15 `template<typename _Tp> _Tp std::__detail::__bincoef (unsigned int __n, unsigned int __k)`

Return the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

Parameters

<code>_↵ _n</code>	The first argument of the binomial coefficient.
<code>_↵ _k</code>	The second argument of the binomial coefficient.

Returns

The binomial coefficient.

Definition at line 2542 of file `sf_gamma.tcc`.

References `std::__detail::_Factorial_table<_Tp>::__n`.

9.3.1.16 `template<typename _Tp> _Tp std::__detail::__bincoef (_Tp __nu, unsigned int __k)`

Return the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

Parameters

<code>__nu</code>	The real first argument of the binomial coefficient.
<code>__k</code>	The second argument of the binomial coefficient.

Returns

The binomial coefficient.

Definition at line 2587 of file `sf_gamma.tcc`.

References `__gamma()`, `__log_bincoef()`, `__log_bincoef_sign()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

9.3.1.17 `template<typename _Tp> _Tp std::__detail::__binomial_cdf (_Tp __p, unsigned int __n, unsigned int __k)`

Return the binomial cumulative distribution function.

The binomial cumulative distribution function is related to the incomplete beta function:

$$P(k|n, p) = I_p(k, n - k + 1)$$

Parameters

$\overleftarrow{_p}$	
$\overleftarrow{_n}$	
$\overleftarrow{_k}$	

Definition at line 560 of file sf_distributions.tcc.

References `__beta_inc()`.

9.3.1.18 `template<typename _Tp> _Tp std::__detail::__binomial_cdfc (_Tp __p, unsigned int __n, unsigned int __k)`

Return the complementary binomial cumulative distribution function.

The binomial cumulative distribution function is related to the incomplete beta function:

$$Q(k|n, p) = I_{1-p}(n - k + 1, k)$$

Parameters

$\overleftarrow{_p}$	
$\overleftarrow{_n}$	
$\overleftarrow{_k}$	

Definition at line 590 of file sf_distributions.tcc.

References `__beta_inc()`.

9.3.1.19 `template<typename _Tp> _Tp std::__detail::__binomial_pdf (_Tp __p, unsigned int __n, unsigned int __k)`

Return the binomial probability mass function.

The binomial cumulative distribution function is related to the incomplete beta function:

$$f(k|n, p) = \binom{n}{k} p^k (1-p)^{n-k}$$

Parameters

\leftrightarrow _p	
\leftrightarrow _n	
\leftrightarrow _k	

Definition at line 523 of file sf_distributions.tcc.

9.3.1.20 `template<typename _Sp, typename _Tp> _Tp std::__detail::__bose_einstein (_Sp __s, _Tp __x)`

Return the Bose-Einstein integral of integer or real order s and real argument x .

See also

https://en.wikipedia.org/wiki/Clausen_function
<http://dlmf.nist.gov/25.12.16>

$$G_s(x) = \frac{1}{\Gamma(s+1)} \int_0^\infty \frac{t^s}{e^{t-s} - 1} dt = Li_{s+1}(e^x)$$

Parameters

\leftrightarrow _s	The order $s \geq 0$.
\leftrightarrow _x	The real argument.

Returns

The real Fermi-Dirac cosine sum $G_s(x)$,

Definition at line 1435 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.21 `template<typename _Tp> _Tp std::__detail::__chebyshev_recur (unsigned int __n, _Tp __x, _Tp __C0, _Tp __C1)`

Return a Chebyshev polynomial of non-negative order n and real argument x by the recursion

$$C_n(x) = 2xC_{n-1} - C_{n-2}$$

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↵ _n</code>	The non-negative integral order
<code>↵ _x</code>	The real argument $-1 \leq x \leq +1$
<code>_C0</code>	The value of the zeroth-order Chebyshev polynomial at x
<code>_C1</code>	The value of the first-order Chebyshev polynomial at x

Definition at line 59 of file sf_chebyshev.tcc.

Referenced by `__chebyshev_t()`, `__chebyshev_u()`, `__chebyshev_v()`, and `__chebyshev_w()`.

9.3.1.22 `template<typename _Tp> _Tp std::__detail::__chebyshev_t(unsigned int __n, _Tp __x)`

Return the Chebyshev polynomial of the first kind $T_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the first kind is defined by:

$$T_n(x) = \cos(n\theta)$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↵ _n</code>	The non-negative integral order
<code>↵ _x</code>	The real argument $-1 \leq x \leq +1$

Definition at line 87 of file sf_chebyshev.tcc.

References `__chebyshev_recur()`.

9.3.1.23 `template<typename _Tp> _Tp std::__detail::__chebyshev_u(unsigned int __n, _Tp __x)`

Return the Chebyshev polynomial of the second kind $U_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the second kind is defined by:

$$U_n(x) = \frac{\sin[(n+1)\theta]}{\sin(\theta)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↔ _n</code>	The non-negative integral order
<code>↔ _x</code>	The real argument $-1 \leq x \leq +1$

Definition at line 116 of file `sf_chebyshev.tcc`.

References `__chebyshev_recur()`.

9.3.1.24 `template<typename _Tp> _Tp std::__detail::__chebyshev_v(unsigned int __n, _Tp __x)`

Return the Chebyshev polynomial of the third kind $V_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the third kind is defined by:

$$V_n(x) = \frac{\cos\left[\left(n + \frac{1}{2}\right)\theta\right]}{\cos\left(\frac{\theta}{2}\right)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↔ _n</code>	The non-negative integral order
<code>↔ _x</code>	The real argument $-1 \leq x \leq +1$

Definition at line 146 of file `sf_chebyshev.tcc`.

References `__chebyshev_recur()`.

9.3.1.25 `template<typename _Tp> _Tp std::__detail::__chebyshev_w (unsigned int __n, _Tp __x)`

Return the Chebyshev polynomial of the fourth kind $W_n(x)$ of non-negative order n and real argument x .

The Chebyshev polynomial of the fourth kind is defined by:

$$W_n(x) = \frac{\sin \left[\left(n + \frac{1}{2} \right) \theta \right]}{\sin \left(\frac{\theta}{2} \right)}$$

where $\theta = \arccos(x)$, $-1 \leq x \leq +1$.

Template Parameters

<code>_Tp</code>	The real type of the argument
------------------	-------------------------------

Parameters

<code>↔ _n</code>	The non-negative integral order
<code>↔ _x</code>	The real argument $-1 \leq x \leq +1$

Definition at line 176 of file `sf_chebyshev.tcc`.

References `__chebyshev_recur()`.

9.3.1.26 `template<typename _Tp> _Tp std::__detail::__chi_squared_pdf (_Tp __chi2, unsigned int __nu)`

Return the chi-squared propability function. This returns the probability that the observed chi-squared for a correct model is less than the value χ^2 .

The chi-squared propability function is related to the normalized lower incomplete gamma function:

$$P(\chi^2|\nu) = \Gamma_P\left(\frac{\nu}{2}, \frac{\chi^2}{2}\right)$$

Definition at line 75 of file `sf_distributions.tcc`.

References `__pgamma()`.

9.3.1.27 `template<typename _Tp> _Tp std::__detail::__chi_squared_pdfc (_Tp __chi2, unsigned int __nu)`

Return the complementary chi-squared propability function. This returns the probability that the observed chi-squared for a correct model is greater than the value χ^2 .

The complementary chi-squared propability function is related to the normalized upper incomplete gamma function:

$$Q(\chi^2|\nu) = \Gamma_Q\left(\frac{\nu}{2}, \frac{\chi^2}{2}\right)$$

Definition at line 99 of file `sf_distributions.tcc`.

References `__qgamma()`.

9.3.1.28 `template<typename _Tp> std::pair<_Tp, _Tp> std::__detail::__chshint (_Tp __x, _Tp & _Chi, _Tp & _Shi)`

This function returns the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals as a pair.

The hyperbolic cosine integral is defined by:

$$Chi(x) = \gamma_E + \log(x) + \int_0^x dt \frac{\cosh(t) - 1}{t}$$

The hyperbolic sine integral is defined by:

$$Shi(x) = \int_0^x dt \frac{\sinh(t)}{t}$$

Definition at line 166 of file sf_hypint.tcc.

References `__chshint_cont_frac()`, and `__chshint_series()`.

9.3.1.29 `template<typename _Tp> void std::__detail::__chshint_cont_frac (_Tp __t, _Tp & _Chi, _Tp & _Shi)`

This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by continued fraction for positive argument.

Definition at line 53 of file sf_hypint.tcc.

Referenced by `__chshint()`.

9.3.1.30 `template<typename _Tp> void std::__detail::__chshint_series (_Tp __t, _Tp & _Chi, _Tp & _Shi)`

This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by series summation for positive argument.

Definition at line 96 of file sf_hypint.tcc.

Referenced by `__chshint()`.

9.3.1.31 `template<typename _Tp> std::complex<_Tp> std::__detail::__clamp_0_m2pi (std::complex<_Tp> __w)`

Definition at line 72 of file sf_polylog.tcc.

Referenced by `__polylog_exp_int_neg()`, `__polylog_exp_int_pos()`, `__polylog_exp_real_neg()`, and `__polylog_exp_↔real_pos()`.

9.3.1.32 `template<typename _Tp> std::complex<_Tp> std::__detail::__clamp_pi (std::complex<_Tp> __w)`

Definition at line 59 of file sf_polylog.tcc.

Referenced by `__polylog_exp_int_neg()`, `__polylog_exp_int_pos()`, `__polylog_exp_real_neg()`, and `__polylog_exp_↔real_pos()`.

9.3.1.33 `template<typename _Tp> std::complex<_Tp> std::__detail::__clausen (unsigned int __m, std::complex<_Tp> __w)`

Return Clausen's function of integer order m and complex argument w . The notation and connection to polylog is from Wikipedia

Parameters

\leftrightarrow _m	The non-negative integral order.
\leftrightarrow _w	The complex argument.

Returns

The complex Clausen function.

Definition at line 1250 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.34 `template<typename _Tp> _Tp std::__detail::__clausen (unsigned int __m, _Tp __w)`

Return Clausen's function of integer order m and real argument w . The notation and connection to polylog is from Wikipedia

Parameters

\leftrightarrow _m	The integer order $m \geq 1$.
\leftrightarrow _w	The real argument.

Returns

The Clausen function.

Definition at line 1274 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.35 `template<typename _Tp> _Tp std::__detail::__clausen_c (unsigned int __m, std::complex<_Tp> __w)`

Return Clausen's cosine sum Cl_m for positive integer order m and complex argument w .

See also

https://en.wikipedia.org/wiki/Clausen_function

Parameters

\leftrightarrow _m	The integer order $m \geq 1$.
\leftrightarrow _w	The real argument.

Returns

The Clausen cosine sum $Cl_m(w)$,

Definition at line 1349 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.36 `template<typename _Tp> _Tp std::__detail::__clausen_c(unsigned int __m, _Tp __w)`

Return Clausen's cosine sum Cl_m for positive integer order m and real argument w .

See also

https://en.wikipedia.org/wiki/Clausen_function

Parameters

\leftrightarrow _m	The integer order $m \geq 1$.
\leftrightarrow _w	The real argument.

Returns

The real Clausen cosine sum $Cl_m(w)$,

Definition at line 1374 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.37 `template<typename _Tp> _Tp std::__detail::__clausen_s(unsigned int __m, std::complex<_Tp> __w)`

Return Clausen's sine sum Sl_m for positive integer order m and complex argument w .

See also

https://en.wikipedia.org/wiki/Clausen_function

Parameters

\leftrightarrow _m	The integer order m \geq 1.
\leftrightarrow _w	The complex argument.

Returns

The Clausen sine sum $Sl_m(w)$,

Definition at line 1299 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.38 `template<typename _Tp> _Tp std::__detail::__clausen_s (unsigned int _m, _Tp _w)`

Return Clausen's sine sum Sl_m for positive integer order m and real argument w.

See also

https://en.wikipedia.org/wiki/Clausen_function

Parameters

\leftrightarrow _m	The integer order m \geq 1.
\leftrightarrow _w	The complex argument.

Returns

The Clausen sine sum $Sl_m(w)$,

Definition at line 1324 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.39 `template<typename _Tp> _Tp std::__detail::__comp_ellint_1 (_Tp _k)`

Return the complete elliptic integral of the first kind $K(k)$ using the Carlson formulation.

The complete elliptic integral of the first kind is defined as

$$K(k) = F(k, \pi/2) = \int_0^{\pi/2} \frac{d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

where $F(k, \phi)$ is the incomplete elliptic integral of the first kind.

Parameters

\leftrightarrow _k	The modulus of the complete elliptic function.
-------------------------	--

Returns

The complete elliptic function of the first kind.

Definition at line 568 of file sf_ellint.tcc.

References `__comp_ellint_rf()`.

Referenced by `__ellint_1()`, `__ellnome_k()`, `__heuman_lambda()`, `__jacobi_zeta()`, `__theta_c()`, `__theta_d()`, `__theta_ \leftrightarrow n()`, and `__theta_s()`.

9.3.1.40 `template<typename _Tp> _Tp std::__detail::__comp_ellint_2 (_Tp _k)`

Return the complete elliptic integral of the second kind $E(k)$ using the Carlson formulation.

The complete elliptic integral of the second kind is defined as

$$E(k, \pi/2) = \int_0^{\pi/2} \sqrt{1 - k^2 \sin^2 \theta} d\theta$$

Parameters

\leftrightarrow _k	The modulus of the complete elliptic function.
-------------------------	--

Returns

The complete elliptic function of the second kind.

Definition at line 642 of file sf_ellint.tcc.

References `__ellint_rd()`, and `__ellint_rf()`.

Referenced by `__ellint_2()`.

9.3.1.41 `template<typename _Tp> _Tp std::__detail::__comp_ellint_3 (_Tp _k, _Tp _nu)`

Return the complete elliptic integral of the third kind $\Pi(k, \nu) = \Pi(k, \nu, \pi/2)$ using the Carlson formulation.

The complete elliptic integral of the third kind is defined as

$$\Pi(k, \nu) = \int_0^{\pi/2} \frac{d\theta}{(1 - \nu \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}}$$

Parameters

<code>__k</code>	The argument of the elliptic function.
<code>__nu</code>	The second argument of the elliptic function.

Returns

The complete elliptic function of the third kind.

Definition at line 732 of file `sf_ellint.tcc`.

References `__ellint_rf()`, and `__ellint_rj()`.

Referenced by `__ellint_3()`.

9.3.1.42 `template<typename _Tp> _Tp std::__detail::__comp_ellint_d (_Tp __k)`

Return the complete Legendre elliptic integral D.

Definition at line 840 of file `sf_ellint.tcc`.

References `__ellint_rd()`.

9.3.1.43 `template<typename _Tp> _Tp std::__detail::__comp_ellint_rf (_Tp __x, _Tp __y)`

Definition at line 238 of file `sf_ellint.tcc`.

Referenced by `__comp_ellint_1()`, and `__ellint_rf()`.

9.3.1.44 `template<typename _Tp> _Tp std::__detail::__comp_ellint_rg (_Tp __x, _Tp __y)`

Definition at line 349 of file `sf_ellint.tcc`.

Referenced by `__ellint_rg()`.

9.3.1.45 `template<typename _Tp> _Tp std::__detail::__conf_hyperg (_Tp __a, _Tp __c, _Tp __x)`

Return the confluent hypergeometric function ${}_1F_1(a; c; x)$.

Parameters

<code>__a</code>	The <i>numerator</i> parameter.
<code>__c</code>	The <i>denominator</i> parameter.
<code>__x</code>	The argument of the confluent hypergeometric function.

Returns

The confluent hypergeometric function.

Definition at line 281 of file sf_hyperg.tcc.

References `__conf_hyperg_luke()`, and `__conf_hyperg_series()`.

9.3.1.46 `template<typename _Tp> _Tp std::__detail::__conf_hyperg_lim (_Tp __c, _Tp __x)`

Return the confluent hypergeometric limit function ${}_0F_1(-; c; x)$.

Parameters

<code>__c</code>	The <i>denominator</i> parameter.
<code>__x</code>	The argument of the confluent hypergeometric limit function.

Returns

The confluent limit hypergeometric function.

Definition at line 109 of file sf_hyperg.tcc.

References `__conf_hyperg_lim_series()`.

9.3.1.47 `template<typename _Tp> _Tp std::__detail::__conf_hyperg_lim_series (_Tp __c, _Tp __x)`

This routine returns the confluent hypergeometric limit function by series expansion.

$${}_0F_1(-; c; x) = \Gamma(c) \sum_{n=0}^{\infty} \frac{1}{\Gamma(c+n)} \frac{x^n}{n!}$$

If a and b are integers and $a < 0$ and either $b > 0$ or $b < a$ then the series is a polynomial with a finite number of terms.

Parameters

<code>__c</code>	The "denominator" parameter.
<code>__x</code>	The argument of the confluent hypergeometric limit function.

Returns

The confluent hypergeometric limit function.

Definition at line 76 of file sf_hyperg.tcc.

Referenced by __conf_hyperg_lim().

9.3.1.48 template<typename _Tp> _Tp std::__detail::__conf_hyperg_luke (_Tp __a, _Tp __c, _Tp __xin)

Return the hypergeometric function ${}_1F_1(a; c; x)$ by an iterative procedure described in Luke, Algorithms for the Computation of Mathematical Functions.

Like the case of the ${}_2F_1$ rational approximations, these are probably guaranteed to converge for $x < 0$, barring gross numerical instability in the pre-asymptotic regime.

Definition at line 176 of file sf_hyperg.tcc.




Referenced by __conf_hyperg().

9.3.1.49 template<typename _Tp> _Tp std::__detail::__conf_hyperg_series (_Tp __a, _Tp __c, _Tp __x)

This routine returns the confluent hypergeometric function by series expansion.

$${}_1F_1(a; c; x) = \frac{\Gamma(c)}{\Gamma(a)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)}{\Gamma(c+n)} \frac{x^n}{n!}$$

Parameters

 __a	The "numerator" parameter.
 __c	The "denominator" parameter.
 __x	The argument of the confluent hypergeometric function.

Returns

The confluent hypergeometric function.

Definition at line 141 of file sf_hyperg.tcc.

Referenced by __conf_hyperg().

9.3.1.50 `template<typename _Tp> _Tp std::__detail::__cos_pi (_Tp __x)`

Return the reperiodized cosine of argument x:

$$\cos_{\pi}(x) = \cos(\pi x)$$

Definition at line 119 of file `sf_trig.tcc`.

References `__cos_pi()`.

Referenced by `__cyl_bessel_jn()`, `__cyl_bessel_jn_neg_arg()`, and `__log_double_factorial()`.

9.3.1.51 `template<typename _Tp> std::complex<_Tp> std::__detail::__cos_pi (std::complex<_Tp> __z)`

Return the reperiodized cosine of complex argument z: $(z) = (x) (y) - i (x) (y)$

Definition at line 239 of file `sf_trig.tcc`.

References `__sin_pi()`.

Referenced by `__cos_pi()`, `__cosh_pi()`, `__sin_pi()`, and `__sinh_pi()`.

9.3.1.52 `template<typename _Tp> _Tp std::__detail::__cosh_pi (_Tp __x)`

Return the reperiodized hyperbolic cosine of argument x:

$$\cosh_{\pi}(x) = \cosh(\pi x)$$

Definition at line 147 of file `sf_trig.tcc`.

References `__cosh_pi()`.

9.3.1.53 `template<typename _Tp> std::complex<_Tp> std::__detail::__cosh_pi (std::complex<_Tp> __z)`

Return the reperiodized hyperbolic cosine of complex argument z: $(z) = (z) = (x) (y) + i (x) (y)$

Definition at line 258 of file `sf_trig.tcc`.

References `__cos_pi()`, and `__sin_pi()`.

Referenced by `__cosh_pi()`.

9.3.1.54 `template<typename _Tp> _Tp std::__detail::__coshint (const _Tp __x)`

Return the hyperbolic cosine integral $Chi(x)$.

The hyperbolic cosine integral is given by

$$Chi(x) = (Ei(x) - E_1(x))/2 = (Ei(x) + Ei(-x))/2$$

Parameters

<code>_↔</code>	The argument of the hyperbolic cosine integral function.
<code>_x</code>	

Returns

The hyperbolic cosine integral.

Definition at line 561 of file sf_expint.tcc.

References `__expint_E1()`, and `__expint_Ei()`.

9.3.1.55 `template<typename _Tp> std::complex<_Tp> std::__detail::__cyl_bessel (std::complex<_Tp> __nu, std::complex<_Tp> __z)`

Return the complex cylindrical Bessel function.

Parameters

in	<code>__nu</code>	The order for which the cylindrical Bessel function is evaluated.
in	<code>__z</code>	The argument at which the cylindrical Bessel function is evaluated.

Returns

The complex cylindrical Bessel function.

Definition at line 1174 of file sf_hankel.tcc.

References `__hankel()`.

9.3.1.56 `template<typename _Tp> _Tp std::__detail::__cyl_bessel_i (_Tp __nu, _Tp __x)`

Return the regular modified Bessel function of order ν : $I_\nu(x)$.

The regular modified cylindrical Bessel function is:

$$I_\nu(x) = \sum_{k=0}^{\infty} \frac{(x/2)^{\nu+2k}}{k! \Gamma(\nu + k + 1)}$$

Parameters

<code>__nu</code>	The order of the regular modified Bessel function.
<code>__x</code>	The argument of the regular modified Bessel function.

Returns

The output regular modified Bessel function.

Definition at line 364 of file sf_mod_bessel.tcc.

References `__cyl_bessel_ij_series()`, and `__cyl_bessel_ik()`.

Referenced by `__rice_pdf()`.

9.3.1.57 `template<typename _Tp> _Tp std::__detail::__cyl_bessel_ij_series (_Tp __nu, _Tp __x, _Tp __sgn, unsigned int __max_iter)`

This routine returns the cylindrical Bessel functions of order ν : J_ν or I_ν by series expansion.

The modified cylindrical Bessel function is:

$$Z_\nu(x) = \sum_{k=0}^{\infty} \frac{\sigma^k (x/2)^{\nu+2k}}{k! \Gamma(\nu + k + 1)}$$

where $\sigma = +1$ or -1 for $Z = I$ or J respectively.

See Abramowitz & Stegun, 9.1.10 Abramowitz & Stegun, 9.6.7 (1) Handbook of Mathematical Functions, ed. Milton Abramowitz and Irene A. Stegun, Dover Publications, Equation 9.1.10 p. 360 and Equation 9.6.10 p. 375

Parameters

<code>__nu</code>	The order of the Bessel function.
<code>__x</code>	The argument of the Bessel function.
<code>__sgn</code>	The sign of the alternate terms -1 for the Bessel function of the first kind. +1 for the modified Bessel function of the first kind.
<code>__max_iter</code>	The maximum number of iterations for sum.

Returns

The output Bessel function.

Definition at line 413 of file sf_bessel.tcc.

References `__log_gamma()`.

Referenced by `__cyl_bessel_i()`, and `__cyl_bessel_j()`.

9.3.1.58 `template<typename _Tp> __gnu_cxx::__cyl_mod_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_ik (_Tp __nu, _Tp __x)`

Return the modified cylindrical Bessel functions and their derivatives of order ν by various means.

Parameters

<code>__nu</code>	The order of the Bessel functions.
<code>__x</code>	The argument of the Bessel functions.

Returns

A struct containing the modified cylindrical Bessel functions of the first and second kinds and their derivatives.

Definition at line 302 of file `sf_mod_bessel.tcc`.

References `__cyl_bessel_ik_asymp()`, `__cyl_bessel_ik_steel()`, and `__sin_pi()`.

Referenced by `__airy()`, `__cyl_bessel_i()`, `__cyl_bessel_k()`, and `__sph_bessel_ik()`.

9.3.1.59 `template<typename _Tp> __gnu_cxx::__cyl_mod_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_ik_asymp (_Tp __nu, _Tp __x)`

This routine computes the asymptotic modified cylindrical Bessel and functions of order ν : $I_\nu(x)$, $N_\nu(x)$. Use this for $x \gg \nu^2 + 1$.

References: (1) Handbook of Mathematical Functions, ed. Milton Abramowitz and Irene A. Stegun, Dover Publications, Section 9 p. 364, Equations 9.2.5-9.2.10

Parameters

<code>__nu</code>	The order of the Bessel functions.
<code>__x</code>	The argument of the Bessel functions.

Returns

A struct containing the modified cylindrical Bessel functions of the first and second kinds and their derivatives.

Definition at line 79 of file `sf_mod_bessel.tcc`.

Referenced by `__cyl_bessel_ik()`, and `__cyl_bessel_ik_steel()`.

9.3.1.60 `template<typename _Tp> __gnu_cxx::__cyl_mod_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_ik_steel (_Tp __nu, _Tp __x)`

Compute the modified Bessel functions $I_\nu(x)$ and $K_\nu(x)$ and their first derivatives $I'_\nu(x)$ and $K'_\nu(x)$ respectively. These four functions are computed together for numerical stability.

Parameters

<code>__nu</code>	The order of the Bessel functions.
<code>__x</code>	The argument of the Bessel functions.

Returns

A struct containing the modified cylindrical Bessel functions of the first and second kinds and their derivatives.

Definition at line 145 of file sf_mod_bessel.tcc.

References `__cyl_bessel_ik_asymp()`, and `__gamma_temme()`.

Referenced by `__cyl_bessel_ik()`.

9.3.1.61 `template<typename _Tp> _Tp std::__detail::__cyl_bessel_j(_Tp __nu, _Tp __x)`

Return the Bessel function of order ν : $J_\nu(x)$.

The cylindrical Bessel function is:

$$J_\nu(x) = \sum_{k=0}^{\infty} \frac{(-1)^k (x/2)^{\nu+2k}}{k! \Gamma(\nu + k + 1)}$$

Parameters

<code>__nu</code>	The order of the Bessel function.
<code>__x</code>	The argument of the Bessel function.

Returns

The output Bessel function.

Definition at line 559 of file sf_bessel.tcc.

References `__cyl_bessel_ij_series()`, and `__cyl_bessel_jn()`.

9.3.1.62 `template<typename _Tp> __gnu_cxx::__cyl_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_jn(_Tp __nu, _Tp __x)`

Return the cylindrical Bessel functions and their derivatives of order ν by various means.

Definition at line 452 of file sf_bessel.tcc.

References `__cos_pi()`, `__cyl_bessel_jn_asymp()`, `__cyl_bessel_jn_steel()`, and `__sin_pi()`.

Referenced by `__airy()`, `__cyl_bessel_j()`, `__cyl_bessel_jn_neg_arg()`, `__cyl_hankel_1()`, `__cyl_hankel_2()`, `__cyl_neumann_n()`, and `__sph_bessel_jn()`.

9.3.1.63 `template<typename _Tp> __gnu_cxx::__cyl_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_jn_asymp(_Tp __nu, _Tp __x)`

This routine computes the asymptotic cylindrical Bessel and Neumann functions of order ν : $J_\nu(x)$, $N_\nu(x)$. Use this for $x \gg \nu^2 + 1$.

References: (1) Handbook of Mathematical Functions, ed. Milton Abramowitz and Irene A. Stegun, Dover Publications, Section 9 p. 364, Equations 9.2.5-9.2.10

Parameters

<code>__nu</code>	The order of the Bessel functions.
<code>__x</code>	The argument of the Bessel functions.

Returns

A struct containing the cylindrical Bessel functions of the first and second kinds and their derivatives.

Definition at line 79 of file sf_bessel.tcc.

Referenced by `__cyl_bessel_jn()`, and `__cyl_bessel_jn_stepped()`.

```
9.3.1.64 template<typename _Tp> __gnu_cxx::__cyl_bessel_t<_Tp, _Tp, std::complex<_Tp>> >
        std::__detail::__cyl_bessel_jn_neg_arg ( _Tp __nu, _Tp __x )
```

Return the cylindrical Bessel functions and their derivatives of order ν and argument $x < 0$.

Definition at line 518 of file sf_bessel.tcc.

References `__cos_pi()`, `__cyl_bessel_jn()`, and `__polar_pi()`.

Referenced by `__cyl_hankel_1()`, `__cyl_hankel_2()`, and `__sph_bessel_jn_neg_arg()`.

```
9.3.1.65 template<typename _Tp> __gnu_cxx::__cyl_bessel_t<_Tp, _Tp, _Tp> std::__detail::__cyl_bessel_jn_stepped ( _Tp __nu,
        _Tp __x )
```

Compute the Bessel $J_\nu(x)$ and Neumann $N_\nu(x)$ functions and their first derivatives $J'_\nu(x)$ and $N'_\nu(x)$ respectively. These four functions are computed together for numerical stability.

Parameters

<code>__nu</code>	The order of the Bessel functions.
<code>__x</code>	The argument of the Bessel functions.

Returns

A struct containing the cylindrical Bessel functions of the first and second kinds and their derivatives.

Definition at line 199 of file sf_bessel.tcc.

References `__cyl_bessel_jn_asymp()`, and `__gamma_temme()`.

Referenced by `__cyl_bessel_jn()`.

9.3.1.66 `template<typename _Tp > _Tp std::__detail::__cyl_bessel_k (_Tp __nu, _Tp __x)`

Return the irregular modified Bessel function $K_\nu(x)$ of order ν .

The irregular modified Bessel function is defined by:

$$K_\nu(x) = \frac{\pi}{2} \frac{I_{-\nu}(x) - I_\nu(x)}{\sin \nu\pi}$$

where for integral $\nu = n$ a limit is taken: $\lim_{\nu \rightarrow n}$. For negative argument we have simply:

$$K_{-\nu}(x) = K_\nu(x)$$

Parameters

<code>__nu</code>	The order of the irregular modified Bessel function.
<code>__x</code>	The argument of the irregular modified Bessel function.

Returns

The output irregular modified Bessel function.

Definition at line 398 of file `sf_mod_bessel.tcc`.

References `__cyl_bessel_ik()`.

9.3.1.67 `template<typename _Tp > std::complex<_Tp> std::__detail::__cyl_hankel_1 (_Tp __nu, _Tp __x)`

Return the cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$.

The cylindrical Hankel function of the first kind is defined by:

$$H_\nu^{(1)}(x) = J_\nu(x) + iN_\nu(x)$$

Parameters

<code>__nu</code>	The order of the spherical Neumann function.
<code>__x</code>	The argument of the spherical Neumann function.

Returns

The output spherical Neumann function.

Definition at line 616 of file `sf_bessel.tcc`.

References `__cyl_bessel_jn()`, `__cyl_bessel_jn_neg_arg()`, and `__polar_pi()`.

9.3.1.68 `template<typename _Tp > std::complex<_Tp> std::__detail::__cyl_hankel_1 (std::complex<_Tp > __nu, std::complex<_Tp > __z)`

Return the complex cylindrical Hankel function of the first kind.

Parameters

in	<code>__nu</code>	The order for which the cylindrical Hankel function of the first kind is evaluated.
in	<code>__z</code>	The argument at which the cylindrical Hankel function of the first kind is evaluated.

Returns

The complex cylindrical Hankel function of the first kind.

Definition at line 1140 of file `sf_hankel.tcc`.

References `__hankel()`.

9.3.1.69 `template<typename _Tp > std::complex<_Tp> std::__detail::__cyl_hankel_2 (_Tp __nu, _Tp __x)`

Return the cylindrical Hankel function of the second kind $H_n^{(2)}u(x)$.

The cylindrical Hankel function of the second kind is defined by:

$$H_\nu^{(2)}(x) = J_\nu(x) - iN_\nu(x)$$

Parameters

<code>__nu</code>	The order of the spherical Neumann function.
<code>__x</code>	The argument of the spherical Neumann function.

Returns

The output spherical Neumann function.

Definition at line 654 of file `sf_bessel.tcc`.

References `__cyl_bessel_jn()`, `__cyl_bessel_jn_neg_arg()`, and `__polar_pi()`.

9.3.1.70 `template<typename _Tp > std::complex<_Tp> std::__detail::__cyl_hankel_2 (std::complex<_Tp > __nu, std::complex<_Tp > __z)`

Return the complex cylindrical Hankel function of the second kind.

Parameters

in	<code>__nu</code>	The order for which the cylindrical Hankel function of the second kind is evaluated.
in	<code>__z</code>	The argument at which the cylindrical Hankel function of the second kind is evaluated.

Returns

The complex cylindrical Hankel function of the second kind.

Definition at line 1157 of file `sf_hankel.tcc`.

References `__hankel()`.

9.3.1.71 `template<typename _Tp > std::complex<_Tp> std::__detail::__cyl_neumann (std::complex<_Tp> __nu,
std::complex<_Tp> __z)`

Return the complex cylindrical Neumann function.

Parameters

in	<code>__nu</code>	The order for which the cylindrical Neumann function is evaluated.
in	<code>__z</code>	The argument at which the cylindrical Neumann function is evaluated.

Returns

The complex cylindrical Neumann function.

Definition at line 1191 of file `sf_hankel.tcc`.

References `__hankel()`.

9.3.1.72 `template<typename _Tp > _Tp std::__detail::__cyl_neumann_n (_Tp __nu, _Tp __x)`

Return the Neumann function of order ν : $N_\nu(x)$.

The Neumann function is defined by:

$$N_\nu(x) = \frac{J_\nu(x) \cos \nu\pi - J_{-\nu}(x)}{\sin \nu\pi}$$

where for integral $\nu = n$ a limit is taken: $\lim_{\nu \rightarrow n}$.

Parameters

<code>__nu</code>	The order of the Neumann function.
<code>__x</code>	The argument of the Neumann function.

Returns

The output Neumann function.

Definition at line 590 of file sf_bessel.tcc.

References `__cyl_bessel_jn()`.

9.3.1.73 `template<typename _Tp> _Tp std::__detail::__dawson (_Tp __x)`

Return the Dawson integral, $F(x)$, for real argument x .

The Dawson integral is defined by:

$$F(x) = e^{-x^2} \int_0^x e^{y^2} dy$$

and it's derivative is:

$$F'(x) = 1 - 2xF(x)$$

Parameters

<code>__x</code>	The argument $-inf < x < inf$.
------------------	---------------------------------

Definition at line 235 of file sf_dawson.tcc.

References `__dawson_cont_frac()`, and `__dawson_series()`.

9.3.1.74 `template<typename _Tp> _Tp std::__detail::__dawson_cont_frac (_Tp __x)`

Compute the Dawson integral using a sampling theorem representation.

Todo this needs some compile-time construction!

Definition at line 73 of file sf_dawson.tcc.

Referenced by `__dawson()`.

9.3.1.75 `template<typename _Tp> _Tp std::__detail::__dawson_series (_Tp __x)`

Compute the Dawson integral using the series expansion.

Definition at line 49 of file sf_dawson.tcc.

Referenced by `__dawson()`.

9.3.1.76 `template<typename _Tp> void std::__detail::__debye_region (std::complex< _Tp> __alpha, int & __indexr, char & __aorb)`

Compute the Debye region in the complex plane.

Definition at line 54 of file sf_hankel.tcc.

Referenced by `__hankel()`.

9.3.1.77 `template<typename _Tp> _Tp std::__detail::__dilog (_Tp __x)`

Compute the dilogarithm function $Li_2(x)$ by summation for $x \leq 1$.

The Riemann zeta function is defined by:

$$Li_2(x) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } s > 1$$

For $|x|$ near 1 use the reflection formulae:

$$Li_2(-x) + Li_2(1-x) = \frac{\pi^2}{6} - \ln(x) \ln(1-x)$$

$$Li_2(-x) - Li_2(1-x) - \frac{1}{2} Li_2(1-x^2) = -\frac{\pi^2}{12} - \ln(x) \ln(1-x)$$

For $x < 1$ use the reflection formula:

$$Li_2(1-x) - Li_2\left(1 - \frac{1}{1-x}\right) - \frac{1}{2} (\ln(x))^2$$

Definition at line 196 of file sf_zeta.tcc.

9.3.1.78 `template<typename _Tp> _Tp std::__detail::__dirichlet_beta (std::complex< _Tp> __w)`

Return the Dirichlet beta function. Currently, w must be real (complex type but negligible imaginary part.) Otherwise `std::domain_error` is thrown.

Parameters

<code>__w</code>	The complex (but on-real-axis) argument.
------------------	--

Returns

The Dirichlet Beta function of real argument.

Exceptions

<code>std::domain_error</code>	if the argument has a significant imaginary part.
--------------------------------	---

Definition at line 1195 of file sf_polylog.tcc.

References `__polylog()`.

9.3.1.79 `template<typename _Tp > _Tp std::__detail::__dirichlet_beta (_Tp __w)`

Return the Dirichlet beta function for real argument.

Parameters

<code>__w</code>	The real argument.
------------------	--------------------

Returns

The Dirichlet Beta function of real argument.

Definition at line 1214 of file sf_polylog.tcc.

References `__polylog()`.

9.3.1.80 `template<typename _Tp > std::complex<_Tp> std::__detail::__dirichlet_eta (std::complex<_Tp > __w)`

Return the Dirichlet eta function. Currently, `w` must be real (complex type but negligible imaginary part.) Otherwise `std::domain_error` is thrown.

Parameters

<code>__w</code>	The complex (but on-real-axis) argument.
------------------	--

Returns

The complex Dirichlet eta function.

Exceptions

<code>std::domain_error</code>	if the argument has a significant imaginary part.
--------------------------------	---

Definition at line 1158 of file sf_polylog.tcc.

References `__polylog()`.

Referenced by `__dirichlet_lambda()`.

9.3.1.81 `template<typename _Tp > _Tp std::__detail::__dirichlet_eta (_Tp __w)`

Return the Dirichlet eta function for real argument.

Parameters

<code>__w</code>	The real argument.
------------------	--------------------

Returns

The Dirichlet eta function.

Definition at line 1176 of file `sf_polylog.tcc`.

References `__polylog()`.

9.3.1.82 `template<typename _Tp > _Tp std::__detail::__dirichlet_lambda (_Tp __w)`

Return the Dirichlet lambda function for real argument.

Parameters

<code>__w</code>	The real argument.
------------------	--------------------

Returns

The Dirichlet lambda function.

Definition at line 1231 of file `sf_polylog.tcc`.

References `__dirichlet_eta()`, and `__riemann_zeta()`.

9.3.1.83 `template<typename _Tp > _GLIBCXX14_CONSTEXPR _Tp std::__detail::__double_factorial (int __n)`

Return the double factorial of the integer `n`.

The double factorial is defined for integral `n` by:

$$n!! = 135...(n-2)n, \text{ odd } n!! = 246...(n-2)n, \text{ even } -1!! = 10!! = 1$$

The double factorial is defined for odd negative integers in the obvious way:

$$(-2m-1)!! = 1/(1(-1)(-3)...(-2m+1)(-2m-1)) = \frac{(-1)^m}{(2m-1)!!}$$

for $n = -2m - 1$.

Definition at line 1673 of file `sf_gamma.tcc`.

References `std::__detail::_Factorial_table< _Tp >::__factorial`, `__log_double_factorial()`, `std::__detail::_Factorial_table< _Tp >::__n`, `_S_double_factorial_table`, and `_S_neg_double_factorial_table`.

9.3.1.84 `template<typename _Tp> _Tp std::__detail::__ellint_1 (_Tp __k, _Tp __phi)`

Return the incomplete elliptic integral of the first kind $F(k, \phi)$ using the Carlson formulation.

The incomplete elliptic integral of the first kind is defined as

$$F(k, \phi) = \int_0^\phi \frac{d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}$$

Parameters

<code>__k</code>	The argument of the elliptic function.
<code>__phi</code>	The integral limit argument of the elliptic function.

Returns

The elliptic function of the first kind.

Definition at line 597 of file `sf_ellint.tcc`.

References `__comp_ellint_1()`, and `__ellint_rf()`.

Referenced by `__heuman_lambda()`.

9.3.1.85 `template<typename _Tp> _Tp std::__detail::__ellint_2 (_Tp __k, _Tp __phi)`

Return the incomplete elliptic integral of the second kind $E(k, \phi)$ using the Carlson formulation.

The incomplete elliptic integral of the second kind is defined as

$$E(k, \phi) = \int_0^\phi \sqrt{1 - k^2 \sin^2 \theta}$$

Parameters

<code>__k</code>	The argument of the elliptic function.
<code>__phi</code>	The integral limit argument of the elliptic function.

Returns

The elliptic function of the second kind.

Definition at line 678 of file `sf_ellint.tcc`.

References `__comp_ellint_2()`, `__ellint_rd()`, and `__ellint_rf()`.

9.3.1.86 `template<typename _Tp > _Tp std::__detail::__ellint_3 (_Tp __k, _Tp __nu, _Tp __phi)`

Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ using the Carlson formulation.

The incomplete elliptic integral of the third kind is defined as

$$\Pi(k, \nu, \phi) = \int_0^\phi \frac{d\theta}{(1 - \nu \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}}$$

Parameters

<code>__k</code>	The argument of the elliptic function.
<code>__nu</code>	The second argument of the elliptic function.
<code>__phi</code>	The integral limit argument of the elliptic function.

Returns

The elliptic function of the third kind.

Definition at line 773 of file `sf_ellint.tcc`.

References `__comp_ellint_3()`, `__ellint_rf()`, and `__ellint_rj()`.

9.3.1.87 `template<typename _Tp > _Tp std::__detail::__ellint_cel (_Tp __k_c, _Tp __p, _Tp __a, _Tp __b)`

Return the Bulirsch complete elliptic integrals.

Definition at line 928 of file `sf_ellint.tcc`.

References `__ellint_rf()`, and `__ellint_rj()`.

9.3.1.88 `template<typename _Tp > _Tp std::__detail::__ellint_d (_Tp __k, _Tp __phi)`

Return the Legendre elliptic integral D.

Definition at line 814 of file `sf_ellint.tcc`.

References `__ellint_rd()`.

9.3.1.89 `template<typename _Tp > _Tp std::__detail::__ellint_el1 (_Tp __x, _Tp __k_c)`

Return the Bulirsch elliptic integrals of the first kind.

Definition at line 856 of file `sf_ellint.tcc`.

References `__ellint_rf()`.

9.3.1.90 `template<typename _Tp> _Tp std::__detail::__ellint_el2 (_Tp __x, _Tp __k_c, _Tp __a, _Tp __b)`

Return the Bulirsch elliptic integrals of the second kind.

Definition at line 877 of file sf_ellint.tcc.

References `__ellint_rd()`, and `__ellint_rf()`.

9.3.1.91 `template<typename _Tp> _Tp std::__detail::__ellint_el3 (_Tp __x, _Tp __k_c, _Tp __p)`

Return the Bulirsch elliptic integrals of the third kind.

Definition at line 902 of file sf_ellint.tcc.

References `__ellint_rf()`, and `__ellint_rj()`.

9.3.1.92 `template<typename _Tp> _Tp std::__detail::__ellint_rc (_Tp __x, _Tp __y)`

Return the Carlson elliptic function $R_C(x, y) = R_F(x, y, y)$ where $R_F(x, y, z)$ is the Carlson elliptic function of the first kind.

The Carlson elliptic function is defined by:

$$R_C(x, y) = \frac{1}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first argument.
<code>__y</code>	The second argument.

Returns

The Carlson elliptic function.

Definition at line 84 of file sf_ellint.tcc.

Referenced by `__ellint_rf()`, and `__ellint_rj()`.

9.3.1.93 `template<typename _Tp> _Tp std::__detail::__ellint_rd (_Tp __x, _Tp __y, _Tp __z)`

Return the Carlson elliptic function of the second kind $R_D(x, y, z) = R_J(x, y, z, z)$ where $R_J(x, y, z, p)$ is the Carlson elliptic function of the third kind.

The Carlson elliptic function of the second kind is defined by:

$$R_D(x, y, z) = \frac{3}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{3/2}}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first of two symmetric arguments.
<code>__y</code>	The second of two symmetric arguments.
<code>__z</code>	The third argument.

Returns

The Carlson elliptic function of the second kind.

Definition at line 166 of file `sf_ellint.tcc`.

Referenced by `__comp_ellint_2()`, `__comp_ellint_d()`, `__ellint_2()`, `__ellint_d()`, `__ellint_el2()`, `__ellint_rg()`, and `__ellint_rj()`.

9.3.1.94 `template<typename _Tp> _Tp std::__detail::__ellint_rf (_Tp __x, _Tp __y, _Tp __z)`

Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind.

The Carlson elliptic function of the first kind is defined by:

$$R_F(x, y, z) = \frac{1}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{1/2}}$$

Parameters

$_x$	The first of three symmetric arguments.
$_y$	The second of three symmetric arguments.
$_z$	The third of three symmetric arguments.

Returns

The Carlson elliptic function of the first kind.

Definition at line 280 of file sf_ellint.tcc.

References `__comp_ellint_rf()`, and `__ellint_rc()`.

Referenced by `__comp_ellint_2()`, `__comp_ellint_3()`, `__ellint_1()`, `__ellint_2()`, `__ellint_3()`, `__ellint_cel()`, `__ellint_el1()`, `__ellint_el2()`, `__ellint_el3()`, and `__heuman_lambda()`.

9.3.1.95 `template<typename _Tp> _Tp std::__detail::__ellint_rg (_Tp __x, _Tp __y, _Tp __z)`

Return the symmetric Carlson elliptic function of the second kind $R_G(x, y, z)$.

The Carlson symmetric elliptic function of the second kind is defined by:

$$R_G(x, y, z) = \frac{1}{4} \int_0^\infty dt [(t+x)(t+y)(t+z)]^{-1/2} \left(\frac{x}{t+x} + \frac{y}{t+y} + \frac{z}{t+z} \right)$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

$_x$	The first of three symmetric arguments.
$_y$	The second of three symmetric arguments.
$_z$	The third of three symmetric arguments.

Returns

The Carlson symmetric elliptic function of the second kind.

Definition at line 411 of file sf_ellint.tcc.

References `__comp_ellint_rg()`, and `__ellint_rd()`.

9.3.1.96 `template<typename _Tp> _Tp std::__detail::__ellint_rj (_Tp __x, _Tp __y, _Tp __z, _Tp __p)`

Return the Carlson elliptic function $R_J(x, y, z, p)$ of the third kind.

The Carlson elliptic function of the third kind is defined by:

$$R_J(x, y, z, p) = \frac{3}{2} \int_0^\infty \frac{dt}{(t+x)^{1/2}(t+y)^{1/2}(t+z)^{1/2}(t+p)}$$

Based on Carlson's algorithms:

- B. C. Carlson Numer. Math. 33, 1 (1979)
- B. C. Carlson, Special Functions of Applied Mathematics (1977)
- Numerical Recipes in C, 2nd ed, pp. 261-269, by Press, Teukolsky, Vetterling, Flannery (1992)

Parameters

<code>__x</code>	The first of three symmetric arguments.
<code>__y</code>	The second of three symmetric arguments.
<code>__z</code>	The third of three symmetric arguments.
<code>__p</code>	The fourth argument.

Returns

The Carlson elliptic function of the fourth kind.

Definition at line 459 of file sf_ellint.tcc.

References `__ellint_rc()`, and `__ellint_rd()`.

Referenced by `__comp_ellint_3()`, `__ellint_3()`, `__ellint_cel()`, `__ellint_el3()`, `__heuman_lambda()`, and `__jacobi_zeta()`.

9.3.1.97 `template<typename _Tp> _Tp std::__detail::__ellnome (_Tp __k)`

Return the elliptic nome given the modulus k .

Definition at line 294 of file `sf_theta.tcc`.

References `__ellnome_k()`, and `__ellnome_series()`.

Referenced by `__theta_c()`, `__theta_d()`, `__theta_n()`, and `__theta_s()`.

9.3.1.98 `template<typename _Tp> _Tp std::__detail::__ellnome_k (_Tp __k)`

Use the arithmetic-geometric mean to calculate the elliptic nome given the , k .

Definition at line 280 of file `sf_theta.tcc`.

References `__comp_ellint_1()`.

Referenced by `__ellnome()`.

9.3.1.99 `template<typename _Tp> _Tp std::__detail::__ellnome_series (_Tp __k)`

Use MacLaurin series to calculate the elliptic nome given the , k .

Definition at line 264 of file `sf_theta.tcc`.

Referenced by `__ellnome()`.

9.3.1.100 `template<typename _Tp> _Tp std::__detail::__expint (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

<code>__n</code>	The order of the exponential integral function.
<code>__x</code>	The argument of the exponential integral function.

Returns

The exponential integral.

Todo Study arbitrary switch to large- n $E_n(x)$.

Todo Find a good asymptotic switch point in $E_n(x)$.

Definition at line 476 of file sf_expint.tcc.

References `__expint_E1()`, `__expint_En_asymp()`, `__expint_En_cont_frac()`, `__expint_En_large_n()`, and `__expint_↵
En_series()`.

Referenced by `__logint()`.

9.3.1.101 `template<typename _Tp> _Tp std::__detail::__expint (_Tp __x)`

Return the exponential integral $Ei(x)$.

The exponential integral is given by

$$Ei(x) = - \int_{-x}^{\infty} \frac{e^t}{t} dt$$

Parameters

<code>↵ __x</code>	The argument of the exponential integral function.
------------------------	--

Returns

The exponential integral.

Definition at line 517 of file sf_expint.tcc.

References `__expint_Ei()`.

9.3.1.102 `template<typename _Tp> _Tp std::__detail::__expint_E1 (_Tp __x)`

Return the exponential integral $E_1(x)$.

The exponential integral is given by

$$E_1(x) = \int_1^{\infty} \frac{e^{-xt}}{t} dt$$

Parameters

\leftrightarrow	The argument of the exponential integral function.
x	

Returns

The exponential integral.

Todo Find a good asymptotic switch point in $E_1(x)$.

Todo Find a good asymptotic switch point in $E_1(x)$.

Definition at line 381 of file sf_expint.tcc.

References `__expint_E1_asymp()`, `__expint_E1_series()`, `__expint_Ei()`, and `__expint_En_cont_frac()`.

Referenced by `__coshint()`, `__expint()`, `__expint_Ei()`, `__expint_En_recursion()`, and `__sinhint()`.

9.3.1.103 `template<typename _Tp> _Tp std::__detail::__expint_E1_asymp (_Tp __x)`

Return the exponential integral $E_1(x)$ by asymptotic expansion.

The exponential integral is given by

$$E_1(x) = \int_1^\infty \frac{e^{-xt}}{t} dt$$

Parameters

\leftrightarrow	The argument of the exponential integral function.
x	

Returns

The exponential integral.

Definition at line 114 of file sf_expint.tcc.

Referenced by `__expint_E1()`.

9.3.1.104 `template<typename _Tp> _Tp std::__detail::__expint_E1_series (_Tp __x)`

Return the exponential integral $E_1(x)$ by series summation. This should be good for $x < 1$.

The exponential integral is given by

$$E_1(x) = \int_1^\infty \frac{e^{-xt}}{t} dt$$

Parameters

<code>_↔</code> <code>_X</code>	The argument of the exponential integral function.
------------------------------------	--

Returns

The exponential integral.

Definition at line 76 of file sf_expint.tcc.

Referenced by `__expint_E1()`.

9.3.1.105 `template<typename _Tp> _Tp std::__detail::__expint_Ei (_Tp __x)`

Return the exponential integral $Ei(x)$.

The exponential integral is given by

$$Ei(x) = - \int_{-x}^{\infty} \frac{e^t}{t} dt$$

Parameters

<code>_↔</code> <code>_X</code>	The argument of the exponential integral function.
------------------------------------	--

Returns

The exponential integral.

Definition at line 356 of file sf_expint.tcc.

References `__expint_E1()`, `__expint_Ei_asyp()`, and `__expint_Ei_series()`.

Referenced by `__coshint()`, `__expint()`, `__expint_E1()`, and `__sinhint()`.

9.3.1.106 `template<typename _Tp> _Tp std::__detail::__expint_Ei_asyp (_Tp __x)`

Return the exponential integral $Ei(x)$ by asymptotic expansion.

The exponential integral is given by

$$Ei(x) = - \int_{-x}^{\infty} \frac{e^t}{t} dt$$

Parameters

\leftrightarrow	The argument of the exponential integral function.
x	

Returns

The exponential integral.

Definition at line 322 of file sf_expint.tcc.

Referenced by __expint_Ei().

9.3.1.107 `template<typename _Tp> _Tp std::__detail::__expint_Ei_series (_Tp __x)`

Return the exponential integral $Ei(x)$ by series summation.

The exponential integral is given by

$$Ei(x) = - \int_{-x}^{\infty} \frac{e^t}{t} dt$$

Parameters

\leftrightarrow	The argument of the exponential integral function.
x	

Returns

The exponential integral.

Definition at line 289 of file sf_expint.tcc.

Referenced by __expint_Ei().

9.3.1.108 `template<typename _Tp> _Tp std::__detail::__expint_En_asymp (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ for large argument.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

\leftrightarrow _n	The order of the exponential integral function.
\leftrightarrow _x	The argument of the exponential integral function.

Returns

The exponential integral.

Definition at line 410 of file sf_expint.tcc.

Referenced by __expint().

9.3.1.109 `template<typename _Tp> _Tp std::__detail::__expint_En_cont_frac (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by continued fractions.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

\leftrightarrow _n	The order of the exponential integral function.
\leftrightarrow _x	The argument of the exponential integral function.

Returns

The exponential integral.

Definition at line 198 of file sf_expint.tcc.

Referenced by __expint(), and __expint_E1().

9.3.1.110 `template<typename _Tp> _Tp std::__detail::__expint_En_large_n (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ for large order.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

\leftrightarrow _n	The order of the exponential integral function.
\leftrightarrow _x	The argument of the exponential integral function.

Returns

The exponential integral.

Definition at line 442 of file sf_expint.tcc.

Referenced by __expint().

9.3.1.111 `template<typename _Tp> _Tp std::__detail::__expint_En_recursion (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by recursion. Use upward recursion for $x < n$ and downward recursion (Miller's algorithm) otherwise.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

\leftrightarrow _n	The order of the exponential integral function.
\leftrightarrow _x	The argument of the exponential integral function.

Returns

The exponential integral.

Todo Find a principled starting number for the $E_n(x)$ downward recursion.

Definition at line 244 of file sf_expint.tcc.

References __expint_E1().

9.3.1.112 `template<typename _Tp> _Tp std::__detail::__expint_En_series (unsigned int __n, _Tp __x)`

Return the exponential integral $E_n(x)$ by series summation.

The exponential integral is given by

$$E_n(x) = \int_1^{\infty} \frac{e^{-xt}}{t^n} dt$$

Parameters

\leftrightarrow _n	The order of the exponential integral function.
\leftrightarrow _x	The argument of the exponential integral function.

Returns

The exponential integral.

Definition at line 150 of file sf_expint.tcc.

References `__psi()`.

Referenced by `__expint()`.

9.3.1.113 `template<typename _Tp> _Tp std::__detail::__exponential_cdf (_Tp __lambda, _Tp __x)`

Return the exponential cumulative probability density function.

The formula for the exponential cumulative probability density function is

$$F(x|\lambda) = 1 - e^{-\lambda x} \text{ for } x \geq 0$$

Definition at line 328 of file sf_distributions.tcc.

9.3.1.114 `template<typename _Tp> _Tp std::__detail::__exponential_cdfc (_Tp __lambda, _Tp __x)`

Return the complement of the exponential cumulative probability density function.

The formula for the complement of the exponential cumulative probability density function is

$$F(x|\lambda) = e^{-\lambda x} \text{ for } x \geq 0$$

Definition at line 350 of file sf_distributions.tcc.

9.3.1.115 `template<typename _Tp> _Tp std::__detail::__exponential_pdf (_Tp __lambda, _Tp __x)`

Return the exponential probability density function.

The formula for the exponential probability density function is

$$f(x|\lambda) = \lambda e^{-\lambda x} \text{ for } x \geq 0$$

Definition at line 308 of file sf_distributions.tcc.

9.3.1.116 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__factorial (unsigned int __n)`

Return the factorial of the integer n.

The factorial is:

$$n! = 12\ldots(n-1)n, 0! = 1$$

Definition at line 1615 of file sf_gamma.tcc.

References `std::__detail::__Factorial_table< _Tp >::__n`, and `_S_factorial_table`.

9.3.1.117 `template<typename _Sp, typename _Tp> _Tp std::__detail::__fermi_dirac (_Sp __s, _Tp __x)`

Return the Fermi-Dirac integral of integer or real order s and real argument x.

See also

https://en.wikipedia.org/wiki/Clausen_function
<http://dlmf.nist.gov/25.12.16>

$$F_s(x) = \frac{1}{\Gamma(s+1)} \int_0^\infty \frac{t^s}{e^{t-s} + 1} dt = -Li_{s+1}(-e^x)$$

Parameters

<code>__s</code>	The order s > -1.
<code>__x</code>	The real argument.

Returns

The real Fermi-Dirac cosine sum `F_s(x)`,

Definition at line 1405 of file sf_polylog.tcc.

References `__polylog_exp()`.

9.3.1.118 `template<typename _Tp> _Tp std::__detail::__fisher_f_cdf (_Tp __F, unsigned int __nu1, unsigned int __nu2)`

Return the F-distribution propability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .

The f-distribution propability function is related to the incomplete beta function:

$$Q(F|\nu_1, \nu_2) = I_{\frac{\nu_2}{\nu_2 + \nu_1 F}}\left(\frac{\nu_2}{2}, \frac{\nu_1}{2}\right)$$

Parameters

<code>__nu1</code>	The number of degrees of freedom of sample 1
<code>__nu2</code>	The number of degrees of freedom of sample 2
<code>__F</code>	The F statistic

Definition at line 468 of file `sf_distributions.tcc`.

References `__beta_inc()`.

9.3.1.119 `template<typename _Tp> _Tp std::__detail::__fisher_f_cdfc (_Tp __F, unsigned int __nu1, unsigned int __nu2)`

Return the F-distribution probability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .

The f-distribution probability function is related to the incomplete beta function:

$$P(F|\nu_1, \nu_2) = 1 - I_{\frac{\nu_2}{\nu_2 + \nu_1 F}}\left(\frac{\nu_2}{2}, \frac{\nu_1}{2}\right) = 1 - Q(F|\nu_1, \nu_2)$$

Parameters

<code>__F</code>	
<code>__nu1</code>	
<code>__nu2</code>	

Definition at line 497 of file `sf_distributions.tcc`.

References `__beta_inc()`.

9.3.1.120 `template<typename _Tp> __gnu_cxx::__fock_airy_t<_Tp, std::complex<_Tp>> std::__detail::__fock_airy (_Tp __x)`

Compute the Fock-type Airy functions $w_1(x)$ and $w_2(x)$ and their first derivatives $w'_1(x)$ and $w'_2(x)$ respectively.

$$w_1(x) = \sqrt{\pi}(Ai(x) + iBi(x))$$

$$w_2(x) = \sqrt{\pi}(Ai(x) - iBi(x))$$

.

Parameters

<code>__x</code>	The argument of the Airy functions.
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Returns

A struct containing the Fock-type Airy functions of the first and second kinds and their derivatives.

Definition at line 541 of file sf_mod_bessel.tcc.

References `__airy()`.

9.3.1.121 `template<typename _Tp> std::complex<_Tp> std::__detail::__fresnel (const _Tp __x)`

Return the Fresnel cosine and sine integrals as a complex number $C(x) + iS(x)$.

The Fresnel cosine integral is defined by:

$$C(x) = \int_0^x \cos\left(\frac{\pi}{2}t^2\right)dt$$

The Fresnel sine integral is defined by:

$$S(x) = \int_0^x \sin\left(\frac{\pi}{2}t^2\right)dt$$

Parameters

<code>__x</code>	The argument
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Definition at line 170 of file sf_fresnel.tcc.

References `__fresnel_cont_frac()`, and `__fresnel_series()`.

9.3.1.122 `template<typename _Tp> void std::__detail::__fresnel_cont_frac (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`

This function computes the Fresnel cosine and sine integrals by continued fractions for positive argument.

Definition at line 109 of file sf_fresnel.tcc.

Referenced by `__fresnel()`.

9.3.1.123 `template<typename _Tp> void std::__detail::__fresnel_series (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`

This function returns the Fresnel cosine and sine integrals as a pair by series expansion for positive argument.

Definition at line 51 of file sf_fresnel.tcc.

Referenced by `__fresnel()`.

9.3.1.124 `template<typename _Tp> _Tp std::__detail::__gamma (_Tp __a)`

Return the gamma function $\Gamma(a)$. The gamma function is defined by:

$$\Gamma(a) = \int_0^\infty e^{-t}t^{a-1}dt (a > 0)$$

.

Parameters

<code>__a</code>	The argument of the gamma function.
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Returns

The gamma function.

Definition at line 2628 of file `sf_gamma.tcc`.

References `__gamma_reciprocal_series()`, `__log_gamma()`, `__log_gamma_sign()`, `std::__detail::_Factorial_table<_Tp>::__n`, and `_S_factorial_table`.

Referenced by `__beta_gamma()`, `__bincoef()`, `__gamma_cdf()`, `__gamma_cdfc()`, `__gamma_pdf()`, `__hurwitz_zeta`, `polylog()`, `__polylog_exp_neg_even()`, `__polylog_exp_pos()`, `__riemann_zeta()`, `__riemann_zeta_glob()`, and `std::__detail::_Airy_series<_Tp>::__S_Scorer2()`.

9.3.1.125 `template<typename _Tp> _Tp std::__detail::__gamma_cdf (_Tp __alpha, _Tp __beta, _Tp __x)`

Return the gamma cumulative propability distribution function.

The formula for the gamma probability density function is:

$$\Gamma(x|\alpha, \beta) = \frac{1}{\beta\Gamma(\alpha)}(x/\beta)^{\alpha-1}e^{-x/\beta}$$

Definition at line 141 of file `sf_distributions.tcc`.

References `__gamma()`, and `__tgamma_lower()`.

9.3.1.126 `template<typename _Tp> _Tp std::__detail::__gamma_cdfc (_Tp __alpha, _Tp __beta, _Tp __x)`

Return the gamma complementary cumulative propability distribution function.

The formula for the gamma probability density function is:

$$\Gamma(x|\alpha, \beta) = \frac{1}{\beta\Gamma(\alpha)}(x/\beta)^{\alpha-1}e^{-x/\beta}$$

Definition at line 162 of file `sf_distributions.tcc`.

References `__gamma()`, and `__tgamma()`.

9.3.1.127 `template<typename _Tp> std::pair<_Tp, _Tp> std::__detail::__gamma_cont_frac (_Tp __a, _Tp __x)`

Return the incomplete gamma function by continued fraction.

Definition at line 2710 of file `sf_gamma.tcc`.

References `__log_gamma()`, `__log_gamma_sign()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

Referenced by `__pgamma()`, `__qgamma()`, `__tgamma()`, and `__tgamma_lower()`.

9.3.1.128 `template<typename _Tp> _Tp std::__detail::__gamma_pdf (_Tp __alpha, _Tp __beta, _Tp __x)`

Return the gamma propability distribution function.

The formula for the gamma probability density function is:

$$\Gamma(x|\alpha, \beta) = \frac{1}{\beta\Gamma(\alpha)} (x/\beta)^{\alpha-1} e^{-x/\beta}$$

Definition at line 121 of file `sf_distributions.tcc`.

References `__gamma()`.

9.3.1.129 `template<typename _Tp> _Tp std::__detail::__gamma_reciprocal_series (_Tp __a)`

Return the reciprocal of the Gamma function by series. The reciprocal of the Gamma function is given by

$$\frac{1}{\Gamma(a)} = \sum_{k=1}^{\infty} c_k a^k$$

where the coefficients are defined by recursion:

$$c_{k+1} = \frac{1}{k} \left[\gamma_E c_k + (-1)^k \sum_{j=1}^{k-1} (-1)^j \zeta(j+1-k) c_j \right]$$

where $c_1 = 1$

Definition at line 2267 of file `sf_gamma.tcc`.

Referenced by `__gamma()`, and `__gamma_temme()`.

9.3.1.130 `template<typename _Tp> std::pair<_Tp, _Tp> std::__detail::__gamma_series (_Tp __a, _Tp __x)`

Return the incomplete gamma function by series summation.

$$\gamma(a, x) = x^a e^{-x} \sum_{k=1}^{\infty} \frac{x^k}{(a)_k}$$

Definition at line 2665 of file `sf_gamma.tcc`.

References `__log_gamma()`, `__log_gamma_sign()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

Referenced by `__pgamma()`, `__qgamma()`, `__tgamma()`, and `__tgamma_lower()`.

9.3.1.131 `template<typename _Tp> __gnu_cxx::__gamma_temme_t<_Tp> std::__detail::__gamma_temme (_Tp __mu)`

Compute the gamma functions required by the Temme series expansions of $N_\nu(x)$ and $K_\nu(x)$.

$$\Gamma_1 = \frac{1}{2\mu} \left[\frac{1}{\Gamma(1-\mu)} - \frac{1}{\Gamma(1+\mu)} \right]$$

and

$$\Gamma_2 = \frac{1}{2} \left[\frac{1}{\Gamma(1-\mu)} + \frac{1}{\Gamma(1+\mu)} \right]$$

where $-1/2 \leq \mu \leq 1/2$ is $\mu = \nu - N$ and N is the nearest integer to ν . The values of $\Gamma(1+\mu)$ and $\Gamma(1-\mu)$ are returned as well.

The accuracy requirements on this are exquisite.

Parameters

<code>__mu</code>	The input parameter of the gamma functions.
-------------------	---

Returns

An output structure containing four gamma functions.

Definition at line 158 of file `sf_bessel.tcc`.

References `__gamma_reciprocal_series()`.

Referenced by `__cyl_bessel_ik_steel()`, and `__cyl_bessel_jn_steel()`.

9.3.1.132 `template<typename _Tp> _Tp std::__detail::__gauss (_Tp __x)`

The CDF of the normal distribution. i.e. the integrated lower tail of the normal PDF.

Definition at line 70 of file `sf_owens_t.tcc`.

9.3.1.133 `template<typename _Tp> _Tp std::__detail::__gegenbauer_poly (unsigned int __n, _Tp __alpha, _Tp __x)`

Return the Gegenbauer polynomial $C_n^\alpha(x)$ of degree n and real order α and argument x .

The Gegenbauer polynomials are generated by a three-term recursion relation:

$$C_n^\alpha(x) = \frac{1}{n} \left[2x(n + \alpha - 1)C_{n-1}^\alpha(x) - (n + 2\alpha - 2)C_{n-2}^\alpha(x) \right]$$

and $C_0^\alpha(x) = 1$, $C_1^\alpha(x) = 2\alpha x$.

Template Parameters

<code>__Talpha</code>	The real type of the order
<code>__Tp</code>	The real type of the argument

Parameters

<code>__n</code>	The non-negative integral degree
<code>__alpha</code>	The real order
<code>__x</code>	The real argument

Definition at line 63 of file `sf_gegenbauer.tcc`.

```
9.3.1.134 template<typename _Tp> __gnu_cxx::__cyl_hankel_t<std::complex<_Tp>, std::complex<_Tp>,
std::complex<_Tp>> std::__detail::__hankel ( std::complex<_Tp> __nu, std::complex<_Tp> __z )
```

Parameters

in	<code>__nu</code>	The order for which the Hankel functions are evaluated.
in	<code>__z</code>	The argument at which the Hankel functions are evaluated.

Returns

A struct containing the cylindrical Hankel functions of the first and second kinds and their derivatives.

Definition at line 1081 of file `sf_hankel.tcc`.

References `__debye_region()`, `__hankel_debye()`, and `__hankel_uniform()`.

Referenced by `__cyl_bessel()`, `__cyl_hankel_1()`, `__cyl_hankel_2()`, `__cyl_neumann()`, and `__sph_hankel()`.

```
9.3.1.135 template<typename _Tp> __gnu_cxx::__cyl_hankel_t<std::complex<_Tp>, std::complex<_Tp>,
std::complex<_Tp>> std::__detail::__hankel_debye ( std::complex<_Tp> __nu, std::complex<_Tp> __z,
std::complex<_Tp> __alpha, int __indexr, char & __aorb, int & __morn )
```

Parameters

in	<code>__nu</code>	The order for which the Hankel functions are evaluated.
in	<code>__z</code>	The argument at which the Hankel functions are evaluated.
in	<code>__alpha</code>	
in	<code>__indexr</code>	
out	<code>__aorb</code>	
out	<code>__morn</code>	

Returns

A struct containing the cylindrical Hankel functions of the first and second kinds and their derivatives.

Definition at line 914 of file sf_hankel.tcc.

References `__sin_pi()`.

Referenced by `__hankel()`.

```
9.3.1.136  template<typename _Tp> void std::_detail::__hankel_params ( std::complex<_Tp> __nu, std::complex<_Tp>
    __zhat, std::complex<_Tp> & __p, std::complex<_Tp> & __p2, std::complex<_Tp> & __nup2, std::complex<
    _Tp> & __num2, std::complex<_Tp> & __num1d3, std::complex<_Tp> & __num2d3, std::complex<_Tp> &
    __num4d3, std::complex<_Tp> & __zeta, std::complex<_Tp> & __zetaphf, std::complex<_Tp> & __zetamhf,
    std::complex<_Tp> & __zetam3hf, std::complex<_Tp> & __zetrat )
```

Compute parameters depending on z and nu that appear in the uniform asymptotic expansions of the Hankel functions and their derivatives, except the arguments to the Airy functions.

Definition at line 109 of file sf_hankel.tcc.

Referenced by `__hankel_uniform_outer()`.

```
9.3.1.137  template<typename _Tp> __gnu_cxx::__cyl_hankel_t<std::complex<_Tp>, std::complex<_Tp>,
    std::complex<_Tp>> std::_detail::__hankel_uniform ( std::complex<_Tp> __nu, std::complex<_Tp> __z )
```

This routine computes the uniform asymptotic approximations of the Hankel functions and their derivatives including a patch for the case when the order equals or nearly equals the argument. At such points, Olver's expressions have zero denominators (and numerators) resulting in numerical problems. This routine averages results from four surrounding points in the complex plane to obtain the result in such cases.

Parameters

in	<code>__nu</code>	The order for which the Hankel functions are evaluated.
in	<code>__z</code>	The argument at which the Hankel functions are evaluated.

Returns

A struct containing the cylindrical Hankel functions of the first and second kinds and their derivatives.

Definition at line 861 of file sf_hankel.tcc.

References `__hankel_uniform_olver()`.

Referenced by `__hankel()`.


```
9.3.1.138 template<typename _Tp > __gnu_cxx::__cyl_hankel_t<std::complex<_Tp>, std::complex<_Tp>,
std::complex<_Tp> > std::__detail::__hankel_uniform_olver ( std::complex<_Tp> __nu, std::complex<_Tp> __z )
```

Compute approximate values for the Hankel functions of the first and second kinds using Olver's uniform asymptotic expansion to of order `nu` along with their derivatives.

Parameters

in	<code>__nu</code>	The order for which the Hankel functions are evaluated.
in	<code>__z</code>	The argument at which the Hankel functions are evaluated.

Returns

A struct containing the cylindrical Hankel functions of the first and second kinds and their derivatives.

Definition at line 778 of file `sf_hankel.tcc`.

References `__hankel_uniform_outer()`, and `__hankel_uniform_sum()`.

Referenced by `__hankel_uniform()`.

```
9.3.1.139 template<typename _Tp> void std::__detail::__hankel_uniform_outer (
    std::complex<_Tp> __nu, std::complex<_Tp> __z, _Tp __eps,
    std::complex<_Tp> &__zhat, std::complex<_Tp> &__1dnsq,
    std::complex<_Tp> &__num1d3, std::complex<_Tp> &__num2d3,
    std::complex<_Tp> &__p, std::complex<_Tp> &__p2,
    std::complex<_Tp> &__etm3h, std::complex<_Tp> &__etrat,
    std::complex<_Tp> &__Aip, std::complex<_Tp> &__o4dp,
    std::complex<_Tp> &__Aim, std::complex<_Tp> &__o4dm,
    std::complex<_Tp> &__od2p, std::complex<_Tp> &__od0dp,
    std::complex<_Tp> &__od2m, std::complex<_Tp> &__od0dm )
```

Compute outer factors and associated functions of `z` and `nu` appearing in Olver's uniform asymptotic expansions of the Hankel functions of the first and second kinds and their derivatives. The various functions of `z` and `nu` returned by `hankel_uniform_outer` are available for use in computing further terms in the expansions.

Definition at line 248 of file `sf_hankel.tcc`.

References `__airy_arg()`, and `__hankel_params()`.

Referenced by `__hankel_uniform_olver()`.

```
9.3.1.140 template<typename _Tp> void std::__detail::__hankel_uniform_sum (
    std::complex<_Tp> __p, std::complex<_Tp> __p2,
    std::complex<_Tp> __num2, std::complex<_Tp> __zetam3hf,
    std::complex<_Tp> __Aip, std::complex<_Tp> __o4dp,
    std::complex<_Tp> __Aim, std::complex<_Tp> __o4dm,
    std::complex<_Tp> __od2p, std::complex<_Tp> __od0dp,
    std::complex<_Tp> __od2m, std::complex<_Tp> __od0dm,
    _Tp __eps, std::complex<_Tp> &__H1sum,
    std::complex<_Tp> &__H1psum, std::complex<_Tp> &__H2sum,
    std::complex<_Tp> &__H2psum )
```

Compute the sums in appropriate linear combinations appearing in Olver's uniform asymptotic expansions for the Hankel functions of the first and second kinds and their derivatives, using up to `nterms` (less than 5) to achieve relative error `eps`.

Parameters

in	<code>__p</code>	
in	<code>__p2</code>	
in	<code>__num2</code>	
in	<code>__zetam3hf</code>	

Parameters

in	<code>_Aip</code>	The Airy function value $Ai()$.
in	<code>__o4dp</code>	
in	<code>_Aim</code>	The Airy function value $Ai()$.
in	<code>__o4dm</code>	
in	<code>__od2p</code>	
in	<code>__od0dp</code>	
in	<code>__od2m</code>	
in	<code>__od0dm</code>	
in	<code>__eps</code>	The error tolerance
out	<code>_H1sum</code>	The Hankel function of the first kind.
out	<code>_H1psum</code>	The derivative of the Hankel function of the first kind.
out	<code>_H2sum</code>	The Hankel function of the second kind.
out	<code>_H2psum</code>	The derivative of the Hankel function of the second kind.

Definition at line 325 of file `sf_hankel.tcc`.

Referenced by `__hankel_uniform_olver()`.

9.3.1.141 `template<typename _Tp> _Tp std::__detail::__harmonic_number (unsigned int __n)`

Definition at line 3244 of file `sf_gamma.tcc`.

References `std::__detail::__Factorial_table< _Tp >::__n`, `_S_harmonic_denom`, `_S_harmonic_numer`, and `_S_num_↵harmonic_numer`.

9.3.1.142 `template<typename _Tp> _Tp std::__detail::__heuman_lambda (_Tp __k, _Tp __phi)`

Return the Heuman lambda function.

Definition at line 986 of file `sf_ellint.tcc`.

References `__comp_ellint_1()`, `__ellint_1()`, `__ellint_rf()`, `__ellint_rj()`, and `__jacobi_zeta()`.

9.3.1.143 `template<typename _Tp> _Tp std::__detail::__hurwitz_zeta (_Tp __s, _Tp __a)`

Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.

The Hurwitz zeta function is defined by:

$$\zeta(s, a) = \sum_{n=0}^{\infty} \frac{1}{(n+a)^s}$$

The Riemann zeta function is a special case:

$$\zeta(s) = \zeta(s, 1)$$

Parameters

\leftrightarrow _s	The argument $s \neq 1$
\leftrightarrow _a	The scale parameter $a > -1$

Definition at line 743 of file sf_zeta.tcc.

References `__hurwitz_zeta_euler_maclaurin()`, and `__riemann_zeta()`.

Referenced by `__psi()`.

9.3.1.144 `template<typename _Tp> _Tp std::__detail::__hurwitz_zeta_euler_maclaurin (_Tp __s, _Tp __a)`

Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.

See also

An efficient algorithm for accelerating the convergence of oscillatory series, useful for computing the polylogarithm and Hurwitz zeta functions, Linas Vep

Parameters

\leftrightarrow _s	The argument $s \neq 1$
\leftrightarrow _a	The scale parameter $a > -1$

Definition at line 695 of file sf_zeta.tcc.

References `_S_Euler_Maclaurin_zeta`.

Referenced by `__hurwitz_zeta()`.

9.3.1.145 `template<typename _Tp> std::complex<_Tp> std::__detail::__hurwitz_zeta_polylog (_Tp __s, std::complex<_Tp> __a)`

Return the Hurwitz Zeta function for real s and complex a . This uses Jonquiere's identity:

$$\frac{(i2\pi)^s}{\Gamma(s)} \zeta(a, 1-s) = Li_s(e^{i2\pi a}) + (-1)^s Li_s(e^{-i2\pi a})$$

Parameters

\leftrightarrow _s	The real argument
\leftrightarrow _a	The complex parameter

Todo This __hurwitz_zeta_polylog prefactor is prone to overflow. positive integer orders s?

Definition at line 1122 of file sf_polylog.tcc.

References __gamma(), and __polylog_exp().

9.3.1.146 `template<typename _Tp > std::complex<_Tp> std::__detail::__hydrogen (unsigned int __n, unsigned int __l, unsigned int __m, _Tp __Z, _Tp __r, _Tp __theta, _Tp __phi)`

Return the bound-state Coulomb wave-function.

Definition at line 49 of file sf_hydrogen.tcc.

References __assoc_laguerre(), __log_gamma(), __psi(), and __sph_legendre().

9.3.1.147 `template<typename _Tp > _Tp std::__detail::__hyperg (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$.

The hypergeometric function is defined by

$${}_2F_1(a, b; c; x) = \frac{\Gamma(c)}{\Gamma(a)\Gamma(b)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)\Gamma(b+n)}{\Gamma(c+n)} \frac{x^n}{n!}$$

Parameters

\leftrightarrow _a	The first <i>numerator</i> parameter.
\leftrightarrow _b	The second <i>numerator</i> parameter.
\leftrightarrow _c	The <i>denominator</i> parameter.
\leftrightarrow _x	The argument of the confluent hypergeometric function.

Returns

The confluent hypergeometric function.

Definition at line 761 of file sf_hyperg.tcc.

References `__hyperg_luke()`, `__hyperg_reflect()`, `__hyperg_series()`, `__log_gamma()`, and `__log_gamma_sign()`.

9.3.1.148 `template<typename _Tp> _Tp std::__detail::__hyperg_luke (_Tp __a, _Tp __b, _Tp __c, _Tp __xin)`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by an iterative procedure described in Luke, Algorithms for the Computation of Mathematical Functions.

Definition at line 352 of file sf_hyperg.tcc.

Referenced by `__hyperg()`.

9.3.1.149 `template<typename _Tp> _Tp std::__detail::__hyperg_reflect (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by the reflection formulae in Abramowitz & Stegun formula 15.3.6 for $d = c - a - b$ not integral and formula 15.3.11 for $d = c - a - b$ integral. This assumes $a, b, c \neq$ negative integer.

The hypergeometric function is defined by

$${}_2F_1(a, b; c; x) = \frac{\Gamma(c)}{\Gamma(a)\Gamma(b)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)\Gamma(b+n)}{\Gamma(c+n)} \frac{x^n}{n!}$$

The reflection formula for nonintegral $d = c - a - b$ is:

$${}_2F_1(a, b; c; x) = \frac{\Gamma(c)\Gamma(d)}{\Gamma(c-a)\Gamma(c-b)} {}_2F_1(a, b; 1-d; 1-x) + \frac{\Gamma(c)\Gamma(-d)}{\Gamma(a)\Gamma(b)} {}_2F_1(c-a, c-b; 1+d; 1-x)$$

The reflection formula for integral $m = c - a - b$ is:

$${}_2F_1(a, b; a+b+m; x) = \frac{\Gamma(m)\Gamma(a+b+m)}{\Gamma(a+m)\Gamma(b+m)} \sum_{k=0}^{m-1} \frac{(m+a)_k(m+b)_k}{k!(1-m)_k} (1-x)^k + (-1)^m$$

Definition at line 487 of file sf_hyperg.tcc.

References `__hyperg_series()`, `__log_gamma()`, `__log_gamma_sign()`, and `__psi()`.

Referenced by `__hyperg()`.

9.3.1.150 `template<typename _Tp> _Tp std::__detail::__hyperg_series (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`

Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by series expansion.

The hypergeometric function is defined by

$${}_2F_1(a, b; c; x) = \frac{\Gamma(c)}{\Gamma(a)\Gamma(b)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)\Gamma(b+n)}{\Gamma(c+n)} \frac{x^n}{n!}$$

This works and it's pretty fast.

Parameters

\longleftrightarrow _a	The first <i>numerator</i> parameter.
\longleftrightarrow _b	The second <i>numerator</i> parameter.
\longleftrightarrow _c	The <i>denominator</i> parameter.
\longleftrightarrow _x	The argument of the confluent hypergeometric function.

Returns

The confluent hypergeometric function.

Definition at line 321 of file sf_hyperg.tcc.

Referenced by __hyperg(), and __hyperg_reflect().

9.3.1.151 `template<typename _Tp> _Tp std::__detail::__ibeta_cont_frac (_Tp __a, _Tp __b, _Tp __x)`

Return the regularized incomplete beta function, $I_x(a, b)$, of arguments a, b, and x.

Parameters

\longleftrightarrow _a	The first parameter
\longleftrightarrow _b	The second parameter
\longleftrightarrow _x	The argument

Definition at line 239 of file sf_beta.tcc.

Referenced by __beta_inc().

9.3.1.152 `template<typename _Tp> std::tuple<_Tp, _Tp, _Tp> std::__detail::__jacobi_sncndn (_Tp __k, _Tp __u)`

Return a tuple of the three primary Jacobi elliptic functions: $sn(k, u)$, $cn(k, u)$, $dn(k, u)$.

Definition at line 416 of file sf_theta.tcc.

9.3.1.153 `template<typename _Tp> _Tp std::__detail::__jacobi_zeta (_Tp __k, _Tp __phi)`

Return the Jacobi zeta function.

Definition at line 949 of file sf_ellint.tcc.

References __comp_ellint_1(), and __ellint_rj().

Referenced by __heuman_lambda().



9.3.1.154 `template<typename _Tp> _Tp std::__detail::__laguerre (unsigned int __n, _Tp __x)`

This routine returns the Laguerre polynomial of order n: $L_n(x)$.

The Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

Parameters

 <code>__n</code>	The order of the Laguerre polynomial.
 <code>__x</code>	The argument of the Laguerre polynomial.

Returns

The value of the Laguerre polynomial of order n and argument x.

Definition at line 320 of file sf_laguerre.tcc.

9.3.1.155 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__lanczos_binet1p (_Tp __z)`

Return the Binet function $J(1+z)$ by the Lanczos method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^*(z))$ defined by


$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

Parameters

 <code>__z</code>	The argument of the log of the gamma function.
--	--

Returns

The logarithm of the gamma function.

Definition at line 2192 of file sf_gamma.tcc.

References `std::__detail::__Factorial_table<_Tp>::__n`.

Referenced by `__lanczos_log_gamma1p()`.

9.3.1.156 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__lanczos_log_gamma1p (_Tp __z)`

Return the logarithm of the gamma function $\log(\Gamma(1 + z))$ by the Lanczos method.

If the argument is real, the log of the absolute value of the Gamma function is returned. The sign to be applied to the exponential of this log Gamma can be recovered with a call to `__log_gamma_sign`.

For complex argument the fully complex log of the gamma function is returned.

Parameters

<code>__z</code>	The argument of the log of the gamma function.
------------------	--

Returns

The logarithm of the gamma function.

Definition at line 2226 of file `sf_gamma.tcc`.

References `__lanczos_binet1p()`, and `__sin_pi()`.

9.3.1.157 `template<typename _Tp> _Tp std::__detail::__legendre_q (unsigned int __l, _Tp __x)`

Return the Legendre function of the second kind by upward recursion on order l .

The Legendre function of the second kind of order l and argument x , $Q_l(x)$, is defined by:

$$Q_l(x) = \frac{1}{2^l l!} \frac{d^l}{dx^l} (x^2 - 1)^l$$

Parameters

<code>__l</code>	The order of the Legendre function. $l \geq 0$.
<code>__x</code>	The argument of the Legendre function. $ x \leq 1$.

Definition at line 124 of file `sf_legendre.tcc`.

9.3.1.158 `template<typename _Tp> _Tp std::__detail::__log_bincoef (unsigned int __n, unsigned int __k)`

Return the logarithm of the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

Parameters

<code>__n</code>	The first argument of the binomial coefficient.
<code>__k</code>	The second argument of the binomial coefficient.

Returns

The logarithm of the binomial coefficient.

Definition at line 2438 of file `sf_gamma.tcc`.

References `__log_gamma()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

Referenced by `__bincoef()`.

9.3.1.159 `template<typename _Tp> _Tp std::__detail::__log_bincoef (_Tp __nu, unsigned int __k)`

Return the logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

Parameters

<code>__nu</code>	The first argument of the binomial coefficient.
<code>__k</code>	The second argument of the binomial coefficient.

Returns

The logarithm of the binomial coefficient.

Definition at line 2475 of file `sf_gamma.tcc`.

References `__log_gamma()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

9.3.1.160 `template<typename _Tp> _Tp std::__detail::__log_bincoef_sign (_Tp __nu, unsigned int __k)`

Return the sign of the exponentiated logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu + 1)}{\Gamma(\nu - k + 1)\Gamma(k + 1)}$$

The binomial coefficients are generated by:

$$(1 + t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

Parameters

<code>__nu</code>	The first argument of the binomial coefficient.
<code>__k</code>	The second argument of the binomial coefficient.

Returns

The sign of the gamma function.

Definition at line 2506 of file `sf_gamma.tcc`.

References `__log_gamma_sign()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

Referenced by `__bincoef()`.

9.3.1.161 `template<typename _Tp> std::complex<_Tp> std::__detail::__log_bincoef_sign (std::complex<_Tp> __nu, unsigned int __k)`

Definition at line 2521 of file `sf_gamma.tcc`.

9.3.1.162 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_double_factorial (_Tp __x)`

Definition at line 1643 of file `sf_gamma.tcc`.

References `__cos_pi()`, and `__log_gamma()`.

Referenced by `__double_factorial()`, and `__log_double_factorial()`.

9.3.1.163 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_double_factorial (int __n)`

Return the logarithm of the double factorial of the integer n .

The double factorial is defined for integral n by:

$$n!! = 135\dots(n-2)n, \text{ odd } n!! = 246\dots(n-2)n, \text{ even } n!! = 10!! = 1$$

The double factorial is defined for odd negative integers in the obvious way:

$$(-2m-1)!! = 1/(1(-1)(-3)\dots(-2m+1)(-2m-1)) = \frac{(-1)^m}{(2m-1)!!}$$

for $n = -2m - 1$.

Definition at line 1709 of file `sf_gamma.tcc`.

References `__log_double_factorial()`, `std::__detail::_Factorial_table<_Tp>::__log_factorial`, `std::__detail::_Factorial_table<_Tp>::__n`, `_S_double_factorial_table`, and `_S_neg_double_factorial_table`.

9.3.1.164 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_factorial (unsigned int __n)`

Return the logarithm of the factorial of the integer n .

The factorial is:

$$n! = 12\dots(n-1)n, 0! = 1$$

Definition at line 1633 of file `sf_gamma.tcc`.

References `__log_gamma()`, `std::__detail::_Factorial_table<_Tp>::__n`, and `_S_factorial_table`.

9.3.1.165 `template<typename _Tp> _Tp std::__detail::__log_gamma (_Tp __a)`

Return $\log(|\Gamma(a)|)$. This will return values even for $a < 0$. To recover the sign of $\Gamma(a)$ for any argument use `__log_gamma_sign`.

Parameters

<code>__a</code>	The argument of the log of the gamma function.
------------------	--

Returns

The logarithm of the gamma function.

Definition at line 2329 of file `sf_gamma.tcc`.

References `__sin_pi()`, and `__spouge_log_gamma1p()`.

Referenced by `__beta_inc()`, `__beta_lgamma()`, `__cyl_bessel_ij_series()`, `__gamma()`, `__gamma_cont_frac()`, `__gamma_series()`, `__hydrogen()`, `__hyperg()`, `__hyperg_reflect()`, `__log_bincoef()`, `__log_double_factorial()`, `__log_factorial()`, `__log_gamma()`, `__log_pochhammer()`, `__log_pochhammer_lower()`, `__pochhammer()`, `__pochhammer_lower()`, `__poly_laguerre_large_n()`, `__polylog_exp_asymp()`, `__polylog_exp_neg()`, `__polylog_exp_neg_even()`, `__polylog_exp_neg_odd()`, `__polylog_exp_pos()`, `__psi()`, `__riemann_zeta()`, and `__sph_legendre()`.

9.3.1.166 `template<typename _Tp> std::complex<_Tp> std::__detail::__log_gamma (std::complex<_Tp> __a)`

Return $\log(\Gamma(a))$ for complex argument.

Parameters

<code>__a</code>	The complex argument of the log of the gamma function.
------------------	--

Returns

The complex logarithm of the gamma function.

Definition at line 2364 of file `sf_gamma.tcc`.

References `std::__detail::_Factorial_table<_Tp>::__log_factorial`, `__log_gamma()`, `std::__detail::_Factorial_table<_Tp>::__n`, `__sin_pi()`, `__spouge_log_gamma1p()`, and `_S_factorial_table`.

9.3.1.167 `template<typename _Tp> _GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_gamma_bernoulli (_Tp __x)`

Return $\log(\Gamma(x))$ by asymptotic expansion with Bernoulli number coefficients. This is like Sterling's approximation.

Parameters

<code>__x</code>	The argument of the log of the gamma function.
------------------	--

Returns

The logarithm of the gamma function.

Definition at line 1826 of file `sf_gamma.tcc`.

9.3.1.168 `template<typename _Tp> _Tp std::__detail::__log_gamma_sign (_Tp __a)`

Return the sign of $\Gamma(x)$. At nonpositive integers zero is returned indicating $\Gamma(x)$ is undefined.

Parameters

<code>__a</code>	The argument of the gamma function.
------------------	-------------------------------------

Returns

The sign of the gamma function.

Definition at line 2405 of file `sf_gamma.tcc`.

Referenced by `__beta_inc()`, `__beta_lgamma()`, `__gamma()`, `__gamma_cont_frac()`, `__gamma_series()`, `__hyperg()`, `__hyperg_reflect()`, `__log_bincoef_sign()`, `__pochhammer()`, and `__pochhammer_lower()`.

9.3.1.169 `template<typename _Tp> std::complex<_Tp> std::__detail::__log_gamma_sign (std::complex<_Tp> __a)`

Definition at line 2417 of file `sf_gamma.tcc`.

9.3.1.170 `template<typename _Tp> _Tp std::__detail::__log_pochhammer (_Tp __a, _Tp __nu)`

Return the logarithm of the (upper) Pochhammer symbol or the rising factorial function. The Pochhammer symbol is defined for integer order by

$$(a)_\nu = \Gamma(a + \nu) / \Gamma(a) = \prod_{k=0}^{\nu-1} (a + k), (a)_0 = 1$$

Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a + \nu)] - \ln[\Gamma(a)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{array}{c} a \\ n \end{array} \right]$$

, and others.

Definition at line 3157 of file `sf_gamma.tcc`.

References `__log_gamma()`, and `__pochhammer()`.

9.3.1.171 `template<typename _Tp> _Tp std::__detail::__log_pochhammer_lower (_Tp __a, _Tp __nu)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function. The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a+1)/\Gamma(a-\nu+1) = \prod_{k=0}^{n-1} (a-k), (a)_0 = 1$$

In particular, $(n)_n = n!$. Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a+1)] - \ln[\Gamma(a-\nu+1)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\underline{n}}$$

,

$$\left\{ \begin{matrix} a \\ n \end{matrix} \right\}$$

, and others.

Definition at line 3010 of file sf_gamma.tcc.

References `__log_gamma()`, and `__pochhammer_lower()`.

9.3.1.172 `template<typename _Tp> _Tp std::__detail::__logint (const _Tp __x)`

Return the logarithmic integral $li(x)$.

The logarithmic integral is given by

$$li(x) = Ei(\log(x))$$

Parameters

\leftrightarrow __x	The argument of the logarithmic integral function.
--------------------------	--

Returns

The logarithmic integral.

Definition at line 538 of file sf_expint.tcc.

References `__expint()`.

9.3.1.173 `template<typename _Tp> _Tp std::__detail::__lognormal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`

Return the lognormal cumulative probability density function.

The formula for the lognormal cumulative probability density function is

$$F(x|\mu, \sigma) = \frac{1}{2} \left[1 - \operatorname{erf} \left(\frac{\ln x - \mu}{\sqrt{2}\sigma} \right) \right]$$

Definition at line 287 of file sf_distributions.tcc.

9.3.1.174 `template<typename _Tp> _Tp std::__detail::__lognormal_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the lognormal probability density function.

The formula for the lognormal probability density function is

$$f(x|\mu, \sigma) = \frac{e^{(\ln x - \mu)^2 / 2\sigma^2}}{\sigma\sqrt{2\pi}}$$

Definition at line 259 of file `sf_distributions.tcc`.

9.3.1.175 `template<typename _Tp> _Tp std::__detail::__normal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`

Return the normal cumulative probability density function.

The formula for the normal cumulative probability density function is

$$F(x|\mu, \sigma) = \frac{1}{2} \left[1 - \operatorname{erf}\left(\frac{x - \mu}{\sqrt{2}\sigma}\right) \right]$$

Definition at line 238 of file `sf_distributions.tcc`.

9.3.1.176 `template<typename _Tp> _Tp std::__detail::__normal_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the normal probability density function.

The formula for the normal probability density function is

$$f(x|\mu, \sigma) = \frac{e^{-(x-\mu)^2 / 2\sigma^2}}{\sigma\sqrt{2\pi}}$$

Definition at line 210 of file `sf_distributions.tcc`.

9.3.1.177 `template<typename _Tp> _Tp std::__detail::__owens_t (_Tp __h, _Tp __a)`

Return the Owens T function:

$$T(h, a) = \frac{1}{2\pi} \int_0^a \frac{\exp[-\frac{1}{2}h^2(1+x^2)]}{1+x^2} dx$$

This implementation is a translation of the Fortran implementation in

See also

Patefield, M. and Tandy, D. "Fast and accurate Calculation of Owen's T-Function", Journal of Statistical Software, 5 (5), 1 - 25 (2000)

Parameters

in	\leftrightarrow _h	The scale parameter.
in	\leftrightarrow _a	The integration limit.

Returns

The owens T function.

Definition at line 92 of file sf_owens_t.tcc.

References __znorm1(), and __znorm2().

9.3.1.178 `template<typename _Tp> _Tp std::__detail::__pgamma (_Tp __a, _Tp __x)`

Return the regularized lower incomplete gamma function. The regularized lower incomplete gamma function is defined by

$$P(a, x) = \frac{\gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

is the lower incomplete gamma function.

Definition at line 2764 of file sf_gamma.tcc.

References __gamma_cont_frac(), and __gamma_series().

Referenced by __chi_squared_pdf().

9.3.1.179 `template<typename _Tp> _Tp std::__detail::__pochhammer (_Tp __a, int __n)`

Return the (upper) Pochhammer function or the rising factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + \nu) / \Gamma(\nu) = \prod_{k=0}^{n-1} (a + k), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{array}{c} a \\ n \end{array} \right]$$

, and others.

Definition at line 3059 of file sf_gamma.tcc.

References __log_gamma(), __log_gamma_sign(), and std::__detail::_Factorial_table<_Tp>::__n.

Referenced by __log_pochhammer(), and __pochhammer().

9.3.1.180 `template<typename _Tp> _Tp std::__detail::__pochhammer (_Tp __a, _Tp __nu)`

Return the (upper) Pochhammer function or the rising factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + \nu)/\Gamma(\nu) = \prod_{k=0}^{n-1} (a + k), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

Definition at line 3114 of file `sf_gamma.tcc`.

References `__log_gamma()`, `__log_gamma_sign()`, `std::__detail::_Factorial_table<_Tp>::__n`, and `__pochhammer()`.

9.3.1.181 `template<typename _Tp> _Tp std::__detail::__pochhammer_lower (_Tp __a, int __n)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and integral order n . The lower Pochhammer symbol is defined by

$$(a)_n = \prod_{k=0}^{n-1} (a - k), (a)_0 = 1 = \Gamma(a + 1)/\Gamma(a - n + 1)$$

In particular, $(n)_n = n!$.

Definition at line 2900 of file `sf_gamma.tcc`.

References `__log_gamma()`, `__log_gamma_sign()`, and `std::__detail::_Factorial_table<_Tp>::__n`.

Referenced by `__log_pochhammer_lower()`, and `__pochhammer_lower()`.

9.3.1.182 `template<typename _Tp> _Tp std::__detail::__pochhammer_lower (_Tp __a, _Tp __nu)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and order ν . The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + 1)/\Gamma(a - \nu + 1) = \prod_{k=0}^{n-1} (a - k), (a)_0 = 1, \nu = n$$

In particular, $(n)_n = n!$.

Definition at line 2957 of file `sf_gamma.tcc`.

References `__log_gamma()`, `__log_gamma_sign()`, and `__pochhammer_lower()`.

9.3.1.183 `template<typename _Tp> std::complex<_Tp> std::__detail::__polar_pi (_Tp __rho, _Tp __phi_pi) [inline]`

Reperiodized complex constructor.

Definition at line 404 of file sf_trig.tcc.

References `__sincos_pi()`, `__gnu_cxx::__sincos_t<_Tp>::cos_value`, and `__gnu_cxx::__sincos_t<_Tp>::sin_value`.

Referenced by `__cyl_bessel_jn_neg_arg()`, `__cyl_hankel_1()`, `__cyl_hankel_2()`, and `__polylog_exp_neg()`.

9.3.1.184 `template<typename _Tp> _Tp std::__detail::__poly_hermite (unsigned int __n, _Tp __x)`

This routine returns the Hermite polynomial of order n: $H_n(x)$.

The Hermite polynomial is defined by:

$$H_n(x) = (-1)^n e^{x^2} \frac{d^n}{dx^n} e^{-x^2}$$

The Hermite polynomial obeys a reflection formula:

$$H_n(-x) = (-1)^n H_n(x)$$

Parameters

\longleftrightarrow __n	The order of the Hermite polynomial.
\longleftrightarrow __x	The argument of the Hermite polynomial.

Returns

The value of the Hermite polynomial of order n and argument x.

Definition at line 179 of file sf_hermite.tcc.

References `__poly_hermite_asymp()`, and `__poly_hermite_recursion()`.

9.3.1.185 `template<typename _Tp> _Tp std::__detail::__poly_hermite_asymp (unsigned int __n, _Tp __x)`

This routine returns the Hermite polynomial of large order n: $H_n(x)$. We assume here that $x \geq 0$.

The Hermite polynomial is defined by:

$$H_n(x) = (-1)^n e^{x^2} \frac{d^n}{dx^n} e^{-x^2}$$

See also

"Asymptotic analysis of the Hermite polynomials from their differential-difference equation", Diego Dominici, arXiv:math/0601078v1 [math.CA] 4 Jan 2006

Parameters

\leftrightarrow _n	The order of the Hermite polynomial.
\leftrightarrow _x	The argument of the Hermite polynomial.

Returns

The value of the Hermite polynomial of order n and argument x.

Definition at line 115 of file sf_hermite.tcc.

References `__airy()`.

Referenced by `__poly_hermite()`.

9.3.1.186 `template<typename _Tp > _Tp std::__detail::__poly_hermite_recursion (unsigned int __n, _Tp __x)`

This routine returns the Hermite polynomial of order n: $H_n(x)$ by recursion on n.

The Hermite polynomial is defined by:

$$H_n(x) = (-1)^n e^{x^2} \frac{d^n}{dx^n} e^{-x^2}$$

Parameters

\leftrightarrow _n	The order of the Hermite polynomial.
\leftrightarrow _x	The argument of the Hermite polynomial.

Returns

The value of the Hermite polynomial of order n and argument x.

Definition at line 71 of file sf_hermite.tcc.

Referenced by `__poly_hermite()`.

9.3.1.187 `template<typename _Tp > _Tp std::__detail::__poly_jacobi (unsigned int __n, _Tp __alpha, _Tp __beta, _Tp __x)`

Compute the Jacobi polynomial by recursion on n :

$$2n(\alpha+\beta+n)(\alpha+\beta+2n-2)P_n^{(\alpha,\beta)}(x) = (\alpha+\beta+2n-1)((\alpha^2-\beta^2)+x(\alpha+\beta+2n-2)(\alpha+\beta+2n))P_{n-1}^{(\alpha,\beta)}(x) - 2(\alpha+n-1)(\beta+n-1)(\alpha+\beta+2n-2)P_{n-2}^{(\alpha,\beta)}(x)$$

Definition at line 59 of file sf_jacobi.tcc.

References `__beta()`.

Referenced by `__poly_radial_jacobi()`.

9.3.1.188 `template<typename _Tpa, typename _Tp> _Tp std::__detail::__poly_laguerre (unsigned int __n, _Tpa __alpha1, _Tp __x)`

This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^{\alpha}(x)$.

The associated Laguerre function is defined by

$$L_n^{\alpha}(x) = \frac{(\alpha+1)_n}{n!} {}_1F_1(-n; \alpha+1; x)$$

where $(\alpha)_n$ is the Pochhammer symbol and ${}_1F_1(a; c; x)$ is the confluent hypergeometric function.

The associated Laguerre polynomial is defined for integral $\alpha = m$ by:

$$L_n^m(x) = (-1)^m \frac{d^m}{dx^m} L_{n+m}(x)$$

where the Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

Template Parameters

<code>_Tpa</code>	The type of the degree.
<code>_Tp</code>	The type of the parameter.

Parameters

<code>__n</code>	The order of the Laguerre function.
<code>__alpha1</code>	The degree of the Laguerre function.
<code>__x</code>	The argument of the Laguerre function.

Returns

The value of the Laguerre function of order n , degree α , and argument x .

Definition at line 250 of file `sf_laguerre.tcc`.

References `__poly_laguerre_hyperg()`, `__poly_laguerre_large_n()`, and `__poly_laguerre_recursion()`.

9.3.1.189 `template<typename _Tpa, typename _Tp> _Tp std::__detail::__poly_laguerre_hyperg (unsigned int __n, _Tpa __alpha1, _Tp __x)`

Evaluate the polynomial based on the confluent hypergeometric function in a safe way, with no restriction on the arguments.

The associated Laguerre function is defined by

$$L_n^{\alpha}(x) = \frac{(\alpha+1)_n}{n!} {}_1F_1(-n; \alpha+1; x)$$

where $(\alpha)_n$ is the Pochhammer symbol and ${}_1F_1(a; c; x)$ is the confluent hypergeometric function.

This function assumes $x \neq 0$.

This is from the GNU Scientific Library.

Template Parameters

<code>_Tpa</code>	The type of the degree.
<code>_Tp</code>	The type of the parameter.

Parameters

<code>__n</code>	The order of the Laguerre function.
<code>__alpha1</code>	The degree of the Laguerre function.
<code>__x</code>	The argument of the Laguerre function.

Returns

The value of the Laguerre function of order n , degree α , and argument x .

Definition at line 131 of file `sf_laguerre.tcc`.

Referenced by `__poly_laguerre()`.

```
9.3.1.190  template<typename _Tpa, typename _Tp > _Tp std::__detail::__poly_laguerre_large_n( unsigned __n, _Tpa __alpha1,
    _Tp __x )
```

This routine returns the associated Laguerre polynomial of order n , degree $\alpha > -1$ for large n . Abramowitz & Stegun, 13.5.21.

Template Parameters

<code>_Tpa</code>	The type of the degree.
<code>_Tp</code>	The type of the parameter.

Parameters

<code>__n</code>	The order of the Laguerre function.
<code>__alpha1</code>	The degree of the Laguerre function.
<code>__x</code>	The argument of the Laguerre function.

Returns

The value of the Laguerre function of order n , degree α , and argument x .

This is from the GNU Scientific Library.

Definition at line 74 of file sf_laguerre.tcc.

References `__log_gamma()`, and `__sin_pi()`.

Referenced by `__poly_laguerre()`.

9.3.1.191 `template<typename _Tpa, typename _Tp> _Tp std::__detail::__poly_laguerre_recursion (unsigned int __n, _Tpa __alpha1, _Tp __x)`

This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^\alpha(x)$ by recursion.

The associated Laguerre function is defined by

$$L_n^\alpha(x) = \frac{(\alpha+1)_n}{n!} {}_1F_1(-n; \alpha+1; x)$$

where $(\alpha)_n$ is the Pochhammer symbol and ${}_1F_1(a; c; x)$ is the confluent hypergeometric function.

The associated Laguerre polynomial is defined for integral $\alpha = m$ by:

$$L_n^m(x) = (-1)^m \frac{d^m}{dx^m} L_{n+m}(x)$$

where the Laguerre polynomial is defined by:

$$L_n(x) = \frac{e^x}{n!} \frac{d^n}{dx^n} (x^n e^{-x})$$

Template Parameters

<code>_Tpa</code>	The type of the degree.
<code>_Tp</code>	The type of the parameter.

Parameters

<code>__n</code>	The order of the Laguerre function.
<code>__alpha1</code>	The degree of the Laguerre function.
<code>__x</code>	The argument of the Laguerre function.

Returns

The value of the Laguerre function of order n , degree α , and argument x .

Definition at line 189 of file sf_laguerre.tcc.

Referenced by `__poly_laguerre()`.

9.3.1.192 `template<typename _Tp > _Tp std::__detail::__poly_legendre_p (unsigned int __l, _Tp __x)`

Return the Legendre polynomial by upward recursion on order l .

The Legendre function of order l and argument x , $P_l(x)$, is defined by:

$$P_l(x) = \frac{1}{2^l l!} \frac{d^l}{dx^l} (x^2 - 1)^l$$

Parameters

<code>__l</code>	The order of the Legendre polynomial. $l \geq 0$.
<code>__x</code>	The argument of the Legendre polynomial.

Definition at line 76 of file `sf_legendre.tcc`.

Referenced by `__assoc_legendre_p()`, and `__sph_legendre()`.

9.3.1.193 `template<typename _Tp > _Tp std::__detail::__poly_prob_hermite_recursion (unsigned int __n, _Tp __x)`

This routine returns the Probabilists Hermite polynomial of order n : $He_n(x)$ by recursion on n .

The Hermite polynomial is defined by:

$$He_n(x) = (-1)^n e^{x^2/2} \frac{d^n}{dx^n} e^{-x^2/2}$$

or

$$He_n(x) = \frac{1}{2^{-n/2}} H_n \left(\frac{x}{\sqrt{2}} \right)$$

where $H_n(x)$ is the Physicists Hermite function.

Parameters

<code>__n</code>	The order of the Hermite polynomial.
<code>__x</code>	The argument of the Hermite polynomial.

Returns

The value of the Hermite polynomial of order n and argument x .

Definition at line 212 of file `sf_hermite.tcc`.

9.3.1.194 `template<typename _Tp> _Tp std::__detail::__poly_radial_jacobi (unsigned int __n, unsigned int __m, _Tp __rho)`

Return the radial polynomial $R_n^m(\rho)$ for non-negative degree n , order $m \leq n$, and real radial argument ρ .

The radial polynomials are defined by

$$R_n^m(\rho) = \sum_{k=0}^{\frac{n-m}{2}} \frac{(-1)^k (n-k)!}{k! \left(\frac{n+m}{2} - k\right)! \left(\frac{n-m}{2} - k\right)!} \rho^{n-2k}$$

for $n - m$ even and identically 0 for $n - m$ odd. The radial polynomials can be related to the Zernike polynomials:

$$Z_n^m(\rho, \phi) = R_n^m(\rho) \cos(m\phi)$$

$$Z_n^{-m}(\rho, \phi) = R_n^m(\rho) \sin(m\phi)$$

for non-negative m, n .

See also

zernike for details on the Zernike polynomials.

Principals of Optics, 7th edition, Max Born and Emil Wolf, Cambridge University Press, 1999, pp 523-525 and 905-910.

Template Parameters

<code>_Tp</code>	The real type of the radial coordinate
------------------	--

Parameters

<code>__n</code>	The non-negative degree.
<code>__m</code>	The non-negative azimuthal order
<code>__rho</code>	The radial argument

Definition at line 144 of file `sf_jacobi.tcc`.

References `__poly_jacobi()`.

Referenced by `__zernike()`, `__gnu_cxx::radpolyf()`, and `__gnu_cxx::radpolyf()`.

9.3.1.195 `template<typename _Tp> _Tp std::__detail::__polylog (_Tp __s, _Tp __x)`

Return the polylog $\text{Li}_s(x)$ for two real arguments.

Parameters

<code>__s</code>	The real index.
<code>__x</code>	The real argument.

Returns

The complex value of the polylogarithm.

Definition at line 1070 of file sf_polylog.tcc.

References `__polylog_exp()`.

Referenced by `__dirichlet_beta()`, `__dirichlet_eta()`, and `__polylog()`.

9.3.1.196 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog (_Tp __s, std::complex<_Tp> __w)`

Return the polylog in those cases where we can calculate it.

Parameters

<code>__s</code>	The real index.
<code>__w</code>	The complex argument.

Returns

The complex value of the polylogarithm.

Definition at line 1100 of file sf_polylog.tcc.

References `__polylog()`, and `__polylog_exp()`.

9.3.1.197 `template<typename _Tp, typename ArgType> __gnu_cxx::__promote_fp_t<std::complex<_Tp>, ArgType>
std::__detail::__polylog_exp (_Tp __s, ArgType __w)`

This is the frontend function which calculates $Li_s(e^w)$. First we branch into different parts depending on the properties of s . This function is the same irrespective of a real or complex w , hence the template parameter `ArgType`.

Note

: I *really* wish we could return a `variant<Tp, std::complex<Tp>>`.

Parameters

<code>__s</code>	The real order.
<code>__w</code>	The real or complex argument.

Returns

The real or complex value of $\text{Li}_s(e^w)$.

Definition at line 1037 of file sf_polylog.tcc.

References `__polylog_exp_int_neg()`, `__polylog_exp_int_pos()`, `__polylog_exp_negative_real_part()`, `__polylog_exp_real_neg()`, and `__polylog_exp_real_pos()`.

Referenced by `__bose_einstein()`, `__clausen()`, `__clausen_c()`, `__clausen_s()`, `__fermi_dirac()`, `__hurwitz_zeta_polylog()`, and `__polylog()`.

9.3.1.198 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_asymp (_Tp __s, std::complex<_Tp> __w)`

This function implements the asymptotic series for the polylog. It is given by

$$2 \sum_{k=0}^{\infty} \zeta(2k) w^{s-2k} / \Gamma(s-2k+1) - i\pi w^{s-1} / \Gamma(s)$$

for $\text{Re}(w) \gg 1$

Don't check this against Mathematica 8. For real u the imaginary part of the polylog is given by $\text{Im}(\text{Li}_s(e^u)) = -\pi u^{s-1} / \Gamma(s)$. Check this relation for any benchmark that you use. The use of `evenzeta` leads to a speedup of about 1000.

Parameters

<code>__s</code>	the real index s .
<code>__w</code>	the large complex argument w .

Returns

the value of the polylogarithm.

Definition at line 658 of file sf_polylog.tcc.

References `__log_gamma()`.

Referenced by `__polylog_exp_int_neg()`, `__polylog_exp_int_pos()`, `__polylog_exp_real_neg()`, and `__polylog_exp_real_pos()`.

9.3.1.199 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_int_neg (int __s, std::complex<_Tp> __w)`

This treats the case where s is a negative integer.

Parameters

$_s$	a negative integer.
$_w$	an arbitrary complex number

Returns

the value of the polylogarithm.

Definition at line 842 of file sf_polylog.tcc.

References `__clamp_0_m2pi()`, `__clamp_pi()`, `__polylog_exp_asymp()`, `__polylog_exp_neg()`, and `__polylog_exp_negative_real_part()`.

Referenced by `__polylog_exp()`.

9.3.1.200 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_int_neg (const int __s, _Tp __w)`

This treats the case where s is a negative integer and w is a real.

Parameters

$_s$	a negative integer.
$_w$	the argument.

Returns

the value of the polylogarithm.

Definition at line 887 of file sf_polylog.tcc.

References `__polylog_exp_asymp()`, `__polylog_exp_neg()`, and `__polylog_exp_negative_real_part()`.

9.3.1.201 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_int_pos (unsigned int __s, std::complex<_Tp> __w)`

Here s is a positive integer and the function descends into the different kernels depending on w .

Parameters

$_s$	a positive integer.
$_w$	an arbitrary complex number.

Returns

The value of the polylogarithm.

Definition at line 744 of file sf_polylog.tcc.

References `__clamp_0_m2pi()`, `__clamp_pi()`, `__polylog_exp_asymp()`, `__polylog_exp_negative_real_part()`, `__polylog_exp_pos()`, and `__riemann_zeta()`.

Referenced by `__polylog_exp()`.

9.3.1.202 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_int_pos (unsigned int __s, _Tp __w)`

Here `s` is a positive integer and the function descends into the different kernels depending on `w`.

Parameters

<code>__s</code>	a positive integer
<code>__w</code>	an arbitrary real argument <code>w</code>

Returns

the value of the polylogarithm.

Definition at line 797 of file sf_polylog.tcc.

References `__polylog_exp_asymp()`, `__polylog_exp_negative_real_part()`, `__polylog_exp_pos()`, and `__riemann_zeta()`.

9.3.1.203 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_neg (_Tp __s, std::complex<_Tp> __w)`

This function treats the cases of negative real index `s`. Theoretical convergence is present for $|w| < 2\pi$. We use an optimized version of

$$Li_s(e^w) = \Gamma(1-s)(-w)^{s-1} + \frac{(2\pi)^{-s}}{\pi} A_p(w)$$

$$A_p(w) = \sum_k \frac{\Gamma(1+k-s)}{k!} \sin\left(\frac{\pi}{2}(s-k)\right) \left(\frac{w}{2\pi}\right)^k \zeta(1+k-s)$$

Parameters

<code>__s</code>	The real index
<code>__w</code>	The complex argument

Returns

The value of the polylogarithm.

Definition at line 294 of file sf_polylog.tcc.

References `__log_gamma()`, `__polar_pi()`, `__riemann_zeta()`, and `__riemann_zeta_m_1()`.

Referenced by `__polylog_exp_int_neg()`, and `__polylog_exp_real_neg()`.

9.3.1.204 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_neg (int __s, std::complex<_Tp> __w)`

This function treats the cases of negative integer index s and branches accordingly

Parameters

<code>__s</code>	the integer index s.
<code>__w</code>	The Argument w

Returns

The value of the Polylogarithm evaluated by a suitable function.

Definition at line 533 of file sf_polylog.tcc.

References `__polylog_exp_neg_even()`, and `__polylog_exp_neg_odd()`.

9.3.1.205 `template<typename _Tp, int __sigma> std::complex<_Tp> std::__detail::__polylog_exp_neg_even (unsigned int __n, std::complex<_Tp> __w)`

This function treats the cases of negative integer index s which are multiples of two.

In that case the sine occurring in the expansion occasionally takes on the value zero. We use that to provide an optimized series for $p = 2n$:

In the template parameter sigma we transport whether $p = 4k(\sigma = 1)$ or $p = 4k + 2(\sigma = -1)$.

$$Li_p(e^w) = \Gamma(1-p)(-w)^{p-1} - A_p(w) - \sigma B_p(w)$$

with

$$A_p(w) = 2(2\pi)^{p-1} \frac{(-p)!}{(2\pi)^{-p/2}} \left(1 + \frac{w^2}{(4\pi^2)}\right)^{(p-1)/2} \cos \left[(1-p) \operatorname{ArcTan} \left(\frac{2\pi}{w} \right) \right]$$

and

$$B_p(w) = -2(2\pi)^{p-1} \sum_{k=0}^{\infty} \frac{\Gamma(2+2k-p)}{(2k+1)!} (-1)^k \left(\frac{w}{2\pi} \right)^{2k+1} (\zeta(2+2k-p) - 1)$$

This is suitable for $|w| < 2\pi$ The original series is (This might be worthwhile if we use the already present table of the Bernoullis)

$$Li_p(e^w) = \Gamma(1-p)(-w)^{p-1} - \sigma(2\pi)^p/\pi \sum_{k=0}^{\infty} \frac{\Gamma(2+2k-p)}{(2k+1)!} (-1)^k \left(\frac{w}{2\pi} \right)^{2k+1} \zeta(2+2k-p)$$

Parameters

\leftrightarrow _n	the integral index $n = 4k$.
\leftrightarrow _w	The complex argument w

Returns

the value of the Polylogarithm.

Definition at line 408 of file sf_polylog.tcc.

References `__gamma()`, and `__log_gamma()`.

Referenced by `__polylog_exp_neg()`.

9.3.1.206 `template<typename _Tp, int __sigma> std::complex<_Tp> std::__detail::__polylog_exp_neg_odd (unsigned int __n, std::complex<_Tp> __w)`

This function treats the cases of negative integer index s which are odd.

In that case the sine occuring in the expansion occasionally vanishes. We use that to provide an optimized series for $p = 1 + 2k$: In the template parameter sigma we transport whether $p = 1 + 4k (\sigma = 1)$ or $p = 3 + 4k (\sigma = -1)$.

$$Li_p(e^w) = \Gamma(1-p)(-w)^{p-1} + \sigma A_p(w) - \sigma B_p(w)$$

with

$$A_p(w) = 2(2\pi)^{p-1} \Gamma(1-p) \left(1 + \frac{w^2}{4\pi^2}\right)^{-1/2+p/2} \cos((1-p) \text{ArcTan}(2\pi/w))$$

and

$$B_p(w) = 2(2\pi)^{p-1} \sum_{k=0}^{\infty} \frac{\Gamma(1+2k-p)}{(2k)!} \left(\frac{-w^2}{4\pi^2}\right)^k (\zeta(1+2k-p) - 1)$$

This is suitable for $|w| < 2\pi$. The use of evenzeta gives a speedup of about 50 The original series is (This might be worthwhile if we use the already present table of the Bernoullis)

$$Li_p(e^w) = \Gamma(1-p)(-w)^{p-1} - 2\sigma(2\pi)^{p-1} \sum_{k=0}^{\infty} \frac{\Gamma(1+2k-p)}{(2k)!} (-1)^k \left(\frac{w}{2\pi}\right)^{2k} \zeta(1+2k-p)$$

Parameters

\leftrightarrow _n	the integral index n = 4k.
\leftrightarrow _w	The complex argument w.

Returns

The value of the Polylogarithm.

Definition at line 483 of file sf_polylog.tcc.

References `__log_gamma()`.

Referenced by `__polylog_exp_neg()`.

9.3.1.207 `template<typename _PowTp, typename _Tp> _Tp std::__detail::__polylog_exp_negative_real_part (_PowTp __s, _Tp __w)`

Theoretical convergence for $\text{Re}(w) < 0$.

Seems to beat the other expansions for $\text{Re}(w) < -\pi/2 - \pi/5$. Note that this is an implementation of the basic series:

$$Li_s(e^z) = \sum_{k=1} e^{kz} * k^{-s}$$

Parameters

<code>__s</code>	is an arbitrary type, integral or float.
<code>__w</code>	something with a negative real part.

Returns

the value of the polylogarithm.

Definition at line 712 of file sf_polylog.tcc.

Referenced by `__polylog_exp()`, `__polylog_exp_int_neg()`, `__polylog_exp_int_pos()`, `__polylog_exp_real_neg()`, and `__polylog_exp_real_pos()`.

9.3.1.208 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_pos (unsigned int __s, std::complex<_Tp> __w)`

This function treats the cases of positive integer index s .

$$Li_s(e^w) = \sum_{k=0, k! \neq s-1} \zeta(s-k) \frac{w^k}{k!} + (H_{s-1} - \log(-w)) \frac{w^{s-1}}{(s-1)!}$$

The radius of convergence is $|w| < 2\pi$. Note that this series involves a $\log(-x)$. gcc and Mathematica differ in their implementation of $\log(e^{i\pi})$: gcc: $\log(e^{+i\pi}) = + - i\pi$ whereas Mathematica doesn't preserve the sign in this case: $\log(e^{+i\pi}) = +i\pi$

Parameters

$_s$	the index s.
$_w$	the argument w.

Returns

the value of the polylogarithm.

Definition at line 142 of file sf_polylog.tcc.

References `__riemann_zeta()`.

Referenced by `__polylog_exp_int_pos()`, and `__polylog_exp_real_pos()`.

9.3.1.209 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_pos (unsigned int __s, _Tp __w)`

This function treats the cases of positive integer index s for real w.

This specialization is worthwhile to catch the differing behaviour of log(x).

$$Li_s(e^w) = \sum_{k=0, k! = s-1} \zeta(s-k) \frac{w^k}{k!} + (H_{s-1} - \log(-w)) \frac{w^{s-1}}{(s-1)!}$$

The radius of convergence is $|w| < 2\pi$. Note that this series involves a $\log(-x)$. The use of `evenzeta` yields a speedup of about 2.5. gcc and Mathematica differ in their implementation of $\log(e^{i\pi})$: gcc: $\log(e^{+i\pi}) = + - i\pi$ whereas Mathematica doesn't preserve the sign in this case: $\log(e^{+i\pi}) = +i\pi$

Parameters

$_s$	the index.
$_w$	the argument

Returns

the value of the Polylogarithm

Definition at line 221 of file sf_polylog.tcc.

References `__riemann_zeta()`.

9.3.1.210 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_pos (_Tp __s, std::complex<_Tp> __w)`

This function treats the cases of positive real index s .

The defining series is

$$Li_s(e^w) = A_s(w) + B_s(w) + \Gamma(1-s)(-w)^{s-1}$$

with

$$A_s(w) = \sum_{k=0}^m \zeta(s-k)w^k/k!$$

$$B_s(w) = \sum_{k=m+1}^{\infty} \sin(\pi/2(s-k))\Gamma(1-s+k)\zeta(1-s+k)(w/2/\pi)^k/k!$$

Parameters

<code>__s</code>	the positive real index s .
<code>__w</code>	The complex argument w .

Returns

the value of the polylogarithm.

Definition at line 572 of file `sf_polylog.tcc`.

References `__gamma()`, `__log_gamma()`, and `__riemann_zeta()`.

9.3.1.211 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_real_neg (_Tp __s, std::complex<_Tp> __w)`

Return the polylog where s is a negative real value and for complex argument. Now we branch depending on the properties of w in the specific functions

Parameters

<code>__s</code>	A negative real value that does not reduce to a negative integer.
<code>__w</code>	The complex argument.

Returns

The value of the polylogarithm.

Definition at line 982 of file `sf_polylog.tcc`.

References `__clamp_0_m2pi()`, `__clamp_pi()`, `__polylog_exp_asymp()`, `__polylog_exp_neg()`, and `__polylog_exp_negative_real_part()`.

Referenced by `__polylog_exp()`.

9.3.1.212 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_real_neg (_Tp __s, _Tp __w)`

Return the polylog where `s` is a negative real value and for real argument. Now we branch depending on the properties of `w` in the specific functions.

Parameters

<code>__s</code>	A negative real value.
<code>__w</code>	A real argument.

Returns

The value of the polylogarithm.

Definition at line 1011 of file `sf_polylog.tcc`.

References `__polylog_exp_asymp()`, `__polylog_exp_neg()`, and `__polylog_exp_negative_real_part()`.

9.3.1.213 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_real_pos (_Tp __s, std::complex<_Tp> __w)`

Return the polylog where `s` is a positive real value and for complex argument.

Parameters

<code>__s</code>	A positive real number.
<code>__w</code>	the complex argument.

Returns

The value of the polylogarithm.

Definition at line 914 of file `sf_polylog.tcc`.

References `__clamp_0_m2pi()`, `__clamp_pi()`, `__polylog_exp_asymp()`, `__polylog_exp_negative_real_part()`, `__polylog_exp_pos()`, and `__riemann_zeta()`.

Referenced by `__polylog_exp()`.

9.3.1.214 `template<typename _Tp> std::complex<_Tp> std::__detail::__polylog_exp_real_pos (_Tp __s, _Tp __w)`

Return the polylog where s is a positive real value and the argument is real.

Parameters

<code>__s</code>	A positive real number tht does not reduce to an integer.
<code>__w</code>	The real argument w.

Returns

The value of the polylogarithm.

Definition at line 951 of file `sf_polylog.tcc`.

References `__polylog_exp_asymp()`, `__polylog_exp_negative_real_part()`, `__polylog_exp_pos()`, and `__riemann_zeta()`.

9.3.1.215 `template<typename _Tp> _Tp std::__detail::__psi (unsigned int __n)`

Return the digamma function of integral argument. The digamma or $\psi(x)$ function is defined as the logarithmic derivative of the gamma function:

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

The digamma series for integral argument is given by:

$$\psi(n) = -\gamma_E + \sum_{k=1}^{\infty} \frac{1}{k}$$

The latter sum is called the harmonic number, H_n .

Definition at line 3275 of file `sf_gamma.tcc`.

References `std::__detail::__Factorial_table<_Tp>::__n`.

Referenced by `__expint_En_series()`, `__hydrogen()`, `__hyperg_reflect()`, and `__psi()`.

9.3.1.216 `template<typename _Tp> _Tp std::__detail::__psi (_Tp __x)`

Return the digamma function. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

For negative argument the reflection formula is used:

$$\psi(x) = \psi(1-x) - \pi \cot(\pi x)$$

.

Definition at line 3358 of file `sf_gamma.tcc`.

References `std::__detail::__Factorial_table<_Tp>::__n`, `__psi()`, `__psi_asymp()`, and `__tan_pi()`.

9.3.1.217 `template<typename _Tp> _Tp std::__detail::__psi (unsigned int __n, _Tp __x)`

Return the polygamma function $\psi^{(n)}(x)$.

The polygamma function is related to the Hurwitz zeta function:

$$\psi^{(n)}(x) = (-1)^{n+1} m! \zeta(m+1, x)$$

Definition at line 3423 of file sf_gamma.tcc.

References `__hurwitz_zeta()`, `__log_gamma()`, and `__psi()`.

9.3.1.218 `template<typename _Tp> _Tp std::__detail::__psi_asymp (_Tp __x)`

Return the digamma function for large argument. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

.

The asymptotic series is given by:

$$\psi(x) = \ln(x) - \frac{1}{2x} - \sum_{n=1}^{\infty} \frac{B_{2n}}{2nx^{2n}}$$

Definition at line 3327 of file sf_gamma.tcc.

Referenced by `__psi()`.

9.3.1.219 `template<typename _Tp> _Tp std::__detail::__psi_series (_Tp __x)`

Return the digamma function by series expansion. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

.

The series is given by:

$$\psi(x) = -\gamma_E - \frac{1}{x} \sum_{k=1}^{\infty} \frac{x-1}{(k+1)(x+k)}$$

Definition at line 3296 of file sf_gamma.tcc.

9.3.1.220 `template<typename _Tp> _Tp std::__detail::__qgamma (_Tp __a, _Tp __x)`

Return the regularized upper incomplete gamma function. The regularized upper incomplete gamma function is defined by

$$Q(a, x) = \frac{\Gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\Gamma(a, x) = \int_x^\infty e^{-t} t^{a-1} dt (a > 0)$$

is the upper incomplete gamma function.

Definition at line 2798 of file `sf_gamma.tcc`.

References `__gamma_cont_frac()`, and `__gamma_series()`.

Referenced by `__chi_squared_pdf()`.

9.3.1.221 `template<typename _Tp> _Tp std::__detail::__rice_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the Rice probability density function.

The formula for the Rice probability density function is

$$p(x|\nu, \sigma) = \frac{x}{\sigma^2} \exp\left(-\frac{x^2 + \nu^2}{2\sigma^2}\right) I_0\left(\frac{x\nu}{\sigma^2}\right)$$

where $I_0(x)$ is the modified Bessel function of the first kind of order 0 and $\nu \geq 0$ and $\sigma > 0$.

Definition at line 186 of file `sf_distributions.tcc`.

References `__cyl_bessel_i()`.

9.3.1.222 `template<typename _Tp> _Tp std::__detail::__riemann_zeta (_Tp __s)`

Return the Riemann zeta function $\zeta(s)$.

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} k^{-s} \text{ for } \Re s > 1 \quad \frac{(2\pi)^s}{\pi} \sin\left(\frac{\pi s}{2}\right) \Gamma(1-s) \zeta(1-s) \text{ for } \Re s < 1$$

Parameters

<code>__s</code>	The argument
------------------	--------------

Definition at line 529 of file sf_zeta.tcc.

References `__gamma()`, `__log_gamma()`, `__riemann_zeta_glob()`, `__riemann_zeta_product()`, `__riemann_zeta_sum()`, and `__sin_pi()`.

Referenced by `__dirichlet_lambda()`, `__hurwitz_zeta()`, `__polylog_exp_int_pos()`, `__polylog_exp_neg()`, `__polylog_exp_pos()`, `__polylog_exp_real_pos()`, and `evenzeta()`.

9.3.1.223 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_alt (_Tp __s)`

Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.

The series is:

$$\zeta(s) = \frac{1}{1 - 2^{1-s}} \sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n^s}$$

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } s > 1$$

For $s < 1$ use the reflection formula:

$$\zeta(s) = 2^s \pi^{s-1} \Gamma(1-s) \zeta(1-s)$$

Definition at line 347 of file sf_zeta.tcc.

9.3.1.224 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_euler_maclaurin (_Tp __s)`

Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.

This is a specialization of the code for the Hurwitz zeta function.

Definition at line 291 of file sf_zeta.tcc.

References `_S_Euler_Maclaurin_zeta`.

9.3.1.225 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_glob (_Tp __s)`

Evaluate the Riemann zeta function by series for all $s \neq 1$. Convergence is great until largish negative numbers. Then the convergence of the > 0 sum gets better.

The series is:

$$\zeta(s) = \frac{1}{1 - 2^{1-s}} \sum_{n=0}^{\infty} \frac{1}{2^{n+1}} \sum_{k=0}^n (-1)^k \frac{n!}{(n-k)!k!} (k+1)^{-s}$$

Havil 2003, p. 206.

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } s > 1$$

For $s < 1$ use the reflection formula:

$$\zeta(s) = 2^s \pi^{s-1} \Gamma(1-s) \zeta(1-s)$$

Definition at line 395 of file sf_zeta.tcc.

References `__gamma()`, and `__sin_pi()`.

Referenced by `__riemann_zeta()`.

9.3.1.226 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_m_1 (_Tp __s)`

Return the Riemann zeta function $\zeta(s) - 1$.

Parameters

$_s$	The argument $s! = 1$
-------	-----------------------

Definition at line 669 of file `sf_zeta.tcc`.

References `__riemann_zeta_m_1_sum()`, `_S_num_zetam1`, and `_S_zetam1`.

Referenced by `__polylog_exp_neg()`.

9.3.1.227 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_m_1_sum (_Tp __s)`

Return the Riemann zeta function $\zeta(s) - 1$ by summation for $s > 1$. This is a small remainder for large s .

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } \Re s > 1$$

Parameters

$_s$	The argument $s! = 1$
-------	-----------------------

Definition at line 639 of file `sf_zeta.tcc`.

Referenced by `__riemann_zeta_m_1()`.

9.3.1.228 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_product (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ using the product over prime factors.

$$\zeta(s) = \prod_{i=1}^{\infty} \frac{1}{1 - p_i^{-s}}$$

where p_i are the prime numbers.

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } \Re s > 1$$

For $s < 1$ use the reflection formula:

$$\zeta(s) = 2^s \pi^{s-1} \Gamma(1-s) \zeta(1-s)$$

Parameters

\longleftrightarrow	The argument
s	

Definition at line 489 of file sf_zeta.tcc.

Referenced by `__riemann_zeta()`.

9.3.1.229 `template<typename _Tp> _Tp std::__detail::__riemann_zeta_sum (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ by summation for $s > 1$.

The Riemann zeta function is defined by:

$$\zeta(s) = \sum_{k=1}^{\infty} \frac{1}{k^s} \text{ for } s > 1$$

For $s < 1$ use the reflection formula:

$$\zeta(s) = 2^s \pi^{s-1} \Gamma(1-s) \zeta(1-s)$$

Definition at line 257 of file sf_zeta.tcc.

Referenced by `__riemann_zeta()`.

9.3.1.230 `template<typename _Tp> _Tp std::__detail::__sin_pi (_Tp __x)`

Return the reperiodized sine of argument x:

$$\sin_{\pi}(x) = \sin(\pi x)$$

Definition at line 69 of file sf_trig.tcc.

References `__sin_pi()`.

Referenced by `__cyl_bessel_ik()`, `__cyl_bessel_jn()`, `__hankel_debye()`, `__lanczos_log_gamma1p()`, `__log_gamma()`, `__poly_laguerre_large_n()`, `__riemann_zeta()`, `__riemann_zeta_glob()`, `__sinc_pi()`, and `__spouge_log_gamma1p()`.

9.3.1.231 `template<typename _Tp> std::complex<_Tp> std::__detail::__sin_pi (std::complex<_Tp> __z)`

Return the reperiodized sine of complex argument z:

$$\sin_{\pi}(z) = \sin(\pi z) = \sin_{\pi}(x) \cosh_{\pi}(y) + i \cos_{\pi}(x) \sinh_{\pi}(y)$$

Definition at line 199 of file sf_trig.tcc.

References `__cos_pi()`.

Referenced by `__cos_pi()`, `__cosh_pi()`, `__sin_pi()`, and `__sinh_pi()`.

9.3.1.232 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::__detail::__sinc (_Tp __x)`

Return the sinus cardinal function

$$\text{sinc}(x) = \frac{\sin(x)}{x}$$

.

Definition at line 51 of file sf_cardinal.tcc.

9.3.1.233 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::__detail::__sinc_pi (_Tp __x)`

Return the reperiodized sinus cardinal function

$$\text{sinc}_{\pi}(x) = \frac{\sin(\pi x)}{\pi x}$$

.

Definition at line 71 of file sf_cardinal.tcc.

References `__sin_pi()`.

9.3.1.234 `template<typename _Tp> __gnu_cxx::__sincos_t<_Tp> std::__detail::__sincos (_Tp __x) [inline]`

Definition at line 319 of file sf_trig.tcc.

9.3.1.235 `template<> __gnu_cxx::__sincos_t<float> std::__detail::__sincos (float __x) [inline]`

Definition at line 327 of file sf_trig.tcc.

9.3.1.236 `template<> __gnu_cxx::__sincos_t<double> std::__detail::__sincos (double __x) [inline]`

Definition at line 339 of file sf_trig.tcc.

9.3.1.237 `template<> __gnu_cxx::__sincos_t<long double> std::__detail::__sincos (long double __x) [inline]`

Definition at line 351 of file sf_trig.tcc.

Referenced by `__sincos_pi()`.

9.3.1.238 `template<typename _Tp> __gnu_cxx::__sincos_t<_Tp> std::__detail::__sincos_pi (_Tp __x)`

Reperiodized sincos.

Definition at line 363 of file `sf_trig.tcc`.

References `__sincos()`, `__gnu_cxx::__sincos_t<_Tp>::cos_value`, and `__gnu_cxx::__sincos_t<_Tp>::sin_value`.

Referenced by `__polar_pi()`.

9.3.1.239 `template<typename _Tp> std::pair<_Tp, _Tp> std::__detail::__sincosint (_Tp __x)`

This function returns the sine $Si(x)$ and cosine $Ci(x)$ integrals as a `pair`.

The sine integral is defined by:

$$Si(x) = \int_0^x dt \frac{\sin(t)}{t}$$

The cosine integral is defined by:

$$Ci(x) = \gamma_E + \log(x) + \int_0^x dt \frac{\cos(t) - 1}{t}$$

Definition at line 226 of file `sf_trigint.tcc`.

References `__sincosint_asymp()`, `__sincosint_cont_frac()`, and `__sincosint_series()`.

9.3.1.240 `template<typename _Tp> void std::__detail::__sincosint_asymp (_Tp __t, _Tp &_Si, _Tp &_Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by asymptotic series summation for positive argument.

The asymptotic series is very good for $x > 50$.

Definition at line 159 of file `sf_trigint.tcc`.

Referenced by `__sincosint()`.

9.3.1.241 `template<typename _Tp> void std::__detail::__sincosint_cont_frac (_Tp __t, _Tp &_Si, _Tp &_Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by continued fraction for positive argument.

Definition at line 52 of file `sf_trigint.tcc`.

Referenced by `__sincosint()`.

9.3.1.242 `template<typename _Tp> void std::__detail::__sincosint_series (_Tp __t, _Tp & _Si, _Tp & _Ci)`

This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by series summation for positive argument.

Definition at line 95 of file `sf_trigint.tcc`.

Referenced by `__sincosint()`.

9.3.1.243 `template<typename _Tp> _Tp std::__detail::__sinh_pi (_Tp __x)`

Return the reperiodized hyperbolic sine of argument x:

$$\sinh_{\pi}(x) = \sinh(\pi x)$$

Definition at line 100 of file `sf_trig.tcc`.

References `__sinh_pi()`.

Referenced by `__sinhc_pi()`.

9.3.1.244 `template<typename _Tp> std::complex<_Tp> std::__detail::__sinh_pi (std::complex<_Tp> __z)`

Return the reperiodized hyperbolic sine of complex argument z:

$$\sinh_{\pi}(z) = \sinh(\pi z) = \sinh(\pi x) \cos_{\pi}(y) + i \cosh(\pi x) \sin_{\pi}(y)$$

Definition at line 220 of file `sf_trig.tcc`.

References `__cos_pi()`, and `__sin_pi()`.

Referenced by `__sinh_pi()`.

9.3.1.245 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::__detail::__sinhc (_Tp __x)`

Return the hyperbolic sinus cardinal function

$$\operatorname{sinhc}(x) = \frac{\sinh(x)}{x}$$

.

Definition at line 96 of file `sf_cardinal.tcc`.

9.3.1.246 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::__detail::__sinhc_pi (_Tp __x)`

Return the reperiodized hyperbolic sinus cardinal function

$$\operatorname{sinhc}_{\pi}(x) = \frac{\sinh(\pi x)}{\pi x}$$

.

Definition at line 114 of file sf_cardinal.tcc.

References `__sinh_pi()`.

9.3.1.247 `template<typename _Tp> _Tp std::__detail::__sinhint (const _Tp __x)`

Return the hyperbolic sine integral $Shi(x)$.

The hyperbolic sine integral is given by

$$Shi(x) = (Ei(x) + E_1(x))/2 = (Ei(x) - Ei(-x))/2$$

Parameters

\leftrightarrow _x	The argument of the hyperbolic sine integral function.
-------------------------	--

Returns

The hyperbolic sine integral.

Definition at line 584 of file sf_expint.tcc.

References `__expint_E1()`, and `__expint_Ei()`.

9.3.1.248 `template<typename _Tp> _Tp std::__detail::__sph_bessel (unsigned int __n, _Tp __x)`

Return the spherical Bessel function $j_n(x)$ of order n and non-negative real argument x .

The spherical Bessel function is defined by:

$$j_n(x) = \left(\frac{\pi}{2x}\right)^{1/2} J_{n+1/2}(x)$$

Parameters

\leftrightarrow _n	The non-negative integral order
\leftrightarrow _x	The non-negative real argument

Returns

The output spherical Bessel function.

Definition at line 754 of file sf_bessel.tcc.

References `__sph_bessel_jn()`.

9.3.1.249 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_bessel (unsigned int __n, std::complex<_Tp> __z)`

Return the complex spherical Bessel function.

Parameters

in	\leftrightarrow _n	The order for which the spherical Bessel function is evaluated.
in	\leftrightarrow _z	The argument at which the spherical Bessel function is evaluated.

Returns

The complex spherical Bessel function.

Definition at line 1274 of file sf_hankel.tcc.

References `__sph_hankel()`.

9.3.1.250 `template<typename _Tp> __gnu_cxx::__sph_mod_bessel_t<unsigned int, _Tp, _Tp> std::__detail::__sph_bessel_ik (unsigned int __n, _Tp __x)`

Compute the spherical modified Bessel functions $i_n(x)$ and $k_n(x)$ and their first derivatives $i'_n(x)$ and $k'_n(x)$ respectively.

Parameters

\longleftrightarrow __n	The order of the modified spherical Bessel function.
\longleftrightarrow __x	The argument of the modified spherical Bessel function.

Returns

A struct containing the modified spherical Bessel functions of the first and second kinds and their derivatives.

Definition at line 421 of file sf_mod_bessel.tcc.

References `__cyl_bessel_ik()`.

9.3.1.251 `template<typename _Tp> __gnu_cxx::__sph_bessel_t<unsigned int, _Tp, _Tp> std::__detail::__sph_bessel_jn (unsigned int __n, _Tp __x)`

Compute the spherical Bessel $j_n(x)$ and Neumann $n_n(x)$ functions and their first derivatives $j'_n(x)$ and $n'_n(x)$ respectively.

Parameters

\longleftrightarrow __n	The order of the spherical Bessel function.
\longleftrightarrow __x	The argument of the spherical Bessel function.

Returns

The output derivative of the spherical Neumann function.

Definition at line 689 of file sf_bessel.tcc.

References `__cyl_bessel_jn()`.

Referenced by `__sph_bessel()`, `__sph_hankel_1()`, `__sph_hankel_2()`, and `__sph_neumann()`.

9.3.1.252 `template<typename _Tp> __gnu_cxx::__sph_bessel_t<unsigned int, _Tp, std::complex<_Tp>> >
std::__detail::__sph_bessel_jn_neg_arg (unsigned int __n, _Tp __x)`

Return the spherical Bessel functions and their derivatives of order ν and argument $x < 0$.

Definition at line 713 of file `sf_bessel.tcc`.

References `__cyl_bessel_jn_neg_arg()`.

Referenced by `__sph_hankel_1()`, and `__sph_hankel_2()`.

9.3.1.253 `template<typename _Tp> __gnu_cxx::__sph_hankel_t<unsigned int, std::complex<_Tp>, std::complex<_Tp>> >
std::__detail::__sph_hankel (unsigned int __n, std::complex<_Tp> __z)`

Helper to compute complex spherical Hankel functions and their derivatives.

Parameters

in	<code>__n</code>	The order for which the spherical Hankel functions are evaluated.
in	<code>__z</code>	The argument at which the spherical Hankel functions are evaluated.

Returns

A struct containing the spherical Hankel functions of the first and second kinds and their derivatives.

Definition at line 1210 of file `sf_hankel.tcc`.

References `__hankel()`.

Referenced by `__sph_bessel()`, `__sph_hankel_1()`, `__sph_hankel_2()`, and `__sph_neumann()`.

9.3.1.254 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_hankel_1 (unsigned int __n, _Tp __x)`

Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$.

The spherical Hankel function of the first kind is defined by:

$$h_n^{(1)}(x) = j_n(x) + in_n(x)$$

Parameters

\leftrightarrow _n	The order of the spherical Neumann function.
\leftrightarrow _x	The argument of the spherical Neumann function.

Returns

The output spherical Neumann function.

Definition at line 815 of file sf_bessel.tcc.

References `__sph_bessel_jn()`, and `__sph_bessel_jn_neg_arg()`.

9.3.1.255 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_hankel_1 (unsigned int __n, std::complex<_Tp> > __z)`

Return the complex spherical Hankel function of the first kind.

Parameters

in	\leftrightarrow _n	The order for which the spherical Hankel function of the first kind is evaluated.
in	\leftrightarrow _z	The argument at which the spherical Hankel function of the first kind is evaluated.

Returns

The complex spherical Hankel function of the first kind.

Definition at line 1240 of file sf_hankel.tcc.

References `__sph_hankel()`.

9.3.1.256 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_hankel_2 (unsigned int __n, _Tp __x)`

Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$.

The spherical Hankel function of the second kind is defined by:

$$h_n^{(2)}(x) = j_n(x) - in_n(x)$$

Parameters

\leftrightarrow _n	The non-negative integral order
\leftrightarrow _x	The non-negative real argument

Returns

The output spherical Neumann function.

Definition at line 849 of file sf_bessel.tcc.

References `__sph_bessel_jn()`, and `__sph_bessel_jn_neg_arg()`.

9.3.1.257 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_hankel_2 (unsigned int __n, std::complex<_Tp> __z)`

Return the complex spherical Hankel function of the second kind.

Parameters

in	\leftrightarrow _n	The order for which the spherical Hankel function of the second kind is evaluated.
in	\leftrightarrow _z	The argument at which the spherical Hankel function of the second kind is evaluated.

Returns

The complex spherical Hankel function of the second kind.

Definition at line 1257 of file sf_hankel.tcc.

References `__sph_hankel()`.

9.3.1.258 `template<typename _Tp> std::complex<_Tp> std::__detail::__sph_harmonic (unsigned int __l, int __m, _Tp __theta, _Tp __phi)`

Return the spherical harmonic function.

The spherical harmonic function of l , m , and θ , ϕ is defined by:

$$Y_l^m(\theta, \phi) = (-1)^m \left[\frac{(2l+1)}{4\pi} \frac{(l-m)!}{(l+m)!} \right] P_l^{|m|}(\cos \theta) \exp^{im\phi}$$

Parameters

<code>__l</code>	The order of the spherical harmonic function. $l \geq 0$.
<code>__m</code>	The order of the spherical harmonic function. $m \leq l$.
<code>__theta</code>	The radian polar angle argument of the spherical harmonic function.
<code>__phi</code>	The radian azimuthal angle argument of the spherical harmonic function.

Definition at line 349 of file `sf_legendre.tcc`.

References `__sph_legendre()`.

9.3.1.259 `template<typename _Tp> _Tp std::__detail::__sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta)`

Return the spherical associated Legendre function.

The spherical associated Legendre function of l , m , and θ is defined as $Y_l^m(\theta, 0)$ where

$$Y_l^m(\theta, \phi) = (-1)^m \left[\frac{(2l+1)}{4\pi} \frac{(l-m)!}{(l+m)!} \right] P_l^m(\cos \theta) \exp^{im\phi}$$

is the spherical harmonic function and $P_l^m(x)$ is the associated Legendre function.

This function differs from the associated Legendre function by argument ($x = \cos(\theta)$) and by a normalization factor but this factor is rather large for large l and m and so this function is stable for larger differences of l and m .

Parameters

<code>__l</code>	The order of the spherical associated Legendre function. $l \geq 0$.
<code>__m</code>	The order of the spherical associated Legendre function. $m \leq l$.
<code>__theta</code>	The radian polar angle argument of the spherical associated Legendre function.

Definition at line 252 of file `sf_legendre.tcc`.

References `__log_gamma()`, and `__poly_legendre_p()`.

Referenced by `__hydrogen()`, and `__sph_harmonic()`.

9.3.1.260 `template<typename _Tp> _Tp std::__detail::__sph_neumann (unsigned int __n, _Tp __x)`

Return the spherical Neumann function $n_n(x)$ of order n and non-negative real argument x .

The spherical Neumann function is defined by:

$$n_n(x) = \left(\frac{\pi}{2x} \right)^{1/2} N_{n+1/2}(x)$$

Parameters

\leftrightarrow _n	The order of the spherical Neumann function.
\leftrightarrow _x	The argument of the spherical Neumann function.

Returns

The output spherical Neumann function.

Definition at line 787 of file sf_bessel.tcc.

References __sph_bessel_jn().

```
9.3.1.261  template<typename _Tp > std::complex<_Tp> std::_detail::__sph_neumann ( unsigned int __n, std::complex<_Tp>
> __z )
```

Return the complex spherical Neumann function.

Parameters

in	\leftrightarrow _n	The order for which the spherical Neumann function is evaluated.
in	\leftrightarrow _z	The argument at which the spherical Neumann function is evaluated.

Returns

The complex spherical Neumann function.

Definition at line 1291 of file sf_hankel.tcc.

References __sph_hankel().

```
9.3.1.262  template<typename _Tp > _GLIBCXX14_CONSTEXPR _Tp std::_detail::__spouge_binet1p ( _Tp __z )
```

Return the Binet function $J(1+z)$ by the Spouge method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^*(z))$ defined by

$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

Parameters

<code>_↔_z</code>	The argument of the log of the gamma function.
-------------------	--

Returns

The logarithm of the gamma function.

Definition at line 2008 of file sf_gamma.tcc.

Referenced by __spouge_log_gamma1p().

9.3.1.263 `template<typename _Tp > _GLIBCXX14_CONSTEXPR _Tp std::__detail::__spouge_log_gamma1p (_Tp __z)`

Return the logarithm of the gamma function $\log(\Gamma(1+z))$ by the Spouge algorithm:

$$\Gamma(z+1) = (z+a)^{z+1/2} e^{-z-a} \left[\sqrt{2\pi} + \sum_{k=1}^{\lceil a \rceil + 1} \frac{c_k(a)}{z+k} \right]$$

where

$$c_k(a) = \frac{(-1)^{k-1}}{(k-1)!} (a-k)^{k-1/2} e^{a-k}$$

and the error is bounded by

$$\epsilon(a) < a^{-1/2} (2\pi)^{-a-1/2}$$

.

If the argument is real, the log of the absolute value of the Gamma function is returned. The sign to be applied to the exponential of this log Gamma can be recovered with a call to __log_gamma_sign.

For complex argument the fully complex log of the gamma function is returned.

See also

Spouge, J. L., Computation of the gamma, digamma, and trigamma functions. SIAM Journal on Numerical Analysis 31, 3 (1994), pp. 931-944

Parameters

<code>_↔_z</code>	The argument of the gamma function.
-------------------	-------------------------------------

Returns

The the gamma function.

Definition at line 2052 of file sf_gamma.tcc.

References `__sin_pi()`, and `__spouge_binet1p()`.

Referenced by `__log_gamma()`.

9.3.1.264 `template<typename _Tp> _Tp std::__detail::__student_t_cdf (_Tp __t, unsigned int __nu)`

Return the Students T probability function.

The students T propability function is related to the incomplete beta function:

$$A(t|\nu) = 1 - I_{\frac{\nu}{\nu+t^2}}\left(\frac{\nu}{2}, \frac{1}{2}\right)A(t|\nu) =$$

Parameters

<code>__t</code>	
<code>__nu</code>	

Definition at line 419 of file `sf_distributions.tcc`.

References `__beta_inc()`.

9.3.1.265 `template<typename _Tp> _Tp std::__detail::__student_t_cdfc (_Tp __t, unsigned int __nu)`

Return the complement of the Students T probability function.

The complement of the students T propability function is:

$$A_c(t|\nu) = I_{\frac{\nu}{\nu+t^2}}\left(\frac{\nu}{2}, \frac{1}{2}\right) = 1 - A(t|\nu)$$

Parameters

<code>__t</code>	
<code>__nu</code>	

Definition at line 442 of file `sf_distributions.tcc`.

References `__beta_inc()`.

9.3.1.266 `template<typename _Tp> _Tp std::__detail::__tan_pi (_Tp __x)`

Return the reperiodized tangent of argument x:

$$\tan_p i(x) = \tan(\pi x)$$

Definition at line 166 of file `sf_trig.tcc`.

Referenced by `__psi()`.

9.3.1.267 `template<typename _Tp> std::complex<_Tp> std::__detail::__tan_pi (std::complex<_Tp> __z)`

Return the reperiodized tangent of complex argument z:

$$\tan_{\pi}(z) = \tan(\pi z) = \frac{\tan_{\pi}(x) + i \tanh_{\pi}(y)}{1 - i \tan_{\pi}(x) \tanh_{\pi}(y)}$$

Definition at line 279 of file sf_trig.tcc.

Referenced by `__tanh_pi()`.

9.3.1.268 `template<typename _Tp> _Tp std::__detail::__tanh_pi (_Tp __x)`

Return the reperiodized hyperbolic tangent of argument x:

$$\tanh_{\pi}(x) = \tanh(\pi x)$$

Definition at line 182 of file sf_trig.tcc.

9.3.1.269 `template<typename _Tp> std::complex<_Tp> std::__detail::__tanh_pi (std::complex<_Tp> __z)`

Return the reperiodized hyperbolic tangent of complex argument z:

$$\tanh_{\pi}(z) = \tanh(\pi z) = \frac{\tanh_{\pi}(x) + i \tan_{\pi}(y)}{1 + i \tanh_{\pi}(x) \tan_{\pi}(y)}$$

Definition at line 301 of file sf_trig.tcc.

References `__tan_pi()`.

9.3.1.270 `template<typename _Tp> _Tp std::__detail::__tgamma (_Tp __a, _Tp __x)`

Return the upper incomplete gamma function. The lower incomplete gamma function is defined by

$$\Gamma(a, x) = \int_x^{\infty} e^{-t} t^{a-1} dt (a > 0)$$

.

Definition at line 2862 of file sf_gamma.tcc.

References `__gamma_cont_frac()`, and `__gamma_series()`.

Referenced by `__gamma_cdfc()`.

9.3.1.271 `template<typename _Tp> _Tp std::__detail::__tgamma_lower (_Tp __a, _Tp __x)`

Return the lower incomplete gamma function. The lower incomplete gamma function is defined by

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

.

Definition at line 2827 of file `sf_gamma.tcc`.

References `__gamma_cont_frac()`, and `__gamma_series()`.

Referenced by `__gamma_cdf()`.

9.3.1.272 `template<typename _Tp> _Tp std::__detail::__theta_1 (_Tp __nu, _Tp __x)`

Return the exponential theta-1 function of period `nu` and argument `x`.

The Neville theta-1 function is defined by

$$\theta_1(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} (-1)^j \exp\left(\frac{-(\nu + j - 1/2)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 2) argument
<code>__x</code>	The argument

Definition at line 192 of file `sf_theta.tcc`.

References `__theta_2()`.

Referenced by `__theta_s()`.

9.3.1.273 `template<typename _Tp> _Tp std::__detail::__theta_2 (_Tp __nu, _Tp __x)`

Return the exponential theta-2 function of period `nu` and argument `x`.

The exponential theta-2 function is defined by

$$\theta_2(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} (-1)^j \exp\left(\frac{-(\nu + j)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 2) argument
<code>__x</code>	The argument

Definition at line 164 of file sf_theta.tcc.

References `__theta_2_asymp()`, and `__theta_2_sum()`.

Referenced by `__theta_1()`, and `__theta_c()`.

9.3.1.274 `template<typename _Tp> _Tp std::__detail::__theta_2_asyp (_Tp __nu, _Tp __x)`

Compute and return the θ_2 function by series expansion.

Definition at line 105 of file sf_theta.tcc.

Referenced by `__theta_2()`.

9.3.1.275 `template<typename _Tp> _Tp std::__detail::__theta_2_sum (_Tp __nu, _Tp __x)`

Compute and return the θ_1 function by series expansion.

Definition at line 51 of file sf_theta.tcc.

Referenced by `__theta_2()`.

9.3.1.276 `template<typename _Tp> _Tp std::__detail::__theta_3 (_Tp __nu, _Tp __x)`

Return the exponential theta-3 function of period `nu` and argument `x`.

The exponential theta-3 function is defined by

$$\theta_3(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} \exp\left(\frac{-(\nu + j)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 1) argument
<code>__x</code>	The argument

Definition at line 218 of file sf_theta.tcc.

References `__theta_3_asymp()`, and `__theta_3_sum()`.

Referenced by `__theta_4()`, and `__theta_d()`.

9.3.1.277 `template<typename _Tp> _Tp std::__detail::__theta_3_asymp (_Tp __nu, _Tp __x)`

Compute and return the θ_3 function by asymptotic series expansion.

Definition at line 130 of file `sf_theta.tcc`.

Referenced by `__theta_3()`.

9.3.1.278 `template<typename _Tp> _Tp std::__detail::__theta_3_sum (_Tp __nu, _Tp __x)`

Compute and return the θ_3 function by series expansion.

Definition at line 79 of file `sf_theta.tcc`.

Referenced by `__theta_3()`.

9.3.1.279 `template<typename _Tp> _Tp std::__detail::__theta_4 (_Tp __nu, _Tp __x)`

Return the exponential theta-2 function of period `nu` and argument `x`.

The exponential theta-2 function is defined by

$$\theta_2(\nu, x) = \frac{1}{\sqrt{\pi x}} \sum_{j=-\infty}^{+\infty} (-1)^j \exp\left(\frac{-(\nu + j)^2}{x}\right)$$

Parameters

<code>__nu</code>	The periodic (period = 2) argument
<code>__x</code>	The argument

Definition at line 246 of file `sf_theta.tcc`.

References `__theta_3()`.

Referenced by `__theta_n()`.

9.3.1.280 `template<typename _Tp> _Tp std::__detail::__theta_c (_Tp __k, _Tp __x)`

Return the Neville θ_c function

Definition at line 339 of file `sf_theta.tcc`.

References `__comp_ellint_1()`, `__ellnome()`, and `__theta_2()`.

9.3.1.281 `template<typename _Tp> _Tp std::__detail::__theta_d (_Tp __k, _Tp __x)`

Return the Neville θ_d function

Definition at line 364 of file `sf_theta.tcc`.

References `__comp_ellint_1()`, `__ellnome()`, and `__theta_3()`.

9.3.1.282 `template<typename _Tp> _Tp std::__detail::__theta_n (_Tp __k, _Tp __x)`

Return the Neville θ_n function

Definition at line 389 of file `sf_theta.tcc`.

References `__comp_ellint_1()`, `__ellnome()`, and `__theta_4()`.

9.3.1.283 `template<typename _Tp> _Tp std::__detail::__theta_s (_Tp __k, _Tp __x)`

Return the Neville θ_s function

Definition at line 313 of file `sf_theta.tcc`.

References `__comp_ellint_1()`, `__ellnome()`, and `__theta_1()`.

9.3.1.284 `template<typename _Tp> _Tp std::__detail::__weibull_cdf (_Tp __a, _Tp __b, _Tp __x)`

Return the Weibull cumulative probability density function.

The formula for the Weibull cumulative probability density function is

$$F(x|\lambda) = 1 - e^{-(x/b)^a} \text{ for } x \geq 0$$

Definition at line 395 of file `sf_distributions.tcc`.

9.3.1.285 `template<typename _Tp> _Tp std::__detail::__weibull_pdf (_Tp __a, _Tp __b, _Tp __x)`

Return the Weibull probability density function.

The formula for the Weibull probability density function is

$$f(x|a, b) = \frac{a}{b} \left(\frac{x}{b}\right)^{a-1} \exp - \left(\frac{x}{b}\right)^a \text{ for } x \geq 0$$

Definition at line 374 of file `sf_distributions.tcc`.

9.3.1.286 `template<typename _Tp> __gnu_cxx::__promote_fp_t<_Tp> std::__detail::__zernike (unsigned int __n, int __m, _Tp __rho, _Tp __phi)`

Return the Zernicke polynomial $Z_n^m(\rho, \phi)$ for non-negative integral degree n , signed integral order m , and real radial argument ρ and azimuthal angle ϕ .

The even Zernicke polynomials are defined by:

$$Z_n^m(\rho, \phi) = R_n^m(\rho) \cos(m\phi)$$

and the odd Zernicke polynomials are defined by:

$$Z_n^{-m}(\rho, \phi) = R_n^m(\rho) \sin(m\phi)$$

for non-negative degree m and $m \leq n$ and where $R_n^m(\rho)$ is the radial polynomial (

See also

[__poly_radial_jacobi](#)).

Principals of Optics, 7th edition, Max Born and Emil Wolf, Cambridge University Press, 1999, pp 523-525 and 905-910.

Template Parameters

<code>_Tp</code>	The real type of the radial coordinate and azimuthal angle
------------------	--

Parameters

<code>__n</code>	The non-negative integral degree.
<code>__m</code>	The integral azimuthal order
<code>__rho</code>	The radial coordinate
<code>__phi</code>	The azimuthal angle

Definition at line 193 of file `sf_jacobi.tcc`.

References `__poly_radial_jacobi()`.

9.3.1.287 `template<typename _Tp> _Tp std::__detail::__znorm1 (_Tp __x)`

Definition at line 58 of file `sf_owens.t.tcc`.

Referenced by `__owens_t()`.

9.3.1.288 `template<typename _Tp> _Tp std::__detail::__znorm2 (_Tp __x)`

Definition at line 47 of file `sf_owens.t.tcc`.

Referenced by `__owens_t()`.

9.3.1.289 `template<typename _Tp = double> _Tp std::__detail::evenzeta (unsigned int __k)`

A function to calculate the values of zeta at even positive integers. For values smaller than thirty a table is used.

Parameters

<code>__k</code>	an integer at which we evaluate the Riemann zeta function.
------------------	--

Returns

$\zeta(k)$

Definition at line 92 of file sf_polylog.tcc.

References `__riemann_zeta()`.

9.3.2 Variable Documentation

9.3.2.1 `template<typename _Tp> constexpr int std::__detail::__max_FGH = _Airy_series<_Tp>::_N_FGH`

Definition at line 179 of file sf_airy.tcc.

9.3.2.2 `template<> constexpr int std::__detail::__max_FGH< double > = 79`

Definition at line 185 of file sf_airy.tcc.

9.3.2.3 `template<> constexpr int std::__detail::__max_FGH< float > = 15`

Definition at line 182 of file sf_airy.tcc.

9.3.2.4 `constexpr size_t std::__detail::_Num_Euler_Maclaurin_zeta = 100`

Coefficients for Euler-Maclaurin summation of zeta functions.

$$B_{2j}/(2j)!$$

where B_k are the Bernoulli numbers.

Definition at line 67 of file sf_zeta.tcc.

9.3.2.5 `constexpr _Factorial_table<long double> std::__detail::_S_double_factorial_table[301]`

Definition at line 278 of file `sf_gamma.tcc`.

Referenced by `__double_factorial()`, and `__log_double_factorial()`.

9.3.2.6 `constexpr long double std::__detail::_S_Euler_Maclaurin_zeta[_Num_Euler_Maclaurin_zeta]`

Definition at line 70 of file `sf_zeta.tcc`.

Referenced by `__hurwitz_zeta_euler_maclaurin()`, and `__riemann_zeta_euler_maclaurin()`.

9.3.2.7 `constexpr _Factorial_table<long double> std::__detail::_S_factorial_table[171]`

Definition at line 88 of file `sf_gamma.tcc`.

Referenced by `__factorial()`, `__gamma()`, `__log_factorial()`, and `__log_gamma()`.

9.3.2.8 `constexpr unsigned long long std::__detail::_S_harmonic_denom[_S_num_harmonic_numer]`

Definition at line 3210 of file `sf_gamma.tcc`.

Referenced by `__harmonic_number()`.

9.3.2.9 `constexpr unsigned long long std::__detail::_S_harmonic_numer[_S_num_harmonic_numer]`

Definition at line 3177 of file `sf_gamma.tcc`.

Referenced by `__harmonic_number()`.

9.3.2.10 `constexpr _Factorial_table<long double> std::__detail::_S_neg_double_factorial_table[999]`

Definition at line 599 of file `sf_gamma.tcc`.

Referenced by `__double_factorial()`, and `__log_double_factorial()`.

9.3.2.11 `template<typename _Tp> constexpr std::size_t std::__detail::_S_num_double_factorials = 0`

Definition at line 263 of file `sf_gamma.tcc`.

9.3.2.12 `template<> constexpr std::size_t std::__detail::_S_num_double_factorials< double > = 301`

Definition at line 268 of file `sf_gamma.tcc`.

9.3.2.13 `template<> constexpr std::size_t std::__detail::_S_num_double_factorials< float > = 57`

Definition at line 266 of file `sf_gamma.tcc`.

9.3.2.14 `template<> constexpr std::size_t std::__detail::_S_num_double_factorials< long double > = 301`

Definition at line 270 of file `sf_gamma.tcc`.

9.3.2.15 `template<typename _Tp > constexpr std::size_t std::__detail::_S_num_factorials = 0`

Definition at line 73 of file `sf_gamma.tcc`.

9.3.2.16 `template<> constexpr std::size_t std::__detail::_S_num_factorials< double > = 171`

Definition at line 78 of file `sf_gamma.tcc`.

9.3.2.17 `template<> constexpr std::size_t std::__detail::_S_num_factorials< float > = 35`

Definition at line 76 of file `sf_gamma.tcc`.

9.3.2.18 `template<> constexpr std::size_t std::__detail::_S_num_factorials< long double > = 171`

Definition at line 80 of file `sf_gamma.tcc`.

9.3.2.19 `constexpr unsigned long long std::__detail::_S_num_harmonic_numer = 29`

Definition at line 3174 of file `sf_gamma.tcc`.

Referenced by `__harmonic_number()`.

9.3.2.20 `template<typename _Tp > constexpr std::size_t std::__detail::_S_num_neg_double_factorials = 0`

Definition at line 583 of file `sf_gamma.tcc`.

9.3.2.21 `template<> constexpr std::size_t std::__detail::_S_num_neg_double_factorials< double > = 150`

Definition at line 588 of file `sf_gamma.tcc`.

9.3.2.22 `template<> constexpr std::size_t std::__detail::_S_num_neg_double_factorials< float > = 27`

Definition at line 586 of file `sf_gamma.tcc`.

9.3.2.23 `template<> constexpr std::size_t std::__detail::_S_num_neg_double_factorials< long double > = 999`

Definition at line 590 of file `sf_gamma.tcc`.

9.3.2.24 `constexpr size_t std::__detail::_S_num_zetam1 = 41`

Table of $\zeta(n) - 1$ from 0 - 40. MPFR - 128 bits.

Definition at line 578 of file `sf_zeta.tcc`.

Referenced by `__riemann_zeta_m_1()`.

9.3.2.25 `constexpr long double std::__detail::_S_zetam1[_S_num_zetam1]`

Definition at line 582 of file `sf_zeta.tcc`.

Referenced by `__riemann_zeta_m_1()`.

Chapter 10

Class Documentation

10.1 `__gnu_cxx::__sincos_t<_Tp>` Struct Template Reference

Public Attributes

- `_Tp cos_value`
- `_Tp sin_value`

10.1.1 Detailed Description

```
template<typename _Tp>
struct __gnu_cxx::__sincos_t<_Tp>
```

A struct to store a cosine and a sine value.

Definition at line 45 of file `sf_trig.tcc`.

10.1.2 Member Data Documentation

10.1.2.1 `template<typename _Tp> _Tp __gnu_cxx::__sincos_t<_Tp>::cos_value`

Definition at line 48 of file `sf_trig.tcc`.

Referenced by `std::__detail::__polar_pi()`, and `std::__detail::__sincos_pi()`.

10.1.2.2 `template<typename _Tp> _Tp __gnu_cxx::__sincos_t<_Tp>::sin_value`

Definition at line 47 of file `sf_trig.tcc`.

Referenced by `std::__detail::__polar_pi()`, and `std::__detail::__sincos_pi()`.

The documentation for this struct was generated from the following file:

- `bits/sf_trig.tcc`

10.2 `std::__detail::__gamma_lanczos_data< _Tp >` Struct Template Reference

10.2.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::__gamma_lanczos_data< _Tp >
```

A struct for Lanczos algorithm Chebyshev arrays of coefficients.

Definition at line 2085 of file `sf_gamma.tcc`.

The documentation for this struct was generated from the following file:

- [bits/sf_gamma.tcc](#)

10.3 `std::__detail::__gamma_lanczos_data< double >` Struct Template Reference

Static Public Attributes

- static constexpr `std::array< double, 10 >` [_S_cheby](#)
- static constexpr `double` [_S_g](#) = 9.5

10.3.1 Detailed Description

```
template<>
struct std::__detail::__gamma_lanczos_data< double >
```

Definition at line 2107 of file `sf_gamma.tcc`.

10.3.2 Member Data Documentation

10.3.2.1 `constexpr std::array<double, 10> std::__detail::__gamma_lanczos_data< double >::_S_cheby` `[static]`

Initial value:

```
{
    5.557569219204146e+03,
    -4.248114953727554e+03,
    1.881719608233706e+03,
    -4.705537221412237e+02,
    6.325224688788239e+01,
    -4.206901076213398e+00,
    1.202512485324405e-01,
    -1.141081476816908e-03,
    2.055079676210880e-06,
    1.280568540096283e-09,
}
```

Definition at line 2112 of file `sf_gamma.tcc`.

10.3.2.2 constexpr double std::__detail::__gamma_lanczos_data< double >::_S_g = 9.5 [static]

Definition at line 2109 of file sf_gamma.tcc.

The documentation for this struct was generated from the following file:

- bits/sf_gamma.tcc

10.4 std::__detail::__gamma_lanczos_data< float > Struct Template Reference

Static Public Attributes

- static constexpr std::array< float, 7 > _S_cheby
- static constexpr float _S_g = 6.5F

10.4.1 Detailed Description

```
template<>
struct std::__detail::__gamma_lanczos_data< float >
```

Definition at line 2090 of file sf_gamma.tcc.

10.4.2 Member Data Documentation

10.4.2.1 constexpr std::array<float, 7> std::__detail::__gamma_lanczos_data< float >::_S_cheby [static]

Initial value:

```
{
    3.307139e+02F,
    -2.255998e+02F,
    6.989520e+01F,
    -9.058929e+00F,
    4.110107e-01F,
    -4.150391e-03F,
    -3.417969e-03F,
}
```

Definition at line 2095 of file sf_gamma.tcc.

10.4.2.2 constexpr float std::__detail::__gamma_lanczos_data< float >::_S_g = 6.5F [static]

Definition at line 2092 of file sf_gamma.tcc.

The documentation for this struct was generated from the following file:

- bits/sf_gamma.tcc

10.5 `std::__detail::__gamma_lanczos_data< long double >` Struct Template Reference

Static Public Attributes

- static constexpr `std::array< long double, 11 >` [_S_cheby](#)
- static constexpr `long double` [_S_g](#) = 10.5L

10.5.1 Detailed Description

```
template<>
struct std::__detail::__gamma_lanczos_data< long double >
```

Definition at line 2127 of file `sf_gamma.tcc`.

10.5.2 Member Data Documentation

10.5.2.1 `constexpr std::array<long double, 11> std::__detail::__gamma_lanczos_data< long double >::_S_cheby`
[static]

Initial value:

```
{
    1.440399692024250728e+04L,
    -1.128006201837065341e+04L,
    5.384108670160999829e+03L,
    -1.536234184127325861e+03L,
    2.528551924697309561e+02L,
    -2.265389090278717887e+01L,
    1.006663776178612579e+00L,
    -1.900805731354182626e-02L,
    1.150508317664389324e-04L,
    -1.208915136885480024e-07L,
    -1.518856151960790157e-10L,
}
```

Definition at line 2132 of file `sf_gamma.tcc`.

10.5.2.2 `constexpr long double std::__detail::__gamma_lanczos_data< long double >::_S_g = 10.5L` [static]

Definition at line 2129 of file `sf_gamma.tcc`.

The documentation for this struct was generated from the following file:

- `bits/sf_gamma.tcc`

10.6 std::__detail::__gamma_spouge_data< _Tp > Struct Template Reference

10.6.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::__gamma_spouge_data< _Tp >
```

A struct for Spouge algorithm Chebyshev arrays of coefficients.

Definition at line 1859 of file sf_gamma.tcc.

The documentation for this struct was generated from the following file:

- bits/sf_gamma.tcc

10.7 std::__detail::__gamma_spouge_data< double > Struct Template Reference

Static Public Attributes

- static constexpr std::array< double, 18 > _S_cheby

10.7.1 Detailed Description

```
template<>
struct std::__detail::__gamma_spouge_data< double >
```

Definition at line 1880 of file sf_gamma.tcc.

10.7.2 Member Data Documentation

10.7.2.1 constexpr std::array<double, 18> std::__detail::__gamma_spouge_data< double >::_S_cheby [static]

Initial value:

```
{
    2.785716565770350e+08,
    -1.693088166941517e+09,
    4.549688586500031e+09,
    -7.121728036151557e+09,
    7.202572947273274e+09,
    -4.935548868770376e+09,
    2.338187776097503e+09,
    -7.678102458920741e+08,
    1.727524819329867e+08,
    -2.595321377008346e+07,
    2.494811203993971e+06,
    -1.437252641338402e+05,
    4.490767356961276e+03,
    -6.505596924745029e+01,
    3.362323142416327e-01,
    -3.817361443986454e-04,
    3.273137866873352e-08,
    -7.642333165976788e-15,
}
```

Definition at line 1884 of file sf_gamma.tcc.

The documentation for this struct was generated from the following file:

- bits/sf_gamma.tcc

10.8 `std::__detail::__gamma_spouge_data< float >` Struct Template Reference

Static Public Attributes

- static constexpr `std::array< float, 7 >` [`_S_cheby`](#)

10.8.1 Detailed Description

```
template<>
struct std::__detail::__gamma_spouge_data< float >
```

Definition at line 1864 of file `sf_gamma.tcc`.

10.8.2 Member Data Documentation

10.8.2.1 `constexpr std::array<float, 7> std::__detail::__gamma_spouge_data< float >::_S_cheby` `[static]`

Initial value:

```
{
    2.901419e+03F,
    -5.929168e+03F,
    4.148274e+03F,
    -1.164761e+03F,
    1.174135e+02F,
    -2.786588e+00F,
    3.775392e-03F,
}
```

Definition at line 1868 of file `sf_gamma.tcc`.

The documentation for this struct was generated from the following file:

- [bits/sf_gamma.tcc](#)

10.9 `std::__detail::__gamma_spouge_data< long double >` Struct Template Reference

Static Public Attributes

- static constexpr `std::array< long double, 22 >` [`_S_cheby`](#)

10.9.1 Detailed Description

```
template<>
struct std::__detail::__gamma_spouge_data< long double >
```

Definition at line 1907 of file `sf_gamma.tcc`.

10.9.2 Member Data Documentation

10.9.2.1 constexpr std::array<long double, 22> std::__detail::__gamma_spouge_data< long double >::__S_cheby [static]

Initial value:

```
{
    1.681473171108908244e+10L,
    -1.269150315503303974e+11L,
    4.339449429013039995e+11L,
    -8.893680202692714895e+11L,
    1.218472425867950986e+12L,
    -1.178403473259353616e+12L,
    8.282455311246278274e+11L,
    -4.292112878930625978e+11L,
    1.646988347276488710e+11L,
    -4.661514921989111004e+10L,
    9.619972564515443397e+09L,
    -1.419382551781042824e+09L,
    1.454145470816386107e+08L,
    -9.923020719435758179e+06L,
    4.253557563919127284e+05L,
    -1.053371059784341875e+04L,
    1.332425479537961437e+02L,
    -7.118343974029489132e-01L,
    1.172051640057979518e-03L,
    -3.323940885824119041e-07L,
    4.503801674404338524e-12L,
    -5.320477002211632680e-20L,
}
```

Definition at line 1911 of file sf_gamma.tcc.

The documentation for this struct was generated from the following file:

- [bits/sf_gamma.tcc](#)

10.10 std::__detail::__Airy<_Tp> Class Template Reference

Public Types

- using [scalar_type](#) = std::__detail::__num_traits_t< [value_type](#) >
- using [value_type](#) = _Tp

Public Member Functions

- constexpr [__Airy](#) ()=default
- [__Airy](#) (const [__Airy](#) &)=default
- [__Airy](#) ([__Airy](#) &&)=default
- constexpr [__AiryState](#)< [value_type](#) > [operator\(\)](#) ([value_type](#) __y) const

Public Attributes

- `scalar_type inner_radius` { `_Airy_default_radII<scalar_type>::inner_radius`}
- `scalar_type outer_radius` { `_Airy_default_radII<scalar_type>::outer_radius`}

10.10.1 Detailed Description

```
template<typename _Tp>
class std::__detail::_Airy< _Tp >
```

Class to manage the asymptotic expansions for Airy functions. The parameters describing the various regions are adjustable.

Definition at line 2497 of file `sf_airy.tcc`.

10.10.2 Member Typedef Documentation

10.10.2.1 `template<typename _Tp> using std::__detail::_Airy< _Tp >::scalar_type = std::__detail::__num_traits_↵
t<value_type>`

Definition at line 2502 of file `sf_airy.tcc`.

10.10.2.2 `template<typename _Tp> using std::__detail::_Airy< _Tp >::value_type = _Tp`

Definition at line 2501 of file `sf_airy.tcc`.

10.10.3 Constructor & Destructor Documentation

10.10.3.1 `template<typename _Tp> constexpr std::__detail::_Airy< _Tp >::_Airy() [default]`

10.10.3.2 `template<typename _Tp> std::__detail::_Airy< _Tp >::_Airy(const _Airy< _Tp > &) [default]`

10.10.3.3 `template<typename _Tp> std::__detail::_Airy< _Tp >::_Airy(_Airy< _Tp > &&) [default]`

10.10.4 Member Function Documentation

10.10.4.1 `template<typename _Tp> constexpr _AiryState< _Tp > std::__detail::_Airy< _Tp >::operator()(value_type
_y) const`

Return the Airy functions for complex argument.

Definition at line 2520 of file `sf_airy.tcc`.

References `std::__detail::__beta()`, `std::__detail::_Airy_series< _Tp >::S_Ai()`, and `std::__detail::_Airy_series< _Tp >::S_Bi()`.

10.10.5 Member Data Documentation

10.10.5.1 `template<typename _Tp> scalar_type std::__detail::_Airy< _Tp >::inner_radius`
`{ _Airy_default_radii<scalar_type>::inner_radius }`

Definition at line 2511 of file sf_airy.tcc.

10.10.5.2 `template<typename _Tp> scalar_type std::__detail::_Airy< _Tp >::outer_radius`
`{ _Airy_default_radii<scalar_type>::outer_radius }`

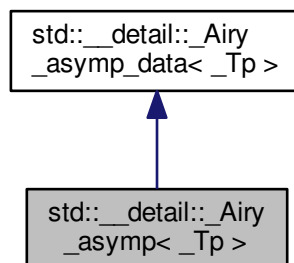
Definition at line 2512 of file sf_airy.tcc.

The documentation for this class was generated from the following file:

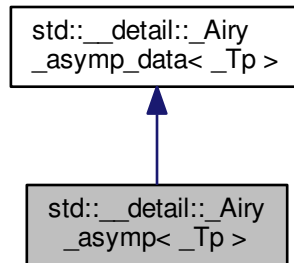
- [bits/sf_airy.tcc](#)

10.11 std::__detail::_Airy_asymp< _Tp > Class Template Reference

Inheritance diagram for std::__detail::_Airy_asymp< _Tp >:



Collaboration diagram for `std::__detail::_Airy_asymp<_Tp>`:



Public Types

- using `_Cmplx` = `std::complex<_Tp>`

Public Member Functions

- `constexpr _Airy_asymp()` = default
- `_AiryState<_Cmplx> _S_absarg_ge_pio3(_Cmplx __z) const`
*This function evaluates $Ai(z)$, $Ai'(z)$ and $Bi(z)$, $Bi'(z)$ from their asymptotic expansions for $|arg(z)| < 2 * \pi/3$ i.e. roughly along the negative real axis.*
- `_AiryState<_Cmplx> _S_absarg_lt_pio3(_Cmplx __z) const`
This function evaluates $Ai(z)$ and $Ai'(z)$ from their asymptotic expansions for $|arg(-z)| < \pi/3$ i.e. roughly along the negative real axis.
- `_AiryState<_Cmplx> operator()(_Cmplx __t, bool __return_fock_airy=false) const`

10.11.1 Detailed Description

```
template<typename _Tp>
class std::__detail::_Airy_asymp<_Tp>
```

A class encapsulating the asymptotic expansions of Airy functions and their derivatives.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 1998 of file `sf_airy.tcc`.

10.11.2 Member Typedef Documentation

10.11.2.1 `template<typename _Tp> using std::__detail::_Airy_asymp<_Tp>::_Cmplx = std::complex<_Tp>`

Definition at line 2003 of file sf_airy.tcc.

10.11.3 Constructor & Destructor Documentation

10.11.3.1 `template<typename _Tp> constexpr std::__detail::_Airy_asymp<_Tp>::_Airy_asymp() [default]`

10.11.4 Member Function Documentation

10.11.4.1 `template<typename _Tp> _AiryState< std::complex<_Tp> > > std::__detail::_Airy_asymp<_Tp>::_S_absarg_ge_pio3(_Cmplx __z) const`

This function evaluates $Ai(z)$, $Ai'(z)$ and $Bi(z)$, $Bi'(z)$ from their asymptotic expansions for $|arg(z)| < 2 * \pi/3$ i.e. roughly along the negative real axis.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Parameters

in	<code>__z</code>	Complex argument at which $Ai(z)$ and $Bi(z)$ and their derivative are evaluated. This function assumes $ z > 15$ and $ arg(z) < 2\pi/3$.
----	------------------	--

Returns

A struct containing z , $Ai(z)$, $Ai'(z)$, $Bi(z)$, $Bi'(z)$.

Definition at line 2271 of file sf_airy.tcc.

References `std::__detail::_AiryState<_Tp>::_z`.

10.11.4.2 `template<typename _Tp> _AiryState< std::complex<_Tp> > > std::__detail::_Airy_asymp<_Tp>::_S_absarg_lt_pio3(_Cmplx __z) const`

This function evaluates $Ai(z)$ and $Ai'(z)$ from their asymptotic expansions for $|arg(-z)| < \pi/3$ i.e. roughly along the negative real axis.

For speed, the number of terms needed to achieve about 16 decimals accuracy is tabled and determined for $|z|$. This function assumes $|z| > 15$ and $|arg(-z)| < \pi/3$.

Note that for speed and since this function is called by another, checks for valid arguments are not made. Hence, an error return is not needed.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Parameters

in	<code>_↔</code> <code>_z</code>	The value at which the Airy function and their derivatives are evaluated.
----	------------------------------------	---

Returns

A struct containing z , $Ai(z)$, $Ai'(z)$, $Bi(z)$, $Bi'(z)$.

Todo Revisit these numbers of terms for the Airy asymptotic expansions.

Definition at line 2301 of file `sf_airy.tcc`.

References `std::__detail::_AiryState<_Tp>::__z`.

10.11.4.3 `template<typename _Tp> _AiryState< std::complex<_Tp>> std::__detail::_Airy_asymp<_Tp>::operator()
(_Cmplx __t, bool __return_fock_airy = false) const`

Return the Airy functions for a given argument using asymptotic series.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 2029 of file `sf_airy.tcc`.

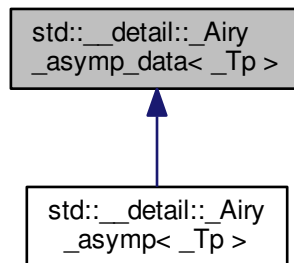
References `std::__detail::_AiryState<_Tp>::__z`.

The documentation for this class was generated from the following file:

- [bits/sf_airy.tcc](#)

10.12 std::__detail::_Airy_asymp_data< _Tp > Struct Template Reference

Inheritance diagram for std::__detail::_Airy_asymp_data< _Tp >:



10.12.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::_Airy_asymp_data< _Tp >
```

A class encapsulating data for the asymptotic expansions of Airy functions and their derivatives.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 632 of file sf_airy.tcc.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.13 std::__detail::_Airy_asymp_data< double > Struct Template Reference

Static Public Attributes

- static constexpr double [_S_c](#) [[_S_max_cd](#)]
- static constexpr double [_S_d](#) [[_S_max_cd](#)]
- static constexpr int [_S_max_cd](#) = 198

10.13.1 Detailed Description

```
template<>
struct std::__detail::_Airy_asymp_data< double >
```

Definition at line 739 of file sf_airy.tcc.

10.13.2 Member Data Documentation

10.13.2.1 `constexpr double std::__detail::_Airy_asymp_data< double >::_S_c[_S_max_cd]` `[static]`

Definition at line 745 of file sf_airy.tcc.

10.13.2.2 `constexpr double std::__detail::_Airy_asymp_data< double >::_S_d[_S_max_cd]` `[static]`

Definition at line 948 of file sf_airy.tcc.

10.13.2.3 `constexpr int std::__detail::_Airy_asymp_data< double >::_S_max_cd = 198` `[static]`

Definition at line 741 of file sf_airy.tcc.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.14 `std::__detail::_Airy_asymp_data< float >` Struct Template Reference

Static Public Attributes

- static constexpr float [_S_c](#) [[_S_max_cd](#)]
- static constexpr float [_S_d](#) [[_S_max_cd](#)]
- static constexpr int [_S_max_cd](#) = 43

10.14.1 Detailed Description

```
template<>
struct std::__detail::_Airy_asymp_data< float >
```

Definition at line 636 of file sf_airy.tcc.

10.14.2 Member Data Documentation

10.14.2.1 `constexpr float std::__detail::_Airy_asymp_data< float >::_S_c[_S_max_cd]` `[static]`

Definition at line 642 of file sf_airy.tcc.

10.14.2.2 `constexpr float std::__detail::_Airy_asymp_data< float >::_S_d[_S_max_cd]` `[static]`

Definition at line 690 of file sf_airy.tcc.

10.14.2.3 `constexpr int std::__detail::_Airy_asymp_data< float >::_S_max_cd = 43` `[static]`

Definition at line 638 of file sf_airy.tcc.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.15 std::__detail::_Airy_asymp_data< long double > Struct Template Reference

Static Public Attributes

- static constexpr long double [_S_c](#) [[_S_max_cd](#)]
- static constexpr long double [_S_d](#) [[_S_max_cd](#)]
- static constexpr int [_S_max_cd](#) = 201

10.15.1 Detailed Description

```
template<>
struct std::__detail::_Airy_asymp_data< long double >
```

Definition at line 1152 of file sf_airy.tcc.

10.15.2 Member Data Documentation

10.15.2.1 `constexpr long double std::__detail::_Airy_asymp_data< long double >::_S_c[_S_max_cd]` `[static]`

Definition at line 1158 of file sf_airy.tcc.

10.15.2.2 `constexpr long double std::__detail::_Airy_asymp_data< long double >::_S_d[_S_max_cd]` `[static]`

Definition at line 1364 of file `sf_airy.tcc`.

10.15.2.3 `constexpr int std::__detail::_Airy_asymp_data< long double >::_S_max_cd = 201` `[static]`

Definition at line 1154 of file `sf_airy.tcc`.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.16 `std::__detail::_Airy_asymp_series< _Sum >` Class Template Reference

Public Types

- using `scalar_type` = `std::__detail::__num_traits_t< value_type >`
- using `value_type` = `typename _Sum::value_type`

Public Member Functions

- `_Airy_asymp_series` (`_Sum __proto`)
- `_Airy_asymp_series` (`const _Airy_asymp_series &`)=default
- `_Airy_asymp_series` (`_Airy_asymp_series &&`)=default
- `_AiryState< value_type > operator()` (`value_type __y`)

Static Public Attributes

- static constexpr `scalar_type _S_sqrt_pi` = `__gnu_cxx::__const_root_pi(scalar_type{})`

10.16.1 Detailed Description

```
template<typename _Sum>
class std::__detail::_Airy_asymp_series< _Sum >
```

Class to manage the asymptotic series for Airy functions.

Template Parameters

<code>_Sum</code>	A sum type
-------------------	------------

Definition at line 2364 of file sf_airy.tcc.

10.16.2 Member Typedef Documentation

10.16.2.1 `template<typename _Sum> using std::__detail::_Airy_asymp_series<_Sum>::scalar_type = std::__detail::_num_traits_t<value_type>`

Definition at line 2369 of file sf_airy.tcc.

10.16.2.2 `template<typename _Sum> using std::__detail::_Airy_asymp_series<_Sum>::value_type = typename _Sum::value_type`

Definition at line 2368 of file sf_airy.tcc.

10.16.3 Constructor & Destructor Documentation

10.16.3.1 `template<typename _Sum> std::__detail::_Airy_asymp_series<_Sum>::_Airy_asymp_series (_Sum __proto) [inline]`

Definition at line 2373 of file sf_airy.tcc.

10.16.3.2 `template<typename _Sum> std::__detail::_Airy_asymp_series<_Sum>::_Airy_asymp_series (const _Airy_asymp_series<_Sum> &) [default]`

10.16.3.3 `template<typename _Sum> std::__detail::_Airy_asymp_series<_Sum>::_Airy_asymp_series (_Airy_asymp_series<_Sum> &&) [default]`

10.16.4 Member Function Documentation

10.16.4.1 `template<typename _Sum> _AiryState< typename _Airy_asymp_series<_Sum>::value_type > std::__detail::_Airy_asymp_series<_Sum>::operator() (value_type __y)`

Return an [_AiryState](#) containing, not actual Airy functions, but four asymptotic Airy components:

Template Parameters

<code>_Sum</code>	A sum type
-------------------	------------

Definition at line 2418 of file sf_airy.tcc.

10.16.5 Member Data Documentation

10.16.5.1 `template<typename _Sum> constexpr _Airy_asymp_series< _Sum >::scalar_type
std::__detail::_Airy_asymp_series< _Sum >::S_sqrt_pi = __gnu_cxx::__const_root_pi(scalar_type{})
[static]`

Definition at line 2371 of file `sf_airy.tcc`.

The documentation for this class was generated from the following file:

- [bits/sf_airy.tcc](#)

10.17 `std::__detail::_Airy_default_radii< _Tp >` Struct Template Reference

10.17.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::_Airy_default_radii< _Tp >
```

Definition at line 2468 of file `sf_airy.tcc`.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.18 `std::__detail::_Airy_default_radii< double >` Struct Template Reference

Static Public Attributes

- static constexpr double [inner_radius](#) {4.0}
- static constexpr double [outer_radius](#) {12.0}

10.18.1 Detailed Description

```
template<>
struct std::__detail::_Airy_default_radii< double >
```

Definition at line 2479 of file `sf_airy.tcc`.

10.18.2 Member Data Documentation

10.18.2.1 constexpr double std::__detail::_Airy_default_radii< double >::inner_radius {4.0} [static]

Definition at line 2481 of file sf_airy.tcc.

10.18.2.2 constexpr double std::__detail::_Airy_default_radii< double >::outer_radius {12.0} [static]

Definition at line 2482 of file sf_airy.tcc.

The documentation for this struct was generated from the following file:

- bits/[sf_airy.tcc](#)

10.19 std::__detail::_Airy_default_radii< float > Struct Template Reference

Static Public Attributes

- static constexpr float [inner_radius](#) {2.0F}
- static constexpr float [outer_radius](#) {6.0F}

10.19.1 Detailed Description

```
template<>
struct std::__detail::_Airy_default_radii< float >
```

Definition at line 2472 of file sf_airy.tcc.

10.19.2 Member Data Documentation

10.19.2.1 constexpr float std::__detail::_Airy_default_radii< float >::inner_radius {2.0F} [static]

Definition at line 2474 of file sf_airy.tcc.

10.19.2.2 constexpr float std::__detail::_Airy_default_radii< float >::outer_radius {6.0F} [static]

Definition at line 2475 of file sf_airy.tcc.

The documentation for this struct was generated from the following file:

- bits/[sf_airy.tcc](#)

10.20 `std::__detail::_Airy_default_radii< long double >` Struct Template Reference

Static Public Attributes

- static constexpr long double [inner_radius](#) {5.0L}
- static constexpr long double [outer_radius](#) {15.0L}

10.20.1 Detailed Description

```
template<>
struct std::__detail::_Airy_default_radii< long double >
```

Definition at line 2486 of file `sf_airy.tcc`.

10.20.2 Member Data Documentation

10.20.2.1 constexpr long double `std::__detail::_Airy_default_radii< long double >::inner_radius` {5.0L} [static]

Definition at line 2488 of file `sf_airy.tcc`.

10.20.2.2 constexpr long double `std::__detail::_Airy_default_radii< long double >::outer_radius` {15.0L} [static]

Definition at line 2489 of file `sf_airy.tcc`.

The documentation for this struct was generated from the following file:

- `bits/sf_airy.tcc`

10.21 `std::__detail::_Airy_series< _Tp >` Class Template Reference

Public Types

- using [_Cmplx](#) = `std::complex< _Tp >`

Static Public Member Functions

- static `std::pair< _Cmplx, _Cmplx > _S_Ai` ([_Cmplx](#) __t)
- static `_AiryState< _Cmplx > _S_Airy` ([_Cmplx](#) __t)
- static `std::pair< _Cmplx, _Cmplx > _S_Bi` ([_Cmplx](#) __t)
- static `_AiryAuxilliaryState< _Cmplx > _S_FGH` ([_Cmplx](#) __t)
- static `_AiryState< _Cmplx > _S_Fock` ([_Cmplx](#) __t)
- static `_AiryState< _Cmplx > _S_Scorer` ([_Cmplx](#) __t)
- static `_AiryState< _Cmplx > _S_Scorer2` ([_Cmplx](#) __t)

Static Public Attributes

- static constexpr int [_N_FGH](#) = 200
- static constexpr _Tp [_S_Ai0](#) = _Tp{3.550280538878172392600631860041831763980e-1L}
- static constexpr _Tp [_S_Aip0](#) = _Tp{-2.588194037928067984051835601892039634793e-1L}
- static constexpr _Tp [_S_Bi0](#) = _Tp{6.149266274460007351509223690936135535960e-1L}
- static constexpr _Tp [_S_Bip0](#) = _Tp{4.482883573538263579148237103988283908668e-1L}
- static constexpr _Tp [_S_eps](#) = __gnu_cxx::__epsilon(_Tp{})
- static constexpr _Tp [_S_Gi0](#) = _Tp{2.049755424820002450503074563645378511979e-1L}
- static constexpr _Tp [_S_Gip0](#) = _Tp{1.494294524512754526382745701329427969551e-1L}
- static constexpr _Tp [_S_Hi0](#) = _Tp{4.099510849640004901006149127290757023959e-1L}
- static constexpr _Tp [_S_Hip0](#) = _Tp{2.988589049025509052765491402658855939102e-1L}
- static constexpr [_Cmplx_S_i](#) {_Tp{0}, _Tp{1}}
- static constexpr _Tp [_S_pi](#) = __gnu_cxx::__const_pi(_Tp{})
- static constexpr _Tp [_S_sqrt_pi](#) = __gnu_cxx::__const_root_pi(_Tp{})

10.21.1 Detailed Description

```
template<typename _Tp>
class std::__detail::_Airy_series<_Tp>
```

This class organizes series solutions of the Airy function.

$$fai(x) = \sum_{k=0}^{\infty} \frac{(2k+1)!!!x^{3k}}{(2k+1)!}$$

$$gai(x) = \sum_{k=0}^{\infty} \frac{(2k+2)!!!x^{3k+1}}{(2k+2)!}$$

$$hai(x) = \sum_{k=0}^{\infty} \frac{(2k+3)!!!x^{3k+2}}{(2k+3)!}$$

This class contains tabulations of the factors appearing in the sums above.

Definition at line 108 of file sf_airy.tcc.

10.21.2 Member Typedef Documentation

10.21.2.1 `template<typename _Tp> using std::__detail::_Airy_series<_Tp>::_Cmplx = std::complex<_Tp>`

Definition at line 112 of file sf_airy.tcc.

10.21.3 Member Function Documentation

10.21.3.1 `template<typename _Tp> std::pair< std::complex< _Tp>, std::complex< _Tp> > std::__detail::_Airy_series< _Tp>::_S_Ai(_Cmplx __t) [static]`

Return the Airy function of the first kind and its derivative by using the series expansions of the auxilliary Airy functions:

$$f_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+1)!!!x^{3k}}{(2k+1)!}$$

$$g_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+2)!!!x^{3k+1}}{(2k+2)!}$$

The Airy function of the first kind is then defined by:

$$Ai(x) = Ai(0)f_{ai}(x) + Ai'(0)g_{ai}(x)$$

where $Ai(0) = 3^{-2/3}/\Gamma(2/3)$, $Ai'(0) = -3^{-1/2}Bi'(0)$ and $Bi(0) = 3^{1/2}Ai(0)$, $Bi'(0) = 3^{1/6}/\Gamma(1/3)$

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 341 of file `sf_airy.tcc`.

Referenced by `std::__detail::_Airy< _Tp>::operator()()`.

10.21.3.2 `template<typename _Tp> _AiryState< std::complex< _Tp> > std::__detail::_Airy_series< _Tp>::_S_Airy(_Cmplx __t) [static]`

Return the Fock-type Airy functions $Ai(t)$, and $Bi(t)$ and their derivatives of complex argument.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Parameters

<code>↵</code>	The complex argument
<code>↵</code>	
<code>↵</code>	
<code>↵</code>	
<code>t</code>	

Definition at line 609 of file `sf_airy.tcc`.

10.21.3.3 `template<typename _Tp> std::pair< std::complex<_Tp>, std::complex<_Tp> > std::__detail::_Airy_series<_Tp>::_S_Bi(_Cmplx __t) [static]`

Return the Airy function of the second kind and its derivative by using the series expansions of the auxilliary Airy functions:

$$f_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+1)!!!x^{3k}}{(2k+1)!}$$

$$g_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+2)!!!x^{3k+1}}{(2k+2)!}$$

The Airy function of the second kind is then defined by:

$$Bi(x) = Bi(0)f_{ai}(x) + Bi'(0)g_{ai}(x)$$

where $Ai(0) = 3^{-2/3}/\Gamma(2/3)$, $Ai'(0) = -3-1/2Bi'(0)$ and $Bi(0) = 3^{1/2}Ai(0)$, $Bi'(0) = 3^{1/6}/\Gamma(1/3)$

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 364 of file sf_airy.tcc.

Referenced by `std::__detail::_Airy<_Tp>::operator()()`.

10.21.3.4 `template<typename _Tp> _AiryAuxilliaryState< std::complex<_Tp> > std::__detail::_Airy_series<_Tp>::_S_FGH(_Cmplx __t) [static]`

Return the auxilliary Airy functions:

$$f_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+1)!!!x^{3k}}{(2k+1)!}$$

$$g_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+2)!!!x^{3k+1}}{(2k+2)!}$$

$$h_{ai}(x) = \sum_{k=0}^{\infty} \frac{(2k+3)!!!x^{3k+2}}{(2k+3)!}$$

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 383 of file sf_airy.tcc.

10.21.3.5 `template<typename _Tp> _AiryState< std::complex<_Tp> > std::__detail::_Airy_series<_Tp>::_S_Fock(_Cmplx __t) [static]`

Return the Fock-type Airy functions $w_1(t)$, and $w_2(t)$ and their derivatives of complex argument.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Parameters

↩	The complex argument
↩	
↩	
↩	
<code>t</code>	

Definition at line 621 of file sf_airy.tcc.

10.21.3.6 `template<typename _Tp> _AiryState< std::complex< _Tp > > std::__detail::_Airy_series< _Tp >::_S_Scorer (_Cmplx_t) [static]`

Return the Scorer functions by using the series expansions of the auxilliary Airy functions:

$$fai(x) = \sum_{k=0}^{\infty} \frac{(2k+1)!!!x^{3k}}{(2k+1)!}$$

$$gai(x) = \sum_{k=0}^{\infty} \frac{(2k+2)!!!x^{3k+1}}{(2k+2)!}$$

$$hai(x) = \sum_{k=0}^{\infty} \frac{(2k+3)!!!x^{3k+2}}{(2k+3)!}$$

The Scorer function is then defined by:

$$Hi(x) = Hi(0) (fai(x) + gai(x) + hai(x))$$

where $Hi(0) = 2/(3^{7/6}\Gamma(2/3))$ and $Hi'(0) = 2/(3^{5/6}\Gamma(1/3))$. The other Scorer function is found from the identity

$$Gi(x) + Hi(x) = Bi(x)$$

Todo Find out what is wrong with the $Hi = fai + gai + hai$ scorer function.

Template Parameters

<code>_Tp</code>	A real type
------------------	-------------

Definition at line 464 of file sf_airy.tcc.

10.21.3.7 `template<typename _Tp> _AiryState< std::complex<_Tp> > std::__detail::_Airy_series<_Tp>::__S_Scorer2(_Cmplx_t) [static]`

Return the Scorer functions by using the series expansions:

$$\begin{aligned}
 Hi(x) &= \frac{3^{-2/3}}{\pi} \sum_{k=0}^{\infty} \Gamma\left(\frac{k+1}{3}\right) \frac{3^{1/3}x}{k!} \\
 Hi'(x) &= \frac{3^{-1/3}}{\pi} \sum_{k=0}^{\infty} \Gamma\left(\frac{k+2}{3}\right) \frac{3^{1/3}x}{k!} \\
 Gi(x) &= \frac{3^{-2/3}}{\pi} \sum_{k=0}^{\infty} \cos\left(\frac{2k-1}{3}\pi\right) \Gamma\left(\frac{k+1}{3}\right) \frac{3^{1/3}x}{k!} \\
 Gi'(x) &= \frac{3^{-1/3}}{\pi} \sum_{k=0}^{\infty} \cos\left(\frac{2k+1}{3}\pi\right) \Gamma\left(\frac{k+2}{3}\right) \frac{3^{1/3}x}{k!}
 \end{aligned}$$

Definition at line 501 of file sf_airy.tcc.

References std::__detail::__gamma().

10.21.4 Member Data Documentation

10.21.4.1 `template<typename _Tp> constexpr int std::__detail::_Airy_series<_Tp>::__N_FGH = 200 [static]`

Definition at line 114 of file sf_airy.tcc.

10.21.4.2 `template<typename _Tp> constexpr _Tp std::__detail::_Airy_series<_Tp>::__S_Ai0 = _Tp{3.550280538878172392600631860041831763980e-1L} [static]`

Definition at line 130 of file sf_airy.tcc.

10.21.4.3 `template<typename _Tp> constexpr _Tp std::__detail::_Airy_series<_Tp>::__S_Aip0 = _Tp{-2.588194037928067984051835601892039634793e-1L} [static]`

Definition at line 132 of file sf_airy.tcc.

10.21.4.4 `template<typename _Tp> constexpr _Tp std::__detail::_Airy_series<_Tp>::__S_Bi0 = _Tp{6.149266274460007351509223690936135535960e-1L} [static]`

Definition at line 134 of file sf_airy.tcc.

10.21.4.5 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_Bip0 =
_Tp{4.482883573538263579148237103988283908668e-1L} [static]`

Definition at line 136 of file sf_airy.tcc.

10.21.4.6 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_eps =
__gnu_cxx::__epsilon(_Tp{}) [static]`

Definition at line 125 of file sf_airy.tcc.

10.21.4.7 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_Gi0 =
_Tp{2.049755424820002450503074563645378511979e-1L} [static]`

Definition at line 142 of file sf_airy.tcc.

10.21.4.8 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_Gip0 =
_Tp{1.494294524512754526382745701329427969551e-1L} [static]`

Definition at line 144 of file sf_airy.tcc.

10.21.4.9 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_Hi0 =
_Tp{4.099510849640004901006149127290757023959e-1L} [static]`

Definition at line 138 of file sf_airy.tcc.

10.21.4.10 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_Hip0 =
_Tp{2.988589049025509052765491402658855939102e-1L} [static]`

Definition at line 140 of file sf_airy.tcc.

10.21.4.11 `template<typename _Tp > constexpr std::complex< _Tp > std::__detail::_Airy_series< _Tp >::_S_i {_Tp{0},
_Tp{1}} [static]`

Definition at line 145 of file sf_airy.tcc.

10.21.4.12 `template<typename _Tp > constexpr _Tp std::__detail::_Airy_series< _Tp >::_S_pi =
__gnu_cxx::__const_pi(_Tp{}) [static]`

Definition at line 126 of file sf_airy.tcc.

```
10.21.4.13 template<typename _Tp > constexpr _Tp std::__detail::__Airy_series< _Tp >::_S_sqrt_pi =
    __gnu_cxx::__const_root_pi(_Tp{}) [static]
```

Definition at line 128 of file sf_airy.tcc.

The documentation for this class was generated from the following file:

- bits/sf_airy.tcc

10.22 std::__detail::__AiryAuxilliaryState< _Tp > Struct Template Reference

Public Types

- using [_Val](#) = std::__detail::__num_traits_t< _Tp >

Public Attributes

- [_Tp __fai_deriv](#)
- [_Tp __fai_value](#)
- [_Tp __gai_deriv](#)
- [_Tp __gai_value](#)
- [_Tp __hai_deriv](#)
- [_Tp __hai_value](#)
- [_Tp __z](#)

10.22.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::__AiryAuxilliaryState< _Tp >
```

A structure containing three auxilliary Airy functions and their derivatives.

Definition at line 80 of file sf_airy.tcc.

10.22.2 Member Typedef Documentation

```
10.22.2.1 template<typename _Tp> using std::__detail::__AiryAuxilliaryState< _Tp >::_Val =
    std::__detail::__num_traits_t<_Tp>
```

Definition at line 82 of file sf_airy.tcc.

10.22.3 Member Data Documentation

10.22.3.1 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__fai_deriv`

Definition at line 86 of file `sf_airy.tcc`.

10.22.3.2 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__fai_value`

Definition at line 85 of file `sf_airy.tcc`.

10.22.3.3 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__gai_deriv`

Definition at line 88 of file `sf_airy.tcc`.

10.22.3.4 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__gai_value`

Definition at line 87 of file `sf_airy.tcc`.

10.22.3.5 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__hai_deriv`

Definition at line 90 of file `sf_airy.tcc`.

10.22.3.6 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__hai_value`

Definition at line 89 of file `sf_airy.tcc`.

10.22.3.7 `template<typename _Tp> _Tp std::__detail::_AiryAuxilliaryState< _Tp >::__z`

Definition at line 84 of file `sf_airy.tcc`.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.23 `std::__detail::_AiryState< _Tp >` Struct Template Reference

Public Types

- using `_Real` = `std::__detail::__num_traits_t< _Tp >`

Public Member Functions

- [_Real true_Wronskian](#) ()
- [_Tp Wronskian](#) () const

Public Attributes

- [_Tp __Ai_deriv](#)
- [_Tp __Ai_value](#)
- [_Tp __Bi_deriv](#)
- [_Tp __Bi_value](#)
- [_Tp __z](#)

10.23.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::_AiryState<_Tp>
```

This struct defines the Airy function state with two presumably numerically useful Airy functions and their derivatives. The data members are directly accessible. The lone method computes the Wronskian from the stored functions. A static method returns the correct Wronskian.

Definition at line 55 of file sf_airy.tcc.

10.23.2 Member Typedef Documentation

10.23.2.1 `template<typename _Tp> using std::__detail::_AiryState<_Tp>::_Real = std::__detail::__num_traits_t<_Tp>`

Definition at line 57 of file sf_airy.tcc.

10.23.3 Member Function Documentation

10.23.3.1 `template<typename _Tp> _Real std::__detail::_AiryState<_Tp>::true_Wronskian () [inline]`

Definition at line 70 of file sf_airy.tcc.

10.23.3.2 `template<typename _Tp> _Tp std::__detail::_AiryState<_Tp>::Wronskian () const [inline]`

Definition at line 66 of file sf_airy.tcc.

References `std::__detail::_AiryState<_Tp>::__Ai_deriv`.

10.23.4 Member Data Documentation

10.23.4.1 `template<typename _Tp> _Tp std::__detail::_AiryState< _Tp >::__Ai_deriv`

Definition at line 61 of file `sf_airy.tcc`.

Referenced by `std::__detail::_AiryState< _Tp >::Wronskian()`.

10.23.4.2 `template<typename _Tp> _Tp std::__detail::_AiryState< _Tp >::__Ai_value`

Definition at line 60 of file `sf_airy.tcc`.

10.23.4.3 `template<typename _Tp> _Tp std::__detail::_AiryState< _Tp >::__Bi_deriv`

Definition at line 63 of file `sf_airy.tcc`.

10.23.4.4 `template<typename _Tp> _Tp std::__detail::_AiryState< _Tp >::__Bi_value`

Definition at line 62 of file `sf_airy.tcc`.

10.23.4.5 `template<typename _Tp> _Tp std::__detail::_AiryState< _Tp >::__z`

Definition at line 59 of file `sf_airy.tcc`.

Referenced by `std::__detail::_Airy_asymp< _Tp >::S_absarg_ge_pio3()`, `std::__detail::_Airy_asymp< _Tp >::S_↵absarg_lt_pio3()`, and `std::__detail::_Airy_asymp< _Tp >::operator()`.

The documentation for this struct was generated from the following file:

- [bits/sf_airy.tcc](#)

10.24 `std::__detail::_Factorial_table< _Tp >` Struct Template Reference

Public Attributes

- `_Tp __factorial`
- `_Tp __log_factorial`
- `int __n`

10.24.1 Detailed Description

```
template<typename _Tp>
struct std::__detail::__Factorial_table<_Tp>
```

Definition at line 65 of file sf_gamma.tcc.

10.24.2 Member Data Documentation

10.24.2.1 template<typename _Tp> _Tp std::__detail::__Factorial_table<_Tp>::__factorial

Definition at line 68 of file sf_gamma.tcc.

Referenced by std::__detail::__double_factorial().

10.24.2.2 template<typename _Tp> _Tp std::__detail::__Factorial_table<_Tp>::__log_factorial

Definition at line 69 of file sf_gamma.tcc.

Referenced by std::__detail::__log_double_factorial(), and std::__detail::__log_gamma().

10.24.2.3 template<typename _Tp> int std::__detail::__Factorial_table<_Tp>::__n

Definition at line 67 of file sf_gamma.tcc.

Referenced by std::__detail::__bernoulli(), std::__detail::__bernoulli_2n(), std::__detail::__bernoulli_series(), std::__detail::__bincoef(), std::__detail::__double_factorial(), std::__detail::__factorial(), std::__detail::__gamma(), std::__detail::__gamma_cont_frac(), std::__detail::__gamma_series(), std::__detail::__harmonic_number(), std::__detail::__lanczos_binet1p(), std::__detail::__log_bincoef(), std::__detail::__log_bincoef_sign(), std::__detail::__log_double_factorial(), std::__detail::__log_factorial(), std::__detail::__log_gamma(), std::__detail::__pochhammer(), std::__detail::__pochhammer_lower(), and std::__detail::__psi().

The documentation for this struct was generated from the following file:

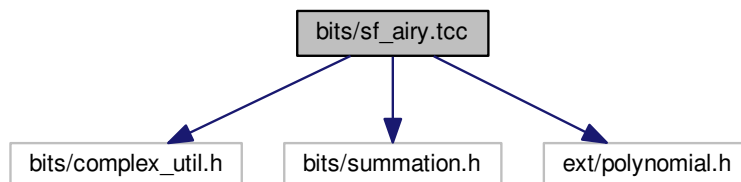
- [bits/sf_gamma.tcc](#)

Chapter 11

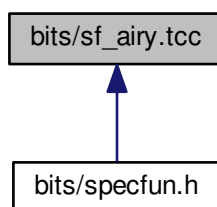
File Documentation

11.1 bits/sf_airy.tcc File Reference

```
#include <bits/complex_util.h>  
#include <bits/summation.h>  
#include <ext/polynomial.h>  
Include dependency graph for sf_airy.tcc:
```



This graph shows which files directly or indirectly include this file:



Classes

- class `std::__detail::_Airy<_Tp>`
- class `std::__detail::_Airy_asymp<_Tp>`
- struct `std::__detail::_Airy_asymp_data<_Tp>`
- struct `std::__detail::_Airy_asymp_data<double>`
- struct `std::__detail::_Airy_asymp_data<float>`
- struct `std::__detail::_Airy_asymp_data<long double>`
- class `std::__detail::_Airy_asymp_series<_Sum>`
- struct `std::__detail::_Airy_default_radii<_Tp>`
- struct `std::__detail::_Airy_default_radii<double>`
- struct `std::__detail::_Airy_default_radii<float>`
- struct `std::__detail::_Airy_default_radii<long double>`
- class `std::__detail::_Airy_series<_Tp>`
- struct `std::__detail::_AiryAuxilliaryState<_Tp>`
- struct `std::__detail::_AiryState<_Tp>`

Namespaces

- `std`
- `std::__detail`

Macros

- `#define _GLIBCXX_BITS_SF_AIRY_TCC 1`

Functions

- `template<typename _Tp>`
`std::complex<_Tp> std::__detail::__airy_ai (std::complex<_Tp> __z)`
Return the complex Airy Ai function.
- `template<typename _Tp>`
`std::complex<_Tp> std::__detail::__airy_bi (std::complex<_Tp> __z)`
Return the complex Airy Bi function.

Variables

- `template<typename _Tp>`
`constexpr int std::__detail::__max_FGH = _Airy_series<_Tp>::_N_FGH`
- `template<>`
`constexpr int std::__detail::__max_FGH<double> = 79`
- `template<>`
`constexpr int std::__detail::__max_FGH<float> = 15`

11.1.1 Detailed Description

This is an internal header file, included by other library headers. You should not attempt to use it directly.

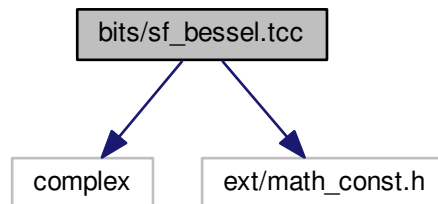
11.1.2 Macro Definition Documentation

11.1.2.1 `#define _GLIBCXX_BITS_SF_AIRY_TCC 1`

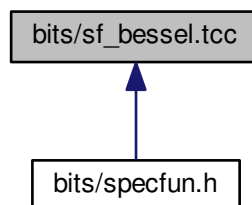
Definition at line 31 of file sf_airy.tcc.

11.2 bits/sf_bessel.tcc File Reference

```
#include <complex>
#include <ext/math_const.h>
Include dependency graph for sf_bessel.tcc:
```



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_BESSEL_TCC 1](#)

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__cyl_bessel_ij_series (_Tp __nu, _Tp __x, _Tp __sgn, unsigned int __max_iter)`
This routine returns the cylindrical Bessel functions of order ν : J_ν or I_ν by series expansion.
- `template<typename _Tp >`
`_Tp std::__detail::__cyl_bessel_j (_Tp __nu, _Tp __x)`
Return the Bessel function of order ν : $J_\nu(x)$.
- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_jn (_Tp __nu, _Tp __x)`
Return the cylindrical Bessel functions and their derivatives of order ν by various means.
- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_jn_asymp (_Tp __nu, _Tp __x)`
This routine computes the asymptotic cylindrical Bessel and Neumann functions of order ν : $J_\nu(x)$, $N_\nu(x)$. Use this for $x \gg \nu^2 + 1$.
- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, std::complex< _Tp > > std::__detail::__cyl_bessel_jn_neg_arg (_Tp __nu, _Tp __x)`
Return the cylindrical Bessel functions and their derivatives of order ν and argument $x < 0$.
- `template<typename _Tp >`
`_gnu_cxx::__cyl_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_jn_steel (_Tp __nu, _Tp __x)`
Compute the Bessel $J_\nu(x)$ and Neumann $N_\nu(x)$ functions and their first derivatives $J'_\nu(x)$ and $N'_\nu(x)$ respectively. These four functions are computed together for numerical stability.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_hankel_1 (_Tp __nu, _Tp __x)`
Return the cylindrical Hankel function of the first kind $H_\nu^{(1)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_hankel_2 (_Tp __nu, _Tp __x)`
Return the cylindrical Hankel function of the second kind $H_n^{(2)}u(x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__cyl_neumann_n (_Tp __nu, _Tp __x)`
Return the Neumann function of order ν : $N_\nu(x)$.
- `template<typename _Tp >`
`_gnu_cxx::__gamma_temme_t< _Tp > std::__detail::__gamma_temme (_Tp __mu)`
Compute the gamma functions required by the Temme series expansions of $N_\nu(x)$ and $K_\nu(x)$.

$$\Gamma_1 = \frac{1}{2\mu} \left[\frac{1}{\Gamma(1-\mu)} - \frac{1}{\Gamma(1+\mu)} \right]$$

and

$$\Gamma_2 = \frac{1}{2} \left[\frac{1}{\Gamma(1-\mu)} + \frac{1}{\Gamma(1+\mu)} \right]$$

where $-1/2 \leq \mu \leq 1/2$ is $\mu = \nu - N$ and N is the nearest integer to ν . The values of $\Gamma(1+\mu)$ and $\Gamma(1-\mu)$ are returned as well.

- `template<typename _Tp >`
`_Tp std::__detail::__sph_bessel` (unsigned int __n, _Tp __x)
Return the spherical Bessel function $j_n(x)$ of order n and non-negative real argument x .
- `template<typename _Tp >`
`_gnu_cxx::__sph_bessel_t< unsigned int, _Tp, _Tp > std::__detail::__sph_bessel_jn` (unsigned int __n, _Tp __x)
Compute the spherical Bessel $j_n(x)$ and Neumann $n_n(x)$ functions and their first derivatives $j'_n(x)$ and $n'_n(x)$ respectively.
- `template<typename _Tp >`
`_gnu_cxx::__sph_bessel_t< unsigned int, _Tp, std::complex< _Tp > > std::__detail::__sph_bessel_jn_neg←_arg` (unsigned int __n, _Tp __x)
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_hankel_1` (unsigned int __n, _Tp __x)
Return the spherical Hankel function of the first kind $h_n^{(1)}(x)$.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_hankel_2` (unsigned int __n, _Tp __x)
Return the spherical Hankel function of the second kind $h_n^{(2)}(x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__sph_neumann` (unsigned int __n, _Tp __x)
Return the spherical Neumann function $n_n(x)$ of order n and non-negative real argument x .

11.2.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.2.2 Macro Definition Documentation

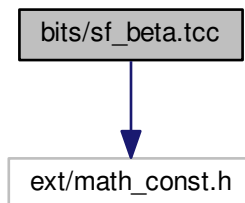
11.2.2.1 `#define _GLIBCXX_BITS_SF_BESSEL_TCC 1`

Definition at line 47 of file `sf_bessel.tcc`.

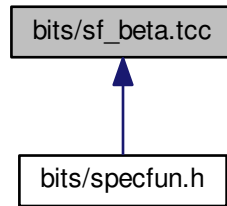
11.3 bits/sf_beta.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for `sf_beta.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_BETA_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__beta \(_Tp __a, _Tp __b\)](#)
Return the beta function $B(a, b)$.
- [template<typename _Tp > _Tp std::__detail::__beta_gamma \(_Tp __a, _Tp __b\)](#)
Return the beta function: $B(a, b)$.
- [template<typename _Tp > _Tp std::__detail::__beta_inc \(_Tp __a, _Tp __b, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__beta_lgamma \(_Tp __a, _Tp __b\)](#)
Return the beta function $B(a, b)$ using the log gamma functions.
- [template<typename _Tp > _Tp std::__detail::__beta_product \(_Tp __a, _Tp __b\)](#)
Return the beta function $B(x, y)$ using the product form.
- [template<typename _Tp > _Tp std::__detail::__ibeta_cont_frac \(_Tp __a, _Tp __b, _Tp __x\)](#)

11.3.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.3.2 Macro Definition Documentation

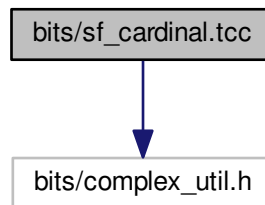
11.3.2.1 `#define _GLIBCXX_BITS_SF_BETA_TCC 1`

Definition at line 49 of file sf_beta.tcc.

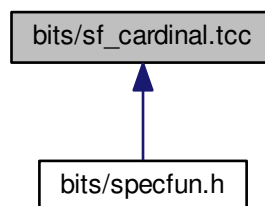
11.4 bits/sf_cardinal.tcc File Reference

```
#include <bits/complex_util.h>
```

Include dependency graph for sf_cardinal.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- `#define _GLIBCXX_BITS_SF_CARDINAL_TCC 1`

Functions

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::__detail::__sinc (_Tp __x)`

Return the sinus cardinal function

$$\text{sinc}(x) = \frac{\sin(x)}{x}$$

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::__detail::__sinc_pi (_Tp __x)`

Return the reperiodized sinus cardinal function

$$\text{sinc}_{\pi}(x) = \frac{\sin(\pi x)}{\pi x}$$

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::__detail::__sinhc (_Tp __x)`

Return the hyperbolic sinus cardinal function

$$\text{sinhc}(x) = \frac{\sinh(x)}{x}$$

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::__detail::__sinhc_pi (_Tp __x)`

Return the reperiodized hyperbolic sinus cardinal function

$$\text{sinhc}_{\pi}(x) = \frac{\sinh(\pi x)}{\pi x}$$

11.4.1 Macro Definition Documentation

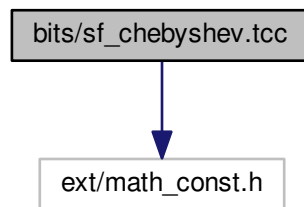
11.4.1.1 `#define _GLIBCXX_BITS_SF_CARDINAL_TCC 1`

Definition at line 30 of file `sf_cardinal.tcc`.

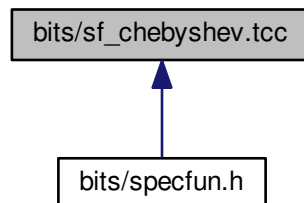
11.5 bits/sf_chebyshev.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_chebyshev.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_CHEBYSHEV_TCC 1](#)

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__chebyshev_recur` (unsigned int __n, _Tp __x, _Tp _C0, _Tp _C1)
- `template<typename _Tp >`
`_Tp std::__detail::__chebyshev_t` (unsigned int __n, _Tp __x)
- `template<typename _Tp >`
`_Tp std::__detail::__chebyshev_u` (unsigned int __n, _Tp __x)
- `template<typename _Tp >`
`_Tp std::__detail::__chebyshev_v` (unsigned int __n, _Tp __x)
- `template<typename _Tp >`
`_Tp std::__detail::__chebyshev_w` (unsigned int __n, _Tp __x)

11.5.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.5.2 Macro Definition Documentation

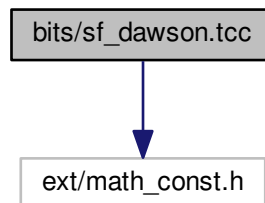
11.5.2.1 `#define _GLIBCXX_BITS_SF_CHEBYSHEV_TCC 1`

Definition at line 31 of file `sf_chebyshev.tcc`.

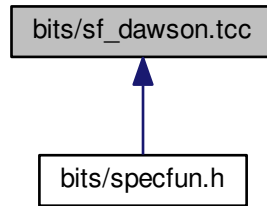
11.6 `bits/sf_dawson.tcc` File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for `sf_dawson.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_DAWSON_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__dawson \(_Tp __x\)](#)
Return the Dawson integral, $F(x)$, for real argument x .
- [template<typename _Tp > _Tp std::__detail::__dawson_cont_frac \(_Tp __x\)](#)
Compute the Dawson integral using a sampling theorem representation.
- [template<typename _Tp > _Tp std::__detail::__dawson_series \(_Tp __x\)](#)
Compute the Dawson integral using the series expansion.

11.6.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.6.2 Macro Definition Documentation

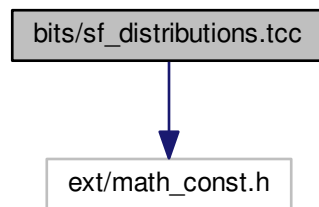
11.6.2.1 [#define _GLIBCXX_BITS_SF_DAWSON_TCC 1](#)

Definition at line 31 of file `sf_dawson.tcc`.

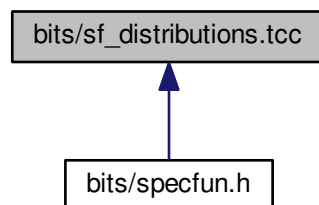
11.7 bits/sf_distributions.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_distributions.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_DISTRIBUTIONS_TCC](#) 1

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__binomial_cdf (_Tp __p, unsigned int __n, unsigned int __k)`
Return the binomial cumulative distribution function.
- `template<typename _Tp >`
`_Tp std::__detail::__binomial_cdfc (_Tp __p, unsigned int __n, unsigned int __k)`
Return the complementary binomial cumulative distribution function.
- `template<typename _Tp >`
`_Tp std::__detail::__binomial_pdf (_Tp __p, unsigned int __n, unsigned int __k)`
Return the binomial probability mass function.
- `template<typename _Tp >`
`_Tp std::__detail::__chi_squared_pdf (_Tp __chi2, unsigned int __nu)`
Return the chi-squared propability function. This returns the probability that the observed chi-squared for a correct model is less than the value χ^2 .
- `template<typename _Tp >`
`_Tp std::__detail::__chi_squared_pdfc (_Tp __chi2, unsigned int __nu)`
Return the complementary chi-squared probability function. This returns the probability that the observed chi-squared for a correct model is greater than the value χ^2 .
- `template<typename _Tp >`
`_Tp std::__detail::__exponential_cdf (_Tp __lambda, _Tp __x)`
Return the exponential cumulative probability density function.
- `template<typename _Tp >`
`_Tp std::__detail::__exponential_cdfc (_Tp __lambda, _Tp __x)`
Return the complement of the exponential cumulative probability density function.
- `template<typename _Tp >`
`_Tp std::__detail::__exponential_pdf (_Tp __lambda, _Tp __x)`
Return the exponential probability density function.
- `template<typename _Tp >`
`_Tp std::__detail::__fisher_f_cdf (_Tp __F, unsigned int __nu1, unsigned int __nu2)`
Return the F-distribution propability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .
- `template<typename _Tp >`
`_Tp std::__detail::__fisher_f_cdfc (_Tp __F, unsigned int __nu1, unsigned int __nu2)`
Return the F-distribution propability function. This returns the probability that the observed chi-square for a correct model exceeds the value χ^2 .
- `template<typename _Tp >`
`_Tp std::__detail::__gamma_cdf (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma cumulative propability distribution function.
- `template<typename _Tp >`
`_Tp std::__detail::__gamma_cdfc (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma complementary cumulative propability distribution function.
- `template<typename _Tp >`
`_Tp std::__detail::__gamma_pdf (_Tp __alpha, _Tp __beta, _Tp __x)`
Return the gamma propability distribution function.
- `template<typename _Tp >`
`_Tp std::__detail::__lognormal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`
Return the lognormal cumulative probability density function.
- `template<typename _Tp >`
`_Tp std::__detail::__lognormal_pdf (_Tp __mu, _Tp __sigma, _Tp __x)`

Return the lognormal probability density function.

- `template<typename _Tp >`
`_Tp std::__detail::__normal_cdf (_Tp __mu, _Tp __sigma, _Tp __x)`

Return the normal cumulative probability density function.

- `template<typename _Tp >`
`_Tp std::__detail::__normal_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the normal probability density function.

- `template<typename _Tp >`
`_Tp std::__detail::__rice_pdf (_Tp __nu, _Tp __sigma, _Tp __x)`

Return the Rice probability density function.

- `template<typename _Tp >`
`_Tp std::__detail::__student_t_cdf (_Tp __t, unsigned int __nu)`

Return the Students T probability function.

- `template<typename _Tp >`
`_Tp std::__detail::__student_t_cdfc (_Tp __t, unsigned int __nu)`

Return the complement of the Students T probability function.

- `template<typename _Tp >`
`_Tp std::__detail::__weibull_cdf (_Tp __a, _Tp __b, _Tp __x)`

Return the Weibull cumulative probability density function.

- `template<typename _Tp >`
`_Tp std::__detail::__weibull_pdf (_Tp __a, _Tp __b, _Tp __x)`

Return the Weibull probability density function.

11.7.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.7.2 Macro Definition Documentation

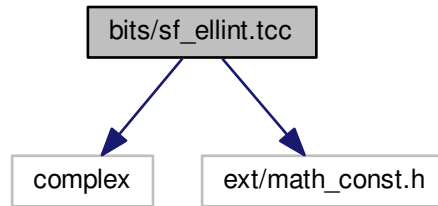
11.7.2.1 `#define _GLIBCXX_BITS_SF_DISTRIBUTIONS_TCC 1`

Definition at line 49 of file `sf_distributions.tcc`.

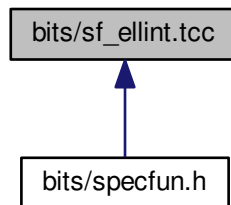
11.8 `bits/sf_ellint.tcc` File Reference

```
#include <complex>
#include <ext/math_const.h>
```

Include dependency graph for sf_ellint.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- `std`
- `std::__detail`

Macros

- `#define _GLIBCXX_BITS_SF_ELLINT_TCC 1`

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_1 (_Tp __k)`
Return the complete elliptic integral of the first kind $K(k)$ using the Carlson formulation.

- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_2 (_Tp __k)`
Return the complete elliptic integral of the second kind $E(k)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_3 (_Tp __k, _Tp __nu)`
Return the complete elliptic integral of the third kind $\Pi(k, \nu) = \Pi(k, \nu, \pi/2)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_d (_Tp __k)`
- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_rf (_Tp __x, _Tp __y)`
- `template<typename _Tp >`
`_Tp std::__detail::__comp_ellint_rg (_Tp __x, _Tp __y)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_1 (_Tp __k, _Tp __phi)`
Return the incomplete elliptic integral of the first kind $F(k, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_2 (_Tp __k, _Tp __phi)`
Return the incomplete elliptic integral of the second kind $E(k, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_3 (_Tp __k, _Tp __nu, _Tp __phi)`
Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ using the Carlson formulation.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_cel (_Tp __k_c, _Tp __p, _Tp __a, _Tp __b)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_d (_Tp __k, _Tp __phi)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_el1 (_Tp __x, _Tp __k_c)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_el2 (_Tp __x, _Tp __k_c, _Tp __a, _Tp __b)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_el3 (_Tp __x, _Tp __k_c, _Tp __p)`
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_rc (_Tp __x, _Tp __y)`
Return the Carlson elliptic function $R_C(x, y) = R_F(x, y, y)$ where $R_F(x, y, z)$ is the Carlson elliptic function of the first kind.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_rd (_Tp __x, _Tp __y, _Tp __z)`
Return the Carlson elliptic function of the second kind $R_D(x, y, z) = R_J(x, y, z, z)$ where $R_J(x, y, z, p)$ is the Carlson elliptic function of the third kind.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_rf (_Tp __x, _Tp __y, _Tp __z)`
Return the Carlson elliptic function $R_F(x, y, z)$ of the first kind.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_rg (_Tp __x, _Tp __y, _Tp __z)`
Return the symmetric Carlson elliptic function of the second kind $R_G(x, y, z)$.
- `template<typename _Tp >`
`_Tp std::__detail::__ellint_rj (_Tp __x, _Tp __y, _Tp __z, _Tp __p)`
Return the Carlson elliptic function $R_J(x, y, z, p)$ of the third kind.
- `template<typename _Tp >`
`_Tp std::__detail::__heuman_lambda (_Tp __k, _Tp __phi)`
- `template<typename _Tp >`
`_Tp std::__detail::__jacobi_zeta (_Tp __k, _Tp __phi)`

11.8.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.8.2 Macro Definition Documentation

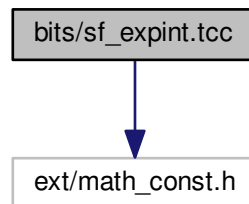
11.8.2.1 `#define _GLIBCXX_BITS_SF_ELLINT_TCC 1`

Definition at line 47 of file `sf_ellint.tcc`.

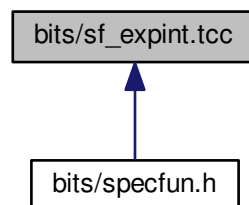
11.9 bits/sf_expint.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for `sf_expint.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_EXPINT_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__coshint \(const _Tp __x\)](#)
Return the hyperbolic cosine integral $Chi(x)$.
- [template<typename _Tp > _Tp std::__detail::__expint \(unsigned int __n, _Tp __x\)](#)
Return the exponential integral $E_n(x)$.
- [template<typename _Tp > _Tp std::__detail::__expint \(_Tp __x\)](#)
Return the exponential integral $Ei(x)$.
- [template<typename _Tp > _Tp std::__detail::__expint_E1 \(_Tp __x\)](#)
Return the exponential integral $E_1(x)$.
- [template<typename _Tp > _Tp std::__detail::__expint_E1_asymp \(_Tp __x\)](#)
Return the exponential integral $E_1(x)$ by asymptotic expansion.
- [template<typename _Tp > _Tp std::__detail::__expint_E1_series \(_Tp __x\)](#)
Return the exponential integral $E_1(x)$ by series summation. This should be good for $x < 1$.
- [template<typename _Tp > _Tp std::__detail::__expint_Ei \(_Tp __x\)](#)
Return the exponential integral $Ei(x)$.
- [template<typename _Tp > _Tp std::__detail::__expint_Ei_asymp \(_Tp __x\)](#)
Return the exponential integral $Ei(x)$ by asymptotic expansion.
- [template<typename _Tp > _Tp std::__detail::__expint_Ei_series \(_Tp __x\)](#)
Return the exponential integral $Ei(x)$ by series summation.
- [template<typename _Tp > _Tp std::__detail::__expint_En_asymp \(unsigned int __n, _Tp __x\)](#)
Return the exponential integral $E_n(x)$ for large argument.
- [template<typename _Tp > _Tp std::__detail::__expint_En_cont_frac \(unsigned int __n, _Tp __x\)](#)
Return the exponential integral $E_n(x)$ by continued fractions.
- [template<typename _Tp > _Tp std::__detail::__expint_En_large_n \(unsigned int __n, _Tp __x\)](#)
Return the exponential integral $E_n(x)$ for large order.

- `template<typename _Tp >`
`_Tp std::__detail::__expint_En_recursion` (unsigned int __n, _Tp __x)
Return the exponential integral $E_n(x)$ by recursion. Use upward recursion for $x < n$ and downward recursion (Miller's algorithm) otherwise.
- `template<typename _Tp >`
`_Tp std::__detail::__expint_En_series` (unsigned int __n, _Tp __x)
Return the exponential integral $E_n(x)$ by series summation.
- `template<typename _Tp >`
`_Tp std::__detail::__logint` (const _Tp __x)
Return the logarithmic integral $li(x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__sinhint` (const _Tp __x)
Return the hyperbolic sine integral $Shi(x)$.

11.9.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

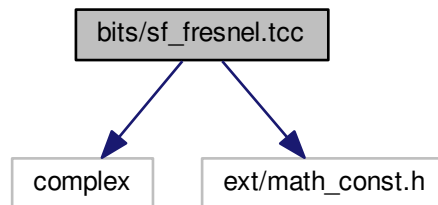
11.9.2 Macro Definition Documentation

11.9.2.1 `#define _GLIBCXX_BITS_SF_EXPINT_TCC 1`

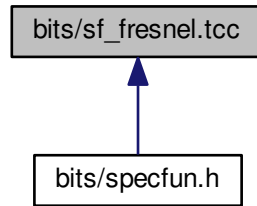
Definition at line 47 of file `sf_expint.tcc`.

11.10 bits/sf_fresnel.tcc File Reference

```
#include <complex>
#include <ext/math_const.h>
Include dependency graph for sf_fresnel.tcc:
```



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_FRESNEL_TCC 1](#)

Functions

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__fresnel (const _Tp __x)`
Return the Fresnel cosine and sine integrals as a complex number $C(x) + iS(x)$ xf .
- `template<typename _Tp >`
`void std::__detail::__fresnel_cont_frac (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`
This function computes the Fresnel cosine and sine integrals by continued fractions for positive argument.
- `template<typename _Tp >`
`void std::__detail::__fresnel_series (const _Tp __ax, _Tp &_Cf, _Tp &_Sf)`
This function returns the Fresnel cosine and sine integrals as a pair by series expansion for positive argument.

11.10.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.10.2 Macro Definition Documentation

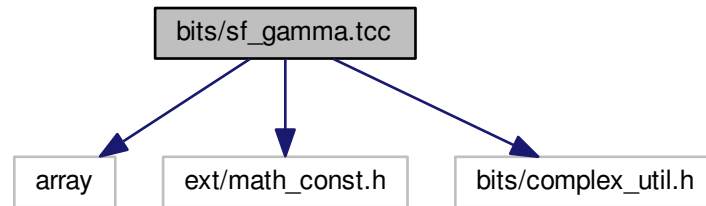
11.10.2.1 [#define _GLIBCXX_BITS_SF_FRESNEL_TCC 1](#)

Definition at line 31 of file `sf_fresnel.tcc`.

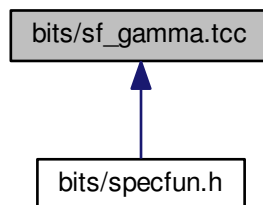
11.11 bits/sf_gamma.tcc File Reference

```
#include <array>
#include <ext/math_const.h>
#include <bits/complex_util.h>
```

Include dependency graph for sf_gamma.tcc:



This graph shows which files directly or indirectly include this file:



Classes

- struct [std::__detail::__gamma_lanczos_data< _Tp >](#)
- struct [std::__detail::__gamma_lanczos_data< double >](#)
- struct [std::__detail::__gamma_lanczos_data< float >](#)
- struct [std::__detail::__gamma_lanczos_data< long double >](#)
- struct [std::__detail::__gamma_spouge_data< _Tp >](#)
- struct [std::__detail::__gamma_spouge_data< double >](#)
- struct [std::__detail::__gamma_spouge_data< float >](#)
- struct [std::__detail::__gamma_spouge_data< long double >](#)
- struct [std::__detail::__Factorial_table< _Tp >](#)

Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_GAMMA_TCC 1](#)

Functions

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli (int __n)`
This returns Bernoulli number B_n .
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli_2n (int __n)`
This returns Bernoulli number B_{2n} at even integer arguments $2n$.
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__bernoulli_series (unsigned int __n)`
This returns Bernoulli numbers from a table or by summation for larger values.

- `template<typename _Tp >`
`_Tp std::__detail::__bincoef (unsigned int __n, unsigned int __k)`
Return the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

- `template<typename _Tp >`
`_Tp std::__detail::__bincoef (_Tp __nu, unsigned int __k)`
Return the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__double_factorial (int __n)`
Return the double factorial of the integer n .
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__factorial (unsigned int __n)`
Return the factorial of the integer n .
- `template<typename _Tp >`
`_Tp std::__detail::__gamma (_Tp __a)`

Return the gamma function $\Gamma(a)$. The gamma function is defined by:

$$\Gamma(a) = \int_0^{\infty} e^{-t} t^{a-1} dt (a > 0)$$

- `template<typename _Tp >`
`std::pair< _Tp, _Tp > std::__detail::__gamma_cont_frac (_Tp __a, _Tp __x)`

Return the incomplete gamma function by continued fraction.

- `template<typename _Tp >`
`_Tp std::__detail::__gamma_reciprocal_series (_Tp __a)`
- `template<typename _Tp >`
`std::pair< _Tp, _Tp > std::__detail::__gamma_series (_Tp __a, _Tp __x)`

Return the incomplete gamma function by series summation.

$$\gamma(a, x) = x^a e^{-x} \sum_{k=1}^{\infty} \frac{x^k}{(a)_k}$$

- `template<typename _Tp >`
`_Tp std::__detail::__harmonic_number (unsigned int __n)`
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__lanczos_binet1p (_Tp __z)`

Return the Binet function $J(1+z)$ by the Lanczos method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^*(z))$ defined by

$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__lanczos_log_gamma1p (_Tp __z)`

Return the logarithm of the gamma function $\log(\Gamma(1+z))$ by the Lanczos method.

- `template<typename _Tp >`
`_Tp std::__detail::__log_bincoef (unsigned int __n, unsigned int __k)`

Return the logarithm of the binomial coefficient. The binomial coefficient is given by:

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

The binomial coefficients are generated by:

$$(1+t)^n = \sum_{k=0}^n \binom{n}{k} t^k$$

- `template<typename _Tp >`
`_Tp std::__detail::__log_bincoef (_Tp __nu, unsigned int __k)`

Return the logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu+1)}{\Gamma(\nu-k+1)\Gamma(k+1)}$$

The binomial coefficients are generated by:

$$(1+t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- `template<typename _Tp >`
`_Tp std::__detail::__log_bincoef_sign (_Tp __nu, unsigned int __k)`

Return the sign of the exponentiated logarithm of the binomial coefficient for non-integral degree. The binomial coefficient is given by:

$$\binom{\nu}{k} = \frac{\Gamma(\nu + 1)}{\Gamma(\nu - k + 1)\Gamma(k + 1)}$$

The binomial coefficients are generated by:

$$(1 + t)^\nu = \sum_{k=0}^{\infty} \binom{\nu}{k} t^k$$

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__log_bincoef_sign (std::complex< _Tp > __nu, unsigned int __k)`
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_double_factorial (_Tp __x)`
- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_double_factorial (int __n)`

Return the logarithm of the double factorial of the integer n.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_factorial (unsigned int __n)`

Return the logarithm of the factorial of the integer n.

- `template<typename _Tp >`
`_Tp std::__detail::__log_gamma (_Tp __a)`

Return $\log(|\Gamma(a)|)$. This will return values even for $a < 0$. To recover the sign of $\Gamma(a)$ for any argument use `__log_gamma_sign`.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__log_gamma (std::complex< _Tp > __a)`

Return $\log(\Gamma(a))$ for complex argument.

- `template<typename _Tp >`
`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__log_gamma_bernoulli (_Tp __x)`

Return $\log(\Gamma(x))$ by asymptotic expansion with Bernoulli number coefficients. This is like Sterling's approximation.

- `template<typename _Tp >`
`_Tp std::__detail::__log_gamma_sign (_Tp __a)`

Return the sign of $\Gamma(x)$. At nonpositive integers zero is returned indicating $\Gamma(x)$ is undefined.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__log_gamma_sign (std::complex< _Tp > __a)`

- `template<typename _Tp >`
`_Tp std::__detail::__log_pochhammer (_Tp __a, _Tp __nu)`

Return the logarithm of the (upper) Pochhammer symbol or the rising factorial function. The Pochhammer symbol is defined for integer order by

$$(a)_\nu = \Gamma(a + \nu)/\Gamma(a) = \prod_{k=0}^{\nu-1} (a + k), (a)_0 = 1$$

Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a + \nu)] - \ln[\Gamma(a)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp std::__detail::__log_pochhammer_lower (_Tp __a, _Tp __nu)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function. The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a+1)/\Gamma(a-\nu+1) = \prod_{k=0}^{n-1} (a-k), (a)_0 = 1$$

In particular, $(n)_n = n!$. Thus this function returns

$$\ln[(a)_\nu] = \ln[\Gamma(a+1)] - \ln[\Gamma(a-\nu+1)], \ln[(a)_0] = 0$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left\{ \begin{matrix} a \\ n \end{matrix} \right\}$$

, and others.

- `template<typename _Tp >`
`_Tp std::__detail::__pgamma (_Tp __a, _Tp __x)`

Return the regularized lower incomplete gamma function. The regularized lower incomplete gamma function is defined by

$$P(a, x) = \frac{\gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

is the lower incomplete gamma function.

- `template<typename _Tp >`
`_Tp std::__detail::__pochhammer (_Tp __a, int __n)`

Return the (upper) Pochhammer function or the rising factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a+\nu)/\Gamma(\nu) = \prod_{k=0}^{n-1} (a+k), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp std::__detail::__pochhammer (_Tp __a, _Tp __nu)`

Return the (upper) Pochhammer function or the rising factorial function. The Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a+\nu)/\Gamma(\nu) = \prod_{k=0}^{n-1} (a+k), (a)_0 = 1$$

Many notations exist:

$$a^{\overline{n}}$$

,

$$\left[\begin{matrix} a \\ n \end{matrix} \right]$$

, and others.

- `template<typename _Tp >`
`_Tp std::__detail::__pochhammer_lower (_Tp __a, int __n)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and integral order n . The lower Pochhammer symbol is defined by

$$(a)_n = \prod_{k=0}^{n-1} (a - k), (a)_0 = 1 = \Gamma(a + 1) / \Gamma(a - n + 1)$$

In particular, $(n)_n = n!$.

- `template<typename _Tp >`
`_Tp std::__detail::__pochhammer_lower (_Tp __a, _Tp __nu)`

Return the logarithm of the lower Pochhammer symbol or the falling factorial function for real argument a and order ν . The lower Pochhammer symbol is defined by

$$(a)_\nu = \Gamma(a + 1) / \Gamma(a - \nu + 1) = \prod_{k=0}^{n-1} (a - k), (a)_0 = 1, \nu = n$$

In particular, $(n)_n = n!$.

- `template<typename _Tp >`
`_Tp std::__detail::__psi (unsigned int __n)`

Return the digamma function of integral argument. The digamma or $\psi(x)$ function is defined as the logarithmic derivative of the gamma function:

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

The digamma series for integral argument is given by:

$$\psi(n) = -\gamma_E + \sum_{k=1}^{\infty} \frac{1}{k}$$

The latter sum is called the harmonic number, H_n .

- `template<typename _Tp >`
`_Tp std::__detail::__psi (_Tp __x)`

Return the digamma function. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

For negative argument the reflection formula is used:

$$\psi(x) = \psi(1 - x) - \pi \cot(\pi x)$$

- `template<typename _Tp >`
`_Tp std::__detail::__psi (unsigned int __n, _Tp __x)`

Return the polygamma function $\psi^{(n)}(x)$.

- `template<typename _Tp >`
`_Tp std::__detail::__psi_asymp (_Tp __x)`

Return the digamma function for large argument. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

- `template<typename _Tp >`
`_Tp std::__detail::__psi_series (_Tp __x)`

Return the digamma function by series expansion. The digamma or $\psi(x)$ function is defined by

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$

- template<typename _Tp >

`_Tp std::__detail::__qgamma (_Tp __a, _Tp __x)`

Return the regularized upper incomplete gamma function. The regularized upper incomplete gamma function is defined by

$$Q(a, x) = \frac{\Gamma(a, x)}{\Gamma(a)}$$

where $\Gamma(a)$ is the gamma function and

$$\Gamma(a, x) = \int_x^\infty e^{-t} t^{a-1} dt (a > 0)$$

is the upper incomplete gamma function.

- template<typename _Tp >

`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__spouge_binet1p (_Tp __z)`

Return the Binet function $J(1+z)$ by the Spouge method. The Binet function is the log of the scaled Gamma function $\log(\Gamma^*(z))$ defined by

$$J(z) = \log(\Gamma^*(z)) = \log(\Gamma(z)) + z - \left(z - \frac{1}{2}\right) \log(z) - \log(2\pi)$$

or

$$\Gamma(z) = \sqrt{2\pi} z^{z-\frac{1}{2}} e^{-z} e^{J(z)}$$

where $\Gamma(z)$ is the gamma function.

- template<typename _Tp >

`_GLIBCXX14_CONSTEXPR _Tp std::__detail::__spouge_log_gamma1p (_Tp __z)`

Return the logarithm of the gamma function $\log(\Gamma(1+z))$ by the Spouge algorithm:

$$\Gamma(z+1) = (z+a)^{z+1/2} e^{-z-a} \left[\sqrt{2\pi} + \sum_{k=1}^{\lceil a \rceil + 1} \frac{c_k(a)}{z+k} \right]$$

where

$$c_k(a) = \frac{(-1)^{k-1}}{(k-1)!} (a-k)^{k-1/2} e^{a-k}$$

and the error is bounded by

$$\epsilon(a) < a^{-1/2} (2\pi)^{-a-1/2}$$

- template<typename _Tp >

`_Tp std::__detail::__tgamma (_Tp __a, _Tp __x)`

Return the upper incomplete gamma function. The lower incomplete gamma function is defined by

$$\Gamma(a, x) = \int_x^\infty e^{-t} t^{a-1} dt (a > 0)$$

- template<typename _Tp >

`_Tp std::__detail::__tgamma_lower (_Tp __a, _Tp __x)`

Return the lower incomplete gamma function. The lower incomplete gamma function is defined by

$$\gamma(a, x) = \int_0^x e^{-t} t^{a-1} dt (a > 0)$$

Variables

- constexpr _Factorial_table< long double > [std::__detail::_S_double_factorial_table](#) [301]
- constexpr _Factorial_table< long double > [std::__detail::_S_factorial_table](#) [171]
- constexpr unsigned long long [std::__detail::_S_harmonic_denom](#) [_S_num_harmonic_number]
- constexpr unsigned long long [std::__detail::_S_harmonic_number](#) [_S_num_harmonic_number]
- constexpr _Factorial_table< long double > [std::__detail::_S_neg_double_factorial_table](#) [999]
- template<typename _Tp >
constexpr std::size_t [std::__detail::_S_num_double_factorials](#) = 0
- template<>
constexpr std::size_t [std::__detail::_S_num_double_factorials< double >](#) = 301
- template<>
constexpr std::size_t [std::__detail::_S_num_double_factorials< float >](#) = 57
- template<>
constexpr std::size_t [std::__detail::_S_num_double_factorials< long double >](#) = 301
- template<typename _Tp >
constexpr std::size_t [std::__detail::_S_num_factorials](#) = 0
- template<>
constexpr std::size_t [std::__detail::_S_num_factorials< double >](#) = 171
- template<>
constexpr std::size_t [std::__detail::_S_num_factorials< float >](#) = 35
- template<>
constexpr std::size_t [std::__detail::_S_num_factorials< long double >](#) = 171
- constexpr unsigned long long [std::__detail::_S_num_harmonic_number](#) = 29
- template<typename _Tp >
constexpr std::size_t [std::__detail::_S_num_neg_double_factorials](#) = 0
- template<>
constexpr std::size_t [std::__detail::_S_num_neg_double_factorials< double >](#) = 150
- template<>
constexpr std::size_t [std::__detail::_S_num_neg_double_factorials< float >](#) = 27
- template<>
constexpr std::size_t [std::__detail::_S_num_neg_double_factorials< long double >](#) = 999

11.11.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.11.2 Macro Definition Documentation

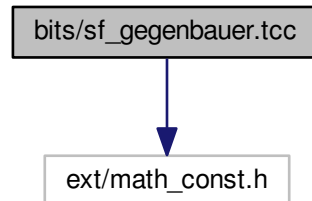
11.11.2.1 `#define _GLIBCXX_BITS_SF_GAMMA_TCC 1`

Definition at line 49 of file `sf_gamma.tcc`.

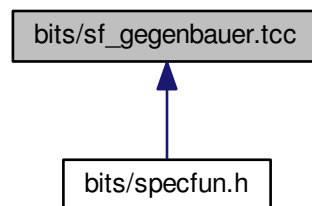
11.12 bits/sf_gegenbauer.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_gegenbauer.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_GEGENBAUER_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__gegenbauer_poly](#) (unsigned int __n, _Tp __alpha, _Tp __x)

11.12.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.12.2 Macro Definition Documentation

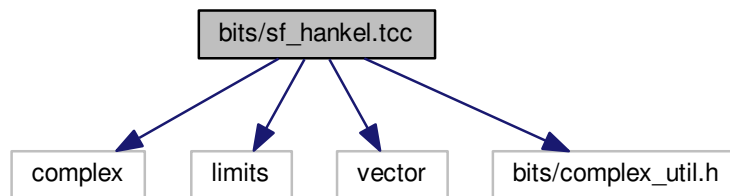
11.12.2.1 `#define _GLIBCXX_BITS_SF_GEGENBAUER_TCC 1`

Definition at line 31 of file `sf_gegenbauer.tcc`.

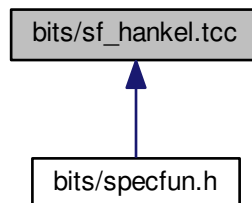
11.13 `bits/sf_hankel.tcc` File Reference

```
#include <complex>
#include <limits>
#include <vector>
#include <bits/complex_util.h>
```

Include dependency graph for `sf_hankel.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- `#define _GLIBCXX_BITS_SF_HANKEL_TCC 1`

Functions

- `template<typename _Tp >`
`void std::__detail::__airy_arg (std::complex< _Tp > __num2d3, std::complex< _Tp > __zeta, std::complex< _Tp > &__argp, std::complex< _Tp > &__argm)`
Compute the arguments for the Airy function evaluations carefully to prevent premature overflow. Note that the major work here is in `safe_div`. A faster, but less safe implementation can be obtained without use of `safe_div`.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_bessel (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
Return the complex cylindrical Bessel function.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_hankel_1 (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
Return the complex cylindrical Hankel function of the first kind.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_hankel_2 (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
Return the complex cylindrical Hankel function of the second kind.
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__cyl_neumann (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
Return the complex cylindrical Neumann function.
- `template<typename _Tp >`
`void std::__detail::__debye_region (std::complex< _Tp > __alpha, int &__indexr, char &__aorb)`
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > std::__detail::__hankel (std::complex< _Tp > __nu, std::complex< _Tp > __z)`
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > std::__detail::__hankel_debye (std::complex< _Tp > __nu, std::complex< _Tp > __z, std::complex< _Tp > __alpha, int __indexr, char &__aorb, int &__morn)`
- `template<typename _Tp >`
`void std::__detail::__hankel_params (std::complex< _Tp > __nu, std::complex< _Tp > __zhat, std::complex< _Tp > &__p, std::complex< _Tp > &__p2, std::complex< _Tp > &__nup2, std::complex< _Tp > &__num2, std::complex< _Tp > &__num1d3, std::complex< _Tp > &__num2d3, std::complex< _Tp > &__num4d3, std::complex< _Tp > &__zeta, std::complex< _Tp > &__zetaphf, std::complex< _Tp > &__zetamhf, std::complex< _Tp > &__zetam3hf, std::complex< _Tp > &__zetrat)`
Compute parameters depending on z and nu that appear in the uniform asymptotic expansions of the Hankel functions and their derivatives, except the arguments to the Airy functions.
- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > std::__detail::__hankel_uniform (std::complex< _Tp > __nu, std::complex< _Tp > __z)`

This routine computes the uniform asymptotic approximations of the Hankel functions and their derivatives including a patch for the case when the order equals or nearly equals the argument. At such points, Olver's expressions have zero denominators (and numerators) resulting in numerical problems. This routine averages results from four surrounding points in the complex plane to obtain the result in such cases.

- `template<typename _Tp >`
`__gnu_cxx::__cyl_hankel_t< std::complex< _Tp >, std::complex< _Tp >, std::complex< _Tp > > std::__detail::__hankel_uniform_olver (std::complex< _Tp > __nu, std::complex< _Tp > __z)`

Compute approximate values for the Hankel functions of the first and second kinds using Olver's uniform asymptotic expansion to of order `nu` along with their derivatives.

- `template<typename _Tp >`
`void std::__detail::__hankel_uniform_outer (std::complex< _Tp > __nu, std::complex< _Tp > __z, _Tp __eps, std::complex< _Tp > &__zhat, std::complex< _Tp > &__1dnsq, std::complex< _Tp > &__num1d3, std::complex< _Tp > &__num2d3, std::complex< _Tp > &__p, std::complex< _Tp > &__p2, std::complex< _Tp > &__etm3h, std::complex< _Tp > &__etrat, std::complex< _Tp > &__Aip, std::complex< _Tp > &__o4dp, std::complex< _Tp > &__Aim, std::complex< _Tp > &__o4dm, std::complex< _Tp > &__od2p, std::complex< _Tp > &__od0dp, std::complex< _Tp > &__od2m, std::complex< _Tp > &__od0dm)`

Compute outer factors and associated functions of `z` and `nu` appearing in Olver's uniform asymptotic expansions of the Hankel functions of the first and second kinds and their derivatives. The various functions of `z` and `nu` returned by `hankel_uniform_outer` are available for use in computing further terms in the expansions.

- `template<typename _Tp >`
`void std::__detail::__hankel_uniform_sum (std::complex< _Tp > __p, std::complex< _Tp > __p2, std::complex< _Tp > __num2, std::complex< _Tp > __zetam3hf, std::complex< _Tp > __Aip, std::complex< _Tp > __o4dp, std::complex< _Tp > __Aim, std::complex< _Tp > __o4dm, std::complex< _Tp > __od2p, std::complex< _Tp > __od0dp, std::complex< _Tp > __od2m, std::complex< _Tp > __od0dm, _Tp __eps, std::complex< _Tp > &__H1sum, std::complex< _Tp > &__H1psum, std::complex< _Tp > &__H2sum, std::complex< _Tp > &__H2psum)`

Compute the sums in appropriate linear combinations appearing in Olver's uniform asymptotic expansions for the Hankel functions of the first and second kinds and their derivatives, using up to `nterms` (less than 5) to achieve relative error `eps`.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_bessel (unsigned int __n, std::complex< _Tp > __z)`

Return the complex spherical Bessel function.

- `template<typename _Tp >`
`__gnu_cxx::__sph_hankel_t< unsigned int, std::complex< _Tp >, std::complex< _Tp > > std::__detail::__sph_hankel (unsigned int __n, std::complex< _Tp > __z)`

Helper to compute complex spherical Hankel functions and their derivatives.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_hankel_1 (unsigned int __n, std::complex< _Tp > __z)`

Return the complex spherical Hankel function of the first kind.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_hankel_2 (unsigned int __n, std::complex< _Tp > __z)`

Return the complex spherical Hankel function of the second kind.

- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_neumann (unsigned int __n, std::complex< _Tp > __z)`

Return the complex spherical Neumann function.

11.13.1 Detailed Description

This is an internal header file, included by other library headers. You should not attempt to use it directly.

11.13.2 Macro Definition Documentation

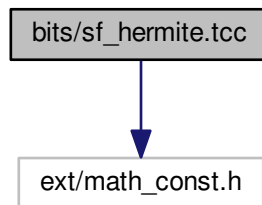
11.13.2.1 `#define _GLIBCXX_BITS_SF_HANKEL_TCC 1`

Definition at line 31 of file sf_hankel.tcc.

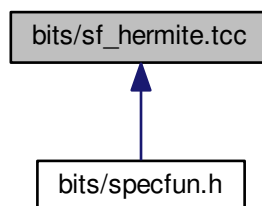
11.14 bits/sf_hermite.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_hermite.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- `#define _GLIBCXX_BITS_SF_HERMITE_TCC 1`

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__poly_hermite` (unsigned int __n, _Tp __x)
This routine returns the Hermite polynomial of order n : $H_n(x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__poly_hermite_asymp` (unsigned int __n, _Tp __x)
This routine returns the Hermite polynomial of large order n : $H_n(x)$. We assume here that $x \geq 0$.
- `template<typename _Tp >`
`_Tp std::__detail::__poly_hermite_recursion` (unsigned int __n, _Tp __x)
This routine returns the Hermite polynomial of order n : $H_n(x)$ by recursion on n .
- `template<typename _Tp >`
`_Tp std::__detail::__poly_prob_hermite_recursion` (unsigned int __n, _Tp __x)
This routine returns the Probabilists Hermite polynomial of order n : $He_n(x)$ by recursion on n .

11.14.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.14.2 Macro Definition Documentation

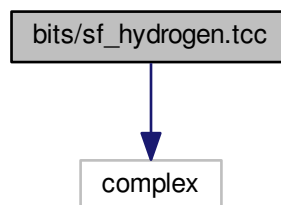
11.14.2.1 `#define _GLIBCXX_BITS_SF_HERMITE_TCC 1`

Definition at line 42 of file `sf_hermite.tcc`.

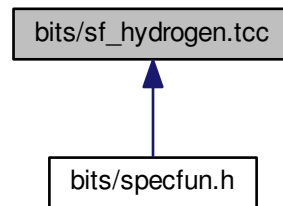
11.15 bits/sf_hydrogen.tcc File Reference

`#include <complex>`

Include dependency graph for `sf_hydrogen.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_HYDROGEN_TCC 1](#)

Functions

- [template<typename _Tp > std::complex< _Tp > std::__detail::__hydrogen \(unsigned int __n, unsigned int __l, unsigned int __m, _Tp __Z, _Tp __r, _Tp __theta, _Tp __phi\)](#)

11.15.1 Detailed Description

This is an internal header file, included by other library headers. You should not attempt to use it directly.

11.15.2 Macro Definition Documentation

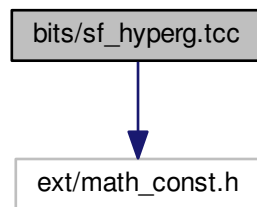
11.15.2.1 [#define _GLIBCXX_BITS_SF_HYDROGEN_TCC 1](#)

Definition at line 31 of file sf_hydrogen.tcc.

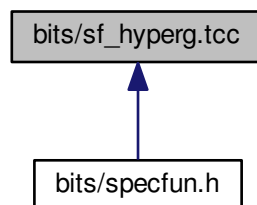
11.16 bits/sf_hyperg.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_hyperg.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_HYPERG_TCC](#) 1

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__conf_hyperg (_Tp __a, _Tp __c, _Tp __x)`
Return the confluent hypergeometric function ${}_1F_1(a; c; x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__conf_hyperg_lim (_Tp __c, _Tp __x)`
Return the confluent hypergeometric limit function ${}_0F_1(-; c; x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__conf_hyperg_lim_series (_Tp __c, _Tp __x)`
This routine returns the confluent hypergeometric limit function by series expansion.
- `template<typename _Tp >`
`_Tp std::__detail::__conf_hyperg_luke (_Tp __a, _Tp __c, _Tp __xin)`
Return the hypergeometric function ${}_1F_1(a; c; x)$ by an iterative procedure described in Luke, Algorithms for the Computation of Mathematical Functions.
- `template<typename _Tp >`
`_Tp std::__detail::__conf_hyperg_series (_Tp __a, _Tp __c, _Tp __x)`
This routine returns the confluent hypergeometric function by series expansion.
- `template<typename _Tp >`
`_Tp std::__detail::__hyperg (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__hyperg_luke (_Tp __a, _Tp __b, _Tp __c, _Tp __xin)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by an iterative procedure described in Luke, Algorithms for the Computation of Mathematical Functions.
- `template<typename _Tp >`
`_Tp std::__detail::__hyperg_reflect (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by the reflection formulae in Abramowitz & Stegun formula 15.3.6 for $d = c - a - b$ not integral and formula 15.3.11 for $d = c - a - b$ integral. This assumes $a, b, c \neq \text{negative integer}$.
- `template<typename _Tp >`
`_Tp std::__detail::__hyperg_series (_Tp __a, _Tp __b, _Tp __c, _Tp __x)`
Return the hypergeometric function ${}_2F_1(a, b; c; x)$ by series expansion.

11.16.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

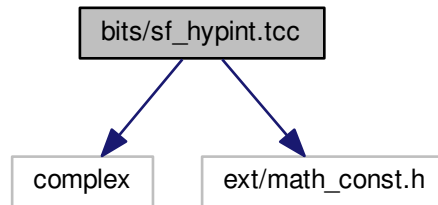
11.16.2 Macro Definition Documentation

11.16.2.1 `#define _GLIBCXX_BITS_SF_HYPERG_TCC 1`

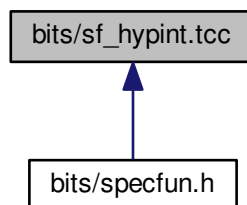
Definition at line 44 of file `sf_hyperg.tcc`.

11.17 bits/sf_hypint.tcc File Reference

```
#include <complex>
#include <ext/math_const.h>
Include dependency graph for sf_hypint.tcc:
```



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_HYPINT_TCC 1](#)

Functions

- `template<typename _Tp >`
`std::pair<_Tp, _Tp > std::__detail::__chshint (_Tp __x, _Tp &_Chi, _Tp &_Shi)`
This function returns the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals as a pair.
- `template<typename _Tp >`
`void std::__detail::__chshint_cont_frac (_Tp __t, _Tp &_Chi, _Tp &_Shi)`
This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by continued fraction for positive argument.
- `template<typename _Tp >`
`void std::__detail::__chshint_series (_Tp __t, _Tp &_Chi, _Tp &_Shi)`
This function computes the hyperbolic cosine $Chi(x)$ and hyperbolic sine $Shi(x)$ integrals by series summation for positive argument.

11.17.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.17.2 Macro Definition Documentation

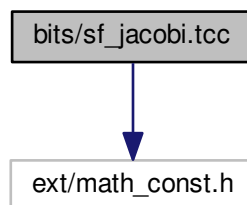
11.17.2.1 `#define _GLIBCXX_BITS_SF_HYPINT_TCC 1`

Definition at line 31 of file `sf_hypint.tcc`.

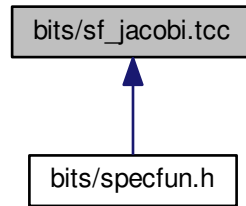
11.18 bits/sf_jacobi.tcc File Reference

`#include <ext/math_const.h>`

Include dependency graph for `sf_jacobi.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_JACOBI_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__poly_jacobi \(unsigned int __n, _Tp __alpha, _Tp __beta, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__poly_radial_jacobi \(unsigned int __n, unsigned int __m, _Tp __rho\)](#)
- [template<typename _Tp > __gnu_cxx::__promote_fp_t< _Tp > std::__detail::__zernike \(unsigned int __n, int __m, _Tp __rho, _Tp __phi\)](#)

11.18.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.18.2 Macro Definition Documentation

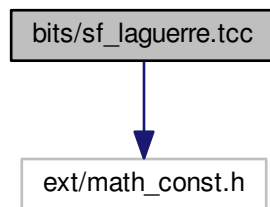
11.18.2.1 [#define _GLIBCXX_BITS_SF_JACOBI_TCC 1](#)

Definition at line 31 of file `sf_jacobi.tcc`.

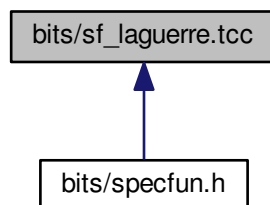
11.19 bits/sf_laguerre.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for sf_laguerre.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_LAGUERRE_TCC 1](#)

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__assoc_laguerre` (unsigned int __n, unsigned int __m, _Tp __x)
This routine returns the associated Laguerre polynomial of order n , degree m : $L_n^m(x)$.
- `template<typename _Tp >`
`_Tp std::__detail::__laguerre` (unsigned int __n, _Tp __x)
This routine returns the Laguerre polynomial of order n : $L_n(x)$.
- `template<typename _Tpa, typename _Tp >`
`_Tp std::__detail::__poly_laguerre` (unsigned int __n, _Tpa __alpha1, _Tp __x)
This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^\alpha(x)$.
- `template<typename _Tpa, typename _Tp >`
`_Tp std::__detail::__poly_laguerre_hyperg` (unsigned int __n, _Tpa __alpha1, _Tp __x)
Evaluate the polynomial based on the confluent hypergeometric function in a safe way, with no restriction on the arguments.
- `template<typename _Tpa, typename _Tp >`
`_Tp std::__detail::__poly_laguerre_large_n` (unsigned __n, _Tpa __alpha1, _Tp __x)
This routine returns the associated Laguerre polynomial of order n , degree $\alpha > -1$ for large n . Abramowitz & Stegun, 13.5.21.
- `template<typename _Tpa, typename _Tp >`
`_Tp std::__detail::__poly_laguerre_recursion` (unsigned int __n, _Tpa __alpha1, _Tp __x)
This routine returns the associated Laguerre polynomial of order n , degree α : $L_n^\alpha(x)$ by recursion.

11.19.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.19.2 Macro Definition Documentation

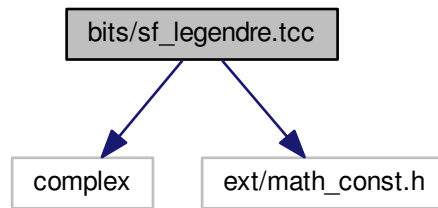
11.19.2.1 `#define _GLIBCXX_BITS_SF_LAGUERRE_TCC 1`

Definition at line 44 of file `sf_laguerre.tcc`.

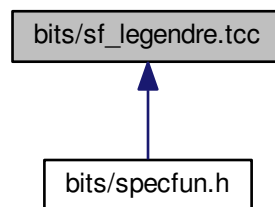
11.20 bits/sf_legendre.tcc File Reference

```
#include <complex>
#include <ext/math_const.h>
```

Include dependency graph for sf_legendre.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_LEGENDRE_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__assoc_legendre_p \(unsigned int __l, unsigned int __m, _Tp __x\)](#)
Return the associated Legendre function by recursion on l and downward recursion on m .

- `template<typename _Tp >`
`_Tp std::__detail::__legendre_q (unsigned int __l, _Tp __x)`
Return the Legendre function of the second kind by upward recursion on order l .
- `template<typename _Tp >`
`_Tp std::__detail::__poly_legendre_p (unsigned int __l, _Tp __x)`
Return the Legendre polynomial by upward recursion on order l .
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sph_harmonic (unsigned int __l, int __m, _Tp __theta, _Tp __phi)`
Return the spherical harmonic function.
- `template<typename _Tp >`
`_Tp std::__detail::__sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta)`
Return the spherical associated Legendre function.

11.20.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.20.2 Macro Definition Documentation

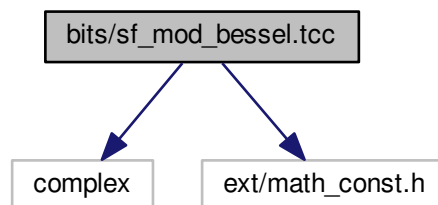
11.20.2.1 `#define _GLIBCXX_BITS_SF_LEGENDRE_TCC 1`

Definition at line 47 of file `sf_legendre.tcc`.

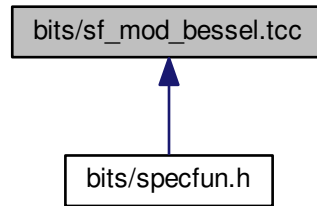
11.21 `bits/sf_mod_bessel.tcc` File Reference

```
#include <complex>
#include <ext/math_const.h>
```

Include dependency graph for `sf_mod_bessel.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_MOD_BESSEL_TCC 1](#)

Functions

- `template<typename _Tp >`
`__gnu_cxx::__airy_t< _Tp, _Tp > std::__detail::__airy (_Tp __z)`
Compute the Airy functions $Ai(x)$ and $Bi(x)$ and their first derivatives $Ai'(x)$ and $Bi'(x)$ respectively.
- `template<typename _Tp >`
`_Tp std::__detail::__cyl_bessel_i (_Tp __nu, _Tp __x)`
Return the regular modified Bessel function of order ν : $I_\nu(x)$.
- `template<typename _Tp >`
`__gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_ik (_Tp __nu, _Tp __x)`
Return the modified cylindrical Bessel functions and their derivatives of order ν by various means.
- `template<typename _Tp >`
`__gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_ik_asymp (_Tp __nu, _Tp __x)`
This routine computes the asymptotic modified cylindrical Bessel and functions of order ν : $I_\nu(x)$, $N_\nu(x)$. Use this for $x \gg \nu^2 + 1$.
- `template<typename _Tp >`
`__gnu_cxx::__cyl_mod_bessel_t< _Tp, _Tp, _Tp > std::__detail::__cyl_bessel_ik_steel (_Tp __nu, _Tp __x)`
Compute the modified Bessel functions $I_\nu(x)$ and $K_\nu(x)$ and their first derivatives $I'_\nu(x)$ and $K'_\nu(x)$ respectively. These four functions are computed together for numerical stability.
- `template<typename _Tp >`
`_Tp std::__detail::__cyl_bessel_k (_Tp __nu, _Tp __x)`
Return the irregular modified Bessel function $K_\nu(x)$ of order ν .

- `template<typename _Tp >`
`__gnu_cxx::__fock_airy_t< _Tp, std::complex< _Tp > > std::__detail::__fock_airy (_Tp __x)`
Compute the Fock-type Airy functions $w_1(x)$ and $w_2(x)$ and their first derivatives $w_1'(x)$ and $w_2'(x)$ respectively.

$$w_1(x) = \sqrt{\pi}(Ai(x) + iBi(x))$$

$$w_2(x) = \sqrt{\pi}(Ai(x) - iBi(x))$$
- `template<typename _Tp >`
`__gnu_cxx::__sph_mod_bessel_t< unsigned int, _Tp, _Tp > std::__detail::__sph_bessel_ik (unsigned int __n, _Tp __x)`
Compute the spherical modified Bessel functions $i_n(x)$ and $k_n(x)$ and their first derivatives $i_n'(x)$ and $k_n'(x)$ respectively.

11.21.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

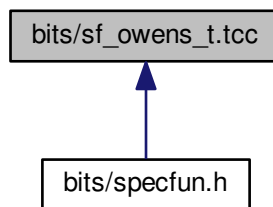
11.21.2 Macro Definition Documentation

11.21.2.1 `#define _GLIBCXX_BITS_SF_MOD_BESSEL_TCC 1`

Definition at line 47 of file `sf_mod_bessel.tcc`.

11.22 `bits/sf_owens_t.tcc` File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- `std`
- `std::__detail`

Macros

- `#define _GLIBCXX_BITS_SF_OWENS_T_TCC 1`

Functions

- `template<typename _Tp >
_Tp std::__detail::__gauss (_Tp __x)`
- `template<typename _Tp >
_Tp std::__detail::__owens_t (_Tp __h, _Tp __a)`
- `template<typename _Tp >
_Tp std::__detail::__znorm1 (_Tp __x)`
- `template<typename _Tp >
_Tp std::__detail::__znorm2 (_Tp __x)`

11.22.1 Detailed Description

This is an internal header file, included by other library headers. You should not attempt to use it directly.

11.22.2 Macro Definition Documentation

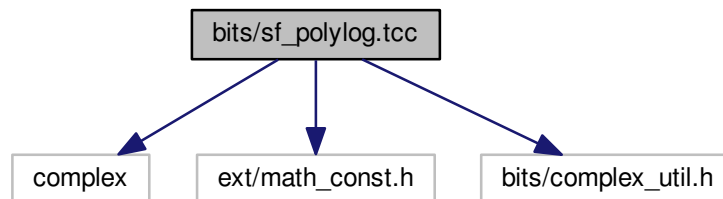
11.22.2.1 `#define _GLIBCXX_BITS_SF_OWENS_T_TCC 1`

Definition at line 31 of file `sf_owens_t.tcc`.

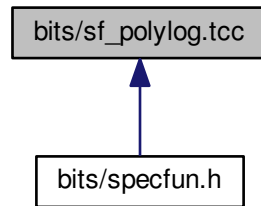
11.23 bits/sf_polylog.tcc File Reference

```
#include <complex>
#include <ext/math_const.h>
#include <bits/complex_util.h>
```

Include dependency graph for `sf_polylog.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_POLYLOG_TCC 1](#)

Functions

- [template<typename _Sp, typename _Tp > _Tp std::__detail::__bose_einstein \(_Sp __s, _Tp __x\)](#)
- [template<typename _Tp > std::complex< _Tp > std::__detail::__clamp_0_m2pi \(std::complex< _Tp > __w\)](#)
- [template<typename _Tp > std::complex< _Tp > std::__detail::__clamp_pi \(std::complex< _Tp > __w\)](#)
- [template<typename _Tp > std::complex< _Tp > std::__detail::__clausen \(unsigned int __m, std::complex< _Tp > __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__clausen \(unsigned int __m, _Tp __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__clausen_c \(unsigned int __m, std::complex< _Tp > __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__clausen_c \(unsigned int __m, _Tp __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__clausen_s \(unsigned int __m, std::complex< _Tp > __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__clausen_s \(unsigned int __m, _Tp __w\)](#)
- [template<typename _Tp > _Tp std::__detail::__dirichlet_beta \(std::complex< _Tp > __w\)](#)

- `template<typename _Tp >`
`_Tp std::__detail::__dirichlet_beta (_Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__dirichlet_eta (std::complex< _Tp > __w)`
- `template<typename _Tp >`
`_Tp std::__detail::__dirichlet_eta (_Tp __w)`
- `template<typename _Tp >`
`_Tp std::__detail::__dirichlet_lambda (_Tp __w)`
- `template<typename _Sp, typename _Tp >`
`_Tp std::__detail::__fermi_dirac (_Sp __s, _Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__hurwitz_zeta_polylog (_Tp __s, std::complex< _Tp > __a)`
- `template<typename _Tp >`
`_Tp std::__detail::__polylog (_Tp __s, _Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp, typename ArgType >`
`__gnu_cxx::__promote_fp_t< std::complex< _Tp >, ArgType > std::__detail::__polylog_exp (_Tp __s, ArgType __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_asymp (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_int_neg (int __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_int_neg (const int __s, _Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_int_pos (unsigned int __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_int_pos (unsigned int __s, _Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_neg (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_neg (int __s, std::complex< _Tp > __w)`
- `template<typename _Tp, int __sigma>`
`std::complex< _Tp > std::__detail::__polylog_exp_neg_even (unsigned int __n, std::complex< _Tp > __w)`
- `template<typename _Tp, int __sigma>`
`std::complex< _Tp > std::__detail::__polylog_exp_neg_odd (unsigned int __n, std::complex< _Tp > __w)`
- `template<typename _PowTp, typename _Tp >`
`_Tp std::__detail::__polylog_exp_negative_real_part (_PowTp __s, _Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_pos (unsigned int __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_pos (unsigned int __s, _Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_pos (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_real_neg (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_real_neg (_Tp __s, _Tp __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_real_pos (_Tp __s, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__polylog_exp_real_pos (_Tp __s, _Tp __w)`

- `template<typename _Tp = double>`
`_Tp std::__detail::evenzeta (unsigned int __k)`

11.23.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.23.2 Macro Definition Documentation

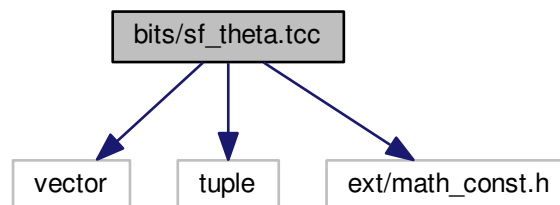
11.23.2.1 `#define _GLIBCXX_BITS_SF_POLYLOG_TCC 1`

Definition at line 41 of file `sf_polylog.tcc`.

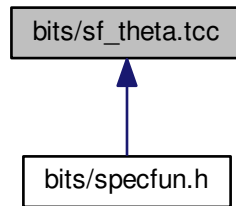
11.24 bits/sf_theta.tcc File Reference

```
#include <vector>
#include <tuple>
#include <ext/math_const.h>
```

Include dependency graph for `sf_theta.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_THETA_TCC 1](#)

Functions

- [template<typename _Tp > _Tp std::__detail::__ellnome \(_Tp __k\)](#)
- [template<typename _Tp > _Tp std::__detail::__ellnome_k \(_Tp __k\)](#)
- [template<typename _Tp > _Tp std::__detail::__ellnome_series \(_Tp __k\)](#)
- [template<typename _Tp > std::tuple< _Tp, _Tp, _Tp > std::__detail::__jacobi_sncndn \(_Tp __k, _Tp __u\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_1 \(_Tp __nu, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_2 \(_Tp __nu, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_2_asymp \(_Tp __nu, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_2_sum \(_Tp __nu, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_3 \(_Tp __nu, _Tp __x\)](#)
- [template<typename _Tp > _Tp std::__detail::__theta_3_asymp \(_Tp __nu, _Tp __x\)](#)

- `template<typename _Tp >`
`_Tp std::__detail::__theta_3_sum (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__theta_4 (_Tp __nu, _Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__theta_c (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__theta_d (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__theta_n (_Tp __k, _Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__theta_s (_Tp __k, _Tp __x)`

11.24.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.24.2 Macro Definition Documentation

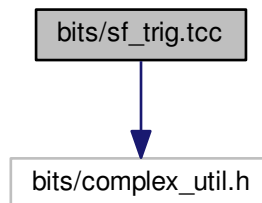
11.24.2.1 `#define _GLIBCXX_BITS_SF_THETA_TCC 1`

Definition at line 31 of file `sf_theta.tcc`.

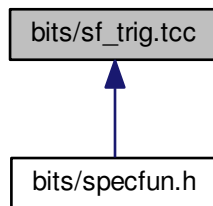
11.25 `bits/sf_trig.tcc` File Reference

```
#include <bits/complex_util.h>
```

Include dependency graph for `sf_trig.tcc`:



This graph shows which files directly or indirectly include this file:



Classes

- struct [__gnu_cxx::__sincos_t](#)< [_Tp](#) >

Namespaces

- [__gnu_cxx](#)
- [std](#)
- [std::__detail](#)

Macros

- [#define _GLIBCXX_BITS_SF_TRIG_TCC](#) 1

Functions

- [template<typename _Tp > _Tp std::__detail::__cos_pi](#) ([_Tp __x](#))
- [template<typename _Tp > std::complex< _Tp > std::__detail::__cos_pi](#) ([std::complex< _Tp > __z](#))
- [template<typename _Tp > _Tp std::__detail::__cosh_pi](#) ([_Tp __x](#))
- [template<typename _Tp > std::complex< _Tp > std::__detail::__cosh_pi](#) ([std::complex< _Tp > __z](#))
- [template<typename _Tp > std::complex< _Tp > std::__detail::__polar_pi](#) ([_Tp __rho](#), [_Tp __phi_pi](#))
- [template<typename _Tp > _Tp std::__detail::__sin_pi](#) ([_Tp __x](#))
- [template<typename _Tp > std::complex< _Tp > std::__detail::__sin_pi](#) ([std::complex< _Tp > __z](#))

- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > std::__detail::__sincos (_Tp __x)`
- `template<>`
`__gnu_cxx::__sincos_t< float > std::__detail::__sincos (float __x)`
- `template<>`
`__gnu_cxx::__sincos_t< double > std::__detail::__sincos (double __x)`
- `template<>`
`__gnu_cxx::__sincos_t< long double > std::__detail::__sincos (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__sincos_t< _Tp > std::__detail::__sincos_pi (_Tp __x)`
- `template<typename _Tp >`
`_Tp std::__detail::__sinh_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__sinh_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp std::__detail::__tan_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__tan_pi (std::complex< _Tp > __z)`
- `template<typename _Tp >`
`_Tp std::__detail::__tanh_pi (_Tp __x)`
- `template<typename _Tp >`
`std::complex< _Tp > std::__detail::__tanh_pi (std::complex< _Tp > __z)`

11.25.1 Detailed Description

This is an internal header file, included by other library headers. You should not attempt to use it directly.

11.25.2 Macro Definition Documentation

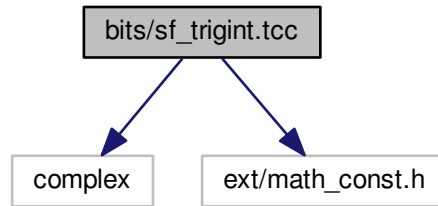
11.25.2.1 `#define _GLIBCXX_BITS_SF_TRIG_TCC 1`

Definition at line 31 of file `sf_trig.tcc`.

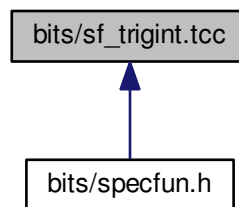
11.26 `bits/sf_trigint.tcc` File Reference

```
#include <complex>
#include <ext/math_const.h>
```

Include dependency graph for sf_trigint.tcc:



This graph shows which files directly or indirectly include this file:



Namespaces

- `std`
- `std::__detail`

Macros

- `#define _GLIBCXX_BITS_SF_TRIGINT_TCC 1`

Functions

- `template<typename _Tp >`
`std::pair< _Tp, _Tp > std::__detail::__sincosint (_Tp __x)`
This function returns the sine $Si(x)$ and cosine $Ci(x)$ integrals as a pair.

- `template<typename _Tp >`
`void std::__detail::__sincosint_asyp (_Tp __t, _Tp &_Si, _Tp &_Ci)`
This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by asymptotic series summation for positive argument.
- `template<typename _Tp >`
`void std::__detail::__sincosint_cont_frac (_Tp __t, _Tp &_Si, _Tp &_Ci)`
This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by continued fraction for positive argument.
- `template<typename _Tp >`
`void std::__detail::__sincosint_series (_Tp __t, _Tp &_Si, _Tp &_Ci)`
This function computes the sine $Si(x)$ and cosine $Ci(x)$ integrals by series summation for positive argument.

11.26.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.26.2 Macro Definition Documentation

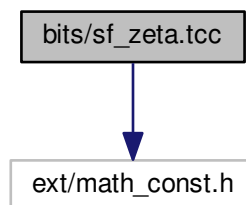
11.26.2.1 `#define _GLIBCXX_BITS_SF_TRIGINT_TCC 1`

Definition at line 31 of file `sf_trigint.tcc`.

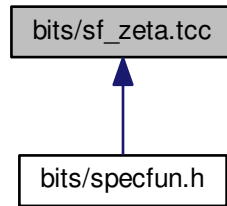
11.27 bits/sf_zeta.tcc File Reference

```
#include <ext/math_const.h>
```

Include dependency graph for `sf_zeta.tcc`:



This graph shows which files directly or indirectly include this file:



Namespaces

- [std](#)
- [std::__detail](#)

Macros

- `#define _GLIBCXX_BITS_SF_ZETA_TCC 1`

Functions

- `template<typename _Tp >`
`_Tp std::__detail::__dilog (_Tp __x)`
Compute the dilogarithm function $Li_2(x)$ by summation for $x \leq 1$.
- `template<typename _Tp >`
`_Tp std::__detail::__hurwitz_zeta (_Tp __s, _Tp __a)`
Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.
- `template<typename _Tp >`
`_Tp std::__detail::__hurwitz_zeta_euler_maclaurin (_Tp __s, _Tp __a)`
Return the Hurwitz zeta function $\zeta(s, a)$ for all $s \neq 1$ and $a > -1$.
- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta (_Tp __s)`
Return the Riemann zeta function $\zeta(s)$.
- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_alt (_Tp __s)`
Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.
- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_euler_maclaurin (_Tp __s)`
Evaluate the Riemann zeta function $\zeta(s)$ by an alternate series for $s > 0$.
- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_glob (_Tp __s)`

Evaluate the Riemann zeta function by series for all $s \neq 1$. Convergence is great until largish negative numbers. Then the convergence of the > 0 sum gets better.

- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_m_1 (_Tp __s)`

Return the Riemann zeta function $\zeta(s) - 1$.

- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_m_1_sum (_Tp __s)`

Return the Riemann zeta function $\zeta(s) - 1$ by summation for $s > 1$. This is a small remainder for large s .

- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_product (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ using the product over prime factors.

- `template<typename _Tp >`
`_Tp std::__detail::__riemann_zeta_sum (_Tp __s)`

Compute the Riemann zeta function $\zeta(s)$ by summation for $s > 1$.

Variables

- `constexpr size_t std::__detail::__Num_Euler_Maclaurin_zeta = 100`
- `constexpr long double std::__detail::__S_Euler_Maclaurin_zeta [_Num_Euler_Maclaurin_zeta]`
- `constexpr size_t std::__detail::__S_num_zetam1 = 41`
- `constexpr long double std::__detail::__S_zetam1 [_S_num_zetam1]`

11.27.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.27.2 Macro Definition Documentation

11.27.2.1 `#define _GLIBCXX_BITS_SF_ZETA_TCC 1`

Definition at line 46 of file `sf_zeta.tcc`.

11.28 bits/specfun.h File Reference

```
#include <bits/c++config.h>
#include <limits>
#include <bits/stl_algobase.h>
#include <bits/specfun_state.h>
#include <bits/specfun_util.h>
#include <type_traits>
#include <bits/numeric_limits.h>
#include <bits/complex_util.h>
#include <bits/sf_trig.tcc>
#include <bits/sf_gamma.tcc>
#include <bits/sf_bessel.tcc>
#include <bits/sf_beta.tcc>
#include <bits/sf_cardinal.tcc>
#include <bits/sf_chebyshev.tcc>
#include <bits/sf_dawson.tcc>
#include <bits/sf_ellint.tcc>
#include <bits/sf_expint.tcc>
#include <bits/sf_fresnel.tcc>
#include <bits/sf_gegenbauer.tcc>
#include <bits/sf_hyperg.tcc>
#include <bits/sf_hypint.tcc>
#include <bits/sf_jacobi.tcc>
#include <bits/sf_laguerre.tcc>
#include <bits/sf_legendre.tcc>
#include <bits/sf_hydrogen.tcc>
#include <bits/sf_mod_bessel.tcc>
#include <bits/sf_hermite.tcc>
#include <bits/sf_theta.tcc>
#include <bits/sf_trigint.tcc>
#include <bits/sf_zeta.tcc>
#include <bits/sf_owens_t.tcc>
#include <bits/sf_polylog.tcc>
#include <bits/sf_airy.tcc>
#include <bits/sf_hankel.tcc>
#include <bits/sf_distributions.tcc>
```

Include dependency graph for specfun.h:



Namespaces

- [__gnu_cxx](#)
- [std](#)

Macros

- [#define __cpp_lib_math_special_functions](#) 201603L
- [#define __STDCPP_MATH_SPEC_FUNCS__](#) 201003L

Enumerations

- enum { [__gnu_cxx::__GLIBCXX_JACOBI_SN](#), [__gnu_cxx::__GLIBCXX_JACOBI_CN](#), [__gnu_cxx::__GLIBCXX_JACOBI_DN](#) }

Functions

- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::airy_ai](#) (_Tp __x)
- template<typename _Tp >
std::complex< [__gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::airy_ai](#) (std::complex< _Tp > __x)
- float [__gnu_cxx::airy_aif](#) (float __x)
- long double [__gnu_cxx::airy_ail](#) (long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::airy_bi](#) (_Tp __x)
- template<typename _Tp >
std::complex< [__gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::airy_bi](#) (std::complex< _Tp > __x)
- float [__gnu_cxx::airy_bif](#) (float __x)
- long double [__gnu_cxx::airy_bil](#) (long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > std::assoc_laguerre](#) (unsigned int __n, unsigned int __m, _Tp __x)
- float [std::assoc_laguerref](#) (unsigned int __n, unsigned int __m, float __x)
- long double [std::assoc_laguerrel](#) (unsigned int __n, unsigned int __m, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > std::assoc_legendre](#) (unsigned int __l, unsigned int __m, _Tp __x)
- float [std::assoc_legendref](#) (unsigned int __l, unsigned int __m, float __x)
- long double [std::assoc_legendrel](#) (unsigned int __l, unsigned int __m, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::bernoulli](#) (unsigned int __n)
- float [__gnu_cxx::bernoullif](#) (unsigned int __n)
- long double [__gnu_cxx::bernoullil](#) (unsigned int __n)
- template<typename _Tpa, typename _Tpb >
[__gnu_cxx::__promote_fp_t< _Tpa, _Tpb > std::beta](#) (_Tpa __a, _Tpb __b)
- float [std::betaf](#) (float __a, float __b)
- long double [std::betal](#) (long double __a, long double __b)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::bincoef](#) (unsigned int __n, unsigned int __k)
- float [__gnu_cxx::bincoefficient](#) (unsigned int __n, unsigned int __k)
- long double [__gnu_cxx::bincoefficientl](#) (unsigned int __n, unsigned int __k)
- template<typename _Tps, typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tps, _Tp > __gnu_cxx::bose_einstein](#) (_Tps __s, _Tp __x)
- float [__gnu_cxx::bose_einsteinf](#) (float __s, float __x)
- long double [__gnu_cxx::bose_einsteinl](#) (long double __s, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_t](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::chebyshev_tf](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::chebyshev_tl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_u](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::chebyshev_uf](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::chebyshev_ul](#) (unsigned int __n, long double __x)

- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_v (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::chebyshev_vf (unsigned int __n, float __x)`
- `long double __gnu_cxx::chebyshev_vl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::chebyshev_w (unsigned int __n, _Tp __x)`
- `float __gnu_cxx::chebyshev_wf (unsigned int __n, float __x)`
- `long double __gnu_cxx::chebyshev_wl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen (unsigned int __m, _Tp __w)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::clausen (unsigned int __m, std::complex< _Tp > __w)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen_c (unsigned int __m, _Tp __w)`
- `float __gnu_cxx::clausen_cf (unsigned int __m, float __w)`
- `long double __gnu_cxx::clausen_cl (unsigned int __m, long double __w)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::clausen_s (unsigned int __m, _Tp __w)`
- `float __gnu_cxx::clausen_sf (unsigned int __m, float __w)`
- `long double __gnu_cxx::clausen_sl (unsigned int __m, long double __w)`
- `float __gnu_cxx::clausenf (unsigned int __m, float __w)`
- `std::complex< float > __gnu_cxx::clausenf (unsigned int __m, std::complex< float > __w)`
- `long double __gnu_cxx::clausenl (unsigned int __m, long double __w)`
- `std::complex< long double > __gnu_cxx::clausenl (unsigned int __m, std::complex< long double > __w)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::comp_ellint_1 (_Tp __k)`
- `float std::comp_ellint_1f (float __k)`
- `long double std::comp_ellint_1l (long double __k)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::comp_ellint_2 (_Tp __k)`
- `float std::comp_ellint_2f (float __k)`
- `long double std::comp_ellint_2l (long double __k)`
- `template<typename _Tp, typename _Tpn >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tpn > std::comp_ellint_3 (_Tp __k, _Tpn __nu)`
- `float std::comp_ellint_3f (float __k, float __nu)`
Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for float modulus k.
- `long double std::comp_ellint_3l (long double __k, long double __nu)`
Return the complete elliptic integral of the third kind $\Pi(k, \nu)$ for long double modulus k.
- `template<typename _Tk >`
`__gnu_cxx::__promote_fp_t< _Tk > __gnu_cxx::comp_ellint_d (_Tk __k)`
- `float __gnu_cxx::comp_ellint_df (float __k)`
- `long double __gnu_cxx::comp_ellint_dl (long double __k)`
- `float __gnu_cxx::comp_ellint_rf (float __x, float __y)`
- `long double __gnu_cxx::comp_ellint_rf (long double __x, long double __y)`
- `template<typename _Tx, typename _Ty >`
`__gnu_cxx::__promote_fp_t< _Tx, _Ty > __gnu_cxx::comp_ellint_rf (_Tx __x, _Ty __y)`
- `float __gnu_cxx::comp_ellint_rg (float __x, float __y)`
- `long double __gnu_cxx::comp_ellint_rg (long double __x, long double __y)`
- `template<typename _Tx, typename _Ty >`
`__gnu_cxx::__promote_fp_t< _Tx, _Ty > __gnu_cxx::comp_ellint_rg (_Tx __x, _Ty __y)`

- `template<typename _Tpa, typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpa, _Tpc, _Tp > __gnu_cxx::conf_hyperg (_Tpa __a, _Tpc __c, _Tp __x)`
- `template<typename _Tpc, typename _Tp >`
`__gnu_cxx::__promote_2< _Tpc, _Tp >::type __gnu_cxx::conf_hyperg_lim (_Tpc __c, _Tp __x)`
- `float __gnu_cxx::conf_hyperg_limf (float __c, float __x)`
- `long double __gnu_cxx::conf_hyperg_liml (long double __c, long double __x)`
- `float __gnu_cxx::conf_hypergf (float __a, float __c, float __x)`
- `long double __gnu_cxx::conf_hypergl (long double __a, long double __c, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::cos_pi (_Tp __x)`
- `float __gnu_cxx::cos_pif (float __x)`
- `long double __gnu_cxx::cos_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::cosh_pi (_Tp __x)`
- `float __gnu_cxx::cosh_pif (float __x)`
- `long double __gnu_cxx::cosh_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::coshint (_Tp __x)`
- `float __gnu_cxx::coshintf (float __x)`
- `long double __gnu_cxx::coshintl (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::cosint (_Tp __x)`
- `float __gnu_cxx::cosintf (float __x)`
- `long double __gnu_cxx::cosintl (long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_i (_Tpnu __nu, _Tp __x)`
- `float std::cyl_bessel_if (float __nu, float __x)`
- `long double std::cyl_bessel_il (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_j (_Tpnu __nu, _Tp __x)`
- `float std::cyl_bessel_jf (float __nu, float __x)`
- `long double std::cyl_bessel_jl (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_bessel_k (_Tpnu __nu, _Tp __x)`
- `float std::cyl_bessel_kf (float __nu, float __x)`
- `long double std::cyl_bessel_kl (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > __gnu_cxx::cyl_hankel_1 (_Tpnu __nu, _Tp __z)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > __gnu_cxx::cyl_hankel_1 (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)`
- `std::complex< float > __gnu_cxx::cyl_hankel_1f (float __nu, float __z)`
- `std::complex< float > __gnu_cxx::cyl_hankel_1f (std::complex< float > __nu, std::complex< float > __x)`
- `std::complex< long double > __gnu_cxx::cyl_hankel_1l (long double __nu, long double __z)`
- `std::complex< long double > __gnu_cxx::cyl_hankel_1l (std::complex< long double > __nu, std::complex< long double > __x)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > __gnu_cxx::cyl_hankel_2 (_Tpnu __nu, _Tp __z)`
- `template<typename _Tpnu, typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > > __gnu_cxx::cyl_hankel_2 (std::complex< _Tpnu > __nu, std::complex< _Tp > __x)`
- `std::complex< float > __gnu_cxx::cyl_hankel_2f (float __nu, float __z)`

- `std::complex< float > __gnu_cxx::cyl_hankel_2f` (`std::complex< float > __nu`, `std::complex< float > __x`)
- `std::complex< long double > __gnu_cxx::cyl_hankel_2l` (`long double __nu`, `long double __z`)
- `std::complex< long double > __gnu_cxx::cyl_hankel_2l` (`std::complex< long double > __nu`, `std::complex< long double > __x`)
- `template<typename _Tpnu, typename _Tp > __gnu_cxx::__promote_fp_t< _Tpnu, _Tp > std::cyl_neumann` (`_Tpnu __nu`, `_Tp __x`)
- `float std::cyl_neumannf` (`float __nu`, `float __x`)
- `long double std::cyl_neumannl` (`long double __nu`, `long double __x`)
- `template<typename _Tp > __gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::dawson` (`_Tp __x`)
- `float __gnu_cxx::dawsonf` (`float __x`)
- `long double __gnu_cxx::dawsonl` (`long double __x`)
- `template<typename _Tp > __gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::dilog` (`_Tp __x`)
- `float __gnu_cxx::dilogf` (`float __x`)
- `long double __gnu_cxx::dilogl` (`long double __x`)
- `template<typename _Tp > _Tp __gnu_cxx::dirichlet_beta` (`_Tp __s`)
- `float __gnu_cxx::dirichlet_betaf` (`float __s`)
- `long double __gnu_cxx::dirichlet_betall` (`long double __s`)
- `template<typename _Tp > _Tp __gnu_cxx::dirichlet_eta` (`_Tp __s`)
- `float __gnu_cxx::dirichlet_etaf` (`float __s`)
- `long double __gnu_cxx::dirichlet_etall` (`long double __s`)
- `template<typename _Tp > _Tp __gnu_cxx::dirichlet_lambda` (`_Tp __s`)
- `float __gnu_cxx::dirichlet_lambdaf` (`float __s`)
- `long double __gnu_cxx::dirichlet_lambdall` (`long double __s`)
- `template<typename _Tp > __gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::double_factorial` (`int __n`)
- `float __gnu_cxx::double_factorialf` (`int __n`)
- `long double __gnu_cxx::double_factoriall` (`int __n`)
- `template<typename _Tp, typename _Tpp > __gnu_cxx::__promote_fp_t< _Tp, _Tpp > std::ellint_1` (`_Tp __k`, `_Tpp __phi`)
- `float std::ellint_1f` (`float __k`, `float __phi`)
- `long double std::ellint_1l` (`long double __k`, `long double __phi`)
- `template<typename _Tp, typename _Tpp > __gnu_cxx::__promote_fp_t< _Tp, _Tpp > std::ellint_2` (`_Tp __k`, `_Tpp __phi`)
- `float std::ellint_2f` (`float __k`, `float __phi`)
- Return the incomplete elliptic integral of the second kind $E(k, \phi)$ for `float` argument.*
- `long double std::ellint_2l` (`long double __k`, `long double __phi`)
- Return the incomplete elliptic integral of the second kind $E(k, \phi)$.*
- `template<typename _Tp, typename _Tpn, typename _Tpp > __gnu_cxx::__promote_fp_t< _Tp, _Tpn, _Tpp > std::ellint_3` (`_Tp __k`, `_Tpn __nu`, `_Tpp __phi`)
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.*
- `float std::ellint_3f` (`float __k`, `float __nu`, `float __phi`)
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$ for `float` argument.*
- `long double std::ellint_3l` (`long double __k`, `long double __nu`, `long double __phi`)
- Return the incomplete elliptic integral of the third kind $\Pi(k, \nu, \phi)$.*

- `template<typename _Tk, typename _Tp, typename _Ta, typename _Tb >`
`__gnu_cxx::__promote_fp_t< _Tk, _Tp, _Ta, _Tb > __gnu_cxx::ellint_cel (_Tk __k_c, _Tp __p, _Ta __a, _Tb __b)`
- `float __gnu_cxx::ellint_celf (float __k_c, float __p, float __a, float __b)`
- `long double __gnu_cxx::ellint_cell (long double __k_c, long double __p, long double __a, long double __b)`
- `template<typename _Tk, typename _Tphi >`
`__gnu_cxx::__promote_fp_t< _Tk, _Tphi > __gnu_cxx::ellint_d (_Tk __k, _Tphi __phi)`
- `float __gnu_cxx::ellint_df (float __k, float __phi)`
- `long double __gnu_cxx::ellint_dl (long double __k, long double __phi)`
- `template<typename _Tp, typename _Tk >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tk > __gnu_cxx::ellint_el1 (_Tp __x, _Tk __k_c)`
- `float __gnu_cxx::ellint_el1f (float __x, float __k_c)`
- `long double __gnu_cxx::ellint_el1l (long double __x, long double __k_c)`
- `template<typename _Tp, typename _Tk, typename _Ta, typename _Tb >`
`__gnu_cxx::__promote_fp_t< _Tp, _Tk, _Ta, _Tb > __gnu_cxx::ellint_el2 (_Tp __x, _Tk __k_c, _Ta __a, _Tb __b)`
- `float __gnu_cxx::ellint_el2f (float __x, float __k_c, float __a, float __b)`
- `long double __gnu_cxx::ellint_el2l (long double __x, long double __k_c, long double __a, long double __b)`
- `template<typename _Tx, typename _Tk, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tx, _Tk, _Tp > __gnu_cxx::ellint_el3 (_Tx __x, _Tk __k_c, _Tp __p)`
- `float __gnu_cxx::ellint_el3f (float __x, float __k_c, float __p)`
- `long double __gnu_cxx::ellint_el3l (long double __x, long double __k_c, long double __p)`
- `template<typename _Tp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up > __gnu_cxx::ellint_rc (_Tp __x, _Up __y)`
- `float __gnu_cxx::ellint_rcf (float __x, float __y)`
- `long double __gnu_cxx::ellint_rcl (long double __x, long double __y)`
- `template<typename _Tp, typename _Up, typename _Vp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up, _Vp > __gnu_cxx::ellint_rd (_Tp __x, _Up __y, _Vp __z)`
- `float __gnu_cxx::ellint_rdf (float __x, float __y, float __z)`
- `long double __gnu_cxx::ellint_rdl (long double __x, long double __y, long double __z)`
- `template<typename _Tp, typename _Up, typename _Vp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up, _Vp > __gnu_cxx::ellint_rf (_Tp __x, _Up __y, _Vp __z)`
- `float __gnu_cxx::ellint_rff (float __x, float __y, float __z)`
- `long double __gnu_cxx::ellint_rfl (long double __x, long double __y, long double __z)`
- `template<typename _Tp, typename _Up, typename _Vp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up, _Vp > __gnu_cxx::ellint_rg (_Tp __x, _Up __y, _Vp __z)`
- `float __gnu_cxx::ellint_rgf (float __x, float __y, float __z)`
- `long double __gnu_cxx::ellint_rgl (long double __x, long double __y, long double __z)`
- `template<typename _Tp, typename _Up, typename _Vp, typename _Wp >`
`__gnu_cxx::__promote_fp_t< _Tp, _Up, _Vp, _Wp > __gnu_cxx::ellint_rj (_Tp __x, _Up __y, _Vp __z, _Wp __p)`
- `float __gnu_cxx::ellint_rjf (float __x, float __y, float __z, float __p)`
- `long double __gnu_cxx::ellint_rjl (long double __x, long double __y, long double __z, long double __p)`
- `template<typename _Tp >`
`_Tp __gnu_cxx::ellnome (_Tp __k)`
- `float __gnu_cxx::ellnomef (float __k)`
- `long double __gnu_cxx::ellnomel (long double __k)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::expint (_Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::expint (unsigned int __n, _Tp __x)`
- `float std::expintf (float __x)`
- `float __gnu_cxx::expintf (unsigned int __n, float __x)`

- long double [std::expintl](#) (long double __x)
- long double [__gnu_cxx::expintl](#) (unsigned int __n, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) > [__gnu_cxx::factorial](#) (unsigned int __n)
- float [__gnu_cxx::factorialf](#) (unsigned int __n)
- long double [__gnu_cxx::factoriall](#) (unsigned int __n)
- template<typename _Tps, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tps, _Tp>](#) > [__gnu_cxx::fermi_dirac](#) (_Tps __s, _Tp __x)
- float [__gnu_cxx::fermi_diracf](#) (float __s, float __x)
- long double [__gnu_cxx::fermi_diracl](#) (long double __s, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) > [__gnu_cxx::fresnel_c](#) (_Tp __x)
- float [__gnu_cxx::fresnel_cf](#) (float __x)
- long double [__gnu_cxx::fresnel_cl](#) (long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) > [__gnu_cxx::fresnel_s](#) (_Tp __x)
- float [__gnu_cxx::fresnel_sf](#) (float __x)
- long double [__gnu_cxx::fresnel_sl](#) (long double __x)
- template<typename _Talpha, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Talpha, _Tp>](#) > [__gnu_cxx::gegenbauer](#) (unsigned int __n, _Talpha __alpha, _Tp __x)
- float [__gnu_cxx::gegenbauerf](#) (unsigned int __n, float __alpha, float __x)
- long double [__gnu_cxx::gegenbauerl](#) (unsigned int __n, long double __alpha, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tp>](#) > [std::hermite](#) (unsigned int __n, _Tp __x)
- float [std::hermitef](#) (unsigned int __n, float __x)
- long double [std::hermitel](#) (unsigned int __n, long double __x)
- template<typename _Tk, typename _Tphi >
[__gnu_cxx::__promote_fp_t<_Tk, _Tphi>](#) > [__gnu_cxx::heuman_lambda](#) (_Tk __k, _Tphi __phi)
- float [__gnu_cxx::heuman_lambdaf](#) (float __k, float __phi)
- long double [__gnu_cxx::heuman_lambdal](#) (long double __k, long double __phi)
- template<typename _Tp, typename _Up >
[__gnu_cxx::__promote_fp_t<_Tp, _Up>](#) > [__gnu_cxx::hurwitz_zeta](#) (_Tp __s, _Up __a)
- template<typename _Tp, typename _Up >
[std::complex<_Tp>](#) > [__gnu_cxx::hurwitz_zeta](#) (_Tp __s, std::complex<_Up> __a)
- float [__gnu_cxx::hurwitz_zetaf](#) (float __s, float __a)
- long double [__gnu_cxx::hurwitz_zetal](#) (long double __s, long double __a)
- template<typename _Tpa, typename _Tpb, typename _Tpc, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Tpa, _Tpb, _Tpc, _Tp>](#) > [__gnu_cxx::hyperg](#) (_Tpa __a, _Tpb __b, _Tpc __c, _Tp __x)
- float [__gnu_cxx::hypergf](#) (float __a, float __b, float __c, float __x)
- long double [__gnu_cxx::hypergl](#) (long double __a, long double __b, long double __c, long double __x)
- template<typename _Ta, typename _Tb, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp>](#) > [__gnu_cxx::ibeta](#) (_Ta __a, _Tb __b, _Tp __x)
- template<typename _Ta, typename _Tb, typename _Tp >
[__gnu_cxx::__promote_fp_t<_Ta, _Tb, _Tp>](#) > [__gnu_cxx::ibetac](#) (_Ta __a, _Tb __b, _Tp __x)
- float [__gnu_cxx::ibetaacf](#) (float __a, float __b, float __x)
- long double [__gnu_cxx::ibetaacl](#) (long double __a, long double __b, long double __x)
- float [__gnu_cxx::ibetaf](#) (float __a, float __b, float __x)
- long double [__gnu_cxx::ibetal](#) (long double __a, long double __b, long double __x)

- `template<typename _Talpha, typename _Tbeta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Talpha, _Tbeta, _Tp > __gnu_cxx::jacobi (unsigned __n, _Talpha __alpha, _Tbeta __beta, _Tp __x)`
- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_cn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_cnf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_cnl (long double __k, long double __u)`
- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_dn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_dnf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_dnl (long double __k, long double __u)`
- `template<typename _Kp, typename _Up >`
`__gnu_cxx::__promote_fp_t< _Kp, _Up > __gnu_cxx::jacobi_sn (_Kp __k, _Up __u)`
- `float __gnu_cxx::jacobi_snf (float __k, float __u)`
- `long double __gnu_cxx::jacobi_snl (long double __k, long double __u)`
- `template<typename _Tk, typename _Tphi >`
`__gnu_cxx::__promote_fp_t< _Tk, _Tphi > __gnu_cxx::jacobi_zeta (_Tk __k, _Tphi __phi)`
- `float __gnu_cxx::jacobi_zetaf (float __k, float __phi)`
- `long double __gnu_cxx::jacobi_zetal (long double __k, long double __phi)`
- `float __gnu_cxx::jacobif (unsigned __n, float __alpha, float __beta, float __x)`
- `long double __gnu_cxx::jacobil (unsigned __n, long double __alpha, long double __beta, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::laguerre (unsigned int __n, _Tp __x)`
- `float std::laguerref (unsigned int __n, float __x)`
- `long double std::laguerrel (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::lbincoef (unsigned int __n, unsigned int __k)`
- `float __gnu_cxx::lbincoeff (unsigned int __n, unsigned int __k)`
- `long double __gnu_cxx::lbincoeffl (unsigned int __n, unsigned int __k)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::ldouble_factorial (int __n)`
- `float __gnu_cxx::ldouble_factorialf (int __n)`
- `long double __gnu_cxx::ldouble_factoriall (int __n)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::legendre (unsigned int __l, _Tp __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::legendre_q (unsigned int __l, _Tp __x)`
- `float __gnu_cxx::legendre_qf (unsigned int __l, float __x)`
- `long double __gnu_cxx::legendre_ql (unsigned int __l, long double __x)`
- `float std::legendref (unsigned int __l, float __x)`
- `long double std::legendrel (unsigned int __l, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::lfactorial (unsigned int __n)`
- `float __gnu_cxx::lfactorialf (unsigned int __n)`
- `long double __gnu_cxx::lfactoriall (unsigned int __n)`
- `template<typename _Ta >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ta > > __gnu_cxx::lgamma (std::complex< _Ta > __a)`
- `std::complex< float > __gnu_cxx::lgammaf (std::complex< float > __a)`
- `std::complex< long double > __gnu_cxx::lgammal (std::complex< long double > __a)`
- `template<typename _Tp >`
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- `float __gnu_cxx::logintf (float __x)`

- long double [__gnu_cxx::logintl](#) (long double __x)
- template<typename _Tp, typename _Tn >
[__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::lpochhammer](#) (_Tp __a, _Tn __n)
- template<typename _Tp, typename _Tn >
[__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::lpochhammer_lower](#) (_Tp __a, _Tn __n)
- float [__gnu_cxx::lpochhammer_lowerf](#) (float __a, float __n)
- long double [__gnu_cxx::lpochhammer_lowerl](#) (long double __a, long double __n)
- float [__gnu_cxx::lpochhammerf](#) (float __a, float __n)
- long double [__gnu_cxx::lpochhammerl](#) (long double __a, long double __n)
- template<typename _Tph, typename _Tpa >
[__gnu_cxx::__promote_fp_t< _Tph, _Tpa > __gnu_cxx::owens_t](#) (_Tph __h, _Tpa __a)
- float [__gnu_cxx::owens_tf](#) (float __h, float __a)
- long double [__gnu_cxx::owens_tl](#) (long double __h, long double __a)
- template<typename _Ta, typename _Tp >
[__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::pgamma](#) (_Ta __a, _Tp __x)
- float [__gnu_cxx::pgammaf](#) (float __a, float __x)
- long double [__gnu_cxx::pgammal](#) (long double __a, long double __x)
- template<typename _Tp, typename _Tn >
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- template<typename _Tp, typename _Tn >
[__gnu_cxx::__promote_fp_t< _Tp, _Tn > __gnu_cxx::pochhammer_lower](#) (_Tp __a, _Tn __n)
- float [__gnu_cxx::pochhammer_lowerf](#) (float __a, float __n)
- long double [__gnu_cxx::pochhammer_lowerl](#) (long double __a, long double __n)
- float [__gnu_cxx::pochhammerf](#) (float __a, float __n)
- long double [__gnu_cxx::pochhammerl](#) (long double __a, long double __n)
- template<typename _Tp, typename _Wp >
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- template<typename _Tp, typename _Wp >
[std::complex< __gnu_cxx::__promote_fp_t< _Tp, _Wp > > __gnu_cxx::polylog](#) (_Tp __s, std::complex< _Tp > __w)
- float [__gnu_cxx::polylogf](#) (float __s, float __w)
- std::complex< float > [__gnu_cxx::polylogf](#) (float __s, std::complex< float > __w)
- long double [__gnu_cxx::polylogl](#) (long double __s, long double __w)
- std::complex< long double > [__gnu_cxx::polylogl](#) (long double __s, std::complex< long double > __w)
- template<typename _Tp >
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- float [__gnu_cxx::psif](#) (float __x)
- long double [__gnu_cxx::psil](#) (long double __x)
- template<typename _Ta, typename _Tp >
[__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::qgamma](#) (_Ta __a, _Tp __x)
- float [__gnu_cxx::qgammaf](#) (float __a, float __x)
- long double [__gnu_cxx::qgammal](#) (long double __a, long double __x)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::radpoly](#) (unsigned int __n, unsigned int __m, _Tp __rho)
- float [__gnu_cxx::radpolyf](#) (unsigned int __n, unsigned int __m, float __rho)
- long double [__gnu_cxx::radpolyl](#) (unsigned int __n, unsigned int __m, long double __rho)
- template<typename _Tp >
[__gnu_cxx::__promote_fp_t< _Tp > std::riemann_zeta](#) (_Tp __s)
- float [std::riemann_zetaf](#) (float __s)
- long double [std::riemann_zetal](#) (long double __s)
- template<typename _Tp >
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- float [__gnu_cxx::sin_pif](#) (float __x)
- long double [__gnu_cxx::sin_pil](#) (long double __x)
- template<typename _Tp >
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- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinc_pi](#) (_Tp __x)
- float [__gnu_cxx::sinc_pif](#) (float __x)
- long double [__gnu_cxx::sinc_pil](#) (long double __x)
- float [__gnu_cxx::sincf](#) (float __x)
- long double [__gnu_cxx::sincl](#) (long double __x)
- [__gnu_cxx::__sincos_t<double> __gnu_cxx::sincos](#) (double __x)
- template<typename _Tp >
 [__gnu_cxx::__sincos_t<_Tp> __gnu_cxx::sincos](#) (_Tp __x)
- template<typename _Tp >
 [__gnu_cxx::__sincos_t<_Tp> __gnu_cxx::sincos_pi](#) (_Tp __x)
- [__gnu_cxx::__sincos_t<float> __gnu_cxx::sincos_pif](#) (float __x)
- [__gnu_cxx::__sincos_t<long double> __gnu_cxx::sincos_pil](#) (long double __x)
- [__gnu_cxx::__sincos_t<float> __gnu_cxx::sincosf](#) (float __x)
- [__gnu_cxx::__sincos_t<long double> __gnu_cxx::sincosl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinh_pi](#) (_Tp __x)
- float [__gnu_cxx::sinh_pif](#) (float __x)
- long double [__gnu_cxx::sinh_pil](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhc](#) (_Tp __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhc_pi](#) (_Tp __x)
- float [__gnu_cxx::sinhc_pif](#) (float __x)
- long double [__gnu_cxx::sinhc_pil](#) (long double __x)
- float [__gnu_cxx::sinhcf](#) (float __x)
- long double [__gnu_cxx::sinhcl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinhint](#) (_Tp __x)
- float [__gnu_cxx::sinhintf](#) (float __x)
- long double [__gnu_cxx::sinhintl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sinint](#) (_Tp __x)
- float [__gnu_cxx::sinintf](#) (float __x)
- long double [__gnu_cxx::sinintl](#) (long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> std::sph_bessel](#) (unsigned int __n, _Tp __x)
- template<typename _Tp >
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- float [__gnu_cxx::sph_bessel_if](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::sph_bessel_il](#) (unsigned int __n, long double __x)
- template<typename _Tp >
 [__gnu_cxx::__promote_fp_t<_Tp> __gnu_cxx::sph_bessel_k](#) (unsigned int __n, _Tp __x)
- float [__gnu_cxx::sph_bessel_kf](#) (unsigned int __n, float __x)
- long double [__gnu_cxx::sph_bessel_kl](#) (unsigned int __n, long double __x)
- float [std::sph_besself](#) (unsigned int __n, float __x)
- long double [std::sph_bessell](#) (unsigned int __n, long double __x)

- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::sph_hankel_1 (unsigned int __n, _Tp __z)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::sph_hankel_1 (unsigned int __n, std::complex< _Tp > __x)`
- `std::complex< float > __gnu_cxx::sph_hankel_1f (unsigned int __n, float __z)`
- `std::complex< float > __gnu_cxx::sph_hankel_1f (unsigned int __n, std::complex< float > __x)`
- `std::complex< long double > __gnu_cxx::sph_hankel_1l (unsigned int __n, long double __z)`
- `std::complex< long double > __gnu_cxx::sph_hankel_1l (unsigned int __n, std::complex< long double > __x)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::sph_hankel_2 (unsigned int __n, _Tp __z)`
- `template<typename _Tp >`
`std::complex< __gnu_cxx::__promote_fp_t< _Tp > > __gnu_cxx::sph_hankel_2 (unsigned int __n, std::complex< _Tp > __x)`
- `std::complex< float > __gnu_cxx::sph_hankel_2f (unsigned int __n, float __z)`
- `std::complex< float > __gnu_cxx::sph_hankel_2f (unsigned int __n, std::complex< float > __x)`
- `std::complex< long double > __gnu_cxx::sph_hankel_2l (unsigned int __n, long double __z)`
- `std::complex< long double > __gnu_cxx::sph_hankel_2l (unsigned int __n, std::complex< long double > __x)`
- `template<typename _Ttheta, typename _Tphi >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ttheta, _Tphi > > __gnu_cxx::sph_harmonic (unsigned int __l, int __m, _Ttheta __theta, _Tphi __phi)`
- `std::complex< float > __gnu_cxx::sph_harmonicf (unsigned int __l, int __m, float __theta, float __phi)`
- `std::complex< long double > __gnu_cxx::sph_harmonicl (unsigned int __l, int __m, long double __theta, long double __phi)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::sph_legendre (unsigned int __l, unsigned int __m, _Tp __theta)`
- `float std::sph_legendref (unsigned int __l, unsigned int __m, float __theta)`
- `long double std::sph_legendrel (unsigned int __l, unsigned int __m, long double __theta)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > std::sph_neumann (unsigned int __n, _Tp __x)`
- `float std::sph_neumannf (unsigned int __n, float __x)`
- `long double std::sph_neumannl (unsigned int __n, long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::tan_pi (_Tp __x)`
- `float __gnu_cxx::tan_pif (float __x)`
- `long double __gnu_cxx::tan_pil (long double __x)`
- `template<typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tp > __gnu_cxx::tanh_pi (_Tp __x)`
- `float __gnu_cxx::tanh_pif (float __x)`
- `long double __gnu_cxx::tanh_pil (long double __x)`
- `template<typename _Ta >`
`std::complex< __gnu_cxx::__promote_fp_t< _Ta > > __gnu_cxx::tgamma (std::complex< _Ta > __a)`
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::tgamma (_Ta __a, _Tp __x)`
- `template<typename _Ta, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Ta, _Tp > __gnu_cxx::tgamma_lower (_Ta __a, _Tp __x)`
- `float __gnu_cxx::tgamma_lowerf (float __a, float __x)`
- `long double __gnu_cxx::tgamma_lowerl (long double __a, long double __x)`
- `std::complex< float > __gnu_cxx::tgammaf (std::complex< float > __a)`
- `float __gnu_cxx::tgammaf (float __a, float __x)`
- `std::complex< long double > __gnu_cxx::tgammal (std::complex< long double > __a)`
- `long double __gnu_cxx::tgammal (long double __a, long double __x)`

- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_1 (_Tpnu __nu, _Tp __x)`
- `float __gnu_cxx::theta_1f (float __nu, float __x)`
- `long double __gnu_cxx::theta_1l (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
`__gnu_cxx::__promote_fp_t< _Tpnu, _Tp > __gnu_cxx::theta_2 (_Tpnu __nu, _Tp __x)`
- `float __gnu_cxx::theta_2f (float __nu, float __x)`
- `long double __gnu_cxx::theta_2l (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
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- `float __gnu_cxx::theta_3f (float __nu, float __x)`
- `long double __gnu_cxx::theta_3l (long double __nu, long double __x)`
- `template<typename _Tpnu, typename _Tp >`
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- `long double __gnu_cxx::theta_4l (long double __nu, long double __x)`
- `template<typename _Tpk, typename _Tp >`
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- `template<typename _Tpk, typename _Tp >`
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- `float __gnu_cxx::theta_df (float __k, float __x)`
- `long double __gnu_cxx::theta_dl (long double __k, long double __x)`
- `template<typename _Tpk, typename _Tp >`
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- `long double __gnu_cxx::theta_nl (long double __k, long double __x)`
- `template<typename _Tpk, typename _Tp >`
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- `float __gnu_cxx::theta_sf (float __k, float __x)`
- `long double __gnu_cxx::theta_sl (long double __k, long double __x)`
- `template<typename _Trho, typename _Tphi >`
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- `float __gnu_cxx::zernikef (unsigned int __n, int __m, float __rho, float __phi)`
- `long double __gnu_cxx::zernikel (unsigned int __n, int __m, long double __rho, long double __phi)`

11.28.1 Detailed Description

This is an internal header file, included by other library headers. Do not attempt to use it directly. Instead, include `<cmath>`.

11.28.2 Macro Definition Documentation

11.28.2.1 `#define __cpp_lib_math_special_functions 201603L`

Definition at line 39 of file `specfun.h`.

11.28.2.2 `#define __STDCPP_MATH_SPEC_FUNCS__ 201003L`

Definition at line 37 of file `specfun.h`.

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