

# Project Part 1

## Pattern Recognition

### ECE 759

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# 1 Introduction

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In this report, we outline the process we undertook to implement two classification algorithms: linear discriminant analysis (LDA) and Decision Trees. We tested our generated classifiers on the Yale Extended Face Dataset B and MNIST [2] datasets. To complete this, we experimented with two feature generation methods: principle components analysis (PCA) and LDA itself (for use in decision trees.) These were primarily useful in training our decision trees, which require a thorough exploration of the feature space to grow. Note that throughout this document, we use the terms '*features*' and '*attributes*' interchangeably.

After presenting an explanation of our algorithms' implementations, we will discuss our current-best results and our preliminary exploration of the hyperparameter space. The hyperparameters are adjustments that variously control the accuracy and computational complexity of our classifiers. A more thorough exploration and validation of these parameters will be presented in the next installment of the project.

Code for this project is included in our project submission. In addition, it's available on GitHub at <https://github.com/n-casale/ece759-project>. The Git repository includes a more thorough representation of the path our code took to its current state.

## 2 Feature Selection

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### 2.1 Decision Tree Feature Generation

---

#### 2.1.1 Feature Generation for Decision Trees

---

In working with the decision trees, we utilized dimensionality reduction techniques including Linear discriminant analysis (LDA) and principle components analysis (PCA) for training and testing 'classical' decision trees, which pass over all features to consider which decision nodes to generate.

LDA reduces data with  $K$  classes in large dimensions (on the order of the number of pixels) to  $K$  dimensions which captures the most energy of the data. Implementing LDA as dimensionality reduction, MNIST and Extended YaleB datasets are reduced to 10 and 38 variables respectively (for each data point.) We then worked with this transformed data as the input to our decision tree classifier for training and testing.

In another implementation, we will consider the effects of utilizing the raw pixel data as features in *random forests* which are ensembles of decision trees trained on randomly chosen features and thresholds.

### 2.2 LDA vs PCA

---

LDA and PCA linearly transform the data to reduce its dimensionality. Dimensionality reduction is helpful in many algorithms because it eases computational requirements and improves the generalizability of the classifier. This latter benefit is conferred by the manner in which dimensionality reduction smoothes out the individual variations in a particular class. A good dimensionality reduction algorithm should maximize the 'distance' between classes in the transformed (reduced) space, while minimizing the variance, or spread of those classes in the transformed space.

The difference between the two techniques is that LDA is supervised whereas PCA is unsupervised. PCA finds orthogonal projections which capture the most variance of each feature, thereby expressing the data along *principle components* that are the most distinct. We can visually exemplify the PCA technique as in the figure below.

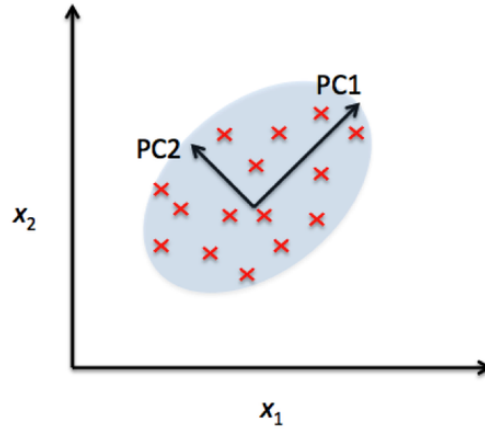


Figure 2.1: PCA implemented on 2-dimensional data [1].

In our implementation, we rely on the *singular value decomposition* (SVD) to generate our features, conventionally described as *scores*. To perform the singular value decomposition and obtain our features, we must first pre-process the data. We arrange it so that the rows of our data  $X$  are the individual images in the dataset, with each column corresponding to a pixel value. Then, we subtract the column-wise empirical mean from each column to render each column zero-mean. Then, we utilize MATLAB's built-in `svd(.)` to obtain the matrices  $[U, S, V]$ . Our features are represented by  $U * S$ . Taking the transpose of this matrix, and extracting the first  $n$  columns, where  $n$  is the number of features we seek to utilize, we have a matrix of features corresponding to each image in our dataset. This method was useful, although not as effective in training decision trees as LDA, which we now discuss.

LDA maximizes the class separability and can be represented visually as in the figure below.

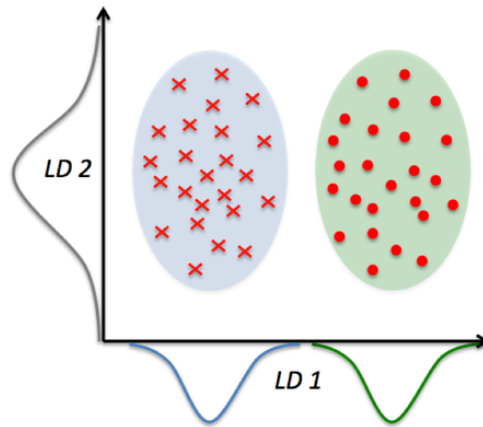


Figure 2.2: LDA visualization [1].

The underlying concept of LDA is taking the eigenvectors of  $\frac{\Sigma_b}{\Sigma_w}$  where  $\Sigma_w$  is within-class scatter matrix and  $\Sigma_b$  is between-class scatter matrix. This division of matrices separates the classes away from one another. This is distinct from PCA, as it is unsupervised, it only captures the data in a minimum number of variables.

## 3 Algorithm Implementations

### 3.1 Decision Tree Algorithm

A binary decision tree is a hierarchical structure that takes input data at its root and propagates it to one of many leaves. Each *leaf* of the tree represents a class designation. To reach a leaf, the features of the data are utilized at *nodes* to make a binary decision: to proceed down the left or right *branch* of the tree? To answer this question, the node also carries a *threshold* that the feature value of the test data is compared against. If the test feature is less than the threshold, we proceed down the left branch. Otherwise, the right. An illustration of a simple decision tree is pictured below.

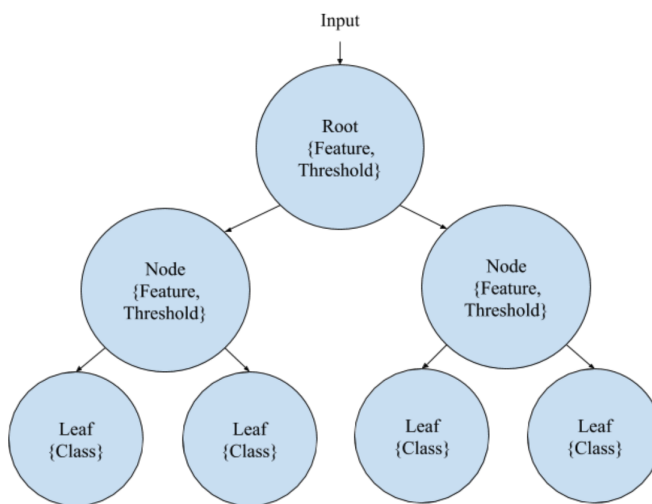


Figure 3.1: An example decision tree.

This decision tree structure needs to be generated before it can be used with test data. To train a decision tree that appropriately classifies our test data according to the features we generated, we employ a recursive function. The function signature is

```
tree = trainDecisionTree(set)
```

Where **set** is the training set, which is a MATLAB structure that contains the raw data (unused), class labels, and generated features. **tree** is the returned structure that can be used during testing. It is essentially a nested structure that contains two types of elements: nodes and leaves. At each node of the tree, a feature and threshold are specified. If a test sample's value at that particular feature is less than the threshold, the sample is passed down the left branch of the node. Similarly, if the sample's feature is greater than the threshold, it goes through the right branch. This is repeated until we reach a leaf node, which specifies a class membership.

The decision tree training algorithm has a few major steps, and proceeds by evaluating a metric called *information gain* at various configurations. For now, suffice it to say that information gain is a scalar that represents the improvement in prediction as we narrow down the set (by growing the tree) to find appropriate leaves. Our implementation most closely follows that of the ID3 and C4.5 algorithms developed by Ross Quinlan in the late 80s and early 90s [3] [4].

1. Check stopping conditions, which generate leaves.
  - If there are no more features to split on, return a leaf with the class mode of the set.
  - The set is smaller than **minLeaf**, which is a tuning parameter that is meant to reduce overfitting of the training data. If this condition is met, return a leaf with the class mode of the set.

- If all samples in the set belong to the same class, return a leaf with the class.
  - If no feature yields an improvement to the information gain (discussed below), then return a leaf with the class mode of the set. Note that this condition is only evaluated after step 2.
2. Iterate over each feature. Sort the set along the current feature. We utilize a threshold that splits the set between adjacent feature values. Because the information gain across thresholds is convex on the whole (see Fig. 3.2), we use a line search that approximates the highest information gain for each threshold.  
Let `attributeBest` and `indBest` be the feature and index that yield the highest information gain. Since the set is sorted, we can simply split the set at the index given by `indBest` for the recursion.
  3. Recur over the subsets given by `indBest` to find the next attribute that yields the highest information gain. Note that we exclude the attribute/feature we chose in this execution of `trainDecisionTree(.)`.

The algorithm is reproduced in pseudocode below.

---

**Algorithm 3.1:** trainDecisionTree
 

---

**Data:** *set* of training samples with class labels (*set*(1)) and attributes (features) (*set*(2)).

*minLeaf*, an integer specifying the minimum number of elements in *set* required to make a splitting node. *i.e.* a leaf is generated if the set has fewer elements than *minLeaf*.

**Result:** *tree*, a structure containing nodes and leaves.

```

1 begin
2   check for base cases:
3   if set(2) =  $\emptyset$  then
4     | no more attributes (features) to split on.
5     | return leaf with mode of set(1) (class labels)
6   if length(set(1)) < minLeaf then
7     | return leaf with mode of set(1) (class labels)
8   thisSetEntropy  $\leftarrow$  getEntropy(set)
9   if not thisSetEntropy then
10    | all samples are in the same class.
11    | return leaf with first element of set(1)
12
13   instantiate tracking variables:
14   attributeBest, thresholdBest, infoGainBest, indexBest  $\leftarrow$  0
15   for attribute  $\in$  range(# of features left in set) do
16     | sort set along attribute.
17     | perform line search heuristic to approximate max information gain by splitting set at various indices.
18     | thisInfoGain  $\leftarrow$  lineSearch(set)
19     | if thisInfoGain > infoGainBest then
20     | | attributeBest  $\leftarrow$  attribute
21     | | infoGainBest  $\leftarrow$  thisInfoGain
22     | | indexBest  $\leftarrow$  index given by line search
23     | | thresholdBest  $\leftarrow$  attribute value midway between indexBest and indexBest + 1
24
25   if not infoGainBest or not attributeBest then
26     | no attribute provides an information gain.
27     | return leaf with mode of set(1) (class labels)
28
29   re-sort set along attributeBest.
30   subsets  $\leftarrow$  getSubsets(set, attributeBest, indexBest)
31   subtree1  $\leftarrow$  trainDecisionTree(subsets(1), minLeaf)
32   subtree2  $\leftarrow$  trainDecisionTree(subsets(2), minLeaf)
33
34   return node with attributeBest, thresholdBest, subtree1, and subtree2

```

---

Once we have trained the decision tree, we can begin to test it by passing the features generated from the test set

through the tree. The testing algorithm is reproduced in pseudocode below.

---

**Algorithm 3.2:** testDecisionTree

---

**Data:** *set* of test samples with class labels (*set*(1)) and attributes (features) (*set*(2)).

*tree*, the struct of structs that represents the trained decision tree.

**Result:** *set*, the input structure modified to include predicted class membership.

---

```

1 begin
2   for each sample ∈ set do
3     treeWalked ← tree
4     classified ← false
5     attributes ← features corresponding to this sample
6     while not classified do
7       if treeWalked is a node then
8         thisAttribute ← attribute given by treeWalked
9         thisAttributeValue ← value of the sample's feature at thisAttribute
10        thisThreshold ← threshold given by treeWalked
11        remove thisAttribute from the sample's feature vector.
12        compare thisAttributeValue to thisThreshold:
13        if thisAttributeValue < thisThreshold then
14          choose left branch.
15          treeWalked ← left branch given by current treeWalked.
16        else
17          choose right branch.
18          treeWalked ← right branch given by current treeWalked.
19      else
20        treeWalked is a leaf.
21        append predicted label to set(2) at this sample.
22        classified ← true

```

---

### 3.1.1 Entropy and Information Gain

When growing the decision tree, the training algorithm utilizes a metric called *information gain* to optimize the predictive power of the tree. Before we can define information gain, we must first understand *entropy*. Entropy is an information theoretic concept that represents the amount of uncertainty in a given set of data. It is defined as

$$H(X) = - \sum_{i=1}^n P(x_i) \log_2 P(x_i) \quad (3.1)$$

Where  $P(x_i)$  is the proportion of the number of elements with class  $x_i$  to the number of elements in the set  $X$ . there are  $n$  classes in the set. Note that if all samples belong to class  $i$ ,  $P(x_i) = 1$  and  $\log_2 P(x_i) = 0$ , so the entropy is zero.

In calculating the information gain of splitting the set into two subsets, we utilize the entropy of the parent set and subtract from it a weighted entropy of each subset [5]. This is better expressed by the following equation:

$$IG(X) = H(X) - \sum_{i=1}^2 \frac{|S_i|}{|X|} H(S_i) \quad (3.2)$$

Where  $|\cdot|$  is the cardinality, or number of elements in the set, and  $S_i$  are the two subsets composed of the elements of  $X$  partitioned across a given threshold for a given feature. The figure below is a plot of the information gain



across splitting indices. So, after partitioning the set across a single attribute, (all elements of  $S_1$  are less than the threshold, and all elements in  $S_2$  are greater), we have a scalar value of information gain to decide which splitting threshold and feature would most improve the predictive ability of the decision tree. The plot below represents just one feature, but this calculation is required across all currently available features in the set. This quickly becomes computationally taxing for a large data-set, so we utilize a line search heuristic to improve the computational time without sacrificing a significant amount of accuracy.

The line search starts in the middle of the set and splits it, computing an information gain (IG). Then, we compare this middle IG to the IGs obtained by splitting the set at the 25% and 75% indices. If either of these reveals a larger IG, we set it to the new 'middle' index and consider the IGs which emerge from splitting the set half-way between the old 'middle' and half-way between the old 'left' or 'right' (depending on which one yielded a larger IG.) This allows us to approximate the maximum value of the information gain for a given feature without a brute-force technique of considering each threshold. We ensured that the line search incorporates a variety of locations to coax it to approaching the global maximum, rather than getting caught in the minor variations between adjacent indices.

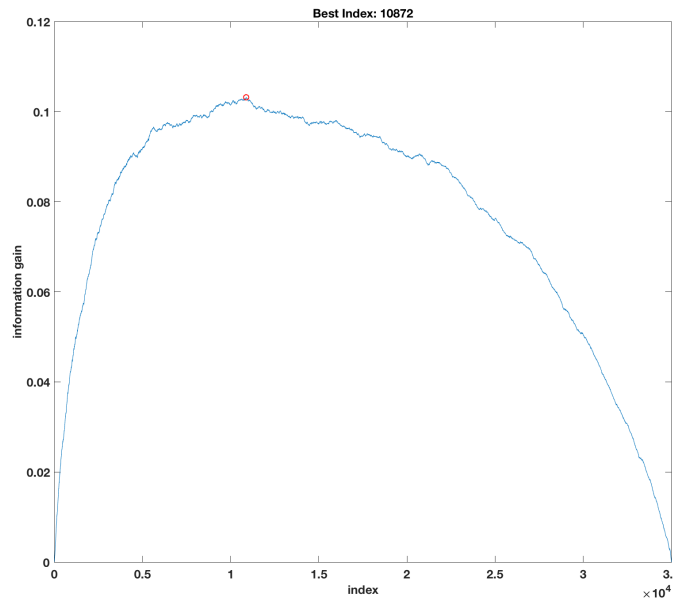


Figure 3.2: Information Gain across all possible thresholds.

## 3.2 Linear Discriminant Analysis (LDA)

Our classification success criterion is the extent to which the error rate is minimized. For LDA, we employ the Bayes Rule to classify our test points after training the classifier. We assign the test point to the class with the highest conditional probability (*i.e.*  $P(w_i|x)$ , where  $w_i$  is the class and  $x$  the test vector). In practice, it is not feasible to get conditional probability for a given point unless we have a large amount of data. So we estimate the distribution and calculate the probabilities from there.

LDA relies on the assumption of a normal distribution for each class. Linear discriminant analysis generally achieves good performance in the tasks of face and object recognition, even though the assumptions of common covariance matrix among groups and normality are often violated (Duda, et al., 2001) (Tao Li, et al., 2006)'.

Since the MNIST and Yale datasets are high-dimensional, we cannot check the normality of individual pixels. Instead, we reduce the dimensions via orthogonal projection. To do this, we employ multiclass LDA, as we have

several classes (10 for MNIST and 38 for Yale B.) The class separation in this case is given by the ratio

$$\frac{\mathbf{w}^T \Sigma_b \mathbf{w}}{\mathbf{w} \Sigma \mathbf{w}} \quad (3.3)$$

In the case of two classes, this reduces to the ratio of between-class variance and within-class variance.

### 3.2.1 Algorithm steps

Below, we describe the steps necessary to construct the LDA classifier. We begin by instantiating some variables with notation:

$n$  is the number of classes.

$N$  is the total number of training data samples.

$N_i$  is the number of points in each class.

$\mu_i$  and  $\mu$  are mean vectors for each class and global mean for the data.

The steps that we follow in our LDA algorithm are as follows.

1. We calculate within-class scatter matrix for each class

$$\Sigma_i = \frac{1}{N_i - 1} \sum_{\mathbf{x} \in D_i} (\mathbf{x} - \mu_i) (\mathbf{x} - \mu_i)^T \quad (3.4)$$

then sum them to obtain

$$\Sigma_W = \sum_{i=1}^c (N_i - 1) \Sigma_i \quad (3.5)$$

2. We then find the average within-class scatter matrix by calculating

$$\Sigma = \frac{\Sigma_W}{N} \quad (3.6)$$

3. We also calculate the between-class scatter matrix by

$$\Sigma_B = \sum_{i=1}^c \frac{N_i}{N} (\mu_i - \mu) (\mu_i - \mu)^T \quad (3.7)$$

4. We need to find eigenvectors and eigenvalues of  $\Sigma^{-1} \Sigma_b$ .
5. We then sort the eigenvectors depending on the magnitude of eigenvalues.
6. The number of highest eigenvalues will be  $c - 1$  which will be 9 and 37 respectively for MNIST and Extended Yale datasets.
7. Project our data onto the subspace(constructed by the eigenvectors of the highest eigenvalues).
8. Since we have reduced dimensions of our data, we can easily apply a discriminant function for a test vector to see which class it belongs
9. The discriminant function for each class is

$$f_i(x_k) = \mu_i^T w_a^{-1} x_k - \frac{1}{2} \mu_i^T w_a^{-1} \mu_i + \ln(P_i) \quad (3.8)$$

where  $P_i$  is the probability of each class.

10. Then we select the class with highest discriminant function evaluation.

### 3.2.2 Helpful Functions

To accomplish the above pseudo code, we used own created functions.

## 4 Test Results

The table below illustrates the lowest classification errors we were able to achieve with our Decision Tree and LDA classifiers on the MNIST and Yale Extended B datasets. For MNIST, we utilized half of the dataset for training and half for testing. However, since the Yale B dataset is so small, we were only able to get lower error rates by using ~95% of the set for training and ~5% for testing.

| Algorithm     | MNIST  | Yale B |
|---------------|--------|--------|
| LDA           |        |        |
| Decision Tree | 17.42% | 57.89% |

Table 4.1: Lowest classification errors achieved with LDA and Decision Trees.

## 4.1 Preliminary Hyperparameter Optimization

### 4.1.1 Decision Trees

The table below illustrates some results that we obtained during various configurations of the decision tree training algorithm on MNIST. In an effort to optimize training time vs. test accuracy, we noticed some trends in the algorithm's performance. Notably, utilizing `minLeaf` doesn't seem to contribute to over-fitting, as was noted in other implementations [6]. This may be in part to the type of algorithm we are using. Particularly, the pure C4.5 algorithm moves back up the tree if certain conditions are met, thereby improving a previously-made split. This bore more complexity than we were able to achieve at this time, but may be responsible for a more simpler tree generation on our part. Note that for MNIST, we used half of the 70k samples for training and half for testing.

| Training Configuration | 1  | 2  | 2  | 2   | 3   | 3   | 1    | 1    | 1    | 1    | 4     | 4     |
|------------------------|----|----|----|-----|-----|-----|------|------|------|------|-------|-------|
| numFeatures            | 30 | 30 | 60 | 200 | 200 | 200 | 30   | 100  | 100  | 20   | 10    | 10    |
| minLeaf                | 1  | 1  | 2  | 2   | 3   | 4   | 4    | 4    | 1    | 1    | 1     | 3     |
| Error Rate (%)         | 22 | 26 | 26 | 26  | 23  | 24  | 22.6 | 23.6 | 23.5 | 22.9 | 17.42 | 20.37 |
| Mins To Train          | 48 | 2  | 2  | 3   | 12  | 12  | 47   | 60   | 102  | 11   | 3     | 3     |

Table 4.2: Hyperparameter Configuration of Decision Tree for MNIST.

The training configurations were primarily modifications to the algorithm's search through the features to find the best one to split the set on. They are as follows:

1. All features were considered for the best information gain in a particular set.
2. The decision tree was grown by considering only the first feature in the set. This was an attempt to reduce the computational complexity.
3. If the number of features left in a set was greater than 5, we considered only the first 5. Otherwise, we considered all features left.
4. For configurations 1-3, we utilized features generated via PCA. For this experiment, we utilized features generated with LDA. This yielded our best performance.

## 5 Conclusion

---

In conclusion, we have shown that utilizing Decision Trees and Linear Discriminant Analysis on the Extended Yale Dataset B and MNIST datasets yields a favorable result. In the next part of this project, we will improve our classification accuracy and partake in a more thorough exploration of the hyperparameter space to optimize and generalize our classifiers.

## 6 References

---

- [1] Sebastian Raschka. What is the difference between lda and pca for dimensionality reduction?, 2018. [Online; accessed 2018-03-14].
- [2] Yann LeCun and Corinna Cortes. MNIST handwritten digit database. 2010.
- [3] Wikipedia contributors. Id3 algorithm — wikipedia, the free encyclopedia, 2017. [Online; accessed 14-March-2018].
- [4] Wikipedia contributors. C4.5 algorithm — wikipedia, the free encyclopedia, 2018. [Online; accessed 14-March-2018].
- [5] Wikipedia contributors. Information gain in decision trees — wikipedia, the free encyclopedia, 2017. [Online; accessed 15-March-2018].
- [6] Mathworks. Matlab documentation - fitctree, 2018. [Online; accessed 2018-03-14].

## 7 Code Listings

---

Below are the primary scripts that solve the project. Please see the `code` folder for supporting functions.

Listing 1: Main Code for Decision Tree on MNIST

```
1  %{
2
3  kudiyar orazymbetov
4  n casale
5
6  ECE 759 Project
7  18/03/16
8
9  this script orchestrates the training and testing of
10 the decision tree classifier
11
12 features are generated using principal component analysis
13
14 %}
15
16 clear; close all;
17 addpath('utility', 'MNIST', 'MNIST/data', 'MNIST/loadMNIST', 'lda');
18
19 fprintf('begin MNIST decision tree script\n');
20
```

```

21 % hyper-parameters
22 N_tr = 35e3; % training samples
23 N_te = 35e3; % test samples
24
25 % for feature selection
26 usePCA = false;
27 if usePCA
28     numFeatures = 30;
29 else % use LDA
30     numFeatures = 10;
31 end
32
33 % for decision tree
34 minLeaf = 1; % to prevent overfitting
35
36 %seed = 152039828;
37 %rng(seed); % for reproducibility
38
39 % partition data
40 % MNIST contains 70k examples
41 [train, test] = loadMNIST(N_tr);
42
43 %% dimensionality reduction / feature generation
44 % via principal component analysis (pca) (svd)
45 st = cputime;
46
47 if usePCA
48     [train, U, V] = pca_(train, numFeatures);
49 else
50     [train, test] = lda_features(train, test, 0:numFeatures-1);
51 end
52
53 fprintf('Features Generated in %4.2f minutes\n', (cputime - st)/60);
54
55 %% train
56 st = cputime;
57
58 tree = trainDecisionTree({train{2:3}}, minLeaf);
59
60 fprintf('Trained in %4.2f minutes\n', (cputime - st)/60);
61
62 %% test
63 st = cputime;
64
65 if usePCA
66     test{3} = (U'*test{1}.*V)';
67     test{3} = test{3}(1:numFeatures,:);
68 end
69
70 test = testDecisionTree(test, tree);
71
72 fprintf('Tested in %4.2f minutes\n', (cputime - st)/60);
73
74 % Classification Error
75 errors = nnz(test{2}(:,1) ~= test{2}(:,2));
76 errorRate = (errors/N_te)*100;

```

```

77
78 filename = sprintf('mnist_tree%2.0f_%d.mat', errorRate, minLeaf);
79 %save(filename, 'tree');
80 %filename = sprintf('UV%2.0f.mat', errorRate);
81 %save(filename, 'U', 'V', '-v7.3');
82
83 fprintf('numFeatures: %d, minLeaf: %d, error rate: %2.2f\n', ...
84         numFeatures, minLeaf, errorRate);
85
86 %% Test Results
87 %{
88
89 numFeatures      : 30 30 60 200 200 200      30 100 100 20 10 (lda)
90 minLeaf          : 1 1 2 2 3 4 4 4 1 1 1
91 Error Rate       : 22 26 26 26 23 24 22.6 23.6 23.5 22.9 18.42
92 Mins To Train    : 48 2 2 3 12 12 47 60 102 11 3
93
94 , - all attributes were considered for the best information gain for a
95 particular set.
96
97 * - for these experiments, the decision tree was grown by considering
98 only the first attribute in the set. all things held equal, this was simply
99 an attempt to reduce the computational complexity.
100
101 & - if the number of attributes was > 5, consider only the first 5, else,
102 consider all attributes (1-5)
103
104 %}

```

Listing 2: Main Code for Decision Tree on Yale B

```

1  %{
2
3  kudiyar orazymbetov
4  n casale
5
6  ECE 759 Project
7  18/03/16
8
9  this script orchestrates the training and testing of
10 the decision tree classifier
11
12 features are generated using principal component analysis
13
14 %}
15
16 clear; close all;
17 addpath('utility', 'YaleB', 'YaleB/data');
18
19 fprintf('begin Yale B decision tree script\n');
20
21 %seed = 152039828;
22 %rng(seed); % for reproducibility
23
24 % hyper-parameters
25 % for feature selection
26 usePCA = false;

```

```

27 if usePCA
28     N_tr = 2414/2; % training samples
29     N_te = N_tr; % test samples
30     numFeatures = 30;
31 else
32     N_tr = 2300; % training samples
33     N_te = 2414 - N_tr; % test samples
34     numFeatures = 38;
35 end
36
37 minLeaf = 1; % to prevent overfitting
38
39 % partition data
40 % YaleB contains 2414 examples
41 [train, test] = loadYaleB(N_tr);
42
43 %% dimensionality reduction / feature generation
44 % via principal component analysis (pca) (svd)
45 st = cputime;
46
47 if usePCA
48     [train, U, V] = pca_(train, numFeatures);
49 else
50     [train, test] = lda_features(train, test, 1:numFeatures);
51 end
52
53 fprintf('Features Generated in %4.2f minutes\n', (cputime - st)/60);
54
55 %% train
56 st = cputime;
57
58 tree = trainDecisionTree({train{2:3}}, minLeaf);
59
60 fprintf('Trained in %4.2f minutes\n', (cputime - st)/60);
61
62 %% test
63 st = cputime;
64
65 if usePCA
66     test{3} = (U'*test{1}.*V)';
67     test{3} = test{3}(1:numFeatures,:);
68 end
69
70 test = testDecisionTree(test, tree);
71
72 fprintf('Tested in %4.2f minutes\n', (cputime - st)/60);
73
74 % Classification Error
75 errors = nnz(test{2}(:,1) ~= test{2}(:,2));
76 errorRate = (errors/N_te)*100;
77
78 filename = sprintf('yaleB_tree%2.0f_%d.mat', errorRate, minLeaf);
79 %save(filename, 'tree');
80 %filename = sprintf('UV%2.0f.mat', errorRate);
81 %save(filename, 'U', 'V', '-v7.3');
82

```

```
83 fprintf('\nnumFeatures: %d, minLeaf: %d, error rate: %2.2f\n', ...
84         numFeatures, minLeaf, errorRate);
85
86 %% Test Results
87 %{
88
89 numFeatures      :
90 minLeaf          :
91 Error Rate       :
92 Mins To Train    :
93
94 , - all attributes were considered for the best information gain for a
95 particular set.
96
97 %}
```