# Project Part 1 Pattern Recognition ECE 759

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# 1 Introduction

In this report, we outline the process we undertook to implement two classification algorithms: linear discriminant analysis (LDA) and Decision Trees. To complete this, we experimented with two feature generation methods: principle components analysis (PCA) and LDA itself (for use in decision trees.) Throughout this document, we use the terms 'features' and 'attributes' interchangeably.

After presenting an explanation of our algorithms' implementations, we will discuss our current-best results and our preliminary exploration of the hyperparameter space. The hyperparameters are adjustments that variously control the accuracy and computational complexity of our classifiers. A more thorough exploration and validation of these parameters will be presented in the next installment of the project.

Code for this project is included in our project submission. In addition, it's available on GitHub at https://github.com/n-casale/ece759-project. The Git repository includes a more thorough representation of the path our code took to its current state.

# 2 Feature Selection

### 2.1 Decision Tree Feature Generation

### 2.1.1 MNIST

In working with the decision trees, we utilized the SVD of each image in the training set.

### 2.2 LDA vs PCA

LDA and PCA linearly transform the data to reduce the dimensions. The difference between the two techniques is that LDA is supervised whereas PCA is unsupervised. PCA finds orthogonal directions which maximize the variance, thereby expressing the data along *principle components* that are the most pronounced. We can view a PCA technique as in Figure (2.1).

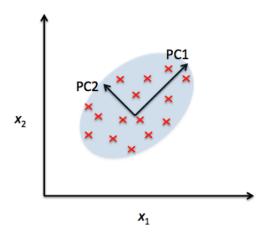


Figure 2.1: PCA implemented on 2-dimensional data [1].

LDA maximizes the class separability and can be viewed as in Figure (2.2).

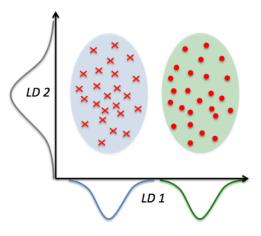


Figure 2.2: LDA visualization [1].

The underlying concept of LDA is taking the eigenvectors of  $\frac{\Sigma_b}{\Sigma}$  where  $\Sigma$  is within-class scatter matrix and  $\Sigma_b$  is between-class scatter matrix. By having this division of matrices, we separate the classes away from each other. On the other hand, since PCA is unsupervised it only tries to capture the data in minimum number of variables.

## 2.3 LDA for MNIST and Extended YaleB

LDA reduces the data with K classes with large dimensions to K-1 dimensions which captures the most energy of the data. Implementing LDA as a dimension reduction, MNIST and Extended YaleB datasets are reduced to 9 and 37 variables for each data point. Then we worked with this transformed data to do further classification.

# 3 Algorithm Implementations

# 3.1 Decision Tree Algorithm

A binary decision tree is a hierarchical structure that takes input data at its root and propagates it to one of many leaves. Each *leaf* of the tree represents a class designation. To reach a leaf, the features of the data are utilized at *nodes* to make a binary decision: to proceed down the left or right *branch* of the tree? To answer this question, the node also carries a *threshold* that the feature value of the test data is compared against. If the test feature is less than the threshold, we proceed down the left branch. Otherwise, the right. An illustration of a simple decision tree is pictured below.

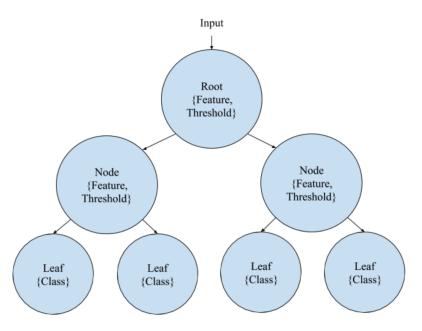


Figure 3.1: An example decision tree.

This decision tree structure needs to be generated before it can be used with test data. To train a decision tree that appropriately classifies our test data according to the features we generated, we employ a recursive function. The function signature is

tree = trainDecisionTree(set)

Where **set** is the training set, which is a MATLAB structure that contains the raw data (unused), class labels, and generated features. **tree** is the returned structure that can be used during testing. It is essentially a nested structure that contains two types of elements: nodes and leaves. At each node of the tree, a feature and threshold are specified. If a test sample's value at that particular feature is less than the threshold, the sample is passed down the left branch of the node. Similarly, if the sample's feature is greater than the threshold, it goes through the right branch. This is repeated until we reach a leaf node, which specifies a class membership.

The decision tree training algorithm has a few major steps, and proceeds by evaluating a metric called *information* gain at various configurations. For now, suffice it to say that information gain is a scalar that represents the improvement in prediction as we narrow down the set (by growing the tree) to find appropriate leaves. Our implementation most closely follows that of the ID3 and C4.5 algorithms developed by Ross Quinlan in the late 80s and early 90s [2] [3].

- 1. Check stopping conditions, which generate leaves.
  - If there are no more features to split on, return a leaf with the class mode of the set.
  - The set is smaller than minLeaf, which is a tuning parameter that is meant to reduce overfitting of the training data. If this condition is met, return a leaf with the class mode of the set.

- If all samples in the set belong to the same class, return a leaf with the class.
- If no feature yields an improvement to the information gain (discussed below), then return a leaf with the class mode of the set. Note that this condition is only evaluated after step 2.
- 2. Iterate over each feature. Sort the set along the current feature. We utilize a threshold that splits the set between adjacent feature values. Because the information gain across thresholds is convex on the whole (see Fig. 3.2), we use a line search that approximates the highest information gain for each threshold.
  - Let attributeBest and indBest be the feature and index that yield the highest information gain. Since the set is sorted, we can simply split the set at the index given by indBest for the recursion.
- 3. Recur over the subsets given by indBest to find the next attribute that yields the highest information gain. Note that we exclude the attribute/feature we chose in this execution of trainDecisionTree(.).

The algorithm is reproduced in pseudocode below.

### **Algorithm 3.1:** trainDecisionTree

```
Data: set of training samples with class labels (set(1)) and attributes (features) (set(2)).
   minLeaf, an integer specifying the minimum number of elements in set required to make a splitting node. i.e.
   a leaf is generated if the set has fewer elements than minLeaf.
   Result: tree, a structure containing nodes and leaves.
 1 begin
       check for base cases:
 \mathbf{2}
       if set(2) = \emptyset then
 3
 4
           no more attributes (features) to split on.
           return leaf with mode of set(1) (class labels)
 5
       if length(set(1)) < minLeaf then
 6
          return leaf with mode of set(1) (class labels)
 7
 8
       thisSetEntropy \longleftarrow getEntropy(set)
       if not thisSetEntropy then
 9
10
           all samples are in the same class.
           return leaf with first element of set(1)
11
12
       instantiate tracking variables:
13
14
       attributeBest \longleftarrow 0
       thresholdBest \longleftarrow 0
15
       infoGainBest \longleftarrow 0
16
       indexBest \longleftarrow 0
17
       for attribute \in range(\# of features left in set) do
18
           sort set along attribute.
19
           perform line search heuristic to approximate max information gain by splitting set at various indices.
20
           thisInfoGain \leftarrow lineSearch(set)
21
           if thisInfoGain > infoGainBest then
22
              attributeBest \longleftarrow attribute
23
               infoGainBest \leftarrow thisInfoGain
24
              indexBest \leftarrow index given by line search
25
               thresholdBest \leftarrow attribute value midway between indexBest and indexBest + 1
26
27
       if not infoGainBest or not attributeBest then
28
           no attribute provides an information gain.
29
30
           return leaf with mode of set(1) (class labels)
31
       re-sort set along attributeBest.
32
       subsets \longleftarrow getSubsets(set, attributeBest, indexBest)
33
       subtree1 \leftarrow trainDecisionTree(subsets(1), minLeaf)
34
       subtree2 \leftarrow trainDecisionTree(subsets(2), minLeaf)
35
36
       return node with attributeBest, thresholdBest, subtree1, and subtree2
```

Once we have trained the decision tree, we can begin to test it by passing the features generated from the test set

through the tree. The testing algorithm is reproduced in psuedocode below.

### Algorithm 3.2: testDecisionTree

```
Data: set of test samples with class labels (set(1)) and attributes (features) (set(2)).
   tree, the struct of structs that represents the trained decision tree.
   Result: set, the input structure modified to include predicted class membership.
      for each sample \in set do
2
          tree Walked \longleftarrow tree
3
          classified \longleftarrow false
4
5
          attributes \leftarrow features corresponding to this sample
           while not classified do
6
              if treeWalked is a node then
7
                  thisAttribute \leftarrow attribute given by treeWalked
8
                  thisAttributeValue \leftarrow value of the sample's feature at thisAttribute
9
                  thisThreshold \leftarrow threshold given by treeWalked
10
                   remove this Attribute from the sample's feature vector.
11
                  compare this Attribute Value to this Threshold:
                  if thisAttributeValue < thisThreshold then
13
                      choose left branch.
14
                      tree Walked \leftarrow left branch given by current tree Walked.
15
                  else
16
                      choose right branch.
17
                      tree Walked \leftarrow right branch given by current tree Walked.
18
              else
19
                  tree Walked is a leaf.
20
                  append predicted label to set(2) at this sample.
21
                  classified \leftarrow true
22
```

### 3.1.1 Entropy and Information Gain

When growing the decision tree, the training algorithm utilizes a metric called *information gain* to optimize the predictive power of the tree. Before we can define information gain, we must first understand *entropy*. Entropy is an information theoretic concept that represents the amount of uncertainty in a given set of data. It is defined as

$$H(X) = -\sum_{i=1}^{n} P(x_i) \log_2 P(x_i)$$
(3.1)

Where  $P(x_i)$  is the proportion of the number of elements with class  $x_i$  to the number of elements in the set X. there are n classes in the set. Note that if all samples belong to class i,  $P(x_i) = 1$  and  $\log_2 P(x_i) = 0$ , so the entropy is zero.

In calculating the information gain of splitting the set into two subsets, we utilize the entropy of the parent set and subtract from it a weighted entropy of each subset. This is better expressed by the following equation:

$$IG(X) = H(X) - \sum_{i=1}^{2} \frac{|S_i|}{|X|} H(S_i)$$
(3.2)

Where  $|\cdot|$  is the cardinality, or number of elements in the set, and  $S_i$  are the two subsets composed of the elements of X partitioned across a given threshold for a given feature. The figure below is a plot of the information gain

across splitting indices. So, after partitioning the set across a single attribute, (all elements of  $S_1$  are less than the threshold, and all elements in  $S_2$  are greater), we have a scalar value of information gain to decide which splitting threshold and feature would most improve the predictive ability of the decision tree. The plot below represents just one feature, but this calculation is required across all currently available features in the set. This quickly becomes computationally taxing for a large data-set, so we utilize a line search heuristic to improve the computational time without sacrificing a significant amount of accuracy.

The line search starts in the middle of the set and splits it, computing an information gain (IG). Then, we compare this middle IG to the IGs obtained by splitting the set at the 25% and 75% indices. If either of these reveals a larger IG, we set it to the new 'middle' index and consider the IGs which emerge from splitting the set half-way between the old 'middle' and half-way between the old 'left' or 'right' (depending on which one yielded a larger IG.) This allows us to approximate the maximum value of the information gain for a given feature without a brute-force technique of considering each threshold. We ensured that the line search incorporates a variety of locations to coax it to approaching the global maximum, rather than getting caught in the minor variations between adjacent indices.

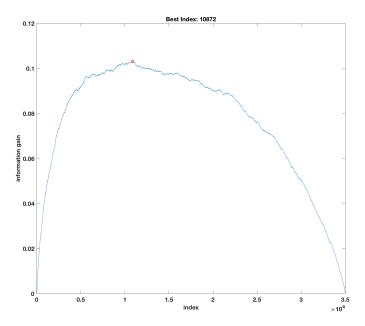


Figure 3.2: Information Gain across all possible thresholds.

# 3.2 Linear Discriminant Analysis

Our classification criterion is to misclassify as small as possible. The rule we employ in classifying the data points is through the use of Bayes Rule. We put the data point to the group with the highest conditional probability (i.e.  $P(w_i|x)$ ). In practice, it is not feasible to get conditional probability for a given point unless we have a huge data. So we should assume the distribution and calculate the probabilities.

LDA relies on the assumption of normal distribution of data for each class. Linear discriminant analysis frequently achieves good performances in the tasks of face and object recognition, even though the assumptions of common covariance matrix among groups and normality are often violated (Duda, et al., 2001) (Tao Li, et al., 2006)'.

Since MNIST and Yale datasets are high-dimensional, we can not check the normality of variables. Instead, we can reduce the dimensions via a projection. We need to employ multiclass LDA as we have several classes. The class separation in this case will be given by the ratio of  $\frac{\boldsymbol{w}^T \Sigma_b \boldsymbol{w}}{\boldsymbol{w} \Sigma \boldsymbol{w}}$ . In the case of two classes, this will reduce just to the

ratio of between-class variance to within-class variance.

### 3.2.1 Algorithm steps

Variable notations:

n is number of classes

N is the total number of training data

 $N_i$  is the number of points in each class

 $\mu_i$  and  $\mu$  are mean vectors for each class and overall mean for the data

The steps that we follow in our LDA algorithm are:

- 1. We calculate within-class scatter matrix  $\Sigma_i = \frac{1}{N_i 1} \sum_{\boldsymbol{x} \in D_i}^n (\boldsymbol{x} \boldsymbol{\mu}_i) (\boldsymbol{x} \boldsymbol{\mu}_i)^T$  for each class, then sum them up to get  $\Sigma_W = \sum_{i=1}^c (N_i 1)\Sigma_i$ .
- 2. Then we find average within-class scatter matrix by calculating  $\Sigma = \frac{\Sigma_W}{N}$
- 3. We also calculate the between-class scatter matrix by  $\Sigma_B = \sum_{i=1}^c \frac{N_i}{N} (\boldsymbol{\mu}_i \boldsymbol{\mu}) (\boldsymbol{\mu}_i \boldsymbol{\mu})^T$ .
- 4. We need to find eigenvectors and eigenvalues of  $\Sigma^{-1}\Sigma_b$ .
- 5. We then sort the eigenvectors depending on the magnitude of eigenvalues.
- 6. The number of highest eigenvalues will be c-1 which will be 9 and 37 for MNIST and Extended Yale datasets.
- 7. Project our data onto the subspace (constructed by the eigenvectors of the highest eigenvalues).
- 8. Since we have reduced dimensions of our data, we can easily apply a discriminant function for a test vector to see which class it belongs
- 9. A discriminant function for each class is  $f_i(x_k) = \mu_i w_a^{-1} x_k^T \frac{1}{2} \mu_i w_a^{-1} \mu_i^T + \ln(P_i)$  is evaluated where  $P_i$  is the probability of each class.
- 10. Then we select a class with highest discriminant function.

### 3.2.2 Helpful Functions

To accomplish the above pseudo code, we used own created functions.

# 4 Test Results

The table below illustrates the lowest classification errors we were able to achieve with our Decision Tree and LDA classifiers on the MNIST and Yale Extended B datasets. For MNIST, we utilized half of the dataset for training and half for testing. However, since the Yale B dataset is so small, we were only able to get lower error rates by using  $\sim 95\%$  of the set for training and  $\sim 5\%$  for testing.

| Algorithm     | MNIST  | Yale B |
|---------------|--------|--------|
| LDA           |        |        |
| Decision Tree | 17.42% | 57.89% |

Table 4.1: Lowest classification errors achieved with LDA and Decision Trees.

# 4.1 Preliminary Hyperparameter Optimization

### 4.1.1 Decision Trees

The table below illustrates some results that we obtained during various configurations of the decision tree training algorithm on MNIST. In an effort to optimize training time vs. test accuracy, we noticed some trends in the algorithm's performance. Notably, utilizing minLeaf doesn't seem to contribute to over-fitting, as was noted in other implementations [4]. This may be in part to the type of algorithm we are using. Particularly, the pure C4.5 algorithm moves back up the tree if certain conditions are met, thereby improving a previously-made split. This bore more complexity than we were able to achieve at this time, but may be responsible for a more simpler tree generation on our part. Note that for MNIST, we used half of the 70k samples for training and half for testing.

| Training Configuration | 1  | 2  | 2  | 2   | 3   | 3   | 1    | 1    | 1    | 1    | 4     | 4     |
|------------------------|----|----|----|-----|-----|-----|------|------|------|------|-------|-------|
| numFeatures            | 30 | 30 | 60 | 200 | 200 | 200 | 30   | 100  | 100  | 20   | 10    | 10    |
| minLeaf                | 1  | 1  | 2  | 2   | 3   | 4   | 4    | 4    | 1    | 1    | 1     | 3     |
| Error Rate (%)         | 22 | 26 | 26 | 26  | 23  | 24  | 22.6 | 23.6 | 23.5 | 22.9 | 17.42 | 20.37 |
| Mins To Train          | 48 | 2  | 2  | 3   | 12  | 12  | 47   | 60   | 102  | 11   | 3     | 3     |

Table 4.2: Hyperparameter Configuration of Decision Tree for MNIST.

The training configurations were primarily modifications to the algorithm's search through the features to find the best one to split the set on. They are as follows:

- 1. All features were considered for the best information gain in a particular set.
- 2. The decision tree was grown by considering only the first feature in the set. This was an attempt to reduce the computational complexity.
- 3. If the number of features left in a set was greater than 5, we considered only the first 5. Otherwise, we considered all features left.
- 4. For configurations 1-3, we utilized features generated via PCA. For this experiment, we utilized features generated with LDA. This yielded our best performance.

# 5 Conclusion

In conclusion, we have shown that utilizing Decision Trees and Linear Discriminant Analysis on the Extended Yale Dataset B and MNIST datasets yields a favorable result. In the next part of this project, we will improve our classification accuracy and partake in a more thorough exploration of the hyperparameter space to optimize and generalize our classifiers.

# 6 References

- [1] Sebastian Raschka. What is the difference between lda and pca for dimensionality reduction?, 2018. [Online; accessed 2018-03-14].
- [2] Wikipedia contributors. Id3 algorithm wikipedia, the free encyclopedia, 2017. [Online; accessed 14-March-2018].
- [3] Wikipedia contributors. C4.5 algorithm wikipedia, the free encyclopedia, 2018. [Online; accessed 14-March-2018].
- [4] Mathworks. Matlab documentation fitctree, 2018. [Online; accessed 2018-03-14].

# 7 Code Listings

Below are the primary scripts that solve the project. Please see the code folder for supporting functions.

Listing 1: Main Code for Decision Tree on MNIST

```
%{
2
   kudiyar orazymbetov
4
   n casale
5
   ECE 759 Project
6
7
   18/03/16
8
9
   this script orchestrates the training and testing of
   the decision tree classifier
   features are generated using principal compenent analysis
13
   %}
14
15
16
   clear; close all;
17
   addpath('utility', 'MNIST', 'MNIST/data', 'MNIST/loadMNIST', 'lda');
18
   fprintf('begin MNIST decision tree script\n');
19
20
21
   % hyper-parameters
22
   N_tr = 35e3; % training samples
23
   N_{te} = 35e3; \% test samples
24
   % for feature selection
25
26
   usePCA = false;
27
   if usePCA
28
            numFeatures = 30;
29
   else % use LDA
30
            numFeatures = 10;
   end
   % for decision tree
34
   minLeaf = 1; % to prevent overfitting
35
```

```
%seed = 152039828;
36
37
   %rng(seed); % for reproducibility
38
39
   % partition data
40
   % MNIST contains 70k examples
   [train, test] = loadMNIST(N_tr);
41
42
   %% dimensionality reduction / feature generation
43
44
   % via prinicpal component analysis (pca) (svd)
   st = cputime;
45
46
47
   if usePCA
48
            [train, U, V] = pca_(train, numFeatures);
49
   else
50
            [train, test] = lda_features(train, test, 0:numFeatures-1);
51
   end
52
   fprintf('Features Generated in %4.2f minutes\n', (cputime - st)/60);
54
55
   %% train
56
   st = cputime;
   tree = trainDecisionTree({train{2:3}}, minLeaf);
58
59
   fprintf('Trained in %4.2f minutes\n',(cputime - st)/60);
60
61
62
   %% test
63
   st = cputime;
64
65
   if usePCA
66
           test{3} = (U'*test{1}'*V)';
67
            test{3} = test{3}(1:numFeatures,:);
68
   end
69
70
   test = testDecisionTree(test, tree);
71
72
   fprintf('Tested in %4.2f minutesn', (cputime - st)/60);
73
74
   % Classification Error
   errors = nnz(test{2}(:,1) ~= test{2}(:,2));
   errorRate = (errors/N_te)*100;
76
78
   filename = sprintf('mnist_tree%2.0f_%d.mat', errorRate, minLeaf);
79
   %save(filename, 'tree');
   %filename = sprintf('UV%2.0f.mat', errorRate);
80
81
   %save(filename, 'U', 'V', '-v7.3');
82
   fprintf('numFeatures: %d, minLeaf: %d, error rate: %2.2f\n', ...
83
            numFeatures, minLeaf, errorRate);
84
85
   %% Test Results
86
87
   %{
88
                                    &
                                        &
                  : 30 30 60 200 200 200
                                            30
                                                100
                                                      100
                                                            20 10 (lda)
89
   numFeatures
                           2
                               2
                                    3
90
                    1
                        1
                                        4
                                             4
                                                        1
                                                             1
91
   Error Rate
                  : 22 26 26
                              26
                                   23
                                       24 22.6 23.6 23.5 22.9
                                                                   18.42
```

```
Mins To Train: 48
92
                        2
                          2
                               3 12
                                      12
                                            47
                                                 60
                                                     102
                                                           11
                                                                      3
93
    , - all attributes were considered for the best information gain for a
94
    particular set.
95
96
97
    * - for these experiments, the decision tree was grown by considering
98
    only the first attribute in the set. all things held equal, this was simply
    an attempt to reduce the computational complexity.
99
100
    & - if the number of attributes was > 5, consider only the first 5, else,
102
    consider all attributes (1-5)
104
   %}
```

Listing 2: Main Code for Decision Tree on Yale B

```
%{
1
2
3
   kudiyar orazymbetov
   n casale
4
5
6
   ECE 759 Project
7
   18/03/16
8
   this script orchestrates the training and testing of
9
   the decision tree classifier
10
11
12
   features are generated using principal compenent analysis
13
14
   %}
15
   clear; close all;
16
   addpath('utility', 'YaleB', 'YaleB/data');
17
18
19
   fprintf('begin Yale B decision tree script\n');
20
   %seed = 152039828;
21
22
   %rng(seed); % for reproducibility
23
24
   % hyper-parameters
25
   % for feature selection
   usePCA = false;
26
   if usePCA
27
28
            N_{tr} = 2414/2; % training samples
29
            N_te = N_tr; % test samples
30
            numFeatures = 30;
31
   else
32
            N_{tr} = 2300; % training samples
            N_{te} = 2414 - N_{tr}; \%  test samples
34
            numFeatures = 38;
35
   end
36
   minLeaf = 1; % to prevent overfitting
38
39
   % partition data
40
   % YaleB contains 2414 examples
   [train, test] = loadYaleB(N_tr);
```

```
42
43
   %% dimensionality reduction / feature generation
   % via prinicpal component analysis (pca) (svd)
44
45
   st = cputime;
46
47
   if usePCA
48
            [train, U, V] = pca_(train, numFeatures);
49
   else
50
            [train, test] = lda_features(train, test, 1:numFeatures);
   end
52
   fprintf('Features Generated in %4.2f minutes\n', (cputime - st)/60);
54
   %% train
56
   st = cputime;
58
   tree = trainDecisionTree({train{2:3}}, minLeaf);
59
60
   fprintf('Trained in %4.2f minutes\n',(cputime - st)/60);
61
   %% test
62
63
   st = cputime;
64
65
   if usePCA
            test{3} = (U'*test{1}'*V)';
66
67
            test{3} = test{3}(1:numFeatures,:);
68
   end
69
   test = testDecisionTree(test, tree);
71
72
   fprintf('Tested in %4.2f minutes\n', (cputime - st)/60);
73
74
   % Classification Error
   errors = nnz(test{2}(:,1) ~= test{2}(:,2));
75
   errorRate = (errors/N_te)*100;
76
77
78
   filename = sprintf('yaleB_tree%2.0f_%d.mat', errorRate, minLeaf);
   %save(filename, 'tree');
79
   %filename = sprintf('UV%2.0f.mat', errorRate);
80
   %save(filename, 'U', 'V', '-v7.3');
81
82
83
   fprintf('\numFeatures: %d, minLeaf: %d, error rate: %2.2f\n', ...
84
           numFeatures, minLeaf, errorRate);
85
   %% Test Results
86
87
   %{
88
89
   numFeatures
90
   minLeaf
91
   Error Rate
92
   Mins To Train:
93
94
   , - all attributes were considered for the best information gain for a
95
   particular set.
96
97
   %}
```