# MAECS

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# **Contents**

	Syml	ools						 	 	 	 	 		2
1	MAE	CS: Model for	Adaptive	Ecosyste	ems in (	Coastal	Seas							4
		General Over							 	 	 	 		4
2	Todo	List												5
3	Data	Type Index												7
	3.1	Class Hierarch	hy					 	 	 	 	 		7
4		Type Index												8
	4.1	Data Types Li	st					 	 	 	 	 	٠	8
5	File I													9
	5.1	File List						 	 	 	 	 		9
6	Data	Type Docume	entation											10
	6.1	fabm_hzg_ma	aecs Modul	le Referen	ice			 	 	 	 	 		10
		6.1.1 Detail	ed Descrip	otion				 	 	 	 	 		10
			er Functio											11
		6.1.2.												11
		6.1.2.	2 get lic	ght extinct										12
		6.1.2.		s init stoic										12
		6.1.2.		s do										13
		6.1.2.		s_ac s get vert										14
	6.2	fabm_hzg_ma			_									14
	0.2		ed Descrip											14
	6.3	maecs function	•											14
	0.0	_	ed Descrip											15
			per Functio											15
		6.3.2.		nternal st										15
		6.3.2.	_	sensitivitie										16
		6.3.2.	_	(										16
		6.3.2.		t										17
		6.3.2.		efunc										17
		6.3.2.		efunc1 .										17
		6.3.2.	•											17
		6.3.2.		ederiv										17
		6.3.2.		g										18
		6.3.2.		nass th small										18
	6.4	fabm_hzg_ma		_										18
	0.4		ed Descrip											18
	6 E													
	6.5	maecs_grazin	•											18
			ed Descrip per Functio											19
														19
		6.5.2.	•	g										19
	0.0	6.5.2.	•	g_losses									•	19
	b.b	maecs primp	rua ivioaule	: Reierend	æ			 	 	 	 	 		19

CONTENTS

	6.6.1	Detailed Description	20
	6.6.2	Member Function/Subroutine Documentation	20
		6.6.2.1 photosynthesis	20
6.7		_types Module Reference	21
	6.7.1	Detailed Description	21
6.8		_types::stoich_pointer Type Reference	21
	6.8.1	Detailed Description	21
6.9		zg_maecs::type_hzg_maecs Type Reference	21
0.40	6.9.1	Detailed Description	22
6.10		_types::type_maecs_allocation_fractions Type Reference	22
6 11		Detailed Description	22 22
0.11		_types::type_maecs_base_model Type Reference	22
6 12		_types::type_maecs_basic_traits Type Reference	22
0.12		Detailed Description	22
6.13		_types::type_maecs_env Type Reference	23
0.10		Detailed Description	23
6.14		_types::type_maecs_life Type Reference	23
		Detailed Description	23
6.15		_types::type_maecs_nutindex Type Reference	23
		Detailed Description	23
6.16		_types::type_maecs_om Type Reference	23
		Detailed Description	24
6.17		_types::type_maecs_phy Type Reference	24
		Detailed Description	24
6.18		_types::type_maecs_rhs Type Reference	24
		Detailed Description	24
6.19		_types::type_maecs_sensitivities Type Reference	24
		Detailed Description	24
6.20		_types::type_maecs_switch Type Reference	24
	6.20.1	Detailed Description	24
6.21	maecs	_types::type_maecs_traitdyn Type Reference	25
	6.21.1	Detailed Description	25
6.22	maecs	_types::type_maecs_zoo Type Reference	25
	6.22.1	Detailed Description	25
		entation	26
7.1		_functions.F90 File Reference	26
7.0	7.1.1	Detailed Description	26
7.2		grazing.F90 File Reference	26
7.0	7.2.1	Detailed Description	26
7.3	maecs_ 7.3.1	_maecsdo_combined.F90 File Reference	27
7.4		Detailed Description	27 27
7.4	7.4.1	Detailed Description	27
7.5		types.F90 File Reference	27
7.5	7.5.1	Detailed Description	28
	7.5.1	betailed bescription	20
Text	ual Mod	el Description	29
8.1	Model	structure	29
	8.1.1	Mass equations	29
8.2	Proces	s Descriptions	30
	8.2.1	Growth rate components and primary production	30
	8.2.2	Respiration and temperature	31
	8.2.3	Multi-nutrient co-limitation	31
	8.2.4	Uptake system allocation and PI-coefficients	32
	8.2.5	Nutrient uptake	33
	8.2.6	Grazing	34
	8.2.7	Sinking loss	34

7

8

CONTENTS

Index	<b>K</b>		41
Biblio	ography	y	39
8.4	l Ackno	pwledgements	39
	8.3.5	Photoacclimation and transport	39
	8.3.4	Costs in P and Si uptake	38
	8.3.3	Uptake activity regulation	38
	8.3.2	Quota-uptake feed-back	37
	8.3.1	Growth derivatives under co-limitation	36
8.3	3 Adapt	tive trait regulation and differential trade-off	35
	8.2.9	Other stuff	35
	8.2.8	Particle aggregation	35

# **Symbols**

#### Symbols used in formulas, respective model parameters, and their descriptions

```
1/h
         syn nut synchrony n queue in nutrient quota limitation
\alpha
         alpha specific light adsorption by chloroplasts
\delta_{\theta}
         adap_theta adap_theta
\delta_R
         adap rub adap rub
\Delta t_{
m v}
         tau regV tau regV
a_{c}hl
         a chl attenuation coefficient due to Chl absorption
        a spm attenuation coefficient of SPM
a_spm
awater a water background attenuation coefficient
Ae<sub>a</sub>ll Ae all Activation energy
basal<sub>r</sub>esp<sub>z</sub>oo basal_resp_zoo basal respiration
const_N C_z oo const_NC_zoo zooplankton N:C ratio
const_{P}C_{z}oo\ const\_{P}C\_{z}oo\ zooplankton\ P:C\ ratio
detCinitial detC_initial Detritus Carbon
detNinitial detN_initial Detritus Nitrogen
detPinitial detP initial Detritus Phosphorus
detS<sub>i</sub>nitial detS_initial Detritus Silicon
dil
         dil dilution of all concentrations except dissolved inorganics
         nutN initial Dissolved Inorganic Nitrogen DIN
domCinitial domC_initial Dissolved Organic Carbon
domNinitial domN initial Dissolved Organic Nitrogen
domPinitial domP initial Dissolved Organic Phosphorus
exudphy exud_phy phytoplankton exudation per production
frac<sub>P</sub>AR frac PAR photosynthetically active fraction of light
gmax g_max maximum grazing rate
hydrol hydrolysis rate
k<sub>g</sub>razC k_grazC half saturation graing
mort<sub>z</sub>oo mort_zoo quadratic mortality
NutOrder NutOrder element order of recursive scheme. lower digit: synchrony element
phiagg phiagg quadratic aggregation rate
phyNinitial phyN_initial Phytplankton Nitrogen
phyPinitial phyP_initial Phytplankton Phosphorus
phyS<sub>i</sub>nitial phyS_initial Phytplankton Silicon
Phy<sub>C</sub> phyC_initial Phytplankton Carbon
Phy_{P}
         nutP initial Dissolved Inorganic Phosphorus DIP
        nutS_initial Dissolved Inorganic Silicon Si
Phy_{Si}
```

 $Q_{\rm P0}$ 

 $Q_{\rm Si0}$ 

```
rel<sub>c</sub>hloropl<sub>m</sub>in rel_chloropl_min chloroplast-C to phy-C ratio
remin remin pelagic remineralisation
         small lower limit for denominator in ratios; small_finite=sqrt(small)
small
T_ref
         T_ref reference temperature
vS<sub>d</sub>et vS det sinking velocity for detritus
vS<sub>p</sub>hy vS_phy sinking velocity for phytoplankton
yield<sub>z</sub>oo yield_zoo yield of herbivory
zooCinitial zooC initial Zooplankton Carbon
zstoich_PN zstoich_PN P-stoichiometry of active compounds(-> P costs)
σ
         sigma Q-dependency of Rubisco activity/chloroplast ratio
\theta_{\rm C}
         theta_LHC Chlorophylla-to-C ratio of LHC
         zeta_CN respiratory costs of N-synthesis/NO3-reduction
\zeta_{\rm CN}
A_{\rm N}^0
         AffN N-Affinity
A_{
m P}^0
         AffP P-Affinity
A_{\rm Si}^0
         AffSi Si-Affinity
f_{\theta}\theta_{C}
         frac_chl_ini Chl:C ratio
         frac_Rub_ini fraction of Rubisco
f_R
         P_max maximum potential photosynthetic rate
P_{\text{max}}
Q_{\rm N}^{\rm ref}
         QN_phy_max maximum N-quota
Q_{
m P}^{
m ref}
         QP phy max subsistence P-quota
Q_{\rm Si}^{\rm ref}
         QSi_phy_max subsistence Si-quota
Q_{\rm N0}
         QN_phy_0 subsistence N-quota
```

QP\_phy\_0 subsistence P-quota

QSi\_phy\_0 subsistence Si-quota

# MAECS: Model for Adaptive Ecosystems in Coastal Seas

### 1.1 General Overview

With regard to the conceptualization of trophic interactions, MAECS resembles the classical N-P-Z-D models (1). The emphasis is on the regulation of a number of physiological processes in the phytoplankton unit, which are resolved following a sophisticated optimization scheme. Energy & nutrient allocation scheme of the phytoplankton, as well as the optimization concept used in MAECS is hinted by the model described by Wirtz and Pahlow (2010). See the last section (2) (available only in the pdf form of the documentation) for a detailed description and model equations with some narration.

Todo (1) include a diagram here

**Todo** (2) find out how to refer to the other sections, e.g., auto-generated by doxygen and added as extra latex packages (maybe Carsten knows already?)

In order to re-generate this documentation, make sure the prerequisites (doxygen,latex, bibtex) installed in your system, then type:

make

inside:

\$FABMDIR/src/models/hzg/maecs/doc/

# **Todo List**

#### Type fabm hzg maecs

looking at the rhs calculations in maecs\_do, id\_Rub and id\_chl are set (correctly) as bulk variables (X\*phyC). however from the units, it looks as if they are registered (wrongly) as property variables (X)??

#### Subprogram fabm\_hzg\_maecs::initialize (self, configunit)

from the rhsv argument of the SET\_ODE's in maecs\_do, it looks as if id\_chl and id\_Rub are (correctly) handled as bulk variables (-phyC multiplied traits). however registered names, units and description of these variables looks as if they are (wrongly) handled as property variables?? So we should change the units, names and desc's?

#### Subprogram fabm\_hzg\_maecs::maecs\_do (self, \_ARGUMENTS\_DO\_)

- : min\_mass correction of phy% and phy%N at this stage requires specification of threshold values. What about back-calculating phy%reg%N from the smooth\_small corrected phy%Q%N?
- : calc\_internal\_states: I don't understand how heta and  $f_{ heta}$  are calculated
- : specific graz rate becomes pop. grazing rate. Do this at the rhs calculations
- : graz\_rate: no temperature modification: forgotten?
- : add the rhs equations
- : add the rhs equations

#### page MAECS: Model for Adaptive Ecosystems in Coastal Seas

(1) include a diagram here (2) find out how to refer to the other sections, e.g., auto-generated by doxygen and added as extra latex packages (maybe Carsten knows already?)

#### Subprogram maecs functions::calc internal states (maecs, phy, det, dom, zoo)

the theta-related calculations should obviously be related to Eq. 8.21 but I get lost. See the Q's therein

phy%frac%Rub=1-phy%frac%Rub : ?? what is this? from now on  $f_R$  is not what we think it is!!

# Subprogram maecs functions::calc sensitivities (maecs, sens, phy, env, nut)

- : a more intuitive name like calc potentials?
- : Q: why maecs instead of self?

#### Subprogram maecs\_functions::min\_mass (maecs, phy, method)

- : assign some meaningful names to case numbers?
- : mm method to be read from the nml?
- : Q: phy%reg%P either non existent or commented out for different cases. Why?
- : add equations

### Subprogram maecs\_functions::queuederiv (n, x)

: add equations

6 Todo List

Subprogram maecs\_functions::queuefunc (n, x, qfunc, qderiv)

: add equations

Subprogram maecs\_grazing::grazing\_losses (zoo, resC, Q\_prey, lossZNut, lossZDet, mswitch)

: add a description and details

# **Data Type Index**

# 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

fabm_hzg_maecs	10
fabm_hzg_maecs::maecs_do	14
maecs_functions	14
fabm_hzg_maecs::maecs_get_vertical_movement	18
maecs_grazing	18
maecs_primprod	19
maecs_types	21
maecs_types::stoich_pointer	21
type_base_model	
maecs_types::type_maecs_base_model	22
maecs_types::type_maecs_allocation_fractions	22
type_maecs_base_model	
fabm_hzg_maecs::type_hzg_maecs	21
maecs_types::type_maecs_basic_traits	
maecs_types::type_maecs_env	
maecs_types::type_maecs_nutindex	
maecs_types::type_maecs_om	
maecs_types::type_maecs_life	
maecs_types::type_maecs_phy	
manage to the activity to a second to the se	
maecs_types::type_maecs_zoo	
maecs_types::type_maecs_rhs	24
maecs_types::type_maecs_rhs	24
maecs_types::type_maecs_rhs	24

# **Data Type Index**

# 4.1 Data Types List

Here are the data types with brief descriptions:

fabm_hzg_maecs	
This is the module registered in FABM	10
fabm_hzg_maecs::maecs_do	14
maecs_functions	
Functions called by maecs_do, maecs_grazing and maecs_primprod	14
fabm_hzg_maecs::maecs_get_vertical_movement	18
maecs_grazing	
Grazing module	18
maecs_primprod	
Primary production module	19
maecs_types	
Data types used in fabm_hzg_maecs are defined here	21
maecs_types::stoich_pointer	21
fabm_hzg_maecs::type_hzg_maecs	
This is the model type FABM uses to create the mode	21
maecs_types::type_maecs_allocation_fractions	22
maecs_types::type_maecs_base_model	22
maecs_types::type_maecs_basic_traits	22
maecs_types::type_maecs_env	23
maecs_types::type_maecs_life	23
maecs_types::type_maecs_nutindex	23
maecs_types::type_maecs_om	23
maecs_types::type_maecs_phy	24
maecs_types::type_maecs_rhs	24
maecs_types::type_maecs_sensitivities	24
maecs_types::type_maecs_switch	24
maecs_types::type_maecs_traitdyn	25
maecs types::type maecs zoo	25

# File Index

# 5.1 File List

Here is a list of all documented files with brief descriptions:

maecs_functions.F90	26
maecs_grazing.F90	26
maecs_maecsdo_combined.F90	
A temporary file built by combining maecs.F90 and maecs_do.F90 for documentation purposes	27
maecs_primprod.F90	27
maecs_types.F90	
Maecs_types module	27
mainpage.doxygen	??

# **Data Type Documentation**

# 6.1 fabm\_hzg\_maecs Module Reference

This is the module registered in FABM.

### **Data Types**

- · interface maecs do
- · interface maecs\_get\_vertical\_movement
- type type\_hzg\_maecs

this is the model type FABM uses to create the mode

### **Private Member Functions**

• subroutine initialize (self, configurit)

initializes the model

subroutine get\_light\_extinction (self, \_ARGUMENTS\_GET\_EXTINCTION\_)

to calculate light extinction when kc changes with depth

· subroutine maecs\_init\_stoichvars (self)

a brief description to be added

• subroutine maecs do (self, ARGUMENTS DO )

This is the main routine where right-hand-sides are calculated.

• subroutine maecs\_get\_vertical\_movement (self, \_ARGUMENTS\_GET\_VERTICAL\_MOVEMENT\_)

handles vertical movement for depth-varying movement rates

### 6.1.1 Detailed Description

This is the module registered in FABM.

all the maecs\_types are made available to this module

**Todo** looking at the rhs calculations in maecs\_do, id\_Rub and id\_chl are set (correctly) as bulk variables (X\*phyC). however from the units, it looks as if they are registered (wrongly) as property variables (X)??

Definition at line 12 of file maecs\_maecsdo\_combined.F90.

# 6.1.2 Member Function/Subroutine Documentation

6.1.2.1 fabm\_hzg\_maecs::initialize ( class (type\_hzg\_maecs), intent(inout), target *self*, integer, intent(in) *configunit* )

[private]

### initializes the model

here the maecs namelists are read and assigned respectively in the model type (self), state & diagnostic variables are registered in FABM and dependencies are imported from FABM

# Model parameters, descriptions and corresponding symbols used in formulas:

#### **Parameters**

nutN_initial	DIN Dissolved Inorganic Nitrogen DIN
nutP_initial	Phy <sub>P</sub> Dissolved Inorganic Phosphorus DIP
nutS_initial	Phy <sub>Si</sub> Dissolved Inorganic Silicon Si
phyC_initial	Phy <sub>C</sub> Phytplankton Carbon
phyN_initial	phyN <sub>i</sub> nitial Phytplankton Nitrogen
phyP_initial	phyP <sub>i</sub> nitial Phytplankton Phosphorus
phyS_initial	phyS <sub>i</sub> nitial Phytplankton Silicon
zooC_initial	zooC <sub>i</sub> nitial Zooplankton Carbon
detC_initial	detC <sub>i</sub> nitial Detritus Carbon
detN_initial	detN <sub>i</sub> nitial Detritus Nitrogen
detP_initial	detP <sub>i</sub> nitial Detritus Phosphorus
detS_initial	detS <sub>i</sub> nitial Detritus Silicon
domC_initial	domCinitial Dissolved Organic Carbon
domN_initial	domN <sub>i</sub> nitial Dissolved Organic Nitrogen
domP_initial	domP <sub>i</sub> nitial Dissolved Organic Phosphorus
frac_Rub_ini	$f_R$ fraction of Rubisco {Rub , f_R{Phy}_{C}, trait x biomass}
frac_chl_ini	$f_{\theta}\theta_{C}$ Chl:C ratio {chl , f_{Phy}_{C}, trait x biomass}
P_max	$P_{ m max}$ maximum potential photosynthetic rate
alpha	lpha specific light adsorption by chloroplasts
sigma	σ Q-dependency of Rubisco activity/chloroplast ratio
theta_LHC	$ heta_{ m C}$ Chlorophylla-to-C ratio of LHC
rel_chloropl_min	rel <sub>c</sub> hloropl <sub>m</sub> in chloroplast-C to phy-C ratio
QN_phy_0	$Q_{ m N0}$ subsistence N-quota
QN_phy_max	$Q_{\rm N}^{\rm ref}$ maximum N-quota {V_NC_max , V_{max,N}^0 , maximum N uptake rate, 0.3 mol-N/(mol-C d)}
AffN	$A_{ m N}^0$ N-Affinity
zeta_CN	$\zeta_{ m CN}$ respiratory costs of N-synthesis/NO3-reduction
zstoich_PN	zstoich <sub>P</sub> N P-stoichiometry of active compounds(-> P costs)
exud_phy	exud <sub>p</sub> hy phytoplankton exudation per production
QP_phy_0	$Q_{ m P0}$ subsistence P-quota
QP_phy_max	$Q_{\rm P}^{\rm ref}$ subsistence P-quota {V_PC_max , V_{max,P}^0 , maximum P uptake rate, 0.03 mol-P/(mol-C d)}
AffP	$A_{\rm P}^0$ P-Affinity
QSi_phy_0	$Q_{ m Si0}$ subsistence Si-quota
QSi_phy_max	$Q_{\rm Si}^{\rm ref}$ subsistence Si-quota {V_SiC_max , V_{max,Si}^0 , maximum Si-uptake rate, 0.02 mol-Si/(mol-C d)}

AITSI AS; IS-ARTINITY         syn_nut       1/h synchrony n_queue in nutrient quota limitation         adap_rub       δ <sub>θ</sub> adap_rub         adap_theta       tau_regV         bi_agg       phi_agg quadratic aggregation rate         vS_phy       vSphy sinking velocity for phytoplankton         vS_det       vS_phy sinking velocity for detritus         hydrol       hydrol hydrolysis rate         remin       remin pelagic remineralisation         Ae_all       Activation energy         T_ref       T <sub>r</sub> cf reference temperature         NutOrder       NutOrder element order of recursive scheme. lower digit: synchrony element         const_NC_zoo       const <sub>N</sub> C <sub>z</sub> oo zooplankton N:C ratio         const_PC_zoo       const <sub>N</sub> C <sub>z</sub> oo zooplankton N:C ratio         g_max       max maximum grazing rate         k_grazC       k <sub>g</sub> razC half saturation graing         yield_zoo       yield_zoo         yield_zoo       yield of herbivory         basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       mort_zoo quadratic mortality         a_water       a_chl attenuation coefficient of SPM         a_chl       a_chl attenuation coefficient due to Chl absorption         frac_PAR       photosynthetically active	4((0)	40.00 400
$ \begin{array}{c} \textit{adap\_rub} & \delta_{\text{R}}  \textit{adap\_rub} \\ \textit{adap\_theta} & \delta_{\theta}  \textit{adap\_theta} \\ \textit{tau\_regV} & \Delta r_{\text{V}}  \textit{tau\_regV} \\ \textit{phi\_agg} & \text{phi\_agg}  \textit{quadratic}  \textit{aggregation}  \textit{rate} \\ \textit{vS\_phy} & \textit{vS\_phy}  \textit{sinking}  \textit{velocity}  \textit{for phytoplankton} \\ \textit{vS\_det} & \textit{vS\_det}  \textit{sinking}  \textit{velocity}  \textit{for detritus} \\ \textit{hydrol} & \textit{hydrol}  \textit{hydrol}  \textit{hydrolysis}  \textit{rate} \\ \textit{remin} & \textit{remin}  \textit{pelagic}  \textit{remineralisation} \\ \textit{Ae\_all} & \textit{Ae\_all}  \textit{Activation}  \textit{energy} \\ \textit{T\_ref} & \textit{T_ref}  \textit{reference}  \textit{temperature} \\ \textit{NutOrder} & \textit{NutOrder}  \textit{element}  \textit{order}  \textit{of}  \textit{recursive}  \textit{scheme.}  \textit{lower}  \textit{digit:}  \textit{synchrony}  \textit{element} \\ \textit{const\_NC\_zoo} & \textit{const_NC\_zoo}  \textit{zooplankton}  \textit{N:C}  \textit{ratio} \\ \textit{const\_PC\_zoo} & \textit{const_PC\_zoo}  \textit{zooplankton}  \textit{P:C}  \textit{ratio} \\ \textit{g\_max} & \textit{g_max}  \textit{maximum}  \textit{grazing}  \textit{rate} \\ \textit{k\_grazC} & \textit{k\_grazC}  \textit{half}  \textit{saturation}  \textit{graing} \\ \textit{yield\_zoo} & \textit{yield\_zoo}  \textit{yield\_zoo}  \textit{yield}  \textit{goo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{basal\_resp\_zoo}  \textit{dagaratic}  \textit{mort_ality} \\ \textit{a\_water} & \textit{a\_w}  \textit{a_w}  \textit{aten background}  \textit{attenuation}  \textit{coefficient}  \textit{d}  \textit{a}  \textit{chl}   \textit{achl}    \textit{atenuation}   \textit{coefficient}  \textit{due to Chl}                   $	AffSi	$A_{\mathrm{Si}}^{0}$ Si-Affinity
$ \begin{array}{c} adap\_theta \\ tau\_regV \\ \Delta I_V tau\_regV \\ phi\_agg \\ phi\_agg \\ vS_phy \\ sinking velocity for phytoplankton \\ vS\_det \\ vS_det \\ sinking velocity for detritus \\ hydrol \\ hydrol hydrol hydrol hydrolysis rate \\ remin \\ remin pelagic remineralisation \\ Ae\_all \\ Ae\_all Activation energy \\ T\_ref \\ T_ref reference temperature \\ NutOrder \\ NutOrder element order of recursive scheme. lower digit: synchrony element \\ const\_NC\_zoo \\ const_NC\_zoo \\ const_NC\_zoo \\ const_PC\_zoo \\ g\_max \\ g_max \\ maximum grazing rate \\ k\_grazC \\ k_grazC \\ half saturation graing \\ yield\_zoo \\ yield\_zoo \\ yield\_zoo \\ yield\_zoo \\ a\_water \\ a\_spm \\ a\_spm \\ a_spm attenuation coefficient due to ChI absorption \\ frac\_PAR \\ frac_PAR \\ photosynthetically active fraction of light \\ small \\ small lower limit for denominator in ratios; small\_finite=sqrt(small) \\ \hline \end{array}$		, , , , , , , , , , , , , , , , , , , ,
tau_regV		. –
phi_agg phiagg quadratic aggregation rate  vS_phy vS_phy sinking velocity for phytoplankton  vS_det vS_det sinking velocity for detritus  hydrol hydrol hydrolysis rate  remin remin pelagic remineralisation  Ae_all Ae_all Activation energy  T_ref T_ref reference temperature  NutOrder NutOrder element order of recursive scheme. lower digit: synchrony element  const_NC_zoo const_NC_zoo zooplankton N:C ratio  const_PC_zoo const_PC_zoo zooplankton P:C ratio  g_max g_max maximum grazing rate  k_grazC k_grazC half saturation graing  yield_zoo yield_zoo yield of herbivory  basal_resp_zoo basal_resp_zoo basal respiration  mort_zoo mort_zoo quadratic mortality  a_water a_water background attenuation coefficient  a_spm a_chl attenuation coefficient due to Chl absorption  frac_PAR frac_PAR photosynthetically active fraction of light  small lower limit for denominator in ratios; small_finite=sqrt(small)	· -	• • •
vS_phy       vS_phy sinking velocity for phytoplankton         vS_det       vS_det sinking velocity for detritus         hydrol       hydrol hydrolysis rate         remin       remin pelagic remineralisation         Ae_all       Ac_all Activation energy         T_ref       T_ref reference temperature         NutOrder       NutOrder element order of recursive scheme. lower digit: synchrony element         const_NC_zoo       constpC_zoo zooplankton N:C ratio         const_PC_zoo       constpC_zoo zooplankton P:C ratio         g_max       g_max maximum grazing rate         k_grazC       k_grazC half saturation graing         yield_zoo       yield_zoo yield of herbivory         basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       mort_zoo quadratic mortality         a_water       a_water background attenuation coefficient         a_spm       attenuation coefficient of SPM         a_chl       a_chl attenuation coefficient due to Chl absorption         frac_PAR       frac_PAR photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	tau_regV	$\Delta t_{ m v}$ tau_regV
vS_det       vS_det sinking velocity for detritus         hydrol       hydrol hydrolysis rate         remin       remin pelagic remineralisation         Ae_all       Acall Activation energy         T_ref       Tref reference temperature         NutOrder       NutOrder element order of recursive scheme. lower digit: synchrony element         const_NC_zoo       const_NC_zoo zooplankton N:C ratio         const_PC_zoo       const_PC_zoo zooplankton P:C ratio         g_max       maximum grazing rate         k_grazC       k_grazC half saturation graing         yield_zoo       yield_zoo yield of herbivory         basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       quadratic mortality         a_water       a_water background attenuation coefficient         a_spm       attenuation coefficient of SPM         a_chl       a_chl attenuation coefficient due to Chl absorption         frac_PAR       frac_PAR photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	phi_agg	phi <sub>a</sub> gg quadratic aggregation rate
hydrol       hydrol hydrolysis rate         remin       remin pelagic remineralisation         Ae_all       Activation energy         T_ref       Tref reference temperature         NutOrder       NutOrder element order of recursive scheme. lower digit: synchrony element         const_NC_zoo       const <sub>N</sub> C_zoo zooplankton N:C ratio         const_PC_zoo       const <sub>P</sub> C_zoo zooplankton P:C ratio         g_max       gaximum grazing rate         k_grazC       kg razC half saturation graing         yield_zoo       yield_zoo yield of herbivory         basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       mort_zoo quadratic mortality         a_water       a_water background attenuation coefficient         a_spm       attenuation coefficient of SPM         a_chl       ach attenuation coefficient due to Chl absorption         frac_PAR       photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	vS_phy	$vS_p hy$ sinking velocity for phytoplankton
remin remin pelagic remineralisation  Ae_all Ae_all Activation energy  T_ref Tref reference temperature  NutOrder NutOrder element order of recursive scheme. lower digit: synchrony element  const_NC_zoo const_NC_zoo zooplankton N:C ratio  const_PC_zoo const_PC_zoo zooplankton P:C ratio  g_max g_max maximum grazing rate  k_grazC k_grazC half saturation graing  yield_zoo yield_zoo yield of herbivory  basal_resp_zoo basal_resp_zoo basal respiration  mort_zoo mort_zoo quadratic mortality  a_water a_water background attenuation coefficient  a_spm a_spm attenuation coefficient of SPM  a_chl attenuation coefficient due to Chl absorption  frac_PAR frac_PAR photosynthetically active fraction of light  small lower limit for denominator in ratios; small_finite=sqrt(small)	vS_det	$vS_d$ et sinking velocity for detritus
Ae_all Activation energy  T_ref Tref reference temperature  NutOrder NutOrder element order of recursive scheme. lower digit: synchrony element  const_NC_zoo const_NC_zoo zooplankton N:C ratio  const_PC_zoo const_PC_zoo zooplankton P:C ratio  g_max g_max maximum grazing rate  k_grazC k_grazC half saturation graing  yield_zoo yield_zoo yield of herbivory  basal_resp_zoo basal_resp_zoo basal respiration  mort_zoo quadratic mortality  a_water a_water background attenuation coefficient  a_spm a_spm attenuation coefficient of SPM  a_chl attenuation coefficient due to Chl absorption  frac_PAR frac_PAR photosynthetically active fraction of light  small small lower limit for denominator in ratios; small_finite=sqrt(small)	hydrol	hydrol hydrolysis rate
$T\_ref \qquad T_ref \qquad T_re$	remin	remin pelagic remineralisation
NutOrder         NutOrder element order of recursive scheme. lower digit: synchrony element           const_NC_zoo         const_NC_zoo zooplankton N:C ratio           const_PC_zoo         const_PC_zoo zooplankton P:C ratio           g_max         g_max maximum grazing rate           k_grazC         k_grazC half saturation graing           yield_zoo         yield_zoo yield of herbivory           basal_resp_zoo         basal_resp_zoo basal respiration           mort_zoo         mort_zoo quadratic mortality           a_water         a_water background attenuation coefficient           a_spm         aspm attenuation coefficient of SPM           a_chl         achl attenuation coefficient due to Chl absorption           frac_PAR         frac_PAR photosynthetically active fraction of light           small         small lower limit for denominator in ratios; small_finite=sqrt(small)	Ae_all	Ae <sub>a</sub> ll Activation energy
$\begin{array}{c} \textit{const}\_\textit{NC}\_\textit{zoo} & const_{N}C_{z}oo \; zooplankton \; N:C \; ratio \\ \\ \textit{const}\_\textit{PC}\_\textit{zoo} & const_{P}C_{z}oo \; zooplankton \; P:C \; ratio \\ \\ \textit{g}\_\textit{max} & g_{m}ax \; maximum \; grazing \; rate \\ \\ \textit{k}\_\textit{grazC} & k_{g}razC \; half \; saturation \; graing \\ \\ \textit{yield}\_\textit{zoo} & yield_{z}oo \; yield \; of \; herbivory \\ \\ \textit{basal}\_\textit{resp}\_\textit{zoo} & basal_{r}esp_{z}oo \; basal \; respiration \\ \\ \textit{mort}\_\textit{zoo} & mort_{z}oo \; quadratic \; mortality \\ \\ \textit{a}\_\textit{water} & a_{w}ater \; background \; attenuation \; coefficient \\ \\ \textit{a}\_\textit{spm} & a_{s}pm \; attenuation \; coefficient \; of \; SPM \\ \\ \textit{a}\_\textit{chl} \; \; a_{c}hl \; attenuation \; coefficient \; due \; to \; Chl \; absorption \\ \\ \textit{frac}\_\textit{PAR} \; \; frac_{P}AR \; photosynthetically \; active \; fraction \; of \; light \\ \\ \textit{small} \; \; small \; \; lower \; limit \; for \; denominator \; in \; ratios; \; small\_finite = sqrt(small) \\ \\ \end{aligned}$	T_ref	T <sub>r</sub> ef reference temperature
$ \begin{array}{cccc} \textit{const}_P C_z \textit{oo} & \textit{const}_P C_z \textit{oo}  \textit{zooplankton}  P:C  \text{ratio} \\ & g_m \textit{ax} & g_m \textit{ax}  \text{maximum}  \text{grazing}  \text{rate} \\ & k_g \textit{raz} C & k_g \textit{raz} C  \text{half}  \text{saturation}  \text{graing} \\ & \textit{yield}_z \textit{oo} & \textit{yield}_z \textit{oo}  \textit{yield}  \textit{of}  \text{herbivory} \\ & \textit{basal}_r \textit{esp}_z \textit{oo}  \text{basal}_r \textit{esp}_z \textit{oo}  \text{basal}  \text{respiration} \\ & \textit{mort}_z \textit{oo}   \text{quadratic}  \text{mortality} \\ & a_w \textit{ater}   \text{background}  \text{attenuation}  \text{coefficient} \\ & a_s \textit{pm}   \text{attenuation}  \text{coefficient}  \text{of}  \text{SPM} \\ & a_c \textit{hl}   \text{attenuation}  \text{coefficient}  \text{due}  \text{to}  \text{Chl}  \text{absorption} \\ & \textit{frac}_P \textit{AR}   \text{photosynthetically}  \text{active}  \text{fraction}  \text{of}  \text{light} \\ & \textit{small}   \text{small}   \text{lower limit}  \text{for}  \text{denominator}  \text{in}  \text{ratios};  \text{small\_finite=sqrt(small)} \\ \end{aligned}$	NutOrder	NutOrder element order of recursive scheme. lower digit: synchrony element
$\begin{array}{c c} g\_max & g_max \ maximum \ grazing \ rate \\ \hline k\_grazC & k_grazC \ half \ saturation \ graing \\ \hline yield\_zoo & yield\_zoo \ yield\_zoo \ yield\_zoo \ yield\_zoo \ yield\_zoo \ basal\_resp\_zoo \ basal\_resp\_zoo \ basal\_resp\_zoo \ basal\_resp\_zoo \ mort\_zoo \ quadratic \ mortality \\ \hline a\_water & a_water \ background \ attenuation \ coefficient \\ \hline a\_spm & a_spm \ attenuation \ coefficient \ of \ SPM \\ \hline a\_chl & a_chl \ attenuation \ coefficient \ due \ to \ Chl \ absorption \\ \hline frac\_PAR & frac_PAR \ photosynthetically \ active \ fraction \ of \ light \\ \hline small \ lower \ limit \ for \ denominator \ in \ ratios; \ small\_finite=sqrt(small) \\ \hline \end{array}$	const_NC_zoo	$const_N C_z$ oo zooplankton N:C ratio
k_grazC       k_grazC half saturation graing         yield_zoo       yield_zoo yield of herbivory         basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       mort_zoo quadratic mortality         a_water       a_water background attenuation coefficient         a_spm       aspm attenuation coefficient of SPM         a_chl       achl attenuation coefficient due to Chl absorption         frac_PAR       frac_PAR photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	const_PC_zoo	const <sub>P</sub> C <sub>z</sub> oo zooplankton P:C ratio
yield_zoo     yieldzoo yield of herbivory       basal_resp_zoo     basal_respzoo basal respiration       mort_zoo     mortzoo quadratic mortality       a_water     a_water background attenuation coefficient       a_spm     aspm attenuation coefficient of SPM       a_chl     achl attenuation coefficient due to Chl absorption       frac_PAR     frac_PAR photosynthetically active fraction of light       small     small lower limit for denominator in ratios; small_finite=sqrt(small)	g_max	g <sub>m</sub> ax maximum grazing rate
basal_resp_zoo       basal_resp_zoo basal respiration         mort_zoo       mort_zoo quadratic mortality         a_water       a_water background attenuation coefficient         a_spm       a_spm attenuation coefficient of SPM         a_chl       a_chl attenuation coefficient due to Chl absorption         frac_PAR       frac_PAR photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	k_grazC	k <sub>g</sub> razC half saturation graing
	yield_zoo	yield <sub>z</sub> oo yield of herbivory
a_water       a_water background attenuation coefficient         a_spm       a_spm attenuation coefficient of SPM         a_chl       a_chl attenuation coefficient due to Chl absorption         frac_PAR       frac_PAR photosynthetically active fraction of light         small       small lower limit for denominator in ratios; small_finite=sqrt(small)	basal_resp_zoo	basal <sub>r</sub> esp <sub>z</sub> oo basal respiration
a_spm aspm attenuation coefficient of SPM  a_chl attenuation coefficient due to Chl absorption  frac_PAR frac_PAR photosynthetically active fraction of light  small lower limit for denominator in ratios; small_finite=sqrt(small)	mort_zoo	mort <sub>z</sub> oo quadratic mortality
a_chl achl attenuation coefficient due to Chl absorption  frac_PAR frac_PAR photosynthetically active fraction of light  small lower limit for denominator in ratios; small_finite=sqrt(small)	a_water	awater background attenuation coefficient
frac_PAR         frac_PAR photosynthetically active fraction of light           small         small lower limit for denominator in ratios; small_finite=sqrt(small)	a_spm	a <sub>s</sub> pm attenuation coefficient of SPM
small   small lower limit for denominator in ratios; small_finite=sqrt(small)	a_chl	a <sub>c</sub> hl attenuation coefficient due to Chl absorption
_ , , , ,	frac_PAR	frac <sub>P</sub> AR photosynthetically active fraction of light
dil dil dilution of all concentrations except dissolved inorganics	small	small lower limit for denominator in ratios; small_finite=sqrt(small)
	dil	dil dilution of all concentrations except dissolved inorganics

**Todo** from the rhsv argument of the SET\_ODE's in maecs\_do, it looks as if id\_chl and id\_Rub are (correctly) handled as bulk variables (-phyC multiplied traits). however registered names, units and description of these variables looks as if they are (wrongly) handled as property variables?? So we should change the units, names and desc's?

Definition at line 144 of file maecs maecsdo combined.F90.

References maecs\_init\_stoichvars().

to calculate light extinction when kc changes with depth

```
extinction coef= a_{\text{water}} + a_{\text{spm}} * (p + d + z)
```

Definition at line 574 of file maecs\_maecsdo\_combined.F90.

```
6.1.2.3 subroutine fabm_hzg_maecs::maecs_init_stoichvars ( class(type_hzg_maecs), intent(inout) self ) [private]
```

a brief description to be added

some details to be added

Definition at line 606 of file maecs\_maecsdo\_combined.F90.

Referenced by initialize().

6.1.2.4 fabm\_hzg\_maecs::maecs\_do ( class (type\_maecs\_base\_model), intent(in) self, \_ARGUMENTS\_DO\_ )

[private]

This is the main routine where right-hand-sides are calculated.

NOTE: Although this subroutine looks as if it's not a part of any module, it is temporarily included in the fabm\_hzg\_maecs module (inside maecs.F90) when compiling the documentation, such that the subroutine is documented under the 'Data Type Documentation' chapter, where the in-body docs are listed

#### **Phytoplankton Equations**

We distinguish between mass state variables (in units of carbon, nitrogen, & phosphorus) and property state variables. For a textual narration and equations, see: Section 8.1

Current 'traits' are:

- nitrogen allocated to rubisco (frac\_Rub)
- · Chla content of chloroplasts (theta)

### General code structure:

- 1. Calculation of quotas, internal states, potential rates
- 2. Calculation of fluxes, mass exchange rates & rates of change of traits variables
- 3. Assign mass exchange rates ('rhs(j,i)')
- 4. Assign rates of change of 'traits' property variables

#### **Detailed Descriptions:**

- 1. Calculation of quotas, internal states, potential rates
  - call min\_mass with method=2, store phy%C and %N in phy%reg
  - call calc\_internal\_states: retrieve phy%Q%X, phy%theta, phy%frac%X
  - if PhotoacclimOn=.false., calculate:
    - phy%chl=phy%C \* self%frac\_chl\_ini
    - phy%frac%theta = self%frac chl ini \* self%itheta max
    - phy%theta= self%frac chl ini / (self%frac Rub ini \* phy%relQ%N\*\*self%sigma)
  - call calc\_sensitivities: retrieve potential rates:  $f_T$ , sens%upt\_pot%C (=LH), sens%upt\_pot%X (=  $V_X$ ), sens%P max

**Todo**: min\_mass correction of phy% and phy%N at this stage requires specification of threshold values. What about back-calculating phy%reg%N from the smooth\_small corrected phy%Q%N?

- : calc\_internal\_states: I don't understand how  $\theta$  and  $f_{\theta}$  are calculated
- 2. Calculation of fluxes, mass exchange rates & rates of change of traits variables & Specify rates of change of traits variables
  - call maecs\_primprod::photosynthesis(): this is where everything happens!
  - if GrazingOn:
    - graz\_rate=rate retrieved from call maecs\_grazing::grazing()
    - lossZ%X=lossZNut%X, floppZ%X=lossZDet%X retrieved from call maecs\_grazing::grazing\_-losses()
    - calculate graz\_rate retr= graz\_rate \* zoo%C and zoo\_mort
  - calc. aggreg\_rate = phi\_agg \*  $(1 e^{-0.02*\text{dom}\%\text{C}}) * phy\%N*det\%N$ 
    - future work: aggreg\_rate=f(size), (see section 8.2.8)
  - calc. degradT=self%hydrol \*  $f_T$  and reminT=self%remin \*  $f_T$

**Todo**: specific graz\_rate becomes pop. grazing rate. Do this at the rhs calculations: graz\_rate: no temperature modification: forgotten?

3. Assign mass exchange rates ('rhs(j,i)')

• phyC= uptake - dil - exud - aggreg rate - graz rate

Todo : add the rhs equations

4. Assign rates of change of 'traits' property variables

· if PhotoacclimOn: rhsvchl

· if RubiscoOn: rhsvRub

Todo: add the rhs equations

Definition at line 699 of file maecs\_maecsdo\_combined.F90.

References maecs\_functions::calc\_internal\_states(), maecs\_functions::calc\_sensitivities(), maecs\_grazing::grazing(), maecs\_grazing::grazing\_losses(), maecs\_functions::min\_mass(), and maecs\_primprod::photosynthesis().

6.1.2.5 subroutine fabm\_hzg\_maecs::maecs\_get\_vertical\_movement ( class(type\_maecs\_base\_model), intent(in) self, \_ARGUMENTS\_GET\_VERTICAL\_MOVEMENT\_ ) [private]

handles vertical movement for depth-varying movement rates

phyto sinking rate depends on the nutritional state, so for each node:

phy%relQ obtained by calling calc\_internal\_states(self,phy,det,dom,zoo)

then phyQstat = phy%relQ%N \* phy%relQ%P

finally, vsink = maecs\_functions::sinking(self%vS\_phy, phyQstat, vsink)

Definition at line 1121 of file maecs maecsdo combined.F90.

 $\label{lem:lem:mass} References \quad maecs\_functions::calc\_internal\_states(), \quad maecs\_functions::min\_mass(), \quad and \quad maecs\_functions::sinking().$ 

The documentation for this module was generated from the following file:

• maecs\_maecsdo\_combined.F90

# 6.2 fabm\_hzg\_maecs::maecs\_do Interface Reference

### 6.2.1 Detailed Description

Definition at line 58 of file maecs\_maecsdo\_combined.F90.

The documentation for this interface was generated from the following file:

maecs\_maecsdo\_combined.F90

# 6.3 maecs functions Module Reference

functions called by maecs\_do, maecs\_grazing and maecs\_primprod

# **Public Member Functions**

- subroutine, public calc\_internal\_states (maecs, phy, det, dom, zoo)
  - calculate the internal states
- subroutine, public calc\_sensitivities (maecs, sens, phy, env, nut)
  - calculate sensitivities
- pure real(rk) function, public uptflex (Aff0, Vmax0, Nut, fAv)
  - calc's pot nut upt as f(external conc, allocations)
- pure real(rk) function foptupt (Aff0, Vmax0, Nut)
  - opt. partitioning between surf upt sites and intern. enzymes for nut assim.
- subroutine, public queuefunc (n, x, qfunc, qderiv)
  - the queue function
- subroutine queuefunc1 (n, x, qfunc, qderiv)
  - numerical approximation of the queue function
- real(rk) function, public queuederiv (n, x)
  - derivative of the queue function ??
- subroutine, public sinking (vS, phys\_status, sinkvel)
  - calculation of the sinking rate
- subroutine, public min\_mass (maecs, phy, method)
  - minimum mass
- pure real(rk) function, public smooth\_small (x, eps)
  - continous smoothing function by kw Apr 2012

#### 6.3.1 Detailed Description

functions called by maecs\_do, maecs\_grazing and maecs\_primprod

Definition at line 8 of file maecs\_functions.F90.

# 6.3.2 Member Function/Subroutine Documentation

6.3.2.1 maecs\_functions::calc\_internal\_states ( type (type\_maecs\_base\_model), intent(in) *maecs*, type (type\_maecs\_phy), intent(inout) *phy*, type (type\_maecs\_om), intent(inout) *det*, type (type\_maecs\_om), intent(inout) *dom*, type (type\_maecs\_zoo), intent(inout) *zoo* )

calculate the internal states

Todo the theta-related calculations should obviously be related to Eq. 8.21 but I get lost. See the Q's therein

- 1. Calculate elemental absolute and relative quotas (Q and relQ):
  - phy%Q%X = phy%X / phy%C where x=N,P,Si
  - phy%relQ%X= (phy%Q%X maecs%qN\_phy\_0) / maecs%iK\_QN where x=N,P,Si
- 2. Calculate Rubisco fraction (convert from the bulk variable)
  - $f_R = \text{phy}\%\text{Rub}/phy_C$
  - Todo phy%frac%Rub=1-phy%frac%Rub: ?? what is this? from now on  $f_R$  is not what we think it is!!
- 3. Calculate  $\theta$  and  $f_{\theta}$  See also: 8.2.4
  - phy%rel<sub>c</sub>hloropl =  $f_R * q_N^{\sigma}$

- Q: phy%rel\_chloropl =
- phy%theta =  $phy_{chl}/phy_C/phy%rel_chloropl$ 
  - Q: does not seem to be equal to eq:ftheta} unless  $phy_{chl}/phy_C = f_{\theta}/\theta_C$
  - Q: what is actually phy%chl? the bulk or the trait variable? i assumed it is the bulk
- phy%frac%theta =  $phy_{chl}/phy_C*$  maecs%itheta<sub>m</sub>ax
  - Q: does not seem to be related to anything ??
- $f_V = \text{phy\%frac\%TotFree} f_\theta f_R$ , where phy%frac%TotFree=1.0
- 4. Calculate zooplankton states:
  - $zoo_{QX} = maecs\%const_NC_zoo, zoo_X = zoo_C * zoo_{QN}, X = N, P$
  - $zoo_{yield} = maecs\%yield_zoo, zoo_{flopp} = 1 maecs\%yield_zoo$

Definition at line 27 of file maecs functions.F90.

References smooth small().

Referenced by fabm\_hzg\_maecs::maecs\_do(), and fabm\_hzg\_maecs::maecs\_get\_vertical\_movement().

6.3.2.2 subroutine, public maecs\_functions::calc\_sensitivities ( type (type\_maecs\_base\_model), intent(in) maecs, type (type\_maecs\_sensitivities), intent(out) sens, type (type\_maecs\_phy), intent(in) phy, type (type\_maecs\_env), intent(in) env, type (type\_maecs\_om), intent(in) nut )

calculate sensitivities

Details:

- sens%f\_T see eq. 8.13
- sens%P max see eq. 8.20
- sens%upt\_pot%C (=LH) see eq. 8.11
- sens%upt\_pot%X, ( =  $V_X$ ), X=N,P,Si calculated by uptflex() according to eq. 8.26

Todo: a more intuitive name like calc\_potentials?

: Q: why maecs instead of self?

Definition at line 158 of file maecs\_functions.F90.

References foptupt(), smooth\_small(), and uptflex().

Referenced by fabm hzg maecs::maecs do().

6.3.2.3 pure real(rk) function, public maecs\_functions::uptflex ( real(rk), intent(in) Aff0, real(rk), intent(in) Vmax0, real(rk), intent(in) Nut, real(rk), intent(in) fAv )

calc's pot nut upt as f(external conc, allocations)

uptake regulation: sites vs. processing

see eq. 8.23 - 8.29

- sensupt\_potX =  $(A_X * DIX * V_{max,X})/(A_X * DIX + V_{max,X}))^{-1}$
- $A_X = f_{A,X} * A_X^0$ , where  $f_{A,X}$  =fOptUpt()
- $V_{max} = (1 f_{A,X}) * V_{max}^{0} * f_{T}$

Definition at line 224 of file maecs\_functions.F90.

Referenced by calc sensitivities().

6.3.2.4 pure real(rk) function maecs\_functions::foptupt ( real(rk), intent(in) Aff0, real(rk), intent(in) Vmax0, real(rk), intent(in) Nut )

opt. partitioning between surf upt sites and intern. enzymes for nut assim.

calculates  $f_{A,X}$  see eq. 8.29.

Definition at line 241 of file maecs functions.F90.

Referenced by calc\_sensitivities().

6.3.2.5 subroutine, public maecs\_functions::queuefunc ( real(rk), intent(in) n, real(rk), intent(in) x, real(rk), intent(out) qfunc, real(rk), intent(out) qderiv )

the queue function

provides both the queuing function and it's derivative with the parameter n->inf :liebig and n $\sim$ 1:product see: Section 8.2.3

Todo: add equations

Definition at line 256 of file maecs\_functions.F90.

Referenced by maecs\_primprod::photosynthesis().

6.3.2.6 subroutine maecs\_functions::queuefunc1 ( real(rk), intent(in) n, real(rk), intent(in) x, real(rk), intent(out) qderiv )

numerical approximation of the queue function

n->inf :liebig n~1:product

Here is an example of adding a snip of code:

```
\begin{array}{lll} nn &=& n+1. \\ hh &=& 1./nn \\ x0 &=& (\log (\exp (nn)-1))*hh \\ en &=& \exp (-nn*(x/(1+hh*x) - x0)) \\ qfunc &=& 1. - hh*log(1.+ en) \\ qderiv &=& 1. / ( (1. + hh * x)**2 * (1.+1./en)) \end{array}
```

Definition at line 279 of file maecs\_functions.F90.

6.3.2.7 real(rk) function, public maecs\_functions::queuederiv ( real(rk), intent(in) n, real(rk), intent(in) x )

derivative of the queue function ??

Returns

queuederiv

Todo: add equations

Definition at line 302 of file maecs\_functions.F90.

6.3.2.8 subroutine, public maecs\_functions::sinking ( real(rk), intent(in) vS, real(rk), intent(in) phys\_status, real(rk), intent(out) sinkvel )

calculation of the sinking rate

- $sinkvel = -vS * e^{-4*phys\_status}$ 
  - phys\_status calculated in fabm\_hzg\_maecs::maecs\_get\_vertical\_movement()
  - Future work: sinkvel=f(size) (see section 8.2.7)

Definition at line 319 of file maecs\_functions.F90.

Referenced by fabm hzg maecs::maecs get vertical movement().

6.3.2.9 subroutine, public maecs\_functions::min\_mass ( type (type\_maecs\_base\_model), intent(in) *maecs*, type (type\_maecs\_phy), intent(inout) *phy*, integer, intent(in), optional *method* )

minimum mass

pushes the phyC,N and P to some lower boundary according to 4 different methods (controlled by the mm\_method parameter): phy%N and phy%C are stored in phy%reg%N and phy%reg%C, respectively

- 1. if phy%N  $\leq$ = 1e-7; phy%N=1e-7, phy%C=phy%N/QN(aver), phy%P=phy%C\*QP(aver)
- 2. ..
- 3. ..
- 4. ..

Todo: assign some meaningful names to case numbers?

: mm method to be read from the nml?

: Q: phy%reg%P either non existent or commented out for different cases. Why?

: add equations

Definition at line 389 of file maecs functions.F90.

References smooth\_small().

Referenced by fabm hzg maecs::maecs do(), and fabm hzg maecs::maecs get vertical movement().

6.3.2.10 pure real(rk) function, public maecs\_functions::smooth\_small ( real(rk), intent(in) x, real(rk), intent(in) eps )

continous smoothing function by kw Apr 2012

smoothly converges x to eps/2 for x<eps

$$x = eps + (x - eps) * e^{x/eps} / (1 + e^{x/eps})$$

Definition at line 496 of file maecs\_functions.F90.

Referenced by calc\_internal\_states(), calc\_sensitivities(), min\_mass(), and maecs\_primprod::photosynthesis().

The documentation for this module was generated from the following file:

• maecs\_functions.F90

# 6.4 fabm\_hzg\_maecs::maecs\_get\_vertical\_movement Interface Reference

#### 6.4.1 Detailed Description

Definition at line 45 of file maecs\_maecsdo\_combined.F90.

The documentation for this interface was generated from the following file:

• maecs maecsdo combined.F90

# 6.5 maecs grazing Module Reference

Grazing module.

#### **Public Member Functions**

• subroutine, public grazing (Imax, HalfSat, preyconc, rate)

calculates grazing rate

• subroutine, public grazing losses (zoo, resC, Q prey, lossZNut, lossZDet, mswitch)

loss rates of grazers to inorganic and organic particulate

#### 6.5.1 Detailed Description

Grazing module.

Definition at line 7 of file maecs\_grazing.F90.

#### 6.5.2 Member Function/Subroutine Documentation

6.5.2.1 subroutine, public maecs\_grazing::grazing ( real(rk), intent(in) *lmax*, real(rk), intent(in) *HalfSat*, real(rk), intent(in) *preyconc*, real(rk), intent(out) *rate* )

calculates grazing rate

rate= 
$$I_{max} * F^2/(K^2 + F^2)$$

Definition at line 20 of file maecs\_grazing.F90.

Referenced by fabm\_hzg\_maecs::maecs\_do().

6.5.2.2 subroutine, public maecs\_grazing::grazing\_losses ( type (type\_maecs\_zoo), intent(in) zoo, real(rk), intent(in) resC, type (type\_maecs\_om), intent(in) Q\_prey, type (type\_maecs\_om), intent(out) lossZNut, type (type\_maecs\_om), intent(out) lossZDet, type (type\_maecs\_switch), intent(in) mswitch)

loss rates of grazers to inorganic and organic particulate

assumes a constant C:N:P unit feeding on variable C:N:P food

Todo: add a description and details

Definition at line 37 of file maecs grazing.F90.

Referenced by fabm\_hzg\_maecs::maecs\_do().

The documentation for this module was generated from the following file:

• maecs\_grazing.F90

# 6.6 maecs\_primprod Module Reference

Primary production module.

### **Public Member Functions**

• subroutine, public photosynthesis (self, sens, phy, uptake, exud, acc)

calculates grazing rate

#### 6.6.1 Detailed Description

Primary production module.

Definition at line 7 of file maecs primprod.F90.

#### 6.6.2 Member Function/Subroutine Documentation

6.6.2.1 maecs\_primprod::photosynthesis ( type (type\_maecs\_base\_model), intent(in) self, type (type\_maecs\_sensitivities), intent(in), target sens, type (type\_maecs\_phy), intent(inout) phy, type (type\_maecs\_om), intent(out), target uptake, type (type\_maecs\_om), intent(out) exud, type (type\_maecs\_traitdyn), intent(out), target acc )

calculates grazing rate

This is the subroutine, where the optimal regulation of phytoplankton traits are described, which is central to the physiological-MAECS

- 1. Prepare loop over structure elements by assigning a poinzer structure
  - · Here, every possible nutrient is asked explicitely; thus first Si then P
  - This is an example of adding a whole code source:

```
! nitrogen
       i = self%nutind%iN
elem(i)%relQ = smooth_small(phy%relQ%N,eps)
elem(i)%Q = smooth_small(phy%Q%N,eps)
elem(i)%upt pot => sens%upt pot%N
elem(i)%upt_act => upt_act%N
elem(i)%upt => uptake%N
= self%zeta_CN
! phosphorus
if (self%PhosphorusOn) then
       i = self%nutind%iP
elem(i)%relQ = smooth_small(phy%relQ%P,eps)
elem(i)%Q = smooth_small(phy%Q%P,eps)
elem(i)%upt_pot => sens%upt_pot%P
elem(i)%upt_act => upt_act%P
elem(i)%upt => uptake%P
elem(i)%iKQ = self%iK_QP
elem(i)%iKQ
                       = self%iK_QP
elem(i)%aV
                        => acc%aV%P
zeta_x(i)
                        = self%zeta_CN * ((1.-f_lip)*q_nolip + f_lip*q_lip)
end if
! silicon
if (self%SiliconOn) then
      i = self%nutind%iSi
elem(i)%relQ = smooth_small(phy%relQ%Si,eps)
elem(i)%Q = smooth_small(phy%Q%Si,eps)
elem(i)%upt_pot => sens%upt_pot%Si
elem(i)%upt_act => upt_act%Si
elem(i)%upt => uptack%Si
elem(1)%upu__ => uptaxesu_
elem(1)%upt => uptaxesu_
= self%iK_QSi
elem(i)%aV
                       => acc%aV%Si
= 0.0_rk
zeta_x(i)
```

Definition at line 20 of file maecs\_primprod.F90.

References maecs\_functions::queuefunc(), and maecs\_functions::smooth\_small().

Referenced by fabm\_hzg\_maecs::maecs\_do().

The documentation for this module was generated from the following file:

maecs\_primprod.F90

# 6.7 maecs\_types Module Reference

Data types used in fabm\_hzg\_maecs are defined here.

## **Data Types**

- · type stoich\_pointer
- type type\_maecs\_allocation\_fractions
- type type\_maecs\_base\_model
- type type\_maecs\_basic\_traits
- · type type\_maecs\_env
- type type\_maecs\_life
- type type\_maecs\_nutindex
- type type\_maecs\_om
- type type\_maecs\_phy
- type type\_maecs\_rhs
- type type\_maecs\_sensitivities
- type type\_maecs\_switch
- type type\_maecs\_traitdyn
- · type type maecs zoo

### 6.7.1 Detailed Description

Data types used in fabm\_hzg\_maecs are defined here.

todo: we should consider including parameter tables for some maecs types. Parser could do it just like in the initialize subroutine.

Definition at line 14 of file maecs\_types.F90.

The documentation for this module was generated from the following file:

· maecs\_types.F90

# 6.8 maecs\_types::stoich\_pointer Type Reference

## 6.8.1 Detailed Description

Definition at line 121 of file maecs\_types.F90.

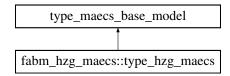
The documentation for this type was generated from the following file:

· maecs types.F90

# 6.9 fabm\_hzg\_maecs::type\_hzg\_maecs Type Reference

this is the model type FABM uses to create the mode

Inheritance diagram for fabm\_hzg\_maecs::type\_hzg\_maecs:



### 6.9.1 Detailed Description

this is the model type FABM uses to create the mode

the parent type (type\_maecs\_base\_model) was defined in maecs\_types module

Definition at line 30 of file maecs\_maecsdo\_combined.F90.

The documentation for this type was generated from the following file:

· maecs maecsdo combined.F90

# 6.10 maecs\_types::type\_maecs\_allocation\_fractions Type Reference

# 6.10.1 Detailed Description

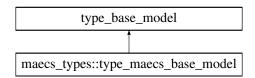
Definition at line 71 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs\_types.F90

# 6.11 maecs\_types::type\_maecs\_base\_model Type Reference

Inheritance diagram for maecs\_types::type\_maecs\_base\_model:



### 6.11.1 Detailed Description

Definition at line 27 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs\_types.F90

# 6.12 maecs\_types::type\_maecs\_basic\_traits Type Reference

### 6.12.1 Detailed Description

Definition at line 66 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs\_types.F90

# 6.13 maecs\_types::type\_maecs\_env Type Reference

### 6.13.1 Detailed Description

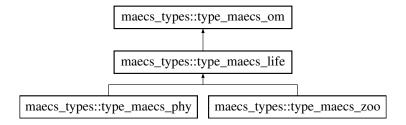
Definition at line 47 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs types.F90

# 6.14 maecs\_types::type\_maecs\_life Type Reference

Inheritance diagram for maecs\_types::type\_maecs\_life:



# 6.14.1 Detailed Description

Definition at line 78 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# 6.15 maecs\_types::type\_maecs\_nutindex Type Reference

# 6.15.1 Detailed Description

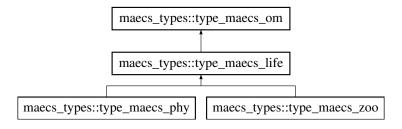
Definition at line 22 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# 6.16 maecs\_types::type\_maecs\_om Type Reference

Inheritance diagram for maecs\_types::type\_maecs\_om:



# 6.16.1 Detailed Description

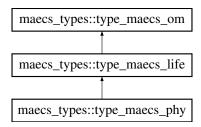
Definition at line 62 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

maecs\_types.F90

# 6.17 maecs\_types::type\_maecs\_phy Type Reference

Inheritance diagram for maecs\_types::type\_maecs\_phy:



# 6.17.1 Detailed Description

Definition at line 83 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs\_types.F90

# 6.18 maecs\_types::type\_maecs\_rhs Type Reference

### 6.18.1 Detailed Description

Definition at line 50 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# 6.19 maecs\_types::type\_maecs\_sensitivities Type Reference

### 6.19.1 Detailed Description

Definition at line 112 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# 6.20 maecs\_types::type\_maecs\_switch Type Reference

# 6.20.1 Detailed Description

Definition at line 57 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

· maecs types.F90

# 6.21 maecs\_types::type\_maecs\_traitdyn Type Reference

# 6.21.1 Detailed Description

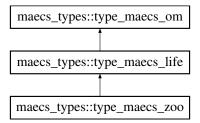
Definition at line 100 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# 6.22 maecs\_types::type\_maecs\_zoo Type Reference

Inheritance diagram for maecs\_types::type\_maecs\_zoo:



# 6.22.1 Detailed Description

Definition at line 94 of file maecs\_types.F90.

The documentation for this type was generated from the following file:

• maecs\_types.F90

# **File Documentation**

# 7.1 maecs\_functions.F90 File Reference

```
#include "fabm_driver.h"
```

# **Data Types**

• module maecs\_functions

functions called by maecs\_do, maecs\_grazing and maecs\_primprod

# 7.1.1 Detailed Description

Author

Richard Hofmeister, Markus Schartau, Kai Wirtz, Onur Kerimoglu Definition in file maecs\_functions.F90.

# 7.2 maecs\_grazing.F90 File Reference

```
#include "fabm_driver.h"
```

# **Data Types**

• module maecs\_grazing

Grazing module.

# 7.2.1 Detailed Description

Author

Richard Hofmeister, Markus Schartau, Kai Wirtz

Definition in file maecs\_grazing.F90.

# 7.3 maecs\_maecsdo\_combined.F90 File Reference

A temporary file built by combining maecs.F90 and maecs\_do.F90 for documentation purposes.

```
#include "fabm_driver.h"
```

# **Data Types**

• module fabm\_hzg\_maecs

This is the module registered in FABM.

type fabm\_hzg\_maecs::type\_hzg\_maecs

this is the model type FABM uses to create the mode

- interface fabm\_hzg\_maecs::maecs\_get\_vertical\_movement
- interface fabm\_hzg\_maecs::maecs\_do

# 7.3.1 Detailed Description

A temporary file built by combining maecs.F90 and maecs\_do.F90 for documentation purposes.

Definition in file maecs\_maecsdo\_combined.F90.

# 7.4 maecs\_primprod.F90 File Reference

```
#include "fabm_driver.h"
```

### **Data Types**

· module maecs\_primprod

Primary production module.

### 7.4.1 Detailed Description

**Author** 

Richard Hofmeister, Markus Schartau, Kai Wirtz, Onur Kerimoglu

Definition in file maecs\_primprod.F90.

# 7.5 maecs\_types.F90 File Reference

```
maecs_types module
```

```
#include "fabm_driver.h"
```

28 File Documentation

# **Data Types**

• module maecs\_types

Data types used in fabm\_hzg\_maecs are defined here.

- type maecs\_types::type\_maecs\_nutindex
- type maecs\_types::type\_maecs\_base\_model
- type maecs\_types::type\_maecs\_env
- type maecs\_types::type\_maecs\_rhs
- type maecs\_types::type\_maecs\_switch
- type maecs\_types::type\_maecs\_om
- type maecs\_types::type\_maecs\_basic\_traits
- type maecs\_types::type\_maecs\_allocation\_fractions
- type maecs\_types::type\_maecs\_life
- type maecs\_types::type\_maecs\_phy
- type maecs\_types::type\_maecs\_zoo
- type maecs\_types::type\_maecs\_traitdyn
- type maecs\_types::type\_maecs\_sensitivities
- type maecs\_types::stoich\_pointer

# 7.5.1 Detailed Description

maecs\_types module

Author

Richard Hofmeister, Kai Wirtz

Definition in file maecs\_types.F90.

# **Textual Model Description**

# 8.1 Model structure

MAECS resolves major functional groups and their dynamics not unlike simple state-of-the-art ecosystem models. All energy and material fluxes in the ecosystem derive from primary production of phytoplankton, here expressed in terms of biomass carbon (C) concentration. Phytoplankton experiences various local and trait dependent loss rates, from sinking, respiration, exudation, to grazing. MAECS versions differ in the degree of resolution in ecological processes; a full account of grazing interactions in the plankton is only addressed by versions that includes size as a major trait. Grazers convert only a fraction of captured phytoplankton to their own biomass; in size-based variants of MAECS we have implemented different formulations for whether this fraction immediately contributes to the biomass of adult grazers or their egg stage, or how many grazer groups are simulated (see below).

Physiological regulation in unicellular autotrophs makes the very kernel of the MAECS version documented here. The intracellular nutrient quotas, in this model version resolved for nitrogen (N), phosphorus (P), and silicon (Si), change over time when uptake does not match demand due to biomass build-up. Differential uptake regulation then leads to highly variable stoichiometries, that not only reflect ambient nutrient and light concentration, but also generalized optimality criteria.

For describing the living compartment of plankton ecosystems MAECS employs much more trait variables (e.g., allocation coefficients) compared to bulk variables (e.g., phytoplankton or zooplankton biomass). The adaptive trait dynamics infers the need of calculating (sometimes long) derivative terms, which also challenges this documentation; however, the gradient-derived terms include very few additional process parameters, so that the number of tunable parameters in relation to simulated and testable dynamics is significantly reduced compared to models that share a similar resolution in plankton physiology or ecology. Most importantly, MAECS seeks to account for biophysical and evolutionary principles as much as possible; resulting in expressions replacing heuristic functions such as Michaelis-Menten approximations of nutrient uptake, Droop representation of cell growth, or Liebig's rule of minimum. Biophysical origins of model formulations further reduces the number of tunable parameters, in particular in the ecological part. Prominent counter-examples, i.e. yet uncertain model formulations or parameters, comprise aggregation dynamics or variations in metabolic interdependency.

### 8.1.1 Mass equations

Basic mass equations common to the two MAECS variants (size and physiology). All coefficients and their meanings are listed in Table ??.

Net change in autotroph C, N, P, Si (cf. Eq.(8.8) and Eq.(8.31)) ...

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{Phy}_{\mathrm{C}} = \mu_{\mathrm{tot}} \cdot \mathrm{Phy}_{\mathrm{C}}$$
(8.1)

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{Phy}_{X} = \underset{(8.23)}{V_{\mathrm{X}}} \cdot \mathrm{Phy}_{\mathrm{C}} - \underset{(8.9)}{M} \cdot \mathrm{Phy}_{X} \quad \text{with} \quad \mathrm{X} = \mathrm{N}, \mathrm{P}, \mathrm{Si}$$
 (8.2)

... in dissolved inorganic nutrients (X=N, P), optionally including silicate

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{DIX} = -V_{\mathrm{X}}\,\mathrm{Phy}_{\mathrm{C}} + \omega_{\mathrm{DOM}}\,\mathrm{DOX}$$
(8.3)

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{DSi} = -V_{\mathrm{Si}}\,\mathrm{Phy_{\mathrm{C}}} + \omega_{\mathrm{Det}}\,\mathrm{Det_{\mathrm{Si}}}_{(8.7)} \tag{8.4}$$

[TODO: include DIC into code]

 $\dots$  in dissolved organic nutrients (X=C, N, P),

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{DOX} = E\,\mathrm{Phy}_X + \omega_{\mathrm{Det}}\,\mathrm{Det}_X - \omega_{\mathrm{DOM}}\,\mathrm{DOX} \tag{8.5}$$

... and in the detrital pool (X=C, N, P, Si).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Det}_{\mathrm{X}} = M'\,\mathrm{Phy}_{X} + M_{Z}\,\mathrm{Zoo}_{X} - \omega_{\mathrm{Det}}\,\mathrm{Det}_{\mathrm{X}} \tag{8.6}$$

where the phytoplankton mortality M' collects contributions from sloppy grazing ((1-y)G) and, in 0D setups, and from sinking (S in Eq.(8.35)). Remineralization of DOM  $\omega_{DOM}$  and hydrolysis of detritus  $\omega_{Det}$  both change with ambient temperature and substrate quality

$$\omega_{\text{DOM}} = f_T \frac{\text{DON}}{\text{DOC}} \, \omega_{\text{DOM}}^* \qquad \qquad \omega_{\text{Det}} = f_T \, \frac{\text{Det}_{\text{N}}}{\text{Det}_{\text{C}}} \, \omega_{\text{Det}}^*$$
 (8.7)

Because of the quality dependency in degradation rates [TODO: justify], element cycles in the water column are easily decoupled within MAECS.

Note that in a chemostat mode, to the dynamics of *all* concentration variables a dilution (D) loss is added, which only for dissolved nutrients also contains reservoir inflow ( $-D \cdot (DIX - DIX^0)$ ).

[TODO: Parameter table]

# 8.2 Process Descriptions

### 8.2.1 Growth rate components and primary production

Temporal changes of the bulk phytoplankton concentration  $Phy_C$  are per construction given in terms of the over all relative growth rate  $\mu_{tot}$ :

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Phy}_{\mathrm{C}} = \mu_{\mathrm{tot}} \cdot \mathrm{Phy}_{\mathrm{C}} \tag{8.8}$$

The relative growth rate of autotrophic unicells (phytoplankton) collects primary production and a number of loss terms

$$\mu_{\text{tot}} = \underbrace{P - \underset{\mu}{R}} - (\underbrace{E}_{(8.45)} + \underbrace{\frac{GZoo_{\text{C}}}{Phy_{\text{C}}}}_{(8.34)} + \underbrace{S}_{(8.35)} + \underbrace{AF}_{(8.40)} + D) = \mu - M$$
(8.9)

with sinking loss given in Eq.(8.35) (relevant only in 0D), aggregate formation in Eq.(8.40) [TODO: living cells in aggregates], grazing G explained in Sec. 8.2.6, exudation rate E formulated in Eq.(8.45), dilution rate D (for running the model in a chemostat mode), and respiration R in Eq.(8.12).

Gross C assimilation P changes with stoichiometric balance as expressed by the multi–nutrient co–limitation factor LF(Eq.(8.14)), maximal photosynthetic capacity  $P_{\text{max}}$  (further depending on, e.g. partitioning, Eq.(8.20), or size in the ecological version, Wirtz (2011, 2013)) and light harvesting success LH

$$P = P_{\text{max}} \cdot \underset{(8.20)}{\text{LF}} \cdot \text{LH}$$
 (8.10)

Light harvesting LH is primarily controlled by ambient light intensity PAR and light adsorption by chloroplasts  $\alpha \cdot \theta$  proportional to the chlorophyll concentration  $\theta$  (cf.Eq.(8.21)). Its functional form derives from Poisson arrival statistics of photons

$$LH = 1 - e^{-\alpha\theta PAR/P_{max}}$$
 (8.11)

#### 8.2.2 Respiration and temperature

Respiratory losses reflect costs of N uptake (Raven, 1984; Pahlow, 2005), while neglecting energetic costs of P-and Si-assimilation

$$R = \zeta V_{\rm N} \tag{8.12}$$

Temperature dependency of respiration thus follows from the factor  $f_T$  in the uptake coefficients in Eq.(8.24). In the current MAECS version, all metabolic rates equally increase with rising temperature following the Arrhenius equation,

$$f_T = e^{-E_a(T^{-1} - T_0^{-1})}$$
 with  $E_a = \frac{T_0^2}{10} \cdot \log(Q_{10})$  (8.13)

with a reference temperature  $T_0$  (here 18°C) where  $f_T$  equals one.

### 8.2.3 Multi-nutrient co-limitation

The co-limitation factor LF is constructed within a metabolic network view of cellular physiology. There, LF reflects not only the availability of singular resources (nutrients) but also how dependent the sub-networks (protein turnover) associated to those nutrients can evolve. In this view, LF quantifies the turnover of the first sub-process (here intracellular nitrogen turnover) times the queuing function that gives the intermittency between the first and the other sub-processes (associated to elements X):

LF = 
$$q_N \cdot g_h (q'_X/q_N) \cdot c_{hq}$$
 with  $c_{hq} = 1 + c_h + h \cdot q_N q'_X$  (8.14)

The relative quota  $q_X$  expresses the availability of nutrient X above a subsistence threshold  $Q_X^0$  normalized by a reference pool size  $Q_X^* - Q_X^0$ . In contrast to most other models resolving variable internal stores (e.g. Morel, 1987),  $Q_X^*$  does not impose [TODO: 'does not impose'=? is it rather 'is not a prescribed'? but what is it then?] an upper boundary of the cell quota  $Q_X$ .

$$q_{\rm X}=rac{Q_{\rm X}-Q_{\rm X}^0}{\Delta Q_{\rm X}} \quad {\rm with} \quad \Delta Q_{\rm X}=Q_{\rm X}^*-Q_{\rm X}^0 \quad {\rm and} \quad {\rm X=N,P,Si,\dots}$$
 (8.15)

In Eq.(8.14), the product  $hq_Nq_X'$  describes the non-linear metabolic interdependency between intracellular turnover of element N and X that is not covered by the simple queuing function.  $g_h$  expresses a "stop and go" dependency while neglecting possible amplification and inhibition effects as explained by Wirtz&Kerimoglu (in prep.). The product term leads to a quadratic influence of the first element  $(q_N)$  and can be considered as most simple account of nonlinear metabolic interdependency. It also ensures symmetry of LF with respect to exchanging the order of nutrients as  $q_1g_h(q_2'/q_1)c_{hq12}\approx q_2g_h(q_1'/q_2)c_{hq21}$ .

The queuing function  $g_h$  can be derived from assuming Poisson statistics in phase-locking of sub-networks [TODO: 'Poisson statistics in phase-locking of sub-networks' sounds scary, please expand!]:

$$g_h(x) = \frac{x - x_h}{1 - x_h}$$
 with  $x_h = x^{1 + h^{-1}}$  (8.16)

The function  $g_h$  introduces as new control parameter the metabolic interdependency h. h resembles the processing intermittency introduced by Wirtz (2012), which describes the probability of phase-locking [TODO: 'phase-locking' is again an unusual term: expand with a sentence?] in independent sub-steps in a process chain.

The correction coefficient  $c_h$  in Eq.(8.14) follows from imposing convergence of LF to the product and Liebig rules. Compliance to the Liebig rule leads to  $c_0=0$  since  $g_0$  describes a stepwise linear function [TODO: it's not clear: when ch=h=0, Eq.(8.14) reduces to  $q_Ng_0(q_X'/q_N)$ ,  $withg_0=-\inf/-\inf$ ]. For the product rule, we use the identity  $g_h(1)=1/(1+h)$  and assume that  $q_X=q_Y=1/2$ , to obtain  $1/4=1/2\cdot(1+h/4+c_h)/(1+h)$  [TODO: it's very unclear where this equation came from], or  $c_h=-1/2+h/4$ . However, the offset in this linear relation conflicts with the condition  $c_0=0$ . Both conditions can be approximately reconciled by a logarithmic function [TODO: does Eq.(8.17) have something to do with all the other equations in this paragraph? if so, how? if not, why not directly listing those 'conditions', providing Eq.(8.17) saying that it is one of the potentially many pragmatic solutions?]

$$c_h = \log(1/4^h + h/2) \tag{8.17}$$

It is mandatory in MAECS to resolve nitrogen. If optionally one, two, or more further nutrients are considered (e.g., P or Si, P and Si, or a micro-nutrient), a recursive scheme is applied. The limiting effect of element X+1 on the processing of element  $X(q_X')$  is then formally equivalent to the LF of the first element (N) limited by the remainder metabolism (LF =  $q_N'$ ) as given in Eq.(8.14):

$$q'_{X} = q_{X} \cdot g_{h}(q'_{X+1}/q_{X}) \cdot c_{hq} \qquad X = P, Si, ...$$
 (8.18)

For the final element we have  $q'_{\rm X}=q_{\rm X}$ . From the (subjective) ordering of elements in the recursive scheme only a small asymmetry arises. [TODO: no matter how small it is, the asymmetry probably requires us to document (and maybe also provide justification, if any) the order we chose]

#### 8.2.4 Uptake system allocation and PI-coefficients

It is assumed that the fraction of free proteins or allocatable resources does not change. [TODO: it is not clear what this means: maybe a diagram helps?] Structural compounds such as cell wall, nucleus, or other non directly functional components are thus kept at a fixed ratio. The pool of free organics (in terms of cellular carbon) is partitioned between photosynthetic machinery and nutrient uptake. Photosynthetic machinery is further sub-divided into light harvesting and processing. The relative pool size of free resource (here in units C!) invested into light-independent reactions, primarily those in Rubisco and the Calvin cycle (Friend, 1991) is denoted as  $f_R$ , the one for the light harvesting complex (LHC)  $f_{\theta}$ . This way, the coefficient  $f_V$  for C-allocation to nutrient uptake becomes a linear function of the C-allocation to LHC  $f_{\theta}$  and to Rubisco  $f_R$ :

$$f_V = 1 - f_R - f_\theta (8.19)$$

Maximum photosynthesis rate  $P_{\text{max}}$  is controlled by the pool fraction  $f_R$  invested into Rubisco/processing and a temperature dependency  $f_T$  given in Eq.(8.13), while the effect of nutrient limitation (namely N) is already included in Eq.(8.10)

$$P_{\text{max}} = f_R \cdot f_T \cdot P_{\text{max}}^*$$
 (8.20)

The fraction of light harvesting carbon depends on the C-fraction partitioned to photosystem processing (electron chain) and the chlorophyll concentration  $\theta$  (relative to a reference value  $\theta_C$ ):

$$f_{\theta} = f_R q_N^{\sigma} \theta / \theta_C \quad \text{or} \quad \theta = f_{\theta} / f_R q_N^{-\sigma} \theta_C$$
 (8.21)

where C stoichiometry of pigment complexes is denoted by  $\theta_C$ . The exponent  $\sigma$  describes an additional linkage of LHC synthesis on the N-status of the cell. Wirtz and Pahlow (2010) proposed that  $\sigma=1$  for diatoms, while  $\sigma=0$  for other autotrophs.

[TODO: 1) so far, it's not clear what's the relevance of  $\theta$  or  $f_{\theta}$  for physiological processes. Maybe a sentence. 2) it's also not clear where these novel and mysterious parameters such as  $f_R$  and  $\theta$  come from. Maybe it's helpful to hint that they are being dynamically optimized, referring to Sec. 8.3]

#### 8.2.5 Nutrient uptake

Nutrient uptake rate of the cell varies with a number of internal, physiological factors, such as the partitioning coefficient  $f_V$  (see above) and the (enzymatic) activity  $a_{V,X}$  (X= N, P, Si, ...), and is furthermore determined by the potential uptake  $V_X^*$ 

$$V_{X} = f_{V} \cdot a_{V,X} \cdot V_{X}^{*}$$
(8.22)

Potential uptake  $V_{\rm X}^*$  reflects ambient nutrient concentration, but also affinity and transport capacities denoted by  $A_{\rm X}$  and  $V_{\rm max,X}$ . Nutrient uptake is a sequential 2-stage process (membrane uptake and intracellular transport) as described by the nutrient affinity  $A_{\rm X}$  and maximal uptake rate  $V_{\rm max,X}$  such that the effective uptake time equals the sum of turnover times in each stage:

$$V_{\rm X}^{*-1} = V_{\rm max,X}^{-1} + (A_{\rm X}\,{\rm DIX})^{-1}$$
 with DIX = DIN, DIP, DSi, . . . (8.23)

Nutrient uptake characteristics are temperature sensitive and assumed to depend on a sub-partitioning of allocatable proteins expressed by the coefficient  $f_{A,X}$ 

$$V_{\text{max},X} = (1 - f_{A,X}) \cdot Q_0 \cdot \int_{(8.13)} V_{\text{max},X}^0$$
 (8.24)

$$A_{\mathbf{X}} = f_{A,\mathbf{X}} \cdot Q_0 \cdot f_T \cdot A_{\mathbf{X}}^0 \tag{8.25}$$

ONUR: What's presently implemented is:

$$V_{\text{max,X}} = (1 - f_{A,X}) \cdot f_T \cdot V_{\text{max,X}}^0$$
 (8.26)

$$A_{\mathbf{X}} = f_{A,\mathbf{X}} \cdot A_{\mathbf{X}}^{0} \tag{8.27}$$

[TODO: differential temperature sensitivity; see Smith 2013]

Protein sub-partitioning of overall uptake machinery  $(f_V)$  into affinity and transport capabilities is instantaneously optimized

$$\frac{\partial V_{\mathbf{X}}^*}{\partial f_{A,\mathbf{X}}} = 0 \tag{8.28}$$

and the resulting optimal sub-partitioning depends on nutrient availability (Pahlow, 2005; Smith et al., 2009)

$$f_{A,X} = \left(1 + \sqrt{A_X^0 \cdot \text{DIX}/V_{\text{max},X}^0}\right)^{-1}$$
 (8.29)

In terms of the autotroph nutrient quota  $Q_{\rm X}$  (X=N, P, Si) imbalance between nutrient uptake and growth demand leads to

$$\frac{\mathrm{d}}{\mathrm{d}t}Q_{\mathrm{X}} = V_{\mathrm{X}} - \mu \cdot Q_{\mathrm{X}} \tag{8.30}$$

or, in the MAECS notation where traits/characteristics are transported as bulk biomasses  $Phy_X$  parallel to the basic phytoplankton concentration  $Phy_C$ 

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Phy}_{X} = V_{\mathrm{X}}\cdot\mathrm{Phy}_{\mathrm{C}} - \underbrace{M}_{(8.9)}\cdot\mathrm{Phy}_{X} \qquad \text{with} \quad Q_{\mathrm{X}} = \frac{\mathrm{Phy}_{X}}{\mathrm{Phy}_{\mathrm{C}}} \tag{8.31}$$

[TODO: exudation]

#### 8.2.6 Grazing

Before merging with the ecological MAECS version, we use primitive (non-biophysical) standards for describing heterotrophic activities:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Zoo}_{\mathrm{C}} = (y \cdot G - \tau_{\mathrm{C}} - M_{\mathrm{Z}}) \cdot \mathrm{Zoo}_{\mathrm{C}}$$
(8.32)

with quadratic and temperature sensitive mortality to represent top-down pressure

$$M_Z = f_T \cdot M_Z^0 \cdot \text{Zoo}_{\mathcal{C}} \tag{8.33}$$

and a Holling-III response function for functional grazing response:

$$G = g_{\text{max}} f_T \cdot \frac{\text{Phy}_{\text{C}}^2}{K_G^2 + \text{Phy}_{\text{C}}^2}$$
(8.34)

[TODO: more complicated loss/leakage terms  $\tau_X$  to ensure homeostasis and mass conservation]

#### 8.2.7 Sinking loss

Vertical losses account for enhanced settling due to aggregate formation which occurs under high concentrations of particles and exopolymeres. As a coastal model, already the basic version of MAECS resolves a benthic compartment independently from the coupled diagenesis model (see below).

The relative loss rate S is, in an idealized picture, the ratio between  $v_s$  and the mixed layer depth (MLD)

$$S = (1 + f_{\text{agg}}) \cdot \frac{v_{\text{S}}}{\text{MLD}}$$
 (8.35)

[TODO: add size as trait or explicit parameter; the following part comes from the size-based model version]

The velocity  $v_s$  of a sinking particle is described by Stokes' law, which for a spherical cell with diameter ESD=  $e^{\ell}$  reads

$$v_{\rm s} = \frac{g\rho'(\ell)\,\mathrm{e}^{2\ell}}{18\nu(T)}\tag{8.36}$$

The unitless excess density  $\rho'$ , the density difference between water and the suspended body, divided by water density, is known to be a function of the physiology and size of the suspended cells (Waite et al., 1997; Kiørboe et al., 1998; Miklasz and Denny, 2010). Dead cells are relatively heavy-weighted ( $\rho' = \rho^{\dagger}$ ,  $\rho^{\dagger} > 0$ ), but  $\rho^{\dagger}$  decreases in large (siliceous) phytoplankton due to an increasing fraction of vacuoles. The allometric relation of vacuolation and excess density reduction is

$$\rho^{\dagger} = \rho_0^{\dagger} e^{-\alpha_{\rho}\ell} \tag{8.37}$$

As vacuoles usually contain a higher concentration of inorganic compounds than the surrounding cytoplasm, the exponent  $\alpha_p$  should be close to the size scaling slope reported for carbon density by Menden-Deuer and Lessard (2000).

Linear dependency between excess density and relative production

$$\rho' = (1 - f_{\text{vac}} \cdot p) \cdot \rho^{\dagger} \tag{8.38}$$

 $f_{\rm vac}$  is the relative volumetric fraction that can be filled with material of reduced density (e.g., gases, lipids, or solutes, the latter listed in Boyd and Gradmann (2002)). This quantity relates to the vacuole structure (Raven and Waite, 2004) and can therefore be formulated as the relative density difference with respect to cells without vacuolation ( $\rho_0^{\dagger}$  in Eq.(8.37))

$$f_{\text{vac}} = \frac{\rho_0^{\dagger} - \rho^{\dagger}}{\rho_0^{\dagger}} = 1 - e^{-\alpha_{\rho}\ell}$$
 (8.39)

# 8.2.8 Particle aggregation

[check with Richard; re-introduce into code]

Aggregation depends on stickiness and particle surface

$$f_{\text{agg}} = f_{\text{agg}}^* \operatorname{EP} \cdot \operatorname{Phy}_{\mathbf{C}} \cdot \operatorname{ESD}^n \tag{8.40}$$

The relative fraction of exopolymeres within the DOM pool is inversely related to DOM quality, which is expressed in terms of the N:C stoichiometry. Stickiness associated with exopolymeres (EP) correlates with DOM quantity and inverse quality

$$EP = \frac{DOC}{DON}DOC$$
 (8.41)

Stickiness not only enhances coagulation efficiency in particle aggregation, it also increases the critical bottom shear stress for sediment resuspension ("biostabilization"). Resuspension of benthic material occurs when bottom shear stress exceeds that "sticky" threshold.

$$RS = RS^* \max \left\{ V_{\text{bshear}} - V_{\text{EP}}^* \text{ EP}, 0 \right\}$$
 (8.42)

so we have for material fluxes due to resuspension

$$\frac{\mathrm{d}}{\mathrm{d}t}C_X^{\mathrm{z=H}} = \ldots + \mathrm{RS}C_X^{\mathrm{ben}} \quad \text{with} \quad C_X = \mathrm{Phy}_X, \mathrm{Det}_X$$
(8.43)

#### 8.2.9 Other stuff

Photoinhibition by depletion of D1-protein

$$u = \frac{q_{\rm N}}{q_{\rm N} + u^* \, \text{Chl:} \, \text{C}^2} \tag{8.44}$$

Exudation reflects imbalance between C uptake and assimilation

$$E = e^* P_{\text{max}}^* f_T \text{LH}$$
 (8.45)

# 8.3 Adaptive trait regulation and differential trade-off

Adaptive trait dynamics in its general form has been proposed as an optimality-seeking principle guiding transient adaptive regulation phenomena on very different levels of description, from organ physiology to population ecology (Wirtz, 2000, 2003; Smith et al., 2011). This principle/equation is applied to all physiological traits in MAECS, in particular to those that primarily control nutrient uptake ( $f_R$  and  $\theta$  through  $f_V$ , and activity  $a_{V,X}$ . C-growth as goal function needs to be extended by "hidden" or indirect effects through a differential link between nutrient uptake  $V_X$  and quota  $Q_X$  for all macro-nutrients:

$$\frac{\mathrm{d}f_{m,X}}{\mathrm{d}t} = \delta_m \left( \frac{\partial \mu}{\partial f_{m,X}} + \sum_{\mathbf{x}} \frac{\partial \mu}{\partial Q_{\mathbf{X}}} \frac{\mathrm{d}Q_{\mathbf{X}}}{\mathrm{d}V_{\mathbf{X}}} \Big|_{\text{tot}} \frac{\partial V_{\mathbf{X}}}{\partial f_{m,X}} \right) \quad \text{with} \quad f_{m,X} = f_{\mathbf{R}}, \theta, a_{\mathbf{V},X} \quad \mathbf{X} = \mathbf{N}, \mathbf{P}, \mathbf{Si}, \dots$$
 (8.46)

[TODO: reduce text or spread to individual eugations]

Diverging from most standard ecosystem models, however, MAECS assumes intricate interdependencies between independent C, N, or P assimilation functions while avoiding prescribed stoichiometric control settings such as maximal N:C or P:C ratios. For doing so, it implies optimality criteria already in the description of basic uptake formulations (lower part of Table ??). These criteria control shifts between high affinity and fast transport nutrient uptake (see above Eq.(8.29)) and in the enzymatic down-regulation of all nutrient uptake activities. Adaptive control in activity secures phytoplankton cells from non-beneficial intracellular accumulation of nutrients, but in the

model also requires to formulate an extended optimality principle by which C costs of nutrient uptake have to be balanced with corresponding C benefits arising fro associated quota changes (Eq.(??)). For both regulations (uptake site/transport partitioning, activity), steady-state solutions or approximations are calculated since physiological uptake regulations proceed at very high speed.

For nitrogen (N), the differential effect of increasing nutrient uptake rate on the quota derives from functional variation applied to the quota uptake equation Eq.(8.30):

$$\delta V_{X} + \frac{\partial V_{X}}{\partial Q_{X}} \delta Q_{X} - \mu \cdot \delta Q_{X} - Q_{X} \cdot \frac{\partial \mu}{\partial Q_{X}} \delta Q_{X} - Q_{X} \cdot \frac{\partial \mu}{\partial V_{X}} \delta V_{X} = 0$$
 (8.47)

or

$$\frac{dQ_X}{dV_X} = (1 + \zeta_X Q_X) \cdot \left(\mu + Q_X \frac{\partial \mu}{\partial Q_X} - \frac{\partial V_X}{\partial Q_X}\right)^{-1}$$
(8.48)

where the derivative of uptake rate on quota may only become non-zero (1) for nitrogen (N) and (2) if C-partitioning to chlorophyll ( $f_{\theta}$  in Eq.(8.21)) is hardwired to the N-quota:

$$\frac{\partial V_{N}}{\partial Q_{N}} = \frac{V_{N}}{f_{V}} \frac{\partial f_{V}}{\partial Q_{N}} = -\frac{\sigma f_{R} \theta}{f_{V} \theta_{C} \Delta Q_{N}} V_{N} = -\sigma' V_{N}$$
(8.49)

#### 8.3.1 Growth derivatives under co-limitation

For the N-turnover and regulation, the differential dependency of  $V_{\rm N}$  on  $Q_{\rm N}$  also enters the marginal increase in primary production when raising intracellular quota; an analytical derivation of the photosynthesis rate P in Eq.(8.10) with respect to each co-limiting quota  $Q_{\rm X}$  reads

$$\frac{\partial \mu}{\partial Q_{X}} = \frac{P}{LF} \frac{\partial LF}{\partial q_{X}} \frac{\partial q_{X}}{\partial Q_{X}} - \zeta \frac{\partial V_{N}}{\partial Q_{X}}$$

$$= d_{X} \frac{\mu + \zeta V_{N}}{\Delta Q_{X}} + \sigma' \zeta V_{N} \qquad \text{with} \quad d_{X} = LF^{-1} \frac{\partial LF}{\partial q_{X}}$$

$$= \left( d_{X} \frac{1 + \zeta Q_{N}}{\Delta Q_{X}} + \sigma' \zeta Q_{N} \right) \cdot \mu$$

$$= d_{QX} \cdot \mu \qquad (8.50)$$

where we assumed a balanced growth relation between growth and uptake ( $\mu Q_{\rm N}=V_{\rm N}$ ), used the relation  $P=\mu+\zeta V_{\rm N}$ . In light of Eq.(8.49) we have  $\sigma_{\rm N}'=\sigma'$  and  $\sigma_{\rm X}'=0$  for other elements that lack direct influence on N-uptake rate

The derivation result  $d_X$  of the (recursive) co-limitation factor  $LF \equiv q_1'$  may contain a number of product terms, depending on where in the scheme the limiting effect of  $Q_X$  is calculated. Consider the series of limitation factors  $q_1, q_2, \ldots q_{No^{nut}}$  (e.g., for  $q_N, q_P, q_{Si}$ ) we start from the first element where the recursive scheme Eq.(8.18) has been invoked only once. For example, if MAECS just resolves its basic element N,

$$d_N = \frac{1}{q'_N} \qquad \qquad \text{for No}^{\text{nut}} = 1 \tag{8.51}$$

or N and P,

$$d_{\rm N} = \frac{1}{q'_{\rm N}} \frac{\partial q'_{\rm N}}{\partial q_{\rm N}} \qquad d_{\rm P} = \frac{1}{q'_{\rm N}} \frac{\partial q'_{\rm N}}{\partial q'_{\rm P}} \frac{\partial q'_{\rm P}}{\partial q_{\rm P}} \qquad \text{for No}^{\rm nut} = 2$$
 (8.52)

Note that  $\partial q'_P/\partial q_P$  is one because P makes the last element in the list, so that the metabolic effect of  $Q_P$  as quantified by  $q'_P$  exclusively depends on the availability of  $Q_P$  as quantified by  $q_P$ . The general form for an arbitrary  $No^{nut}$  continues the sequential differentiation from the first element (here usually N) to the element X under consideration. So starting from  $q'_1$  we calculate the use efficiency of element X again using the chain-rule:

$$d_{X} = \frac{1}{q_{1}'} \frac{\partial q_{1}'}{\partial q_{2}'} \frac{\partial q_{2}'}{\partial q_{3}'} \cdots \frac{\partial q_{X}'}{\partial q_{X}}$$
(8.53)

Note that the last term in the product of differentials  $(\partial q'_{\rm X}/\partial q_{\rm X})$  is either one if X is the last element in the sequence, and otherwise given by Eq.(8.54). The differentials in Eqs.(8.51)–(8.53) characterize the recursive effect of metabolic efficiencies of  $q'_{\rm X}$  formulated in Eq.(8.18)

$$\frac{\partial q_{\mathbf{X}}'}{\partial q_{\mathbf{X}}} = q_{\mathbf{X}}' \cdot \left( q_{\mathbf{X}}^{-1} - \frac{\partial g_h}{\partial x} \frac{q_{\mathbf{X}+1}'}{g_h q_{\mathbf{X}}^2} + \frac{h q_{\mathbf{X}+1}'}{c_{hq}} \right) \tag{8.54}$$

or, if we differentiate with respect to the second efficiency:

$$\frac{\partial q_{\mathbf{X}}'}{\partial q_{\mathbf{X}+1}'} = q_{\mathbf{X}}' \cdot \left( \frac{\partial g_h}{\partial x} \frac{1}{g_h q_{\mathbf{X}}} + \frac{h q_{\mathbf{X}}}{c_{hq}} \right) \tag{8.55}$$

where the coefficient  $c_{hq}$  given in Eq.(8.14) is written without nutrient specific indices. Step-wise derivation of the queuing function  $(x-x_h)/(1-x_h)$  with  $x_h=x^{1+h^{-1}}$  in Eq.(8.16) yields

$$\frac{\partial g_{h}}{\partial x} = \frac{(1 - (1 + h^{-1})x_{h}/x) \cdot (1 - x_{h}) + (x - x_{h}) \cdot (1 + h^{-1})x_{h}/x}{(1 - x_{h})^{2}}$$

$$= \frac{(xh - (h+1)x_{h}) \cdot (1 - x_{h}) + (x - x_{h}) \cdot (h+1)x_{h}}{xh \cdot (1 - x_{h})^{2}}$$

$$= \frac{xh - (h+1)x_{h} - xhx_{h} + (h+1)x_{h}^{2} + x \cdot (h+1)x_{h} - (h+1)x_{h}^{2}}{xh \cdot (1 - x_{h})^{2}}$$

$$= \frac{xh + (x-1-h) \cdot x_{h}}{xh \cdot (1 - x_{h})^{2}} \tag{8.56}$$

[TODO: numerical approximation to avoid problems at x = 1]

#### 8.3.2 Quota-uptake feed-back

Eq.(8.48) provides a first estimate for the differential trade-off required for a fully coherent application of the optimality principle to physiological regulation. However, a marginal change in quota after a differential change in uptake rate may propagate back to the uptake rate, if the latter directly depends on  $Q_N$ . This direct, differential feed-back between changes in  $Q_N$  and  $V_N$  reads

$$\frac{dQ_{N}}{dV_{N}}\Big|_{tot} = \frac{dQ_{N}}{dV_{N}} \cdot \left(1 + \frac{dQ_{N}}{dV_{N}} \frac{\partial V_{N}}{\partial Q_{N}}\right)$$

$$(8.57)$$

$$\frac{dQ_{N}}{dV_{N}} \frac{\partial V_{N}}{\partial Q_{N}} = -(1 + \zeta Q_{N}) \cdot \left(\mu + Q_{N} \frac{\partial \mu}{\partial Q_{N}} - \frac{\partial V_{N}}{\partial Q_{N}}\right)^{-1} \sigma' V_{N}$$

$$= -(1 + \zeta Q_{N}) \cdot \left(1 + Q_{N} \left[d_{N} \frac{1 + \zeta Q_{N}}{Q_{N} - Q_{N0}} + \sigma' \zeta Q_{N}\right] + \sigma' Q_{N}\right)^{-1} \sigma' Q_{N}$$

$$= -(1 + \zeta Q_{N}) \cdot \left((Q_{N})^{-1} + d_{N} \frac{1 + \zeta Q_{N}}{Q_{N} - Q_{N0}} + \sigma' \cdot (1 + \zeta Q_{N})\right)^{-1} \sigma'$$

$$= -\sigma' \cdot \left(\underbrace{(Q_{N}(1 + \zeta Q_{N}))^{-1} + d_{N}(Q_{N} - Q_{N0})^{-1}}_{e_{N}} + \sigma'\right)^{-1}$$

$$= -\frac{\sigma'}{e_{N} + \sigma'}$$
(8.58)

In all other cases apart of nitrogen, the uptake dependency on the quota vanishes:

$$\frac{\partial V_{\rm X}}{\partial Q_{\rm X}} = 0$$
 and  $\frac{\mathrm{d}Q_{\rm X}}{\mathrm{d}V_{\rm X}}\Big|_{\rm tot} = \frac{\mathrm{d}Q_{\rm X}}{\mathrm{d}V_{\rm X}}$  with  $\mathrm{X} = P, Si$  (8.59)

The product of the quota-uptake differential (without feed-back) and the growth-quota differential in Eq.(8.46) combines Eq.(8.48) and Eq.(8.50) and again assumes  $V_X = Q_X \mu$ :

$$\frac{dQ_X}{dV_X} \frac{\partial \mu}{\partial Q_X} = (1 + \zeta_X Q_X) \cdot \left(\mu + Q_X \frac{\partial \mu}{\partial Q_X} - \frac{\partial V_X}{\partial Q_X}\right)^{-1} \cdot d_{QX} \cdot \mu$$

$$= (1 + \zeta_X Q_X) \cdot \left(1 + Q_X d_{QX} + \sigma'_X V_X \mu^{-1}\right)^{-1} \cdot d_{QX}$$

$$= \frac{(1 + \zeta_X Q_X) \cdot d_{QX}}{1 + Q_X \cdot (d_{QX} + \sigma'_X)}$$
(8.60)

### 8.3.3 Uptake activity regulation

In the current version of MAECS, regulation of all uptake activity traits  $a_{\rm X}$  is supposed to be very fast compared to the simulated dynamics and therefore not integrated in time according to Eq.(8.46), but assumed to be in steady-state. If the marginal benefit of uptake  ${\rm d}\mu/{\rm d}a_{\rm X}$  is negative, activity is ceased; at positive benefit,  $a_{\rm X}$  approaches one, while at neutral growth effect  ${\rm d}\mu/{\rm d}a_{\rm X}\approx 0$ , the activity smoothly varies at 1/2. This behavior is emulated by the non-linear function

$$a_{\mathbf{X}} = \left(1 + e^{-\Delta t_{\mathbf{V}} d\mu / da_{\mathbf{X}}}\right)^{-1} \tag{8.61}$$

For optimization in N-uptake activity  $a_N$  based on its the marginal C gain the extended optimality principle integrates Eq.(8.46) and Eqs.(8.50)–(8.60):

$$\frac{d\mu}{da_{X}} = \frac{\partial \mu}{\partial a_{X}} + \frac{\partial \mu}{\partial Q_{X}} \frac{dQ_{X}}{dV_{X}} \Big|_{tot} \frac{\partial V_{X}}{\partial a_{X}}$$

$$= -\zeta_{X} \frac{V_{X}}{a_{X}} + \frac{\partial \mu}{\partial Q_{X}} \frac{dQ_{X}}{dV_{X}} \frac{e_{N}}{e_{N} + \sigma'_{X}} \frac{V_{X}}{a_{X}}$$

$$= \left(-\zeta_{X} + \frac{(1 + \zeta_{X} Q_{X}) \cdot d_{QX}}{1 + Q_{X} \cdot (d_{QX} + \sigma'_{X})} \frac{e_{N}}{e_{N} + \sigma'_{X}}\right) \cdot \frac{V_{X}}{a_{X}} \tag{8.62}$$

where, again,  $\sigma_N'=\sigma'$  and  $\sigma_X'=0$  for other elements that lack direct influence on uptake.

#### 8.3.4 Costs in P and Si uptake

For a first estimation of the C-costs of P- and Si-uptake (with units mol-C/mol-X) we link the latter to N-assimilation. This means that energetic costs of P- and Si-assimilation are not accounted for as additional terms but assumed to be already included in protein synthesis that are chararized by  $\zeta \equiv \zeta_N$  (with units mol-C/mol-N). For the P-link, we use the N-stoichiometry in RNA (N:P  $\approx$  3.8:1) and phospholipids (N:P  $\approx$  0.8:1 mol-N/mol-P)

$$\frac{\partial \mu}{\partial V_{X}} = \frac{\partial \mu}{\partial V_{N}} \frac{\partial V_{N}}{\partial V_{X}} = -\zeta_{N} \cdot \frac{Q_{N}^{0*}}{Q_{N}^{0*}} = -\zeta_{X}$$
(8.63)

with Eq.(8.14) Eq.(8.18)

$$\zeta_{\rm P} = \left[ (1 - f_{\rm Lip}) \, 3.8 + f_{\rm Lip} \, 0.8 \right] \cdot \zeta_{\rm N} \quad \text{and} \quad \zeta_{\rm Si} = 0$$
 (8.64)

[TODO: check and simplify]

[TODO: include proteins/membranes (N:P ≫ 16:1) under low growth conditions ]

#### 8.3.5 Photoacclimation and transport

MAECS resolves transient photoacclimation as adaptive dynamics in allocation traits (Eq.(8.46)). The optimality principle extended by the differential quota-based trade-off Eq.(8.60) seeks to find an allocation key between nutrient uptake, LHC and light-independent processes (Rubisco) that maximizes relative C-uptake rate  $\mu$ . The optimality condition includes marginal growth benefits of all nutrients (see Eq.(8.46)):

$$\frac{\mathrm{d}}{\mathrm{d}t} f_{\mathrm{R}} = \delta_{R} \left( \frac{\partial \mu}{\partial f_{\mathrm{R}}} + \sum_{\mathbf{x}} \frac{\partial \mu}{\partial Q_{\mathbf{X}}} \frac{\mathrm{d}Q_{\mathbf{X}}}{\mathrm{d}V_{\mathbf{X}}} \Big|_{\mathrm{tot}} \frac{\partial V_{\mathbf{X}}}{\partial f_{\mathrm{R}}} \right) \tag{8.65}$$

and similar for the chloroplast CHL:C ratio  $\theta$ :

$$\frac{\mathrm{d}}{\mathrm{d}t}\theta = \delta_R \left( \frac{\partial \mu}{\partial \theta} + \sum_{\mathbf{x}} \frac{\partial \mu}{\partial Q_{\mathbf{x}}} \frac{\mathrm{d}Q_{\mathbf{x}}}{\mathrm{d}V_{\mathbf{x}}} \Big|_{\text{tot}} \frac{\partial V_{\mathbf{x}}}{\partial \theta} \right)$$
(8.66)

The differential growth loss by increasing allocation to photosynthesis apparati down-sizes the nutrient uptake machinery. All uptake and indirect derivatives of the photoacclimation traits that induce these differential costs had been already introduced above.

Flexibilities in chloroplast CHL:C ratio and in C-allocation to Rubisco are given following Wirtz and Eckhardt (1996); Wirtz (2000)

$$\delta_{\theta} = \delta_{\theta}^* \cdot \theta \cdot (\theta_C - \theta) \qquad \delta_R = \delta_R^* \cdot f_R \cdot (1 - f_R) \tag{8.67}$$

Partial derivatives of photosynthesis rates with respet to  $\theta$  and  $f_R$  (see Eq.(8.20) and Eq.(8.22)):

$$\frac{\partial \mu}{\partial f_{R}} = \frac{P}{f_{R}} - \zeta \frac{\partial V_{N}}{\partial f_{R}}$$

$$= \frac{P}{f_{R}} + \zeta \cdot \left(1 + \frac{q_{N}^{\sigma} \theta}{\theta_{C}}\right) \cdot a_{V,N} V_{X}^{*}$$
(8.68)

$$\frac{\partial \mu}{\partial \theta} = \frac{P}{LH} \frac{\partial LH}{\partial \theta} - \zeta \frac{\partial V_{N}}{\partial \theta}$$

$$= \frac{P}{LH} \frac{\alpha PAR}{P_{\text{max}}} (1 - LH) - \zeta \frac{q_{N}^{\sigma} f_{R}}{\theta_{C}} \cdot a_{V,N} V_{X}^{*} \tag{8.69}$$

For transporting photoacclimation traits in 1D-3D, MAECS integrates them as bulk variables by employing a "carrier" biomass variable (usually  $Phy_C$ ). With Eq.(8.21) we have for the bulk chlorophylla concentration

$$Chl = f_{\theta} \theta_{C} Phy_{C} = f_{R} q_{N}^{\sigma} \theta Phy_{C}$$
(8.70)

and bulk Rubisco concentrations

$$Rub = f_R Phy_C (8.71)$$

[TODO: write down full equations]

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# Index

calc_internal_states	maecs_maecsdo_combined.F90, 27
maecs_functions, 15	maecs_primprod, 19
calc_sensitivities	photosynthesis, 20
maecs_functions, 16	maecs_primprod.F90, 27
	maecs_types, 21
fabm_hzg_maecs, 10	maecs_types.F90, 27
get_light_extinction, 12	maecs_types::stoich_pointer, 21
initialize, 11	maecs_types::type_maecs_allocation_fractions, 2
maecs_do, 12	maecs_types::type_maecs_base_model, 22
maecs_get_vertical_movement, 14	maecs_types::type_maecs_basic_traits, 22
maecs_init_stoichvars, 12	maecs_types::type_maecs_env, 23
fabm_hzg_maecs::maecs_do, 14	maecs_types::type_maecs_life, 23
fabm_hzg_maecs::maecs_get_vertical_movement,	maecs_types::type_maecs_nutindex, 23
18	maecs_types::type_maecs_om, 23
fabm_hzg_maecs::type_hzg_maecs, 21	maecs_types::type_maecs_phy, 24
foptupt	maecs_types::type_maecs_rhs, 24
maecs_functions, 16	maecs_types::type_maecs_sensitivities, 24
	maecs_types::type_maecs_switch, 24
get_light_extinction	maecs_types::type_maecs_traitdyn, 25
fabm_hzg_maecs, 12	maecs_types::type_maecs_zoo, 25
grazing	min_mass
maecs_grazing, 19	maecs functions, 18
grazing losses	_ ,
maecs grazing, 19	photosynthesis
_5	maecs_primprod, 20
initialize	
fabm_hzg_maecs, 11	queuederiv
_	maecs_functions, 17
maecs_do	queuefunc
fabm_hzg_maecs, 12	maecs_functions, 17
maecs_functions, 14	queuefunc1
calc_internal_states, 15	maecs_functions, 17
calc_sensitivities, 16	
foptupt, 16	sinking
min_mass, 18	maecs_functions, 17
queuederiv, 17	smooth_small
queuefunc, 17	maecs_functions, 18
queuefunc1, 17	
sinking, 17	uptflex
smooth_small, 18	maecs_functions, 16
uptflex, 16	
maecs_functions.F90, 26	
maecs_get_vertical_movement	
fabm_hzg_maecs, 14	
maecs_grazing, 18	
grazing, 19	
grazing, 19 grazing losses, 19	
maecs_grazing.F90, 26	
maecs_init_stoichvars	
fabm_hzg_maecs, 12	