



中山大學  
SUN YAT-SEN UNIVERSITY

# Part II [Problem]

## 4. Test Adequacy (Blackbox, level-2)



**SE-307 Software Testing Techniques**

<http://my.ss.sysu.edu.cn/wiki/display/SE307/Home>

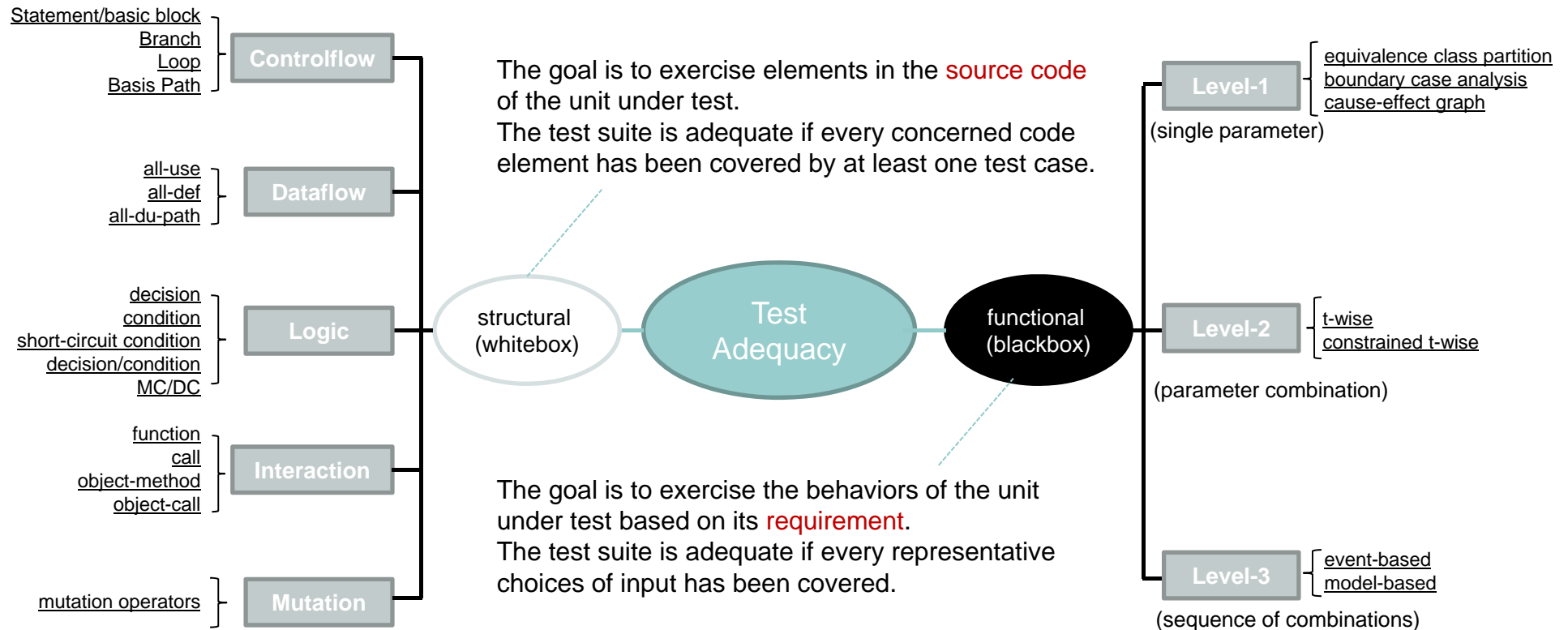
Instructor: Dr. Wang Xinming, School of Software, Sun Yat-Sen University

# Review: Test Adequacy

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- **Test adequacy** is about the questions:
  - What is the goal of test suite design?
  - Is our test suite 'adequate'?
  - When can we stop designing new test cases?
- **Whitebox (Structural)** approach to test adequacy:
  - The goal is to exercise elements in the **source code**. e.g. statements, basic blocks, branches, loops, basis-paths, conditions, du-paths, function-calls, etc.
  - Our test suite is considered adequate **if every concerned code element is covered by at least one test case**.
- **Blackbox (Functional)** approach to test adequacy:
  - The goal is to exercise the behaviors of the units-under-test based on its **requirement**, without considering its implementation detail. Such a unit can be a method, a class, a sub-system, or the whole programs.
  - Our test suite is considered adequate **if it covers representative choices of input to the unit-under-test**.

# Review

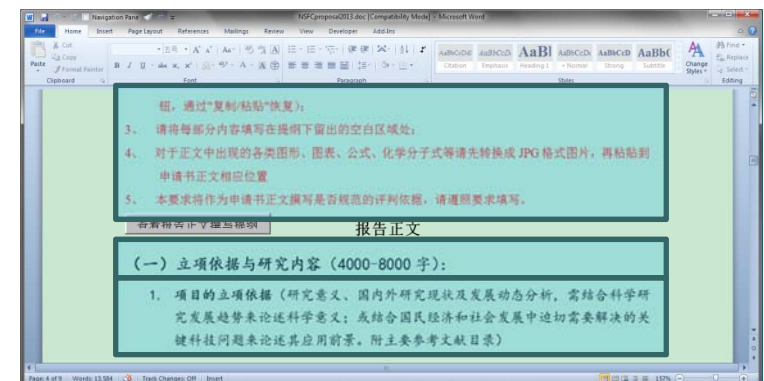
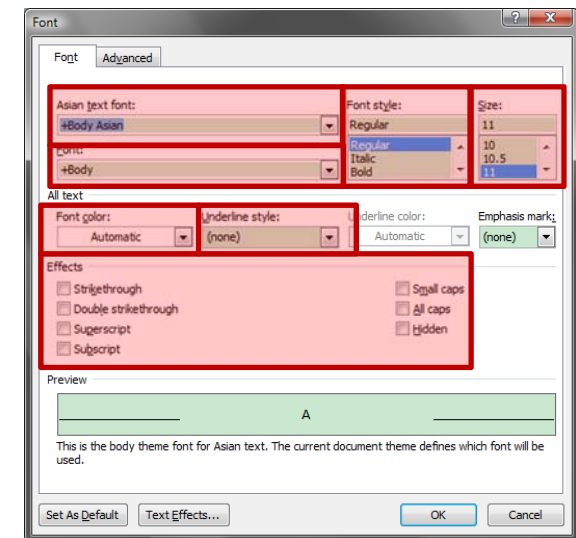


# Review: 3 Levels of Blackbox Adequacy

- **Level 1: *Single*** input parameter
  - Cover the representative choices for **one single input parameter**.
  - e.g. the font type. (宋体 or 黑体 or Arial or ....)
- **Level 2: *Combination*** of input parameters
  - Cover the representative **combinations of multiple parameters**.
  - e.g. settings in the whole font dialog. (宋体-加粗-11号-红色 or 宋体-普通-小四-黑色 or 黑体-加粗-12号-黄色 or ...)
- **Level 3: *Sequence*** of parameter combinations
  - Cover the representative **sequences of parameter combinations**.
  - e.g. font settings for multiple paragraphs. (e.g. 为不同的段落设置不同的字体)。

Asian text font:

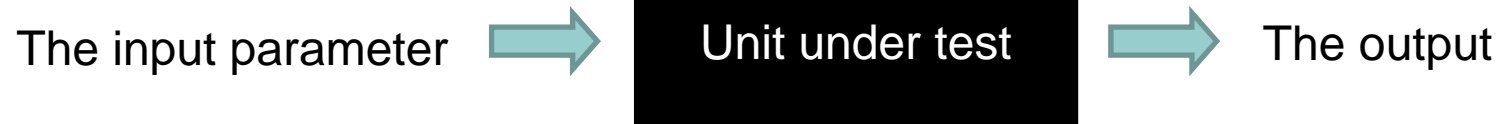
+Body Asian



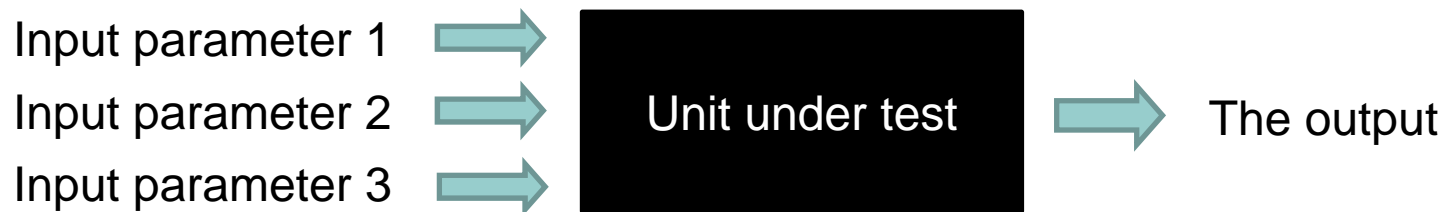
# Illustration of The Three Levels

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## Level 1



## Level 2



## Level 3



# Review: Level-1 Techniques

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- **Equivalence class partitioning (ECP, 等价类划分)**
  - Partition the input domain of the parameter into equivalence classes
  - Adequacy criterion: cover each partition at least once
- **Boundary value analysis (BVA, 边界值分析)**
  - Analyze the boundary cases for each equivalence class in ECP.
  - Adequacy criterion: cover each boundary case at least once.
- **Cause-effect graph and decision table (因果图和决策表)**
  - Analyze the causal relation between input and output as *edges*.
  - Adequacy criterion: cover each edge at least once.

# Level-2: Adequacy For Combination

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# Why Combination?

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Many faults are triggered by **interaction** between input parameters of the unit under test.

Example:

```
if (altitude_adj == 0 ) {  
    if (volume < 2.2) {  
        faulty code here!  
    }else { good code, no problem}  
} else {  
    .....  
}
```

Only test data that satisfies **altitude\_adj==0** and **volume <2.2** can trigger the failure.



# The Problem

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- Level-1 techniques suggests a set of values for each individual parameter
  - Each cover one equivalence class or boundary case
- Now we have  $K$  parameters. Can we test all their value combinations?
  - Usually impossible as there are too many.
- This problem is ubiquitous.

# Combination Problem: Case 1

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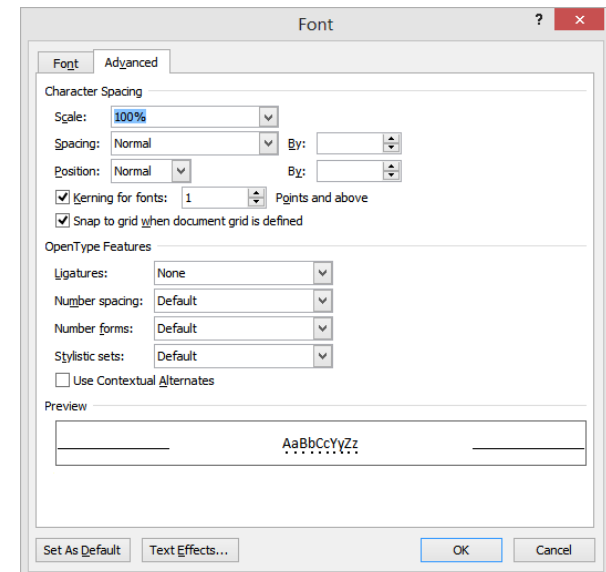
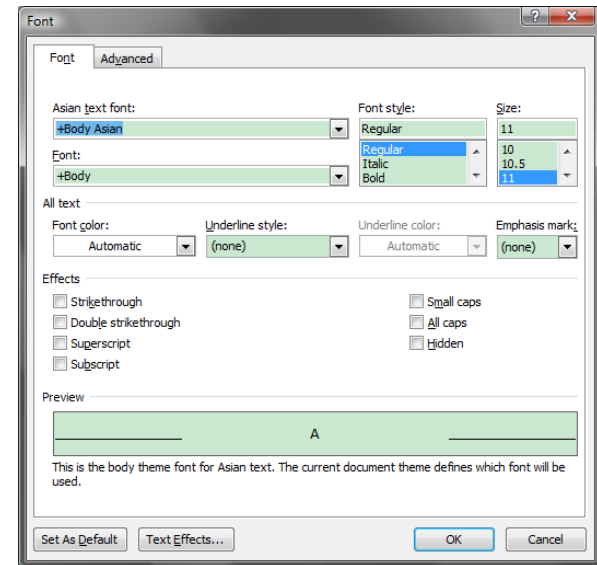
- Unit under test is a Java method with 5 parameters:

`foo( a, b, c, d, e )`

- Determine equivalence classes for each parameter, select a representative value from each equivalence class
  - For **a**, we might have:  $[-\infty, -4]$   $[-3, -1]$   $[0]$   $[1, 12]$   $[13, +\infty]$
  - For **b**, we might have:  $[0, 19]$   $[20]$   $[21, 50]$   $[51, +\infty]$
  - .....
- To test the method, we need to select combinations of equivalence classes.
  - Suppose every parameter has 10 equivalence classes & boundary cases
  - Total combinations will be  $5^{10} = 9765625$  – too many to test them all.
- Test adequacy for parameter combination: **Which combinations shall we cover?**

# Combination Problem: Case 2

- Unit under test is a feature or a sub-system
- Office font setting dialog parameters:
  - font type**: Arial, Courier, Tahoma,...
  - font style**: Regular, Italic, Bold
  - font size**: 1, [5~10], [10, 20]
  - font color**: red, green, blue
  - underline style**: solid, dash, double-dash
  - underline color**: red, green, blue
  - emphasis mark**: line, dot
  - superscript**: none, raise by 3, raise by 5, ...
  - spacing**: normal, expanded, condensed
- Total combinations will be at least:  
 $3 \times 3 \times 17 \times 3 \times 3 \times 3 \times 2 \times 3 \times 3 = 74358$
- Again, the total combinations are too many. The question is **which combinations shall we cover?**



# Combination Problem: Case 3

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Unit under test is a Android application

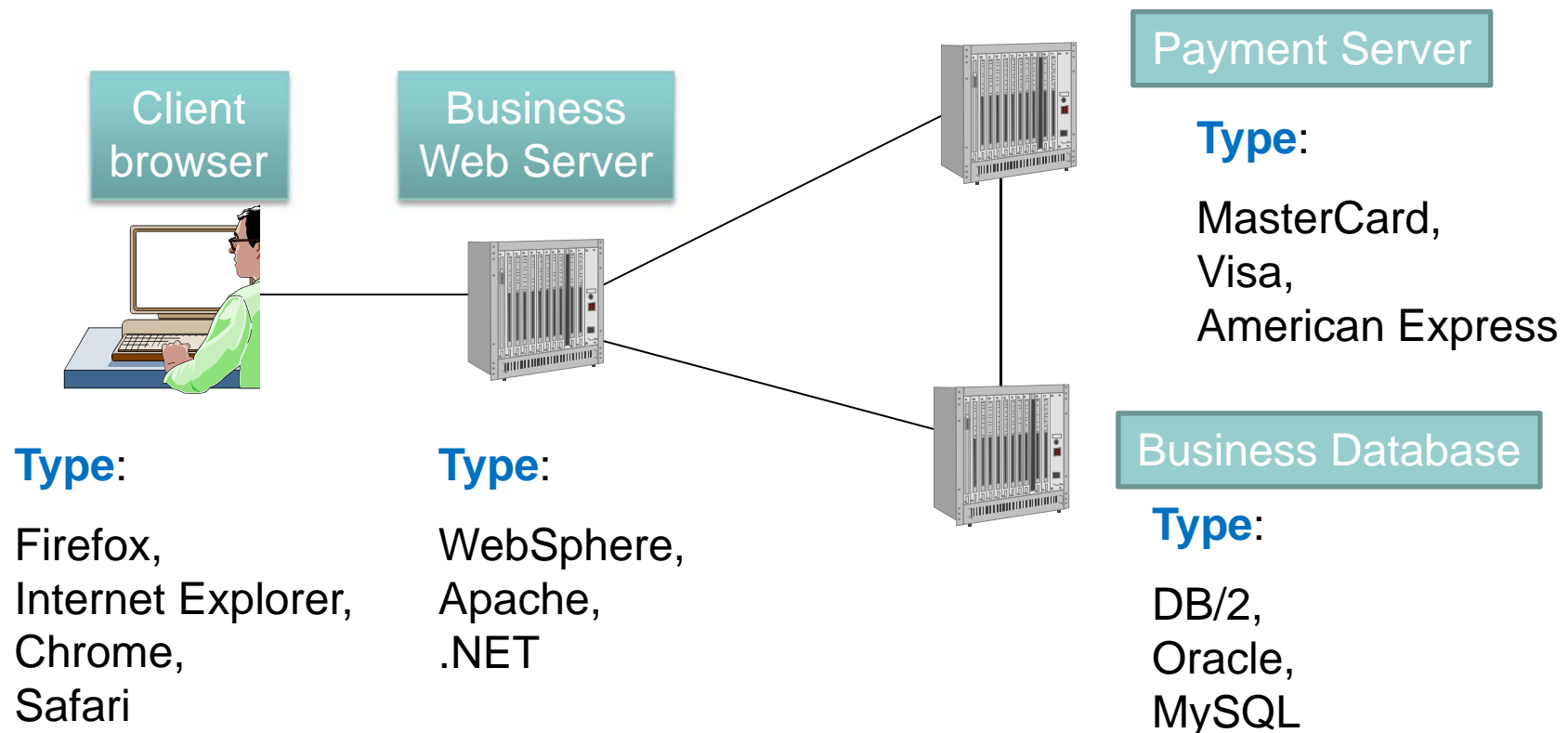
| Parameter Name            | Values                                   | # Values |
|---------------------------|--|----------|
| <b>HARDKEYBOARDHIDDEN</b> | NO, UNDEFINED, YES                       | 3        |
| <b>KEYBOARDHIDDEN</b>     | NO, UNDEFINED, YES                       | 3        |
| <b>KEYBOARD</b>           | 12KEY, NOKEYS, QWERTY, UNDEFINED         | 4        |
| <b>NAVIGATIONHIDDEN</b>   | NO, UNDEFINED, YES                       | 3        |
| <b>NAVIGATION</b>         | DPAD, NONAV, TRACKBALL, UNDEFINED, WHEEL | 5        |
| <b>ORIENTATION</b>        | LANDSCAPE, PORTRAIT, SQUARE, UNDEFINED   | 4        |
| <b>SCREENLAYOUT_LONG</b>  | MASK, NO, UNDEFINED, YES                 | 4        |
| <b>SCREENLAYOUT_SIZE</b>  | LARGE, MASK, NORMAL, SMALL, UNDEFINED    | 5        |
| <b>TOUCHSCREEN</b>        | FINGER, NOTOUCH, STYLUS, UNDEFINED       | 4        |

Total device configurations:  $3 \times 3 \times 4 \times 3 \times 5 \times 4 \times 4 \times 5 \times 4 = 172,800$

Which combinations shall we cover?

# Combination Problem: Case 4

- Unit under test is a B2C system.
- Total system configuration =  $4 \times 3 \times 3 \times 3 = 36$
- Which combinations shall we cover?



# Combination Problem: Case 5

Unit under test is a radar system with on-off switches. Software must produce the right response for any combination of switch settings:



Total switch settings:  $2^{34} = 1.7 \times 10^{10}$

Do you want to try testing all of them?

# Level-2 Techniques

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- **Combinatorial Coverage** (组合覆盖)
  - Adequacy criterion: cover each t-way interaction at least once
- **Constrained Combinatorial Coverage** (带约束的组合覆盖)
  - Adequacy criterion: combinatorial coverage subject to additional constraints between parameters

# Combinatorial Coverage: Definition

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- Let  $p$  be the number of parameters:
  - Parameters are indexed  $1, \dots, p$ .
- For each parameter  $i$ , suppose that there are  $n_i$  concerned values
  - These values are from the  $n_i$  equivalence classes & boundary cases of this parameter.
- t-way interactions** between parameters  $i, i+1, \dots, i+t-1$ : the  $n_i * n_{i+1} * \dots * n_{i+t-1}$  value combinations.
  - Assumption:** parameters are **independent**. That is, the choice of values for any parameter does not affect the choice of values for any other parameter.
  - We will remove this restriction later in *constrained combinatorial coverage*.
- t-wise (combinatorial) coverage**: cover all the t-way interactions between any set of  $t$  parameters.
  - Special case: pairwise (combinatorial) coverage -- covering all two-way interactions



# Example

- Suppose that we have three parameters, each of which has two possible values.
  - A, B for parameter 1.
  - J, K for parameter 2.
  - Y, Z for parameter 3.
- There are  $2^3 = 8$  possible **full combinations**.
- How about their two-way interaction?

|   |   |   |
|---|---|---|
| A | J | Y |
| A | J | Z |
| A | K | Y |
| A | K | Z |
| B | J | Y |
| B | J | Z |
| B | K | Y |
| B | K | Z |

# Pairwise Coverage

- Cover the  $C(3, 2) = 12$  two-way interactions.

Two-way interactions  
between parameter 1 and 2

|   |   |  |
|---|---|--|
| A | J |  |
| A | K |  |
| B | J |  |
| B | K |  |

Two-way interactions  
between parameter 1 and 3

|   |  |   |
|---|--|---|
| A |  | Y |
| A |  | Z |
| B |  | Y |
| B |  | Z |

Two-way interactions  
between parameter 2 and 3

|  |   |   |
|--|---|---|
|  | J | Y |
|  | J | Z |
|  | K | Y |
|  | K | Z |

# Full combination vs. 2-way Interaction

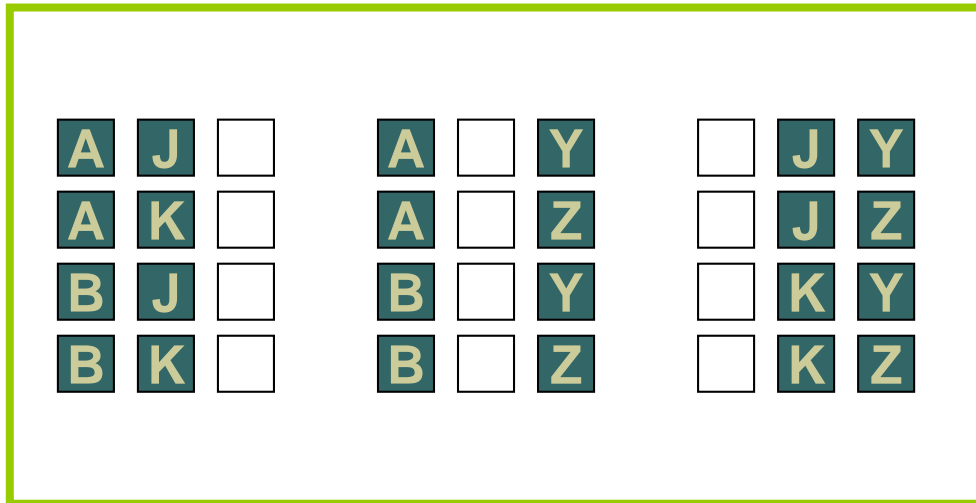
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One full combination...

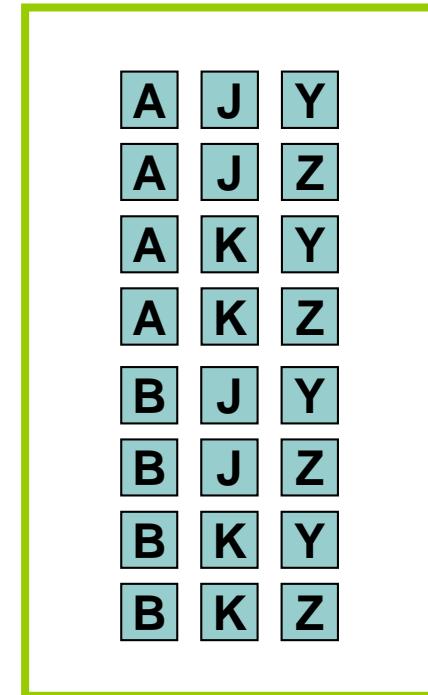
... covers 3 two-way interactions.

|   |   |   |
|---|---|---|
| A | J | Y |
| A | J |   |
| A |   | Y |
|   | J | Y |

# Pairwise Coverage



Goal: cover all two-way interactions...



...using a subset of full combinations.

# Why (only) Two-way Interaction?

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- Fault analysis reveals that two-way interaction between parameters is a common source of failure in complex systems.

Meanwhile....

- The number of test cases required to cover all *t*-way interactions grows exponentially with *t*.

Number of combinations needed to cover all *t*-way interactions:  $O(v^t \log n)$

for *v* values, *n* variables, *t*-way interactions

# Evidence

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- **Case 1:** Evaluation of FDA recall class failures in medical devices: **98% of the problems** could have been detected by testing the device with all pairs of parameter settings.

*Reference: D. R. Wallace and D. R. Kuhn, 2001. The Effectiveness of Combinatorial Testing.*

- **Case 2:** Mozilla web browser defect study: **75% of the faults** can be exposed by covering the two-way interactions between parameters.

*Reference: Pairwise Testing: A Best Practice That Isn't:*

<http://www.testingeducation.org/wtst5/PairwisePNSQC2004.pdf>

- **Case 3:** AT&T email system defect study: the 1000 test cases that satisfy pairwise coverage expose **20% more defects** than the 1500 test cases that were designed originally in an ad hoc way.

# Real World Example

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- F-16 fighter failure caused by the interaction between the location of LANTIRN pod and that of ventral fin.



Figure 1. LANTIRN pod carriage on the F-16.

Information from a US AIR FORCE INSTITUTE OF TECHNOLOGY report:

<http://www.dtic.mil/cgi-bin/GetTRDoc?Location=U2&doc=GetTRDoc.pdf&AD=ADA506375>

# Selecting Test Cases for Pairwise Coverage

## Covered two-way Interactions

|          |          |  |          |  |          |  |  |          |          |
|----------|----------|--|----------|--|----------|--|--|----------|----------|
| <b>A</b> | <b>J</b> |  | <b>A</b> |  | <b>Y</b> |  |  | <b>J</b> | <b>Y</b> |
| A        | K        |  | A        |  | Z        |  |  | J        | Z        |
| B        | J        |  | B        |  | Y        |  |  | K        | Y        |
| B        | K        |  | B        |  | Z        |  |  | K        | Z        |

coverage:  $3 / 12 = 25\%$

## Full combinations (test cases)

|          |          |          |
|----------|----------|----------|
| <b>A</b> | <b>J</b> | <b>Y</b> |
| A        | J        | Z        |
| A        | K        | Y        |
| A        | K        | Z        |
| B        | J        | Y        |
| B        | J        | Z        |
| B        | K        | Y        |
| B        | K        | Z        |



# Selecting Test Cases for Pairwise Coverage

Covered two-way Interactions

|   |   |  |   |  |   |  |   |   |
|---|---|--|---|--|---|--|---|---|
| A | J |  | A |  | Y |  | J | Y |
| A | K |  | A |  | Z |  | J | Z |
| B | J |  | B |  | Y |  | K | Y |
| B | K |  | B |  | Z |  | K | Z |

coverage:  $6 / 12 = 50\%$

Full combinations  
(test cases)

|   |   |   |
|---|---|---|
| A | J | Y |
| A | J | Z |
| A | K | Y |
| A | K | Z |
| B | J | Y |
| B | J | Z |
| B | K | Y |
| B | K | Z |

# Selecting Test Cases for Pairwise Coverage

Covered two-ways Interactions

|   |   |  |   |  |   |  |   |   |
|---|---|--|---|--|---|--|---|---|
| A | J |  | A |  | Y |  | J | Y |
| A | K |  | A |  | Z |  | J | Z |
| B | J |  | B |  | Y |  | K | Y |
| B | K |  | B |  | Z |  | K | Z |

coverage:  $9 / 12 = 75\%$

Full combinations  
(test cases)

|   |   |   |
|---|---|---|
| A | J | Y |
| A | J | Z |
| A | K | Y |
| A | K | Z |
| B | J | Y |
| B | J | Z |
| B | K | Y |
| B | K | Z |

# Selecting Test Cases for Pairwise Coverage

Covered two-ways Interactions

|   |   |  |   |  |   |  |   |   |
|---|---|--|---|--|---|--|---|---|
| A | J |  | A |  | Y |  | J | Y |
| A | K |  | A |  | Z |  | J | Z |
| B | J |  | B |  | Y |  | K | Y |
| B | K |  | B |  | Z |  | K | Z |

coverage:  $12 / 12 = 100\%$

Full combinations  
(test cases)

|   |   |   |
|---|---|---|
| A | J | Y |
| A | J | Z |
| A | K | Y |
| A | K | Z |
| B | J | Y |
| B | J | Z |
| B | K | Y |
| B | K | Z |

# Finding pairwise adequate test cases

---

**Question:** how to cover all two-way interactions with **the fewest number of test cases?**

# Transform the Problem

|     | AJY   | AJZ    | AKY    | AKZ    | BJY    | BJZ    | BKY    | BKZ    |          |
|-----|-------|--------|--------|--------|--------|--------|--------|--------|----------|
| A J | $x_1$ | $+x_2$ |        |        |        |        |        |        | $\geq 1$ |
| A   | $x_1$ |        | $+x_3$ |        |        |        |        |        | $\geq 1$ |
|     | $x_1$ |        |        |        | $+x_5$ |        |        |        | $\geq 1$ |
| A K |       |        | $x_3$  | $+x_4$ |        |        |        |        | $\geq 1$ |
| A   |       | $x_2$  |        | $+x_4$ |        |        |        |        | $\geq 1$ |
|     |       | $x_2$  |        |        |        | $+x_6$ |        |        | $\geq 1$ |
| B J |       |        |        |        | $x_5$  | $+x_6$ |        |        | $\geq 1$ |
| B   |       |        |        |        | $x_5$  |        | $+x_7$ |        | $\geq 1$ |
|     |       |        | $x_3$  |        |        |        | $+x_7$ |        | $\geq 1$ |
| B K |       |        |        |        |        |        | $x_7$  | $+x_8$ | $\geq 1$ |
| B   |       |        |        |        |        | $x_6$  |        | $+x_8$ | $\geq 1$ |
|     |       |        |        | $x_4$  |        |        |        | $+x_8$ | $\geq 1$ |

Minimize:  $x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 + x_8;$   $x_i \in \{0,1\}$

# Classic $\{0,1\}$ -integer programming

- Solution of  $\{0,1\}$ -integer programming is an NP-complete problem.
- But there are still plenty of (fast enough) tools to address it (e.g. the NEOS online solver: <http://www.neos-server.org/neos/> or the bintprog function in Matlab)
- A little experiment for extra solutions:

| # Params | # Values per param | # Constraints | # Interactions | Result: # combinations | Run time (s) |
|----------|--------------------|---------------|----------------|------------------------|--------------|
| 3        | 2                  | 12            | 8              | 4                      | <0.01        |
| 4        | 2                  | 24            | 16             | 5                      | 0.01         |
| 5        | 2                  | 40            | 32             | 6                      | 0.70         |
| 6        | 2                  | 60            | 64             | 6                      | 16.57        |
| 7        | 2                  | 84            | 128            | 6                      | 441.21       |
| 4        | 3                  | 54            | 81             | 9                      | 0.08         |
| 5        | 3                  | 90            | 243            | *                      | *            |

\* process killed after running for 6.5 hours

Besides, one or two extra test cases will not kill us – A greedy algorithm is usually good enough.

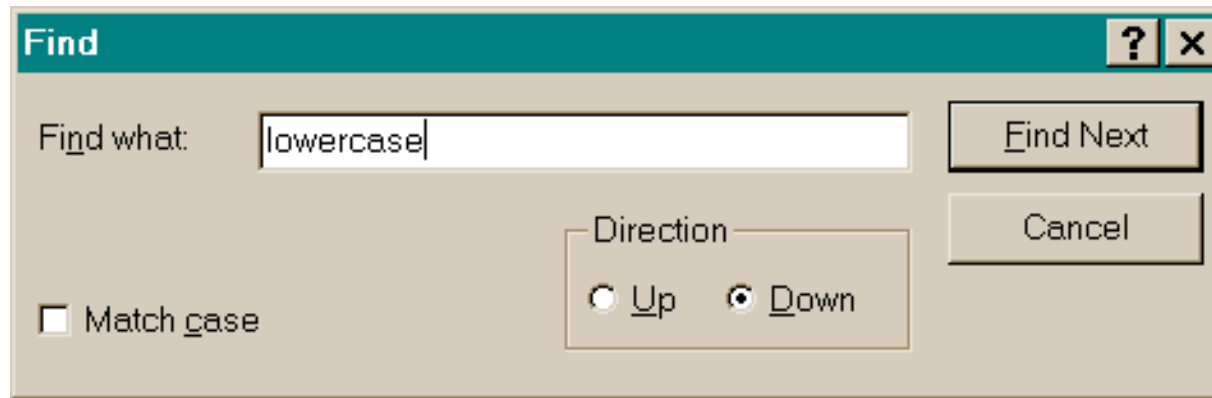
# Greedy Algorithm

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- **Input:**  $N$  parameters  $x_1, x_2, \dots, x_N$ , with  $v_1, v_2, \dots, v_N$  values, respectively.
- **Output:**  $K$  combinations of the values of  $x_1, x_2, \dots, x_N$  that achieve two-ways interactions
- Initialize the result set as empty
- For each parameter  $x_i$  ( $i$  in  $[0, N-1]$ ),
  - For each of the  $v_i * v_{i+1}$  interactions between the  $v_i$  values of  $x_i$  and  $v_{i+1}$  values of  $x_{i+1}$ ,
    - If the interaction has been covered by one of the combinations in the result set, ignore it.
    - Otherwise, create a combination that cover this interaction and the most amount of interactions not yet covered.
- Return the result set.

# Quiz 1: Pairwise Coverage

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- Test a simple Find dialog. It takes three inputs:
  - Find what: a text string.
  - Match case: yes or no
  - Direction: up or down
- For the text string, consider three values: “lowercase” and “Mixed Cases” and “CAPITALS”.
- Total combinations:  $2 \times 2 \times 3 = 12$
- What are the combinations that satisfy pairwise coverage?
  - LYD, MYU, CYD, LNU, MND, CNU



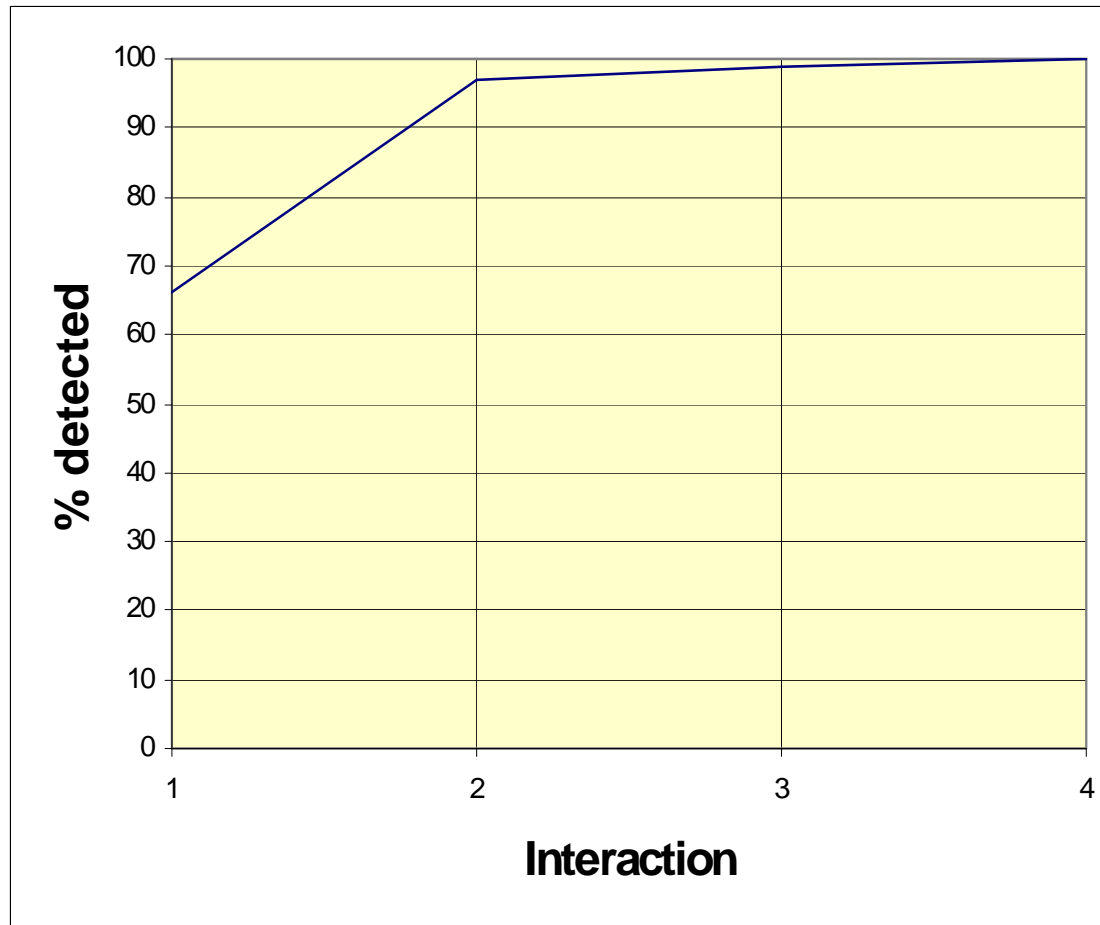
# From Pairwise to T-wise Coverage

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- The only obstacle is the *cost*.
  - Recall that the number of test cases needed to cover all  $t$ -way interactions is  $O(v^t \log n)$  for  $v$  values,  $n$  variables
  - However, depends on the actual system, the growth on  $t$  might not be as high as exponential.
- The key issue is whether the benefit justifies the cost.

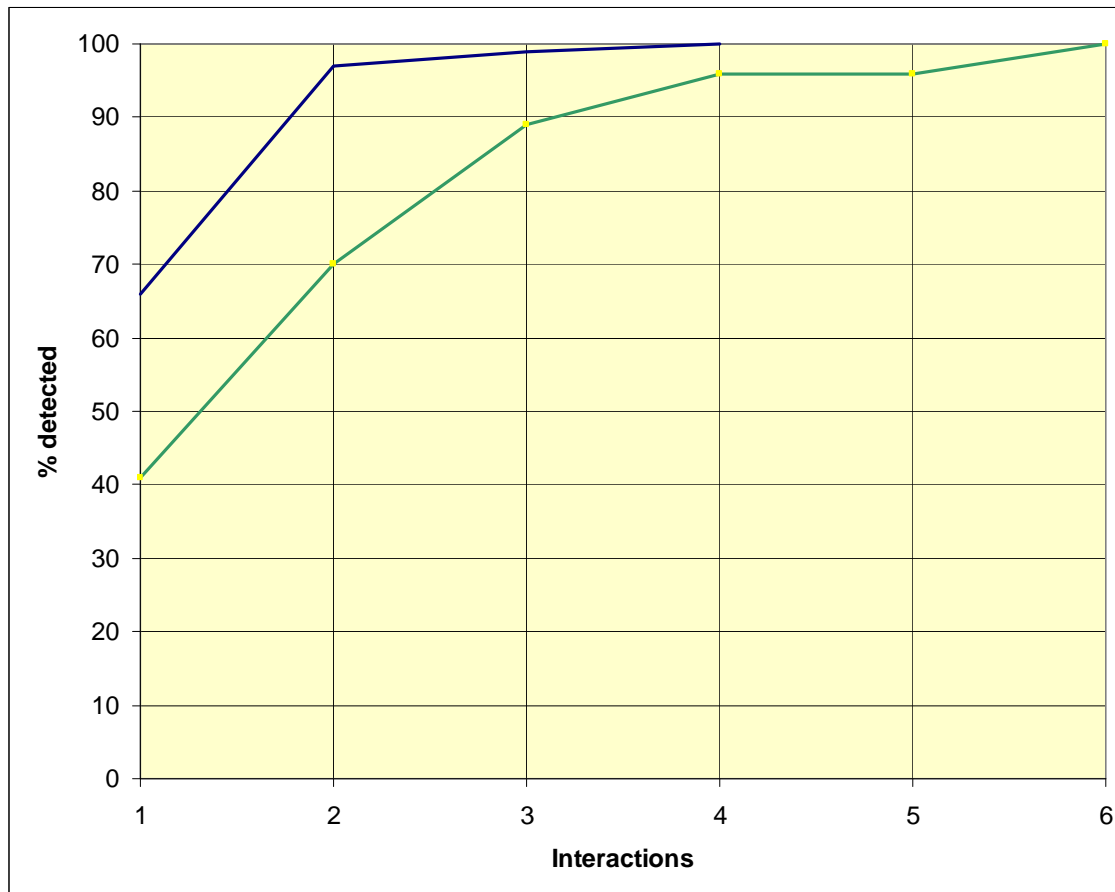
# Empirical Study by

## Medical device



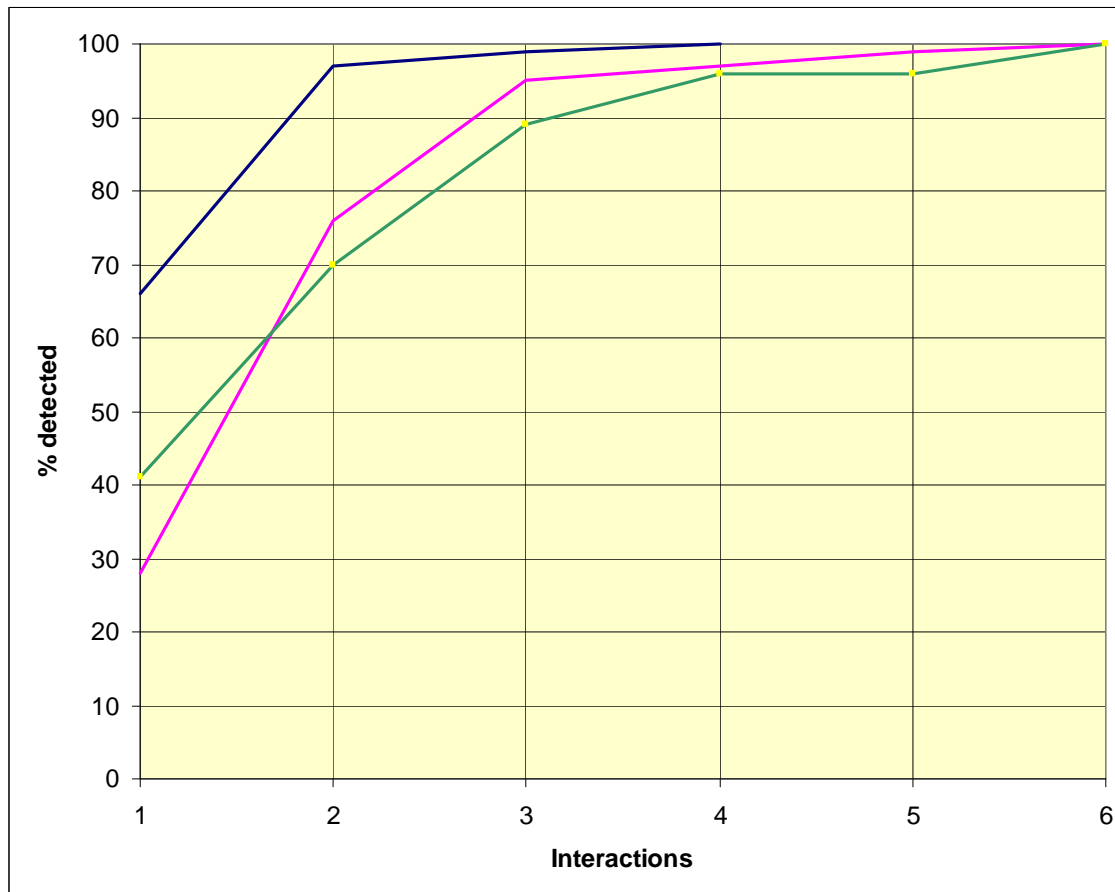
# Empirical Study by

## Server (green)



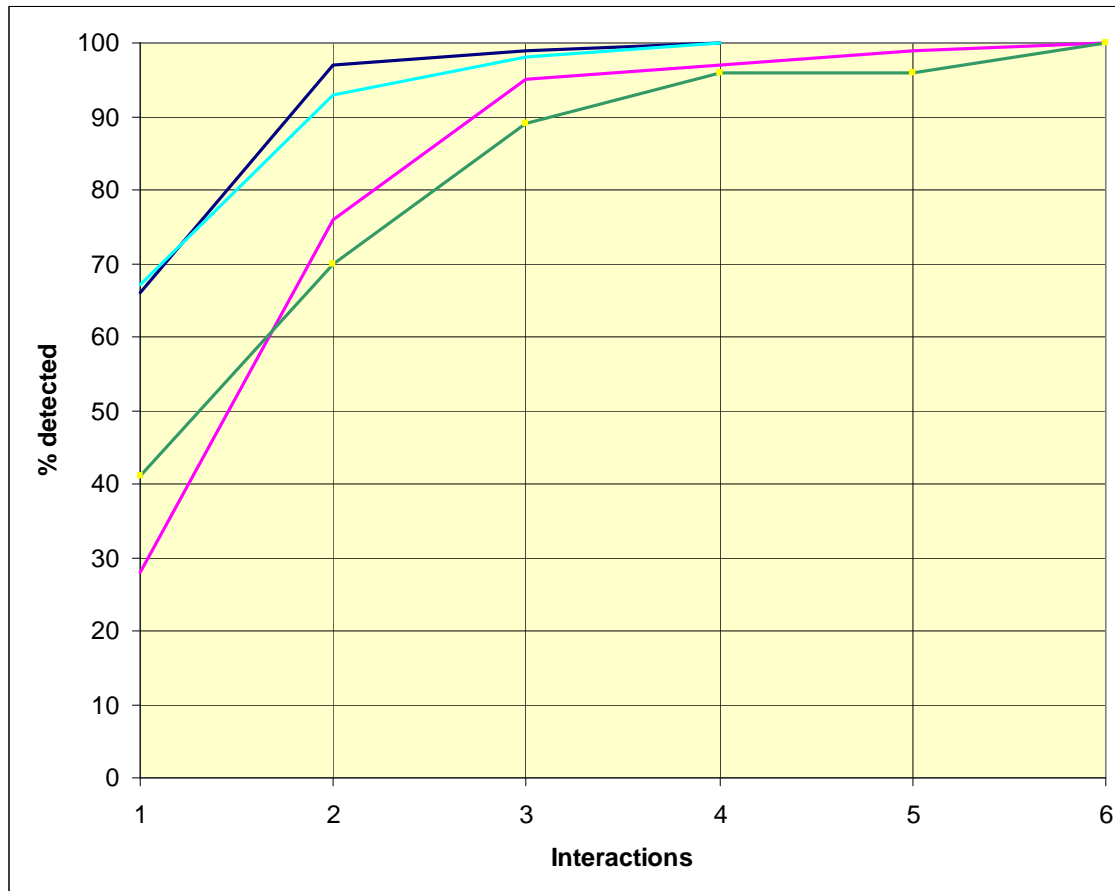
# Empirical Study by

## Browser (magenta)



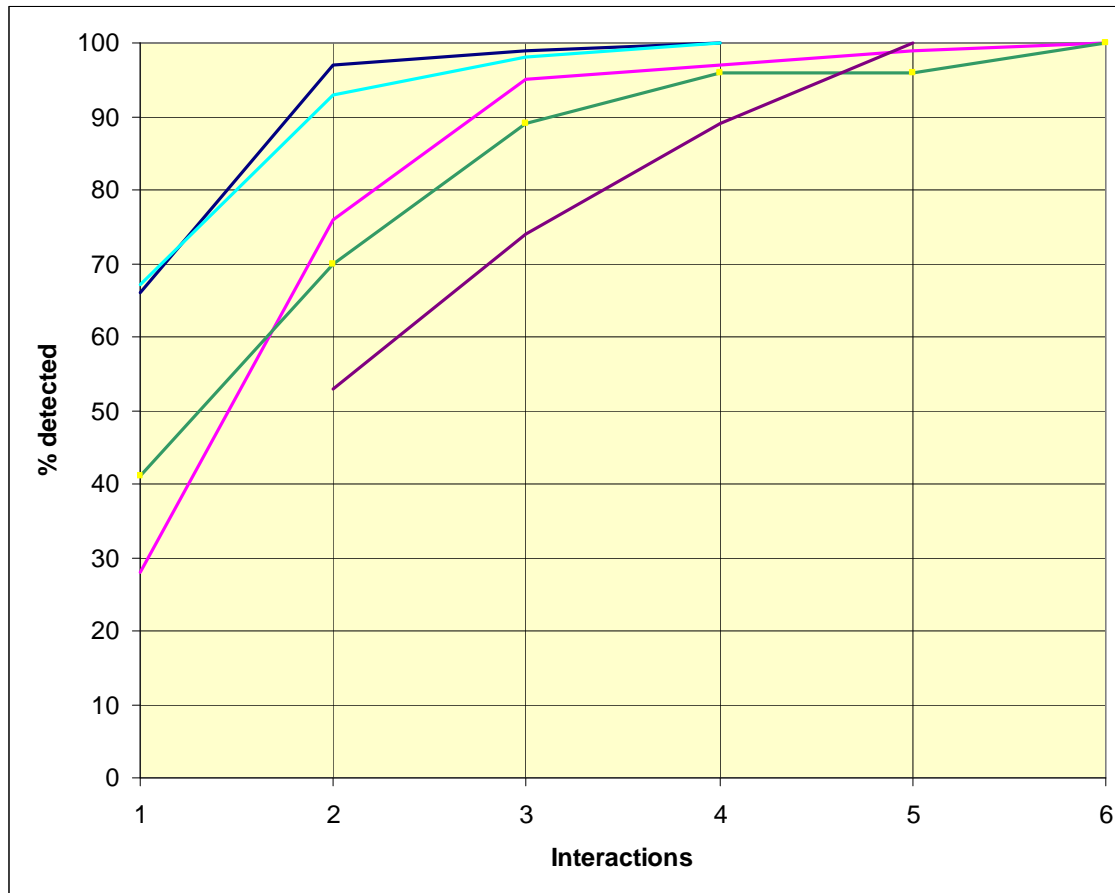
# Empirical Study by

NASA Goddard distributed database (light blue)



# Empirical Study by

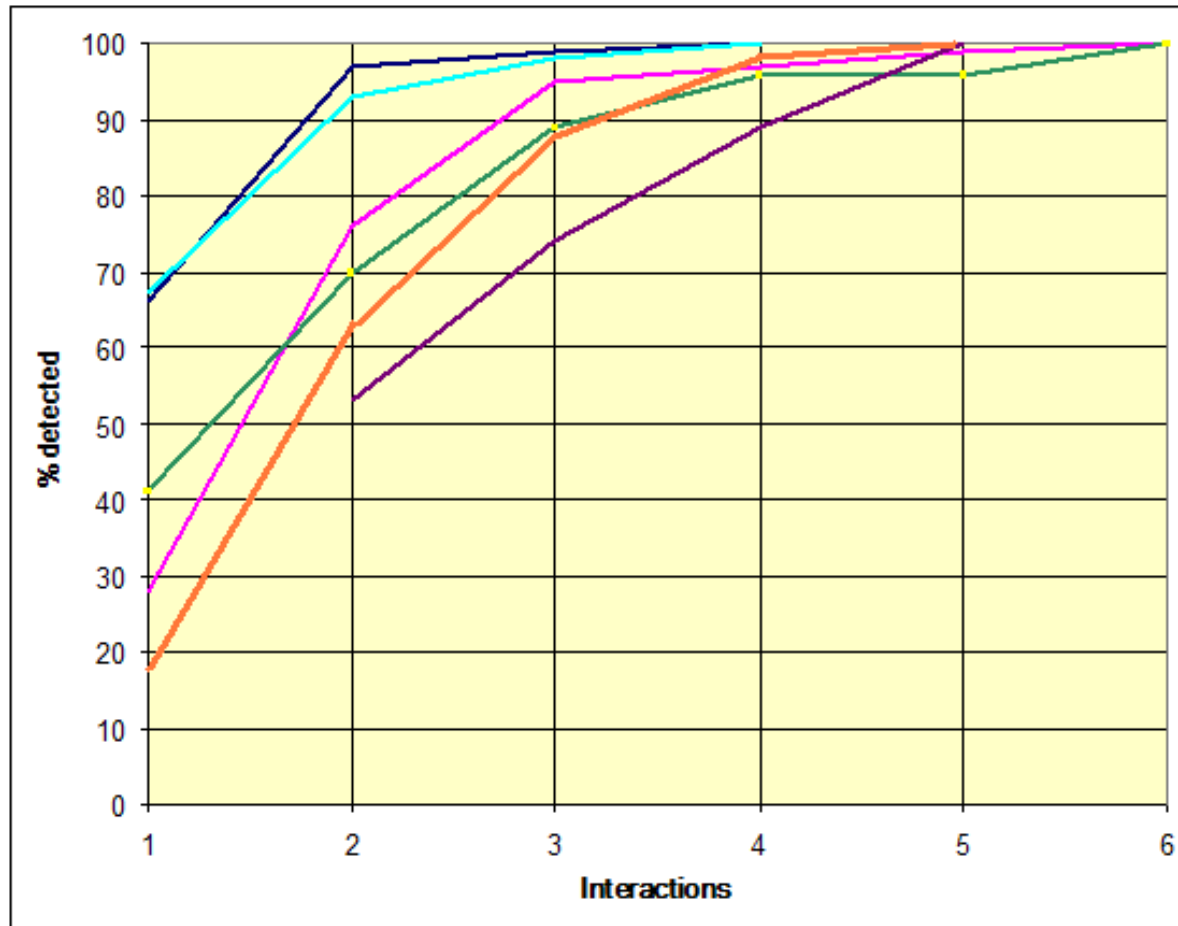
## FAA Traffic Collision Avoidance System module (purple)



# Empirical Study by

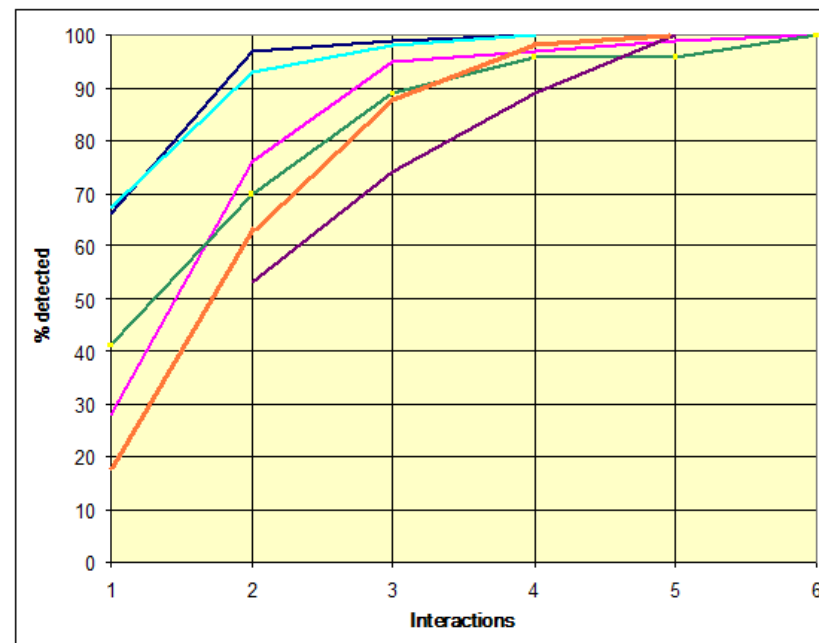


Network security (Bell, 2006) (orange)



# So what?

- As suggested from 《How we test software at Microsoft》 :
  - Pairwise coverage as the base line.
  - Time allowed, improve the test suite to 3~6-wise combinatorial coverage.
- It is generally agreed that there is little benefit beyond 6-wise combinatorial coverage.





# Tool 1: ACTS

<http://csrc.nist.gov/groups/SNS/acts/>

- Developed by NIST. Free for academic use. But need to write an email to ask for the software. (The course website provides a link to a local copy)
- Support 2~6-way coverage (called 'strength of interaction')
- Allow for mixed strength: e.g. cover 2-way for all, 3-way for a selected subset of parameters.

**New System Form**

Parameters Relations Constraints

**System Name** TCAS

**System Parameter**

Parameter Name

Parameter Type Boolean

**Parameter Values**

Selected Parameter Boolean

Simple Value

Range Value 0 3

true,false

Add-> Remove->

Add to Table

Add System Cancel

**Saved Parameters**

| Parameter Name       | Parameter Value                 |
|----------------------|---------------------------------|
| Cur_Vertical_Sep     | [299,300,601]                   |
| High_Confidence      | [true,false]                    |
| Two_of_Three_Reports | [true,false]                    |
| Own_Tracked_Alt      | [1,2]                           |
| Other_Tracked_Alt    | [1,2]                           |
| Own_Tracked_Alt_Rate | [600,601]                       |
| Alt_Layer_Value      | [0,1,2,3]                       |
| Up_Separation        | [0,399,400,499,500,639,640,7... |
| Down_Separation      | [0,399,400,499,500,639,640,7... |
| Other_RAC            | [NO_INTENT,DO_NOT_CLIMB,...]    |
| Other_Capability     | [TCAS_CA,Other]                 |
| Climb_Inhibit        | [true,false]                    |

Remove Modify

# Tool 2: PICT from Microsoft

<http://download.microsoft.com/download/f/5/5/f55484df-8494-48fa-8dbd-8c6f76cc014b/pict33.msi>

- Command line tool to generate T-way coverage test suite.
  - If T=2 (default) then it is pairwise coverage.
- Example input: test.txt

**Type:** Primary, Logical, Single, Span, Stripe, Mirror, RAID-5  
**Size:** 10, 100, 500, 1000, 5000, 10000, 40000  
**Format:** quick, slow  
**File system:** FAT, FAT32, NTFS  
**Cluster size:** 512, 1024, 2048, 4096, 8192, 16384, 32768, 65536  
**Compression:** on, off

Also support  
mixed strength  
with ***Sub-Models***

- Output of “pict /o:2 test.txt”

| Type    | Size  | Format | File system | Cluster size | Compression |
|---------|-------|--------|-------------|--------------|-------------|
| Primary | 40000 | quick  | NTFS        | 1024         | off         |
| Span    | 100   | slow   | FAT32       | 16384        | on          |
| RAID-5  | 500   | quick  | FAT         | 4096         | on          |
| Primary | 5000  | slow   | FAT32       | 4096         | off         |
| RAID-5  | 1000  | slow   | FAT         | 32K          | on          |
| Stripe  | 500   | slow   | NTFS        | 2048         | on          |
| RAID-5  | 10    | quick  | FAT32       | 2048         | on          |
| Primary | 10    | slow   | FAT         | 1024         | on          |
| Logical | 100   | quick  | NTFS        | 32768        | on          |
| Primary | 5000  | quick  | NTFS        | 512          | off         |
| Span    | 500   | slow   | FAT32       | 32768        | off         |
| Mirror  | 5000  | slow   | NTFS        | 64096        | on          |
| RAID-5  | 100   | slow   | NTFS        | 4096         | off         |
| RAID-5  | 10    | slow   | FAT         | 512          | on          |
| Logical | 1000  | quick  | FAT32       | 8192         | on          |
| Logical | 100   | quick  | NTFS        | 4096         | off         |
| Single  | 10000 | quick  | FAT         | 65536        | off         |

# Tool 3: Category-Partition Testing

---

- Proposed by Ostrand and Balcer in a 1988 CACM paper.
  - The input language is called TSL (Test Specification Language). We will use TSL to refer to category-partition testing and the tool.
  - The resource page on our SE-307 course website provides the source code of the tool.
  - We will use this tool in assignment #3.
- Why not ATCS or PICT in assignment #3? Because:
  - 1) we have the source code of the tool, so that you might modify it for your own tasks in the future (the importance of open source).
  - 2) it supported more sophisticated constraints on the parameters, as we will see later.
- One problem, though, is that the tool only generates **all** feasible combinations. It is up to you to select a subset to achieve t-wise combinatorial coverage.

# TSL in a nutshell

---

- Parameters are called **categories** in TSL, while the values of parameter are grouped into **choices**.
  - The original paper discuss two kinds of categories: *parameters* and *environments*. They are handled in the exactly same way in the tool.
  - Choices are strings that describe equivalence classes & boundary cases of the parameters.
    - This is different from ACTS and PICT. They use concrete values. This is not an essential difference, though.

# Example: "find" command in Linux

---

- Syntax: `find <Pattern> <file>`
- Function:
  - Locate one or more instances of a given pattern in a text file. All lines in the file that contains the pattern are printed. A line containing the pattern is written only once, regardless of the number of occurrence.
- Pattern:
  - The pattern is any string whose length does not exceed the maximum length of a line in the file. It can be quoted or unquoted. To include a blank in the pattern, the entire pattern must be enclosed in quotes `"`. To include the quotation mark in the pattern, two consecutive quotes must be used.
- Examples:
  - `find john myfile` displays lines that contains john
  - `find "john smith" myfile` displays lines that contains john smith
  - `find "john" " smith" myfile` displays lines that contain john" smith

# TSL for **find**

---

**Parameters:****Pattern size:**

- empty
- single character
- many character
- longer than any line in the file

**Quoting:**

- pattern is quoted
- pattern is not quoted
- pattern is improperly quoted

**Embedded blanks:**

- no embedded blank
- one embedded blank
- several embedded blanks

**Embedded quotes:**

- no embedded quotes
- one embedded quote
- several embedded quotes

**File name:**

- good file name
- no file with this name
- omitted

**Environments:****Number of occurrences of pattern in file:**

- none
- exactly one
- more than one

**Pattern occurrences on target line:**

- # assumes line contains the pattern
- one
- more than one

# TSL for **find**

## Parameters:

### Pattern size:

- empty
- single character
- many character
- longer than any line in the file

### Quoting:

- pattern is quoted
- pattern is not quoted
- pattern is improperly quoted

### Embedded blanks:

- no embedded blank
- one embedded blank
- several embedded blanks

### Embedded quotes:

- no embedded quotes
- one embedded quote
- several embedded quotes

### File name:

- good file name
- no file with this name
- omitted

## Environments:

### Number of occurrences of pattern in file:

- none
- exactly one
- more than one

### Pattern occurrences on target line:

- # assumes line contains the pattern
- one
- more than one

parameter (**category**)

## Notes:

Environments describe “indirect” parameter. In the tool they are handled in exactly the same way as the “direct” parameter.

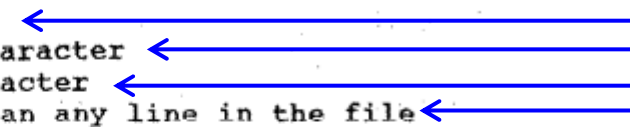


# TSL for **find**

## Parameters:

### Pattern size:

empty  
single character  
many character  
longer than any line in the file



equivalence classes and  
boundary cases of the  
parameter **(choices)**

### Quoting:

pattern is quoted  
pattern is not quoted  
pattern is improperly quoted

### Embedded blanks:

no embedded blank  
one embedded blank  
several embedded blanks

### Embedded quotes:

no embedded quotes  
one embedded quote  
several embedded quotes

### File name:

good file name  
no file with this name  
omitted

## Environments:

### Number of occurrences of pattern in file:

none  
exactly one  
more than one

### Pattern occurrences on target line:

# assumes line contains the pattern  
one  
more than one

## Notes:

ACTS and PICT use *actual values*,  
while TSL use *classes*.

This is a fundamental difference: by  
using classes as choices for parameter,  
TSL allow us to describe the real parameter  
with multiple “virtual parameters”.



# TSL for **find**

## Parameters:

### Pattern size:

empty  
single character  
many character  
longer than any line in the file

### Quoting:

pattern is quoted  
pattern is not quoted  
pattern is improperly quoted

### Embedded blanks:

no embedded blank  
one embedded blank  
several embedded blanks

### Embedded quotes:

no embedded quotes  
one embedded quote  
several embedded quotes

### File name:

good file name  
no file with this name  
omitted

## Environments:

### Number of occurrences of pattern in file:

none  
exactly one  
more than one

### Pattern occurrences on target line:

# assumes line contains the pattern  
one  
more than one

- **Note:** a complex parameter can be described by multiple “virtual parameters”.
  - The real parameter “pattern” is described by “pattern size”, “quoting”, etc.
  - The real parameter “file” is described by “filename”, “number of pattern occurrence in the file”, etc.
- Another possible way to handle complex parameter: use cause-effect graph to generate equivalence classes:
  - Try it yourselves and think about the pros and cons of each method.

# Where does TSL come from?

## Parameters:

### Pattern size:

empty  
single character  
many character  
longer than any line in the file

### Quoting:

pattern is quoted  
pattern is not quoted  
pattern is improperly quoted

### Embedded blanks:

no embedded blank  
one embedded blank  
several embedded blanks

### Embedded quotes:

no embedded quotes  
one embedded quote  
several embedded quotes

### File name:

good file name  
no file with this name  
omitted

## Environments:

### Number of occurrences of pattern in file:

none  
exactly one  
more than one

### Pattern occurrences on target line:

# assumes line contains the pattern  
one  
more than one

## From the requirement

### Function:

Locate one or more instances of a given pattern in a text file. All lines in the file that contains the pattern are printed. A line containing the pattern is written only once, regardless of the number of occurrence.

### Pattern:

The pattern is any string whose length does not exceed the maximum length of a line in the file. It can be quoted or unquoted. To include a blank in the pattern, the entire pattern must be enclosed in quotes ". To include the quotation mark in the pattern, two consecutive quotes must be used.

# Running the tool on TSL

---

- Generated all feasible combinations of choices. Each combination is called a “test frame”
- A test frame for `find`:

```
Pattern size : empty
Quoting : pattern is quoted
Embedded blanks : several embedded blanks
Embedded quotes : no embedded quotes
File name : good file name
Number of occurrences of pattern in file : none
Pattern occurrences on target line : one
```

- Test frame is not test case. You need another tool to generate a test case from a test frame.
- In the original category-partition method, it is done manually as it is domain-specific.

# Level-2 Techniques

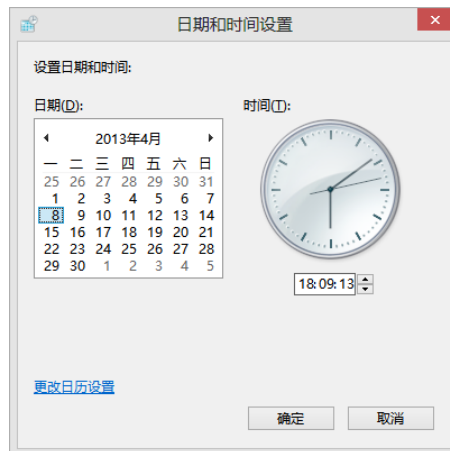
---

- **Combinatorial Coverage** (组合覆盖)
  - Adequacy criterion: cover each t-way interaction at least once
- **Constrained Combinatorial Coverage** (带约束的组合覆盖)
  - Adequacy criterion: combinatorial coverage subject to additional constraints between parameters

# Why Constraints?

- **Reason 1:** rule out *infeasible* (不可能) combinations
  - They are impossible to input through user interface.
  - Need to differentiate *infeasible* (不可能) from *invalid* (非法).
    - e.g. the combination year=2013, month=2, day=30.

infeasible



invalid



VS.

- Rule out *infeasible combinations*, not *invalid combinations*.
  - On the contrary, we shall deliberately insert invalid combination into the pairwise-coverage test suite, if they have not been covered.

# Why Constraints?

---

- **Reason 1:** rule out *infeasible* (不可能) combinations
  - Especially important for TSL.

Consider this test frame:

Pattern size : empty

Quoting : pattern is quoted

Embedded blanks : several embedded blanks

Embedded quotes : no embedded quotes

File name : good file name

Number of occurrences of pattern in file : none

Pattern occurrences on target line : one

# Why Constraints?

---

- **Reason 2:** rule out *redundant* (冗余) combinations
  - Some values of one parameter might trigger the system to bypass whatever values the other parameters take.

Example:

```
public static void main (String args[]) {  
    if (args.length > 2) {  
        Quit.now("Usage: java STS attributes.txt [s|st|ts|t]");  
    }  
    ...  
}
```

We only need one parameter combination with `args.length>2`. Others are all redundant, as they exercise exactly the same behavior of the program.

- Constraints can be used to rule out redundant combinations and reduce the size of test suite.

# Introducing Constraints

---

- Be careful!
  - Some combinations might NOT be really infeasible or redundant, as you believe.
  - Suggestion: think twice before introducing constraints.
- Types of constraints:
  - Property constraints: rule out infeasible combinations
  - Error/single constraints: rule out redundant combinations



# Property Constraints

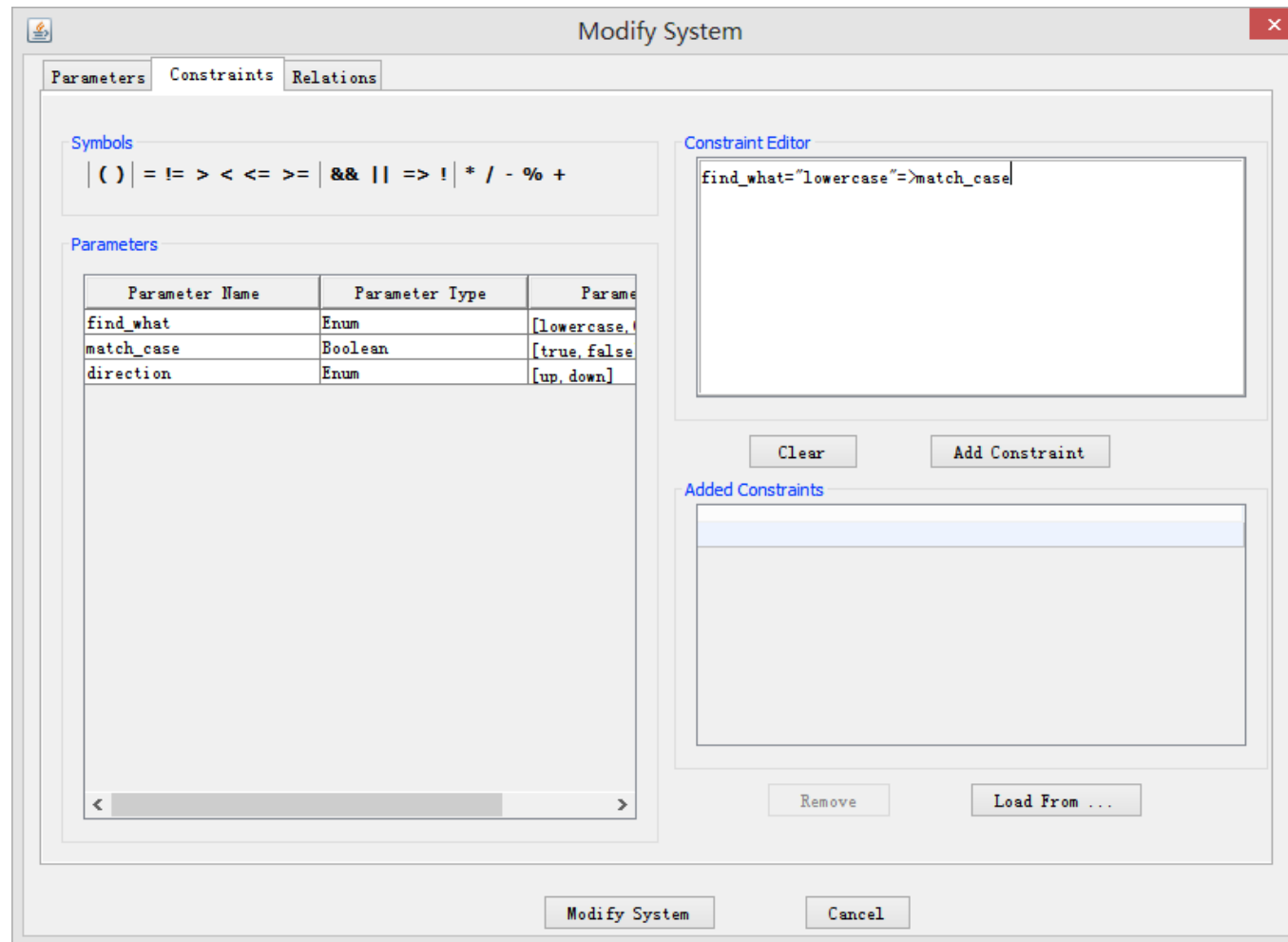
---

- Typically expressed using first-order logic
  - The tools will not generate combinations that make these constraints false.
  - e.g. `not (month=February and day>=30)`
  - e.g. `if find_what = lowercase then match_case = true`
- ACTS, PICT, and TSL all support property constraints

|                              |                |  |      |  |     |  |     |  |             |
|------------------------------|----------------|--|------|--|-----|--|-----|--|-------------|
| <b>&lt;Boolean_Op&gt;</b>    | <b>:=</b> "&&" |  | " "  |  | ">" |  |     |  |             |
| <b>&lt;Relational_Op&gt;</b> | <b>:=</b> "="  |  | "!=" |  | ">" |  | "<" |  | ">="   "<=" |
| <b>&lt;Arithmetic_Op&gt;</b> | <b>:=</b> "+"  |  | "-"  |  | "*" |  | "/" |  | "%"         |

# Property Constraints in ATCS

- Example: `find_what="lowercase"=>match_case`



# Property Constraints in PICT

---

- Essentially the same with ATCS
- Minor differences:
  - ACTS:  $a \neq b$       PICT:  $[a] \neq [b]$
  - ACTS:  $A \Rightarrow B$       PICT: IF A THEN B
  - PICT additionally supports IF A THEN B ELSE C
  - PICT directly supports set operation.  
e.g. IF  $[a] \in \{12, 24\}$  THEN  $[\text{compress}] = \text{"true"}$
  - In ACTS, you need to use  $a=12 \mid a=24$  instead.

# Property Constraints in TSL

---

- Use [**property** ...] and [**if** ...] to express property constraints

Example 1:

P1:

c1. [**property** p1]

P2:

c2. [**if** p1]

mean  $P2=c2 \Rightarrow P1=c1$

That is, a combination with  $P2=c2$  but  $P1 \neq c1$  is infeasible

# Property Constraints in TSL

---

- Use [**property** ...] and [**if** ...] to express property constraints

Example 2:

P1:

c1. [**property** p1]

P2:

c2. [**property** p1]

P3:

c3. [**if** p1]

mean  $P3=c3 \Rightarrow (P1=c1 \mid \mid P2=c2)$

That is, a combination with  $P3=c3$  but  $P1 \neq c1$  and  $P2 \neq c2$  is infeasible

# Property Constraints in TSL

---

- Use [**property** ...] and [**if** ...] to express property constraints

Example 3:

P1:

c1. [**property** p1]

P2:

c2. [**property** p2]

P3:

c3. [**if** p1 && p2]

mean  $P3=c3 \Rightarrow (P1=c1 \ \&\& \ P2=c2)$

That is, a combination with  $P3=c3$  but  $P1 \neq c1$  or  $P2 \neq c2$  is infeasible

# Property Constraints in TSL

---

- Use [**property** ...] and [**if** ...] to express property constraints

Example 4:

P1:

c1. [**property** p1]

P2:

c2. [**property** p2]

P3:

c3. [**if** p1 || p2]

mean  $P3=c3 \Rightarrow (P1=c1 \ || \ P2=c2)$

The same with example 2!



# Error/Single Constraints

---

- Error/single constraint is usually expressed as a *label* on a value or a class of the parameter.
- It means that we need only one of the combinations that covers this value/class, regardless of interaction strength.
  - The difference between error constraint and single constraint is conceptual only – the former rules out redundancy caused by invalid input, the latter by valid input.
  - The tools handle them in the same way.

- Example:

```
public static void main (String args[]) {  
    if (args.length > 2) {  
        Quit.now("Usage: java STS attributes.txt [s|st|ts|t]");  
    }  
}
```

We shall label the class “args.length>2” with an error constraint.

# Error/Single Constraints in PICT

---

- Use '~' as the label

- Example:

`parameter1: ~-1, 0, 1, 2`

means that whenever parameter1 takes the value of -1, the system will report an error and stop. Therefore, we only need to cover one of the combinations in which parameter1 is -1 – it is pointless to try more as the system does not use the other parameters when parameter1 is -1.

- **Note:** ATCS does not support error/single constraints

# Error/Single Constraints in TSL

---

- Use [**single**] and [**error**] as the label.
- Much more sophisticated, as they can be used with property constraints to express *conditional error/single constraints*
  - Not possible with PICT and ATCS.

- Example:

P1 :

c1. [**property** p1]

P2 :

c2. [**if** p1] [**else**] [**error**]

means combinations with  $P1 \neq c1$  and  $P2 = c2$  are invalid combinations (but feasible!) that trigger the system to report error and stop. We only need one of them in the test suite.

# How the Tool Works

---

- **Step 1:** Read the TSL specification.
- **Step 2:** Generate test frames that satisfy [single]/[error] constraints.
- **Step 3:** Generate test frames that do not satisfy any [single]/[error] constraints

```
/* Generate the frames according to what flags are set */
int generator( Flag flags )
{
    count_only = flags & COUNT_ONLY;
    num_frames = 0;

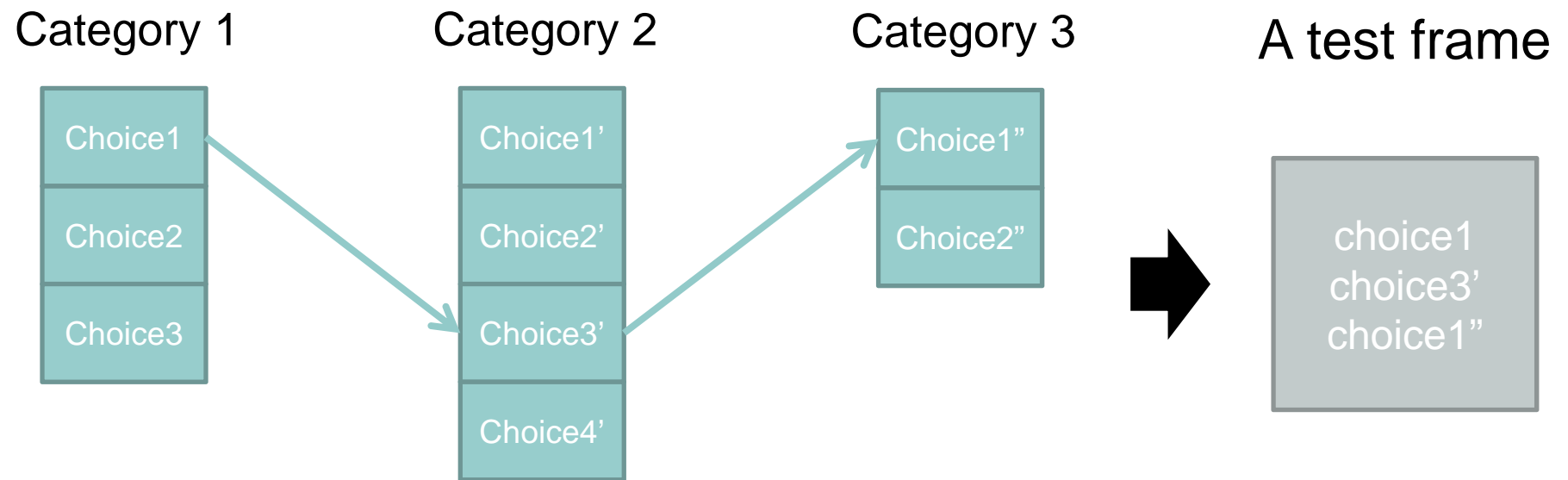
    if ( !count_only )
    {
        if ( flags & STD_OUTPUT )
            file_ptr = stdout;
        else
            file_ptr = fopen( out_file, "w" );
    }

    /* make_singles (through write_single) and make_frames increment num_frames */
    make_singles();
    make_frames( 0 );

    return num_frames;
}
```

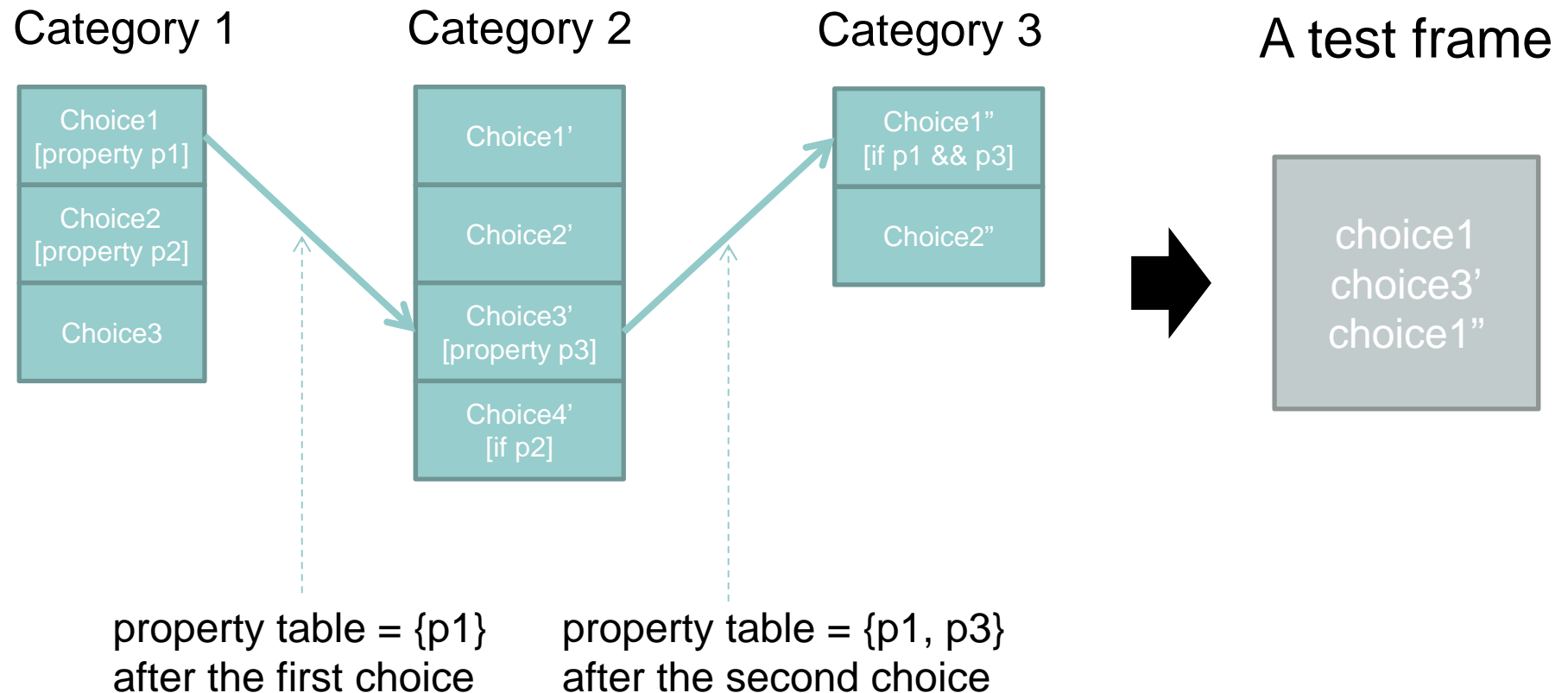
# How the Tool Works

- Without considering constraints, generate test frames are easy
  - Backtracking



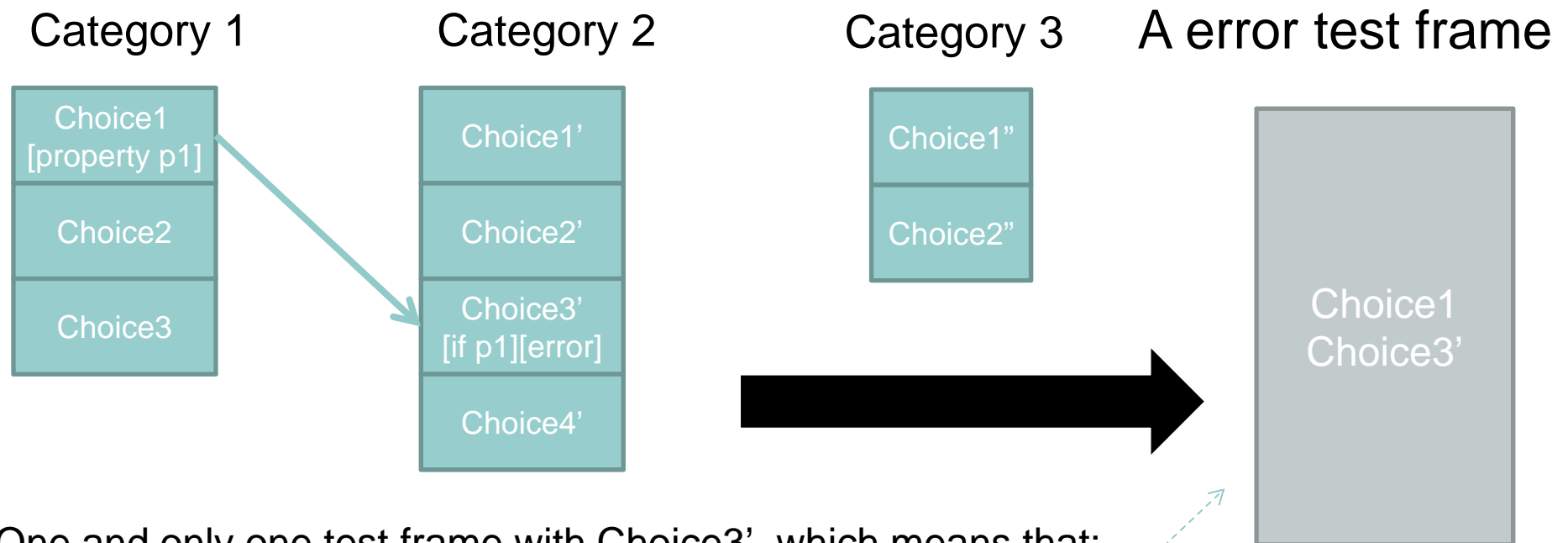
# Considering Property Constraints

- Maintaining a property table
  - Add property to the table when selecting a choice
  - Remove it from the table when backtracking



# Considering Error/Single Constraints

- Stop when encountering a choice with [error]/[single] constraint
  - If [error]/[single] is conditional, then the condition needs to be checked first against the property table.



One and only one test frame with Choice3', which means that:

- (1) Does not traverse the remaining categories.
- (2) After backtracking, does not traverse Choice3' anymore.

# How Choices Are Selected

---

- Examples:

- `[if NonEmpty]`

Reads: if `NonEmpty` is true combine this choice with others.

- `[if Hmmmmm] [single]`

Reads: if `Hmmmmm` is true make a single frame with this choice.

- `[if Radical] [property Cool] [else] [error]`

Reads: if `Radical` is true set `Cool` to true and combine this choice with others, else make an error frame with this choice.

- `[if NoWay] [single] [else]`

Reads: if `NoWay` is true make a single frame with this choice, else combine this choice with others.



# How Choices Are Selected

---

- Examples:

- `[property IC] [single]`  
Reads: make a single frame with this choice. (the property list is ignored)
- `[single] [if Random] [property RandQuoted]`  
Reads: make a single frame with this choice. (the selector expression is ignored)
- `[property Oh, Yeah]`  
Reads: set Oh and Yeah to true and combine this choice with others.
- `[property Long] [if Unquoted] [error] [else] [property Zero]`  
Reads: if Unquoted is true make an error frame with this choice, else set Zero to true and combine this choice with others. (the first property list is ignored)

# Complete TSL for **find**

---

## Parameters:

### Pattern size:

|                                  |                     |
|----------------------------------|---------------------|
| empty                            | [property Empty]    |
| single character                 | [property NonEmpty] |
| many character                   | [property NonEmpty] |
| longer than any line in the file | [error]             |

### Quoting:

|                              |                   |
|------------------------------|-------------------|
| pattern is quoted            | [property Quoted] |
| pattern is not quoted        | [if NonEmpty]     |
| pattern is improperly quoted | [error]           |

### Embedded blanks:

|                         |                          |
|-------------------------|--------------------------|
| no embedded blank       | [if NonEmpty]            |
| one embedded blank      | [if NonEmpty and Quoted] |
| several embedded blanks | [if NonEmpty and Quoted] |

### Embedded quotes:

|                         |                        |
|-------------------------|------------------------|
| no embedded quotes      | [if NonEmpty]          |
| one embedded quote      | [if NonEmpty]          |
| several embedded quotes | [if NonEmpty] [single] |

### File name:

|                        |         |
|------------------------|---------|
| good file name         |         |
| no file with this name | [error] |
| omitted                | [error] |

## Environments:

### Number of occurrences of pattern in file:

|               |                                |
|---------------|--------------------------------|
| none          | [if NonEmpty] [single]         |
| exactly one   | [if NonEmpty] [property Match] |
| more than one | [if NonEmpty] [property Match] |

### Pattern occurrences on target line:

|                                     |                     |
|-------------------------------------|---------------------|
| # assumes line contains the pattern |                     |
| one                                 | [if Match]          |
| more than one                       | [if Match] [single] |

# Complete TSL for **find**

## Parameters:

### Pattern size:

|                                  |                     |
|----------------------------------|---------------------|
| empty                            | [property Empty]    |
| single character                 | [property NonEmpty] |
| many character                   | [property NonEmpty] |
| longer than any line in the file | [error]             |

### Quoting:

|                              |                   |
|------------------------------|-------------------|
| pattern is quoted            | [property Quoted] |
| pattern is not quoted        | [if NonEmpty]     |
| pattern is improperly quoted | [error]           |

### Embedded blanks:

|                         |                          |
|-------------------------|--------------------------|
| no embedded blank       | [if NonEmpty]            |
| one embedded blank      | [if NonEmpty and Quoted] |
| several embedded blanks | [if NonEmpty and Quoted] |

### Embedded quotes:

|                         |                        |
|-------------------------|------------------------|
| no embedded quotes      | [if NonEmpty]          |
| one embedded quote      | [if NonEmpty]          |
| several embedded quotes | [if NonEmpty] [single] |

### File name:

|                        |         |
|------------------------|---------|
| good file name         |         |
| no file with this name | [error] |
| omitted                | [error] |

## Environments:

### Number of occurrences of pattern in file:

|               |               |                  |
|---------------|---------------|------------------|
| none          | [if NonEmpty] | [single]         |
| exactly one   | [if NonEmpty] | [property Match] |
| more than one | [if NonEmpty] | [property Match] |

### Pattern occurrences on target line:

# assumes line contains the pattern

|               |                     |
|---------------|---------------------|
| one           | [if Match]          |
| more than one | [if Match] [single] |

Reduce the redundancy:  
if the pattern is empty then  
it surely does not include  
embedded blank

# Complete TSL for **find**

## Parameters:

### Pattern size:

|                                  |                     |
|----------------------------------|---------------------|
| empty                            | [property Empty]    |
| single character                 | [property NonEmpty] |
| many character                   | [property NonEmpty] |
| longer than any line in the file | [error]             |

### Quoting:

|                              |                   |
|------------------------------|-------------------|
| pattern is quoted            | [property Quoted] |
| pattern is not quoted        | [if NonEmpty]     |
| pattern is improperly quoted | [error]           |

### Embedded blanks:

|                         |                          |
|-------------------------|--------------------------|
| no embedded blank       | [if NonEmpty]            |
| one embedded blank      | [if NonEmpty and Quoted] |
| several embedded blanks | [if NonEmpty and Quoted] |

### Embedded quotes:

|                         |                        |
|-------------------------|------------------------|
| no embedded quotes      | [if NonEmpty]          |
| one embedded quote      | [if NonEmpty]          |
| several embedded quotes | [if NonEmpty] [single] |

### File name:

|                        |         |
|------------------------|---------|
| good file name         |         |
| no file with this name | [error] |
| omitted                | [error] |

## Environments:

### Number of occurrences of pattern in file:

|               |                                |
|---------------|--------------------------------|
| none          | [if NonEmpty] [single]         |
| exactly one   | [if NonEmpty] [property Match] |
| more than one | [if NonEmpty] [property Match] |

### Pattern occurrences on target line:

|                                     |                     |
|-------------------------------------|---------------------|
| # assumes line contains the pattern |                     |
| one                                 | [if Match]          |
| more than one                       | [if Match] [single] |

Avoid infeasible combination:  
if the pattern is not quoted, then it is impossible to include embedded blanks

# Case Study with TSL: 电脑销售系统

---

**Direct Input:** a description on the computer system that is selected by the customer.

**Indirect Input (environment):** a database that contains all computer models available for sale.



# Case Study with TSL: 电脑销售系统

---

- Requirement on the input
  - The computer system description consists of a model number and a set of (slot, component) pairs.
  - The model number determines a set of constraints on available components and the available logic slots for components.
  - Slots may be required or optional. Required slots must be assigned with a suitable component to obtain a legal configuration, while optional slots may be left empty or filled depending on the customers' needs.
- Example:
  - *The required “slots” of the ThinkPad E430 laptop computer include a screen, a processor, a hard disk, memory, and an operating system. The optional slots include external storage devices such as a CD/DVD writer.*

# Case Study with TSL: 电脑销售系统

---

- Requirement on the input
  - The set of (slot, component) pairs are corresponding to the required and optional slots of the model.
  - A component is a choice that can be varied within a model. Valid components is determined by the model. The special value empty is allowed for optional slots.
  - In addition to being compatible or incompatible with a particular model and slot, individual components may be compatible or incompatible with each other.
  
- Example:
  - *The default configuration of the ThinkPad E430 includes 2 gigabytes of memory; 4 and 8 gigabyte memory are also available. The default operating system is Windows 8, home edition, but Windows 8, professional edition may also be selected. The professional edition requires at least 4 gigabytes of memory.*

# Step 1: Parameters and Choices

---

- The requirement:
  - *The computer system description consists of **a model number** and a set of (slot, component) pairs.*
- **Parameter:** model number of the computer system
  - Malformed
  - Not in database
  - Valid



# Step 1: Parameters and Choices

---

- The requirement:
  - The model number determines a set of constraints on available components and the available logic slots for components. Slots may be required or optional.
- **Parameter:** number of required slots specified by the model
  - 0
  - 1
  - Many #more than one
- **Parameter:** number of optional slots specified by the model
  - 0
  - 1
  - Many #more than one

# Step 1: Parameters and Choices

---

- The requirement:
  - The set of (slot, component) pairs are corresponding to the required and optional slots of the model.
- **Parameter:** correspondence between slots specified by the model and slots described by the system
  - Omitted slots #e.g. model specifies a DVD slot but system omits it.
  - Extra slots
  - Mismatched slots #that is, have both omitted slots and extra slots
  - Complete correspondence

# Step 1: Parameters and Choices

---

- The requirement:
  - The computer system description consists of a model number and a set of (slot, component) pairs. **Required slots must be assigned with a suitable component to obtain a legal configuration**
- **Parameter:** how many required slots are non-empty in the system
  - 0
  - $<$  total number of required slots specified by the model
  - $=$  total number of required slots specified by the model

# Step 1: Parameters and Choices

---

- The requirement:
  - The model number determines a set of **constraints on available components**
  - A component is a choice that can be varied within a model. **Valid components for each slot is determined by the model.**
  - In addition to being compatible or incompatible with a particular model and slot, **individual components may be compatible or incompatible with each other.**
  
- **Parameter:** Selection of components for required slots in the system
  - All valid choices.
  - $\geq 1$  incompatible with model
  - $\geq 1$  incompatible with slots
  - $\geq 1$  incompatible with another selection

# Step 1: Parameters and Choices

---

- The requirement:
  - The computer system description consists of a model number and a set of (slot, component) pairs.
  - Optional slots **may be left empty or filled** depending on the customers' needs.
- **Parameter:** how many optional slots are non-empty in the system
  - 0
  - < total number of optional slots specified by the model
  - = total number of optional slots specified by the model

# Step 1: Parameters and Choices

---

- The requirement:
  - The special value **empty** is allowed for optional slots.
  - In addition to being compatible or incompatible with a particular model and slot, **individual components may be compatible or incompatible with each other.**
- **Parameter:** selection of components for optional slots in the system
  - All valid with empty choices.
  - All valid with at least one non-empty choice.
  - $\geq 1$  incompatible with model
  - $\geq 1$  incompatible with slots
  - $\geq 1$  incompatible with another selection

# Step 2: Identify Constraints

---

Number of required slots specified by the model:

|      |                 |
|------|-----------------|
| 0    |                 |
| 1    | [property RSNE] |
| Many | [property RSNE] |

How many required slots are non-empty in the system:

|                         |                   |
|-------------------------|-------------------|
| 0                       | [if RSNE] [error] |
| < number required slots | [error]           |
| = number required slots |                   |

Number of optional slots specified by the model:

|      |                 |
|------|-----------------|
| 0    |                 |
| 1    | [property OSNE] |
| Many | [property OSNE] |

How many optional slots are non-empty in the system:

|                         |           |
|-------------------------|-----------|
| 0                       |           |
| < number optional slots | [if OSNE] |
| = number optional slots | [if OSNE] |

## Step 2: Identify Constraints

---

Model number:

|                 |         |
|-----------------|---------|
| Malformed       | [error] |
| Not in database | [error] |
| Valid           |         |

Correspondence between slots specified by the model and slots described by the system:

|                         |         |
|-------------------------|---------|
| Omitted slots           | [error] |
| Extra slots             | [error] |
| Mismatched slots        | [error] |
| Complete correspondence |         |



## Step 2: Identify Constraints

---

- Selection of components for required slots in the system
  - All valid choices.
  - $\geq 1$  incompatible with model [if RSNE] [error]
  - $\geq 1$  incompatible with slots [if RSNE] [error]
  - $\geq 1$  incompatible with another selection [if RSNE] [error]
  
- selection of components for optional slots in the system
  - All valid with empty choices.
  - All valid with at least one non-empty choice.
  - $\geq 1$  incompatible with model [if OSNE] [error]
  - $\geq 1$  incompatible with slots [if OSNE] [error]
  - $\geq 1$  incompatible with another selection [if OSNE] [error]

# The Complete TSL Specification

- Model number
  - Malformed [error]
  - Not in database [error]
  - Valid
- Number of required slots specified by the model
  - 0
  - 1 [property RSNE]
  - Many [property RSNE]
- Number of optional slots specified by the model
  - 0
  - 1 [property OSNE]
  - Many [property OSNE]
- Correspondence between slots specified by the model and slots described by the system
  - Omitted slots [error]
  - Extra slots [error]
  - Mismatched slots [error]
  - Complete correspondence
- # of required slots that are non-empty in the system
  - 0 [if RSNE] [error]
  - < number required slots [if RSNE] [error]
  - = number required slots
- Selection of components for required slots in the system
  - All valid choices.
  - $\geq 1$  incompatible with slots [if RSNE][error]
  - $\geq 1$  incompatible with another selection [if RSNE][error]
  - $\geq 1$  incompatible with model [if RSNE][error]
- # of optional slots that are non-empty in the system
  - 0
  - < number optional slots [if OSNE]
  - = number optional slots [if OSNE]
- Selection of components for optional slots in the system
  - All valid with empty.
  - All valid with at least one non-empty choice. [if OSNE]
  - $\geq 1$  incompatible with slots [if OSNE][error]
  - $\geq 1$  incompatible with another selection [if OSNE][error]
  - $\geq 1$  incompatible with model [if OSNE][error]

# An Example Test Frame

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- Model number: **Valid**
- Number of required slots specified by the model: **Many**
- Number of optional slots specified by the model: **0**
- Correspondence between slots specified by the model and slots described by the system: **complete**
- # of required slots that are non-empty in the system: **=**
- Selection of components for required slots in the system: **all valid**
- # of optional slots that are non-empty in the system: **0**
- Selection of components for optional slots in the system: **all valid with empty.**

# Thank you!

