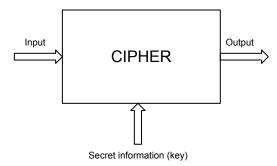
# **AES Timing Attacks**

Hardware and Software Design for Cryptographic Applications

April 12, 2013

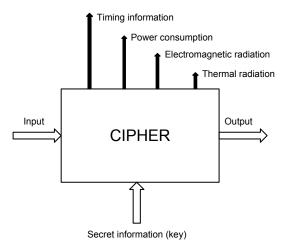
#### Ciphers as a Black Box

In theory, encryption (and decryption) implementations operate as black boxes.



# Information Leakage

In reality, it's hard to prevent additional information from being leaked at runtime.



#### Side Channel Attacks

**Definition**: Any attack on a cryptosystem using information leaked given off as a byproduct of the physical implementation of the cryptosystem, rather than a theoretical weakness [1], is a side channel attack.

We focus on timing attacks for software implementations of AES.

We assume the attacker can *easily* capture this timing information.

## History of Timing Attacks on Cryptographic Primitives

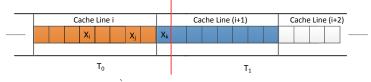
- RSA's modular exponentiation ( $c \equiv m^e \pmod{n}$ )
  - Square-and-multiply algorithms for  $\mathcal{O}(\log_2(n))$  complexity has branch statement whose execution depends directly on e.
- Branch statements to compute the multiplicative inverse of elements in GF(2<sup>8</sup>)
   [3].
- Timing attacks against OpenSSL [4].
- Cacche hit ratio is predicted to be a fruitful side-channel for launching attacks [5].

### Timing Attacks on AES

- Rijndael was deemed not susceptible to timing attacks in the AES contest
- AES targeted attacks can be based on statistical evidence [2].
  - Observation: The entire encryption time can be affected by the input bytes  $p_i^0 \oplus k_i^0$  Why?
  - Step 1: Capture timing data on a reference and target machine for each value of a particular input byte p<sub>i</sub><sup>0</sup> ⊕ k<sub>i</sub><sup>0</sup> = x<sub>i</sub><sup>0</sup>
  - Step 2: Perform correlation between reference and target data
  - Step 3: Heel click.
- Or they can be more targeted:
  - Exploit relationships between secret information of the primitive and known data.
  - This is the approach of Bonneau et al., among others.

### Cache Memory





 $\langle x_i \rangle = \langle x_i \rangle$  are the higher bits of the data entry.

Data is pulled into cache based on the most-significant bits in its address.

#### Cache Collisions Reveal Weaknesses

Let 
$$T_E(K, P)$$
 be the encryption time for a plaintext  $P$  using key  $K$ . Let  $\overline{T}_E(K) = \frac{1}{n} \sum_{i=1}^n T_E(K, P_i)$ , where  $P_i$  is a random plaintext from  $\{0|1\}^{128}$ .

**Cache-Collision Assumption [?].** For any pair of table lookups i,j, given a large enough number of *random* AES encryption that use the *same key*,  $\overline{T}_{E}(K)$  will be lower when  $\langle I_i \rangle = \langle I_i \rangle$  than when  $\langle I_i \rangle \neq \langle I_i \rangle$ 

Note: The table lookup indices must be independent for random plaintexts.

### Cache Collisions (cont'd)

Let a and b be two memory addresses looked up in memory. Let  $\langle a \rangle$  and  $\langle b \rangle$  denote the MSBs of a and b, respectively.

- Cache memory is organized into *lines* 
  - MSB is mapped to the cache line index, LSB is mapped to the line (block) offset
- Reads on a and b cause a collision if  $\langle a \rangle = \langle b \rangle$  (assuming other memory reads have not evicted (or invalidated) a or b from the cache.
- If  $\langle a \rangle \neq \langle b \rangle$  then a cache collision *might* occur.
- We cannot say for certain whether or not the lower LSBs are equivalent...

#### Attacks from Cache Collisions

That's it! We may now build an attack based on this result.

#### **LUT-Based Implementations**

Let  $X^i$  be the state of AES at round i. With the exception of i = 10, we have:

$$\begin{split} \boldsymbol{X}^{i+1} &= \{ T_0[\boldsymbol{x}_0^i] \oplus T_1[\boldsymbol{x}_5^i] \oplus T_2[\boldsymbol{x}_{10}^i] \oplus T_3[\boldsymbol{x}_{15}^i] \oplus \{k_0^i, k_1^i, k_2^i, k_3^i\}, \\ & T_0[\boldsymbol{x}_4^i] \oplus T_1[\boldsymbol{x}_9^i] \oplus T_2[\boldsymbol{x}_{14}^i] \oplus T_3[\boldsymbol{x}_3^i] \oplus \{k_4^i, k_5^i, k_6^i, k_7^i\}, \\ & T_0[\boldsymbol{x}_8^i] \oplus T_1[\boldsymbol{x}_{13}^i] \oplus T_2[\boldsymbol{x}_2^i] \oplus T_3[\boldsymbol{x}_7^i] \oplus \{k_8^i, k_9^i, k_{10}^i, k_{11}^i\}, \\ & T_0[\boldsymbol{x}_{12}^i] \oplus T_1[\boldsymbol{x}_1^i] \oplus T_2[\boldsymbol{x}_6^i] \oplus T_3[\boldsymbol{x}_{11}^i] \oplus \{k_{12}^i, k_{13}^i, k_{14}^i, k_{15}^i\} \} \end{split}$$

#### First Round

- First round:  $x_i^0 = p_i \oplus k_i$
- With the T-box implementation,  $x_0^0$ ,  $x_4^0$ ,  $x_8^0$ , and  $x_{12}^0$  are used as indices into  $T_0$
- If we are looking for cache collisions, we must consider input bytes of the same T-box.

$$\langle x_i^0 \rangle = \langle x_j^0 \rangle \Rightarrow \langle p_i \rangle \oplus \langle k_i \rangle = \langle p_j \rangle \oplus \langle k_j \rangle$$
$$\Rightarrow \langle p_i \rangle \oplus \langle p_j \rangle = \langle k_i \rangle \oplus \langle k_j \rangle$$

# First Round Attack Algorithm

```
ALGORITHM 1: FirstRoundAttack(N<sub>s</sub>)
 1. n \leftarrow 2^8 - 1
 2: T \leftarrow \operatorname{array}[0 \dots n, 1 \dots n, 0 \dots n]
 3: for count = 0 \rightarrow N_s do
       P \leftarrow RandomBytes(16)
 4:
      start \leftarrow time()
 5.
 6: C \leftarrow E_K(P)
 7: end \leftarrow time()
 8: tt \leftarrow (start - end)
      for all i, i do
                                                                                 \triangleright i, j are input bytes of the same T-box
 9:
                  T[i,j,\langle p_i\rangle \oplus \langle p_i\rangle] \leftarrow T[i,j,\langle p_i\rangle \oplus \langle p_i\rangle] + tt
10.
           end for
11:
12. end for
13: T[i, j, \langle p_i \rangle \oplus \langle p_i \rangle] \leftarrow T[i, j, \langle p_i \rangle \oplus \langle p_i \rangle] / N_s
14: mi, mj \leftarrow min(t)
                                                                                                         15: \langle k_{mi} \rangle \oplus \langle k_{mi} \rangle \leftarrow \langle p_{mi} \rangle \oplus \langle p_{mi} \rangle
```

# First Round Attack Algorithm (cont'd)

$$X^{i+1} = \{ T_{0}[x_{0}^{i}] \oplus T_{1}[x_{5}^{i}] \oplus T_{2}[x_{10}^{i}] \oplus T_{3}[x_{15}^{i}] \oplus \{k_{0}^{i}, k_{1}^{i}, k_{2}^{i}, k_{3}^{i}\},$$

$$T_{0}[x_{4}^{i}] \oplus T_{1}[x_{9}^{i}] \oplus T_{2}[x_{14}^{i}] \oplus T_{3}[x_{3}^{i}] \oplus \{k_{4}^{i}, k_{5}^{i}, k_{6}^{i}, k_{7}^{i}\},$$

$$T_{0}[x_{8}^{i}] \oplus T_{1}[x_{13}^{i}] \oplus T_{2}[x_{2}^{i}] \oplus T_{3}[x_{7}^{i}] \oplus \{k_{8}^{i}, k_{9}^{i}, k_{10}^{i}, k_{11}^{i}\},$$

$$T_{0}[x_{12}^{i}] \oplus T_{1}[x_{1}^{i}] \oplus T_{2}[x_{6}^{i}] \oplus T_{3}[x_{11}^{i}] \oplus \{k_{12}^{i}, k_{13}^{i}, k_{14}^{i}, k_{15}^{i}\}\}$$

# First Round Attack Algorithm (cont'd)

$$\begin{split} X^{i+1} &= \{ \overleftarrow{T_0[x_0^i]} \oplus T_1[x_5^i] \oplus T_2[x_{10}^i] \oplus T_3[x_{15}^i] \oplus (k_0^i, k_1^i, k_2^i, k_3^i], \\ & \overleftarrow{T_0[x_4^i]} \oplus T_1[x_9^i] \oplus T_2[x_{14}^i] \oplus T_3[x_3^i] \oplus (k_4^i) k_5^i, k_6^i, k_7^i\}, \\ & \overleftarrow{T_0[x_8^i]} \oplus T_1[x_{13}^i] \oplus T_2[x_2^i] \oplus T_3[x_7^i] \oplus (k_8^i) k_9^i, k_{10}^i, k_{11}^i\}, \\ & \overleftarrow{T_0[x_{12}^i]} \oplus T_1[x_1^i] \oplus T_2[x_6^i] \oplus T_3[x_{11}^i] \oplus (k_{12}^i) k_{13}^i, k_{14}^i, k_{15}^i\} \} \end{split}$$

#### First Round Limitation

We only know that 
$$\langle k_0 \rangle \oplus \langle k_4 \rangle = \Delta_1$$
,  $\langle k_0 \rangle \oplus \langle k_8 \rangle = \Delta_2$ ,  $\langle k_0 \rangle \oplus \langle k_{12} \rangle = \Delta_3$ ,  $\langle k_4 \rangle \oplus \langle k_8 \rangle = \Delta_4$ ,  $\langle k_4 \rangle \oplus \langle k_{12} \rangle = \Delta_5$ , and  $\langle k_8 \rangle \oplus \langle k_{12} \rangle = \Delta_6$ .

Of course, there exists **18** other equations we can derive for  $T_1$ ,  $T_2$ , and  $T_3$ .

We cannot determine the lower log<sub>2</sub> bits of each key... What to do now?

#### The Last Round

When i = 10, the lookup table is just the S-box S. At this point, the ciphertext C is:

$$\begin{split} C &= \{S[x_0^{10}] \oplus k_0^{10}, S[x_5^{10}] \oplus k_1^{10}, S[x_{10}^{10}] \oplus k_2^{10}, S[x_{15}^{10}] \oplus k_3^{10}, \\ S[x_4^{10}] \oplus k_5^{10}, S[x_9^{10}] \oplus k_6^{10}, S[x_{14}^{10}] \oplus k_7^{10}, S[x_3^{10}] \oplus k_7^{10}, \\ S[x_8^{10}] \oplus k_8^{10}, S[x_{13}^{10}] \oplus k_9^{10}, S[x_2^{10}] \oplus k_{10}^{10}, S[x_7^{10}] \oplus k_{11}^{10}, \\ S[x_{12}^{10}] \oplus k_{12}^{10}, S[x_1^{10}] \oplus k_{13}^{10}, S[x_6^{10}] \oplus k_{14}^{10}, S[x_{11}^{10}] \oplus k_{15}^{10} \} \end{split}$$

#### Final Round Collisions

Let  $x_s$  and  $x_t$  be two random bytes in the last round.

We will always have that  $c_i = k_i^{10} \oplus S[x_s]$  and  $c_j = k_j^{10} \oplus S[x_t]$ . If  $x_s = x_t$ , then a collision will usually occur and  $c_i = k_i^{10} \oplus \alpha$  and  $c_j = k_i^{10} \oplus \alpha$ .

Therefore, 
$$c_i \oplus c_j = k_i^{10} \oplus k_j^{10}$$

#### **Final Round Misses**

What if  $x_s \neq x_t$ ?

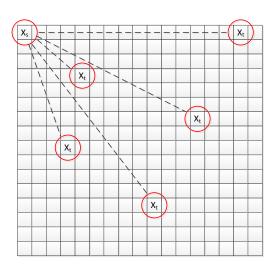
 $c_i \oplus c_j \neq k_i^{10} \oplus k_j^{10} \Rightarrow$  two different values came out of the LUT!

AES Timing Attacks

Cache Timing Attacks on AES

Last Round Attack

# S-Box Nonlinearity



#### Final Round Misses (cont'd)

The *S-box nonlinearity* means that the difference between  $S[x_s]$  and  $S[x_t]$  does not imply a fixed difference between  $x_s$  and  $x_t$ .

If  $c_i \oplus c_j \neq k_i^{10} \oplus k_j^{10}$ , then  $x_s$  and  $x_t$  are two *random* values.

# Final Round Attack Algorithm

# ALGORITHM 2: LastRoundAttack(N<sub>s</sub>)

```
1. n \leftarrow 2^8 - 1
 2: diffs \leftarrow [0, \dots, 2^n - 1, 0, \dots, 2^n - 1]
 3: T \leftarrow \operatorname{array}[0...2^n - 1, 0...2^n - 1, 0...2^n - 1]
 4: for count = 0 \rightarrow N_s do
      P \leftarrow RandomBytes(16)
 5.
 6: start ← time()
 7: C \leftarrow E_{\kappa}(P)
 8: end \leftarrow time()
 9: tt \leftarrow (start - end)
10: for i, j in C do
              T[i,j,C_i\oplus C_i] \leftarrow T[i,j,C_i\oplus C_i] + tt
11:
         end for
12:
13: end for
14: T[i,j,\Delta_{i,i}] \leftarrow T[i,j,\Delta_{i,i}]/N_s
15: \Delta'_{i,i} \leftarrow min(T,i,j)
16: return all \Delta'_{i,i}
```

# Final Round Attack Algorithm (cont'd)

With knowledge of  $\Delta_{i,j}$  for all i,j such that  $\Delta_{i,j}=k_i^{10}\oplus k_j^{10}$  the attacker can now make informed guesses at the key

caw: I think I should include an example here

Thanks to Rijndael's invertible key schedule,  $[k^{10}]$  can be reverted back to  $[k^{0}]$ .

Done.

AES Timing Attacks

Cache Timing Attacks on AES

Last Round Attack

# **Timing Attack Countermeasures**

caw: keep?

#### References

- J. Bonneau, I. Mironov. Cache-collision timing attacks against AES. *Cryptographic Hardware and Embedded Systems CHES 2006*, Springer Berlin Heidelberg, (2006), 201-215.
- 2 D. J. Bernstein. Cache-timing attacks on AES. April 2005. http://cr.yp.to/antiforgery/cachetiming-20050414.pdf.
- 3 F. Koeune, J. J. Quisquater. A timing attack against Rijndael. *Technical Report CG-1999/1*, June 1999.
- 4 D. Brumley, D. Boneh. Remote timing attacks are practical. *Computer Networks* **48(5)** (2005), 701-706.
- 5 J. Kelsey, B. Schneier, D. Wagner, C. Hall. Side channel cryptanalysis of product ciphers. *Journal of Computer Security* **8(2/3)** (2000).