## **Intelligent Systems Assignment:**

### **Search Methods**

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# **Approach**

One of the first obstacles I faced was definition of the problem. My first attempt was the most intuitional approach an OOP programmer could take; I tried designing everything as an object. I defined everything as different objects – the grid, the blocks and the ③. I've also had a class that was designed to entail the state of the current grid configuration.

### Definition of Problem

At one point I realized that there was a much simpler and efficient approach that would take less time to implement, less resources to compile and it would be easier for someone else to understand it.

I did the following: I encoded the whole grid and configuration as a **string** in the form of **"000000000ABCX"**. Obviously, the X is the ③. Each 0 is an empty block and {A, B, C} are the blocks that we need to build the tower for the goal state (**"00000A000B000C0X"**). Every four symbols form a row in the grid. My whole problem revolves around manipulating the position of the **chars** in the **string.** 

#### Methods

My methods are self-explanatory. The methods that move the X are called void moveLeft(), void movePight(), void moveUp(), void moveDown(). I have Boolean methods isMoveRight(), isMoveUp(), isMoveUp() that check if a movement is possible given the current configuration. The methods for moving X also check if movement is possible but this redundant check is there because I needed it for debugging and that doesn't affect performance at all. My other methods are LinkedList<BlockPuzzle> generateChildBfs, LinkedList<BlockPuzzle> generateChildDfs, ArrayList<BlockPuzzle> generateChildAStar. These methods generate children for each algorithm and use different approach in doing it. For BFS I check if a move is possible and I add it to the Linked List. For DFS I have a random number generator that manipulates the order of checks so DFS doesn't get stuck. IDS uses the same method as DFS. For A\* I am doing the same as in BFS, however, I am also calculating the Manhattan distance and I am adding the successor nodes to an Array List.

## **Evidence**

To prove that my implementation works, I will provide output for several of the algorithms that showcases the directions needed to find a solution for the given problem. Additionally, I will include information about the nodes expanded, depth and memory used for each algorithm. This should hopefully give a good base idea of how it all works.

**BFS Output for reaching Goal State** after expanding **8 448 993 nodes**, depth is 14, memory used is around 1.135GB. **BFS** is always consistent, if the configuration doesn't change and the sequence of checks (which move to add first to the queue) remains the same.

- **0.** [0000 0000 0000 ABCX] Initial State
- 1. [0000 0000 000X ABC0] UP
- 2. [0000 0000 00X0 ABC0] LEFT
- 3. [0000 0000 0X00 ABC0] LEFT
- 4. [0000 0000 0B00 AXC0] DOWN
- 5. [0000 0000 0B00 XAC0] LEFT
- 6. [0000 0000 XB00 0AC0] UP
- 7. [0000 0000 BX00 0AC0] RIGHT
- 8. [0000 0000 BA00 0XC0] DOWN
- 9. [0000 0000 BA00 0CX0] RIGHT
- **10.** [0000 0000 BAX0 0C00] UP
- **11.** [0000 00X0 BA00 0C00] UP
- 12. [0000 0X00 BA00 0C00] LEFT
- 13. [0000 0A00 BX00 0C00] DOWN
- **14. [0000 0A00 XB00 0C00]** LEFT -> Goal State

**DFS Output for reaching Goal State** is mostly random in the range of  $10\,000 - 100\,000$  nodes expanded. The depth is between  $15\,000 - 120\,000$ . Memory used is in the range of 0,06GB. I can provide directions for reaching goal state in **DFS** but it going to take a lot of space in the report because of the size of the depth.

**IDS Output for reaching Goal State** is random in the range of 8 000 000 – 13 000 000 nodes expanded, which is a bit more than **BFS**. In some unlucky cases, it could go above 13 mil. Depth is always 14, just like in **BFS** and memory is around 0,07GB which is similar to **DFS**. For identical configuration, the directions for reaching a goal state are the same as in **BFS**.

A\* Output for reaching Goal State is consistent and returns around 1000 nodes expanded for the base problem. The size depends on the sequence of checks (which move to add first to the priority queue). Priority Queue compares f for every state (f = h (Manhattan distance) + g (Depth)) and picks the lower value. Depth is always 14 and memory used is around 0,009GB. I am providing a sequence of moves that is generated by the algorithm and reaches a goal state. The moves are easily trackable and that clearly shows that the algorithm works as intended.

- **0.** [0000 0000 0000 ABCX] Initial State
- 1. [0000 0000 000X ABC0] UP
- 2. [0000 0000 00X0 ABC0] LEFT
- 3. [0000 0000 0X00 ABC0] LEFT
- 4. [0000 0000 0B00 AXC0] DOWN
- 5. [0000 0000 0B00 XAC0] LEFT
- **6. [0000 0000 XB00 0AC0]** UP

- 7. [0000 0000 BX00 0AC0] RIGHT
- 8. [0000 0000 BA00 0XC0] DOWN
- 9. [0000 0000 BA00 0CX0] RIGHT
- **10.** [0000 0000 BAX0 0C00] UP
- **11. [0000 00X0 BA00 0C00]** UP
- **12. [0000 0X00 BA00 0C00]** LEFT
- **13. [0000 0A00 BX00 0C00]** DOWN
- **14.** [0000 0A00 XB00 0C00] LEFT -> Goal State

# Scalability study

My initial tests were based on the original problem. I've plotted the results on the graphs bellow.

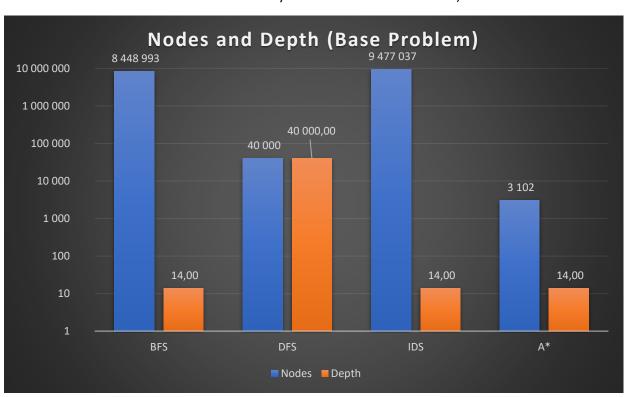
I am using log representation of the values on the graphs.

BFS and DFS are the first two algorithms that I have implemented. Both can find a solution, however, there are several distinctive differences between them. The memory graph (in the Extras section) shows that BFS takes much more memory (O(b<sup>d</sup>) space complexity), compared to DFS (O(bd)). However, BFS is much shallower than DFS and always finds the optimal solution, which is not the case for DFS. That is represented in the difference in the time complexity. BFS is O(b<sup>d</sup>), while time complexity for DFS is O(b<sup>m</sup>), where m is the maximum depth for a node, which is much worse because our tree is infinite (© always has at least 2 moves).

From the graphs we can see that **BFS** and **IDS** have the same depth and almost the same number of nodes expanded. However, the main difference is the memory requirement. For **BFS**, we need 1.135GBytes to solve the original problem and for **IDS** that is merely 0,07GBytes which is much closer to the memory value of **DFS**. From the results, we can clearly see that **IDS** combines the best of traits of **BFS** and **DFS** in one; **O(bd)** space complexity of **DFS** and it is optimal and finds the shallowest solution, like **BFS**. Unfortunately, the time complexity for **IDS** is as bad as **BFS**, **O(bd)**, but it is still better than **DFS**. The reason for this is that it generates all nodes for each level, just like **BFS**. The space complexity is much better because we traverse the nodes as if we are doing **DFS** and we do not store them in memory.

Clearly,  $A^*$  is the best algorithm for this problem.  $A^*$  outperformed every other algorithm in almost every scenario. It finds an optimal solution and time complexity is  $O(b^d)$ , where d is solution depth, which is not the worst, compared to the others. Space complexity is not a serious issue because the scale of the problem is small (Graph in Extra section).

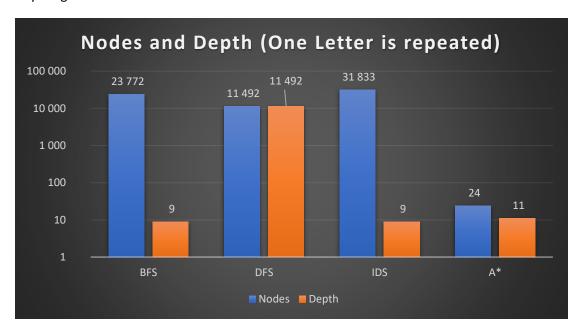
(Values for DFS and IDS are average. DFS is between 10k - 120k and IDS is mostly between 7mil. - 12mil. I've settled with these values because they are the most common ones.)



I also altered the problem several times to further explore the differences in the characteristics of the algorithms.

### INPUT "0AAA00000000ABCX"

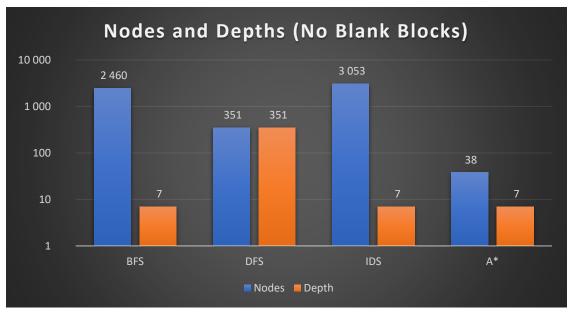
First case makes the problem easier by adding a few more "A" blocks. This significantly boosts the performance for each of the algorithms, especially for A\*, which expands less nodes than DFS, however, the solution is not optimal. I tried figuring out why that was the case and I couldn't find anything relevant.



For the second analysis, I am filling all empty blocks with letters. This boosts up the speed even more.

#### INPUT "ABCABCABCABCX"

In this example, A\* clearly outperforms all other algorithms and finds the optimal solution. **BFS** is also doing great because there are not as many states and it even manages to beat **IDS** and **DFS**. In the next section, the graphs showcase how space complexity of **A\*** is the best and how **BFS**'s space complexity is almost the same as **DFS** and **IDS** for this easier problem.



### Extras and limitations

#### Limitations

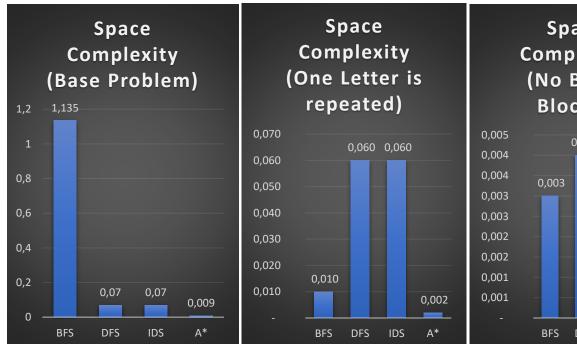
- Because I am using strings, I can't directly access the positions of the letter blocks, which could be beneficial in some scenarios.
- Rescaling the problem is also very hard for my implementation and even a 5x5 grid is not solvable for any of my algorithms because it takes way too much memory.
- Also, using strings as nodes just keeps creating new strings in the memory, even though I am using a String Builder, it is still very demanding.
- My DFS children generator method uses 4 different configurations for adding checking for possible moves. A random number from 1 to 4 chooses which configuration is going to be used. I am not sure if that is the best way to randomize the results and, in some cases, it might still cause unnecessary loops, which are not observable while running the code
- My implementation cannot solve the problem, if there are a lot of blank squares in the initial configuration. For example, "00A00000B00X000C" is unsolvable and I run out of memory for every algorithm.

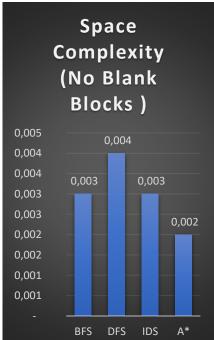
#### Extras

Space complexity for different configurations represented in GBytes.

For smaller case problems, space complexity is not an issue, even for BFS.

### Configurations:





We can conclude, that A\* is the best algorithm of the four in every case. It has the most efficient time complexity, it expands the least nodes and it requires less memory. Using heuristics is way better than doing uninformed search in terms of efficiency and speed.

# References

I've used several webpages for pseudocodes. I've written everything by myself. I've used the pseudocodes only for guidelines.

http://www.mathcs.emory.edu/~cheung/Courses/171/Syllabus/11-Graph/bfs.html

https://en.wikipedia.org/wiki/Depth-first\_search

http://www.cs.toronto.edu/~heap/270F02/node36.html

https://www.geeksforgeeks.org/iterative-deepening-searchids-iterative-deepening-depth-first-searchiddfs/

https://en.wikipedia.org/wiki/Iterative\_deepening\_depth-first\_search

Artificial Intelligence, A Modern Approach, Third Edition – Course Book

## Code

### **Main Class**

```
Runtime.getRuntime().freeMemory(); //Used to calculate memory usage
        BlockPuzzle blockPuzzle1 = new BlockPuzzle("0AA0A0000000ABCX");
        BlockPuzzle blockPuzzle2 = new BlockPuzzle("ABCABCABCABCABCX");
```

```
System.out.println("Memory used: " + ((afterUsedMembeforeUsedMem)/Math.pow(10,9)) + " GBytes");
    public static boolean isGoalState(String currentState){
currentState.charAt(5)+currentState.charAt(9)+currentState.charAt(13)).equa
    public static void bfsQUEUE(BlockPuzzle initialState) {
         LinkedList<BlockPuzzle> queue = new LinkedList<BlockPuzzle>();
             Iterator<BlockPuzzle> i =
```

```
BlockPuzzle node = i.next();
node.getStateDepth());
node.getCurrentState());
                    System.out.println();
                    System.out.println("Steps: " + steps);
                    System.out.println("Goal at depth: " +
node.getStateDepth());
node.getCurrentState());
```

```
public static BlockPuzzle bfsQueueDIRECTIONS(BlockPuzzle initialState) {
BlockPuzzle.generateChildBfs(state).listIterator();
                BlockPuzzle node = i.next();
                if (!(isGoalState(node.getCurrentState()))){
                    queue.add(node);
node.getCurrentState());
    public static BlockPuzzle bfsListDIRECTIONS(BlockPuzzle initialState) {
        while (queue.size() != 0) {
            Iterator<BlockPuzzle> i =
BlockPuzzle.generateChildBfs(state).listIterator();
                BlockPuzzle node = i.next();
```

```
} else {
node.getStateDepth());
node.getCurrentState());
    public static void dfs(BlockPuzzle initialState) {
        Stack<BlockPuzzle> stack = new Stack<>();
        ArrayList<BlockPuzzle> children;
parent.getStateDepth());
parent.getCurrentState());
BlockPuzzle.generateChildDfsLIST(parent).size(); i++) {
                   children = BlockPuzzle.generateChildDfsLIST(parent);
                    stack.push(children.get(i));
    public static BlockPuzzle dfsDIRECTIONS(BlockPuzzle initialState) {
        Stack<BlockPuzzle> stack = new Stack<>();
```

```
BlockPuzzle state = stack.pop();
            Iterator<BlockPuzzle> i =
BlockPuzzle.generateChildDfs(state).listIterator();
node.getCurrentState());
    public static boolean Depth Limited Search (BlockPuzzle problem, int
parent.getStateDepth());
                System.out.println("Goal state: " +
parent.getCurrentState());
            if (parent.getStateDepth() == limit) {
```

```
public static void Iterative Deepening Search(BlockPuzzle problem) {
Iterative_Deepening_SearchDIRECTIONS(BlockPuzzle problem) {
    public static void AStar(BlockPuzzle problem) {
        PriorityQueue<BlockPuzzle> pQueue = new
PriorityQueue<BlockPuzzle>();
        pQueue.add(problem);
        while (pQueue.size() != 0) {
            BlockPuzzle parent = pQueue.poll();
                System.out.println("Goal at depth: " +
parent.getStateDepth());
                System.out.println("Goal state: " +
parent.getCurrentState());
                pQueue.clear();
BlockPuzzle.generateChildAStarList(parent).size(); i++) {
                    pQueue.add(children.get(i));
```

```
public static BlockPuzzle AStarDIRECTIONS(BlockPuzzle problem) {
        PriorityQueue<BlockPuzzle> pQueue = new
PriorityQueue<BlockPuzzle>();
        pQueue.add(problem);
        while (pQueue.size() != 0) {
            BlockPuzzle parent = pQueue.poll();
                System.out.println("Steps: " + step);
                System.out.println("Goal at depth: " +
parent.getStateDepth());
                System.out.println("Goal state: " +
parent.getCurrentState());
                pQueue.clear();
     * @param problem the goal state which will be used to generate the
    public static ArrayList<String> generateDirections(BlockPuzzle
        ArrayList<String> directions = new ArrayList<>();
        String temp = problem.getCurrentState() + " " +
problem.getDirection();
        directions.add(temp);
problem.getParent().getDirection());
```

```
Collections.reverse(directions);
   return directions;
}
```

### **BlockPuzzle class**

```
public BlockPuzzle() {
   StringBuilder stringBuilder = new StringBuilder();
```

```
stringBuilder.append("0");
            stringBuilder.append(symbols[n]);
* @param initialState the configuration for the problem
public BlockPuzzle(String initialState) {
 * @param size
            stringBuilder.append("0");
            stringBuilder.append(symbols[n]);
    initialState = stringBuilder.toString();
```

```
public String getCurrentState() {
public String getInitialState() {
public void setInitialState(String initialState) {
public Integer getSize() {
public Integer getSmileyPosition() {
public void setSmileyPosition(Integer smileyPosition) {
public static Integer getTreeDepth() {
public static void setTreeDepth(Integer treeDepth) {
   BlockPuzzle.treeDepth = treeDepth;
public Integer getStateDepth() {
public void setStateDepth(Integer stateDepth) {
public BlockPuzzle getParent() {
public void setParent(BlockPuzzle parent) {
```

```
public Integer getF() {
public String getDirection() {
   this.direction = direction;
private String moveLeft() {
```

```
currentState = new String(tempState);
```

```
private String moveUp(){
            currentState = new String(tempState);
            currentState = new String(tempState);
           currentState = new String(tempState);
```

```
tempState[smileyPosition] = 'X';
            currentState = new String(tempState);
           currentState = new String(tempState);
private String dummyUp(){
        smileyPosition-=4;
```

```
tempState[smileyPosition] = 'X';
                tempState[smileyPosition+4] = dummy;
        String currentState = getCurrentState();
        if (smileyPosition <= 11 && smileyPosition >= 0) {
            smileyPosition+=4;
            if (currentState.charAt(smileyPosition) != '0'){
   public static LinkedList<BlockPuzzle> generateChildBfs(BlockPuzzle
parent) {
        LinkedList<BlockPuzzle> childStates = new LinkedList<>();
```

```
child2.direction = directions[1];
          child4.moveDown();
          childStates.add(child4);
          child3.parent = parent;
          child3.direction = directions[2];
          child3.moveUp();
          childStates.add(child3);
  return childStates;
* Cparam parent of the children that are going to be generated
```

child2.initialState = parent.getCurrentState();

```
@return LinkedList with the children states
    public static LinkedList<BlockPuzzle> generateChildDfs(BlockPuzzle
parent) {
        LinkedList<BlockPuzzle> childStates = new LinkedList<>();
                child1.direction = directions[0];
                child1.moveLeft();
                childStates.add(child1);
                child4.moveDown();
                childStates.add(child2);
            if (parent.isMoveUp()){
                BlockPuzzle child3 = new BlockPuzzle();
                child3.smileyPosition = parent.getSmileyPosition();
                child3.currentState = child3.initialState;
                child3.parent = parent;
                child3.stateDepth = parent.stateDepth+1;
                child3.direction = directions[2];
                child3.moveUp();
```

```
Collections.shuffle(childStates);
        return childStates;
    public static ArrayList<BlockPuzzle> generateChildDfsLIST(BlockPuzzle
parent) {
                child2.smileyPosition = parent.getSmileyPosition();
                child2.initialState = parent.getCurrentState();
                child2.stateDepth = parent.stateDepth+1;
                child2.direction = directions[1];
                child2.moveRight();
                childStates.add(child2);
                child1.initialState = parent.getCurrentState();
                child1.stateDepth = parent.stateDepth+1;
                child1.currentState = child1.initialState;
                child1.parent = parent;
                child1.direction = directions[0];
                child1.moveLeft();
                childStates.add(child1);
            if (parent.isMoveUp()){
                BlockPuzzle child3 = new BlockPuzzle();
                child3.currentState = child3.initialState;
```

```
child3.parent = parent;
                child3.direction = directions[2];
                child3.moveUp();
        return childStates;
      * @param parent of the children that are going to be generated
    public static LinkedList<BlockPuzzle> generateChildAStar(BlockPuzzle
parent) {
        LinkedList<BlockPuzzle> childStates = new LinkedList<>();
        if (parent.isMovementPossible()){
                child2.moveRight();
                childStates.add(child2);
                child1.moveLeft();
                child1.g = parent.g + 1;
                child1.moveRight();
                child1.f = manhattanDistance(child1.getCurrentState()) +
child1.q;
                childStates.add(child1);
                BlockPuzzle child3 = new BlockPuzzle();
                child3.smileyPosition = parent.getSmileyPosition();
                child3.currentState = child3.initialState;
```

```
child3.f = manhattanDistance(child3.getCurrentState()) +
child3.q;
                childStates.add(child3);
        return childStates;
     * @param parent of the children that are going to be generated
   public static ArrayList<BlockPuzzle> generateChildAStarList(BlockPuzzle
                child1.currentState = child1.initialState;
                child1.parent = parent;
                child1.direction = directions[0];
                child1.moveLeft();
                child1.f = manhattanDistance(child1.getCurrentState()) +
child1.q;
                childStates.add(child1);
            if (parent.isMoveUp()){
                BlockPuzzle child3 = new BlockPuzzle();
```

```
child3.initialState = parent.getCurrentState();
                child3.currentState = child3.initialState;
                child3.direction = directions[2];
child3.g;
                childStates.add(child3);
                child2.initialState = parent.getCurrentState();
child2.q;
                childStates.add(child2);
       return childStates;
     * @return Integer that represents the Manhattan distance
```

```
distance+=Math.abs(i-9);
    private boolean isMoveLeft() {
Math.sqrt(size);
   private boolean isMoveDown() {
        return smileyPosition <= (size-1)-Math.sqrt(size) && smileyPosition
    private boolean isMovementPossible() {
```

```
* @param o the second object that we compare
  * @return 1 if this.Object f > o.f, -1 if this.Object f < o.f, 0 if

equal
  */
  @Override
  public int compareTo(BlockPuzzle o) {
    if (this.f > o.f) {
        return 1;
    } else if (this.f < o.f) {
        return -1;
    } else {
        return 0;
    }
}</pre>
```