

Semi-Supervised Clustering Using Genetic Algorithms

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Abstract

A semi-supervised clustering algorithm is proposed that combines the benefits of supervised and unsupervised learning methods. Data are segmented/clustered using an unsupervised learning technique that is biased toward producing segments or clusters as pure as possible in terms of class distribution. These clusters can then be used to predict the class of future points. For example in database marketing, the technique can be used to identify and characterize segments of the customer population likely to respond to a promotion. One benefit of the approach is that it allows unlabeled data with no known class to be used to improve classification accuracy. The objective function of an unsupervised technique, e.g. K-means clustering, is modified to minimize both the within cluster variance of the input attributes and a measure of cluster impurity based on the class labels. Minimizing the within cluster variance of the examples is a form of capacity control to prevent overfitting. For the output labels, impurity measures from decision tree algorithms such as the Gini index can be used. A genetic algorithm optimizes the objective function to produce clusters. Non-empty clusters are labeled with the majority class. Experimental results show that using class information improves the generalization ability compared to unsupervised methods based only on the input attributes. The results also indicate that the method performs very well even when few training examples are available. Training using information from unlabeled data can improve classification accuracy on that data as well.

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1 Introduction

In this work, we examine an approach to solve classification problems that combines supervised and unsupervised learning techniques. In supervised learning, we assume we are given a set of labeled training points, and the task is to construct some function that will correctly predict the labels of future points. In unsupervised learning such as clustering, the task is to segment unlabeled training data into clusters that reflect some meaningful structure in the data. For the Semi-Supervised Learning Problem (SSLP) we assume that we are given both labeled and unlabeled points. The task is then to predict the labels of the unlabeled points using all the available labeled data, as well as unlabeled data. One would expect a better generalization ability of the resulting classifier due to the better understanding of the input distribution resulting from using all the available data. The semi-supervised learning problem can be used to perform transductive inference [17]. In transduction, we are given a set of training data and a set of testing data, and the learning task is to predict the labels of the specific testing data only. Different testing data will produce different classification functions. The intuition is that transduction is a simpler problem because we are trying to construct a function that is valid only at specific points, versus in induction where the goal is to construct a function valid at all future testing points.

Transduction was proposed with respect to support vector machines in [17]. The basic support vector machine for inductive inference finds a separating hyperplane between two different classes by maximizing the margin of separation between the classes and minimizing the misclassification error. The key notion is that capacity control based on maximizing the margin as measured on the labeled training data prevents overfitting. For transduction, the capacity control is done based on all of the available data, both labeled and unlabeled. There are

two recent approaches for constructing semi-supervised support vector machines algorithm. In [1], integer programming was used to construct linear support vector machines. Computational results on UC Irvine data sets [12] such as the ones investigated in this paper found small improvements using both labeled and unlabeled data. More recently, an iterative quadratic programming method [10] for constructing both linear and nonlinear support vector machines found that incorporating unlabeled data led to significant improvements on large information retrieval problems. Both of these approaches were based on incorporating unlabeled data into a classification method.

In this paper we take the approach of incorporating label information into an unsupervised learning approach. Our goal is to group both labeled and unlabeled data into the clusters where each cluster is as pure as possible in terms of class distribution provided by labeled data. The advantage of such an approach is that it can be used for both inductive and transductive inference. In addition the clusters help characterize segments of the population likely or unlikely to possess the target characteristic represented by the label. This additional information can be useful for several applications. For example, in database marketing only the most pure clusters of customer would be included in a marketing campaign and new products may be designed to reach customers in marginal clusters.

As a base to our semi-supervised algorithm, we use an unsupervised clustering method optimized with a genetic algorithm incorporating a measure of classification accuracy used in decision tree algorithms, the GINI index [4]. Here we examine clustering algorithms that minimize some objective function applied to k -cluster centers. Each point is assigned to the nearest cluster center by Euclidean distance. The goal is to choose the cluster centers that minimize some measure of cluster quality. Typically a cluster dispersion metric is used. If the

mean square error, a measure of within cluster variance, is used than the problem becomes similar to the classic K-means clustering [9]. We also experimented with an alternative metric, the Davis-Bouldin Index [7], that is a function of both the within cluster variance and between cluster center distances. By minimizing an objective function that minimizes a linear combination of the cluster dispersion measure and the Gini Index, the algorithm becomes semi-supervised. The details of the problem formulation are given in Section 2. Since the objective function is highly nonlinear and discontinuous with many local minima, we optimize it using the C++ based genetic algorithm library package GALib [18].

GAs are well known for being able to deal with complex search problems by implementing an evolutionary stochastic search. Because of this, GAs have been successfully applied to a variety of challenging optimization problems. The NP-hard nature of the clustering problem makes GA a natural choice for solving it such as in [2, ?, 15, 13, 6]. A common objective function in these implementations is to minimize the square error of the cluster dispersion:

$$E = \sum_{k=1}^K \sum_{x \in C_k} \|x - m_k\|^2 \quad (1)$$

where K is the number of clusters, m_k is the center of cluster C_k . This is indeed the objective function for the K-means clustering algorithms. The algorithm proposed in [15] modifies this objective function by using the inverse of Davies-Bouldin index defined in [7, 9] and minimizing it by using evolutionary programming.

GAs are also implemented in [13] to minimize the function E (1). Genomes are represented by N-bit long strings where N is the number of data points. Each bit in genomes represents cluster membership. Although proper crossover and mutation operations are defined for this scheme, it is not a scalable algorithm due to the length of the genomes.

Clustering algorithms are widely used in pattern recognition. A clustering algorithm based on GAs for machine vision is introduced in [6]. The basic problem defined in [6] is to group objects to a fixed number of clusters. A new gene representation, Boolean Matching Code (BMC), is defined in [6] as an alternative way to Linear Code (LC) used in [13]. The basic idea in BMC is that each gene represents one cluster with N binary bits where N is the number of objects. In this case the total size of solution space is 2^{KN} . Although the size of the solution space in LC is $2^{N \log K}$, BMC reaches the convergence earlier than LC by utilizing better crossover and mutation operations. A single gene crossover operation was proposed in [6].

Since the proposed algorithm performs transduction using both labeled and unlabeled data in the learning task, there are some substantial differences between the proposed algorithm in this paper and the algorithms proposed in [15, 13, 6]. But the core implementation of the GA has some similarities.

In Section 2, the problem definition and the proposed algorithm are given. Details about the GA implementation are given in Section 3. Experimental results are given in Section 4. A comparison with 3 nearest neighbor and linear and quadratic discriminant analyses is also reported in Section 4. Finally, we summarize our findings in the Section 5.

Related approaches for combining supervised and unsupervised learning exist. For example LVQ [11] and CTM [5] also use the approach of adapting a primarily unsupervised method to perform classification. This paper helps address the interesting, but still open question, of how well such methods can exploit the information in unlabeled data to support transductive inference.

2 Problem Definition

Clustering, in general, is defined as grouping similar objects together by optimizing some similarity measure for each cluster such as within group variance. Since clustering generally works in an unsupervised fashion, it is not necessarily guaranteed to group the same type (class) of objects together. In this case, we need to introduce supervision to the our learning scheme through some measure of cluster impurity. The basic idea is to find a set of clusters then minimize a linear combination of the cluster dispersion and cluster impurity measures. More specifically, select $K > 2$ cluster centers, m_k ($k = 1, \dots, K$), that minimize the following objective function:

$$\min_{m_k, k=1, \dots, K} \quad \beta * Cluster_Dispersion + \alpha * Cluster_Impurity \quad (2)$$

where $\alpha > 0$ and $\beta > 0$ are positive regularization parameters.

If $\alpha = 0$, then the result is a purely unsupervised clustering algorithm. If $\beta = 0$ the result is a purely supervised algorithm that tries to minimize the cluster impurity. As in the K-means algorithm, each point is assumed to belong to the nearest cluster center as measured by Euclidean distance. Each non-empty cluster is assigned a class label corresponding to the majority class of points belonging to that cluster. Two cluster dispersion measures from the clustering literature will be examined: mean square error (see Section 2.1) and Davis-Bouldin Index (see Section 2.2). It is important to note that for the induction case, cluster dispersion is based on the labeled training data. For the transduction case, the cluster dispersion is based on all available data, both labeled and unlabeled. For the cluster impurity measure, a measure of partition quality common in decision tree algorithms, the Gini Index, is used (see Section 2.3). Since the objective function (Eq.2) is highly discontinuous with many local

minima, we optimize it using the genetic algorithm library (see Section 3) GA-Lib. When a solution is found, it might contain clusters with little or no points assigned to them. These clusters are deleted and relevant points are reassigned to their nearest cluster centers. Practical details of this algorithm are discussed in the computational results section (see Section 4). The resulting algorithm can be summarized as follows:

Algorithm 2.1 *Semi-supervised clustering algorithm*

- *Within genetic algorithm:*
 1. *Determine cluster centers*
 2. *Partition the labeled data by distance to closest cluster center.*
 3. *Find non-empty clusters, assign a label to non-empty clusters by majority class vote within them.*
 4. *Compute dispersion and impurity measures:*
 - *Induction: Use labeled data.*
 - *Transduction: Use labeled + unlabeled data.*
- *Prune clusters with few members.*
- *Reassign the points to final non-empty clusters.*

2.1 First Dispersion Measure: MSE

The average within cluster variance is frequently used in clustering techniques as a measure of cluster quality. Commonly known as the mean square error (MSE), this quantity is defined as:

$$MSE = \frac{1}{N} \sum_{k=1}^K \sum_{x \in C_k} \|x - m_k\|^2 s, \quad (3)$$

where N is the number of points, K is the number of clusters, and m_k is the center of cluster C_k . The K-means algorithm minimizes the MSE objective.

2.2 Second Dispersion Measure:DBI

We use the Davies-Bouldin index as an alternative to MSE. DBI is determined as follows [9] : Given a partition of the N points into K clusters, one first defines the following measure of within-to-between cluster spread for two clusters, C_j and C_k for $1 \leq j, k \leq K$ and $j \neq k$.

$$R_{j,k} = \frac{e_j + e_k}{D_{jk}}, \quad (4)$$

where e_j and e_k are the average dispersion of C_j and C_k , and D_{jk} is the Euclidean distance between C_j and C_k . If m_j and m_k are the centers of C_j and C_k , then

$$e_j = \frac{1}{N_j} \sum_{x \in C_j} \|x - m_j\|^2 \quad (5)$$

and $D_{jk} = \|m_j - m_k\|^2$, where m_j is the center of cluster C_j consisting of N_j points.

The term R_k for each C_k is defined as

$$R_k = \max_{j \neq k} R_{j,k}. \quad (6)$$

Now the DBI is defined as:

$$DB(K) = 1/K \sum_{k=1}^K R_k \quad (7)$$

The DBI can be incorporated into any clustering algorithm to evaluate a particular segmentation of data. The DBI takes into account cluster dispersion

and the distance between cluster means . Well separated compact clusters are preferred. The DBI favors small numbers of clusters. Optimizing the DBI frequently eliminates clusters by forcing them to be empty.

2.3 Impurity Measure: Gini-Index

The Gini index has been used extensively in the literature to determine the impurity of a certain split in decision trees [4]. Usually, the root and intermediate nodes are partitioned to two children nodes. In this case, left and right nodes will have different Gini index values. If any split reduces the impurity, the decision tree at that node is partitioned further and the decision rule which yields the minimum impurity is selected. Clustering using K cluster centers partitions the input space into K regions. Therefore clustering can be considered as a K -nary partition at a particular node in a decision tree, and the Gini index can be applied to determine the impurity of such a partition. In this case, Gini Index of a certain cluster is computed as:

$$GiniP_j = 1.0 - \sum_{i=1}^k \left(\frac{P_{ji}}{N_j}\right)^2 \quad j \text{ in } 1, \dots, K \quad (8)$$

where P_{ji} is the number of points belong to i^{th} class in cluster j . N_j is the total number of points in cluster j . The impurity measure of a particular partitioning into K clusters is:

$$impurity = \frac{\sum_{j=1}^K T_{P_j} * GiniP_j}{N} \quad (9)$$

where N is the number of points in the dataset.

We found the Gini index to be generally preferable over other impurity measures such as the number of misclassified points. If the simple number of misclassified points is used, then the misclassified points may be distributed evenly throughout all the clusters. The Gini Index favors solutions with pure clusters

even at the expense of total classification error. Other decision tree splitting criterion such as Information Gain could also be used for cluster impurity measures [14].

3 Genetic Representation and Algorithm

The objective function (Eq. 2) defined in the previous section is discontinuous and non-convex. Finding an optimal solution to this problem is extremely difficult, so heuristic search is desirable. Heuristic search approaches such as genetic algorithms (GA), evolutionary programming, simulated annealing and tabu search have been used extensively in the literature to optimize related problems. We utilized a genetic algorithm approach because the objective function defined can be readily used as a fitness function in the GA. The authors in [15, 13, 6] used their own customized GAs for clustering. As opposed to developing a genetic algorithm from scratch, we customized the general purpose GA library, GAlib [18], utilizing the floating-point representation but otherwise utilizes Goldberg’s simple GA approach [8]. This algorithm uses non-overlapping populations. In each generation, the algorithm creates an entirely new population of individuals by selecting from the previous population then mating to produce the new offspring for the new population. This process continues until stopping criteria have been met. An the elitist strategy was applied which allows the best individual to pass to the new generation.

In a genetic algorithm application major concerns are genome representation, initialization, selection, crossover and mutation operators, stopping criteria and most importantly the fitness function. The objective function (Eq.2), defined above, is directly used as the fitness function without any scaling. The genome representation consists of an array of Kd real numbers, where d is the number of dimensions in the data and K is the number of clusters. Each set of d numbers

represents one cluster center. This type of representation brings several advantages over prior discrete representation of cluster membership. First, cluster memberships are assigned based on Euclidean distance metric in this case instead of assigning them based on the values of genome. Second, each genome requires less search space than previous applications for the large datasets, since the length of the genomes depends only on the number of clusters (K) and the dimensionality (d) of the dataset, not the number of data points. It is therefore possible to handle the large datasets with this representation.

Default genetic operators defined for `GARRealGenome` class in `GAlib` were applied. A mutation with Gaussian noise is the default in this case. Uniform crossover was applied as the default crossover operation. Although the uniform initializer is used by default, the population was initialized by sampling from the data. A uniform selection rule was used for selecting mating individuals (parents).

Two stopping criteria were applied. The algorithm stops when either of them is satisfied. One of these criteria is the maximum number of generations. The other one is the convergence after a certain number of consecutive generations.

The genetic algorithm yields reasonable results for both induction and transduction problems. The experimental findings are summarized in the next section.

4 Experimental Results

The goals in this computational approach are to determine if combining supervised and unsupervised learning approaches techniques could lead to improved generalization, and to investigate if performing transductive inference using unlabeled data for training could lead to improvements over inductive inference.

We experimented with eight datasets from the UC-Irvine Machine Learning Repository [12]¹. The datasets have all originally two-class output variable except Housing. The output variable for this dataset was categorized at the level of 21.5. Each dataset was divided into three subsets after a standard normalization. We call these subsets the learning, testing and working sets. Currently 40% of data is for learning, 30% is for testing and remaining 30% is for working sets. For each dataset, two scenarios have been tested to understand the difference between inductive and transductive inferences. For inductive inference, the algorithm is applied to labeled training data and then tested on the testing data. For transductive inference, the algorithm is applied to labeled training data, unlabeled working data, and unlabeled testing data, and then tested on the testing data.

We report experiments using seven different fitness functions. The two different cluster dispersion measures, MSE (Eq.3) and Davies-Bouldin Index (Eq.7), are applied to induction in a completely unsupervised mode ($\beta = 1, \alpha = 0$) and semi-supervised mode ($\alpha > 0, \beta > 0$), and transduction in a semi-supervised mode ($\alpha > 0, \beta > 0$). We also tried the completely supervised case based on only the Gini index ($\beta = 0, \alpha = 1$). For transduction, both the cluster dispersion measure and the Gini index are based on the labeled and unlabeled data. In transduction, the Gini index (Eq.8) becomes:

$$GiniP_j = 1.0 - \sum_{i=1}^k \left(\frac{P_{ji}}{\hat{N}_j} \right)^2 \quad j \text{ in } 1, \dots, K \quad (10)$$

\hat{N}_j is equal to number of labeled and unlabeled points in cluster j .

The best parameter set for the problem was picked by trial and error. We use same set of GA parameters for each dataset. The maximum number of

¹The datasets and their corresponding sizes are: Bright(14 variables, 2462 points), Sonar(60,208), Cleveland Heart(13,297), Ionosphere(34,351), Boston Housing(13,506), House Votes (16,435), Breast Cancer Prognosis(30,569), and Pima Diabetes (8,769)

generations is 500, mutation probability is 0.01, probability of crossover is 0.95, and number of generations to converge is 50. Experiments are conducted based on 10 bootstrap samples. For brevity only the average testing set error results are reported here. A paired t-test was used to assess the significance of difference of the testing set errors within a dataset. Errors with a p-value less than 0.2 were considered significant. To insure that the weaker performance of MSE was not based on poor choice of parameters, (K, β, α) for each dataset were chosen based on trials with the inductive MSE with Gini index². For the DBI based results, the same values of K were used for each dataset, and the fixed values of $\beta = 0.01$ and $\alpha = 0.1$ were used for all datasets.

4.1 First Dispersion Measure:MSE

The results using the first dispersion measure, MSE, are reported in Table 1. The first column, MSE-only, indicates how the totally unsupervised approach of clustering based on only the unlabeled training data would perform. The second column, GINI-only shows how the completely supervised approach of clustering using the GINI index on the labeled training data performs. The third column is the proposed approach using both the MSE and GINI based on the labeled training data. The forth column indicates how MSE+GINI performs transductive inference when all the available data is used. A **bold** number is the minimum error for a given dataset, an *italic* number indicates that the result is significantly different from the transduction result. The totally unsupervised MSE-only approach always performs significantly worse than any of the supervised methods. Surprisingly, the GINI-only complete supervised approach was the best on four of the eight datasets. The transductive MSE+GINI method based on all available data showed no consistent improvements over the induc-

²The (k, β, α) values applied for each dataset were bright (15, 0.01, 0.99), sonar (7, 0.1, 1), heart (7, 0.25, 0.75), ionosphere (7, 0.01, 0.99), house (7, 0.1, 0.9), housing (11, 0.01, 0.99), prognosis (11, 0.4, 0.6), and pima (11, 0.01, 0.99).

tion approach. This is consistent with other researchers who have reported that doing transductive inference using a regression estimate where the variance estimate was based on all the available data (both labeled and unlabeled) actually degraded results [3].

The MSE based approaches showed poor performance. To examine why consider the results of the MSE-based fitness functions on the cartoon example shown in Figure 4.1. The top plot shows the induction result (using just labeled data) and the bottom plot shows the transduction result (using both labeled and unlabeled data) cases. Note that on the center cluster transduction does work appropriately. The inductive MSE+GINI method does not separate the cluster in the center of the figure, because such separation will result an impure cluster on the right. Using the additional unlabeled data, the transductive MSE+GINI reduces cluster dispersion by splitting the center cluster (bottom of Figure 1). On the other hand, both the transductive MSE+GINI method does not catch the downward shift of the top right cluster. Because the added unlabeled points are roughly equal distance from two top right cluster centers, adding unlabeled data has little effect despite the fact that a natural gap exists between the two clusters. The MSE minimizes only the compactness of the clusters. It is necessary to find clusters that are both compact and well separated. The DBI index is much more effective in this regard and the computational results are greatly improved when this cluster dispersion metric is applied.

4.2 Second Dispersion Measure:DBI

The DBI dispersion measure was much more effective than the MSE with regards to transduction. For the cartoon example, the top of the Figure 2 shows the resulting partition after using DBI in fitness function for the induction case. By using DBI, the method was able to catch the vertical shift within the data in

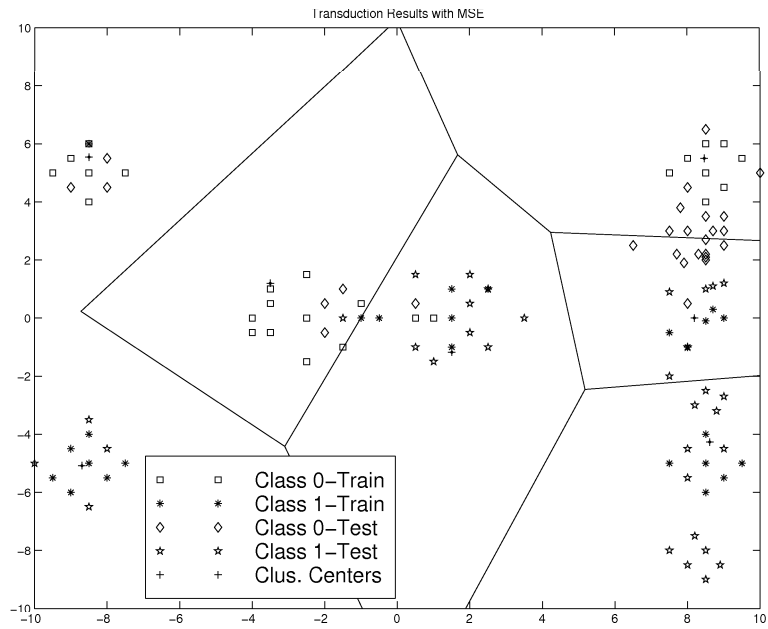
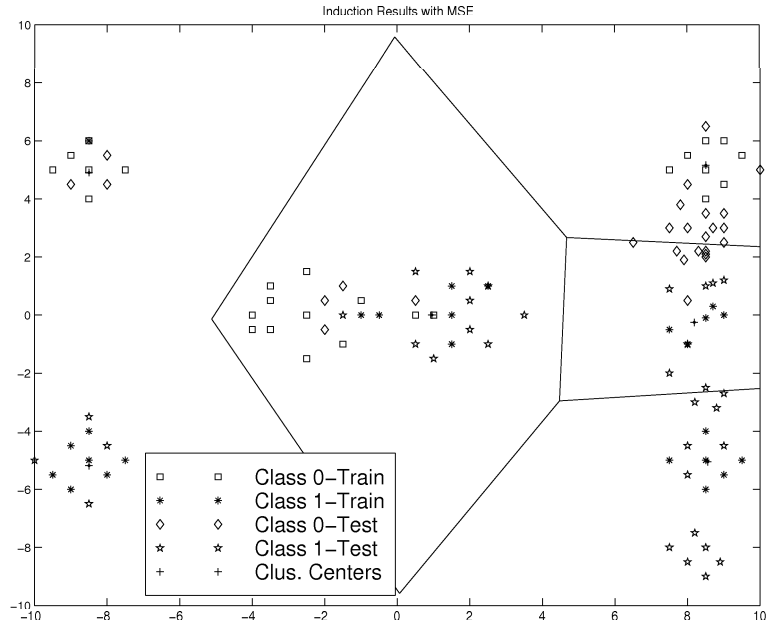


Figure 1: Induction and Transduction Results using MSE

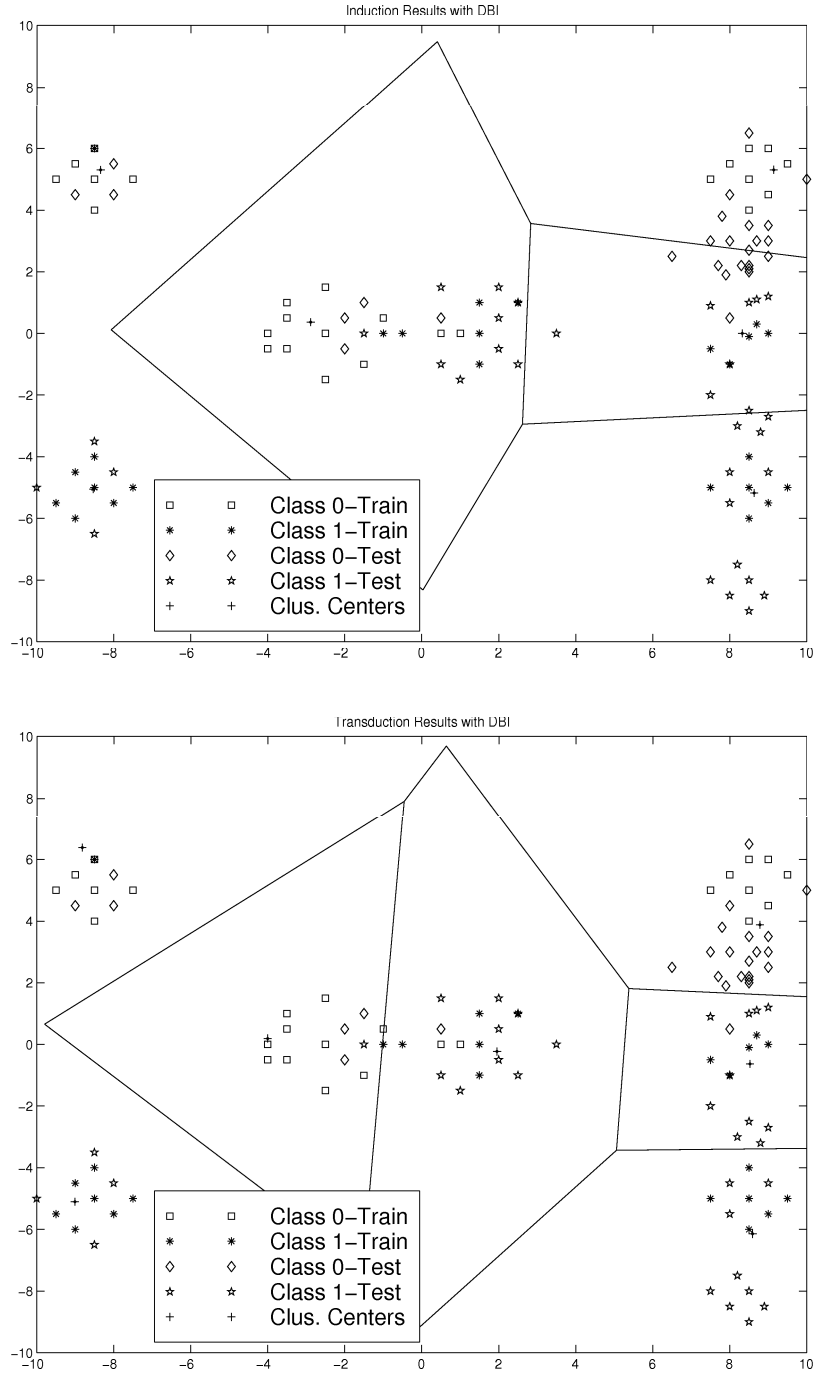


Figure 2: Induction and Transduction Results using DBI

transductive inference. The results for the DBI dispersion measure (Eq.7) on the UC-Irvine Data are reported in Table 2. The same experimental setup and parameters as mentioned above were used except that the maximum number of generations is set to 300. The same K was used as in MSE approach, but the regularization parameters due to the different magnitude of the DBI. As a purely unsupervised approach DBI-only was even worse than MSE-only at classification. The inductive DBI+GINI approach was not significantly different from the GINI-Only approach. The transductive DBI+GINI was either better or not significantly worse than GINI-only approach. Transductive DBI+GINI consistently produced the best classification results of all the seven approaches tested primarily due to the more compact and better separated clusters found by DBI over MSE. The evidence indicates that capacity control based on both labeled and unlabeled data is much more effective using the DBI criterion than MSE.

Another finding from the results is that DBI dispersion measure favors a fewer number of non-empty clusters compared to the MSE dispersion measure. On average, using DBI dispersion measure resulted in 53.33%, 33.33%, 28.36%, 17.91%, 30.84%, 33.33%, 51.11% and 50.91% fewer non-empty clusters than MSE dispersion measure for transductive inference on the UCI datasets respectively.

In Table 3, results from some other classification techniques are compared with transductive DBI+GINI – specifically 3 nearest neighbor classifier, linear and quadratic discriminant classifiers. The discriminant analysis was done using the SAS procedure DISCRIM [16]. All results are reported on the test datasets. The DBI-GINI is consistently one of the better methods.

Table 1: Results Using MSE in Fitness Function

	Induction			Transduction
Data Set	MSE-Only	GINI-Only	MSE+GINI	MSE+GINI
Bright	<i>0.06585</i>	0.01084	0.02507	0.02263
Sonar	<i>0.43279</i>	0.2541	0.22951	0.26066
Heart	<i>0.23636</i>	<i>0.21477</i>	0.2	0.19659
Iono.	<i>0.25673</i>	0.14423	0.12788	0.12981
Housing	<i>0.25828</i>	0.15629	<i>0.18874</i>	0.16887
House	<i>0.09846</i>	0.06692	0.06	0.06308
Prognos.	<i>0.1</i>	0.05059	<i>0.06235</i>	0.05235
Pima	<i>0.32402</i>	0.27118	0.30131	0.30393

Table 2: Results Using DBI in Fitness Function

	Induction			Transduction
Data Set	DBI-Only	GINI-Only	DBI+GINI	DBI+GINI
Bright	<i>0.26897</i>	0.01084	<i>0.01992</i>	0.01165
Sonar	<i>0.50656</i>	0.2541	<i>0.27049</i>	0.23771
Heart	<i>0.3841</i>	<i>0.21477</i>	<i>0.21136</i>	0.19155
Iono.	<i>0.34327</i>	0.14423	0.12885	0.13558
Housing	<i>0.4563</i>	0.15629	<i>0.17086</i>	0.15497
House	<i>0.11769</i>	0.06692	0.07462	0.06923
Prognos.	<i>0.38059</i>	<i>0.05059</i>	<i>0.04941</i>	0.04353
Pima	<i>0.34585</i>	0.27118	0.28428	0.28122

Table 3: Comparison between Transductive DBI+GINI and 3-NN, LD, and QD

Data Set	3-NN	LinDisc	QuadDisc	DBI+GINI
Bright	<i>0.01247</i>	<i>0.02387</i>	<i>0.02112</i>	0.01165
Sonar	0.2098	<i>0.38025</i>	<i>0.35256</i>	0.23771
Heart	0.19773	0.1745	<i>0.22334</i>	0.19155
Iono.	<i>0.18846</i>	0.14624	0.1294	0.13558
Housing	<i>0.16291</i>	0.16013	<i>0.19946</i>	0.15497
House	0.06154	0.0414	0.06995	0.06923
Prognos.	0.04235	0.04797	<i>0.05348</i>	0.04353
Pima	0.28777	0.2313	<i>0.26401</i>	0.28122

5 Conclusion

A novel method for semi-supervised learning that combines supervised and unsupervised learning techniques has been introduced in this paper. The basic idea is to take an unsupervised clustering method, label each cluster with class membership, and simultaneously optimize the misclassification error of the resulting clusters. The intuition behind the approach is that the unsupervised component of objective acts like a form of regularization or capacity control during supervised learning to avoid overfitting. The objective function is a linear combination of a measure of cluster dispersion and a measure of cluster impurity. The method can exploit any available unlabeled data during training since the cluster dispersion measure does not require class labels. This allows the approach to be used for transductive inference, the process of constructing a classifier using both the labeled training data and the unlabeled testing data. Experimental results also show that using DBI for cluster dispersion instead of MSE helps transductive inference. This is due to the compact and well separated clusters found by minimizing DBI. DBI finds solution using much fewer clusters than MSE with much greater accuracy. The basic ideas in this paper: incorporating classification information into an unsupervised algorithm and using the resulting algorithm for transductive inference are applicable to many types of unsupervised learning and are promising areas of future research.

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