

$$\mathbf{MT} = \begin{pmatrix} \cos(\theta) & \cos(\alpha) (-\sin(\theta)) & \sin(\alpha) \sin(\theta) & a \cos(\theta) \\ \sin(\theta) & \cos(\alpha) \cos(\theta) & \sin(\alpha) (-\cos(\theta)) & a \sin(\theta) \\ 0 & \sin(\alpha) & \cos(\alpha) & d \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\text{Out[16]=} \begin{pmatrix} \cos(\theta) & -\cos(\alpha) \sin(\theta) & \sin(\alpha) \sin(\theta) & a \cos(\theta) \\ \sin(\theta) & \cos(\alpha) \cos(\theta) & -\cos(\theta) \sin(\alpha) & a \sin(\theta) \\ 0 & \sin(\alpha) & \cos(\alpha) & d \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{MT01} = \mathbf{MT} /. \{\theta \rightarrow \theta1, d \rightarrow 0, \alpha \rightarrow 0, a \rightarrow 11\}$$

$$\text{Out[17]=} \begin{pmatrix} \cos(\theta1) & -\sin(\theta1) & 0 & 11 \cos(\theta1) \\ \sin(\theta1) & \cos(\theta1) & 0 & 11 \sin(\theta1) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{MT12} = \mathbf{MT} /. \{\theta \rightarrow \theta2, d \rightarrow 0, \alpha \rightarrow 0, a \rightarrow 12\}$$

$$\text{Out[18]=} \begin{pmatrix} \cos(\theta2) & -\sin(\theta2) & 0 & 12 \cos(\theta2) \\ \sin(\theta2) & \cos(\theta2) & 0 & 12 \sin(\theta2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{MT23} = \mathbf{MT} /. \{\theta \rightarrow -\theta3, d \rightarrow 0, \alpha \rightarrow 0, a \rightarrow 13\}$$

$$\text{Out[19]=} \begin{pmatrix} \cos(\theta3) & \sin(\theta3) & 0 & 13 \cos(\theta3) \\ -\sin(\theta3) & \cos(\theta3) & 0 & -13 \sin(\theta3) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{MT02} = \text{FullSimplify}[\mathbf{MT01}.\mathbf{MT12}]$$

[\[simplifica completamente\]](#)

$$\text{Out[20]=} \begin{pmatrix} \cos(\theta1 + \theta2) & -\sin(\theta1 + \theta2) & 0 & 11 \cos(\theta1) + 12 \cos(\theta1 + \theta2) \\ \sin(\theta1 + \theta2) & \cos(\theta1 + \theta2) & 0 & 11 \sin(\theta1) + 12 \sin(\theta1 + \theta2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{MT03} = \text{FullSimplify}[\mathbf{MT01}.\mathbf{MT12}.\mathbf{MT23}]$$

[\[simplifica completamente\]](#)

$$\text{Out[21]=} \begin{pmatrix} \cos(\theta1 + \theta2 - \theta3) & -\sin(\theta1 + \theta2 - \theta3) & 0 & 11 \cos(\theta1) + 12 \cos(\theta1 + \theta2) + 13 \cos(\theta1 + \theta2 - \theta3) \\ \sin(\theta1 + \theta2 - \theta3) & \cos(\theta1 + \theta2 - \theta3) & 0 & 11 \sin(\theta1) + 12 \sin(\theta1 + \theta2) + 13 \sin(\theta1 + \theta2 - \theta3) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{Ori} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\text{Out[22]=} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\mathbf{P1} = \begin{pmatrix} \mathbf{x1} \\ \mathbf{y1} \\ \mathbf{0} \\ \mathbf{1} \end{pmatrix}$$

$$\text{Out[23]} = \begin{pmatrix} \mathbf{x1} \\ \mathbf{y1} \\ \mathbf{0} \\ \mathbf{1} \end{pmatrix}$$

**MT01**

$$\text{Out[24]} = \begin{pmatrix} \cos(\theta 1) & -\sin(\theta 1) & 0 & l1 \cos(\theta 1) \\ \sin(\theta 1) & \cos(\theta 1) & 0 & l1 \sin(\theta 1) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

**MT01.Ori**

$$\text{Out[25]} = \begin{pmatrix} l1 \cos(\theta 1) \\ l1 \sin(\theta 1) \\ 0 \\ 1 \end{pmatrix}$$

**MT02.Ori**

$$\text{Out[26]} = \begin{pmatrix} l1 \cos(\theta 1) + l2 \cos(\theta 1 + \theta 2) \\ l1 \sin(\theta 1) + l2 \sin(\theta 1 + \theta 2) \\ 0 \\ 1 \end{pmatrix}$$

**MT03.Ori**

$$\text{Out[27]} = \begin{pmatrix} l1 \cos(\theta 1) + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 - \theta 3) \\ l1 \sin(\theta 1) + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 - \theta 3) \\ 0 \\ 1 \end{pmatrix}$$

**MT02.Ori /. { $\theta 1 \rightarrow \frac{\pi}{2}$ ,  $\theta 2 \rightarrow \frac{\pi}{2}$ ,  $l1 \rightarrow 150$ ,  $l2 \rightarrow 80$ }**

$$\text{Out[28]} = \begin{pmatrix} -80 \\ 150 \\ 0 \\ 1 \end{pmatrix}$$