Exercise 7.1

Q.1 Solve the following equations

(i)
$$\frac{2}{3}x - \frac{1}{2}x = x + \frac{1}{6}$$

Solution:
$$\frac{2}{3}x - \frac{1}{2}x = x + \frac{1}{6}$$

$$\frac{4x-3x}{6} = \frac{6x+1}{6}$$

$$x = 6\frac{(6x+1)}{6}$$

$$x = 6x + 1$$

$$-6x + x = 1$$

$$-5x = 1$$

$$x = \frac{1}{-5}$$

$$x = -\frac{1}{5}$$

To check

Substitution
$$x = -\frac{1}{5}$$

$$\frac{2}{3} \times \frac{-1}{5} - \frac{1}{2} \times \frac{-1}{5} = \frac{-1}{5} + \frac{1}{6}$$

$$\frac{-2}{15} + \frac{1}{10} = \frac{-6+5}{30}$$

$$\frac{-2\times2+1\times3}{30} = \frac{-1}{30}$$

$$\frac{-4+3}{30} = \frac{-1}{30}$$

$$\frac{-1}{30} = \frac{-1}{30}$$

Solution Set =
$$\left\{-\frac{1}{5}\right\}$$

(ii)
$$\frac{x-3}{3} - \frac{x-2}{2} = -1$$

Solution
$$\frac{x-3}{3} - \frac{x-2}{2} = -1$$

By taking L.C.M

$$\frac{2(x-3)-3(x-2)}{6} = -1$$
$$2x-6-3x+6=-6$$

-x = -6

Multiplying both sets by −1

$$-1 \times -x = -1 \times -6$$

$$x = 6$$

To check

$$\frac{x-3}{3} - \frac{x-2}{2} = -1$$

$$\frac{6-3}{3} - \frac{6-2}{2} = -1$$

$$\frac{3}{3} - \frac{4}{2} = -1$$

$$\frac{6-12}{6} = -1$$

$$\frac{\sqrt{6}}{6} = -1$$

$$-1 = -1$$

Solution Set $= \{6\}$

(iii) $\frac{1}{2}\left(x-\frac{1}{6}\right)+\frac{2}{3}=\frac{5}{6}+\frac{1}{3}\left(\frac{1}{2}-3x\right)$

Solution
$$\frac{1}{2} \left(x - \frac{1}{6} \right) + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left(\frac{1}{2} - 3x \right)$$

$$\frac{1}{2} \left(\frac{6x-1}{6} \right) + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left(\frac{1-6x}{2} \right)$$

$$\frac{6x-1}{12} + \frac{2}{3} = \frac{5}{6} + \frac{1-6x}{6}$$

$$\frac{6x-1+8}{12} = \frac{5+1-6x}{6}$$

$$\frac{\cancel{8}(6x+7)}{\cancel{12}^2} = 6-6x$$

$$\frac{6x+7}{2} = 6-6x$$

$$6x + 7 = 2(6 - 6x)$$

$$6x + 7 = 12 - 12x$$

$$6x + 12x = 12 - 7$$

$$18x = 5$$

$$x = \frac{5}{18}$$

When
$$x = \frac{5}{18}$$

$$\frac{1}{2} \left[\frac{15}{18} - \frac{1}{6} \right] + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left[\frac{1}{2} - 3 \left(\frac{5}{18} \right) \right]$$

$$\frac{1}{2} \left[\frac{5-3}{18} \right] + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left[\frac{1}{2} - \frac{5}{6} \right]$$

$$\frac{1}{2} \left[\frac{2}{18} \right] + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left[\frac{3-5}{6} \right]$$

$$\frac{1}{2} \left[\frac{2}{18} \right] + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left[\frac{-2^{1}}{6^{3}} \right]$$

$$\frac{1}{18} + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left[\frac{-1}{3} \right]$$

$$\frac{1+12}{18} = \frac{5}{6} \cdot \frac{1}{9}$$

$$\frac{13}{18} = \frac{15 - 2}{18}$$

$$\frac{13}{18} = \frac{13}{18}$$

Solution Set =
$$\left\{ \frac{5}{18} \right\}$$

(iv)
$$x + \frac{1}{3} = 2 \left[x - \frac{2}{3} \right] - 6x$$

Solution
$$x + \frac{1}{3} = 2\left[x - \frac{2}{3}\right] - 6x$$

$$\frac{3x+1}{3} = 2\left\lceil \frac{3x-2}{3} \right\rceil - 6x$$

$$\frac{3x+1}{3} = \frac{6x-4}{3} - 6x$$

Taking L.C.M of right side

$$\frac{3x+1}{2} = \frac{6x-4-18x}{2}$$

$$\frac{3x+1}{\cancel{2}} = \frac{\left(-12x-4\right)}{\cancel{2}}$$

$$3x+1 = -12x-4$$

$$3x + 12x = -4 - 1$$

$$15x = -5$$

$$x = \frac{-5}{15}$$

$$x = \frac{-1}{3}$$

To check

$$x + \frac{1}{3} = 2\left[x - \frac{2}{3}\right] - 6x$$

When
$$x = \frac{-1}{3}$$

$$\frac{-1}{\sqrt{3}} + \frac{1}{\sqrt{3}} = 2 \left[-\frac{1}{3} - \frac{2}{3} \right] - 6 \left(-\frac{1}{3} \right)$$

$$0=2\left[\frac{-1-2}{3}\right]+\frac{1}{3}$$

$$0=2\left[\frac{-\cancel{3}}{\cancel{3}}\right]+2$$

$$0=2(-1)+2$$

Solution Set =
$$\left\{ \frac{-1}{3} \right\}$$

 $5 + \frac{1}{5(x-3)}$

(v)
$$\frac{5(x-3)}{6} - x = 1 - \frac{x}{9}$$

Solution $\frac{5(x-3)}{6} - x = 1 - \frac{x}{9}$

$$\frac{5x - 15 - 6x}{6} = \frac{9 - x}{9}$$

$$\frac{-15-x}{6} = \frac{9-x}{9}$$

$$9(-15-x)=6(9-x)$$

$$-135 - 9x = 54 - 6x$$

$$-135 - 54 = -6x + 9x$$

$$-189 = 3x$$

$$\frac{-189}{3} = x$$

$$x = -63$$

$$\frac{5(x-3)}{6} - x = 1 - \frac{x}{9}$$

When
$$x = -63$$

$$\frac{5(-63-3)}{6} - (-63) = 1 - \frac{(-63)^{7}}{9}$$

$$\frac{5(-66^{11})}{6} + 63 = 1 + 7$$

(vi)
$$\frac{x}{3x-6} = 2 - \frac{2x}{x-2}, x \neq 2$$

Solution
$$\frac{x}{3x-6} = 2 - \frac{2x}{x-2}, x \neq 2$$

$$\frac{x}{3(x-2)} = \frac{2(x-2)-2x}{x-2}$$

$$\frac{x}{3(x-2)} = \frac{2x-4-2x}{x-2}$$

$$\frac{x}{3(x-2)} = \frac{-4}{x-2}$$

$$x(x-2) = -4 \times 3(x-2)$$

$$x(x-2) = -12(x-2)$$

$$x(x-2)+12(x-2)=0$$

$$(x-2)(x+12)=0$$

$$x - 2 = 0$$
, or $x + 12 = 0$

$$x = 2$$
, or $x = -12$

$$x = 2$$
 (Rejected because $x \neq 2$)

Hence x = -12

To check

$$\frac{x}{3x-6} = 2 - \frac{2x}{x-2}$$

When x = -12

$$\frac{-12}{3(-12)-6} = 2 - \frac{2(-12)}{-12-2}$$

$$\frac{-12}{-36-6} = 2 + \frac{24}{-14}$$

$$\frac{-12}{-42} = 2 - \frac{24}{14}$$

$$\frac{12}{42} = 2 - \frac{12}{7}$$

$$\frac{2}{7} = \frac{14 - 12}{7}$$

$$\frac{2}{7} = \frac{2}{7}$$

Solution Set={-12}

(vii)
$$\frac{2x}{2x+5} = \frac{2}{3} - \frac{5}{4x+10}$$

Solution $\frac{2x}{2x+5} = \frac{2}{3} - \frac{5}{4x+10}$

$$\frac{2x}{2x+5} = \frac{2(4x+10)-3\times5}{3(4x+10)}$$

$$\frac{2x \times 3(4x+10)}{2x+5} = 8x+20-15$$

$$\frac{6x \times 2\left(2x+5\right)}{\left(2x+5\right)} = 8x+5$$

$$12x = 8x + 5$$

$$12x - 8x = 5$$

$$4x = 5$$

$$x = \frac{5}{4}$$

$$\frac{2x}{2x+5} = \frac{2}{3} - \frac{5}{4x+10}$$

When
$$x = \frac{5}{4}$$

$$\frac{2\left(\frac{5}{4}\right)}{2\left(\frac{5}{4}\right)+5} = \frac{2}{3} - \frac{5}{4\left(\frac{5}{4}\right)+10}$$

$$\frac{\frac{5}{2}}{\frac{5}{2}+5} = \frac{2}{3} - \frac{5}{5+10}$$

$$\frac{\frac{5}{2}}{\frac{5+10}{2}} = \frac{2}{3} - \frac{5}{15}$$

$$\frac{\frac{5}{2}}{\frac{15}{2}} = \frac{2}{3} - \frac{1}{3}$$

$$\frac{\cancel{5}}{\cancel{2}} \times \frac{\cancel{2}}{\cancel{\cancel{2}}} = \frac{2-1}{3}$$

$$\frac{1}{3} = \frac{1}{3}$$

Solution Set =
$$\left\{\frac{5}{4}\right\}$$

(viii)
$$\frac{2x}{x-1} + \frac{1}{3} = \frac{5}{6} + \frac{2}{x-1}$$
 $x \ne 1$

Solution
$$\frac{2x}{x-1} + \frac{1}{3} = \frac{5}{6} + \frac{2}{x-1}$$
 $x \ne 1$
$$\frac{3 \times 2x + 1(x-1)}{3(x-1)} = \frac{5(x-1) + 2 \times 6}{6(x-1)}$$

$$\frac{6x+x-1}{3(x-1)} = \frac{5x-5+12}{6(x-1)}$$

$$\frac{7x-1}{3(x-1)} = \frac{5x-5+12}{6(x-1)}$$

$$7x-1 = \frac{5(x-1)(5x+7)}{(x-1)}$$

$$2(7x-1)=5x+7$$

$$14x - 2 = 5x + 7$$

$$14x - 5x = 4 + 2$$

$$9x = 9$$

$$x=\frac{9}{9}$$

$$x=1$$

No solution because $x \neq 1$.

(ix)
$$\frac{2}{x^2 - 1} - \frac{1}{x+1} = \frac{1}{x+1} \quad x \neq \pm 1$$
Solution
$$\frac{2}{x^2 - 1} - \frac{1}{x+1} = \frac{1}{x+1} \quad x \neq \pm 1$$

$$\frac{2}{(x-1)(x+1)} - \frac{1}{x+1} = \frac{1}{x+1}$$

$$\frac{2 - (x - 1)}{(x - 1)(x + 1)} = \frac{1}{x + 1}$$

$$\frac{2 - (x - 1)}{(x - 1)(x + 1)} = \frac{1}{x + 1}$$

$$2-x+1=\frac{(x-1)(x+1)}{(x+1)}$$

$$3 - x = x - 1$$

$$1+3=x+x$$

$$4=2x$$

$$\frac{4}{2} = x$$

$$x = 2$$

To check

$$\frac{2}{2^2 - 1} - \frac{1}{2 + 1} = \frac{1}{2 + 1}$$

$$\frac{2}{4 - 1} - \frac{1}{3} = \frac{1}{3}$$

$$\frac{2}{3} - \frac{1}{3} = \frac{1}{3}$$

$$\frac{2 - 1}{3} = \frac{1}{3}$$

$$\frac{1}{3} = \frac{1}{3}$$

Solution Set =
$$\{2\}$$

(x)
$$\frac{2}{3x+6} = \frac{1}{6} - \frac{1}{2x+4}$$

Solution
$$\frac{2}{3x+6} = \frac{1}{6} - \frac{1}{2x+4}$$

$$\frac{2}{3(x+2)} = \frac{1}{6} - \frac{1}{2(x+2)}$$

$$\frac{2}{3(x+2)} = \frac{x+2-3}{6(x+2)}$$

$$\frac{2\times 6(x+2)}{3(x+2)} = x-1$$

$$4 = x - 1$$

 $4 + 1 = x$

$$4+1 = x$$
$$x = 5$$

$$\frac{2}{3(5)+6} = \frac{1}{6} - \frac{1}{2(5)+4}$$

$$\frac{2}{15+6} = \frac{1}{6} - \frac{1}{10+4}$$

$$\frac{2}{21} = \frac{1}{6} - \frac{1}{14}$$

$$\frac{2}{21} = \frac{7-3}{42}$$

$$\frac{\overline{21}}{2}$$
 $\frac{\overline{42}}{42}$

$$\frac{2}{21} = \frac{\cancel{A}^2}{\cancel{A2}^{21}}$$

$$\frac{2}{21} = \frac{2}{21}$$

Solution Set = $\{5\}$



Q.2 Check each equation and check for extraneous solution, if any

(i)
$$\sqrt{3x+4} = 2$$

Solution: $\sqrt{3x+4} = 2$
Taking square on both side $(\sqrt{3x+4})^2 = (2)^2$
 $3x+4=4$

$$3x = 4 - 4$$
$$3x = 0$$
$$x = \frac{0}{3}$$

$$x = 0$$

To check

$$\sqrt{3x + 4} = 2$$
When $x = 0$

$$\sqrt{3(0)+4} = 2$$

$$\sqrt{4} = 2$$
$$2 = 2$$

$$\vec{L}.H.\vec{S} = R.H.S$$

Solution Set = $\{0\}$

(ii)
$$\sqrt[3]{2x-4} - 2 = 0$$

Solution: $\sqrt[3]{2x-4} - 2 = 0$
 $\sqrt[3]{2x-4} = 2$

Taking cube on both sides

$$\left(\sqrt[3]{2x-4}\right)^3 = (2)^3$$

$$2x - 4 = 8$$

$$2x = 8 + 4$$

$$2x = 12$$

$$x = \frac{12}{2}$$

$$x = 6$$

To check

$$\sqrt[3]{2x-4}-2=0$$

When
$$x = 6$$

$$\sqrt[3]{2x-4} - 2 = 0$$

$$\sqrt[3]{2(6)-4}-2=0$$

$$\sqrt{12-4}-2=0$$

$$\sqrt[3]{8} - 2 = 0$$

$$\sqrt[3]{2^3} - 2 = 0$$

$$2-2=0\\
0=0$$

$$L.H.S = R.H.S$$

Solution Set =
$$\{6\}$$

(iii)
$$\sqrt{x-3} - 7 = 0$$

Solution: $\sqrt{x-3} - 7 = 0$

$$\sqrt{x-3} = 7$$

Taking square on both side

$$\left(\sqrt{x-3}\right)^2 = \left(7\right)^2$$

$$x-3=49$$

$$x = 49 + 3$$

$$x = 52$$

$$\sqrt{x-3} - 7 = 0$$

When
$$x = 52$$

$$\sqrt{52-3}-7=0$$

$$\sqrt{49} - 7 = 0$$

$$7 - 7 = 0$$

$$0 = 0$$

$$L.H.S = R.H.S$$

Solution Set = $\{52\}$

(iv)
$$2\sqrt{t+4} = 5$$

Solution: $2\sqrt{t+4} = 5$

Taking square on both side

$$\left(2\sqrt{t+4}\right)^2 = \left(5\right)^2$$

$$4(t+4)=25$$

$$t+4=\frac{25}{4}$$

$$t = \frac{25}{4} - 4$$

$$t = \frac{25 - 16}{4}$$

$$t = \frac{9}{4}$$

$$2\sqrt{t+4} = 5$$

When
$$t = \frac{9}{4}$$

$$2\sqrt{\frac{9}{4}+4}=5$$

$$2\sqrt{\frac{9+16}{4}} = 5$$

$$2\sqrt{\frac{25}{4}} = 5$$

$$2 \times \frac{5}{2} = 5$$

$$5 = 5$$
L.H.S = R.H.S

Solution Set = $\left\{\frac{9}{4}\right\}$

(v)
$$\sqrt[3]{2x+3} = \sqrt[3]{x-2}$$

Solution: $\sqrt[3]{2x+3} = \sqrt[3]{x-2}$
Taking cube on both sides
 $(\sqrt[3]{2x+3})^3 = (\sqrt[3]{x-2})^3$
 $2x+3=x-2$
 $2x-x=-2-3$
 $x=-5$
To check
 $\sqrt[3]{2x+3} = \sqrt[3]{x-2}$
When $x=-5$
 $\sqrt[3]{2(-5)+3} = \sqrt[3]{-5-2}$
 $\sqrt[3]{-10+3} = \sqrt[3]{-7}$
 $\sqrt[3]{-7} = \sqrt[3]{-7}$
L.H.S = R.H.S
Solution Set = $\{-5\}$

(vi)
$$\sqrt[3]{2-t} = \sqrt[3]{2t-28}$$

Solution: $\sqrt[3]{2-t} = \sqrt[3]{2t-28}$
Taking cube on both sides
$$(\sqrt[3]{2-t})^3 = (\sqrt[3]{2t-28})^3$$

$$2-t = 2t-28$$

$$2+28 = 2t+t$$

$$30 = 3t$$

$$\frac{30}{3} = t$$

$$t = 10$$
To check
$$\sqrt[3]{2-t} = \sqrt[3]{2t-28}$$
When $t = 10$

$$\sqrt[3]{2-10} = \sqrt[3]{2(10)-28}$$

$$\sqrt[3]{-8} = \sqrt[3]{20-28}$$

$$\sqrt[3]{-8} = \sqrt[3]{-8}$$
L.H.S = R.H.S
Solution Set = $\{10\}$

(vii)
$$\sqrt{2t+6} - \sqrt{2t-5} = 0$$

Solution: $\sqrt{2t+6} - \sqrt{2t-5} = 0$
 $\sqrt{2t+6} = \sqrt{2t-5}$
Taking square on both side
 $(\sqrt{2t+6})^2 = (\sqrt{2t-5})^2$
 $2t+6=2t-5$
 $2t-2t=-5-6$
 $0=-11$
Solution is not possible
Solution Set={} or ϕ
(viii) $\sqrt{\frac{x+1}{2x+5}} = 2$ $x \neq \frac{-5}{2}$
Taking square on both side
 $(\sqrt{\frac{x+1}{2x+5}})^2 = (2)^2$
 $\frac{x+1}{2x+5} = 4$
 $x+1=4(2x+5)$
 $x+1=8x+20$
 $1-20=8x-x$
 $-19=7x$
 $-\frac{19}{7}=x$
Or, $x=\frac{-19}{7}$
To check
 $\sqrt{\frac{x+1}{2x+5}} = 2$
When $x=\frac{-19}{7}$
 $\sqrt{(\frac{-19}{7}+1)} \div [2 \times \frac{-19}{7}+5] = 2$
 $\sqrt{\frac{-12}{7}} \div [\frac{-38+35}{7}] = 2$

$$\sqrt{\frac{-\cancel{\cancel{\cancel{2}}}^4}{\cancel{\cancel{\cancel{7}}}} \times \frac{\cancel{\cancel{\cancel{7}}}}{-\cancel{\cancel{\cancel{\cancel{3}}}}} = 2$$

$$\sqrt{4} = 2$$

$$L = L$$

 $L.H.S = R.H.S$

Solution Set =
$$\left\{ \frac{-19}{7} \right\}$$

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Report any mistake at freeilm786@gmail.com



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