

# Exercise 10.3

In the figure,  $\overline{AB} \cong \overline{DC}$ ,  $\overline{AD} \cong \overline{BC}$  prove that  $\angle A = \angle C$ ,  $\angle ABC \cong \angle ADC$ **Q.1** 

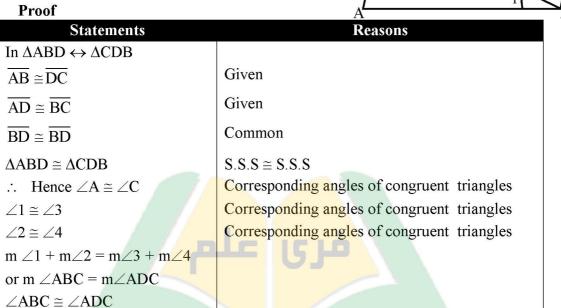
Given

In the figure  $\overline{AB} \cong \overline{DC}$ ,  $\overline{AD} \cong \overline{BC}$ 

To prove

 $\angle A \cong \angle C$ 

 $\angle ABC \cong \angle ADC$ 



In the figure  $\overline{LN}\cong \overline{MP}$ ,  $\overline{MN}\cong \overline{LP}$  prove that  $\angle N\cong \angle P$ ,  $\angle NML\cong \angle PLM$ 0.2

Given

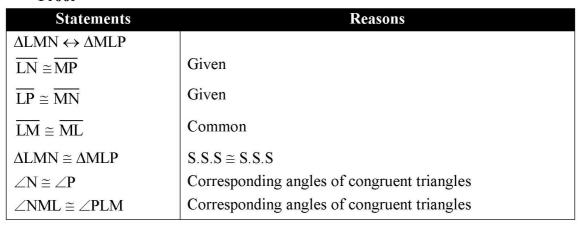
In the figure

 $\overline{LN}\cong\overline{MP}$  and  $\overline{LP}\cong\overline{MN}$ 

To prove

 $\angle N \cong \angle P$  and  $\angle NML \cong \angle PLM$ 

**Proof** 



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Q.3 Prove that median bisecting the base of an isosceles triangle bisects the vertex angle and it is perpendicular to the base

#### Given

$$\Delta ABC$$

(i) 
$$\overline{AB} \cong \overline{AC}$$

(ii) Point P is mid point of  $\overline{BC}$  i.e:  $\overline{BP} = \overline{CP}$ 

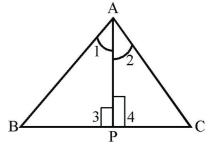
P is joined to A, i.e.  $\overline{AP}$  is median

### To prove

$$\angle 1 \cong \angle 2$$

$$\overline{AP} \perp \overline{BC}$$

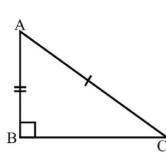
## Proof

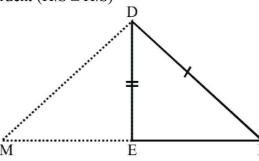


Statements	Reasons
$\triangle ABP \leftrightarrow \triangle ACP$	
$\overline{AB} \cong \overline{AC}$	Given
$\overline{BP} \cong \overline{CP}$	Given
$\overline{AP} \cong \overline{AP}$	Common
$\Delta ABP \cong \Delta ACP$	$S.S.S \cong S.S.S$
∠1 ≅ ∠2	Corresponding angles of congruent triangles
∠3 ≅ ∠4(i)	TE GP
$m \angle 3 + m \angle 4 = 180^{\circ}$ (ii)	Corresponding angles of congruent triangles
Thus $m \angle 3 = m \angle 4 = 90$	
$\therefore \overline{AP} \perp \overline{BC}$	From equation (i) and (ii)

## **Theorem 10.1.4**

If in the corresponding of the two right angled triangles, the hypotenuse and one side of one triangle are congruent to the hypotenuse and the corresponding side of the other them the triangles are congruent  $(H.S \cong H.S)$ 





#### Given

$$\triangle ABC \leftrightarrow \triangle DEF$$

$$\angle B \cong \angle E$$
 (right angles)

$$\overline{CA} \cong \overline{FD}, \overline{AB} \cong \overline{DE}$$

#### To Prove

$$\triangle ABC \cong \triangle DEF$$

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#### Construction

Prove  $\overline{FE}$  to a point M such that  $\overline{EM} \cong \overline{BC}$  and join the point D and M

#### Proof

Statements	Reasons
$m\angle DEF + \angle DEM = 180^{\circ}$ (i)	Supplementary angles
Now m $\angle$ DEF = 90°(ii)	Given
$\therefore$ m $\angle$ DEM = 90°	{ from (i) and (ii) }
In $\triangle ABC \leftrightarrow \triangle DEM$	
$\overline{\mathrm{BC}}\cong\overline{\mathrm{EM}}$	Construction
∠ABC ≅ ∠DEM	(Each angle equal to 90°)
$\overline{AB} \cong \overline{DE}$	Given
$\Delta ABC \cong \Delta DEM$	SAS postulate
ad $\angle C = \angle M$	Corresponding angles of congruent triangles
$\overline{\mathrm{CA}} \cong \overline{\mathrm{MD}}$	Corresponding sides of congruent triangles
$\operatorname{But} \overline{\operatorname{CA}} \cong \overline{\operatorname{FD}}$	Given
$\overline{\mathrm{MD}} \cong \overline{\mathrm{FD}}$	Each is congruent to $\overline{\text{CA}}$
In DMF	
∠F ≅∠M	$\overline{\text{MD}} \cong \overline{\text{FD}} \text{ (proved)}$
$But \angle C \cong \angle M$	(Proved)
$\angle C \cong \angle F$	Each is congruent to ∠M
n n	Given
∠ABC ≅ ∠DEF	Given
$\overline{AB} \cong \overline{DE}$	(Proved)
Hence $\triangle ABC \cong \triangle DEF$	$(S.A.A \cong S.A.A)$

## Example

If perpendiculars from two vertices of a triangle to the opposite sides are congruent, then the triangle is isosceles.

#### Given

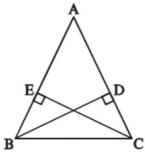
In  $\triangle ABC$ ,  $\overline{BD} \perp \overline{AC}$ ,  $\overline{CE} \perp \overline{AB}$ 

Such that  $\overline{BD} \cong \overline{CE}$ 

## To prove

 $\overline{AB} \cong \overline{AC}$ 

#### **Proof**



Statements	Reasons
In $\triangle BCD \leftrightarrow \triangle CBC$	
∠BDC≅∠BEC	$\overline{BD} \perp \overline{AC}, \overline{CE} \perp \overline{AB}$ given $\Rightarrow$ each angle = 90°
$\overline{\mathrm{BC}} \cong \overline{\mathrm{BC}}$	Common hypotenuse
$\overline{BD} \cong \overline{CE}$	Given
ΔBCD≅ΔCBE	H.S≅H.S
∠BCA≅∠CBE	Corresponding angles $\Delta$ s
Thus ∠BCA≅∠CBA	
Hence $\overline{AB} = \overline{AC}$	In ΔABC,∠BCA≅∠CBA

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## **Last Updated: September 2020**

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