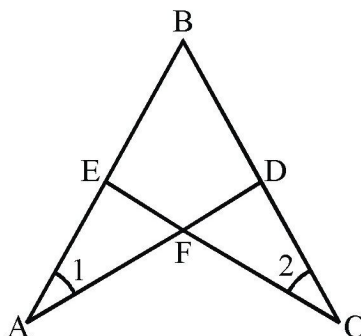


Exercise 10.1

- Q.1** In the given figure
 $\angle 1 \cong \angle 2$ and $\overline{AB} \cong \overline{CB}$
Prove that
 $\triangle ABD \cong \triangle CBE$



Proof

Statements	Reasons
In $\triangle ABD \leftrightarrow \triangle CBE$	
$\overline{AB} \cong \overline{CB}$	Given
$\angle BAD \cong \angle BCE$	Given $\angle 1 \cong \angle 2$
$\angle ABD \cong \angle CBE$	Common
$\triangle ABD \cong \triangle CBE$	S.A.A \cong S.A.A

- Q.2** From a point on the bisector of an angle, perpendiculars are drawn to the arms of the angle. Prove that these perpendiculars are equal in measure.

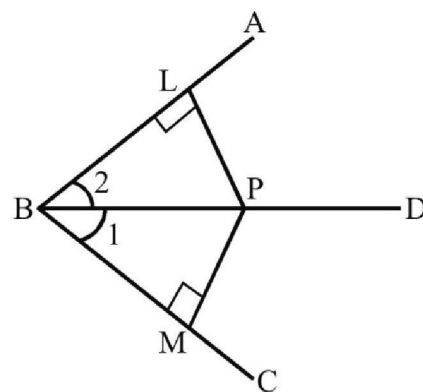
Given

\overline{BD} is bisector of $\angle ABC$. P is point on \overline{BD} and \overline{PL} and \overline{PM} are perpendicular to \overline{AB} and \overline{CB} respectively

To prove

$\overline{PL} \cong \overline{PM}$

Proof



Statements	Reasons
In $\triangle BLP \leftrightarrow \triangle BMP$	
$\overline{BP} \cong \overline{BP}$	Common
$\angle BLP \cong \angle BMP$	Each right angle (given)
$\angle LBP \cong \angle MBP$	Given \overline{BD} is bisector of angle B
$\therefore \triangle BLP \cong \triangle BMP$	S.A.A \cong S.A.A
So $\overline{PL} \cong \overline{PM}$	Corresponding sides of congruent triangles

Q.3 In a triangle ABC, the bisectors of $\angle B$ and $\angle C$ meet in point I prove that I is equidistant from the three sides by $\triangle ABC$

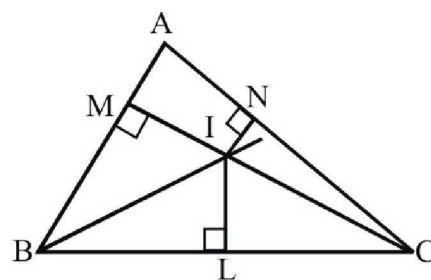
Given

In $\triangle ABC$, the bisector of $\angle B$ and $\angle C$ meet at I and \overline{IL} , \overline{IM} , and \overline{IN} are perpendiculars to the three sides of $\triangle ABC$.

To prove

$$\overline{IL} \cong \overline{IM} \cong \overline{IN}$$

Proof



Statements	Reasons
In $\triangle ILB \leftrightarrow \triangle IMB$	
$\overline{BI} \cong \overline{BI}$	Common
$\angle IBL \cong \angle IBM$	Given BI is bisector of $\angle B$
$\angle ILB \cong \angle IMB$	Given each angle is right angles
$\triangle ILB \cong \triangle IMB$	SAA \cong S.A.A
$\therefore \overline{IL} \cong \overline{IM}$ _____ (i)	Corresponding sides of $\cong \Delta$'s
Similarly	
$\triangle INC \cong \triangle INC$	
So $\overline{IL} \cong \overline{IN}$ _____ (ii)	
from (i) and (ii)	Corresponding sides of $\cong \Delta$ s
$\overline{IL} \cong \overline{IM} \cong \overline{IN}$	
\therefore I is equidistant from the three sides of $\triangle ABC$.	

Theorem 10.1.2

If two angles of a triangles are congruent then the sides opposite to them are also congruent

Given

In $\triangle ABC$, $\angle B \cong \angle C$

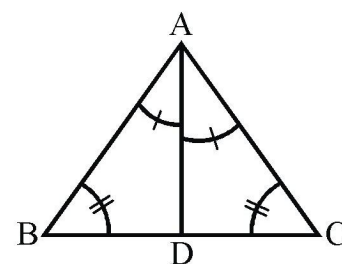
To prove

$$\overline{AB} \cong \overline{AC}$$

Construction

Draw the bisector of $\angle A$, meeting \overline{BC} at point D

Proof



Statements	Reasons
In $\triangle ABD \leftrightarrow \triangle ACD$	
$\overline{AD} \cong \overline{AD}$	Common
$\angle B \cong \angle C$	Given
$\angle BAD \cong \angle CAD$	Construction
$\triangle ABD \cong \triangle ACD$	S.A.A \cong S.A.A
Hence $\overline{AB} \cong \overline{AC}$	(Corresponding sides of congruent triangles)

Example 1

If one angle of a right triangle is of 30° , the hypotenuse is twice as long as the side opposite to the angle.

Given

In $\triangle ABC$, $m\angle B = 90^\circ$ and $m\angle C = 30^\circ$

To prove

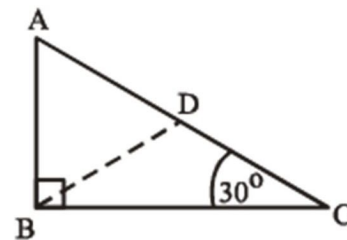
$$m\overline{AC} = 2m\overline{AB}$$

Constructions

At, B construct $\angle CBD$ of 30°

Let \overline{BD} cut \overline{AC} at the point D.

Proof



Statements	Reasons
In $\triangle ABD$, $m\angle A = 60^\circ$	$m\angle ABC = 90^\circ$, $m\angle C = 30^\circ$
$m\angle ABD = m\angle ABC$, $m\angle CBD = 60^\circ$	$m\angle ABC = 90^\circ$, $m\angle CBD = 30^\circ$
$\therefore m\angle ADB = 60^\circ$	Sum of measures of \angle s of a \triangle is 180°
$\therefore \triangle ABD$ is equilateral	Each of its angles is equal to 60°
$\therefore \overline{AB} \cong \overline{BD} \cong \overline{AD}$	Sides of equilateral \triangle
In $\triangle BCD$, $\overline{BD} \cong \overline{CD}$	$\angle C = \angle CBD$ (each of 30°),
Thus $m\overline{AC} = m\overline{AD} + m\overline{CD}$	$\overline{AD} \cong \overline{AB}$ and $\overline{CD} \cong \overline{BD} \cong \overline{AB}$
$= m\overline{AB} + m\overline{AB}$	
$= 2(m\overline{AB})$	

Example 2

If the bisector of an angle of a triangle bisects the side opposite to it, the triangle is isosceles.

Given

In $\triangle ABC$, \overline{AD} bisect $\angle A$ and $\overline{BD} \cong \overline{CD}$

To prove

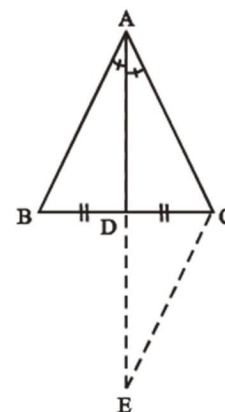
$$\overline{AB} \cong \overline{AC}$$

Construction

Produce \overline{AD} to E, and take $\overline{ED} \cong \overline{AD}$

Join C to E

Proof



Statements	Reasons
In $\triangle ADB \leftrightarrow \triangle EDC$	
$\overline{AD} \cong \overline{ED}$	Construction
$\angle ADB \cong \angle EDC$	Vertical angles
$\overline{BD} \cong \overline{CD}$	Given
$\therefore \triangle ADB \cong \triangle EDC$	S.A.S. Postulate
$\therefore \overline{AB} \cong \overline{EC} \dots (i)$	Corresponding sides
and $\angle BAD \cong \angle E$	Corresponding angles
But $\angle BAD \cong \angle CAD$	Given
$\therefore \angle E \cong \angle CAD$	Each $\cong \angle BAD$
In $\triangle ACE$, $\overline{AC} \cong \overline{EC} \dots (ii)$	$\angle E \cong \angle CAD$ (proved)
Hence $\overline{AB} \cong \overline{AC}$	From (i) and (ii)

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Report any mistake at freeilm786@gmail.com

