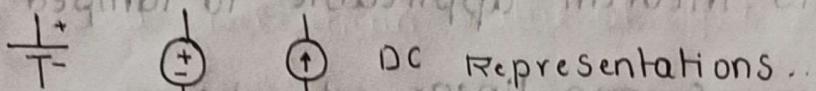


24/11/22

Unit-3 : Single phase AC circuits (1-φ circuit)

discrete segment of addressable memory cell



- * AC wave: A wave that repeats with time

For DC \rightarrow {independent of time}

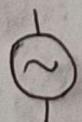
For AC \rightarrow {dependent of time}

- * The magnitude of alternating quantity &

its direction changes with respect to time

& polarity changes {alternating quantity fluctuates}

→ This type of wave is called AC wave.

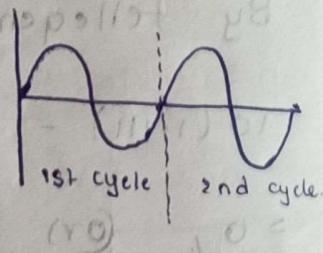


$\sim \rightarrow$ AC representation

- * Cycle: Cycle is a part of wave which contains

positive, negative & 0 values

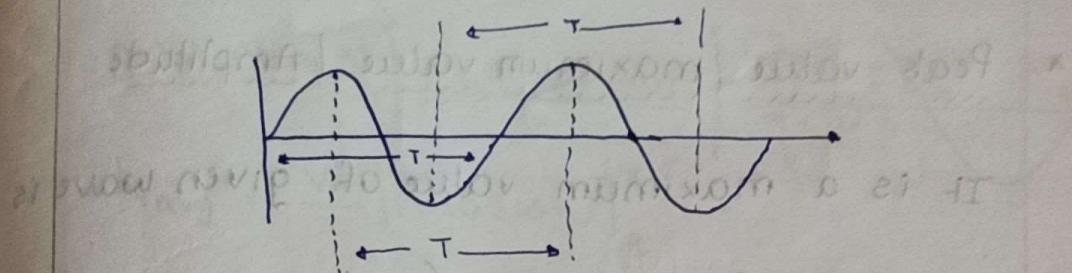
which repeats uniformly.



- * Time period: Time taken to complete one

cycle is called Time period (T) • Represented

by ' T '



- * Frequency (f) is equal to no. of cycles per unit time, measured in Hertz.

$$f = \frac{\text{no. of cycles}}{\text{time}} \quad \text{e.g. } 1 \text{ Hz} = \frac{\text{one cycle}}{1 \text{ sec}}$$

* Indian current frequency = 50 Hz

* US Supply frequency = 60 Hz

Q A time period of alternating wave is 30 sec.

what is its frequency ... $f = \frac{1}{30} = \boxed{0.03} \text{ Hz}$ { $f = \frac{1}{T}$ }

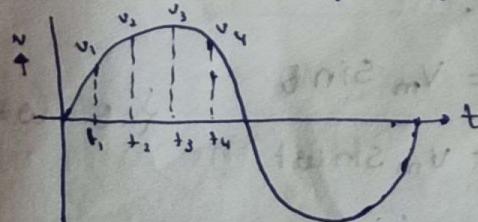
Q A time period of AC wave is 20 milli seconds.

what is its frequency $\rightarrow f = \frac{1000}{20} = 50 \text{ Hz}$ { $f = \frac{1}{T}$ }

Q An Alternating wave has 50Hz frequency. what is its time period. $T = \frac{1}{f} = \frac{1}{50} = 0.02 \text{ sec.}$

* Instantaneous values:

The values at particular instant of time of quantity

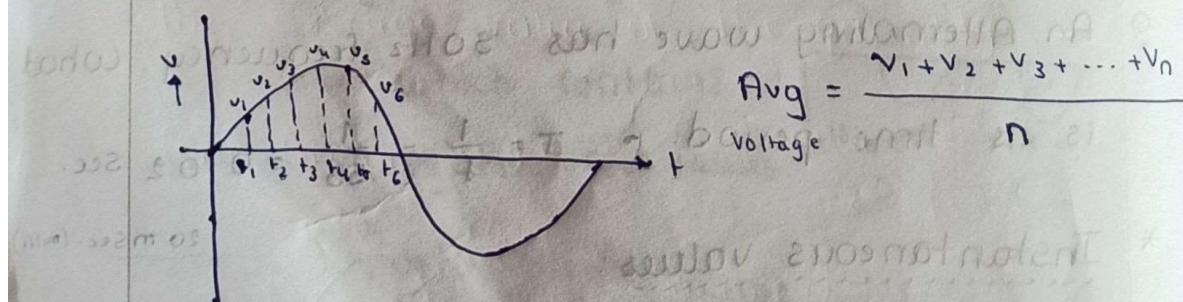


v_1, v_2, v_3 & v_4 are instantaneous voltages

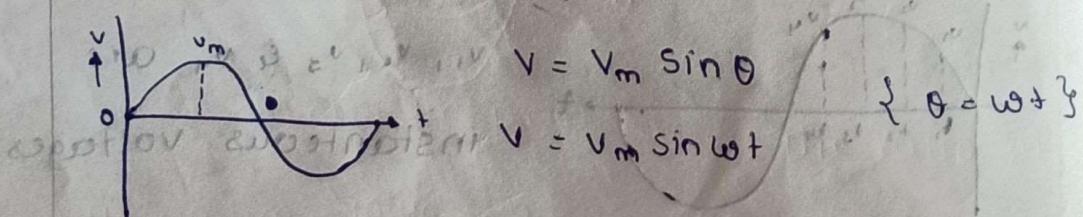
- * Peak value / maximum value / Amplitude:
It is a maximum value of given wave is the amplitude of wave (highest value) (crest value)

- * Average value of AC wave:
It can be defined as, when DC source is connected to circuit & we calculated the charge transferred for 't' time, "then the charge transferred by the AC circuit is as same as charge transferred by DC source calculated for the same time 't' is known average value of AC wave."

1) Graphical method for finding Avg.:



2) Analytical method for finding Avg.:



$$\text{Now } V_{avg} = \frac{1}{\pi} \int_0^{\pi} v_m \sin \omega t \, dt$$

$$V_{avg} = \frac{v_m}{\pi} [(-\cos \omega t)]_0^\pi$$

$$V_{avg} = \frac{v_m}{\pi} [-\cos \pi + \cos 0]$$

$$V_{avg} = \frac{2v_m}{\pi}$$

$$V_{avg} = 0.636 V_m \quad \text{Similary } I_{avg} = 0.636 I_m$$

V_m = maximum value of voltage

I_m = maximum value of current.

* RMS value of an AC Wave (Root Mean Square):

- The value obtained when heat produced

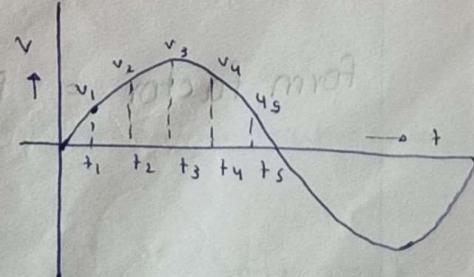
by DC supply must be equal to the heat

produced by AC supply calculated for

same circuit & in same time, is rms value.

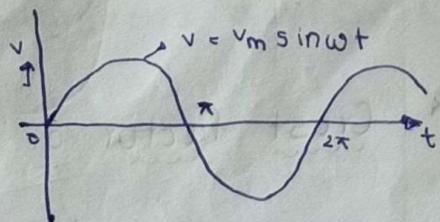
① Graphical method

$$V_{rms} = \sqrt{\frac{v_1^2 + v_2^2 + v_3^2 + \dots + v_n^2}{n}}$$



② Analytical method

$$V_{rms} = \sqrt{\frac{\int_0^{2\pi} v_m^2 \sin^2 \omega t \, dt}{2\pi}}$$



$$\begin{aligned}
 &= \left[\frac{V_m^2}{2\pi} \cdot \int_0^{2\pi} \left(\frac{1 - \cos(\omega t)}{2} \right) dt \right]^{\frac{1}{2}} \\
 &= \left\{ \frac{V_m^2}{4\pi} \cdot \left[\omega t \Big|_0^{2\pi} - \frac{\sin(\omega t)}{\omega} \Big|_0^{2\pi} \right] \right\}^{\frac{1}{2}} \\
 &= \left\{ \frac{V_m^2}{4\pi} \left[2\pi - \left(\frac{\sin 2\pi}{2} - \frac{\sin 0}{2} \right) \right] \right\}^{\frac{1}{2}}
 \end{aligned}$$

$$\begin{aligned}
 &= \left(\frac{V_m^2}{24\pi} \cdot 2\pi \right)^{\frac{1}{2}} \\
 &= \frac{V_m}{\sqrt{2}}
 \end{aligned}$$

$$= 0.707 V_m \text{ or no to follow ESR}$$

$$\boxed{V_{rms} = 0.707 V_m} \quad V_m = \text{maximum value of voltage}$$

$$\text{Similarly } \boxed{I_{rms} = 0.707 I_m}$$

* Form factor: The ratio of rms value to the average value of the quantity is called

$$\text{form factor} = FF = \frac{\text{Rms value}}{\text{Avg value}}$$

$$= \frac{0.707 V_m}{0.636 V_m}$$

$$= \underline{\underline{1.11}}$$

* Crest factor or peak factor: The ratio of maximum value to the rms value is peak factor

$$PF = \frac{\text{Max value}}{\text{Rms value}}$$

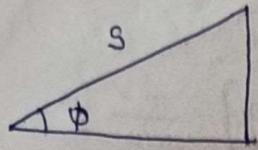
$$PF = \frac{V_m}{0.707 V_m} = 1.414.$$

- * **Power factor:** Represented by $\cos\phi$. power factor is the angle between voltage & current.
- * **Active power:-** / V_I power or true power
 - Active power $P = VI \cos\phi$ in watts.
- * The power consumed by active elements in a circuit having different elements is called Active power.
- * **Reactive power / Imaginary power (Q):-** The power consumed by reactive elements in a circuit having different elements is called passive power.

$$Q = VI \sin\phi \quad (\text{VAR}) \quad \text{volt ampere reactive power.}$$

- * **Apparent power:(s):** $S = VI$ { Volt amp}
- The power given to apparent devices is known as apparent power :-

* Power triangle:-



vector sum = 99

voltage drop

$$= s = \sqrt{P^2 + Q^2}$$

$$P = \sqrt{s^2 - Q^2}$$

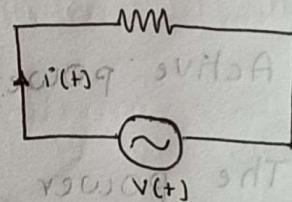
$$\text{Power } P = \text{voltage } V \times \text{current } I \times \cos \phi$$

$$\text{Power } Q = \text{voltage } V \times \text{current } I \times \sin \phi$$

* AC through Resistor:

Consider a resistance R resistor

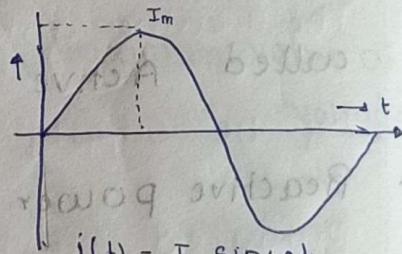
and voltage source



connected in series. Current flowing is $i(t)$.

* Here impedance (z)

= Resistance (R).



$$i(t) = I_m \sin \omega t$$

$$V(t) = I_m \cdot z \cdot \sin \omega t$$

Now, we have

$$V(t) = V_m \sin \omega t$$

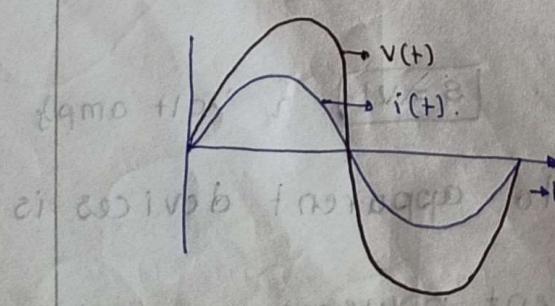
$$V_m = I_m \cdot z$$

$$I(t) = I_m \sin \omega t$$

z = impedance.

Here phase difference

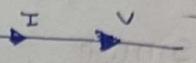
$$\phi = 0^\circ$$



* For a resistive circuit, the phase angle b/w

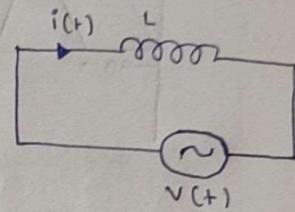
voltage & current is zero., so

$$\text{power factor} = \cos\phi = \cos 0^\circ = 1,$$

- * Phasor diagram {  } phase angle $\phi = 0^\circ$

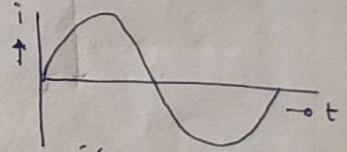
- * AC through pure inductor:

Consider a inductor of
inductance (L) & AC source



connected in series.

Assume that current flowing in inductor
is sinusoidal current



- * Voltage across inductor

$$\text{is } V(t) = L \cdot \frac{di(t)}{dt}$$

$$V(t) = L \cdot \frac{d}{dt} (I_m \sin \omega t)$$

$$V(t) = I_m \cdot L \cdot \omega \cos \omega t$$

$$V(t) = I_m \cdot L \cdot \omega \sin (\omega t + 90^\circ)$$

$$V(t) = V_m \sin (\omega t + 90^\circ) \rightarrow \textcircled{1}$$

$$V(t) \boxed{V_m = I_m \cdot \omega \cdot L} \quad \{ X_L = 2\pi f \cdot L \}$$

where $\omega L = X_L$ { inductive reactance (Ω)}

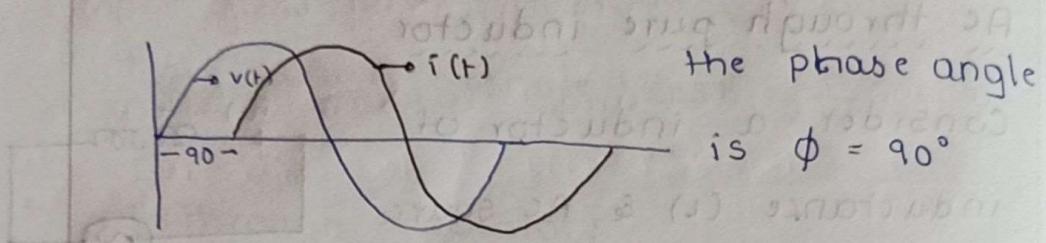
- * For practical inductor, $Z = R + jX_L$

- * For pure inductor, $Z = jX_L$

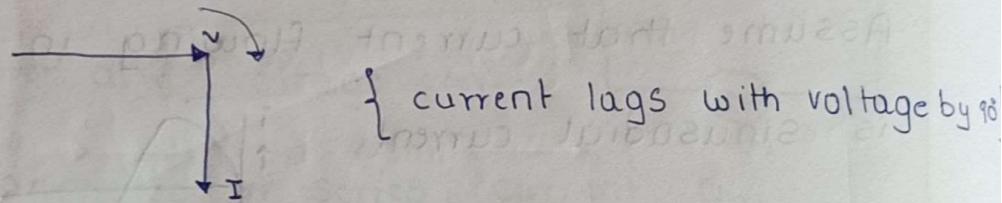
From ①

$$V(t) = V_m \sin(\omega t + \phi) \text{ & also}$$

$$I(t) = I_m \sin \omega t, \text{ so graph is...}$$



- * Vector representation / phasor diagram.



- * We know impedance $Z = \frac{V(t)}{i(t)} = \frac{I_m \cdot \omega \cdot L \cdot \sin(\omega t + 90^\circ)}{I_m \sin \omega t} = \omega L \angle 90^\circ = X_L \angle 90^\circ$

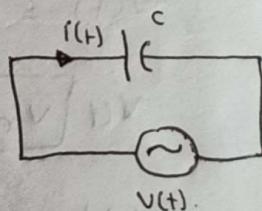
for pure inductor. $Z = jX_L$

- * AC through pure inductor.

- * Consider capacitor of

capacitance 'c' & voltage

AC source connected in series.



- * Assume current flowing through circuit is sinusoidal current.

We know $i(t) = C \cdot \frac{dv(t)}{dt}$

$$\rightarrow v(t) = \frac{1}{C} \int i(t) dt.$$

$$\rightarrow v(t) = \frac{1}{C} \int I_m \sin \omega t dt$$

$$= \frac{I_m}{\omega C} [-\cos \omega t]$$

$$= \frac{I_m}{\omega C} \sin(\omega t - 90^\circ)$$

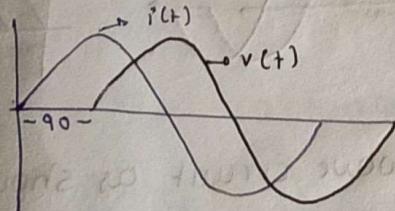
$$v(t) = V_m \sin(\omega t - 90^\circ) \rightarrow \textcircled{1} \quad \left\{ \begin{array}{l} \frac{1}{\omega C} = X_C \\ X_C = \frac{1}{2\pi f C} \end{array} \right. \quad (\text{a})$$

We have

$$\left\{ \begin{array}{l} X_C = \text{capacitive} \\ \text{reactance} \end{array} \right.$$

$$v(t) = V_m \sin(\omega t - 90^\circ)$$

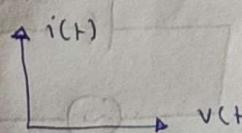
$$i(t) = I_m \sin \omega t, \text{ so graph is.}$$



the phase angle

$$\phi = 90^\circ$$

vector representation / phasor diagram



current leads voltage

by 90°

* We know impedance $Z = \frac{v(t)}{i(t)} = \frac{\frac{I_m}{\omega C} \sin(\omega t - 90^\circ)}{I_m \sin \omega t}$

$$Z = \frac{1}{\omega C} \frac{\sin(\omega t - 90^\circ)}{\sin \omega t}$$

$$Z = X_C \angle -90^\circ$$

$$\boxed{Z = -jX_C} \quad \text{for pure capacitor.}$$

* for practical capacitor, $Z = R - jX_C$ {R is low}

Important points:

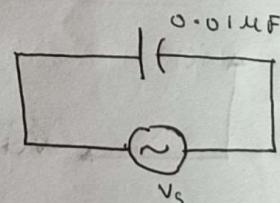
	Resistor	inductor	capacitor.
Symbol			
$I(t)$	$I(t) = I_m \sin \omega t$	$I(t) = I_m \sin(\omega t + 90^\circ)$	$I(t) = I_m \sin(\omega t - 90^\circ)$
$V(t)$	$V(t) = V_m \sin \omega t$	$V(t) = V_m \sin(\omega t + 90^\circ)$	$V(t) = V_m \sin(\omega t - 90^\circ)$
power factor	unity	lag	lead
phasor			
sine wave			

Q For a sinusoidal wave circuit as shown in fig.

The frequency of sine wave is 2 kHz. Determine

the capacitive reactance.

$$A F = 2 \text{ kHz}$$



$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

$$X_C = \frac{1}{2(3.14)(2000)(0.01 \times 10^{-6})}$$

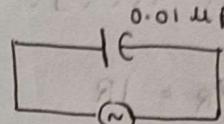
$$X_C = 7.96 \times 10^3 \Omega$$

$$X_C = 7.96 \text{ k}\Omega$$

Q Determine the rms value of current for the circuit shown.

$$A \quad X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

$$= \frac{1}{2\pi (5 \times 10^3) (0.01 \times 10^{-6})}$$



$$V_{rms} = 5V$$

$$f = 5 \text{ kHz.}$$

$$= 3.18 \times 10^3 \Omega$$

$$= 3.18 \text{ k}\Omega. = X_C.$$

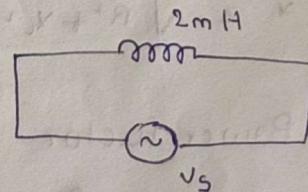
$$\text{Now } I_{rms} = \frac{V_{rms}}{X_C} \quad \{ z = X_C \}$$

$$I_{rms} = \frac{5V}{3.18 \times 10^3} \rightarrow I_{rms} = 1.57 \text{ mA}$$

Q A sinusoidal voltage is applied to given circuit with a frequency of 3 kHz. find the inductive reactance.

$$A \quad f = 3 \text{ kHz.}$$

$$X_L = 2\pi f L$$



$$= 2\pi (3 \times 10^3) \cdot 2 \times 10^{-3}$$

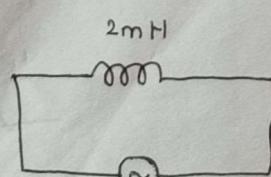
$$= 37.69 \Omega$$

Q Find the value of I_{rms} for given circuit.

$$A \quad X_L = 2\pi f L = 2\pi (10 \times 10^3) (2 \times 10^{-3})$$

$$X_L = 125.6 \Omega$$

$$I_{rms} = \frac{V_{rms}}{Z} \quad (z = X_L) \text{ Here}$$



$$V_{rms} = 10V$$

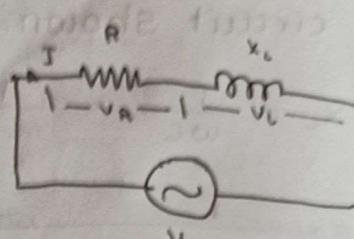
$$f = 10 \text{ kHz.}$$

$$I_{rms} = \frac{10}{125.6 \Omega} = 79 \text{ mA}$$

- AC through R-L Series circuit:

- $V_R = IR$

$$V_L = I \cdot X_L$$



The effective voltage

$$V_s = \sqrt{V_R^2 + V_L^2}$$

$$V_s = \sqrt{(IR)^2 + (IX_L)^2}$$

$$V_s = \sqrt{I^2 (R^2 + X_L^2)}$$

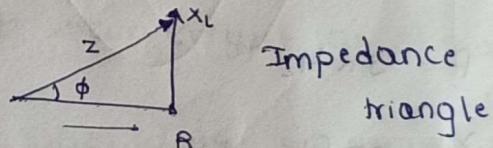
$$V_s = I \sqrt{R^2 + X_L^2}$$

$$V_s = I Z \quad \{ Z = \sqrt{R^2 + X_L^2} \text{ (magnitude)} \}$$

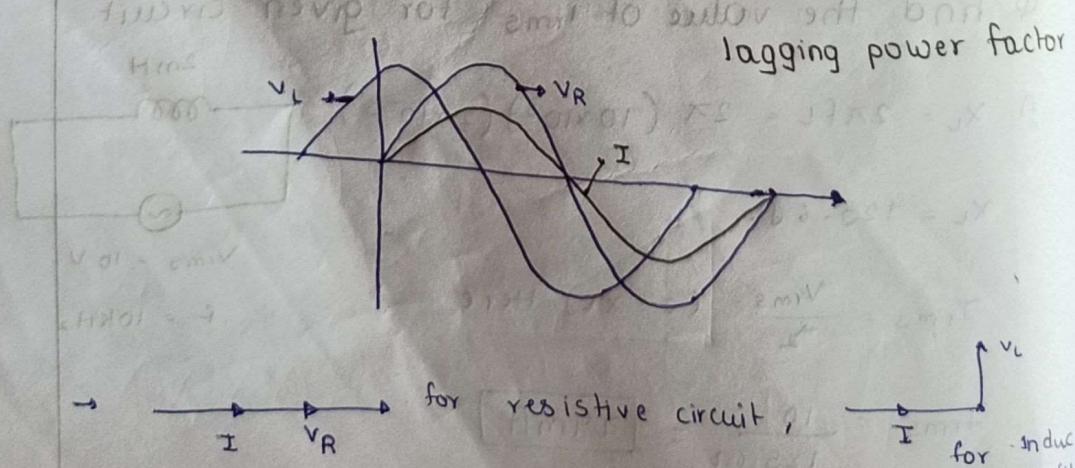
- $Z = \sqrt{R^2 + X_L^2}$

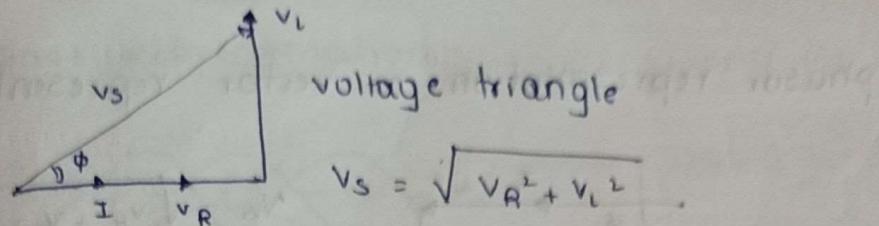
Power factor

$$\cos \phi = \frac{R}{Z}$$



- phasor diagram or vector difference representation
is in down
- Now wave representation.

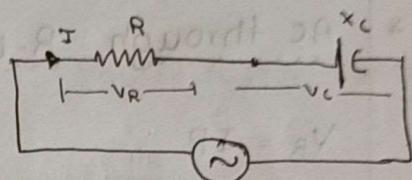




Power factor (PF) = $\cos\phi = \frac{V_R}{V_s}$

* AC through RC series circuit!

$$\begin{aligned} V_R &= IR \\ V_C &= I \cdot X_C \end{aligned} \quad \left. \begin{array}{l} \text{voltage formulae} \\ \text{i.e.} \end{array} \right\}$$



* R is resistance of complete circuit i.e. it the resistance of resistor + resistance of capacitor.

$$V_s = \sqrt{V_R^2 + V_C^2}$$

$$V_s = \sqrt{IR^2 + IX_C^2}$$

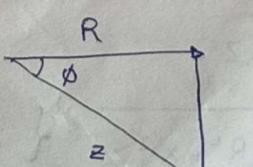
$$V_s = I \sqrt{R^2 + X_C^2}$$

$$V_s = IZ \quad \left. \begin{array}{l} Z = \sqrt{R^2 + X_C^2} \quad (\text{Here}) \end{array} \right\}$$

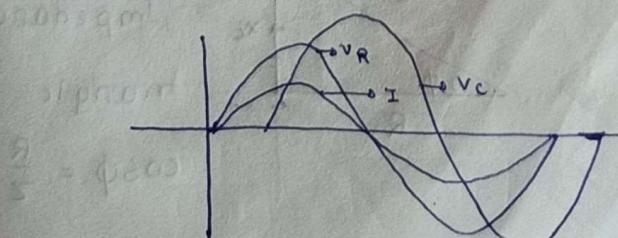
$$Z = \sqrt{R^2 + X_C^2} \quad \left. \begin{array}{l} Z = R - jX_C \quad (\text{with direction}) \end{array} \right\}$$

Impedance triangle

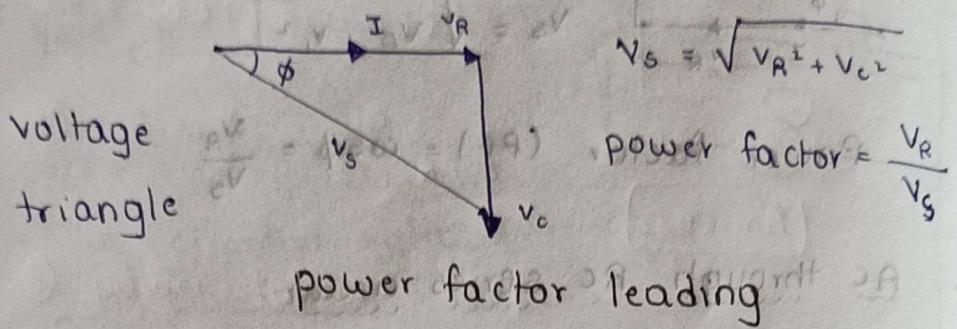
$$\text{Power factor } \cos\phi = \frac{R}{Z}$$



* Wave representation



- * phasor representation or vector representation

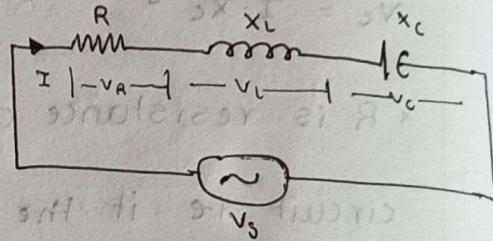


- * AC through R-L-C circuit series circuit.

$$V_R = IR$$

$$V_L = IX_L$$

$$V_C = IX_C$$



- * R is resistance of whole circuit

$$V_s = \sqrt{V_R^2 + (V_L - V_C)^2}$$

$$V_s = \sqrt{(IR)^2 + (IX_L - IX_C)^2}$$

$$V_s = I \sqrt{R^2 + X^2}$$

$X \rightarrow$ Net reactance

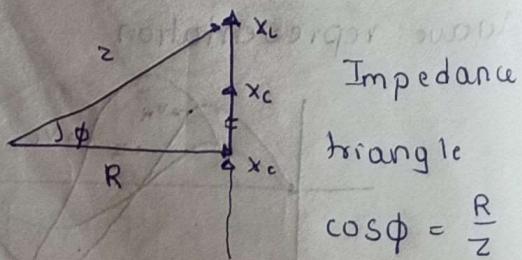
$$= X_L - X_C$$

$$V_s = I \cdot Z$$

$$Z = \sqrt{R^2 + X^2}$$

$$X = X_L - X_C$$

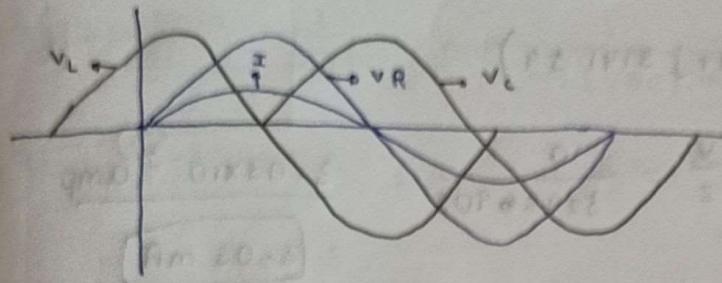
$$\{ Z = R + jX \quad (X = X_L - X_C) \}$$



- * Vector

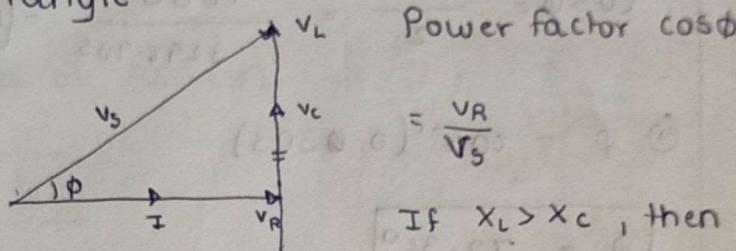
Representation

Wave representation:



- * Vector representation: $v = \text{vector sum}$

voltage triangle



If $x_L = x_C$,

power factor is unity.

$$\text{Power factor } \cos \phi = \frac{V_R}{V_S}$$

If $x_L > x_C$, then

Lagging power factor

If $x_C > x_L$ then

Leading power factor

- Q For the circuit shown below,

find the impedance Z , current I , phase angle

~~total apparent power~~, power factor, ϕ ,

voltage across V_R (resistor), power factor,

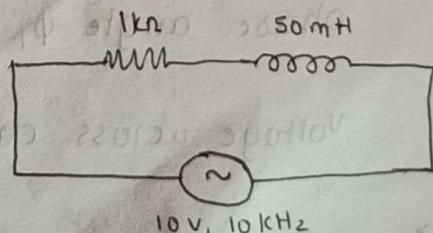
voltage across inductor V_L .

A Given $R = 1000\Omega$

$$L = 50 \times 10^{-3} \text{ H},$$

$$V = 10 \text{ V},$$

$$f = 10 \times 10^3 \text{ Hz}$$



$$\textcircled{1} Z = \sqrt{R^2 + X_L^2}$$

$$X_L = \omega L = 2\pi f L = 62.8 \Omega$$

$$Z = \sqrt{1000^2 + 3141.59^2}$$

$$= 2\pi (10 \times 10^3) (50 \times 10^{-3})$$

$$= 3141.59 \Omega$$

$$Z = \boxed{3296.905 \Omega}$$

$$Z = (1000 + j 3141.59)$$

$$\textcircled{2} \quad I = \frac{V}{Z} = \frac{10}{3296.905} = \frac{3.03 \times 10^{-3} \text{ amp}}{= 3.03 \text{ mA}}$$

$$\textcircled{3} \quad \text{power factor} = \cos \phi$$

$$\cos \phi = \frac{R}{Z} = \frac{1000}{3296.905} = \boxed{0.303 \text{ lagging}}$$

$$\textcircled{4} \quad \phi = \cos^{-1}(0.303)$$

$$\boxed{\phi = 72.36^\circ}$$

$$\textcircled{5} \quad V_R : IR = (3.03 \times 10^{-3}) 10^3 = \boxed{3.03 \text{ V}}$$

$$\textcircled{6} \quad V_L = IX_L = (3.03 \times 10^{-3})(3141.59) = \boxed{9.519 \text{ V}}$$

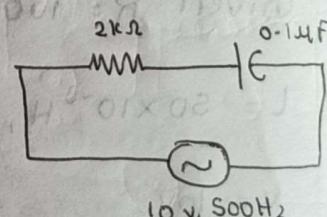
Q For the circuit shown below, find the total impedance (Z), current in circuit I , power factor, phase angle ϕ , voltage across resistor V_R & voltage across capacitor V_C .

$$R = 2000 \Omega$$

$$C = 0.1 \times 10^{-6} \text{ F}$$

$$V = 10 \text{ V}$$

$$F = 500 \text{ Hz}$$



$$\textcircled{1} \quad Z = \sqrt{R^2 + X_C^2} \quad \text{solution second option}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} = \frac{1}{2\pi (500)(0.1 \times 10^{-6})}$$

$$X_C = 3183.09 \Omega$$

$$Z = \sqrt{2000^2 + 3183.09^2}$$

$$\boxed{Z = 3759.26 \Omega} \quad Z = (2000 + j3183.09) \Omega$$

$$\textcircled{2} \quad \text{The value of current } I = \frac{V}{Z} = \frac{10}{3759.26}$$

$$\boxed{I = 2.66 \text{ mA}}$$

$$\textcircled{3} \quad \text{power factor } \cos \phi = \frac{R}{Z} = \frac{2000}{3759.26}$$

$$\boxed{\cos \phi = 0.532 \text{ leading}}$$

$$\textcircled{4} \quad \text{phase angle } \phi = \cos^{-1}(0.532)$$

$$\phi = \cos^{-1}(0.532)$$

$$\boxed{\phi = 57.85^\circ}$$

$$\textcircled{5} \quad \text{Voltage across resistor, } V_R = IR$$

$$= (2.66 \times 10^{-3})(2000) = \boxed{5.32 \text{ V}}$$

$$\textcircled{6} \quad \text{Voltage across capacitor, } V_C = I \cdot X_C$$

$$= (2.66 \times 10^{-3})(3183.09) = \boxed{8.467 \text{ V}}$$

* Determine the source voltage & phase angle in the circuit when the voltage across resistor is 20V

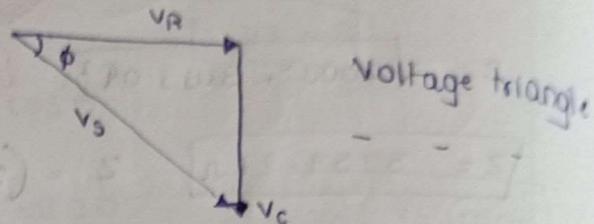
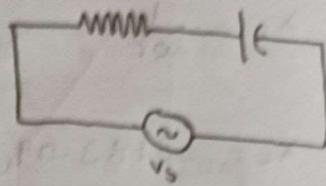
voltage across capacitor is 30V

A) $V_R = 20V$ & $V_L = 30V$

$$V_S = \sqrt{V_R^2 + V_L^2}$$

$$= \sqrt{20^2 + 30^2}$$

$$= 36.05V$$



$$\phi = \tan^{-1} \left(\frac{V_L}{V_R} \right)$$

$$\phi = \tan^{-1} \left(\frac{30}{20} \right)$$

$$= 56.30^\circ$$

* power factor = $\cos\phi$

$$= \cos(56.30^\circ) = 0.554$$

= 0.554 leading

Q) Determine the source voltage, phase angle &

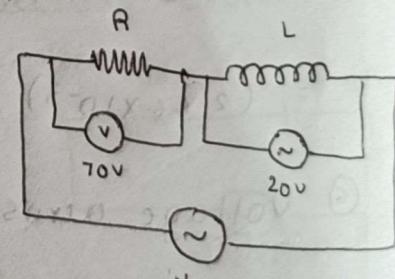
power factor of given circuit

A)

i) $V_R = 70V$, $V_L = 20V$

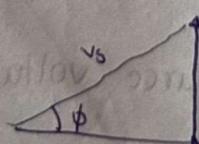
$$V_S = \sqrt{V_R^2 + V_L^2}$$

$$V_S = \sqrt{70^2 + 20^2}$$



$$V_S = 72.8V$$

② $\phi = \tan^{-1} \left(\frac{V_L}{V_R} \right)$



$$\phi = 15.94^\circ$$

③ Power factor $= \cos \phi = \cos(15.94)$

$= 0.96$ lagging.

Q In the circuit shown in figure, I, P.F, ϕ & voltage across each element in the circuit.

A $R = 10\Omega, L = 0.5H, C = 10\mu F$

$V = 50V, f = 50Hz$

① $Z = \sqrt{R^2 + (x_L - x_C)^2}$

$x_L = \omega L = 2\pi f L = 2\pi (50) (0.5)$

$x_L = 157.079 \Omega$

$x_C = 1/(2\pi f C) = 1/(2\pi (50) (10) \times 10^{-6}) = 318.30 \Omega$

$Z = \sqrt{10^2 + (318.30 - 157.079)^2}$

$Z = \sqrt{10^2 + (161.23)^2}$

$Z = 161.53 \Omega$

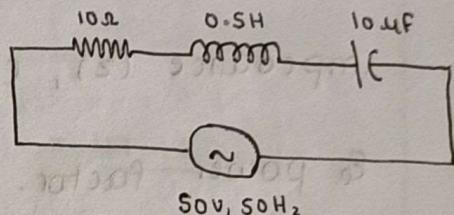
$(Z = R + j(x_L - x_C)) \quad \{ Z = R + j(x_L - x_C) \}$

② $I = \frac{V}{Z} = \frac{50}{161.53} = 0.309 A$

③ Power factor $\cos \phi = \frac{R}{Z} = \frac{10}{161.53} = 0.061$ leading

④ $\phi = \cos^{-1}(0.061)$

$\phi = 86.50^\circ$



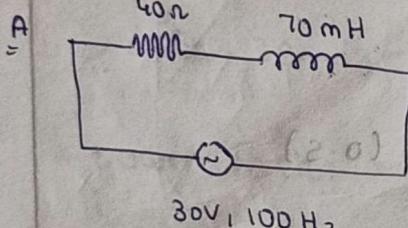
$$\rightarrow V_R = I(R) = 0.309 (10) = \underline{3.90V}$$

$$\rightarrow V_L = I(X_L) = 0.309 (157.07) = \underline{47.121V}$$

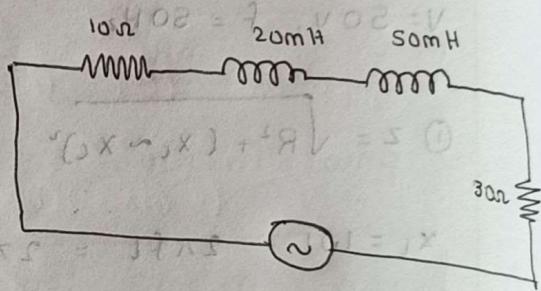
$$\rightarrow V_C = I(X_C) = 0.309 (318.30) = \underline{95.49V}$$

Q A supply voltage of 30V, 100 Hz is given to the series circuit shown in below figure. Determine impedance (Z), current in circuit I, phase angle

\Rightarrow power factor.



30V, 100Hz



$\Rightarrow \text{PF} = \frac{R}{Z} = \cos \phi$

$$① Z = \sqrt{R^2 + X_L^2}$$

$$X_L = 2\pi f L$$

$$X_L = 2\pi (100) (70 \times 10^{-3}) = 43.98 \Omega$$

$$* Z = \sqrt{40^2 + 43.98^2}$$

$$\rightarrow Z = \sqrt{40^2 + 43.98^2} = \underline{59.45 \Omega}$$

$$② I = \frac{V}{Z} = \frac{30}{59.45} = 0.50A$$

$$③ \text{PF} = \cos \phi = \frac{R}{Z} = \frac{40}{59.45} = 0.67 \text{ lagging}$$

$$④ \phi = \cos^{-1}(0.67) = 47.93^\circ$$

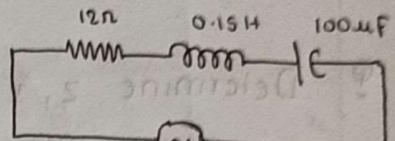
$$\therefore \text{lagging} = 47.93^\circ$$

Q Determine impedance Z , current I , power factor, ϕ , voltage across each element of given circuit.

$R = 12\Omega, L = 0.15H$

$C = 100\mu F, V_s = 100V,$

$f = 50Hz.$



$V_s = 100V, 50Hz$

$$\textcircled{1} \quad Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$X_L = 2\pi fL = 2\pi (50) (0.15) = 47.12\Omega$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC} = \frac{1}{2\pi (50)(100 \times 10^{-6})} = 31.83\Omega$$

$$X = X_L - X_C$$

$$= 47.12 - 31.83$$

$$= 15.29\Omega$$

$$Z = \sqrt{12^2 + 15.29^2}$$

$$Z = 19.43 \quad (30.6 \times 0.1 + 0.6 = 5) \quad 5.05 \times 18.21 = 5$$

$$Z = (12 + j 15.29)\Omega$$

$$\textcircled{2} \quad I = \frac{V}{Z} = \frac{100}{19.43} = 5.14A$$

$$\textcircled{3} \quad PF = \cos \phi = \frac{R}{Z} = \frac{12}{19.43} = 0.617 \text{ lagging.}$$

$$\textcircled{4} \quad \phi = \cos^{-1}(0.617)$$

$$\phi = 51.90^\circ$$

$$\textcircled{5} \quad \text{Voltage } V_R = IR = 5.14 \times 12 = 61.68$$

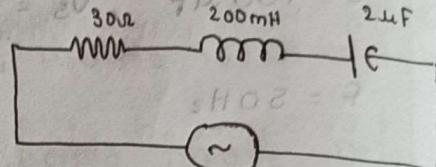
$$V_L = I \times L = 5.14 \times 47.12 = \underline{242.19 \text{ V}}$$

$$V_C = I \times C = 5.14 \times 31.03 = \underline{163.60 \text{ V}}$$

Q Determine Z, I, ϕ, V_R, V_L & V_C in given circuit

A $R = 30\Omega, L = 200\text{mH}$

$C = 2\mu\text{F}, V = 10\text{V}, f = 50\text{Hz}$



$$\textcircled{1} Z = \sqrt{R^2 + (X_L \sim X_C)^2}$$

$$X_L = 2\pi f L = 2\pi(50)(200 \times 10^{-3}) = 62.83\Omega$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi(50)(2 \times 10^{-6})} = 1591.5\Omega$$

$$X = X_C - X_L$$

$$X = 1591.5 - 62.83 = 1528.67\Omega$$

$$Z = \sqrt{30^2 + 1528.67^2}$$

$$\underline{Z = 1528.96\Omega} \quad (z = 30 + j1528.67)$$

$$\textcircled{2} I = \frac{V}{Z} = \frac{10}{1528.96} = 0.00654\text{A}$$

$$= 6.54\text{mA}$$

$$\textcircled{3} \text{ PF} = \cos \phi = \frac{R}{Z} = \frac{30}{1528.96} = 0.019 \text{ leading}$$

$$\textcircled{4} \phi = \cos^{-1}(0.019)$$

$$= 88.91^\circ$$

$$V_R = 0.00654 \times 30 = \underline{0.196\text{V}}$$

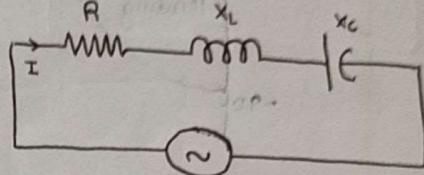
$$V_L = 0.00654 \times 62.83 = \underline{0.40V}$$

$$V_C = 0.00654 \times 1591.5 = \underline{10.40V}$$

* RLC Series resonance:

(i) IF $X_L > X_C$, PF lagging

$$X_L = 2\pi f L$$



Inductive circuit $X_L \propto f$ {f is frequency}

(ii) IF $X_C > X_L$

capacitive circuit, $X_C \propto \frac{1}{f}$ { $X_C = \frac{1}{2\pi f C}$ }

PF leading.

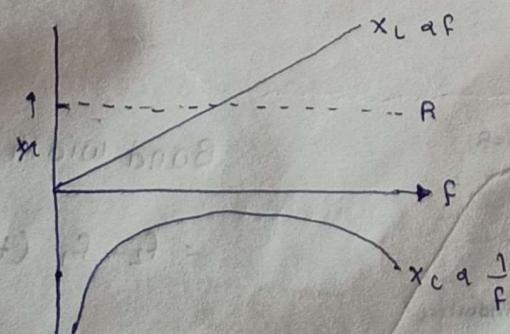
* If $X_L = X_C$, the circuit is said to be in resonance

Here $Z = R$, net reactance = 0 is..

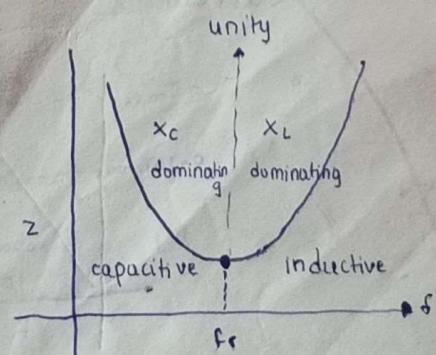
$$* 2\pi f_r L = \frac{1}{2\pi f_r C}$$

$$f_r = \frac{1}{2\pi\sqrt{LC}} \text{ Hz} \quad \{ f_r = \text{resonant frequency} \}$$

* Graphs: frequency vs impedance.

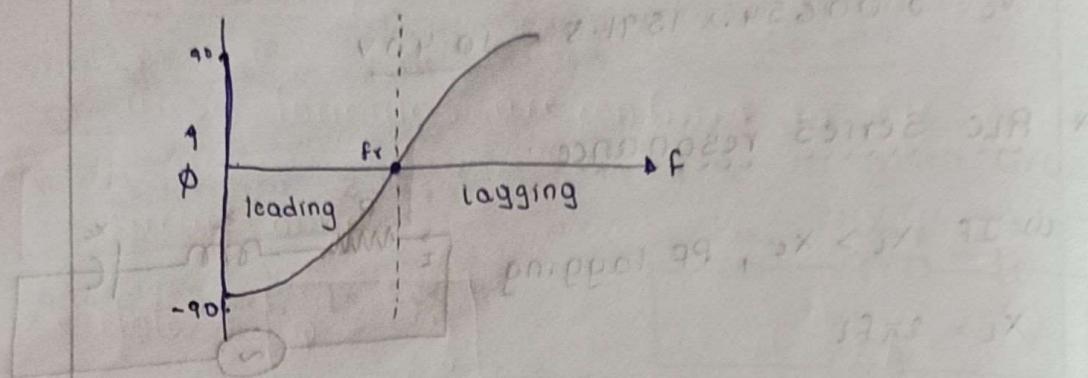


combination of all 3:

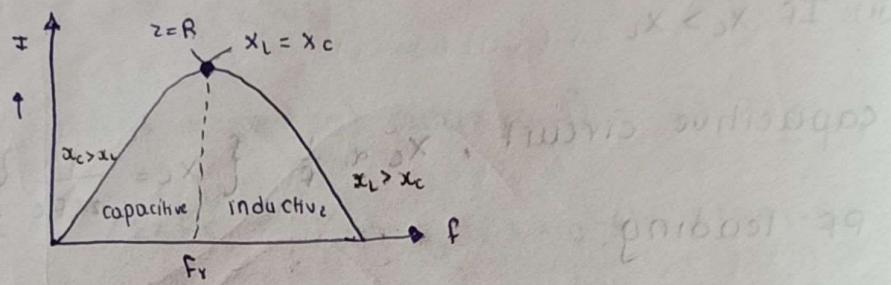


f_r = resonant frequency.

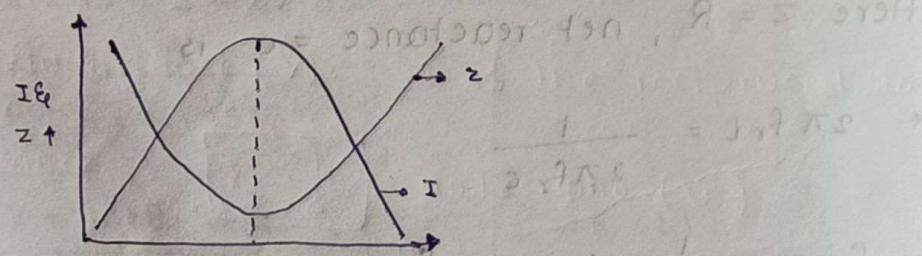
frequency vs phase angle ϕ :



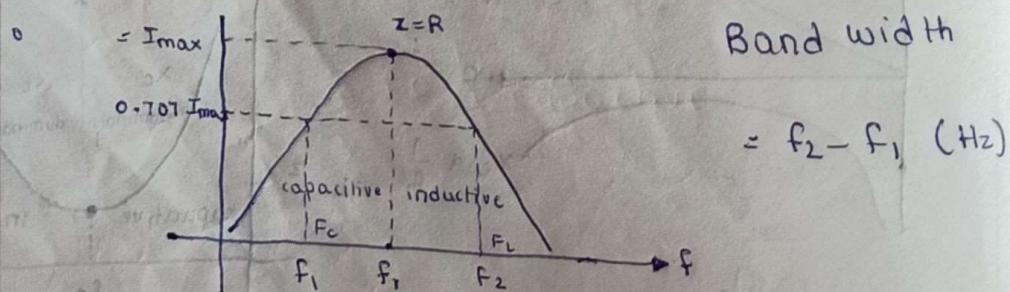
frequency vs current:



frequency vs $I \& Z$



- * Band width: Range of frequency which is at the 2 points matches with the voltage and current



$$\text{Band width} = f_2 - f_1 = \frac{R}{2\pi L} \quad \{ \text{formula} \}$$

$$f_r - f_1 = \frac{R}{4\pi L}$$

$$f_2 - f_r = \frac{R}{4\pi L}$$

$$f_1 = f_r - \frac{R}{4\pi L}$$

$$f_2 = f_r + \frac{R}{4\pi L}$$

* Bandwidth of RLC circuit

A Quality factor: It is the ratio of electric energy stored in the circuit and energy dissipated in the capacitive part of the circuit. It is calculated for one period.

$$Q = \left[2\pi \times \frac{1}{2} L I^2 \right] / \left[(I/I_0)^2 R t \right] \quad \text{Watts.}$$

$$Q = \frac{2\pi \times \frac{1}{2} L I^2}{\frac{I^2}{2} R \left(\frac{1}{f} \right)} \quad \{ t = \frac{1}{f} \}$$

$$Q = \frac{2\pi L F}{R} = \frac{\omega L}{R} = \frac{x_L}{R}$$

$$Q = \frac{x_L}{R}$$

(no units). { in inductor or capacitor & resistor are given}

$$* \text{ In capacitive circuit} \rightarrow Q = \frac{2\pi \frac{1}{2} C V^2}{\frac{I^2}{2} R \left(\frac{1}{f} \right)}$$

$$Q = \frac{2\pi C (I^2 x_C^2)}{I^2 R \left(\frac{1}{f} \right)}$$

$$\{ V = I x_C \}$$

$$Q = \frac{2\pi f C x_C^2}{R} \rightarrow Q = \frac{\omega C x_C^2}{R} \rightarrow Q = \frac{\omega C \times \frac{1}{\omega^2 C^2}}{R}$$

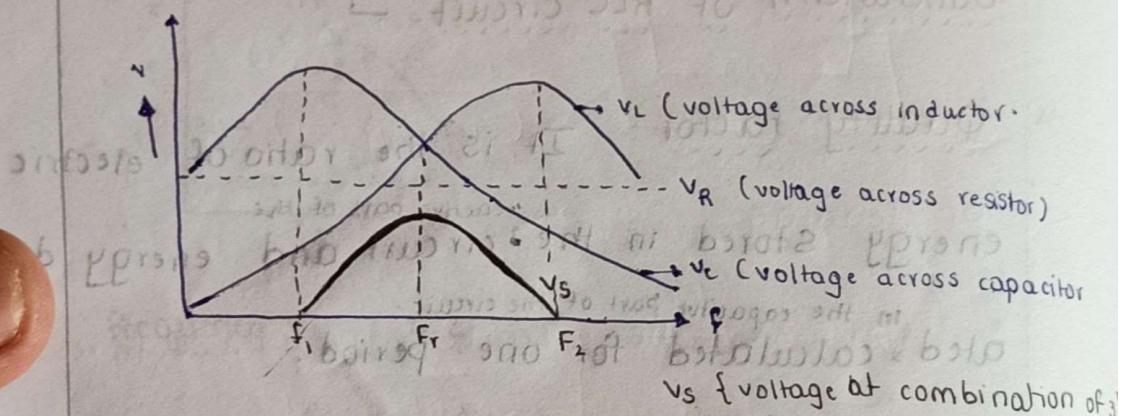
$$Q = \frac{1}{\omega C R}$$

for capacitive circuit $\Phi = \frac{x_c}{R}$
for resistive circuit.

- * These formulas are confined to RLC Series circuit only.

- * Note $\rightarrow Q = \frac{F_r}{B \cdot w}$ Frequency (resonant) / Bandwidth.

- * Voltage vs frequency graph



- * Admittance (y): It is the reciprocal of impedance $\rightarrow y = \frac{1}{z}$ units \rightarrow mho (Ω^{-1}) or S (siemens)

$$y = z^{-1} \text{ or } \frac{1}{z}, \text{ we know } z = R + jx$$

$$\text{and here } y = G + jB$$

$$\{ G = \text{conductance} = \frac{1}{R}, B = \text{susceptance} = \frac{1}{x} \}$$

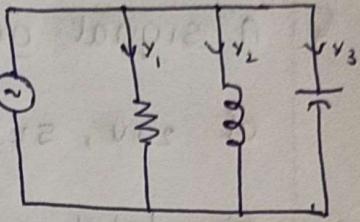
$$\rightarrow B_L = \frac{1}{x_L} = \frac{1}{2\pi f L} \text{ (inductive susceptance)} \rightarrow v$$

$$\rightarrow B_C = \frac{1}{x_C} = 2\pi f C \text{ (capacitive susceptance)} \rightarrow v$$

$$\rightarrow B = \frac{1}{x} \text{ (susceptance)} \rightarrow v$$

1*) consider

first branch admittance $y_1 \rightarrow$

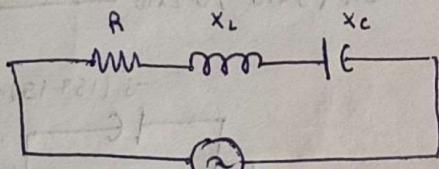


Second branch admittance $\rightarrow y_2$

third branch admittance $\rightarrow y_3$

then equivalent admittance $[Y_T = y_1 + y_2 + y_3]$

2) Now



Here

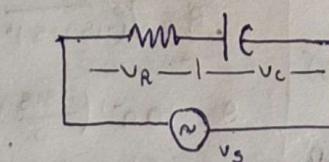
$$Z = \sqrt{R^2 + (x_L - x_C)^2}$$

Then $y = \sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{x_L} - \frac{1}{x_C}\right)^2} = \sqrt{\left(\frac{1}{R}\right)^2 + (B_L - B_C)^2}$

As, $Z = \frac{1}{y}$, we get

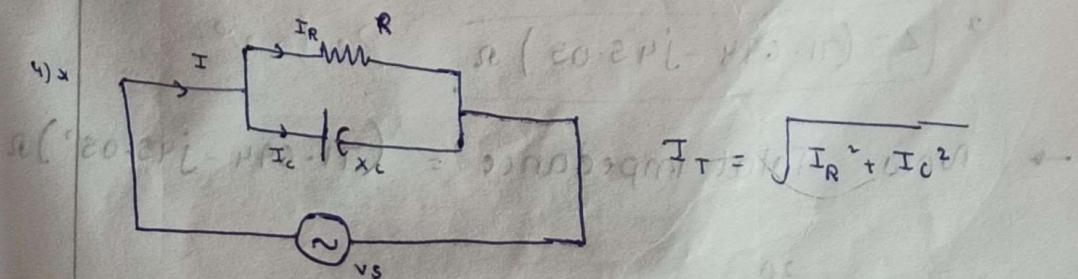
$$Z = \sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{x_L} - \frac{1}{x_C}\right)^2}$$

3) Next



$$v_s = \sqrt{v_R^2 + v_C^2}$$

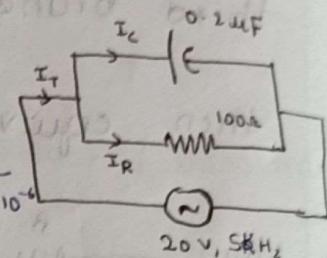
$$v_s = v_R - j v_C$$



Q A signal generator supplies a sine wave of 20V, 5kHz to the circuit shown in figure. find The total current I_T , phase angle ϕ , total impedance of the circuit

A

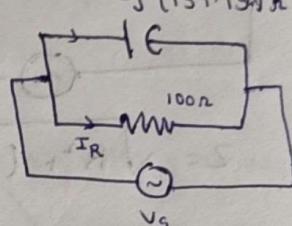
$$Z = \frac{X_R}{X_C} = \frac{1}{2\pi F C} = \frac{1}{2\pi (5 \times 10^3) 0.2 \times 10^{-6}}$$



$$X_C = 159.154 \Omega$$

$$* Z = \frac{(100)(-j159.154)}{(100-j159.154)}$$

$$\left\{ \frac{1}{Z} = \frac{1}{R} + \frac{1}{X_C} \right\} = \left\{ \frac{1}{Z} = \frac{1}{100} - \frac{1}{j(159.154)} \right\}$$



$$* Z = \frac{0-j15915.49}{100-j159.154}$$

$$a+jb \rightarrow R(\theta)$$

$$R = \sqrt{a^2 + b^2}$$

$$* Z = \frac{15915.49 \angle -90^\circ}{187.95 \angle -57.85^\circ}$$

$$\theta = \tan^{-1}\left(\frac{b}{a}\right)$$

$$\text{Now } 0-j15915$$

$$R = \sqrt{(-15915)^2} = 15915$$

$$\theta = \tan^{-1}\left(\frac{-15915}{0}\right) = 90^\circ$$

$$* Z = 84.67 \angle (-32.15^\circ) \Omega$$

$$* \text{ Total impedance} = 84.67 \angle -32.15^\circ \text{ with } \phi$$

$$* [Z = (71.694 - j45.05) \Omega] \text{ Rectangle}$$

$$\rightarrow \text{Now Total impedance} = (71.694 - j45.05) \Omega$$

$$* I_R = \frac{20}{100} = 0.2 A$$

$$* I_C = \frac{20}{159.15 \Omega} = 0.12 A = 0.1256 A$$

$$I_T = (0.2 - j0.12) A$$

$$I_T = \sqrt{0.2^2 + (0.12)^2}$$

$$\boxed{I_T = 0.23 A} \rightarrow \boxed{I_T = 0.2361 A}$$

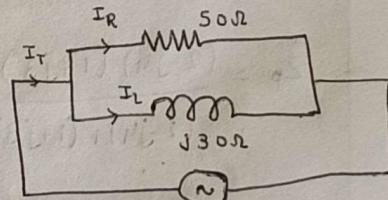
$$\rightarrow Z = \frac{V}{I} = \frac{20}{0.2361} = \underline{84.67 \Omega} \quad \{ \text{almost equal } 84.67 \}$$

$$\rightarrow \text{phase angle } \boxed{\phi = 32.15^\circ}$$

Q A 50Ω resistor connected with

Determine the total impedance and line current of the circuit.

$$A) Z_T = \frac{(50)(j30)}{(50+j30)} = \frac{0+j1500}{50+j30}$$



$$Z_T = \frac{1500 \angle 90^\circ}{58.309 \angle 30.96^\circ}$$

$$Z_T = 25.725 \angle 90 - 30.96^\circ$$

$$Z_T = 25.725 \angle 59.04^\circ \quad \{ \text{total impedance & } \phi \}$$

$$1) Z_T = (13.233 + j22.05) \Omega \quad \text{complex form.}$$

$$2) I_T = I_R + jI_L \rightarrow ①$$

$$I_R = \frac{20 \angle 0^\circ}{50 \angle 0^\circ} = 0.4 \text{ amp A}$$

Substitute in ①

$$I_L = \frac{20 \angle 0^\circ}{30 \angle 90^\circ} = 0.66 \angle -90^\circ \text{ A} \quad (\text{current lagging})$$

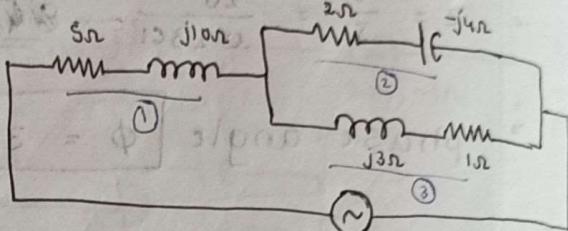
$$I_T = 0.4 + j0.66$$

$$I_T = \sqrt{(0.4)^2 + (0.66)^2}$$

$$I_T = \underline{0.77A} \quad \left\{ z = \frac{20}{0.77} \left\{ \frac{v}{i} \right\} = 25.9 \approx 25.71 \right.$$

Q) Determine equivalent impedance of the circuit shown in figure.

S) Consider



$$Z_1 = (5+j10)\Omega \rightarrow \textcircled{1}$$

$$Z_2 = (2-j4)\Omega \rightarrow \textcircled{2}$$

$$Z_3 = (1+j3)\Omega \rightarrow \textcircled{3}$$

$$\text{Now } Z_{\text{parallel}} = (\textcircled{2} \text{ & } \textcircled{3} \text{ in parallel}) \quad \frac{Z_2 \times Z_3}{Z_2 + Z_3}$$

$$Z_p = \frac{(2-j4)(1+j3)}{(2-j4)+(1+j3)}$$

$$Z_p = \frac{(4.47 \angle -63.43^\circ)(3.16 \angle 71.56^\circ)}{(3.16 \angle -18.43^\circ)}$$

$$Z_p = \frac{14.125 \angle 8.13^\circ}{3.16 \angle -18.43^\circ}$$

$$Z_p = 4.47 \angle 26.56^\circ \Omega \quad \text{(Impedance of parallel combination)}$$

$$= (3.998 + j1.99) \Omega$$

$$Z_T = (5+j10)\Omega + (3.998 + j1.99)\Omega$$

$$Z_T = (8.998 + j11.99) \Omega$$

* calculate using admittance.

$$Y_2 = \frac{1}{2-j4} \rightarrow ②$$

$$Y_2 = \frac{2+j4}{2^2-(j4)^2} = \frac{2+j4}{4+16} = \frac{2+j4}{20} = \frac{1+j2}{10} = \frac{1}{10} + j\frac{1}{5}$$

$$Y_2 = (0.1 + j0.2) \Omega^{-1}$$

$$Y_3 = \frac{1}{1+j3} = \frac{1-j3}{1^2+3^2} = \frac{1}{10} - j\frac{3}{10} =$$

$$Y_3 = (0.1 - j0.33) \Omega^{-1}$$

$$Y_P = Y_2 + Y_3$$

$$Y_P = (0.1 + j0.2) \Omega^{-1} + (0.1 - j0.33) \Omega^{-1}$$

$$Y_P = (0.2 - j0.1) \Omega^{-1}$$

$$Z_P = \frac{1}{0.2 - j0.1} \quad \left\{ Z = \frac{1}{Y_P} \right\}$$

$$Z_P = (4 + j2) \Omega \text{ almost same.}$$

$$Z_T = 1 / (154 \sqrt{Y_0}) \Omega$$

$$\rightarrow Y_T = \frac{Y_1 Y_P}{Y_1 + Y_P} \quad \left\{ Y_1 = \frac{1}{5+j10} = \frac{5-j10}{25} = \frac{1}{25} - j\frac{2}{25} \right\}$$

~~$$\rightarrow Y_T = \frac{(0.04 - j0.08)(0.2 - j0.1)}{0.04 - j0.08 + 0.2 - j0.1} \quad \left\{ Y_1 = 0.04 - j0.08 \right\}$$~~

~~$$\rightarrow Y_T = \frac{0.0008 - j0.0004 - j0.016 + 0.008}{0.24 - j0.18} \quad \begin{matrix} \text{wrong} \\ \text{don't read} \end{matrix}$$~~

$$\rightarrow Y_T = \frac{0.016 - j0.020}{0.24 - j0.18} = \frac{0.026}{0.3} \angle -51.30^\circ$$

$$= 0.0866 \angle -14.43$$

$$= 0.084 - j0.022 \quad Z_T$$

This also

$$= Z_T = \frac{1}{0.084 - j0.022}$$

$$= Z_T = \frac{0.084 + j0.022}{0.084^2 + 0.022^2} = \frac{0.3 \angle -36.87}{0.0264 \angle -51.30}$$

$$Z_T = 11.53 \angle 14.43$$

$$Z_T = 11.166 + j2.87$$

$$Z_T = 11.166 + j2.87 \quad \text{almost okay!}$$

$$* Y_T = \frac{(0.004 - j0.08)(0.2 - j0.1)}{0.04 - j0.08 + 0.02 - j0.1}$$

$$Y_T = \frac{0.008 - j0.004 - j0.016 + 0.008}{0.24 - j0.18}$$

$$Y_T = \frac{0 - j0.020}{0.24 - j0.18} = \frac{0.02 \angle -90}{0.3 \angle -36.87}$$

$$Z_T = \frac{0.3 \angle -36.87}{0.02 \angle -90}$$

$$Z_T = 1.5 \angle 53.13$$

$$Z_T = 8.996 + j12.003$$

* For RL Series

$$Z = R + jX_L$$

$$Y = G - jB_L$$

For RC Series

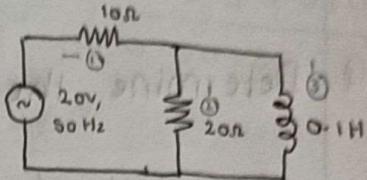
$$Z = R - jX_C$$

$$Y = G + jB_C$$

Q For the circuit shown in figure, Determine the value of I_{total} , Z_{total} and phase angle ϕ .

$$X_C = 2\pi f L = 2\pi (50) (0.1)$$

$$X_C = 31.41 \Omega$$



$$\text{Complex form } X_C = j31.41 \Omega$$

$$Z_P = \frac{20(j31.41)}{20 + j31.41} = \frac{0 + j628.2}{20 + j31.41} = \frac{628.2 \angle 90^\circ}{37.23 \angle 57.51^\circ}$$

$$Z_P = 16.87 \angle 32.49^\circ$$

$$Z_P = 14.230 + j9.062$$

$$Z_T = 10 + (14.230 + j9.062)$$

$$Z_T = 24.230 + j9.062$$

$$Z_T = 25.86 \angle 20.50^\circ$$

$$Y_2 = \frac{1}{20} = 0.05 \angle 0^\circ \quad \text{using admittance}$$

$$Y_3 = \frac{1}{j31.41} = \frac{0 - j31.41}{986.588} = \frac{31.41 \angle 90^\circ}{986.588}$$

$$Y_P = Y_2 + Y_3 = 0.05 + \angle 0^\circ + 0.0318 \angle 90^\circ$$

$$Y_P = \frac{0.05}{0.05 + 0.0318 \angle 90^\circ} = \frac{0.05}{0.0818 \angle 90^\circ} = \frac{0.05}{0.0818} \angle 90^\circ$$

$$Y_T = \frac{1}{10} = 0.1 \angle 0^\circ \rightarrow Y_T = \frac{(0.05 - j0.0018)(0.1)}{0.1 + 0.05 - j0.0018}$$

$$Y_T = \frac{0.05 - j0.0018}{0.15 - j0.0018} = \frac{(0.05 - j0.0018) \angle 90^\circ}{0.15 \angle -11.96^\circ} = \frac{0.05 \angle 90^\circ}{0.153 \angle -11.96^\circ}$$

$$Z_T = \frac{0.153 \angle -11.96^\circ}{0.0387 \angle -20.49^\circ} = \frac{0.153 \angle -11.96^\circ}{0.036 - j0.0018}$$

$$\phi = 20.50^\circ \text{ lagging}$$

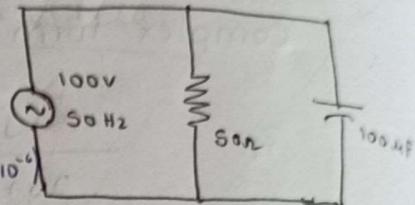
$$I_T = \frac{V}{Z_T} = \frac{20}{25.868 \angle 20.50^\circ} = (0.773 \angle -20.50^\circ) A$$

lagging

Q Determine the impedance and phase angle of circuit shown in figure.

A

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} = \frac{1}{2\pi 50(100 \times 10^{-6})} =$$



$$X_C = 31.83 \Omega$$

$$\text{Complex} = -j31.83 \Omega$$

$$\text{Impedance} = \frac{50(-j31.83)}{50 + j31.83} = \frac{-j1591.5}{50 + j31.83}$$

$$= \frac{1591.5 \angle -90^\circ}{59.27 \angle -32.48^\circ} = 26.85 \angle -57.52^\circ$$

$$= \boxed{26.85 \angle -57.5^\circ} = Z \text{ polar}$$

$$\rightarrow \boxed{Z = (14.418 - j22.65) \Omega} \text{ rect.}$$

$$\boxed{\phi = 57.5^\circ} \text{ phase angle.}$$

→ By admittance.

$$Y_1 = \frac{1}{50} = 0.02$$

$$Y_2 = \frac{1}{-j31.83} = \frac{j31.83}{1013.14} = \frac{31.83 \angle 90^\circ}{1013.14} = 0.031 \angle 90^\circ$$

$$Y_2 = j0.0314$$

$$Y_T = 0.02 + j0.0314$$

$$Z_T = \frac{0.02 - j0.0314}{0.02 + j0.0314 (0.02 - j0.0314)}$$

$$Z_T = \frac{0.02 - j0.0314}{0.0004 + 0.00096} = \frac{0.02 - j0.0314}{0.00138}$$

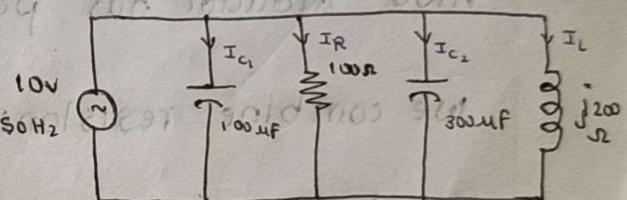
$$Z_T = 14.49 - j22.75$$

Q For the parallel circuit shown in figure. Find the magnitude of current in each branch &

what is the phase angle b/w applied voltage and current with respect to applied voltage

and current with respect to applied voltage

$$X_{C_1} = \frac{1}{2\pi f C} \\ = \frac{1}{2\pi (50)(100 \times 10^{-6})}$$



$$= 31.830 \Omega$$

$$I_{C_1} = \frac{V}{X_C} = \frac{10}{31.830} = 0.314 A$$

$$I_R = \frac{V}{R} = \frac{10}{100} = 0.1 A$$

$$X_{C_2} = \frac{1}{2\pi (50)(300 \times 10^{-6})} = 10.61 \Omega$$

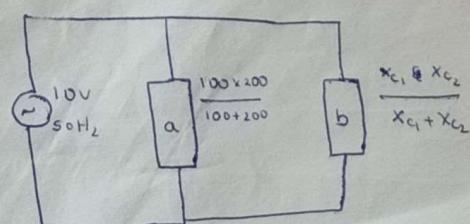
$$I_{C_2} = \frac{V}{X_{C_2}} = \frac{10}{10.61} = 0.94 A$$

$$I_L = \frac{10}{200} = 0.05 A$$

Now

$$a = 66.66 \Omega = 66.66 \Omega$$

$$b = 7.963 \Omega = 7.963 \Omega$$



a & b are in parallel

$$Z = \frac{ab}{a+b} = \frac{+66.66(-j7.93)}{+66.66 + j7.93} = \frac{-j530.813}{66.66 - j530.813} = \frac{530.813}{67.134/6.8}$$

$$Y = \frac{530.813/10/j20}{0.1j530.813/10} = \frac{530.813}{530.813/10} = 0.013$$

As both the capacitors have -ve reactances, (-j)

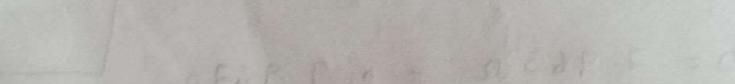
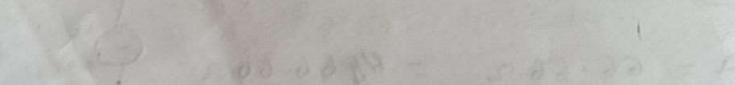
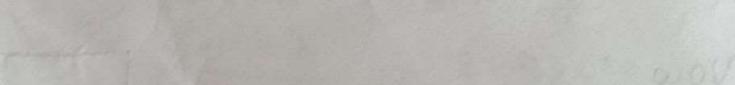
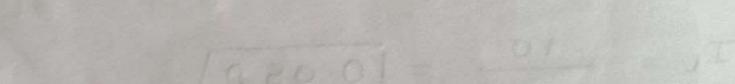
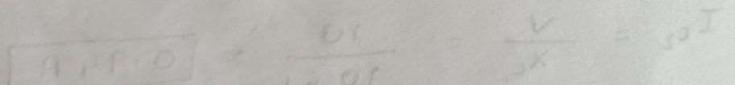
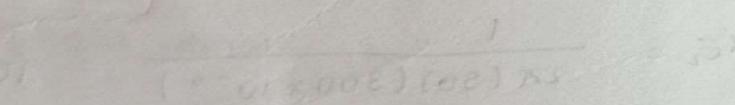
as we combine the reactance of them parallel.

Also inductor has positive reactance (+jx).

we combine resistance of resistor and

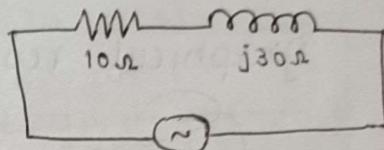
reactance of inductor parallelly.

$$Z = \frac{530.813 L-90}{67.134 L^6.812} = 7.906 L$$



The circuit shown in figure, a voltage of $V = 50 \sin(\omega t + 30^\circ)$ is applied. Determine the power, reactive power and apparent power, power factor of given circuit.

$$V(t) = V_m \sin(\omega t + \phi)$$



passes.

ϕ means $V_m \times$ at angle ϕ

$$\therefore V(t) = 50 \sin(\omega t + 30^\circ)$$

~~$\therefore V = 50 L 30^\circ \quad \{ V_m = 50 \} \text{ maximum voltage}$~~

~~$\therefore Z = 10 + j30 = 31.62 \angle 71.56^\circ$~~

Now calculate I_{rms} or $(I_{eff}) = \frac{V_{eff}}{Z}$

$$\frac{V_{rms}}{Z} = \frac{\frac{50}{\sqrt{2}} \angle 30^\circ}{31.62 \angle 71.56^\circ} \quad \left\{ V_{rms} = \frac{V_m}{\sqrt{2}} \right\}$$

$$I_{eff} = 1.118 \angle -41.56^\circ$$

$$I_{max} = I_{eff} \times \sqrt{2} = 1.118 \sqrt{2}$$

$$I_{max} = 1.58 A$$

$$I(t) = I_m \sin(\omega t - 41.56^\circ) A$$

$$I(t) = 1.58 \sin(\omega t - 41.56^\circ) A$$

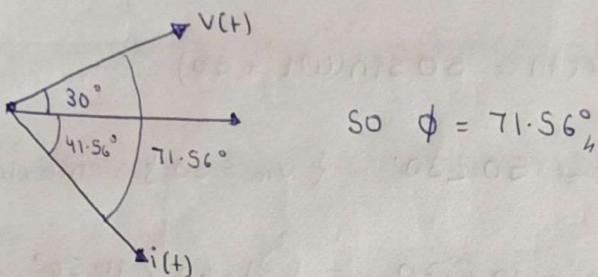
True power (or) Active power.

We know true power $P = V_{\text{eff}} I_{\text{eff}} \cos \phi$

$$P = \left(\frac{50}{\sqrt{2}} \right) \left(\frac{1.58}{\sqrt{2}} \right) \cos 71.56^\circ$$

$$P = 12.49 \text{ watts}$$

Graphical representation of $v(t)$ & $i(t)$



② Reactive power

$$Q = VI \sin \phi$$

$$Q = \frac{50}{\sqrt{2}} \left(\frac{1.58}{\sqrt{2}} \right) \sin 71.56^\circ$$

$$Q = 37.47 \text{ VAR}$$

{volt Ampere Reactive power}

③ Apparent power:

$$S = VI$$

$$S = \frac{50}{\sqrt{2}} \left(\frac{1.58}{\sqrt{2}} \right)$$

$$S = 39.5 \rightarrow \text{VA} \quad \{\text{volt ampere}\}$$

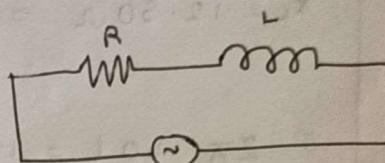
(Or) $\Rightarrow S = \sqrt{P^2 + Q^2}$, we get same value.

$$S = 39.49 \text{ VA}$$

④ Power factor $\rightarrow \cos \phi = \cos(11.56) = 0.316$
lag

Q Determine the circuit constants for the network shown in figure, if the applied voltage to the network is $v(t) = 100\sin(50t + 20^\circ)$.
The true power in the given network is 200 watts and the power factor is 0.707 lag.

-ing
A



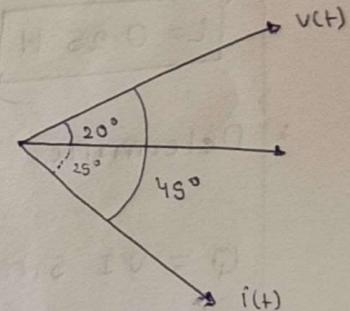
$$v(t) = 100 \sin(50t + 20^\circ)$$

$$V = \frac{100}{\sqrt{2}} \angle 20^\circ \text{ volts}$$

$$P = 200 \text{ W} \text{ (given)}$$

$$\text{PF} = \cos \phi = 0.707 \text{ lag}$$

$$\phi = \cos^{-1}(0.707) = 45^\circ$$



$$P = VI \cos \phi$$

$$I = \frac{P}{V \cos \phi} = \frac{200}{\frac{100}{\sqrt{2}} (0.707)}$$

$$I = 4 \text{ Amp} \quad \{ \text{Here } I = I_{\text{rms}} \text{ or } I_{\text{eff}} \}$$

$$I_m = I_{\text{rms}} \times \sqrt{2}$$

$$I_m = 5.665 \text{ Amp}$$

$$i(t) = 5.65 \sin(50t - 25^\circ) \text{ A}$$

$$\text{We know } Z = \frac{V}{I}$$

$$Z = \frac{(100/\sqrt{2}) \angle 20^\circ}{(5.65/\sqrt{2}) \angle -25^\circ}$$

$$Z = \frac{17}{8.69} \angle 45^\circ \Omega$$

$$Z = (12.50 + j12.50) \Omega$$

$$R = 12.50 \Omega$$

$$X_L = 12.50 \Omega = \omega L = 2\pi f L$$

$$= 2\pi \cdot 50 L = 12.50 \quad \{ \omega = 50 \text{ given} \}$$

$$= L = \frac{12.50}{50}$$

$$L = 0.25 \text{ H}$$

→ Determine reactive & apparent power for same circuit

$$Q = VI \sin \phi$$

$$Q = \frac{100}{\sqrt{2}} \left(\frac{5.65}{\sqrt{2}} \right) \sin 45^\circ$$

$$Q = 200 \text{ VAR (Reactive)}$$

$$S = VI = \frac{100}{\sqrt{2}} \cdot \frac{5.65}{\sqrt{2}}$$

$$S = 282.84 \text{ VA } \{ \text{Apparent} \}$$

Complex form of $S = P + jQ$

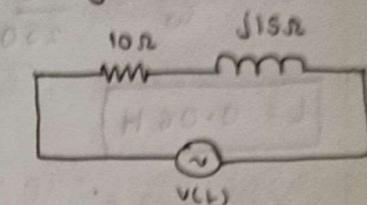
$$S = 200 + j 200$$

Q A voltage of $V(t) = 150 \sin(250t)$ is applied to the circuit shown in figure, determine the power delivered to the circuit and the value of inductance in Henry.

$$V(t) = 150 \sin 250t$$

$$V_m = 150 \text{ V}$$

$$\omega = 250$$



$$V_{rms} = \frac{150}{\sqrt{2}} \angle 0^\circ$$

$$V = 106.06 \text{ V}$$

$$\text{and } Z = 10 + 15j$$

$$\rightarrow Z = 18.02 \angle 56.30^\circ$$

$$\rightarrow I = \frac{V}{Z} = \frac{150}{\sqrt{2}} \angle 0^\circ$$

$$18.02 \angle 56.30^\circ$$

$$I = 5.88 \angle -56.30^\circ \text{ A} \quad \left\{ \begin{array}{l} I_m = 5.88 \times \sqrt{2} = 8.31 \text{ A} \\ \text{and } I(t) = 8.31 \sin(250t - 56.30^\circ) \end{array} \right.$$

$$\phi = 56.30^\circ$$

$$\cos \phi = \cos(56.30^\circ) = 0.55 \text{ lag}$$

\rightarrow Power delivered or average power = $VI \cos \phi$

$$P = VI \cos \phi$$

$$P = \frac{150}{\sqrt{2}} \times \frac{8.31}{\sqrt{2}} \cos(56.30^\circ)$$

$$P = 124.5$$

$$P = 345.80 \text{ watts}$$

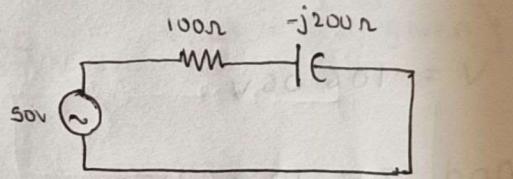
$$X_L = \omega L \quad \{ \omega = 250 \} \quad \& \quad X_L = 15 \Omega$$

$$L = \frac{X_L}{\omega} = \frac{15}{250}$$

$$L = 0.06 \text{ H}$$

Q) Determine the power factor, true power, reactive power and apparent power of given circuit.

$$\text{A} \quad Z = 100 - j200 \Omega$$



$$Z = 223.6 \angle -63.43^\circ$$

$$\phi = 63.43^\circ$$

$$\text{Power factor } \cos \phi = \cos(63.43) = 0.44 \text{ lead}$$

$$\text{True current } I = \frac{V}{Z} = \frac{50}{223.6} = 0.223 \text{ A}$$

$$\text{True power} = VI \cos \phi$$

$$P = (50)(0.223)(0.44)$$

$$P = 4.987 \text{ watts}$$

$$(\text{or}) \quad P = I^2 R$$

$$\text{Reactive power} \rightarrow Q = VI \sin \phi$$

$$Q = (50)(0.223) \sin(63.43)$$

$$Q = 9.97 \text{ VAR}$$

$$\text{also } Q = I^2 X_C = (0.223)^2 (200)$$

$$Q = 9.945$$

Apparent power $S = V I$

$$S = 50 (0.223) = 11.15 \text{ VA}$$

$$\text{also } S = I^2 Z \rightarrow (0.223)^2 (223.6)$$

$$S = 11.119 \text{ VA}$$

$$\text{also } S = \sqrt{P^2 + Q^2}$$

In a certain RC circuit, the true power is 300 watts and the reactive power is 1000 VAR. What is the apparent power & power factor.

$$P = 300 \text{ W}$$

$$Q = 1000 \text{ VAR}$$

$$S = \sqrt{P^2 + Q^2}$$

$$S = \sqrt{300^2 + 1000^2}$$

$$S = 1044.03 \text{ VA}$$

$$P = S \cos \phi \quad \{ S = VI \}$$

$$\cos \phi = \frac{P}{S} = \frac{300}{1044.03}$$

$$\cos \phi = 0.287 \text{ Lead}$$