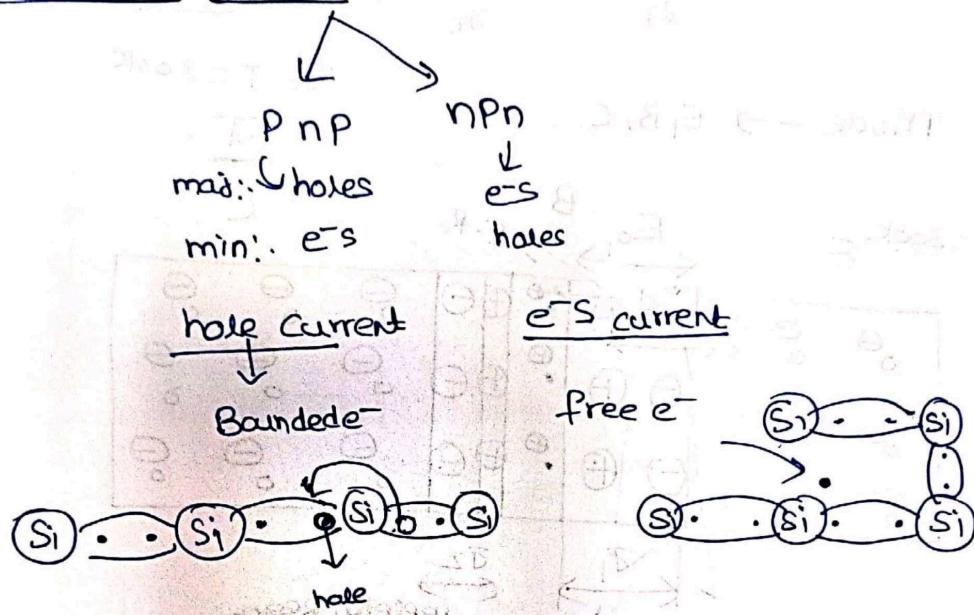


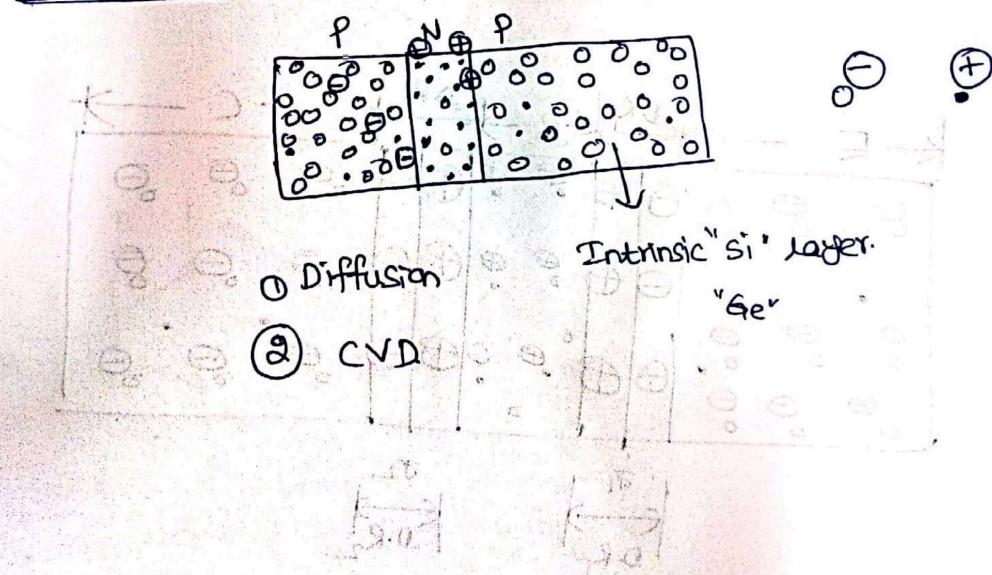
2

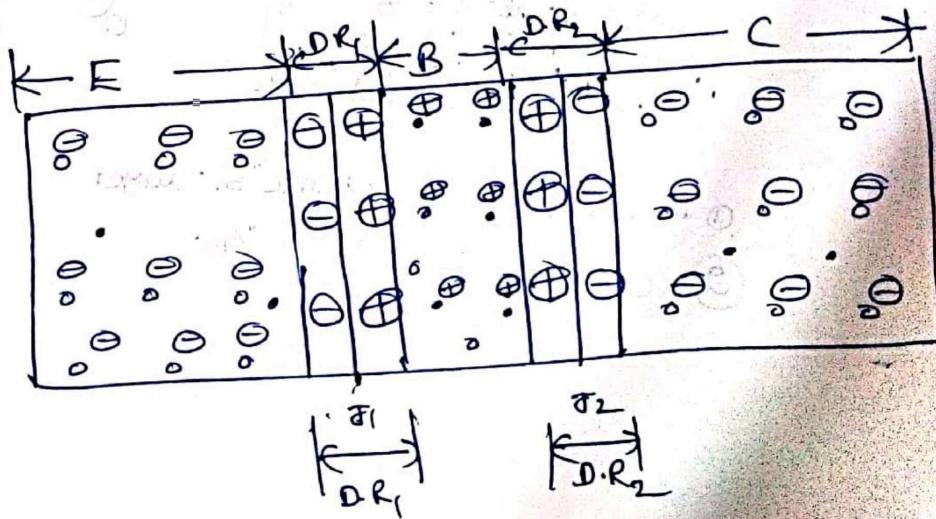
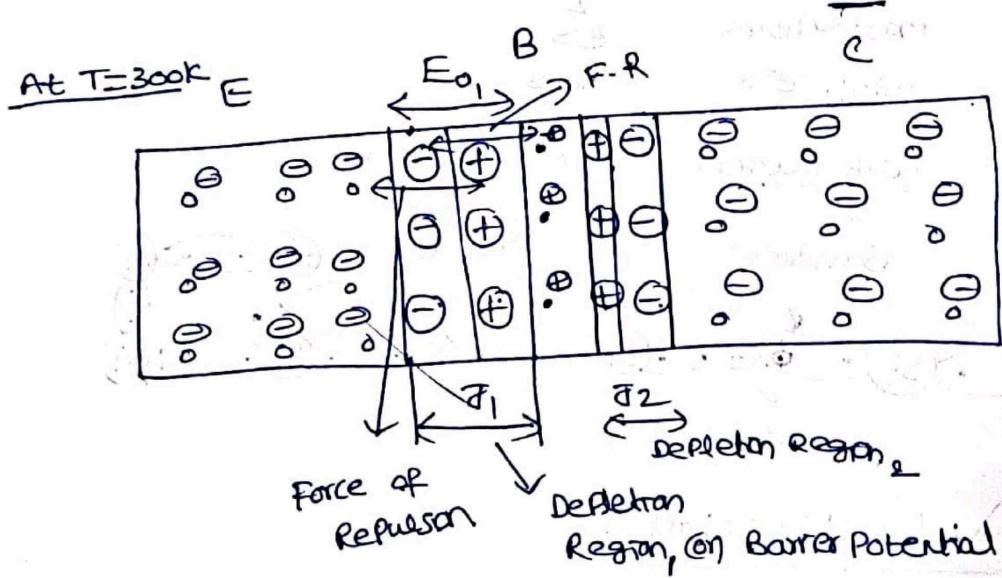
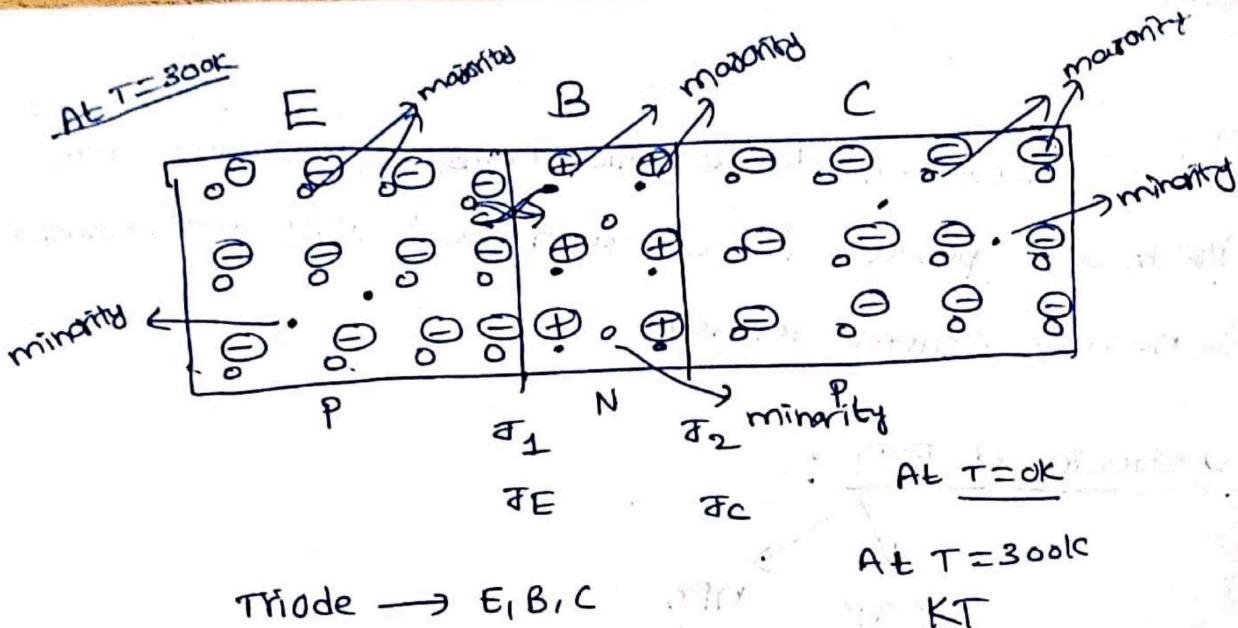
BJT: An electronic device which transfers current from I/P to O/P Resistor & produces current with the help of Both Positive & negative charged particle

### Construction of BJT:



### P N P Transistor:





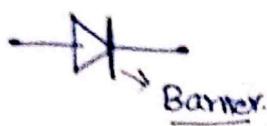
At  $T=300K$  & Equilibrium

## Schematic Diagram or symbol of BJT:

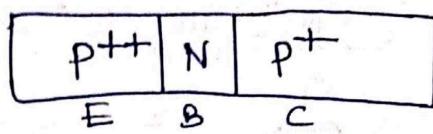
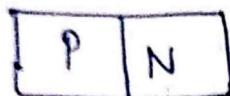
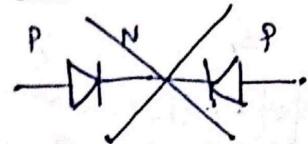
6

3

P-N Diode

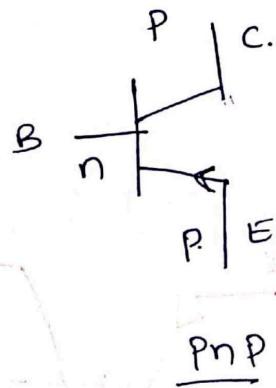
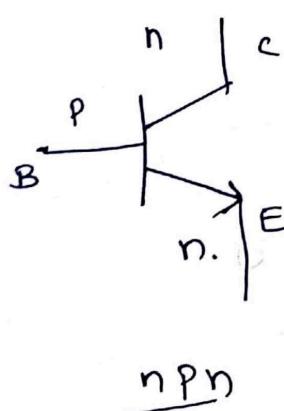
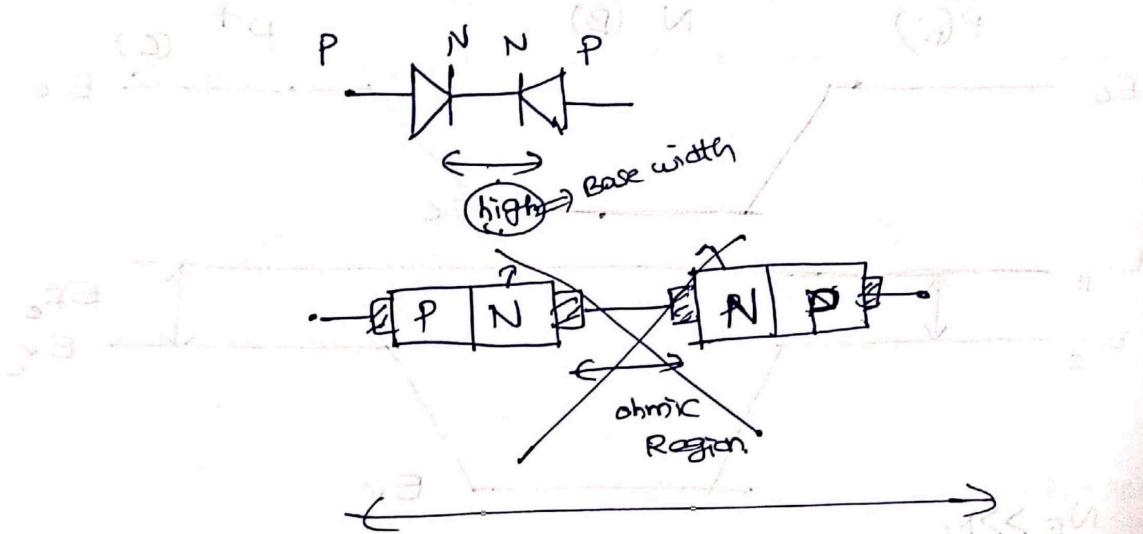


BJT



will back to back connection of two P-N diodes can form a BJT ??

NO



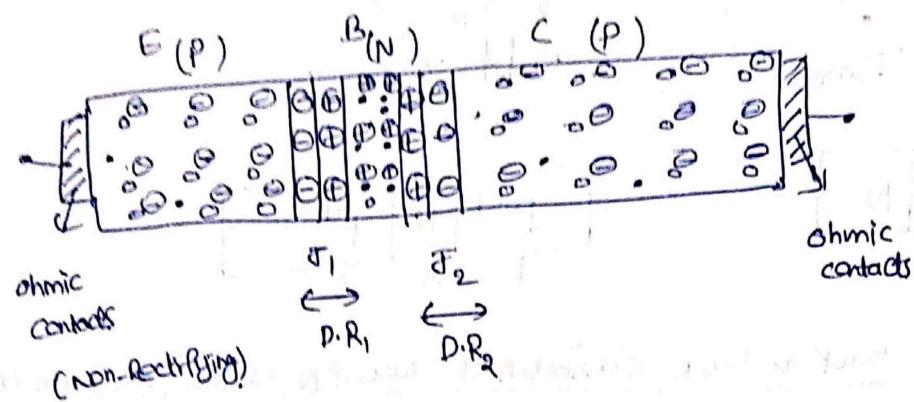
7

Fermi-Energy diagram of BJT in open circuit condition

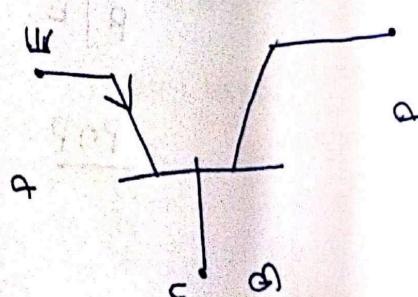
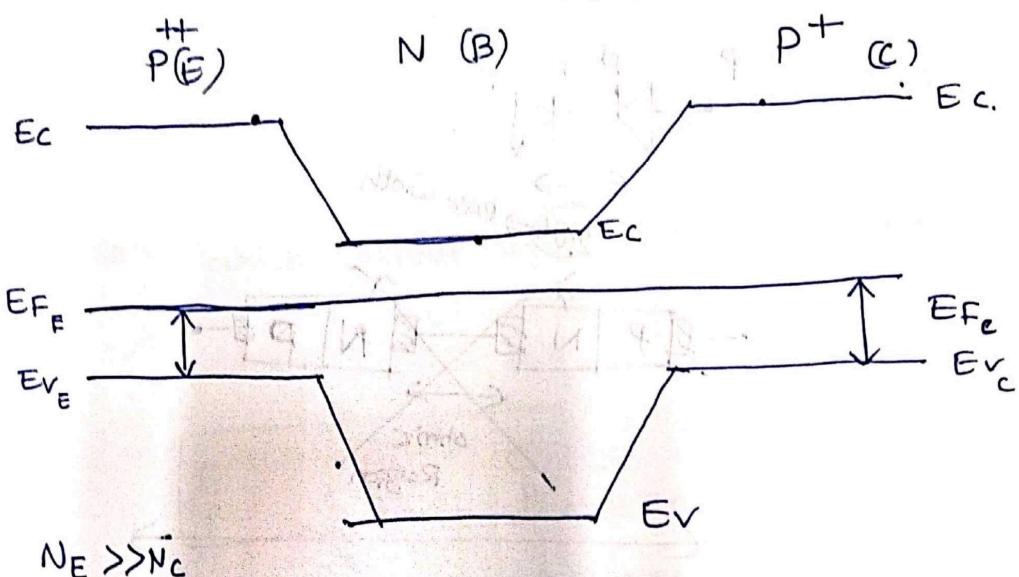
(a) Equilibrium

①

②



$$\phi_m < \phi_s$$



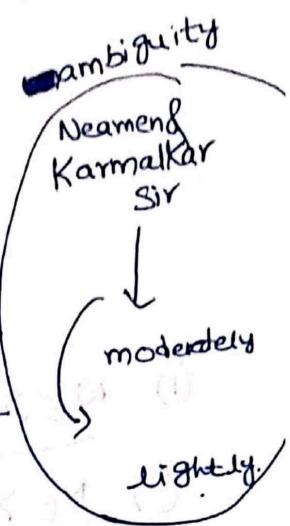
## 4

### Design specifications of E, B, C in BJT

① Size

② Doping

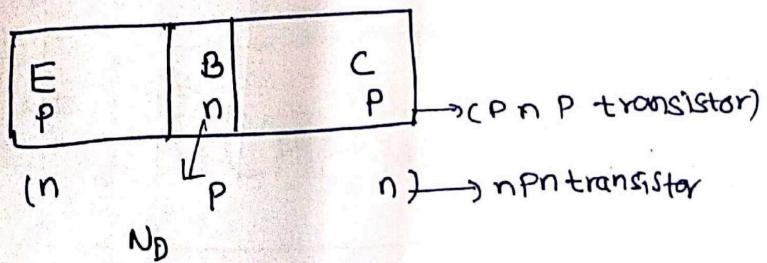
Terminal	<u>Size</u>	<u>Doping</u>
Emitter	moderate.	heavily
Base	thin.	lightly
Collector	high	moderately



Emitter: Emits  $e^-$ s, i.e. it supplies  $e^-$ s to O/P (or) holes to the Base.

Base : control action (it controls the supply of  $e^-$ s (or) holes from i/p to O/P)

Collector: which collects the  $e^-$ s & produces current (or) holes as O/P.

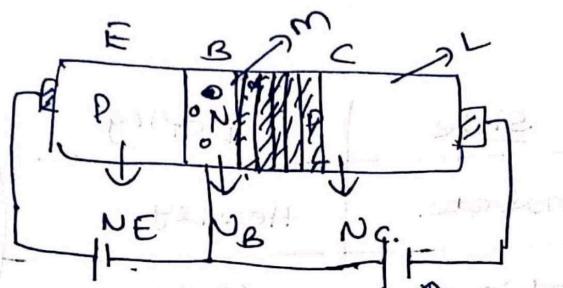


$$\text{Power dissipation} = P = \sigma E \text{ watts/cm}^3$$

$$\Downarrow P \propto \frac{1}{A \text{ or } \text{volume}}$$

Collector-High

If Base is moderately doped ??



(i)  $N_E \gg N_c \gg N_B$  (millman)

(ii)  $N_E \gg N_B > N_c$  (Karmalkar)

TOPICS like

⇒ Base width

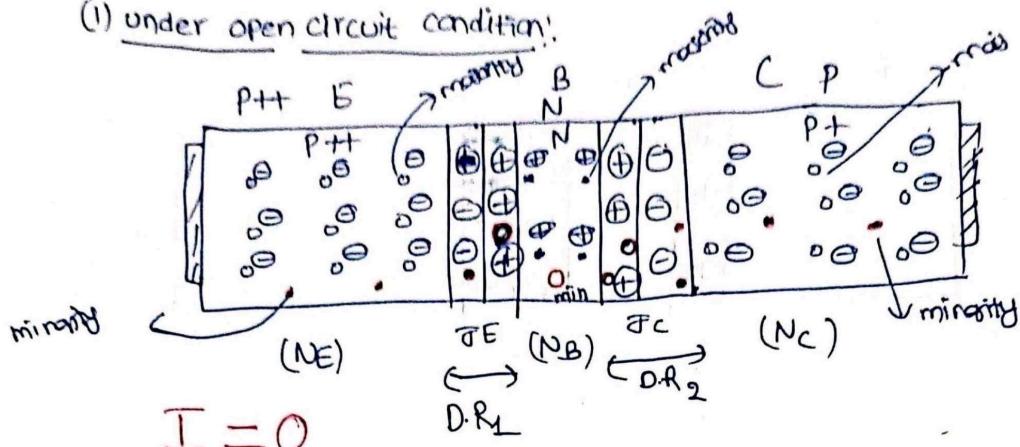
base modulation

⇒ Punch through (or)

Reach-through

### Working of BJT:

(i) under open circuit condition:



$$I = 0$$

$$V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A \cdot N_D}{n_i^2} \right) = \frac{kT}{q} \ln \left( \frac{N_E \cdot N_B}{n_i^2} \right)$$

$$V_{bi_2} = \frac{kT}{q} \ln \left( \frac{N_A \cdot N_D}{n_i^2} \right) = \frac{kT}{q} \ln \left( \frac{N_C \cdot N_B}{n_i^2} \right)$$

$$\frac{N_E \gg N_C > N_B}{p^{++} \quad p^+ \quad n}$$

$$V_{bi_1} > V_{bi_2}$$

$$\Downarrow \omega = \sqrt{\frac{2e}{qV} \left( \frac{1}{N_E} + \frac{1}{N_B} \right) (V_{bi})} \approx 0.7 \text{ V.}$$

$10^{17}, 10^{18}, \text{ (} 10^{19} \text{)}$

$$\uparrow \omega_2 = \sqrt{\frac{2e}{qV} \left( \frac{1}{N_C} + \frac{1}{N_B} \right) (V_{bi_2})} \approx 0.6$$

$\omega_1 > \omega_2$

$(V_{bi_1} > V_{bi_2})$

$\omega_2 > \omega_1$

$\omega_{D.R_2} > \omega_{D.R_1}$

$$\omega_1 = \sqrt{10^{-19} \times 0.7}$$

$$\omega_2 = \sqrt{10^{-15} \times 0.6}$$

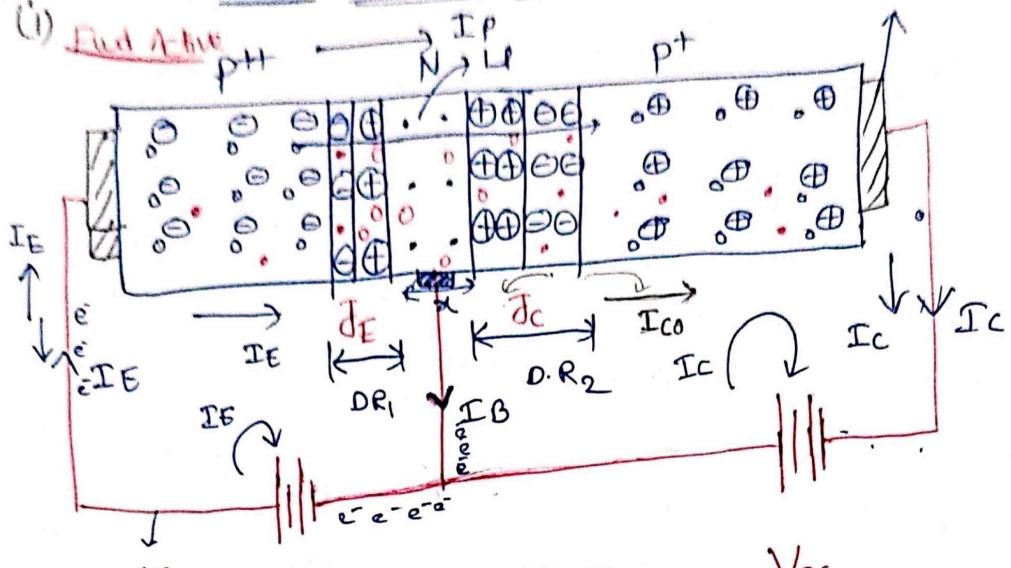
$\omega_2 > \omega_1$

modes of operation of BJT

drift contacts

Working of BJT in clamped CKT condition

(i) Forward bias



conducting  
wire.

$$V_{EB} = V_E - V_B$$

$$\alpha \ll L_p$$

$$V_{EB} = +ve$$

$$L_p = \sqrt{D_p N_p}$$

$$V_{BC}$$

$$\begin{aligned} V_{CB} &= -ve \\ &= V_C - V_B \\ &= (-ve) \end{aligned}$$

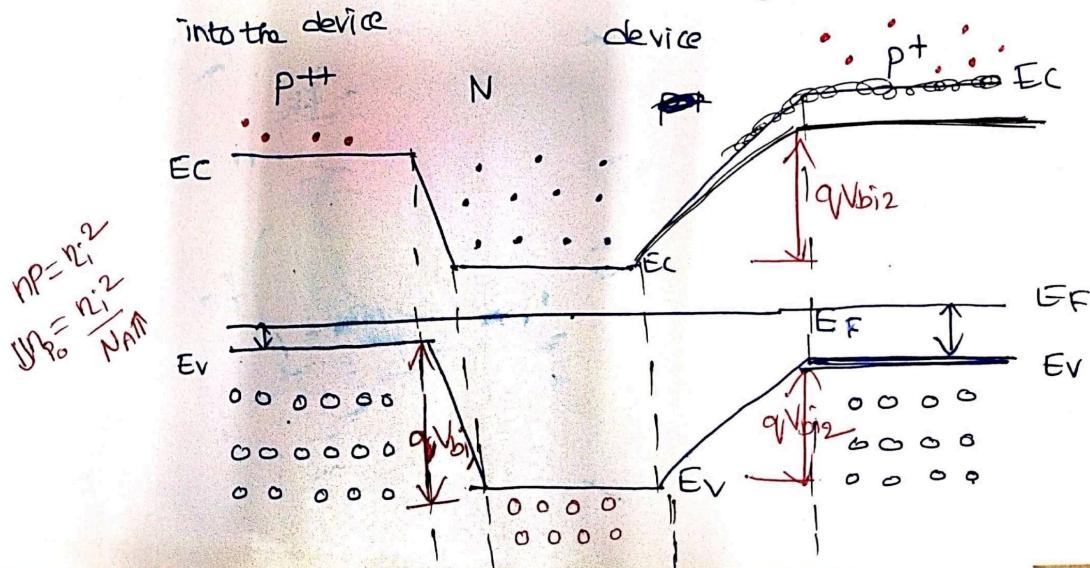
$$V_{CB} = -ve$$

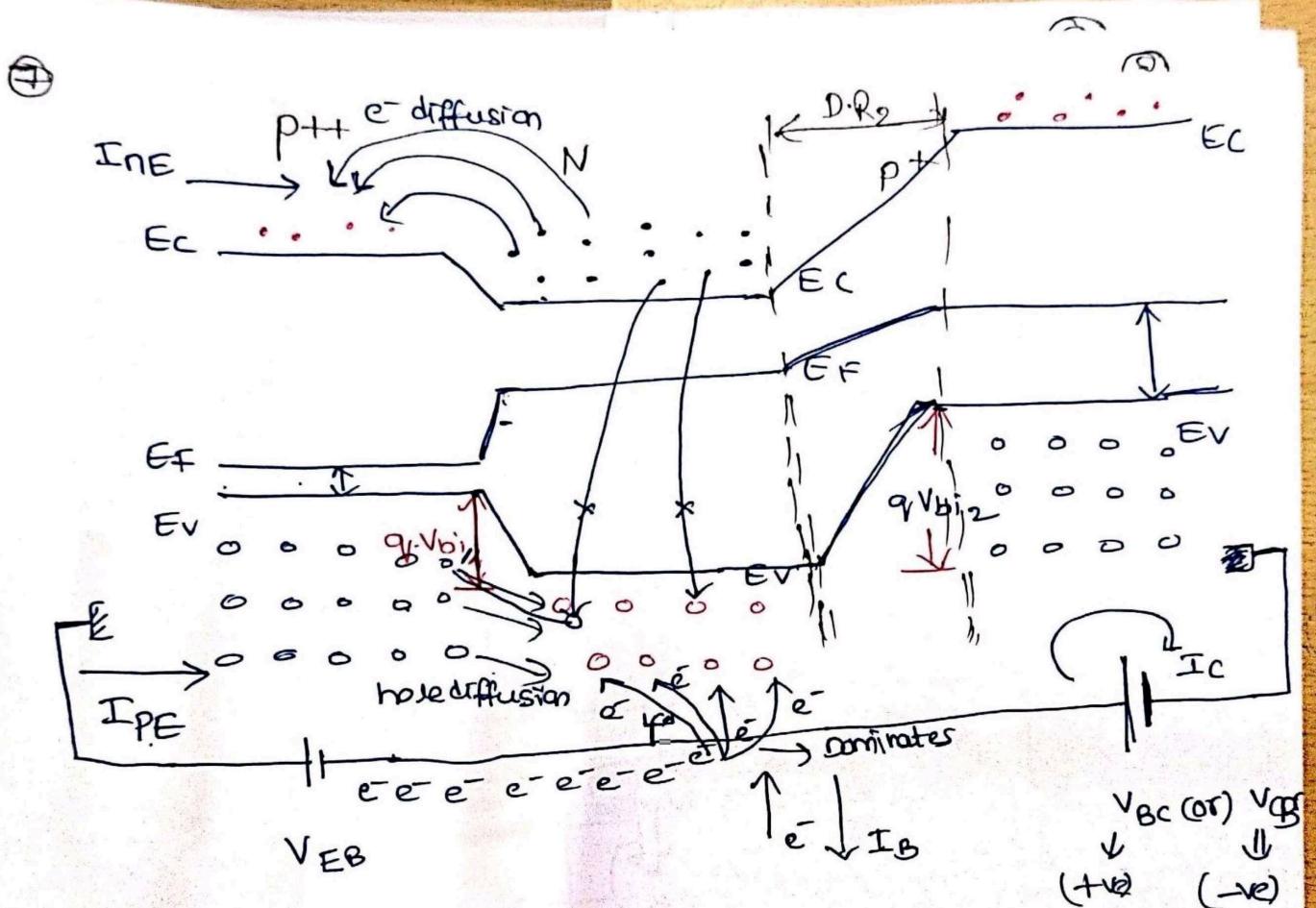
According to conservation of charge (KCL)

$$\star \boxed{I_E = I_B + I_C}$$

current entering  
into the device

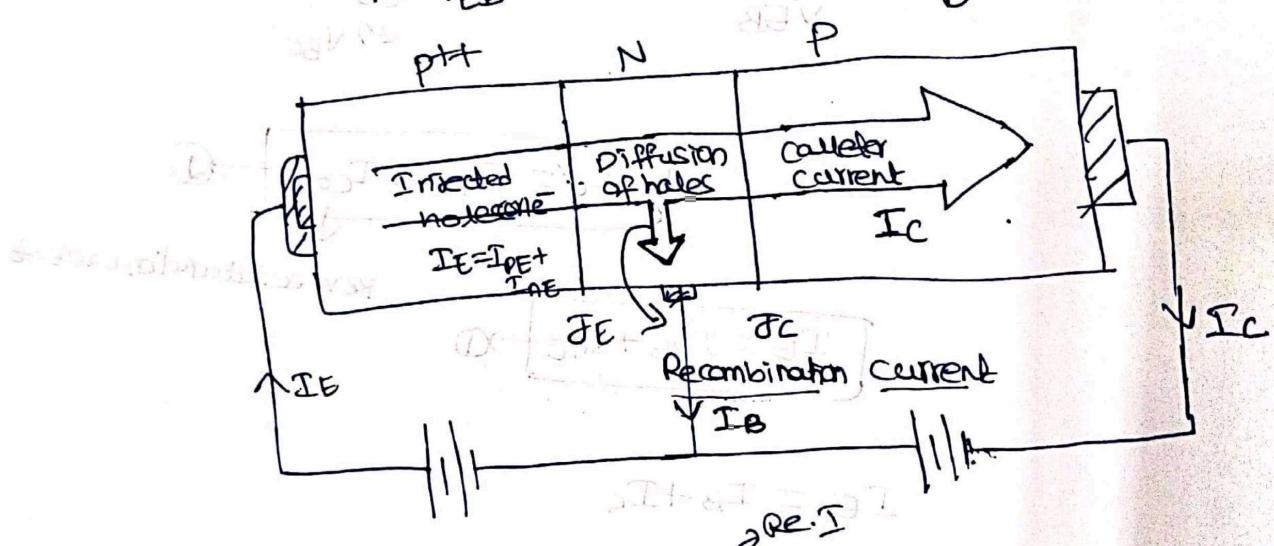
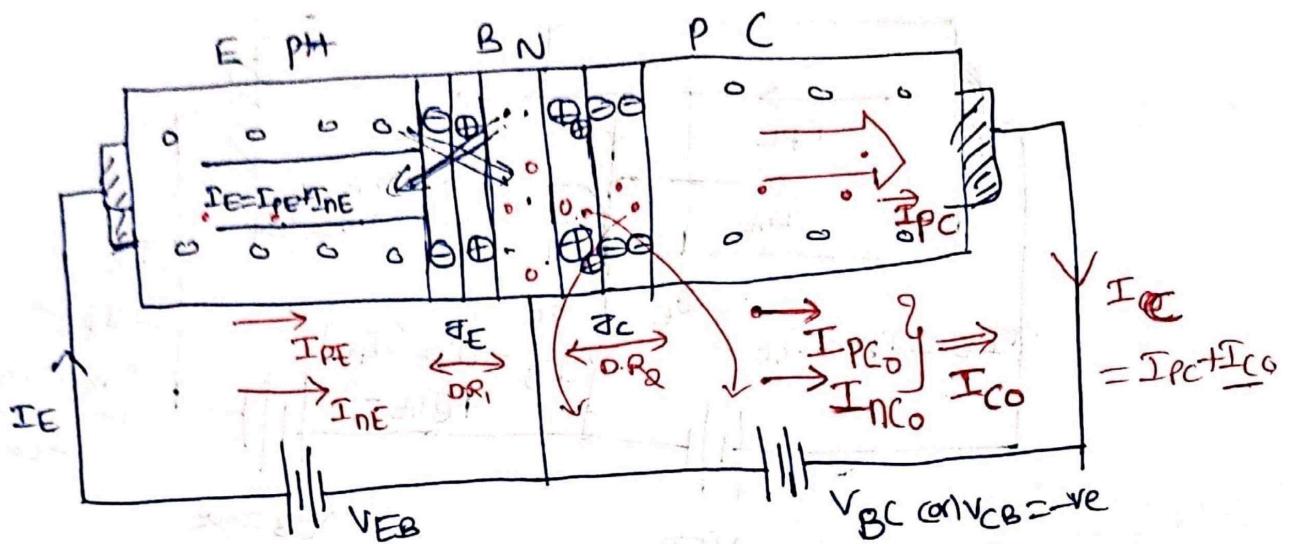
current leaving from the  
device





(8)

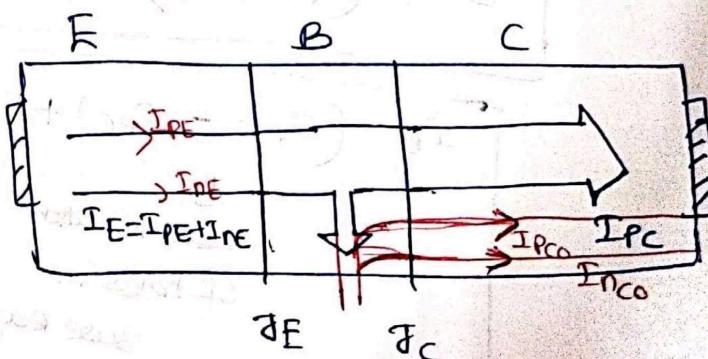
## Current components of BJT in Forward Active mode!

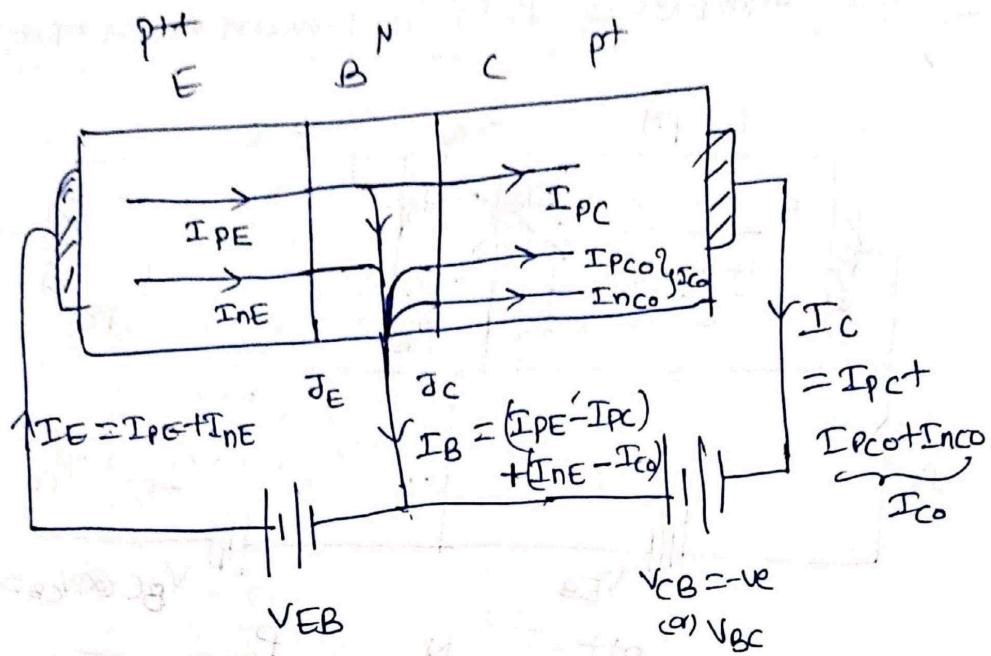


$$I_E = I_B + I_C \rightarrow \text{off}$$

$$I_C = I_E - I_B$$

IP  
(off)  $\rightarrow$  (on)  $\rightarrow$  IP  
loss





$$I_C = I_{PC} + I_{Co} \quad (1)$$

Reverse saturation current

$$I_E = I_{PE} + I_{nE} \quad (2)$$

$$I_E = I_B + I_C$$

$$I_B = I_E - I_C$$

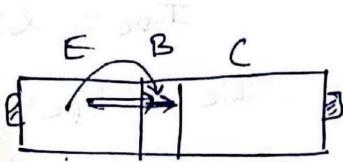
$$= (I_{PE} + I_{nE}) - (I_{PC} + I_{Co})$$

$$I_B = (I_{PE} + I_{nE}) - (I_{PC} + I_{PCo} + I_{nCo}) \quad (3)$$

$$I_B = (I_{PE} - I_{PC}) + (I_{nE} - I_{Co})$$

Recombination  
of holes in  
Base Region

Recombination of  
e<sup>-</sup>s in Base  
Region

Performance parameters:① Emitter Injection efficiency ( $\mu^*$ )② Base Transportation factor ( $\beta^*$ )③ DC gain ( $\alpha$ ,  $\beta$ ,  $\mu$ )① Emitter Injection efficiency ( $\mu^*$ )

$$\mu^* = \frac{I_{PE}}{I_E}$$

 $I_E$ 

$$I_E = I_{PE} + I_{NE}$$

$$\mu^* = \frac{I_{PE}}{I_{PE} + I_{NE}}$$

② Base Transportation factor: ( $\beta^*$ )

$$\beta^* = \frac{I_{PC}}{I_{PE}}$$

$$I_{PE}$$

③ DC gain or DC current gain ( $\alpha$ ,  $\beta$ ,  $\mu$ )

$$CB - \alpha = \frac{OIP}{IIP} = \frac{I_C}{I_E}$$

$$CE - \beta = \frac{I_C}{I_B}$$

$$CC - \mu = \frac{I_E}{I_C}$$

$$\alpha = \frac{I_C}{I_E} = \frac{I_C}{I_E} = \frac{I_{PC}}{I_E}$$

$$I_C = I_{PC} + I_{CO}$$

$$I_C \approx I_{PC}$$

$$\alpha = \frac{I_{PC}}{I_E}$$

$$I_{PC} = \alpha I_E$$

$$I_C = I_{PC} + I_{CO}$$

$$I_C = \alpha I_E + I_{CO} \Rightarrow C-B$$

CB

$$I_C = \alpha I_E + I_{CBO}$$

Reverse sat current

In CB when emitter is

open.

CE:

$$I_C = \beta I_B + I_{CEO}$$

CC:

$$I_E = \beta I_B + I_{CCO}$$

Relation b/w  $\alpha$ ,  $\beta^*$ ,  $\mu^*$

$$\mu^* = \frac{I_{PE}}{I_E}$$

$$\beta^* = \frac{I_{PC}}{I_{PE}}$$

$$\alpha = \frac{I_{PC}}{I_E} = \left( \frac{I_{PC}}{I_{PE}} \right) \times \frac{I_{PE}}{I_E}$$

★  $\alpha = \beta^* \times \mu^*$

Relation b/w  $\alpha$ ,  $B$ ,  $\mu$

$$\alpha = \frac{I_{PC}}{I_E}$$

neglecting Reverse  
sat Currents

$$I_C = I_{PC} + \cancel{I_{CE}}$$

$$I_C \approx I_{PC}$$

$$\alpha = \frac{I_C}{I_E}$$

$$\beta = \frac{I_C}{I_B}$$

$$\mu = \frac{I_E}{I_B}$$

Relation b/w  $\alpha, \beta, \gamma$ :

$$I_E = I_B + I_C \rightarrow (1)$$

①

$$\frac{I_E}{I_B} = \frac{I_B}{I_C} + \frac{I_C}{I_B}$$

$$\gamma = 1 + \beta$$

$$\beta = \gamma - 1$$

$$I_C = \alpha I_E \rightarrow (2)$$

Sub eq ① in ②

$$I_C = \alpha (I_B + I_C)$$

$$I_C = \alpha I_B + \alpha I_C$$

$$I_C - \alpha I_C = \alpha I_B$$

$$I_C (1 - \alpha) = \alpha I_B$$

$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}$$

$$\beta = \frac{\alpha}{1 - \alpha}$$

$$\gamma = 1 + \beta$$

$$\gamma = 1 + \frac{\alpha}{1 - \alpha}$$

$$\gamma = \frac{1 - \alpha + \alpha}{1 - \alpha} = \frac{1}{1 - \alpha}$$

$$I_C = \beta I_B \rightarrow (3)$$

$$I_C = \beta (I_E - I_C)$$

$$I_C = \beta I_E - \beta I_C$$

$$I_C + \beta I_C = \beta I_E$$

$$(1 + \beta) I_C = \beta I_E$$

$$\alpha = \frac{I_C}{I_E} = \frac{\beta}{1 + \beta}$$

$$\alpha = \frac{\beta}{1 + \beta}$$

$$\alpha = \frac{\beta - 1}{\gamma - \beta} = \frac{\beta - 1}{\gamma}$$

1

## Relation between $\alpha$ , $\beta$ & $\mu$

We know that  $I_E = I_B + I_C$   $\rightarrow \textcircled{1}$

Divide eq  $\textcircled{1}$  with  $I_E$ , we will get

$$\frac{I_E}{I_E} = \frac{I_B}{I_E} + \frac{I_C}{I_E} \quad (\because CB \Rightarrow \alpha = \frac{I_C}{I_E})$$

$$1 = \frac{I_B}{I_E} + \frac{I_C}{I_E} \quad CE \Rightarrow \beta = \frac{I_C}{I_B}$$

$$1 = \frac{I_B}{I_E} + \alpha \quad (\because \alpha = \frac{I_C}{I_E}) \quad CC \Rightarrow \mu = \frac{I_E}{I_B}$$

$$1 - \frac{I_B}{I_E} = \alpha$$

$$\alpha = 1 - \frac{I_B}{I_C} \times \frac{I_C}{I_E} = 1 - \frac{1}{\beta} \times \alpha$$

$$\alpha = 1 - \frac{\alpha}{B}$$

$$1 - \alpha = \frac{\alpha}{B}$$

$$B = \frac{\alpha}{1 - \alpha}$$

"B" in terms of "α"

②

TO get the Relation "α" in terms of "B" add 1 to eq ② on both sides

$$B+1 = \frac{\alpha}{1 - \alpha} + 1$$

$$B+1 = \frac{\alpha + 1 - \alpha}{1 - \alpha} = \frac{1}{1 - \alpha}$$

$$1 + B = \frac{1}{1 - \alpha}$$

$$1 - \alpha = \frac{1}{1 + B}$$

$$1 - \frac{1}{1 + B} = \alpha$$

$$\alpha = \frac{1 + B - 1}{1 + B} = \frac{B}{1 + B}$$

$$\alpha = \frac{B}{1 + B}$$

③

we know that  $I_E = I_B + I_C \rightarrow \text{divide it with } I_B$  we get

$$\frac{I_E}{I_B} = \frac{I_B}{I_B} + \frac{I_C}{I_B}$$

$$\frac{I_E}{I_B} = 1 + \frac{I_C}{I_B}$$

$$(\because \text{we know that } A = \frac{I_E}{I_B})$$

$$A = 1 + \beta \quad \text{--- (4)}$$

$$\beta = \frac{I_C}{I_B}$$

$$\text{But we know that } \beta = \frac{\alpha}{1-\alpha}$$

$$\text{so from (4)} \quad A = 1 + \frac{\alpha}{1-\alpha} = \frac{1-\alpha+\alpha}{1-\alpha} = \frac{1}{1-\alpha}$$

$$A = \frac{1}{1-\alpha}$$

& we can write " $\alpha$ " in terms of  $A$  ie

$$1-\alpha = \frac{1}{A} \quad 1 - \frac{1}{A} = \alpha \Rightarrow \alpha = \frac{A-1}{A}$$

Relation b/w  $\alpha, \beta, \mu$ : Given a ratio  $\alpha = \frac{P}{Q}$  &  $\beta = \frac{Q}{R}$  then

$\Rightarrow \alpha$  in terms of  $\beta$  &  $\mu$  is

$$\alpha = \frac{\beta}{1+\beta}, \quad \alpha = \frac{\mu-1}{\mu}$$

$\Rightarrow \beta$  in terms of  $\alpha$  &  $\mu$  is

$$\beta = \frac{\alpha}{1-\alpha}, \quad \beta = \mu-1$$

$\Rightarrow \mu$  in terms of  $\alpha$  &  $\beta$  is

$$\mu = \frac{1}{1-\alpha}, \quad \mu = 1+\beta$$

## Circuit Configurations of BJT:

(i) There are three circuit configurations of BJT

(i) Common Emitter

(ii) Common Base

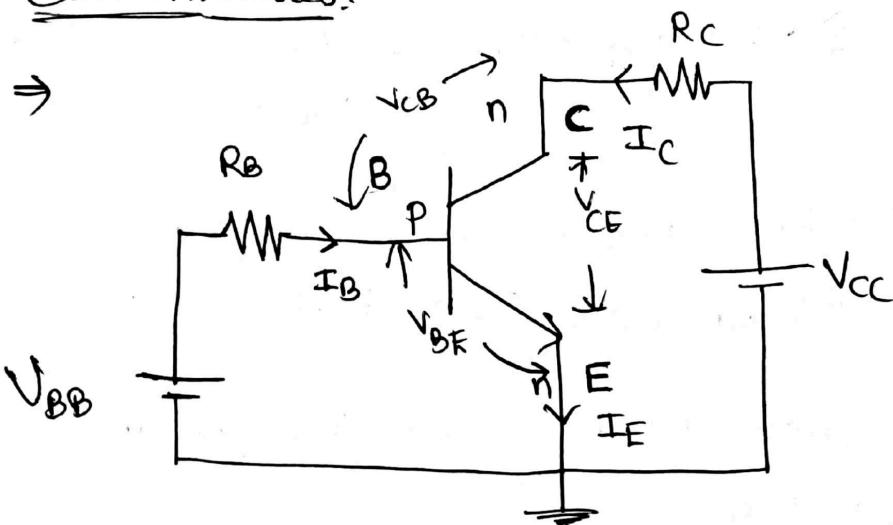
(iii) Common collector.

Common Emitter: Emitter is grounded & Emitter is common to both input (Base) and output (Collector)

Common Base : Base is grounded & Base is common to both input (Emitter) and output (Collector)

Common collector : Collector is grounded & collector is common to both input (Base) and output (Emitter)

### Common Emitter:



- ⇒ The emitter is grounded, Emitter is common to base and collector.
- ⇒  $R_B \Rightarrow$  Input Resistance,  $R_C \Rightarrow$  Output Resistance

⇒  $R_B, R_C \Rightarrow$  will provide drop in input voltage, in order to reduce the sudden changes in voltage.

⇒ From KCL of the above circuit,  $I_E = I_B + I_C$

The gain of the common emitter circuit configuration is "B"

$$B = \frac{\text{output of the collector } C \text{ (base current in pnp)}}{\text{Input current}}$$

$$B = \frac{I_{PC}}{I_B}$$

where  $I_C = I_{PC} + I_{CO}$ , so  $I_{PC} \approx I_{PC}$ ; since  $I_{CO}$  is negligible

$$I_C \approx I_{PC}$$

$$B = \frac{I_{PC}}{I_B} \quad (\text{or}) \quad B \approx \frac{I_C}{I_B}$$

As we know that  $I_C = I_{PC} + I_{CO} \rightarrow A$

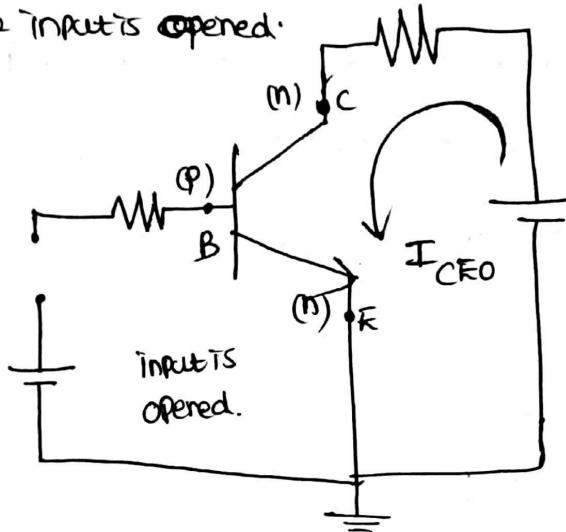
$$\therefore I_{PC} = B I_B \rightarrow B$$

substitute eq(B) in eq(A)

$$I_C = B I_B + I_{CO} \rightarrow C$$

$$I_C = \beta I_B + I_{C0}$$

Where  $I_{C0}$  is the Reverse saturation current, which is measured in between Collector & Emitter when Base is opened (or) the input is opened.



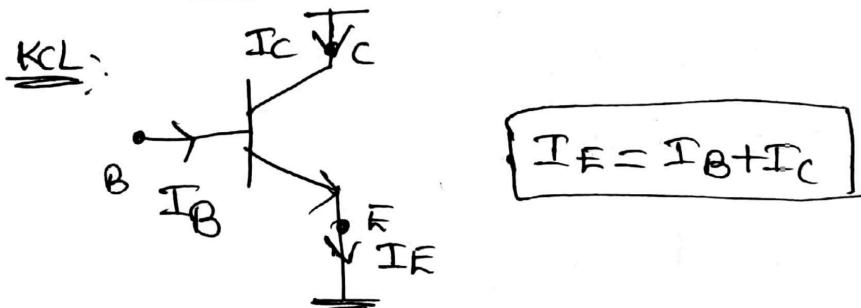
$$I_C = I_{C0} \quad \text{when } I_B = 0 \text{ (or) Base is opened.}$$

When we apply input

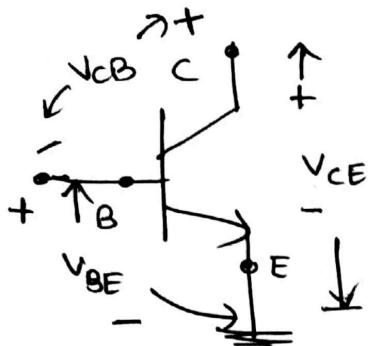
$$I_C = \beta I_B + I_{C0}$$

$I_{C0}$  = Reverse saturation current b/w collector & emitter  
(or) collector to emitter reverse saturation current

KVL & KCL in CE: (In Forward active mode)



KVL:



By applying KVL

$$-V_{BE} - V_{CB} + V_{CE} = 0$$

$$V_{CE} = V_{CB} + V_{BE}$$

For nPN

V-I Characteristics of CE amplifier:

- ⇒ To draw the VI characteristics, we know which two port N/W Parameters that we are using for the Analysis of Transistor. Because we have grounded one of the three terminals of BJT, so we have to use two port N/W parameters
- ⇒ Among the six ( $h_{11}$ ) Two port N/W Parameters, we are using " $h$ -Parameter model" to analyze BJT

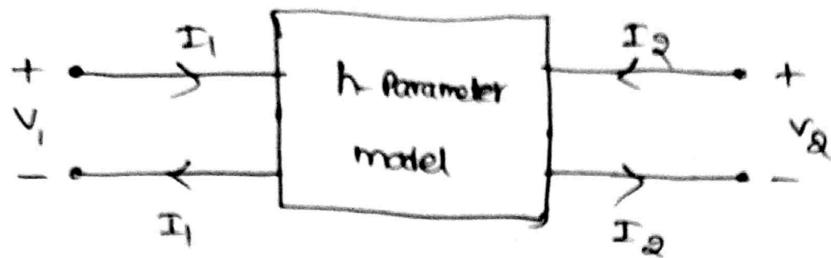
Why we are using  $h$ -Parameter model for the Analysis of BJT?

In BJT, the output current ( $I_C$ ) and input Voltage ( $V_{BE}$ ) are dependent parameters like  $h$ -parameter model.

In  $h$ -parameter model

$$V_1 = h_{11}I_1 + h_{12}V_2$$

$$I_2 = h_{21}I_1 + h_{22}V_2$$



$V_1, I_1 \Rightarrow$  input voltage & current

$V_2, I_2 \Rightarrow$  output voltage & current

where  $V_1, I_2$  are dependent parameters

Similarly In BJT input voltage  $V_{BE}$  and output current  $I_C$  are dependent parameters So

$$V_1 = V_{BE} \quad V_2 = V_{CE}$$

$$I_1 = I_B \quad I_2 = I_C$$

so h-parameter model for BJT is

$$V_{BE} = h_{11} I_B + h_{12} V_{CE}$$

$$I_C = h_{21} I_B + h_{22} V_{CE}$$

$\Rightarrow$  Since  $I_C$  (output current) depends on input current ( $I_B$ ) and output voltage ( $V_{CE}$ ), i.e. In forward active mode

$I_C = f(I_B)$  and if we  $\uparrow V_{CE}$ ,  $I_C \uparrow$ . So  $I_C$  depends on  $I_B$  &  $V_{CE}$

$$\therefore I_C = h_{21} I_B + h_{22} V_{CE}$$

⇒ Input Voltage  $V_{BE}$  depends on  $V_{CE}$  and  $I_E$ . i.e. If we  $\uparrow$  (increase)  $V_{CE}$ , Reverse bias across  $J_{C}\uparrow$ , then width of the depletion Region  $\uparrow$  and penetrates into Base Region, due to this Effective Base width  $\downarrow$ , so now we have to give less  $V_{BE}$  to make the holes to penetrate into Base Region.

i.e. Input voltage  $V_{BE}$  to be given  $\downarrow$ , because of the reduction in  $I_B$  due to  $\downarrow$  in  $I_B$ ,  $I_C\uparrow$  which makes the  $I_B$  ~~to be given~~ less than Previous Input for the required  $I_C$  which requires less " $V_{BE}$ " to be given to get " $I_C$ ".

( $\uparrow$  = Increase ;  $\downarrow$  = Decrease)

So

$$V_{BE} = h_{11}I_B + h_{12}V_{CE} \rightarrow \textcircled{A}$$

$$I_C = h_{21}I_B + h_{22}V_{CE} \rightarrow \textcircled{B}$$

⇒ To draw the input V-I characteristics of the BJT, we need i/P voltage ( $V_{BE}$ ) on x-axis and input current ( $I_B$ ) on y-axis

So From eq  $\textcircled{A}$

$$\underline{V_{BE}} = h_{11} \underline{I_B} + h_{12} \underline{V_{CE}} \Rightarrow V_{CE} \text{ constant}$$

$$I_C = h_{21} \underline{I_B} + h_{22} \underline{V_{CE}}$$

To draw the V-I ds for  $\underline{V_{BE}}$  and  $\underline{I_B}$ ,  $\underline{V_{CE}}$  is constant

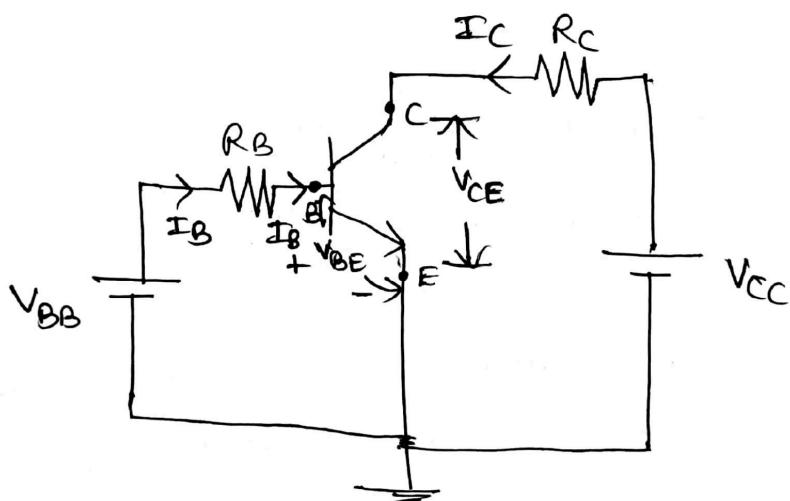
⇒ To draw the input V-I characteristics for  $V_{BE}$  and  $I_B$ , the output voltage ( $V_{CE}$ ) is constant.

⇒ Similarly to draw the output V-I characteristics for  $V_{CE}$  and  $I_C$ , the input current  $I_B$  is constant.

$$I_C = h_{21} I_B + h_{22} V_{CE}$$

Input V-I Characteristics of CE Amplifier:

⇒ To draw the V-I characteristics of CE amplifier, output voltage is kept constant.



Input voltage of BJT is " $V_{BE}$ " and input current " $I_B$ " will be drawn when  $V_E$  is constant

⇒ The practical circuit connection to measure voltage  $V_{BE}$  and current  $I_B$  includes Voltmeter and Ammeter

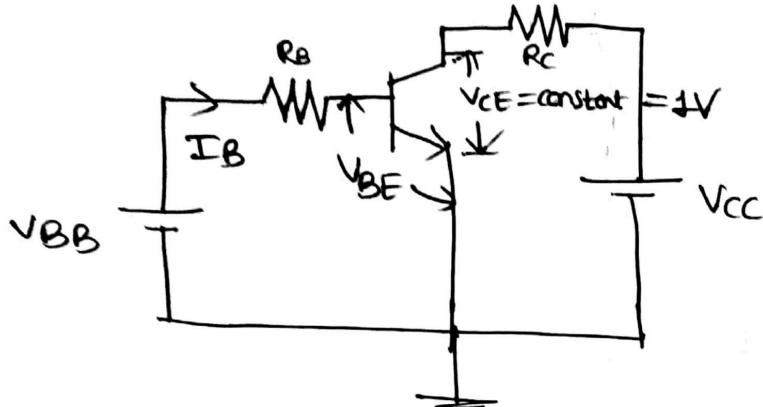
$$V_{BE} = h_{11} I_B + h_{12} V_{CE}$$

↓                    ↓                     $\downarrow$

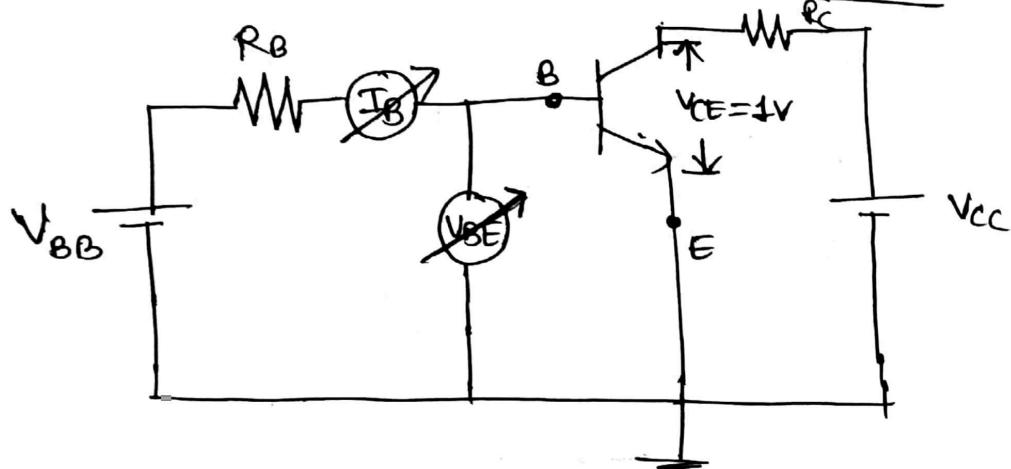
Variable            Variable            keep it as a  
constant to draw  $V-I$  plots

Case 11

When  $V_{CE} = 1V$  (Fixed or constant)



## Practical circuit to measure voltages & currents

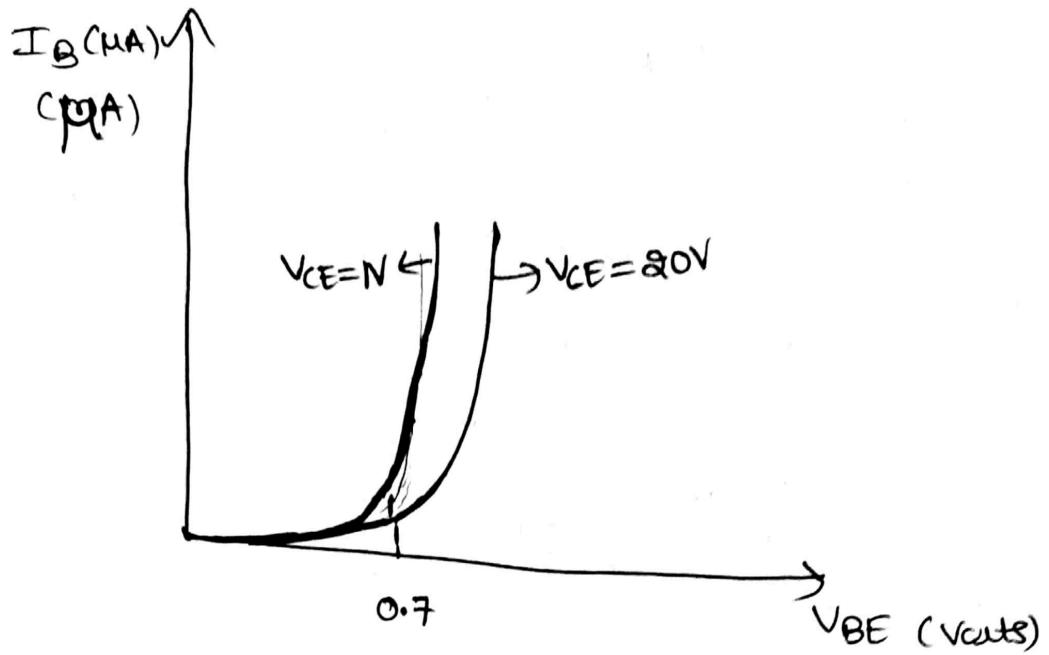


⇒ when we keep output voltage constant  $V_{CE} = 1V$  (or) (sometimes  $V_{CE} = 0V$ )

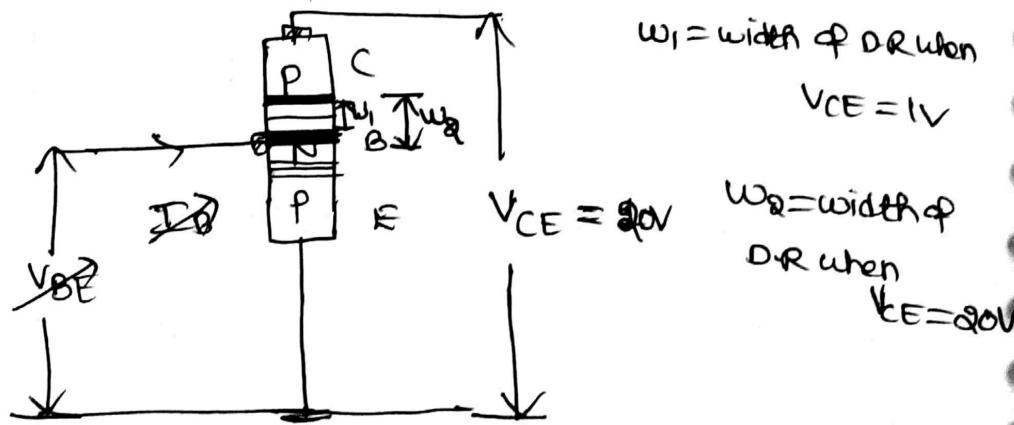
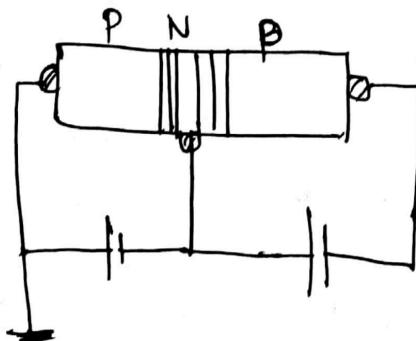
The input characteristics  $V_{BE}$  vs  $I_B$  are same as

PN diode VI characteristics. ie when we  $\uparrow$   $V_{BE}$ ,  $I_B$   $\uparrow$  exponentially after Cut-in Voltage. ( $0.7V$ ) for  $V_E$  = small

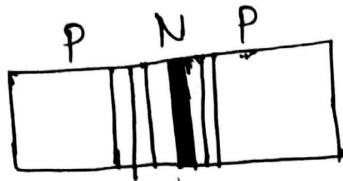
Values ( $V_{CE} = 0.1$  to 1)



Case (ii) For  $V_{CE} = 20V$



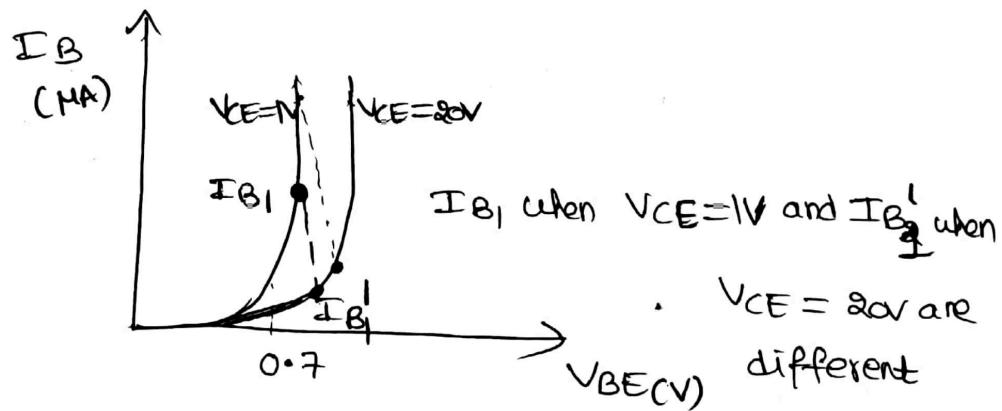
⇒ The depletion Region width  $\uparrow$  becoz of the Reverse bias Voltage  $V_{CE} = 20V$  ie " $w_1$ "  $\uparrow$  to " $w_2$ " and penetrates more into Base Region, so that width of the Base Region  $\downarrow$



$w_{B_1}$  = Effective Base width when  $V_{CE} = 1V$   
 $w_{B_2}$  = Effective Base width when  $V_{CE} = 20V$

⇒ Becoz of the Reverse Voltage  $V_{CE} = 20V$ , the width of the depletion Region  $\uparrow$  and Effective Base width  $\downarrow$ , This process is called "Base width modulation"(or) "Early Effect"

⇒ Because of the Early Effect, Base width  $\downarrow$ , so Recombination Region  $\downarrow$  then Recombination current ( $I_{RB}$ )  $\downarrow$



$I_B$   $\downarrow$  to  $I_B'$  for the same input  $V_{BE}$  becoz of the  $\uparrow$  in Reverse Voltage  $V_{CE}$  from 1 to 20V

Parameters to be obtained from the input V-I characteristic of CE:

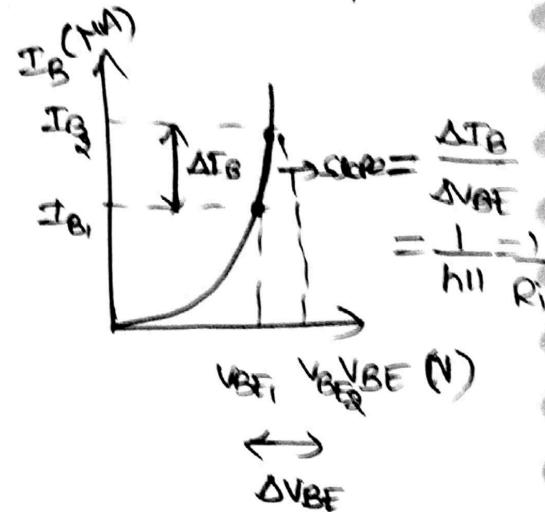
$$V_{BE} = h_{11} I_B + h_{12} V_{CE} \quad \text{--- constant}$$

$$\text{Input Resistance } (R_i) = h_{11} = \frac{V_{BE}}{I_B} \Big|_{V_{CE}=0}$$

$$h_{12} = \frac{V_{BE}}{V_{CE}} \Big|_{I_B=0} \quad \text{Reverse Voltage gain}$$

$$h_{11} = \frac{V_{BE}}{I_B} = \frac{\text{Input voltage}}{\text{Input current}} = \text{Input Resistance } R_i$$

$$R_i = h_{11} = \frac{V_{BE}}{I_B}$$



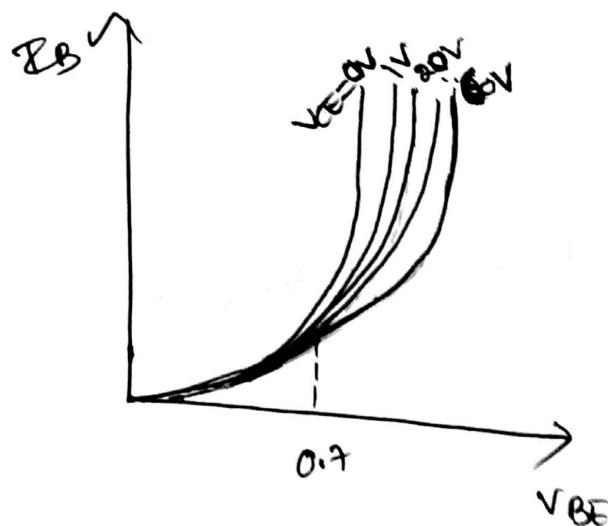
Slope of  $I_B$  vs  $V_{BE}$  is

$$\text{Slope} = \frac{\Delta I_B}{\Delta V_{BE}} = \frac{1}{h_{11}} = \frac{1}{R_i} = \frac{1}{\text{Input Resistance}}$$

∴ so

$$\text{Input Resistance } (R_i) = \frac{1}{\text{Slope of } I_B \text{ vs } V_{BE}}$$

Input VI char (CTS):



$$R_i = \frac{\Delta V_{BE}}{\Delta I_B} = h_{11}$$

## Output V-I characteristics of CE Amplifier:

⇒ output characteristics are drawn between output voltage ( $V_{CE}$ ) and output current ( $I_C$ )

From h-parameter model

$$I_C = h_{11} I_B + h_{22} V_{CE}$$

↓  
input current  
 $I_B$   
current  
constant

↓  
output voltage

while calculating drawing output V-I characteristics

Input current ( $I_B$ ) is constant

we know that in Common Emitter Configuration input current

$$I_C = \beta I_B + I_{CEO} \rightarrow @$$

we can also write this eq @ as below from the output current equation of common base circuit configuration

i.e. In CB qpcurrent

$$I_C = \alpha I_E + I_{CBO} \quad (\because I_E = I_B + I_C)$$

$$I_C = \alpha (I_B + I_C) + I_{CBO}$$

$$I_C(1 - \alpha) = \alpha I_B + I_{CBO}$$

$$I_C = \frac{\alpha}{1 - \alpha} I_B + \frac{1}{1 - \alpha} I_{CBO}$$

$$I_C = \left( \frac{\alpha}{1-\alpha} \right) I_B + \frac{1}{1-\alpha} I_{CBO}$$

We know that  $B = \frac{\alpha}{1-\alpha}$  then  $I_C$  becomes

$$I_C = B I_B + \frac{1}{1-\alpha} I_{CBO} \rightarrow \textcircled{b}$$

Compare equations  $\textcircled{a}$  and  $\textcircled{b}$  we can write

★ ★

$$I_{CEO} = \frac{1}{1-\alpha} I_{CBO}$$

So the QP current equation of common emitter configuration can also be represented in terms of ' $\alpha$ ' as

$$I_C = B I_B + \frac{1}{1-\alpha} I_{CBO} \rightarrow \textcircled{c}$$

(or)

$$I_C = B I_B + I_{CEO} \rightarrow \textcircled{d}$$

⇒ To draw the output characteristics, the input current  $I_B$  is constant

From equation  $\textcircled{d}$

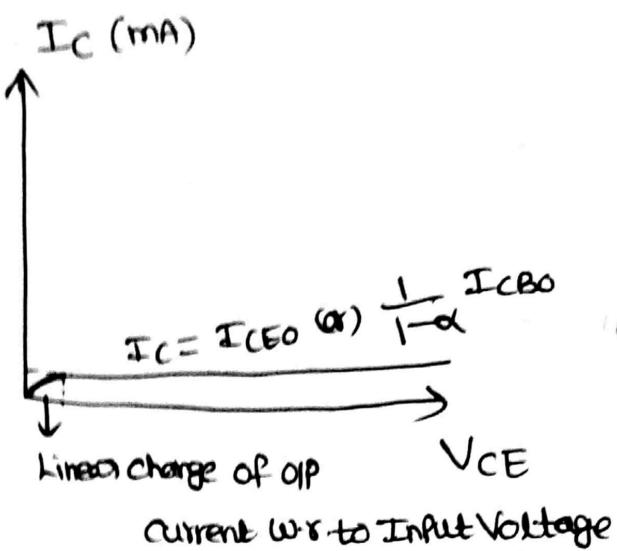
$$I_C = I_{CEO} \mid I_B \neq 0$$

(or)

From eq  $\textcircled{c}$   $I_C = \frac{I_{CBO}}{1-\alpha} \mid I_B = 0$

Case(i)

when  $I_B = 0$



Case(ii)

when  $I_B \neq 0$  ( $I_B = 10\text{mA}, 20\text{mA}, \dots$ )

- ⇒ If Input current  $I_B = 10\text{mA}$  (or a non-zero value), the output varies in accordance with the input ie it is a function of input current and output voltage
- ⇒  $I_C$  varies linearly with output voltage  $V_{CE}$  and it reaches to a maximum value, ie called saturation  $\Rightarrow$  current  $I_{CEO}$  when  $I_B = 0$  (Base is open).
- ⇒ when  $I_B \neq 0$  ie when  $I_B = 10\text{mA}, 20\text{mA}, \dots$ , then the output current  $I_C$  varies linearly with voltage  $V_{CE}$ .

$$I_C = \beta I_B + I_{CEO}$$

& Before reaching the saturation

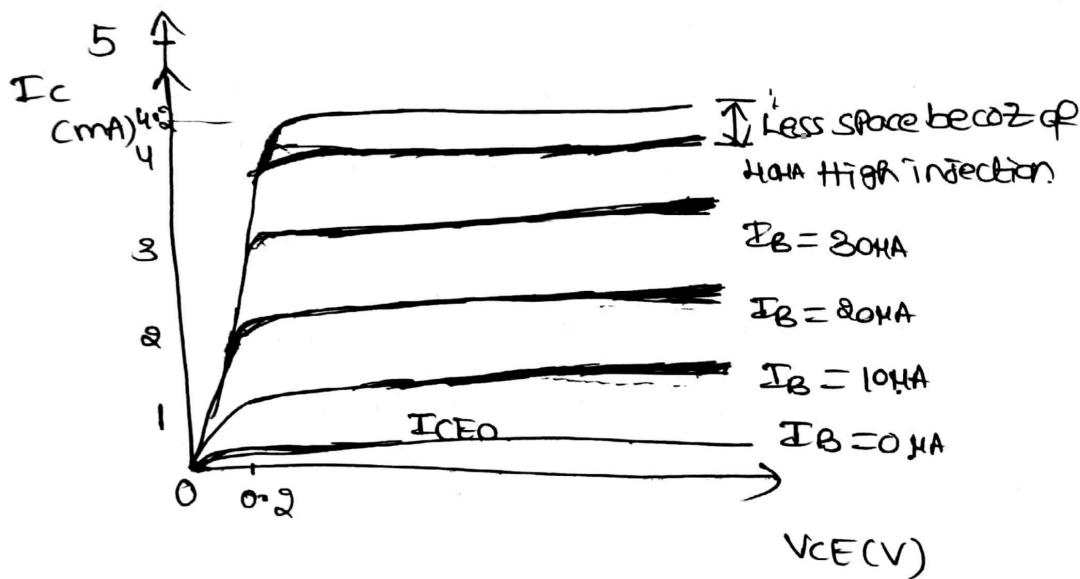
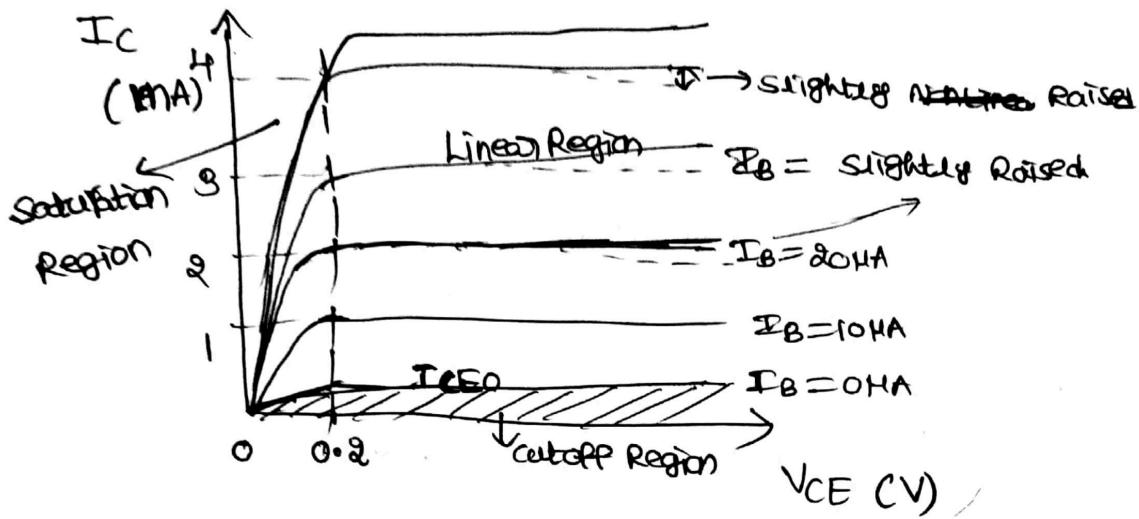
current  $I_C$  varies linearly with voltage  $V_{CE}$ .

For further values of " $I_B = 20\text{mA}, \dots$ ", the value of  $I_C$

↑ with input  $I_B$  and  $I_C$  increases linearly with  $V_{CE}$  before reaching saturation

$$I_C \uparrow = \beta I_B \uparrow + I_{CEO}$$

$I_C \uparrow$  linear with  $V_{CE}$  before reaching saturation



⇒ As the  $I_B \uparrow$ , the injection into Base Region  $\uparrow$ , i.e., due to that gain ( $\beta$ )  $\downarrow$

ie 
$$\left( \beta = \frac{I_C}{I_B} \right) \downarrow$$

$\downarrow \beta \text{ if we } \uparrow I_B$

$$\text{gain} = \beta = \frac{I_C}{I_B}$$

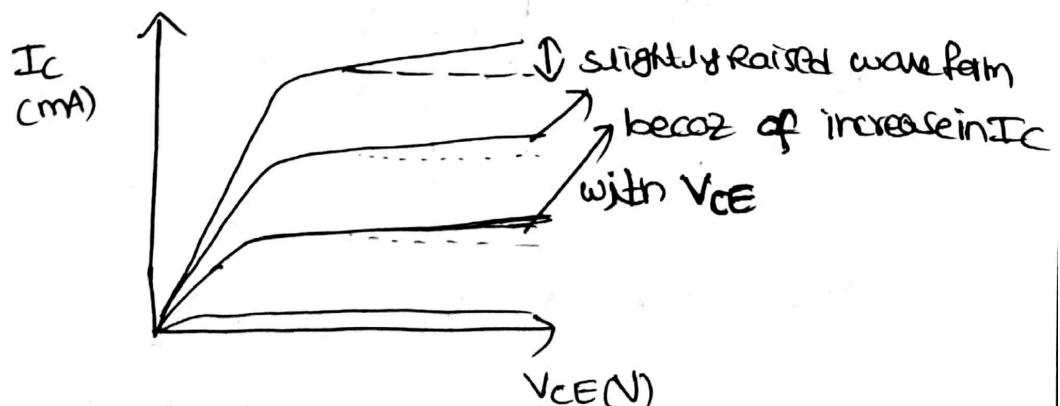
$\beta \Rightarrow$  can also be written as

$$\beta = \frac{\Delta I_C}{\Delta I_B}$$

⇒ Becoz of the increase in  $I_B$ , the Recombination also increases, Becoz of that Recombination current output current  $I_C \uparrow$  so gain  $\downarrow$  ie ( $\beta \downarrow$ )

⇒ The lines which are shown as slightly raised are not Straight Lines becoz As we are  $\uparrow V_{CE}$ , the Depletion Region  $\uparrow$  and penetrates into Base Region which reduces the Effective Base Width called as Base width modulation (or) Early Effect

⇒ Due to the Early Effect  $I_C \uparrow$  becoz of the Reduction of Recombination current with respect to "V<sub>CE</sub>". So as V<sub>CE</sub>  $\uparrow$  the collector current I<sub>C</sub>  $\uparrow$ , becoz of the Early effect. So the graphs are not straight lines, they are just slightly raised with respect to V<sub>CE</sub>



⇒ There are three Regions of operation in output characteristics of CE

- ① Cutoff Region
- ② Saturation Region
- ③ Linear Region



### Cutoff Region:

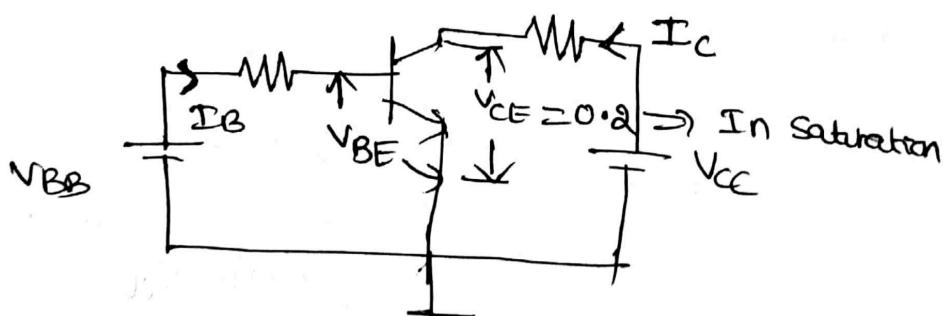
⇒ The Region below  $I_{CEQ}$  is called cutoff Region because the (or)  $I_B = 0$  Current is nearly zero Amperes because of the Reverse Bias Condition of Emitter Base junction & Collector Base junction

⇒ The Region below  $I_B = 0$  is cutoff Region, To get  $I_B = 0$  we have to provide Reverse bias at  $\mathcal{J}_E$  which leads to  $\mathcal{J}_E, \mathcal{J}_C = R \cdot B$

### Saturation Region:

⇒ The Region before  $V_{CE} = 0.2V$  is called saturation Region, BeCoz both the junctions are in Forward bias condition

In CE  $\mathcal{J}_E = F \cdot B$ ,  $\mathcal{J}_C = R \cdot B$

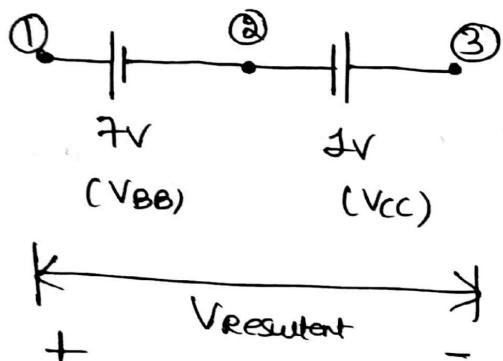
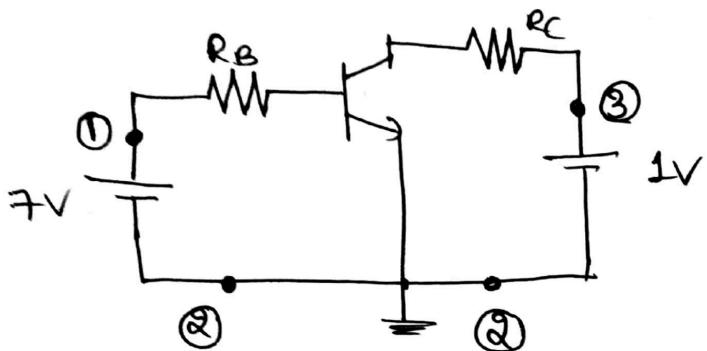


$V_{BE} = F \cdot B$  &  $V_{CE} = 0.2$  V across  $\mathcal{J}_C$  which is very negligible R.B Voltage

For suppose  $V_{BE} = 5V$  (to give  $V_{BE} = 5V$ ,  $V_{BB}$  must be  $> 5V$ )

so let us assume  $V_{BB} = 7V$  & to provide  $V_{CE} = 0.2V$

$V_{CC}$  must be  $> 0.2V$ , so consider  $V_{CC} = 1V$  (or) around  $1V$



$$-V_{resultant} + 7V - 1V = 0$$

$$V_{resultant} = 6V \approx 7V \quad (V_{BB} \text{ is dominating } V_{CC})$$

$\Rightarrow V_{BB}$  is dominating  $\Rightarrow V_{CE}$  (when it is very small only) then

it seems that  $V_{BB}$  is present at " $\text{f}_C$ " which is a forward bias condition so both  $\text{B}_E$  &  $\text{f}_C$  forward biased  
so the region behind  $0.2V$  is saturation region

( $0.2V$  is the practically observed value obtained from  $V_{CE(sat)}$ )

$$V_{CE(\text{sat})} = 0.2V \Rightarrow \text{for silicon}$$

$$V_{CE(\text{sat})} = 0.1V \Rightarrow \text{for Germanium}$$

The condition for saturation is

$$I_{B(\text{min})} \geq \frac{I_C}{\beta}$$

In Linear Region (or) Active Region the equation  $I_C = \beta I_B$

i.e  $I_C$  is greater than " $I_B$ " or equal to  $I_B$

$$\text{since } I_C = \beta I_B + I_{CE0}$$

$$I_C \geq \beta I_B$$

But In saturation Region that condition will become

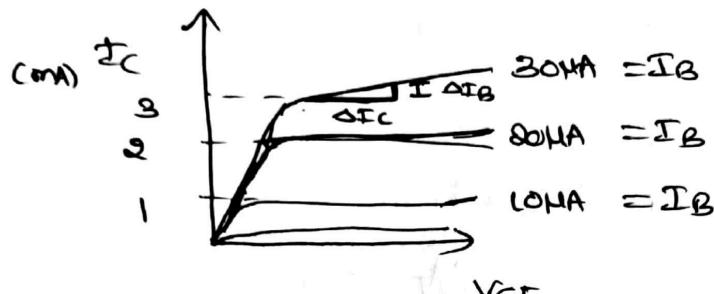
Reverse i.e  $I_C \leq \beta I_B$  (where  $I_B = I_{B(\text{min})}$ )

$$\Rightarrow I_C \leq \beta I_{B(\text{min})}$$

$$I_{B(\text{min})} \geq \frac{I_C}{\beta} \Rightarrow \text{saturation Region condition}$$

## Linear Region (or) Active Region:-

⇒ The Region after  $0.2V$  is a Linear Region. It is called Linear Region because output ( $I_C$ ) varies linearly in accordance with the input ( $I_B$ )



As we are  $\uparrow I_B$ ,  $I_C \uparrow$  linearly with a slope called  $B$  (or) gain

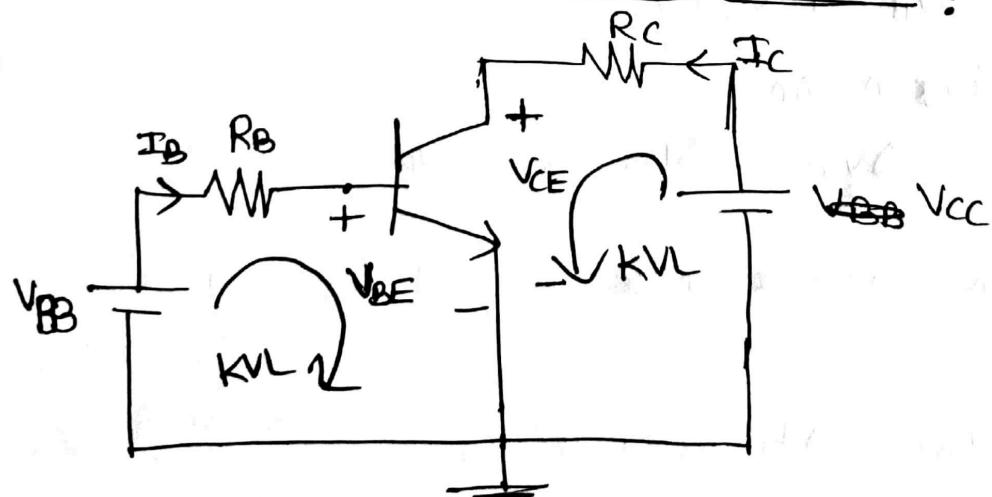
$$B = \frac{\Delta I_C}{\Delta I_B}$$

$$I_C = B I_B$$

$\Downarrow$   
 $y = mx + c$  form)

⇒ we are also calling this Region as Active Region because the transistor acts as an Amplifier in this Region

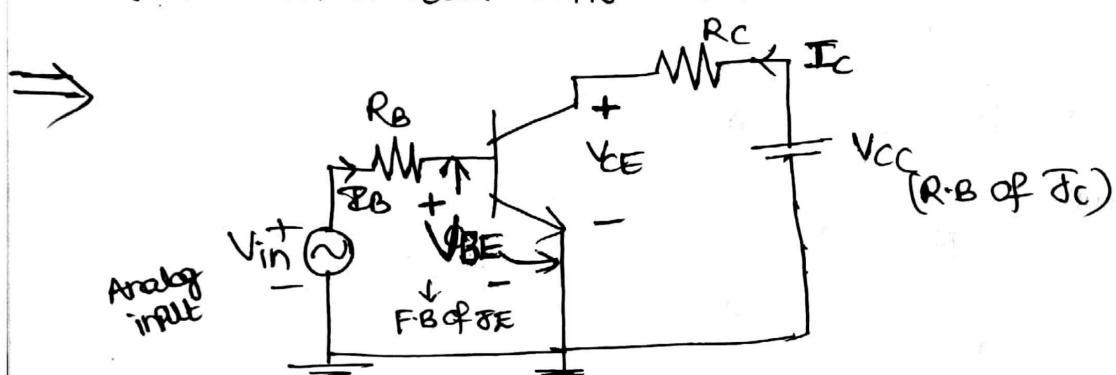
\*\*\*\*\*  $V_{BE}$   
How the transistor acts as an Amplifier?



⇒ This is the Common Emitter Amplifier with 'DC' Voltages (Biasing)

⇒ But Amplifier is the one which amplifies the Analog input (Human voice, music etc.,.)  $\Rightarrow$  DC is not an input, it is just a biasing voltage which is used to set the Q-point. (V<sub>CE</sub>, I<sub>C</sub>) to make the transistor to act as an Amplifier.

⇒ Amplifier amplifies the input Analog signal, so the input to be given is Analog input which is applied across the Emitter & Baseterminals for common emitter configuration.



Apply KVL at top side

$$-V_{in} + I_B R_B + V_{BE} = 0$$

$$V_{in} = I_B R_B + V_{BE}$$

Change in V<sub>in</sub>

$$\Delta V_{in} = \Delta I_B R_B + \Delta V_{BE}$$

$V_{BE}$  = Base to emitter DC voltage to overcome Barrier

Potential = 0.7 V

(F.B of  $\beta_E$ )

$$\Delta V_{in} = \Delta I_B R_B + \Delta (0.7)$$

$$\Delta V_{in} = \Delta I_B R_B + 0V$$

$$\Delta V_{in} = \Delta I_B R_B$$

$$\Delta V_{in} = \Delta I_B R_B \rightarrow \textcircled{A}$$

Apply KVL at output side

$$-V_{cc} + I_C R_C + V_{CE} = 0$$

$$V_{cc} = I_C R_C + V_{CE}$$

$$\Delta V_{cc} = \Delta I_C R_C + \Delta V_{CE}$$

$$0 = \Delta I_C R_C + \Delta V_{CE}$$

$$\Delta V_{CE} = -\Delta I_C R_C$$

(or)

$$\Delta V_o = -\Delta I_C R_C \rightarrow \textcircled{B}$$

$$\frac{\textcircled{B}}{\textcircled{A}} = \frac{\Delta V_o}{\Delta V_{in}} = \frac{-\Delta I_C R_C}{\Delta I_B R_B}$$

$$\Rightarrow A_V = \text{Voltage gain} = \frac{\Delta V_o}{\Delta V_{in}} = -\frac{\Delta I_C R_C}{\Delta I_B R_B}$$

So,  $A_V = -B \frac{R_C}{R_B}$

$$\therefore B = \frac{I_C}{I_B} \text{ (or) } \frac{\Delta I_C}{\Delta I_B}$$

$$\frac{\Delta V_o}{\Delta V_{in}} = -B \frac{R_C}{R_B}$$

$\Delta V_o = \left( -B \frac{R_C}{R_B} \right) \Delta V_{in}$

$\Rightarrow$  Output varies linearly with respect to Input in Linear Region, ie when  $\beta_E = R_B$

$$\beta_E = R_B$$

$\Delta V_o \Rightarrow$  change in output

$\Delta V_{in} \Rightarrow$  change in input

output is  $180^\circ$  phase shift with input  $\rightarrow$  gain  $\Rightarrow$  so amplified output

$$\boxed{\Delta V_o = \left( -\frac{\beta R_C}{R_B} \right) \Delta V_{in}} \rightarrow \textcircled{C}$$

$180^\circ$  phase shift

★ ★ Why CE Amplifier is having  $180^\circ$  phase shift:

$$\Delta V_o = -\frac{\beta R_C}{R_B} \Delta V_{in}$$

The output of the amplifier  $\Delta V_o$  is out of phase from the above equation.

We know that the gain  ~~$\beta \approx 100$~~   $\beta \approx 50-200$

(For high frequency low power BJT)

$$\because \stackrel{\text{wkt}}{\alpha = 0.98} \quad \beta = \frac{\alpha}{1-\alpha} \Rightarrow \frac{0.98}{1-0.98} \Rightarrow \frac{0.98}{0.02} \Rightarrow 49 \quad \stackrel{\beta \approx 1000}{\approx 50}$$

so From eqn  $\textcircled{C}$

$$\Delta V_o = -50 \times \frac{R_C}{R_B} \Delta V_{in}$$

(minimum  $\beta$ )

$$\text{Voltage Gain } A_v = \frac{\Delta V_o}{\Delta V_{in}} = -50 \times \frac{R_C}{R_B}$$

$$\text{Gain} = A_v = -50 \times \frac{R_C}{R_B}$$

★ Gain with  $180^\circ$  phase shift has  
been produced in CE amplifier

Hence CE amplifier acts as an  
Amplifier

⇒ Similarly CB & CC also acts as amplifiers

Common Base  $\xrightarrow{\text{acts as}}$  Voltage Amplifier

Common Emitter  $\xrightarrow{\hspace{1cm}}$  Power Amplifier

★ Common Collector  $\xrightarrow{\hspace{1cm}}$  Current Amplifier  
(Emitter follower)

## Common Base Configurations -

Base is common to both i/p & o/p, so called common Base Configuration

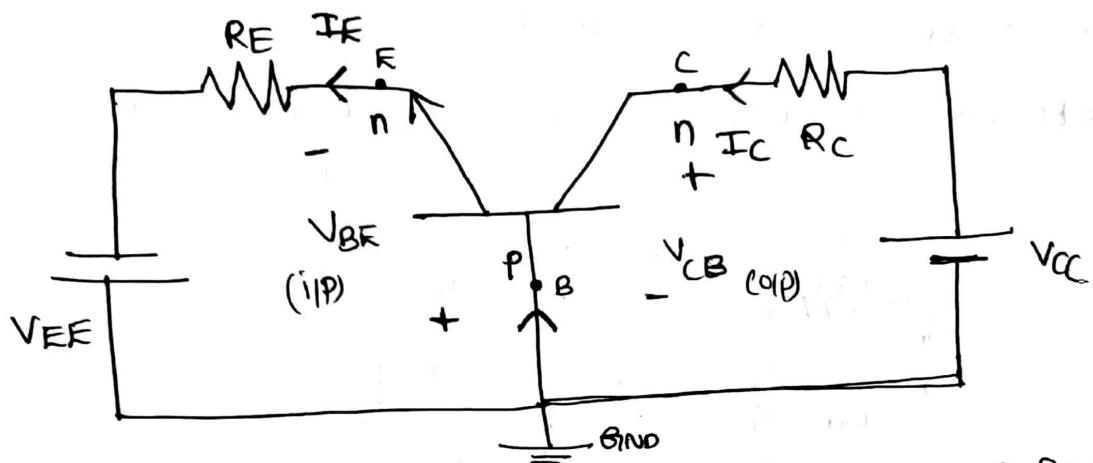


Fig @ Common Base Configuration CKT

- ⇒  $R_E$  = input Resistance,  $R_C$  = o/p Resistance
- ⇒ Base is grounded & is common to both Emitter (i/p), collector (o/p).
- ⇒ From KCL for the above CKT

$$I_E = I_B + I_C$$

- ⇒ The gain (or) DC gain of the CKT configuration is " $\alpha$ "

$$\alpha = \frac{\text{output of the collectorie (I}_C\text{)}}{\text{input current I}_E\text{}}$$

$$\alpha = \frac{I_C}{I_E} \quad (\text{or}) \quad \alpha \simeq \frac{I_C}{I_E} \frac{\frac{D_I C}{I_E}}{\frac{D_I E}{I_E}}$$

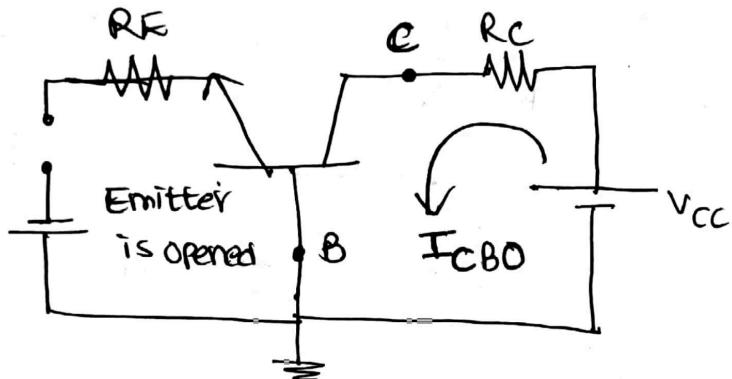
wkt

$$I_C = I_{pc} + I_{Co}$$

$$I_C = \alpha I_E + I_{Co} \quad (\text{since } \frac{I_{pc}}{I_E} = \alpha)$$

$I_{Co}$  :- Reverse saturation current, which is measured in between collector & base, when emitter is opened

$\downarrow$  (Cir p)



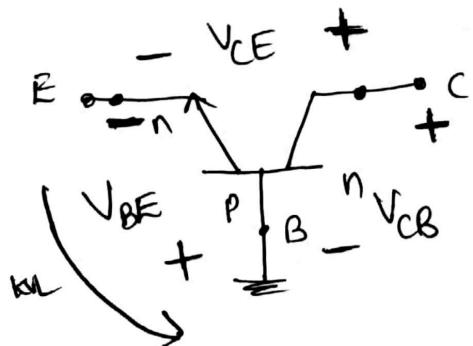
$$I_C = I_{Co} = I_{CBO}$$

when  $I_E = 0$ , emitter is opened

When we will input  $I_E$ , the output current equation is

$$I_C = \alpha I_E + I_{CBO}$$

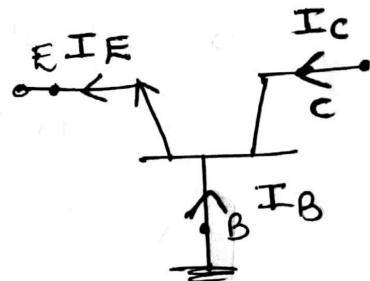
KVL in CB



$$-V_{BE} - V_{CB} + V_{CE} = 0$$

$$V_{CE} = V_{BE} + V_{CB}$$

KCL in CB



$$I_E = I_B + I_C$$

## VI Characteristics of CB Amplifier:

h-Parameters for CB Amplifier is

$$V_1 = h_{11} I_1 + h_{12} V_2$$

$V_1, V_2$  = ip & oip voltage

$$I_2 = h_{21} I_1 + h_{22} V_2$$

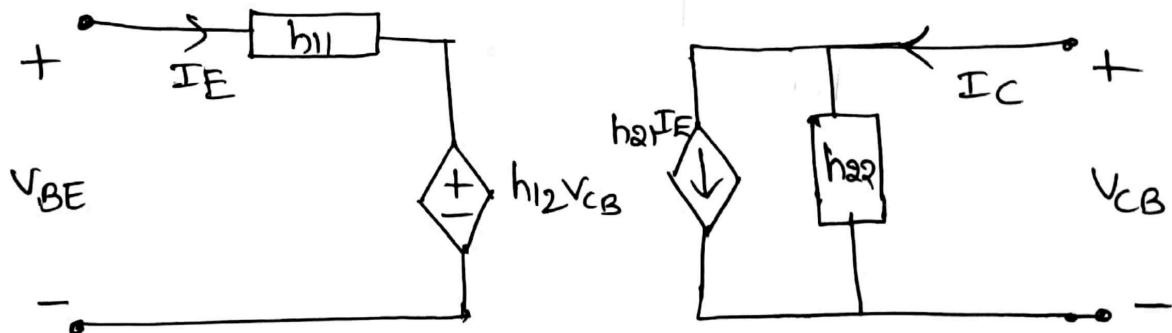
$I_1, I_2$  = ip & oip currents

$$V_1 = V_{BE}, \quad V_2 = V_{CB} : \quad I_1 = I_E, \quad I_2 = I_C$$

so

$$V_{BE} = h_{11} I_E + h_{12} V_{CB}$$

$$I_C = h_{21} I_E + h_{22} V_{CB}$$



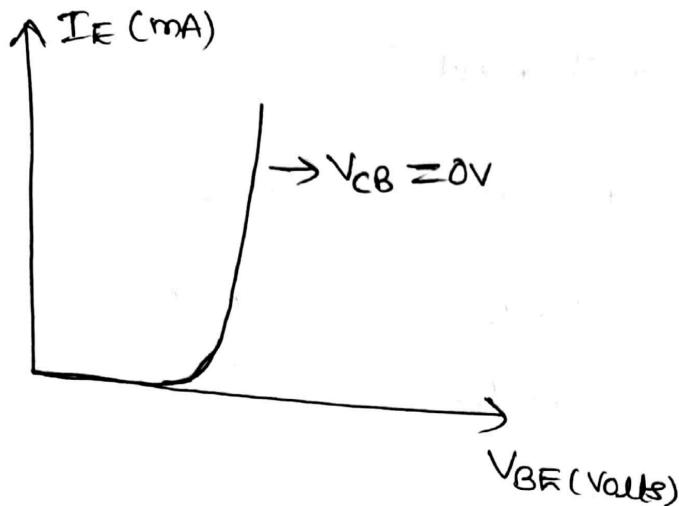
## Input V-I Characteristics of CB Configuration:

Graph between  $V_{BE}$  and  $I_E$  when  $V_{CB}$  is constant

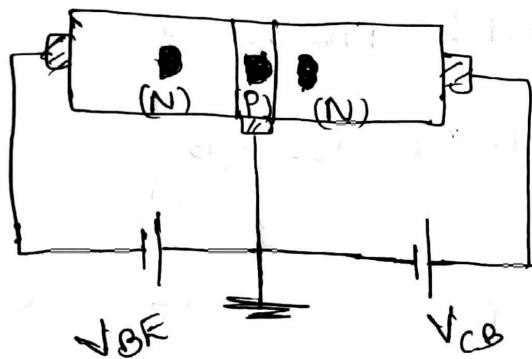
$$V_{BE} = h_{11} I_E + h_{12} \text{ (V}_CB \text{ constant)}$$

Case(i) when  $V_{CB} = 0V$

$I_E$  varies with  $V_{BE}$  same as in PN diode after 0.7V



Case(ii) :- when  $V_{CB} = 1V/10V$  --.



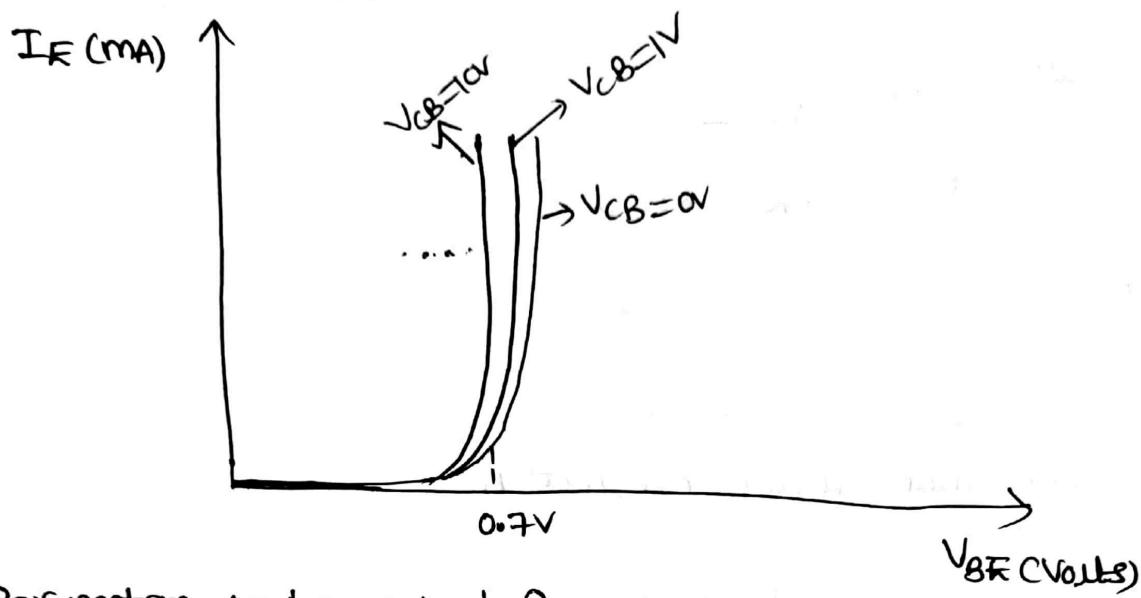
⇒ When  $V_{CB}$  is given a non-zero value, then the Reverse Bias across the Collector-Base junction increases, then width of the depletion Region increases which causes reduction in Base width

⇒ The Recombination current  $\downarrow$  because of the reduction in Base width, ie the concentration of "charge carriers in Base Region"  $\downarrow$  so charge-flow in Base Region  $\downarrow$  to time  $\downarrow$  then  $I_B \downarrow$ .

\* The concentration of charge carriers  $\uparrow$ , compared to <sup>in</sup> high width of Base, Before early effect, Because of the reduction in Base width, the base carries less no of charge carriers than earlier so the more charge carriers remained in emitter Region which causes the increase in current in emitter Region ( $I_E \uparrow$ )

→ when  $V_{CB} \uparrow$ , depletion region width  $\uparrow$ , effective base width  $\downarrow$

$I_B \downarrow$  then  $I_E \uparrow$



Parameters to be obtained from i/pcls

$$\frac{V_{BE}}{I_E} = h_{11} = R_i = \text{Input Resistance}$$

$$\frac{V_{BE}}{V_{CB}} = h_{12} = \text{Reverse voltage gain}$$

Output V-I characteristics of CB configuration

The output V-I cls will be obtained when input current  $I_E$  is constant

$$I_C = h_{21} \frac{I_E}{J} + h_{22} \cdot V_B$$

input current constant.

Output characteristics are drawn between output voltage and output current.

$$I_C = \alpha I_E + I_{CBO} \rightarrow \text{④ output current equation of CB amplifier}$$

Case(i) : When  $I_E = 0$

$$I_C = \alpha I_E + I_{CBO}$$

$$I_E = 0, I_C = 0 + I_{CBO}$$

$$I_C = I_{CBO}$$

From common emitter configuration

$$I_C = \beta I_B + I_{CEO}$$

$$I_C = \beta I_B + \frac{1}{1-\alpha} I_{CBO}$$

$$I_{CEO} = \frac{1}{1-\alpha} I_{CBO}$$

$$I_{CEO} = \frac{1}{(1-\alpha)} (I_{CBO})$$

$$I_{CEO} = (1+\beta) I_{CBO}$$

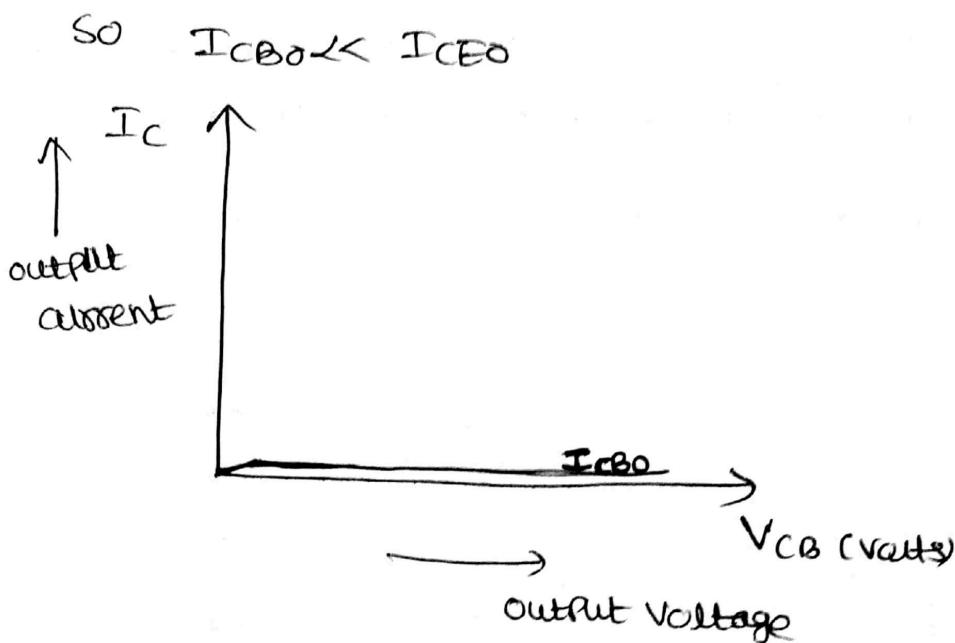
$$\text{where } \frac{1}{1-\alpha} = 1+\beta = 1 + \frac{\alpha}{1-\alpha} = \frac{1-\alpha+\alpha}{1-\alpha} = \frac{1}{1-\alpha}$$

$$I_{CEO} = (1+\beta) I_{CBO} \rightarrow \text{In CE}$$

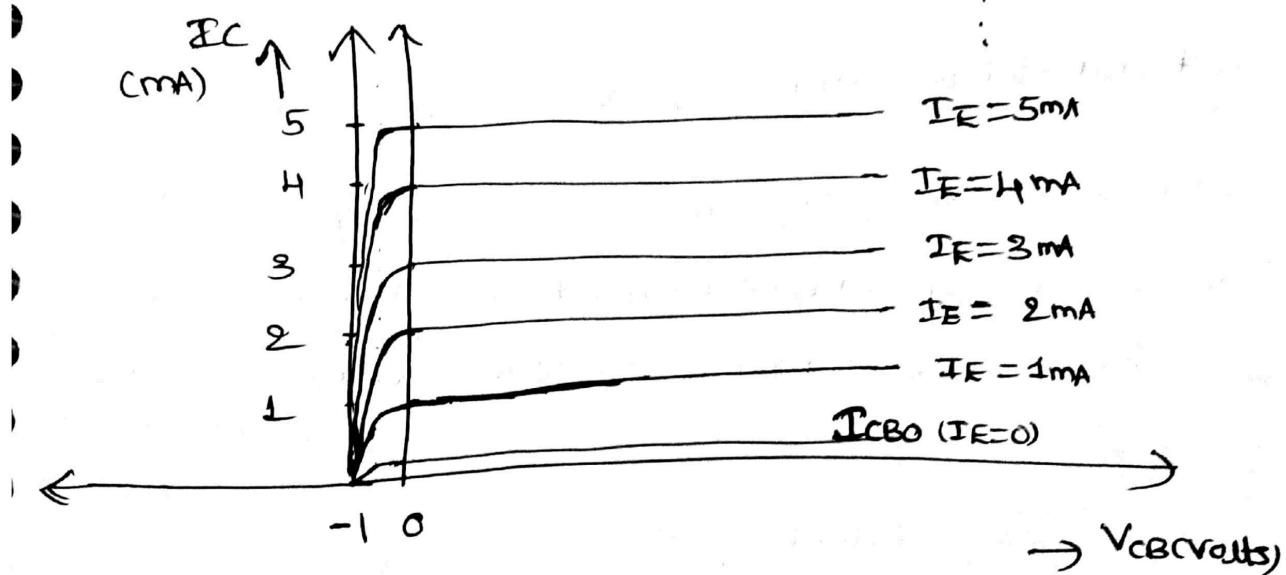
so

$$I_{CEO} > I_{CBO}$$

Reverse saturation current in CE is greater than CB



Case(ii) when  $I_E \neq 0$ ,  $1\text{mA}, 2\text{mA}, \dots$



$\Rightarrow$  when  $I_E$  is a non zero value, the collector current varies linearly with  $I_E$ , because the gain " $\alpha$ " in common base configuration is almost 1 or 0.995 to 0.998 practically ie

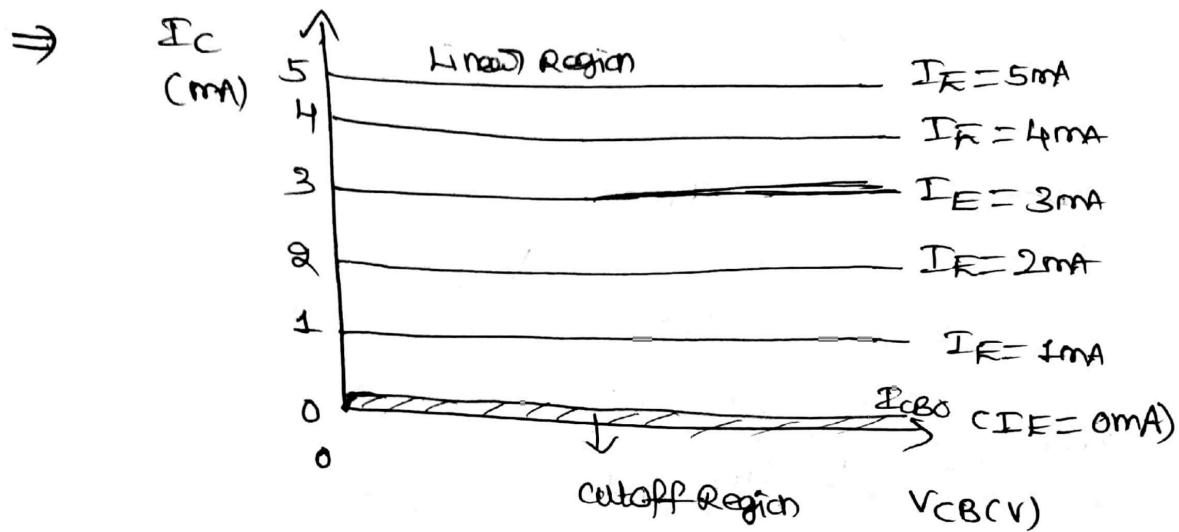
$$\alpha \approx 1 \text{ or } \alpha = 0.995 - 0.998$$

so

$I_C \approx I_E$

⇒ As  $\alpha$  is almost '1'  $I_C$  is almost equal to "I<sub>E</sub>" when it is operated in Active mode (Forward active mode):

$\mathcal{F}_E := F\cdot B$ ,  $\mathcal{F}_C := R\cdot B$



Output characteristics when  $-V < V_{CB} < 0$  ? :

⇒ when  $V_{CB} = -V$  value, the  $\mathcal{F}_C \Rightarrow$  collector base junction is also in forward biased condition, we know that the  $\mathcal{F}_E \Rightarrow$  Emitter base junction is already in forward bias condition so, now

$\mathcal{F}_E = \text{Forward Bias}$

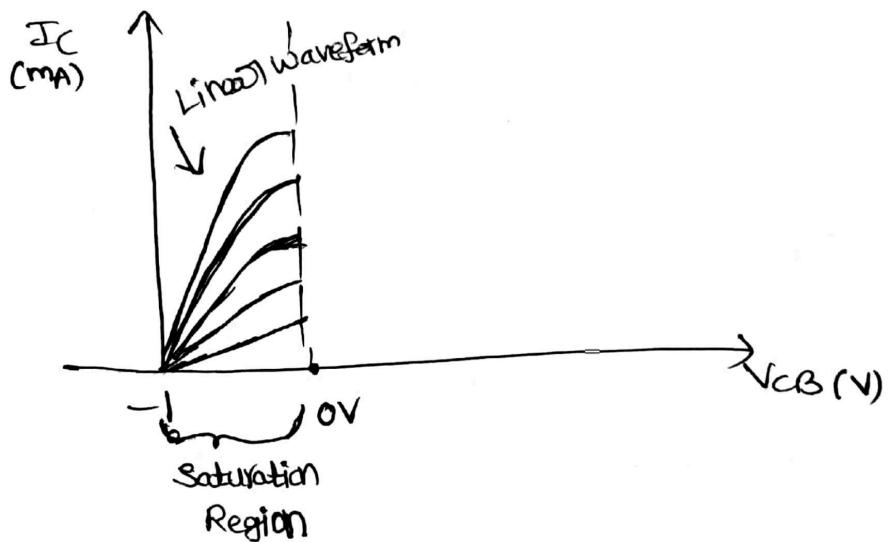
$\mathcal{F}_C = \text{Forward Bias}$

If both the junctions are in forward bias condition, then the collector current  $I_C$  is not a function of  $I_E$

$$I_C \neq f(I_E)$$

In saturation region  $I_C$  &  $I_E$  varies independently

- ⇒  $I_C$  varies linearly with  $V_{CB}$  and  $I_E$  varies linearly with  $V_{BE}$ , but the variations are not dependent
- so in O/P V-I characteristics,  $I_C$  varies linearly with  $V_{CB}$  but does not depend on " $I_E$ "



#### ⇒ Regions of Operation:-

- Cutoff Region:-
- ⇒ The Region below  $I_E = 0\text{mA}$  is called Cutoff Region
- ⇒ To get  $I_E = 0\text{mA}$ ,  $V_{BE} = 0\text{V}$ , which makes the emitter-base junction Reverse Bias. As we already know that  $J_C$  is in Reverse bias condition, so both the junctions are in Reverse bias condition and the transistor is said to be in Cutoff Region

#### Saturation Region:-

- ⇒ The  $J_E$  is already in R.B condition, If we apply  $V_{CB}$  -ve, then  $J_E$  is in R.B

- ⇒ we know that, we are operating the transistor in forward active mode to make it to act as a transistor so  $\beta_E$  is in forward Bias condition and If  $V_{CB}$  is  $-ve$  ie  $V_{CB} < 0V$ , then  $\beta_C$  is also in forward Bias condition
- ⇒ when Both the Junctions are in Forward Bias Condition, then the transistor is said to be in saturation Region.

### Active Region:

- ⇒ when ~~Both~~  $\beta_E = F.B$ ,  $\beta_C = R.B$ , then the transistor acts as an Amplifier and the Region of operation is Active Region (or) Linear Region
- ⇒ In this Region input current ( $I_E$ ) and output current ( $I_C$ ) are in Linear Relation ie output current ( $I_C$ ) varies Linearly with input current ( $I_E$ ) with a slope " $\alpha$ " also called gain

$$I_C = f(I_E)$$

$$I_C \propto \alpha I_E \Rightarrow y = mx \text{ form}$$

$$y = ap, m = \text{slope}, x = \text{input}$$

Linear Region means, the Region where output current varies Linearly with input current. Then we can use the transistor as an Amplifier in this Region

⇒ The lines in Active Region, ie the output V-I plots of CB

As in Active Region are STRAIGHT LINES, because the gain  $\alpha$  is not high, it is almost equal to "1", so we will get straight lines.

But in CE configuration, the V-I plots of CE amplifier are not straight lines because of the gain  $\beta = \frac{I_C}{I_B}$ , since " $\beta$ " is high, the lines are not straight lines  $\Rightarrow \beta$  is 50 to 400 and  $\alpha$  is 0.995 to 0.998 practically

★★  
Note:

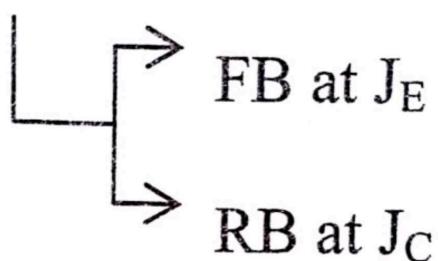
⇒ h-Parameters are valid in Active Region (or) Linear Region only.

## TRANSISTOR BIASING:

- The basic function of a transistor is to do amplification. The process of raising the strength of a weak signal without any change in its shape is known as faithful amplification.
  - The proper maintenance of zero signal collector current ( $I_{CQ}$ ) and collector-emitter voltage ( $V_{CEQ}$ ) in transistor circuit during the passage of AC signal is considered as 'biasing'.
  - When a transistor is not properly biased, it provides unfaithful amplification and produces distortion in the output signal.
  - In order to produce distortion-free output in amplifier circuits, the supply voltages and the passive elements in the circuit must be suitably chosen.
  - The supply voltage and resistances in a transistor biasing circuit establish a set of DC voltage  $V_{CEQ}$  and current  $I_{CQ}$  to operate the transistor at a desired point called operating point or Quiescent point or Q-point in the active region.
-

## Requirements of Biasing

### 1. Active region of operation



### 2. Operating point (Q-pt) establishment *Q-Point:*

A point in the active region at which, a BJT provides faithful amplification against the weak input signal applied and delivers undistorted output signal is called as operating point or Quiescent point or Q point.

---

**Note 2:** In an amplifier circuit, if the operating point is established near to the cut off region ( $Q_2$  in fig.6) some portion of the amplified output signal will be clipped off in the negative half cycle i.e certain amount of information may be lost in the output signal.

**Note 3:** In an amplifier circuit if the operating point is established at the middle of DC load line or at the centre of active region ( $Q$  in fig.6), the amplifier provides faithful amplification against the small or weak AC input signal applied and delivers undistorted output signal.

### 3. Q-point Stability:

There are two factors which are responsible for the instability of operating point. They are:

- The transistor parameters are temperature dependent.
- When a transistor is replaced by another transistor of same type, there is a wide spread in the values of transistor parameters due to manufacturing errors.

*Therefore stabilization of the Q-point is necessary against*

- (a) Variations of minority carrier current,  $I_{CO}$  with temperature ( $I_C \rightarrow I_{CO} \rightarrow$  Minority carrier concentration  $\rightarrow$  Temp).
- (b) Variations of  $\beta$  in case of replacement of transistors ( $I_c \rightarrow \beta \rightarrow \alpha \rightarrow$  Base width  $\rightarrow$  manufacturing errors).
- (c) Variations of junction voltage of the transistor,  $V_{BE}$  with temperature ( $I_c \rightarrow I_B \rightarrow V_{BE} \rightarrow$  Temp).

### Temperature dependence of $I_C$ :

- The instability of  $I_C$  is principally caused by the following three sources:
- The  $I_{CO}$  doubles for every  $10^\circ C$  rise in temperature.
- Increase of  $\beta$  with increase of temperature.
- The  $V_{BE}$  decreases about  $2.5\text{mV}$  per  $^\circ C$  increase in temperature.

#### 4. Stability Factor:

It is the measure of the stability of operating point in a transistor amplifier circuit.

##### *(a) Stability factor, S:*

The variation of collector current with the variations in reverse saturation current  $I_{CO}$  in a BJT at constant  $\beta$  and  $V_{BE}$  is considered as stability factor, S.

$$S = \left( \frac{\partial I_c}{\partial I_{co}} \right) \text{ with } \beta \text{ and } V_{BE} \text{ Constant}$$

##### *(b) Stability factor, $S^1$ :*

The variation of  $I_C$  with the variation in  $\beta$  at a constant  $I_{CO}$  and  $V_{BE}$  is considered as stability factor  $S^1$ .

$$S^1 = \left( \frac{\partial I_c}{\partial \beta} \right) \text{ with } I_{CO} \text{ and } V_{BE} \text{ constant.}$$

##### *(c) Stability factor $S^{11}$ :*

The variation of  $I_C$  with the variations in  $V_{BE}$  at a constant  $I_{CO}$  and  $\beta$  is considered as  $S^{11}$ .

$$S^{11} = \left( \frac{\partial I_c}{\partial V_{BE}} \right) \text{ with } I_{CO} \text{ and } \beta \text{ Constant.}$$

### ***Derivation of Stability Factor (S):***

Consider the collector current equation of a BJT in CE configuration:

$$I_c = \beta I_B + (1+\beta) I_{CO} \text{ ----- (1)}$$

Differentiating equation (1) w.r.t.  $I_c$

$$1 = \beta \frac{\partial I_B}{\partial I_c} + (1 + \beta) \frac{\partial I_{CO}}{\partial I_c}$$

$$\frac{\partial I_{CO}}{\partial I_c} = \frac{1 - \beta \left( \frac{\partial I_B}{\partial I_c} \right)}{(1 + \beta)}$$

$$\Rightarrow \frac{\partial I_c}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \frac{\partial I_B}{\partial I_c}}$$

$$\therefore S = \frac{\partial I_c}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \left[ \frac{\partial I_B}{\partial I_c} \right]} \text{ ----- (2)}$$

## I | Biasing Circuits

### 1. Fixed Bias :

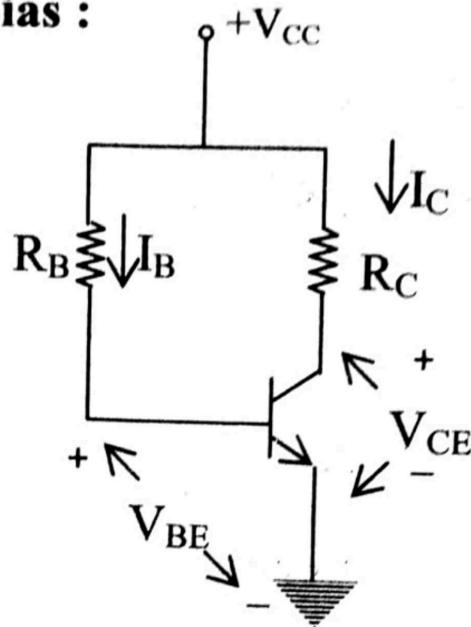


Figure.7

### *Q- Point establishment:*

#### Step 1: KVL for input section

$$V_{cc} - I_B R_B - V_{BE} = 0 \quad \dots \dots (1)$$

$$I_B = \frac{V_{cc} - V_{BE}}{R_B} \quad \dots \dots (2)$$

$$\therefore I_{CQ} = \beta I_B = \beta \left[ \frac{V_{cc} - V_{BE}}{R_B} \right] \quad \dots \dots (3)$$

#### Step 2: KVL for output section

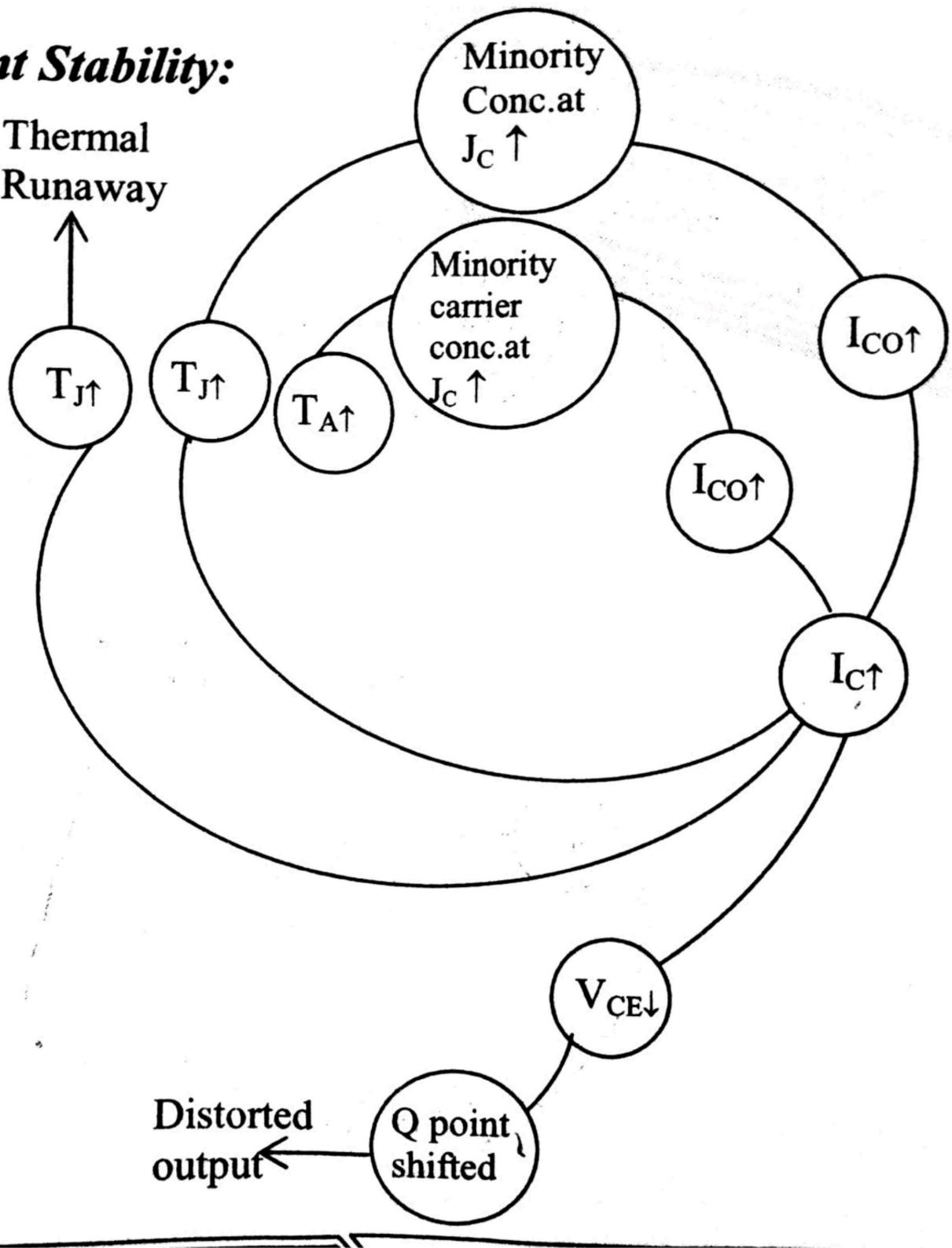
$$V_{cc} - I_C R_C - V_{CE} = 0 \quad \dots \dots (4)$$

$$\therefore V_{CEQ} = V_{cc} - I_{CQ} R_C \quad \dots \dots (5)$$

$$\therefore Q = [V_{CEQ} \quad I_{CQ}] \quad \dots \dots (6)$$

## ***Q-point Stability:***

Thermal Runaway



**Stability factor, S:**

$$S = \frac{\partial I_C}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \left[ \frac{\partial I_B}{\partial I_C} \right]} \quad \dots \dots (1)$$

KVL for the input section of fig.7

$$I_B = \frac{V_{CC} - V_{BE}}{R_B} \quad \dots \dots (2)$$

$$\Rightarrow \frac{\partial I_B}{\partial I_C} = 0 \quad \dots \dots (3)$$

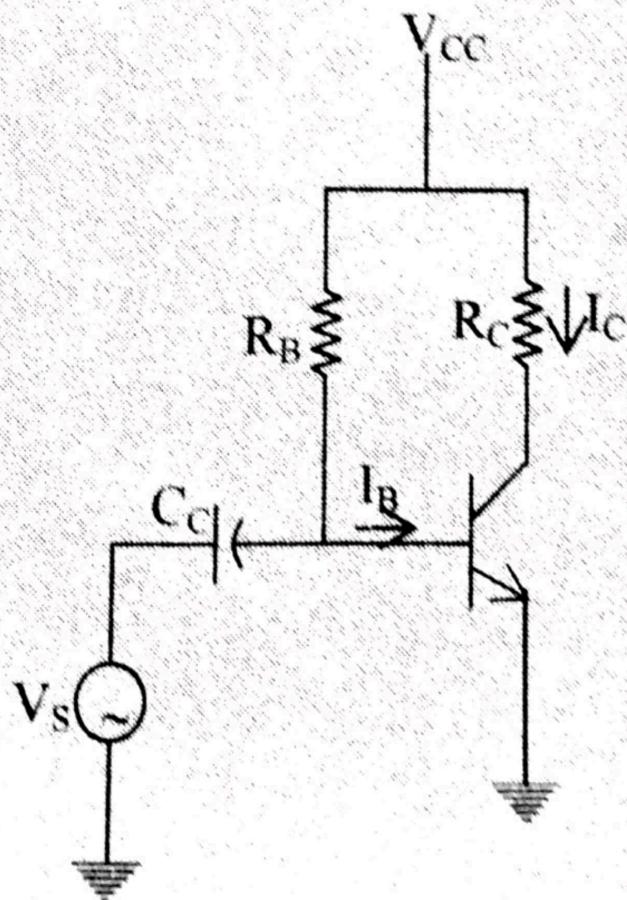
$$\therefore S = 1 + \beta \quad \dots \dots (4)$$

**Draw backs:**

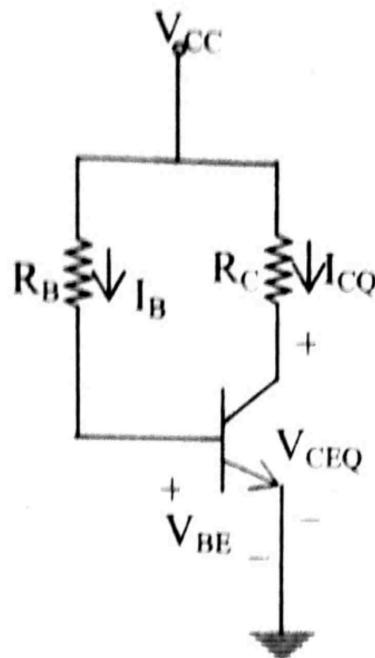
- Operating point is unstable with the variations in temperature and  $\beta$ .
- Possibility of thermal runaway.

**Example.1:**

For the circuit shown below, find the value of  $R_B$  &  $R_C$  required to establish a Q- point of 6 V & 1mA. Given  $V_{CC} = 12$  V,  $\beta = 100$   $V_{BE} = 0.7$  V



**Sol:** Consider the DC equivalent of the given circuit



**Step.1:** KVL to output loop:

$$V_{CC} - I_C R_C - V_{CE} = 0$$

$$\Rightarrow R_C = (V_{CC} - V_{CE}) / I_C = 6 \text{ K}\Omega$$

$$\text{Step.2: } I_{BQ} = \frac{I_{CQ}}{\beta} = \frac{1 \times 10^{-3}}{100} = 10 \mu A$$

**Step.3:** Applying KVL to input loop

$$V_{CC} - I_B R_B - V_{BE} = 0$$

$$R_B = \frac{V_{CC} - V_{BE}}{I_{BQ}}$$

$$= \frac{12 - 0.7}{10 \times 10^{-6}}$$

$$= \frac{11.3}{10} \times 10^6$$

$$\therefore R_B = 1.13 \text{ M}\Omega$$

## 2. Collector-to-Base bias or Collector feedback bias

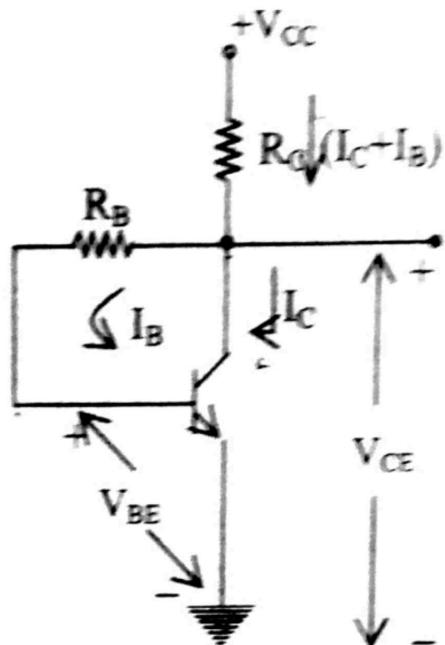


Figure.8

### Q-point establishment:

**Step1:** KVL for the input,

$$V_{CC} - (I_C + I_B)R_C - I_B R_B - V_{BE} = 0 \quad \text{---(1)}$$

$$V_{CC} - (1 + \beta)I_B R_C - I_B R_B - V_{BE} = 0 \quad \text{---(2)}$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + (1 + \beta)R_C} \quad \text{---(3)}$$

$$I_{CQ} = \beta \left[ \frac{V_{CC} - V_{BE}}{R_B + (1 + \beta)R_C} \right] \quad \text{---(4)}$$

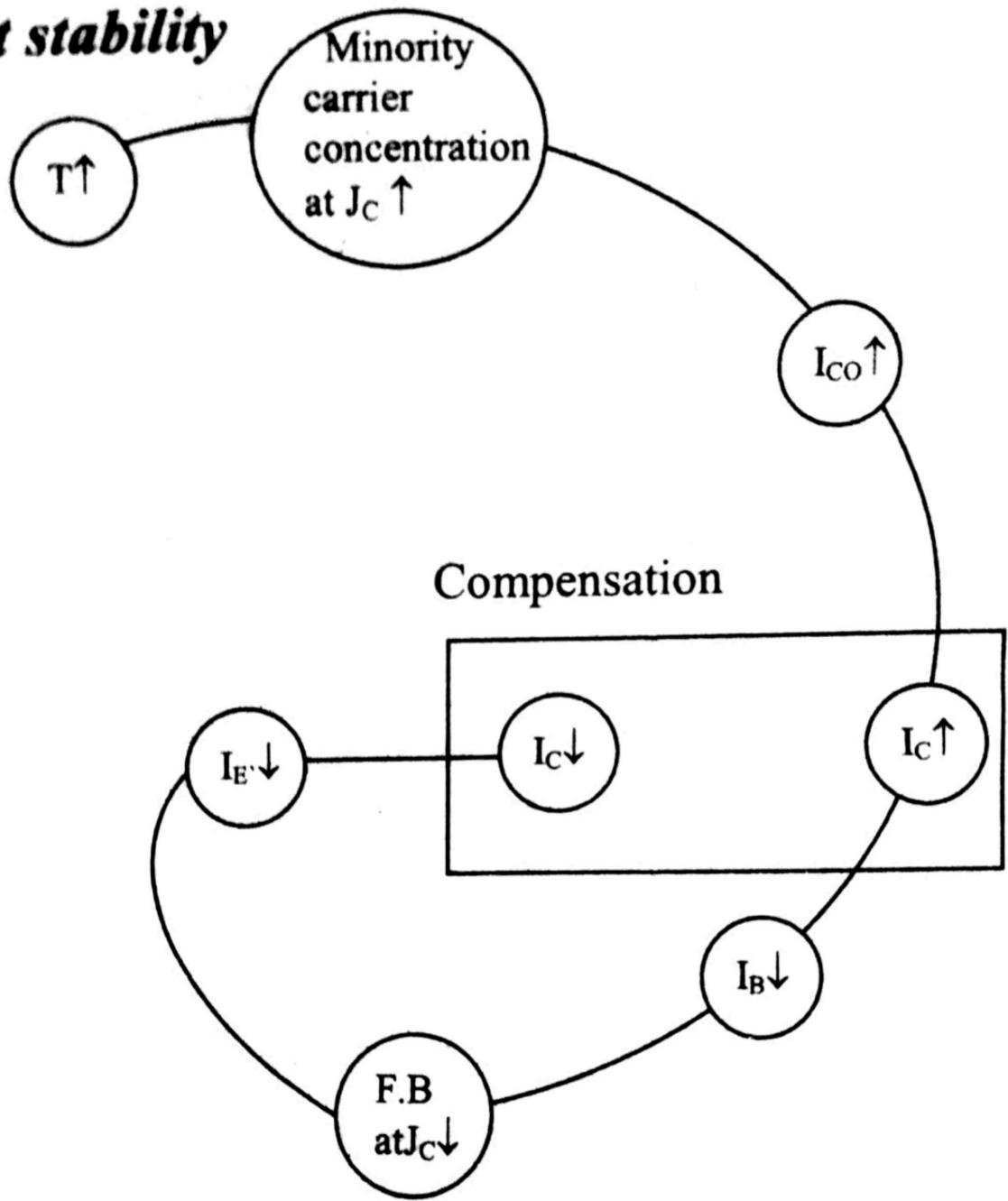
**Step2:** KVL for the output,

$$+ V_{CC} - (I_C + I_B) R_C - V_{CE} = 0 \quad \text{---(5)}$$

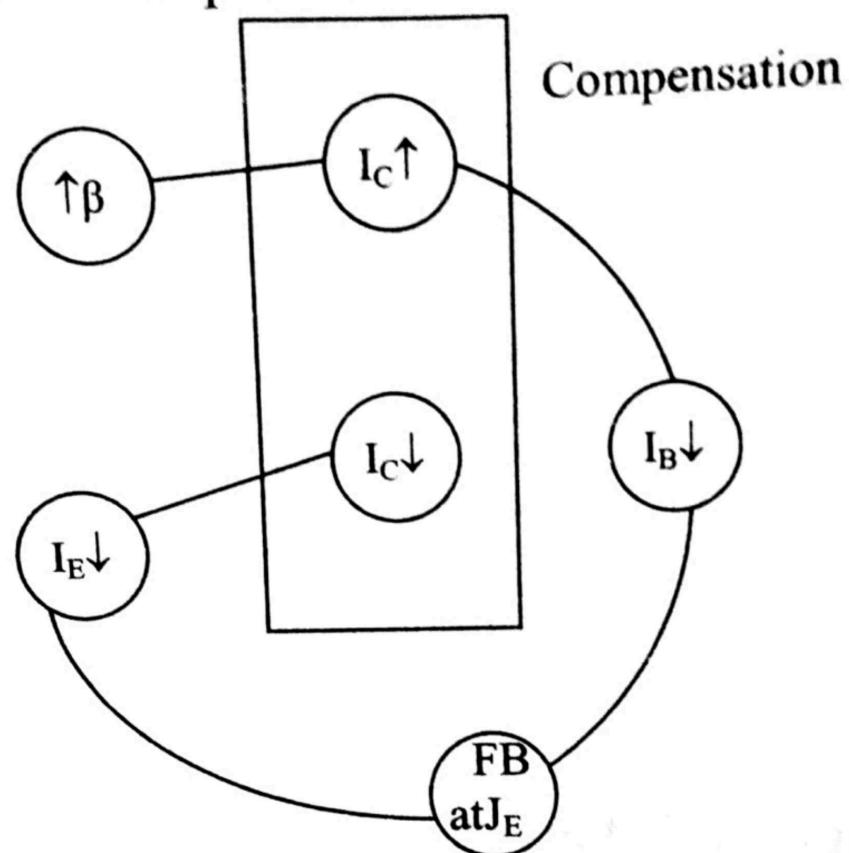
$$V_{CEQ} \approx V_{CC} - I_{CQ} R_C \quad \text{---(6)}$$

$$\therefore Q = [V_{CEQ}, I_{CQ}] \quad \text{---(7)}$$

## ***Q Point stability***



**Note:** The increase in  $I_C$  due to the increase in  $I_{CO}$  is compensated by the decrease in  $I_C$  due to the decrease in base current ( $I_B$ ) of the circuit during the temperature variations.



**Note:** The increase in  $I_C$  due to increase in  $\beta$  of the transistor is compensated by the decrease in  $I_C$  due to the decrease in base current of the circuit.

**Stability factor, S:**

$$S = \frac{\partial I_C}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \left[ \frac{\partial I_B}{\partial I_C} \right]} \quad \dots \dots (1)$$

KVL for the input section of fig.8

$$V_{CC} - (I_C + I_B)R_C - I_B R_B - V_{BE} = 0 \quad \dots \dots (2)$$

$$\Rightarrow V_{CC} - I_C R_C - I_B (R_C + R_B) - V_{BE} = 0 \quad \dots \dots (3)$$

$$\Rightarrow I_B = \frac{V_{CC} - V_{BE} - I_C R_C}{R_C + R_B} \quad \dots \dots (4)$$

$$\Rightarrow \frac{\partial I_B}{\partial I_C} = \frac{-R_C}{R_C + R_B} \quad \dots \dots (5)$$

$$\therefore S = \frac{1 + \beta}{1 + \beta \left( \frac{R_C}{R_C + R_B} \right)} \quad \dots \dots (6)$$

**Drawback.**

## **Drawback:**

**The resistor  $R_B$  connected between collector and base in a collector to base bias circuit, not only provides DC stabilization to the operating point**

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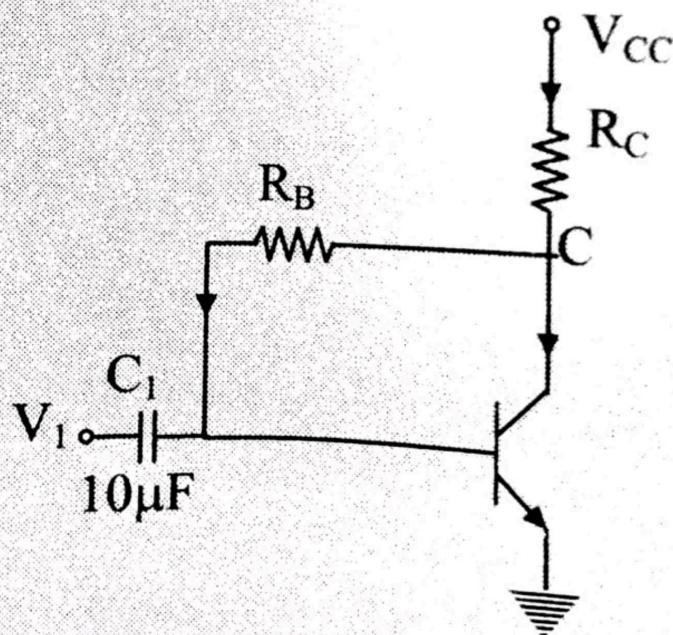
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but also causes AC negative feedback at the input section of the amplifier, which will in turn reduce the overall AC gain of the amplifier.

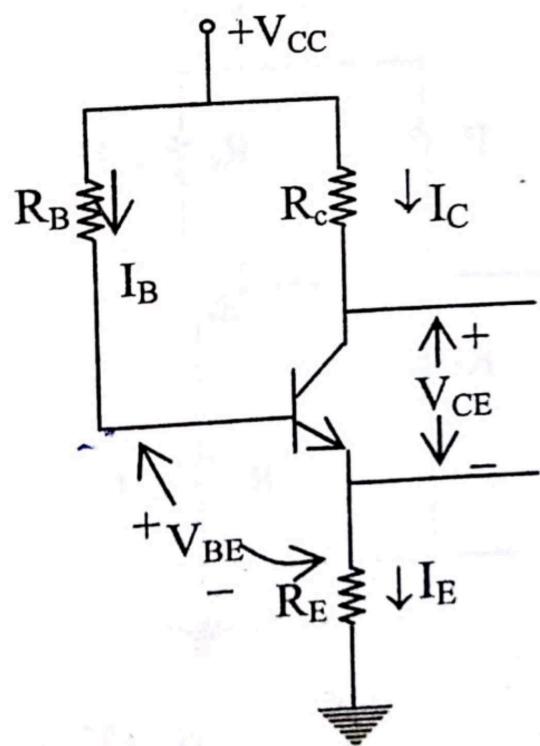
### **Example.2:**

In a common emitter circuit an N-PN transistor having a value of  $\beta = 50$  is used with  $V_{CC} = 10V$  and  $R_C = 2K\Omega$ . If a  $100K\Omega$  resistor is connected between collector and base and  $V_{BE} = 0$ , determine.

- (i) the position of quiescent point and
- (ii) stability factor S.

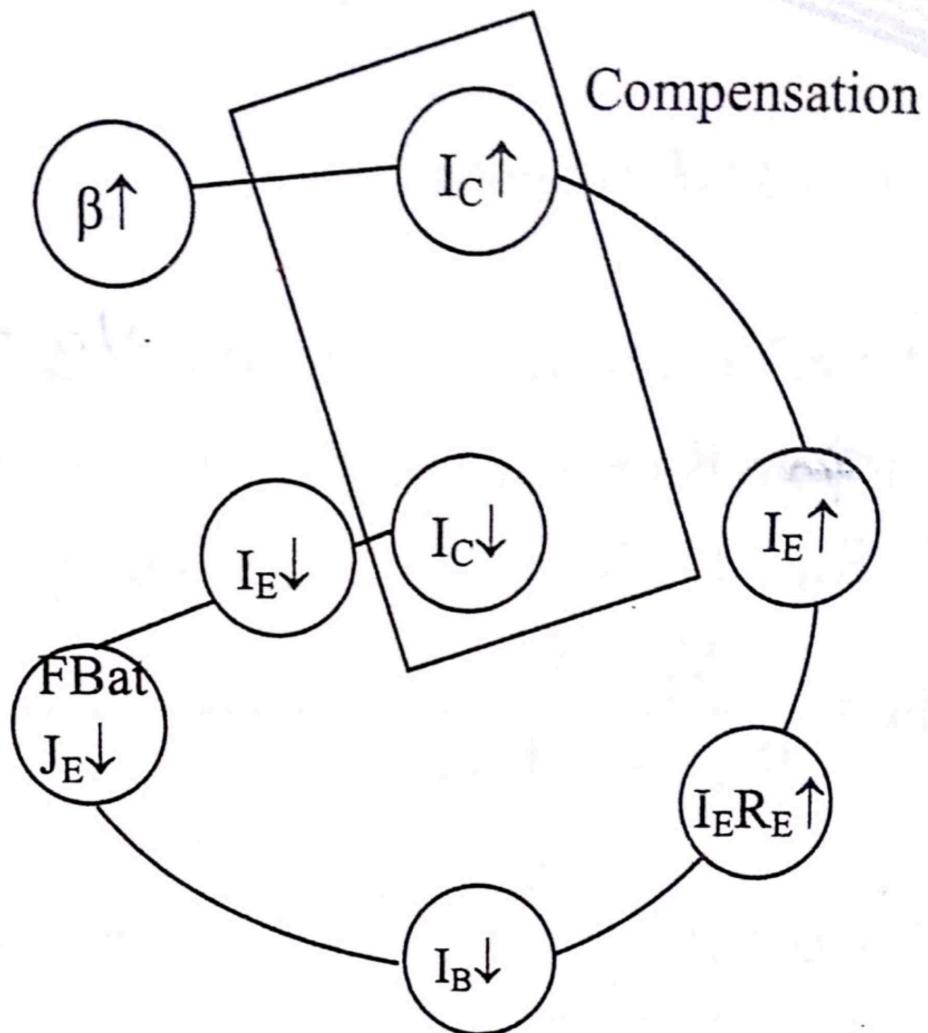


### 3. Fixed bias with emitter resistor or Emitter Bias



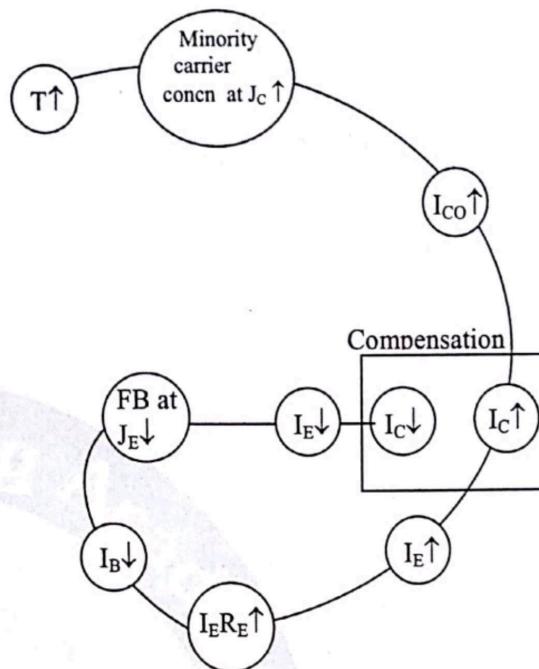
**Q<sub>1</sub>-Point Establishment:**

## *Q-Point stability:*



### Emitter

**Note:** The increases in  $I_C$  due to the increase in  $\beta$  is compensated by the decrease in  $I_C$  due to the increase in  $I_E R_E$



**Note:** The increase in  $I_C$  due to the increase in  $I_{CO}$  is compensated by the decrease in  $I_C$  due to the increase in voltage drop across  $R_E$  during the variations in temperature.

**Stability Factor, S:**

$$S = \frac{\partial I_C}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \left[ \frac{\partial I_B}{\partial I_C} \right]}$$

KVL for the input section of fig.9

$$V_{CC} - I_B R_B - V_{BE} - I_E R_E = 0 \quad \dots \dots \dots (1)$$

$$\Rightarrow V_{CC} - I_B R_B - V_{BE} - I_C R_E - I_B R_E = 0 \quad \dots \dots \dots (2)$$

[Since  $I_E = I_C + I_B$ ]

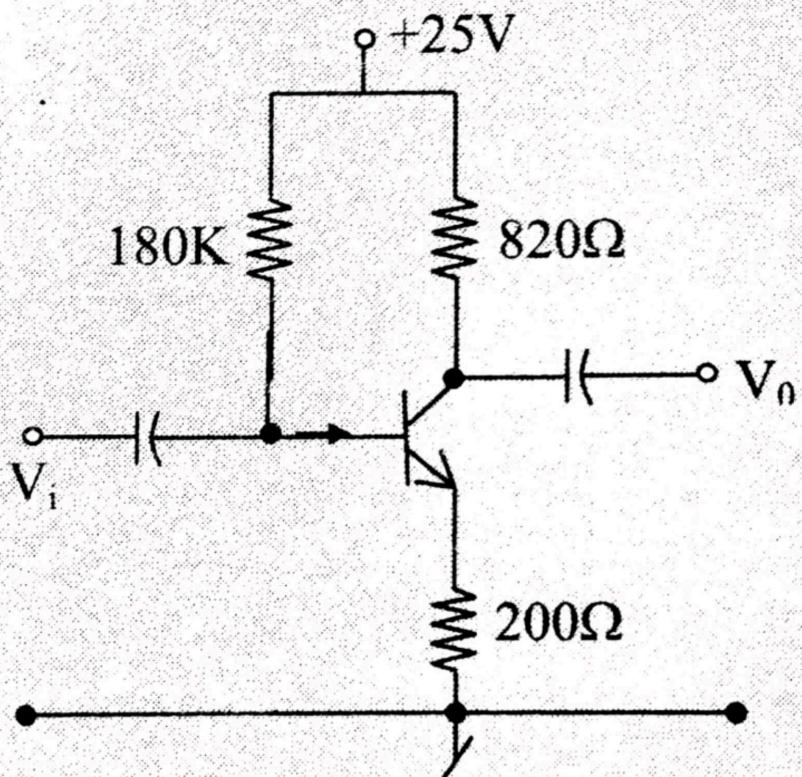
$$\Rightarrow I_B = \frac{V_{CC} - V_{BE} - I_C R_E}{R_E + R_B} \quad \dots \dots \dots (3)$$

$$\Rightarrow \frac{\partial I_B}{\partial I_C} = - \frac{R_E}{R_B + R_E} \quad \dots \dots \dots (4)$$

$$\therefore S = \frac{1 + \beta}{1 + \beta \left[ \frac{R_E}{R_E + R_B} \right]} \quad \dots \dots \dots (5)$$

**Example.3:**

Find  $I_C$  and  $V_{CE}$  for the following circuit of  $\beta = 80$  for BJT.



#### 4. Voltage-divider bias or self-bias:

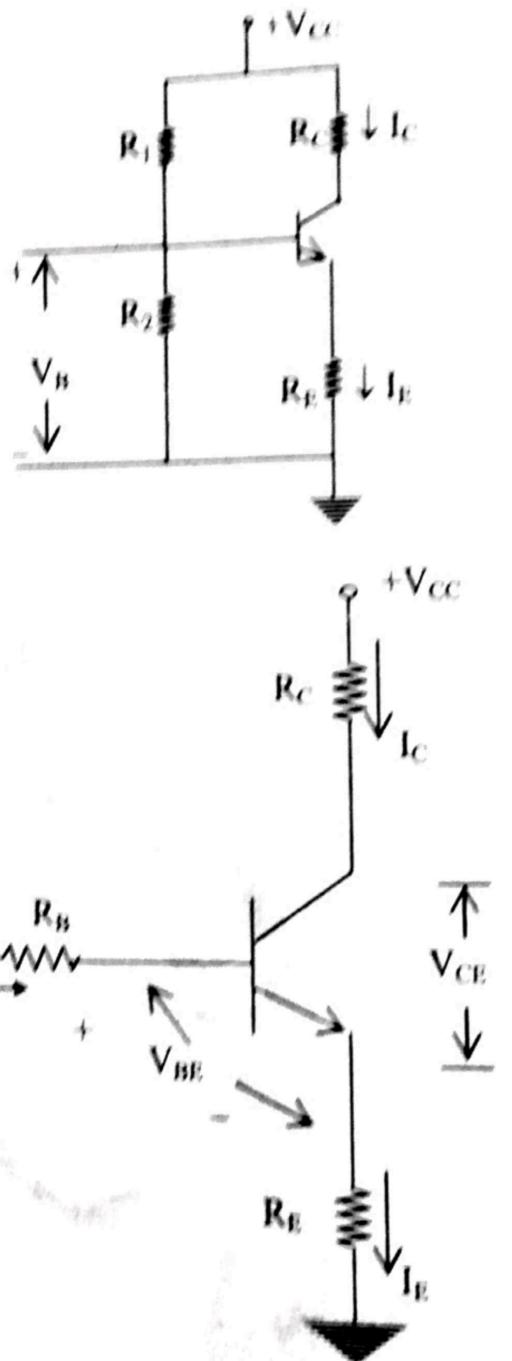


Figure 11: Thevenin equivalent of self-bias ckt

Where  $V_B = V_{Th} = \frac{V_{CC} R_2}{R_1 + R_2}$

And  $R_B = R_{Th} = \frac{R_1 R_2}{R_1 + R_2}$

Q. Poles

### *Q-Point Establishment:*

Step 1 : KVL for the I/P section  $V_B - I_B R_B - V_{BE} - I_E R_E = 0$

$$V_B - I_B R_B - V_{BE} - I_E R_E = 0 \quad (1)$$

$$I_B R_B - (1 + \beta) I_B R_E = V_B + V_{BE} \quad (2)$$

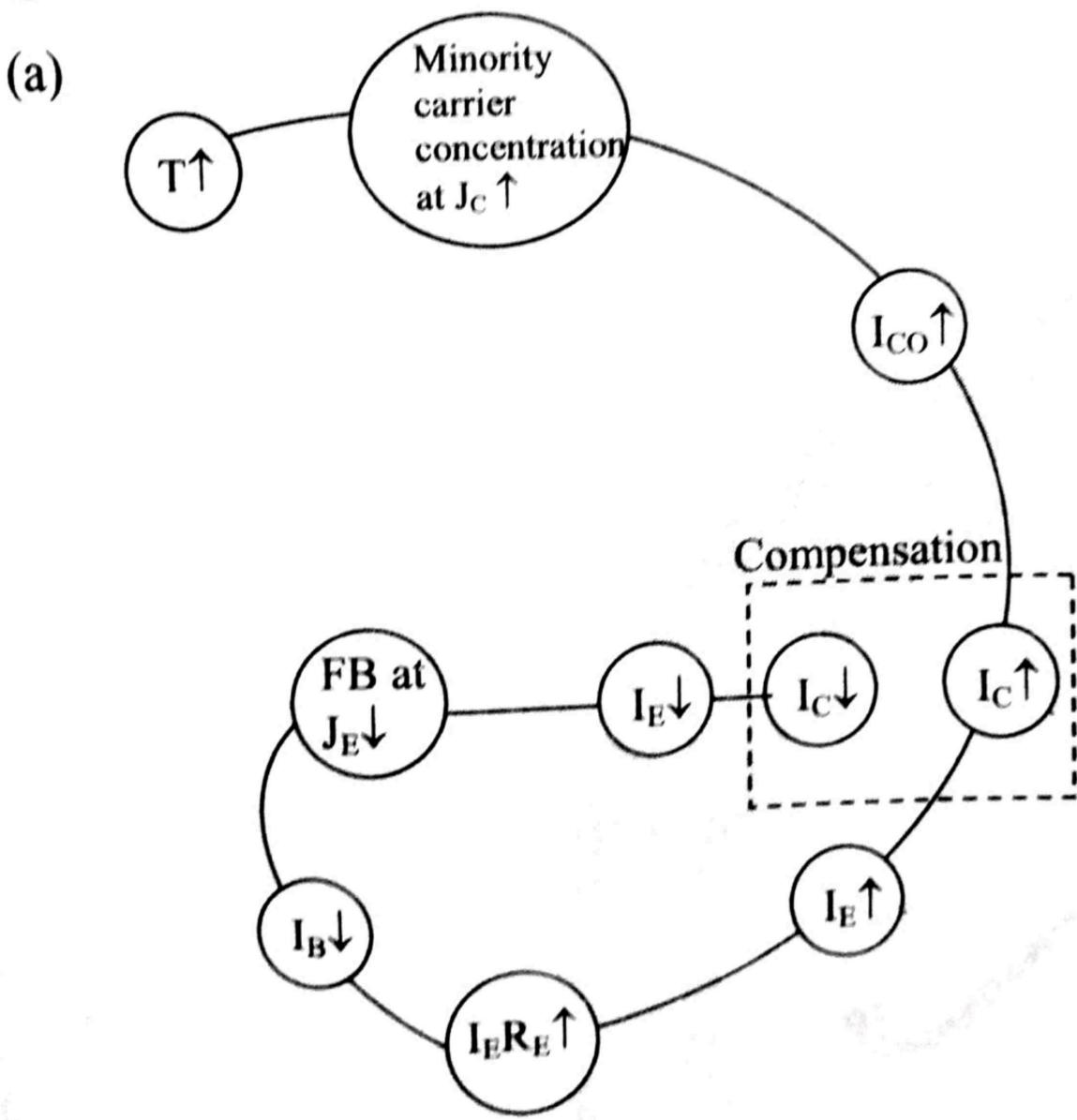
$$I_B = \frac{V_B + V_{BE}}{R_B + (1 + \beta) R_E} \quad (3)$$

$$\therefore I_{CQ} = \beta \left[ \frac{V_B + V_{BE}}{R_B + (1 + \beta) R_E} \right] \quad (4)$$

## Step 2: KVL for the O/P section

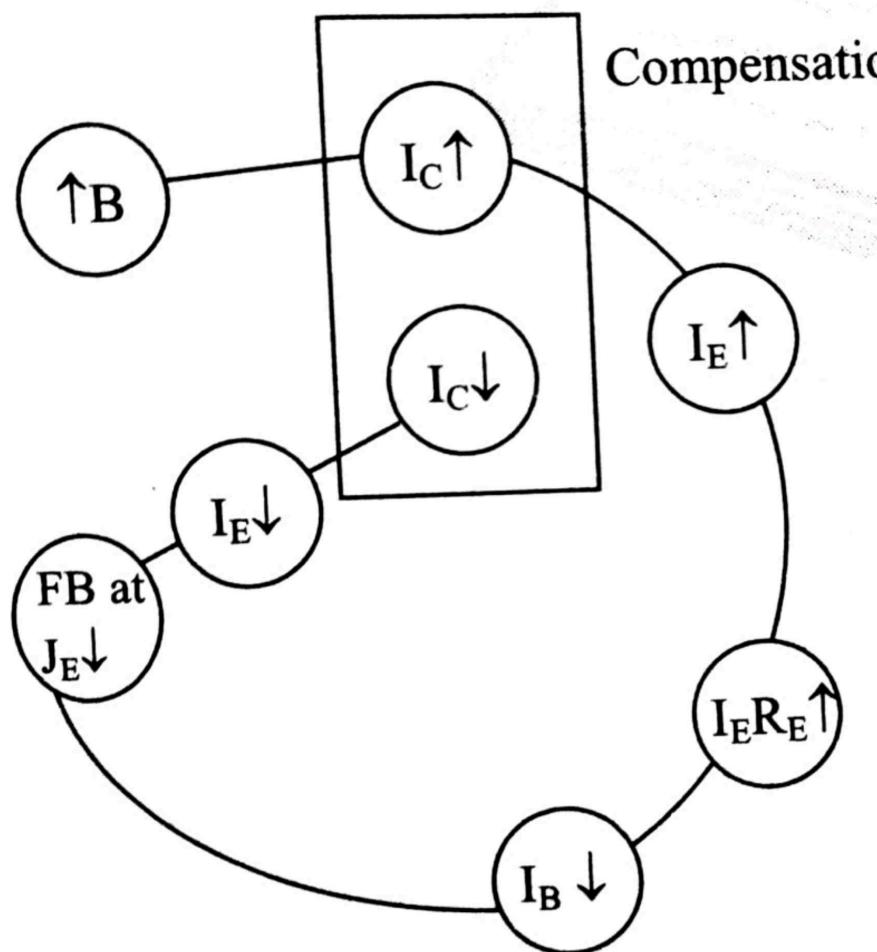
$$\therefore V_{CEQ} = V_{CC} - I_{CQ}(R_C + R_E) \dots\dots (6)$$

### ***Q- Point stability:***



**Note:** The Increase in  $I_C$  Due to the increase in  $I_{CO}$  is compensated by the decrease in  $I_C$  due to increase in voltage drop across  $R_E$  during temperature variations.

b)



**Note:** The increase in  $I_C$  due to the increase in  $\beta$  is compensated by the decrease in  $I_C$  due to the increase in voltage drop across  $R_E$ .

## Stability Factor, S:

$$S = \frac{\partial I_C}{\partial I_{CO}} = \frac{1 + \beta}{1 - \beta \left[ \frac{\partial I_B}{\partial I_C} \right]} \quad \text{---(1)}$$

KVL for the input section of fig.11

$$V_B - I_B R_B - V_{BE} - I_E R_E = 0 \quad \text{---(2)}$$

$$V_B - I_B R_B - V_{BE} - I_C R_E - I_B R_E = 0 \quad \text{---(3)}$$

$$I_B = \frac{V_B - V_{BE} - I_C R_E}{R_E + R_B} \quad \text{---(4)}$$

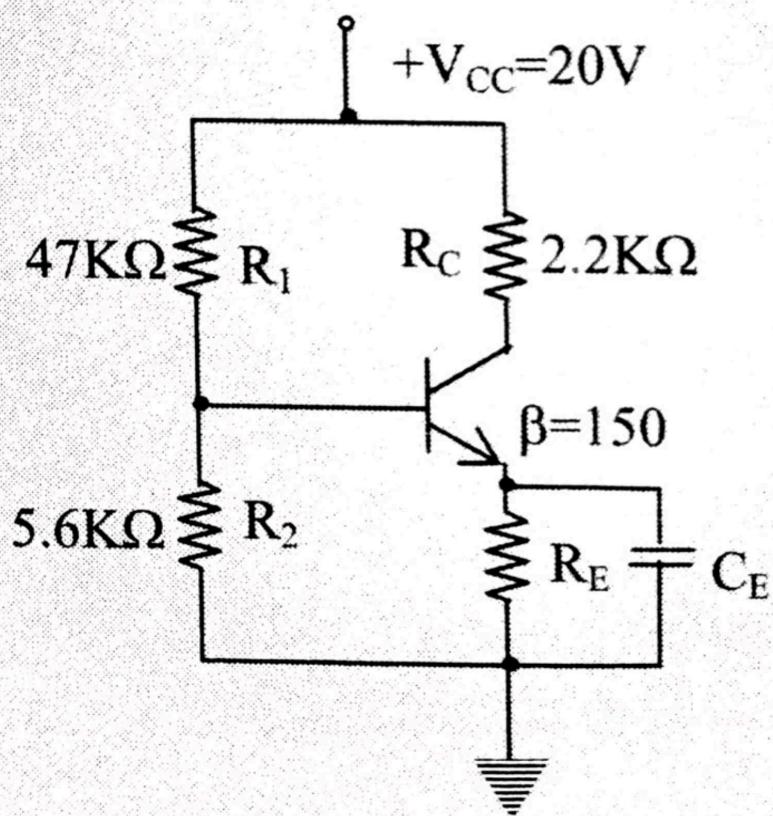
$$\frac{\partial I_B}{\partial I_C} = \frac{-R_E}{R_E + R_B} \quad \text{---(5)}$$

$$S = \frac{1 + \beta}{1 + \beta \left( \frac{R_E}{R_E + R_B} \right)} \quad \text{---(6)}$$

**Note:** For the reasonable values of  $R_1$ ,  $R_2$  &  $R_E$  the Stability factor of a self bias circuit can be less than 10.

### Example.5:

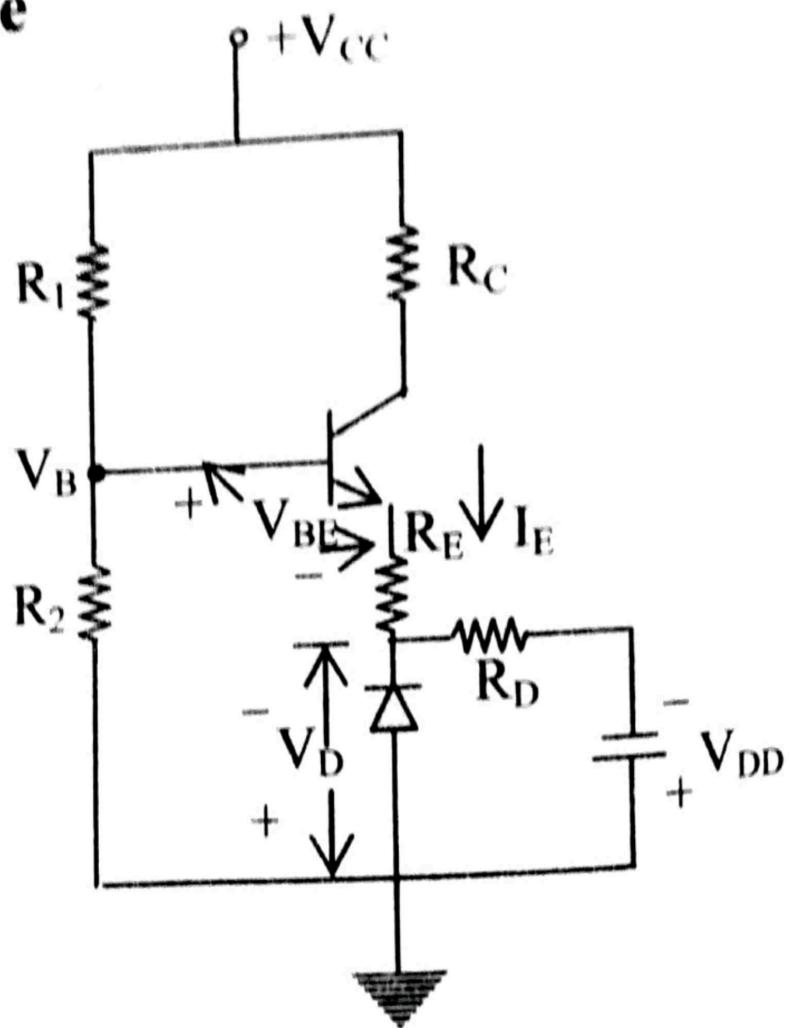
For a voltage divider biasing circuit shown below. Find  $I_C$ ,  $V_{CE}$ ,  $I_B$ ,  $V_E$  and  $V_B$ .



### ***Example.6:***

In a self-bias circuit, a BJT with  $h_{fe} = 100$ ,  $V_{BE} = 0.7V$  and  $I_{CO} = 0$  is used. Calculate the values of  $R_1$  and  $R_C$  such that it's  $I_C = 1mA$  and  $V_{CE} = 2.5V$

# 1. Diode compensation for $V_{BE}$ variations with temperature



KVL for Base- Emitter Loop

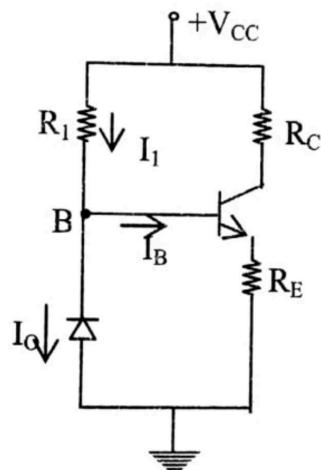
$$V_B - V_{BE} - I_E R_E + V_D = 0 \quad \dots \dots (1)$$

$$\therefore I_E = \frac{V_B - V_{BE} + V_D}{R_E} \quad \dots \dots (2)$$

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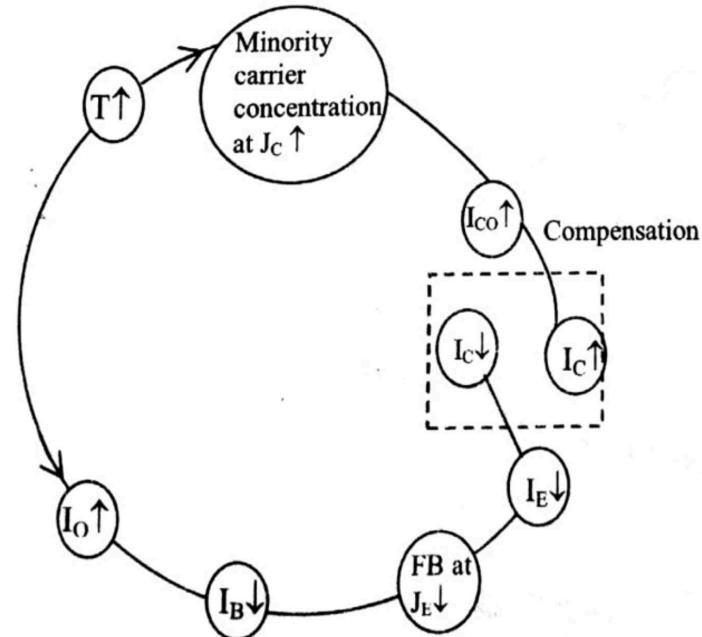
**Note:** The variations in  $I_E$  due to the variations in the junction voltage of BJT,  $V_{BE}$  are compensated by the corresponding variations in junction voltage of the diode,  $V_D$  during temperature variations.

## 2. Diode compensation for $I_{CO}$ variations with temperature



KCL at node B

$$I_1 = I_B + I_O \Rightarrow I_B = I_1 - I_O \text{ ----(1)}$$



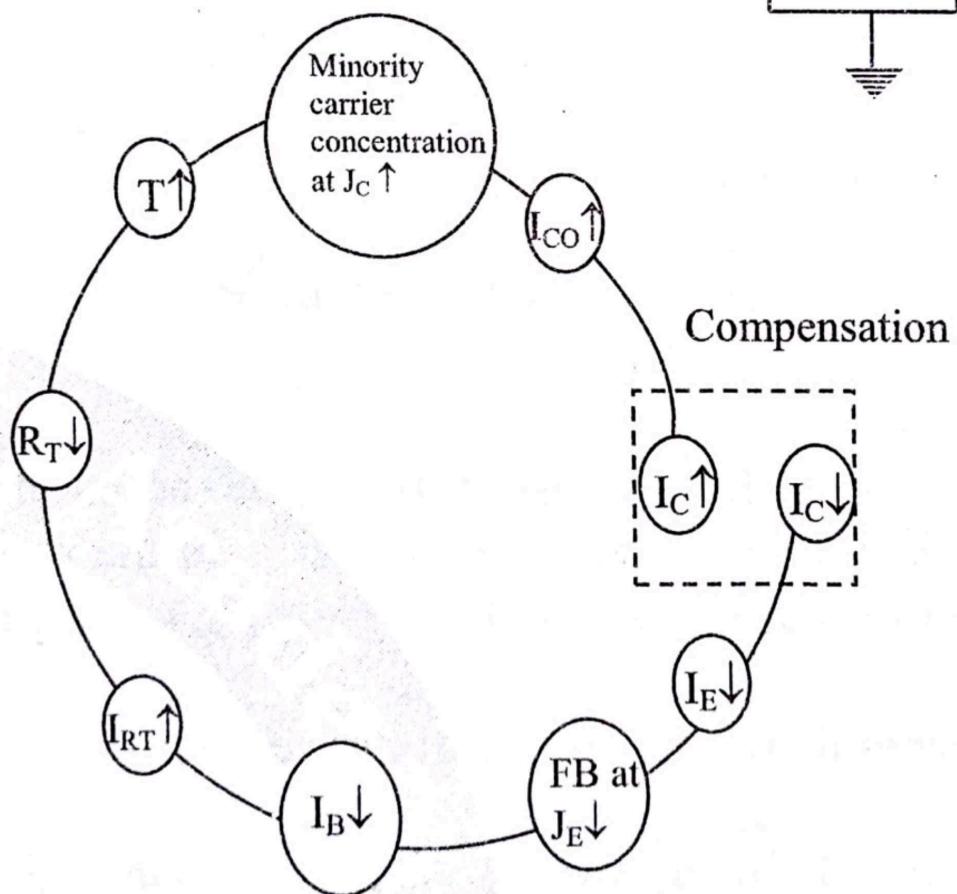
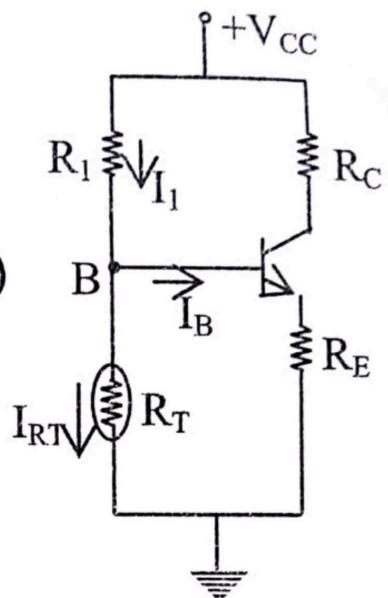
**Note:** The increase in  $I_C$  due to the increase in  $I_{CO}$  is compensated by the corresponding increase in reverse saturation current,  $I_O$  in the diode during temperature variations.

## Thermistor compensation for $I_{CO}$ variations with temperature:

*Thermistor* is a temperature dependant resistance which has got negative temperature coefficient. i.e the resistance of a thermistor varies inversely with the variations in temperature.

KCL at node B

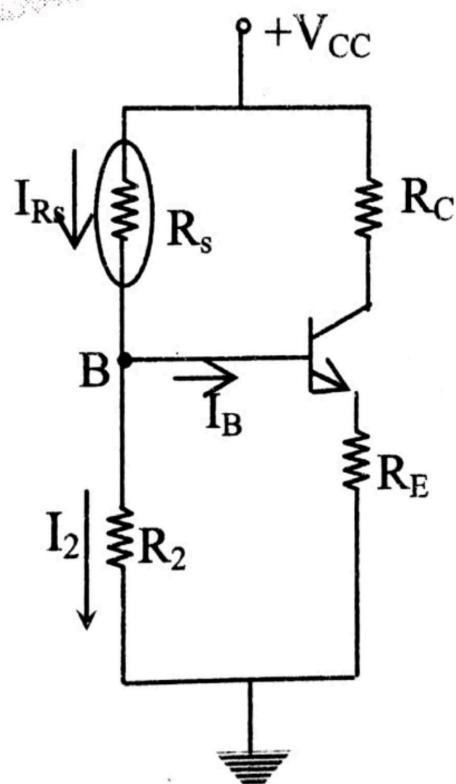
$$I_1 = I_B + I_{RT} \Rightarrow I_B = I_1 - I_{RT} \text{ ----(1)}$$



**Note:** The Increase in  $I_C$  due to increase  $I_{CO}$  is compensated by decrease in the resistance of Thermistor during increase in temperature.

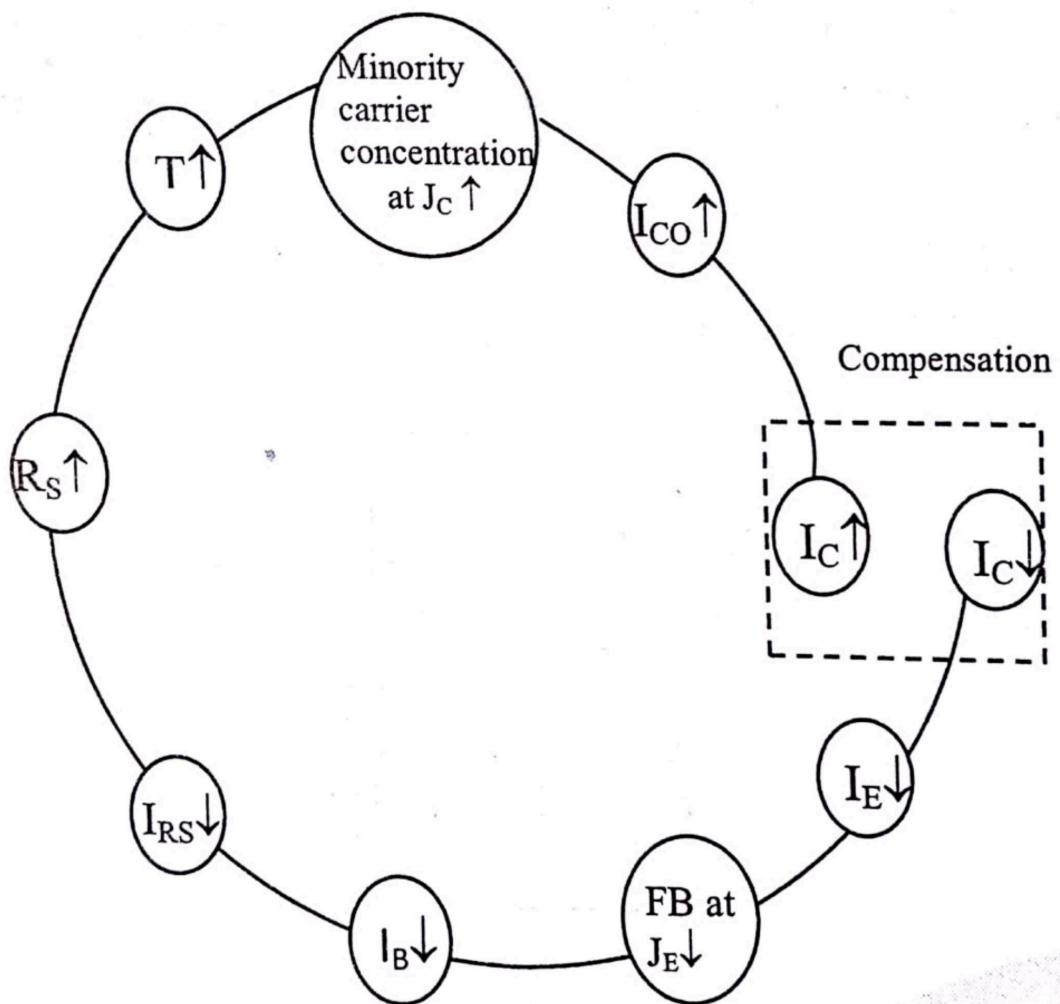
#### 4. **Sensistor compensation for $I_{CO}$ variations with temperature:**

*Sensistor* is variable resistor or temperature dependant resistor which has got positive temperature coefficient. i.e the resistance of sensistor varies in proportional with the variations in temperature.



**KCL at B**

$$I_{RS} = I_B + I_2 \Rightarrow I_B = I_{RS} - I_2 \text{ ----- (1)}$$



**Note:** The increase in  $I_C$  due to the increase  $I_{CO}$  is compensated by the increase in the resistance of sensistor during the increase in temperature.

Thermal stability in collector-emitter junction

## Thermal stability in electronic devices:

- Let  $T_A$  °C be the ambient temperature i.e., the temperature of surroundings air around transistor and  $T_j$  °C, the temperature of collector-base junction of the transistor. Then

$$T_j - T_A \propto P_D \quad \dots \dots (1)$$

Where  $P_D$  is the power released at a reverse biased p-n junction of an electronic device under steady state condition.

$$\Rightarrow T_j - T_A = \Theta P_D \quad \dots \dots (2)$$

Where  $\Theta$  is the thermal resistance of an electronic device expressed in °C / Watt.

### Note:

- For a low power, low cost transistor, the thermal resistance  $\Theta$  is around  $1000$  °C/Watt
- For a high power quality transistor thermal resistance  $\Theta$  is  $0.02$  °C /watt.

Assuming the ambient temperature in equation (2) as constant,

$$\partial T_j = \Theta \partial P_D \quad \dots \dots (3)$$

$$\Rightarrow \frac{\partial P_D}{\partial T_j} = \frac{1}{\Theta} \quad \dots \dots (4)$$

- Let  $P_C$  is the power released at the reverse bias collector junction of a BJT during its real time operation.

$$\therefore \frac{\partial P_C}{\partial T_j} < \frac{\partial P_D}{\partial T_j} \quad \dots \quad (5)$$

$$\therefore \frac{\partial P_C}{\partial T_j} < \frac{1}{\Theta} \quad \dots \quad (6)$$

**This is the condition to prevent thermal runaway in transistors.**

- From Fixed bias circuit,  
 $V_{CE} = V_{CC} - I_C R_C \quad \dots \quad (7)$
- The power dissipation at the collector junction of a BJT is given by

$$P_C = V_{CE} I_C \quad \dots \quad (8)$$

$$= V_{CC} I_C - I_C^2 R_C \quad \dots \quad (9)$$

$$\frac{\partial P_C}{\partial I_C} = V_{CC} - 2 I_C R_C \quad \dots \quad (10)$$

From equation (4):  $\frac{\partial P_C}{\partial T_j} < \frac{1}{\Theta}$

$$\frac{\partial P_C}{\partial I_C} \times \frac{\partial I_C}{\partial T_j} < \frac{1}{\Theta} \quad \dots \quad (11)$$

- Since  $\frac{\partial I_C}{\partial T_j}$  is the positive and  $\frac{1}{\Theta}$  is approximately zero for low power transistor,  $\frac{\partial P_C}{\partial I_C}$  should be negative

$$\Rightarrow \frac{\partial P_C}{\partial I_C} = V_{CC} - 2 I_C R_C < 0 \quad \dots \quad (12)$$

$$\Rightarrow I_C \geq \frac{V_{CC}}{2 R_C} \quad \dots \quad (13)$$

- Substituting equation (13) in (7)

$$\therefore V_{CE} \leq \frac{V_{CC}}{2} \quad \dots \quad (14)$$

**Note: This is the condition for thermal stability in transistors**