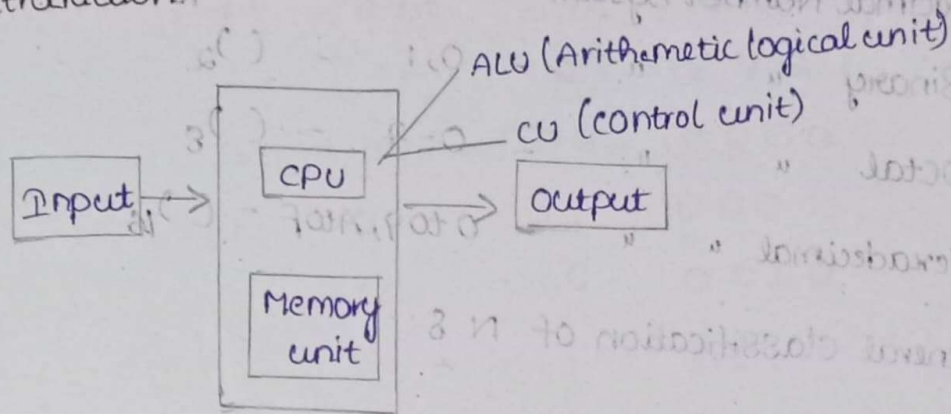


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# Functional unit of computer

## Introduction:



- \* Memory register (or)

Buffer register → Temporary storage

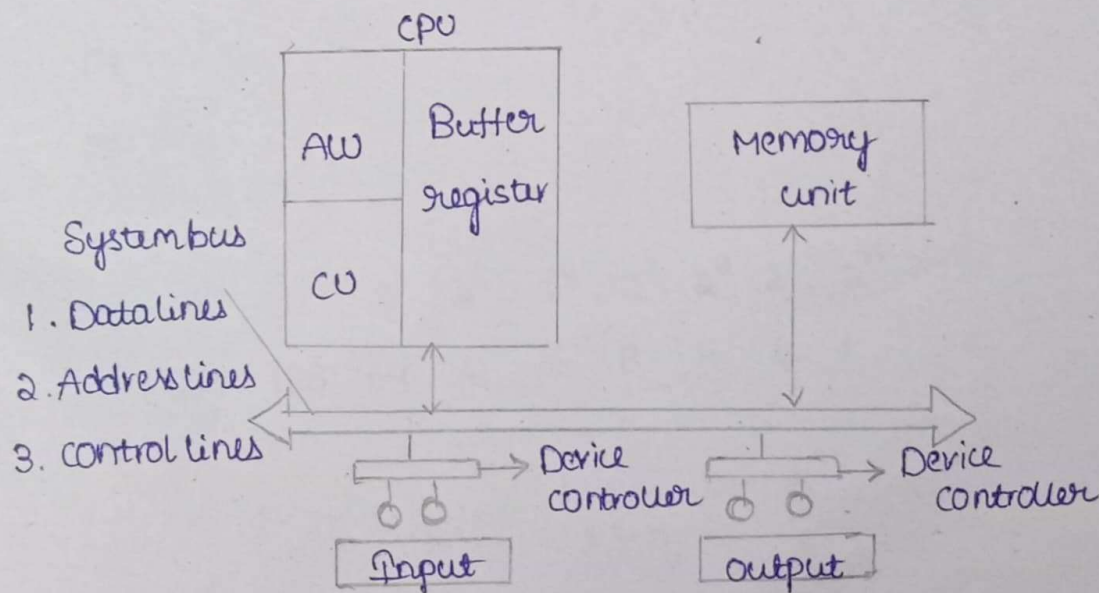
- \* CU → to control all the operations

- \* Memory unit → primary unit

Secondary unit → (It will fetch instruction by instructions)

- \* CPU can access primary memory or directly can access input.

## Basic functional units of a computer: (Interconnection)



## Number Systems

1. Decimal Number System - 0 to 9 -  $( )_{10}$
2. Binary " " - 0, 1 -  $( )_2$
3. Octal " " - 0-7 -  $( )_8$
4. Hexadecimal " " - 0 to 9, A to F -  $( )_{16}$

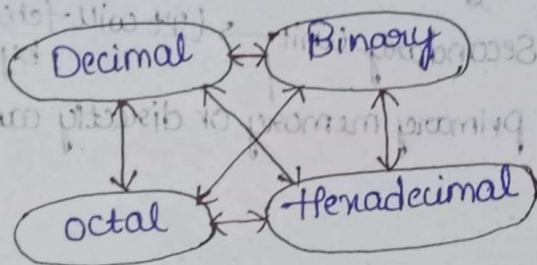
General classification of N.S. :-

1. Positional NS
2. Non-positional NS

I, II, III, ...

We can't perform any arithmetic op's

It is used to represent the roman numbers



# Representation of Binary numbers:-

NO.	1-bit	2-bit	3-bit	4-bit
0	0	00	000	0000
1	1	01	001	0001
2		10	010	0010
3			011	0011
4			100	0100
5			101	0101
6			110	0110
7			111	0111
8				1000
9				1001
10				1010
11				1011
12				1100
13				1101
14				1110
15				1111

$2^8$   $2^7$   $2^6$   $2^5$   $2^4$   $2^3$   $2^2$   $2^1$   $2^0$   
 256 128 64 32 16 8 4 2 1

$$\begin{aligned}
 & 01 \times 1 + 01 \times 2 + 01 \times 4 + 01 \times 8 + 01 \times 16 + 01 \times 32 + 01 \times 64 + 01 \times 128 + 01 \times 256 \\
 & = 1 + 2 + 4 + 8 + 16 + 32 + 64 + 128 + 256 \\
 & = 511
 \end{aligned}$$



Conversion methods:

Binary to decimal:

1. Convert 11011 into decimal

$$\begin{aligned} \overleftarrow{(11011)} &\Rightarrow 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 \\ &= 16 + 8 + 0 + 2 + 1 = 27 \end{aligned}$$

2.  $(11010.101)_2 = (?)_{10}$

$$\begin{aligned} (11010.101)_2 &= 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} \\ &= 16 + 8 + 0 + 2 + 0.5 + 0.25 + 0.125 \\ &= (26.875)_{10} \end{aligned}$$

Octal to decimal:

1.  $(1054)_8 = (?)_{10}$

$$\begin{aligned} (1054)_8 &= 1 \times 8^3 + 0 \times 8^2 + 5 \times 8^1 + 4 \times 8^0 \\ &= 512 + 0 + 40 + 4 \\ &= (556)_{10} \end{aligned}$$

2.  $(22.74)_8 = (?)_{10}$

$$\begin{aligned} (22.74)_8 &= 2 \times 8^1 + 2 \times 8^0 + 7 \times 8^{-1} + 4 \times 8^{-2} \\ &= 16 + 2 + 0.875 + 0.0625 \\ &= (18.9375)_{10} \end{aligned}$$

Hexadecimal to decimal conversion:

$$\begin{aligned} 1. (A23)_{16} &\Rightarrow 10 \times 16^2 + 2 \times 16^1 + 3 \times 16^0 \\ &= 2560 + 32 + 3 \\ &= (2595)_{10} \end{aligned}$$

$$\begin{aligned} 2. (A23.351)_{16} &\Rightarrow 10 \times 16^2 + 2 \times 16^1 + 3 \times 16^0 + 3 \times 16^{-1} + 5 \times 16^{-2} + 1 \times 16^{-3} \\ &= 2595 + 0.1875 + 0.0195 + 0.0002441 \\ &= (2595.20727)_{10} \end{aligned}$$

# Decimal to Binary conversion

1.  $(21)_{10} = (?)_2$

$$\begin{array}{r|l} 2 & 21 - 1 \\ \hline 2 & 10 - 0 \\ 2 & 5 - 1 \\ 2 & 2 - 0 \\ & 1 \end{array}$$

Shortcut

$$\begin{array}{cccccc} 16 & 8 & 4 & 2 & 1 \\ 1 & 0 & 1 & 0 & 1 \end{array}$$

$$16 + 4 + 1 \Rightarrow 21$$

$$(21)_{10} = (10101)_2$$

2.  $(38.15)_{10}$

$$\begin{array}{r|l} 2 & 38 \\ \hline 2 & 19 - 0 \\ 2 & 9 - 1 \\ 2 & 4 - 1 \\ 2 & 2 - 0 \\ & 1 - 0 \end{array}$$

$$0.15 \times 2 = 0.3 \Rightarrow 0$$

$$0.3 \times 2 = 0.6 \Rightarrow 0$$

$$0.6 \times 2 = 1.2 \Rightarrow 1$$

$$0.2 \times 2 = 0.4 \Rightarrow 0$$

$$0.4 \times 2 = 0.8 \Rightarrow 0$$

$$0.8 \times 2 = 1.6 \Rightarrow 1$$

iterate

$$(38.15)_{10} = (100110.001)_2$$

Octal to binary conversion:

1.  $(71)_8 = (?)_2$



$((111) (001))_2$

$\Rightarrow (111001)_2$

2.  $(765.031)_8 = (?)_2$

$(111 110 101. 000 011 001)_2$

Binary to octal conversion:

1.  $(10010.1011)_2$

empty units 0

$\frac{010}{2} \frac{010}{2} \frac{101}{5} \frac{100}{4} \Rightarrow (22.54)_8$

Binary to Hexadecimal conversion:

1.  $1011001001.100001$

$\frac{0010}{2} \frac{1100}{C} \frac{1001}{9} \frac{1000}{8} \frac{0100}{4} \Rightarrow (2C9.84)_{16}$

Octal to Hexadecimal conversion:

1.  $(256)_8 = (?)_{16}$

Step-1: convert each binary digit into its 3-bits binary code

$(\overset{2}{010} \overset{5}{101} \overset{6}{110})_8$

Step-2: convert " " " " " " 4-bits " "

$0110101110$

$\frac{0000}{(0} \frac{1010}{A} \frac{1110}{E)}_{16}$



## Hexadecimal to octal conversion:

1.  $(2AB)_{16} \rightarrow (?)_8$

$\begin{array}{ccc} 2 & A & B \\ 0010 & 1010 & 1011 \end{array} \Rightarrow \text{Each value into 3-bits}$

$\begin{array}{cccc} 0010 & 1010 & 1011 & \\ \hline 1 & 2 & 5 & 3 \end{array} \Rightarrow (1253)_8$

## Hexadecimal to binary conversion:

1.  $(47A)_{16}$

$\begin{array}{ccc} 4 & 7 & A \\ 0100 & 0111 & 1010 \end{array}$

$\Rightarrow (010001111010)_2$

## Hexadecimal to decimal conversion:

$(A23)_{16} \Rightarrow A \times 16^2 + 2 \times 16^1 + 3 \times 16^0$   
 $= 2560 + 32 + 3 = (2595)_{10}$

## Decimal to octal conversion:

1.  $(574)_{10} \Rightarrow (?)_8$

$\begin{array}{r} 8 \overline{) 574} \\ 8 \overline{) 71} \end{array}$

$\begin{array}{r} 8 \overline{) 71} \end{array}$

$\begin{array}{r} 8 \overline{) 71} \end{array}$

$1 - 0 \Rightarrow (1076)_8$

2.  $(18.6875)_{10} = (?)_8$

$\begin{array}{r} 8 \overline{) 18} \\ 2 - 2 \end{array}$

$0.6875 \times 8 = 5.5 = 5$

$= 4$

$\Rightarrow (22.54)_8$

$8(2FF) = 8(1FF)$

$8(2FF) = 8(FFF)$

$8(108) = 8(110)$

2/5/22

Data representation:

1. Data types

2. complements

Alphabets

Numeric

Special Symbols

(@, \$, -)

Types of data that we can give input to the computer

Signed  
-ve (1)    +ve (0)

⇒ To deal with -ve numbers

⇒ In conversion of Subtraction to addition

⇒ Classified into 2 types

1.  $(r-1)$ 's complement  $[(r^n-1)-N]$

2.  $r$ 's complement  $[r^n-N]$

Decimal  $\rightarrow$  9's & 10's

Binary  $\rightarrow$  1's & 2's

Ex:  $-(132)_{10}$

$r=10$ ;  $N=132$ ;  $n=3$  (no. of digits)

999  
- 132

867 is the 9's complement

1

868  $\Rightarrow$  10's complement

$-(1001)_2$

$r=2$ ;  $N=1001$ ;  $n=4$

1001  $\Rightarrow$  0110  $\Rightarrow$  1's complement

1

0111  $\Rightarrow$  2's complement  $=(301)_8$

PF2 | 8  
(476)<sub>8</sub> 14 | 8

$r=8$ ;  $N=476$ ;  $n=3$

$[(8^3-1)-(476)_8]$

$=(511)_{10} - (476)_8$

$=(777)_8 - (476)_8$



\* To deal with decimal no.s we have two representations

1. Fixed point representation

2. floating "

Ex:  $736.0 \rightarrow$  integer (extremely right) } Fixed point  
 $.736 \rightarrow$  ~~float~~ fraction (extremely left) }

$7.36$   
 $73.6$   
 $736.4$  } Floating Point

Fixed point representation:-

\* Either Signed (or) unsigned

$\Rightarrow$  To deal with Signed no.s, we have 3 methodologies

1. Signed magnitude representation

2. " 1's complement

3. " 2's "

Ex:  $-(14)_{10}$

1  $\rightarrow$   $(\underline{00001110})$   
 $\hookrightarrow$  magnitude will be +ve

2  $\rightarrow$   $(\underline{11110001})$   
 $\hookrightarrow$  1's complement of magnitude

3  $\rightarrow$   $(\underline{11110010})$   
 $\hookrightarrow$  2's complement of magnitude

Arithmetic addition:

Adding the no.s in signed 2's complement system require only addition and complementation

- \* Add the two no.s, including their sign bits
- \* Discard any carryout of the sign (leftmost) bit position

Note: -ve no.s must be initially be in 2's complement and if the sum obtained after the addition is -ve it is in 2's complement form

Ex: +6 0000 0110

+13 0000 1101

+19 0001 0011

-6 0000 0110 (6)

1111 1001 (1's complement)

1

1111 1010

+13 0000 1101

+7 0000 0111

(0111 0000) 1

(1000 1111) 1

(0100 1111) 1

## Arithmetic Subtraction:

2's complement Subtraction includes following steps

- \* Take the 2's complement of number to be subtracted including the sign bit
- \* Add it the next number
- \* Discard the carry out of the sign bit position.

Ex:  $-6 - (-13) = +7$

-6

2's complement of -13

$$\begin{array}{r} 11111101 \\ 00001101 \\ \hline 00000111 \end{array}$$



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## Floating point representation:

⇒ The number should be represented in the form of

$$m \times r^e \rightarrow \text{exponent}$$

$\downarrow$        $\downarrow$   
 mantissa    radix

$$(or) \quad s \times b^e \rightarrow \text{exponent}$$

$\downarrow$        $\downarrow$   
 Significant    base

Ex:  $4.2 \times 10^8$

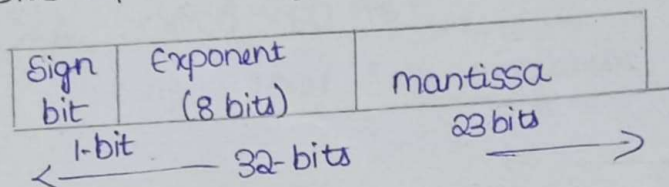
$\downarrow$        $\downarrow$   
 m      r

IEEE notation:

It can be of 16-bits, 32-bits, 64-bits, 128-bits

$\downarrow$        $\uparrow$   
 Half-precision    quadtruple

32-bits representation:

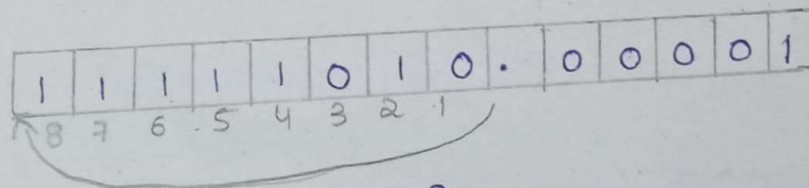


Ex: ~~2450.00~~  $(250.03125)_{10}$

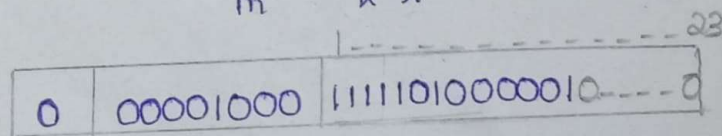
$(250)_{10} = 11111010$

$.03125 = 0.00001$

⇒  $(11111010.00001)_2$



$(1111101000001) \times 2^8$   
 $m \quad \times r^e$



for exponent → add zeroes to left

for mantissa → " " " right

$$2. (102.9375)_{10}$$

$$\downarrow \quad \downarrow$$

$$(1100110.1111)_2$$

1	1	0	0	1	1	0	.	1	1	1	1
7	6	5	4	3	2	1					

$$(11001101111) \times 2^7$$

$$m \quad \times 2^e$$

0	0000	0111	1100110111100
			23

$$\begin{array}{r} 2 \overline{) 102} - 0 \\ 2 \overline{) 51} - 1 \\ 2 \overline{) 25} - 1 \\ 2 \overline{) 12} - 0 \\ 2 \overline{) 6} - 0 \\ 2 \overline{) 3} - 1 \\ 1 \end{array}$$

$$0.9375 \times 2 = 1.875 = 1$$

$$0.875 \times 2 = 1.75 = 1$$

$$0.75 \times 2 = 1.5 = 1$$

$$0.5 \times 2 = 1 = 1$$

$$3. (250.75)_{10}$$

$\downarrow$

$$(11111010.11)_2$$

1	1	1	1	1	0	1	0	.	1	1
8	7	6	5	4	3	2	1			

$$(1111101011) \times 2^8$$

$$m \quad \times 2^e$$

0	0000	1000	11111010110
			23

$$\begin{array}{r} 2 \overline{) 250} - 0 \\ 2 \overline{) 125} - 1 \\ 2 \overline{) 62} - 0 \\ 2 \overline{) 31} - 1 \\ 2 \overline{) 15} - 1 \\ 2 \overline{) 7} - 1 \\ 2 \overline{) 3} - 1 \end{array}$$

$$0.75 \times 2 = 1.50 \Rightarrow 1$$

$$0.50 \times 2 = 1 \Rightarrow 1$$

$$0 \times 2 = 0 \Rightarrow 0$$

$$4. (173.75)_{10}$$

$\downarrow$

$$(10101101.11)_2$$

1	0	1	0	1	1	0	1	.	1	1
---	---	---	---	---	---	---	---	---	---	---

$$(1010110111) \times 2^8$$

$$m \quad \times 2^e$$

0	0000	1000	1010110111
			23

$$\begin{array}{r} 2 \overline{) 173} - 1 \\ 2 \overline{) 86} - 0 \\ 2 \overline{) 43} - 1 \\ 2 \overline{) 21} - 1 \\ 2 \overline{) 10} - 0 \\ 2 \overline{) 5} - 1 \\ 2 \overline{) 2} - 0 \end{array}$$

$$0.75 \times 2 = 1.50 \Rightarrow 1$$

$$0.50 \times 2 = 1 \Rightarrow 1$$



## Character representation:

1. BCD  $\rightarrow$  Binary coded decimal
2. EBCDIC  $\rightarrow$  Extended binary coded decimal interchange code
3. ASCII  $\rightarrow$  English (American)
4. ISCII  $\rightarrow$  Indian standard code for information interchange
5. Unicode  $\rightarrow$  local languages

$\Rightarrow$  Character set = 26 uppercase letters, 26 lowercase letters, 0 to 9 digits and special characters are used in computer

$\Rightarrow$  All these character set are denoted through numbers only

### 1. BCD:

$\Rightarrow$  This encoding system is not in the practise ~~to~~ right now.

This  $2^6$  bit encoding system

$\Rightarrow$  can handle  $2^6 = 64$  characters only

### ~~2.~~ 2. ASCII (United States)

$\Rightarrow$  can handle english characters only ( $2^7 = 128$  characters)

$\Rightarrow$  Most of the computers use this system

$\Rightarrow$  Each character has individual numbers

$\Rightarrow$  New version ( $2^8 = 256$  characters i.e., 0 to 255 unique numbers)

$\Rightarrow$  ASCII code is equivalent to the uppercase letter 'A' is 65

$\Rightarrow$  Binary representation of ASCII (7 bit) value 1000001

" " (8 bit) " 01000001

### 3. ~~ASCII~~ EBCDIC

$\Rightarrow$  Similar to ASCII code with 8 bit representation

$\Rightarrow$  Formulated by IBM

ISCII  $\Rightarrow$  Handles the character of Indian local languages



⇒ can handle 256 characters ( $2^8$ )  
EBCDIC ⇒ the input code in ASCII can be converted to EBCDIC system and vice-versa

ASCII ⇒ Now, it is integrated with unicode  
unicode:

⇒ It was generated to handle all the coding system of universal languages

⇒ 16 bit code can handle 65536 characters

Computer Organization vs Computer Architecture:

Computer Organization      Computer Architecture

- \* Computer organization refers to the operational units and their interconnections that realize the architectural specifications
- \* Computer Architecture refers to those parameters of a computer system that are visible to a programmer or those parameters that have a direct impact on the logical execution of a program.

- \* Examples of computer organizational attributes include those hardware details transparent to the programmer
- \* Examples of Architecture include instruction set, the no. of used to represent different datatypes, I/O mechanism etc.

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