

17-04-2023

3. POLARIZATION

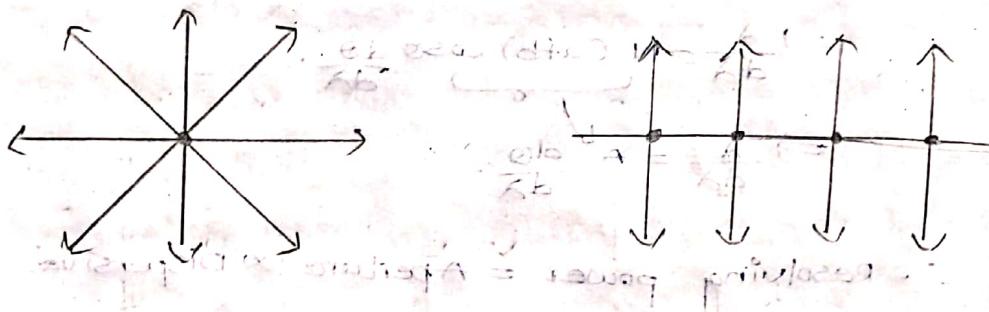
Introduction.

* Polarization: One-sidedness of Light.

→ The phenomenon of restricting the vibrations of electric vector E of light, in a particular plane is called the polarization of light.

* Unpolarized Light:

→ The light wave that has vibrations in all directions perpendicular to the direction of propagation of light is known as unpolarized light.



* Plane polarized light:

→ The light wave that has vibrations in one plane is said to be plane polarized light.

→ The vibrations along one straight line perpendicular to the direction of propagation of light is called plane polarized light.

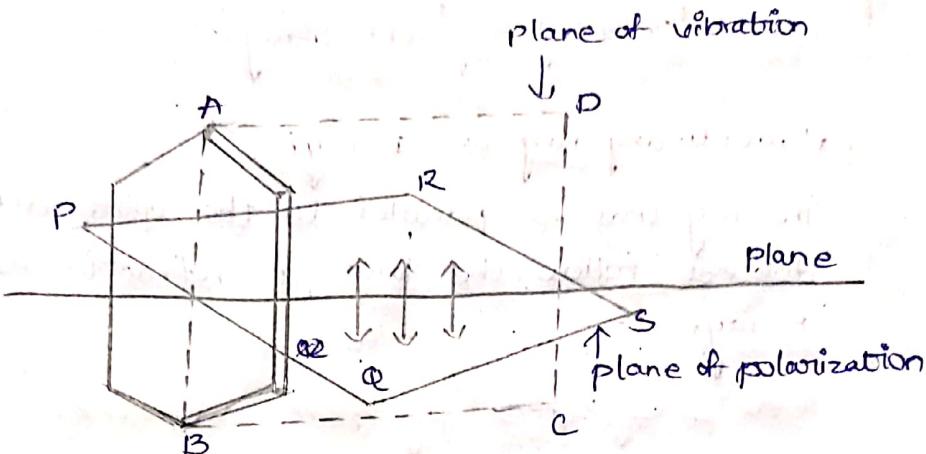


* Plane of vibration:

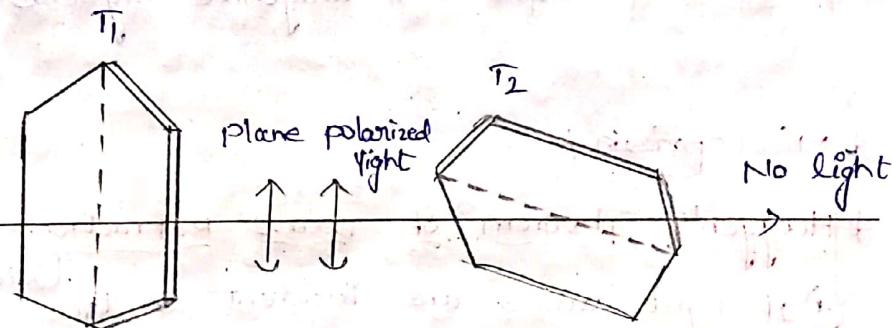
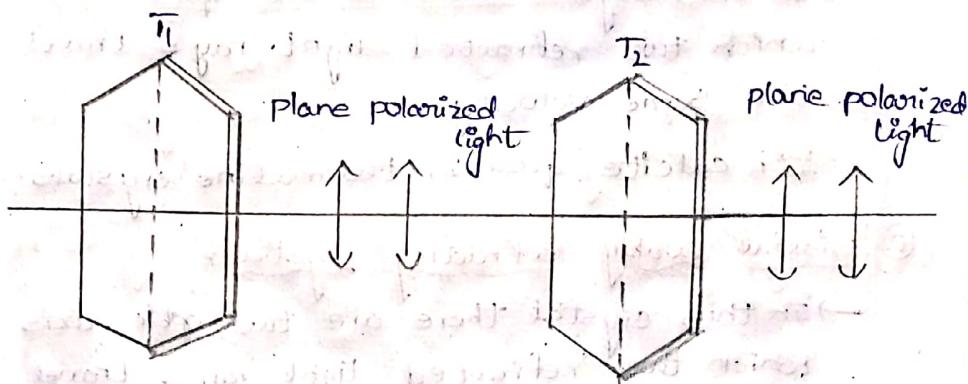
→ A plane in which the vibrations of polarized light are confined is called plane of vibration of plane polarized light.

* Plane of polarization:

→ The plane perpendicular to plane of vibration is called the plane of polarization of plane polarized light.



* Transverse Nature of Light:



* Double Refraction and doubly Refracting crystals:

→ The phenomenon in which incident light ray splits into ordinary (or) O-ray and extraordinary (or) E-ray by quartz, calcite or tourmaline crystals is called as 'double refraction' & the crystals which show double refraction are called as 'doubly refracting crystals'.

ordinary ray (o-ray) :-

→ The ray that is perpendicular to the optic axis and ~~does not~~ follow the laws of refraction is called ordinary ray (or) O-ray.

Extraordinary ray (or) E-ray :-

→ The ray that is parallel to the optic axis and ~~does not~~ follow the laws of refraction is called E-ray.

* Types of doubly refracting crystals :-

① Uniaxial doubly refracting crystal :-

→ In this crystal there is one optic axis along which two refracted light rays travel with the same velocity.

Ex calcite, quartz, tourmaline crystals.

② Biaxial doubly refracting crystal :-

→ In this crystal there are two optic axis along which two refracted light rays travel with same velocity.

Ex mica, topaz and corundum crystals.

* Nicol prism :-

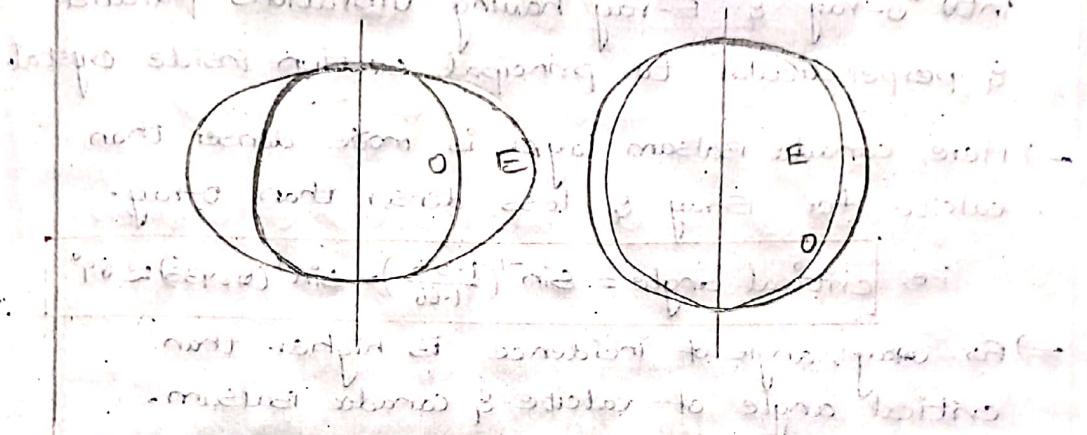
* Huygen's Theorem of Double Refraction [Based on Secondary wavelets]

① If light waves are incident on the surface of uniaxial doubly refracting crystals, each point on the surface of crystal becomes the origin of two secondary wavelets, O-ray & E-ray

② The wavefront of O-ray is spherical because it travels with same velocity in all directions.

③ The wavefront of E-ray is ellipsoid because it travels with different velocity in different directions.

- ④ Along optic axis, the velocities of O-ray and E-ray are constant.
- ⑤ In negative crystals (calcite) $v_O > v_E$, hence $v_O < v_{UE}$. This means that velocity of E-ray is greater than O-ray inside the crystal. so, spherical wavefront lies inside the ellipsoid as shown. in fig (a).
- ⑥ In positive crystals $v_O < v_E$, hence $v_O > v_{UE}$. This means velocity of O-ray is greater than E-ray inside crystal. so, spherical wavefront lies outside ellipsoid in fig (b).



* Nicol prism:

→ In 1828, William Nicol invented an optical device used for producing & analyzing plane polarized light.

Principle:

→ Nicol prism is based on phenomenon of double refraction.

→ In Nicol, O-ray is eliminated by total internal reflection & E-ray is transmitted through crystal

which is plane polarized light.

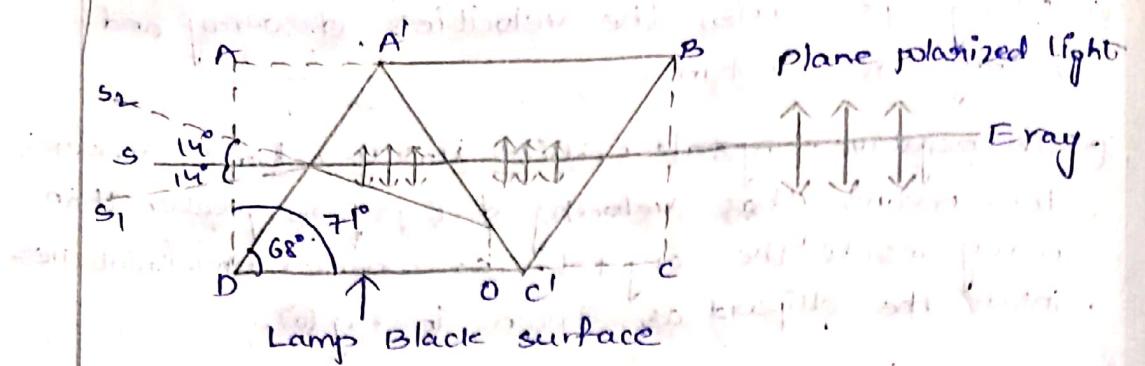
Construction:

→ consider a calcite crystal whose length is 3 times its width.

→ cut it so that it makes 90° with two end faces.

→ The two surfaces are ground, polished optically flat and then cemented together with a transparent material called Canada Balsam.

→ For sodium light, refractive indices are 1.66, 1.55 & 1.49 for O-ray, Canada balsam and E-ray respectively.



Working

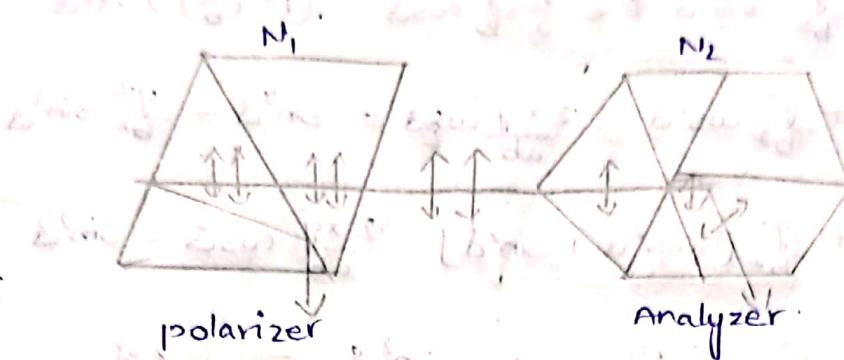
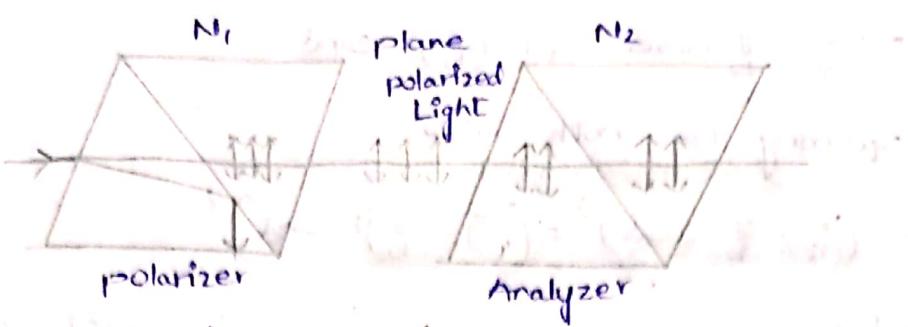
- If an ordinary light falls on face A'D, it splits into 'O-ray' & 'E-ray' having vibrations parallel & perpendicular to principal section inside crystal.
- Here, Canada Balsam layer is more denser than calcite for E-ray & less denser than O-ray.

i.e. $\text{critical angle} = \sin^{-1}\left(\frac{1.55}{1.66}\right) = \sin^{-1}(0.933) \approx 69^\circ$.

- For O-ray, angle of incidence is higher than critical angle of calcite & Canada Balsam.
- By Total Internal reflection, 'O-ray' is reflected from layer of Canada Balsam & absorbed by lamp black surface.
- 'E-ray' transmitted from Canada balsam layer is plane polarized light.
- In this way, Nicol prism acts as a polarizer.

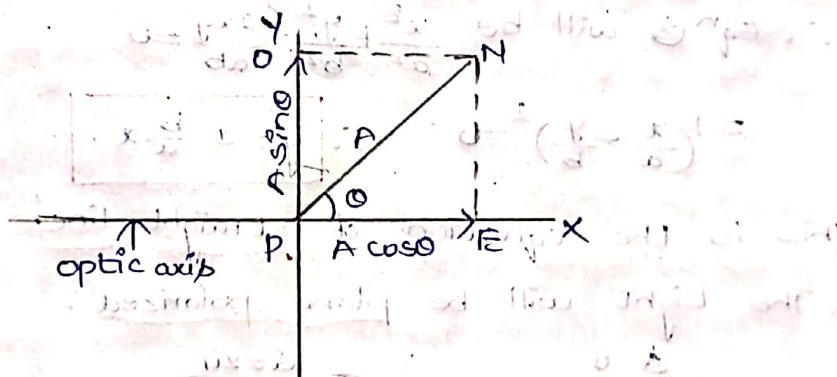
Nicol prism as an Analyzer

- If two Nicol prisms N₁ & N₂ are parallel then only E-ray passes through them. Here First Nicol acts as polarizer and other acts as analyzer.
- When second Nicol is gradually rotated then intensity of E-ray decreases.
- If N₁ & N₂ are perpendicular then no light comes out. Here, if N₂ is rotated, then intensity of emergent light increases.
- In this way, Nicol prism acts as an Analyzer.



* Mathematical Treatment for Production and Analysis of plane, circularly and Elliptical polarized Light.

→ Let a beam of plane polarized light fall normally on a calcite crystal cut with faces parallel to optic axis.



For E-ray, $x = A \cos \theta \sin(\omega t + \delta)$ [δ is phase difference]

For O-ray, $y = A \sin \theta \sin \omega t$

Let $a = A \cos \theta$, $b = A \sin \theta$.

$$\Rightarrow x = a \sin(\omega t + \delta) \Rightarrow \frac{x}{a} = \sin \omega t \cos \delta + \cos \omega t \sin \delta \quad \text{--- (1)}$$

$$\Rightarrow y = b \sin \omega t \Rightarrow \frac{y}{b} = \sin \omega t \quad \text{--- (2)}$$

From (1) & (2) [substitute (2) in (1)].

$$\Rightarrow \frac{x}{a} = \frac{y}{b} \cos \delta + \cos \omega t \sin \delta$$

$$\Rightarrow \frac{x}{a} = \frac{y}{b} \cos \delta + \sqrt{1 - \left(\frac{y}{b}\right)^2} \sin \delta \quad \left[\because \cos^2 \omega t + \sin^2 \omega t = 1 \right]$$

$$\Rightarrow \frac{x}{a} - \frac{y}{b} \cos \delta = \sqrt{1 - \left(\frac{y}{b}\right)^2} \sin \delta$$

squaring on both sides

$$\Rightarrow \left(\frac{x}{a} - \frac{y}{b} \cos \delta\right)^2 = \left(\sqrt{1 - \left(\frac{y}{b}\right)^2} \sin \delta\right)^2$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} \cos^2 \delta - 2 \cdot \frac{x}{a} \cdot \frac{y}{b} \cos \delta = (1 - \left(\frac{y}{b}\right)^2) \sin^2 \delta.$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} \cos^2 \delta - 2 \frac{xy}{ab} \cos \delta = \sin^2 \delta - \frac{y^2}{b^2} \sin^2 \delta$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} [\cos^2 \delta + \sin^2 \delta] - 2 \frac{xy}{ab} \cos \delta = \sin^2 \delta$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} - 2 \frac{xy}{ab} \cos \delta = \sin^2 \delta. \quad \rightarrow \textcircled{3}$$

∴ Equation $\textcircled{3}$ is 'General equation of ellipse'

case-1:

If $\delta = 0, 2\pi, 4\pi, \dots, (2n)\pi$ then $\cos \delta = 1$ and $\sin \delta = 0$.

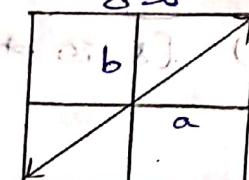
$$\therefore \text{Eqn } \textcircled{3} \text{ will be } \frac{x^2}{a^2} + \frac{y^2}{b^2} + 2xy = 0$$

$$\Rightarrow \left(\frac{x}{a} - \frac{y}{b}\right)^2 = 0 \quad \therefore y = \pm \frac{b}{a}x.$$

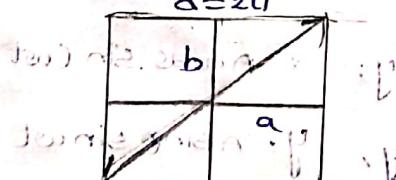
This is the equation of straight line.

∴ The light will be plane polarized.

$$\delta = 0$$



$$\delta = 2\pi$$



case-2:

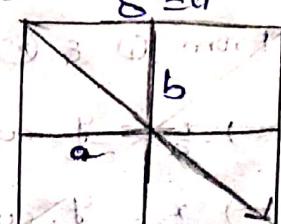
If $\delta = \pi, 3\pi, 5\pi, \dots, (2n+1)\pi$ then $\cos \delta = -1, \sin \delta = 0$.

$$\therefore \frac{x^2}{a^2} + \frac{y^2}{b^2} + 2xy = 0 \Rightarrow \left(\frac{x}{a} + \frac{y}{b}\right)^2 = 0 \quad \delta = \pi$$

$$\therefore y = -\frac{b}{a}x$$

This is again equation of straight line.

∴ Light will be plane polarized.

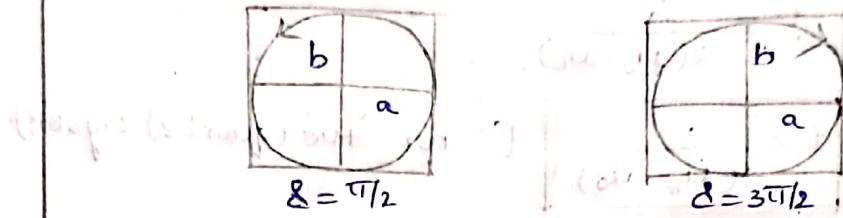


case - 3 :

If $\delta = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots, (2n+1)\frac{\pi}{2}$ and $a \neq b$, then
 $\cos \delta = 0$ & $\sin \delta = 1$.

$$\therefore \boxed{\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1} \rightarrow \text{Ellipse equation.}$$

\therefore Light will be elliptically polarized.



case - 4 :

If $\delta = (2n+1)\frac{\pi}{2}$ and $a = b$, then $\cos \delta = 0$ & $\sin \delta = 1$

$$\therefore \boxed{x^2 + y^2 = a^2} \rightarrow \text{circle equation}$$

\therefore Light will be circularly polarized. [$90^\circ = 45^\circ$].



*Retardation Plates:

\rightarrow It is used to produce a phase difference b/w ordinary & extraordinary rays [O-ray & E-ray] during transmission through doubly refracting crystals.

\rightarrow These are two types:

① Quarter-wave plate

② Half-wave plate

① Quarter-wave plate:

Here phase difference $= \frac{\pi}{2}$

path difference $= \frac{\lambda}{4}$

We have, $\Delta = (\mu_0 - \mu_E)t$. $\left[\because \mu_0 = \text{refractive index of O-ray \& E-ray} \right]$

$$\Rightarrow \frac{\lambda}{4} = (\mu_0 - \mu_E)t$$

$$\Rightarrow t = \frac{\lambda}{4(\mu_0 - \mu_E)}$$

$$\therefore \boxed{t = \frac{\lambda}{4(\mu_E - \mu_0)}}$$

For 'true' (quartz) crystal.

② Half-wave plate :-

Here, phase difference = π .

path difference = $\frac{\lambda}{2}$

We have, $\Delta = (\mu_0 - \mu_E)t$

$$\Rightarrow \frac{\lambda}{2} = (\mu_0 - \mu_E)t$$

$$\therefore t = \frac{\lambda}{2(\mu_0 - \mu_E)}$$

$$\boxed{t = \frac{\lambda}{2(\mu_E - \mu_0)}} \quad [\rightarrow \text{for 'ice' (quartz) crystal}]$$

* Production of plane polarized, circularly and Elliptically polarized Light.

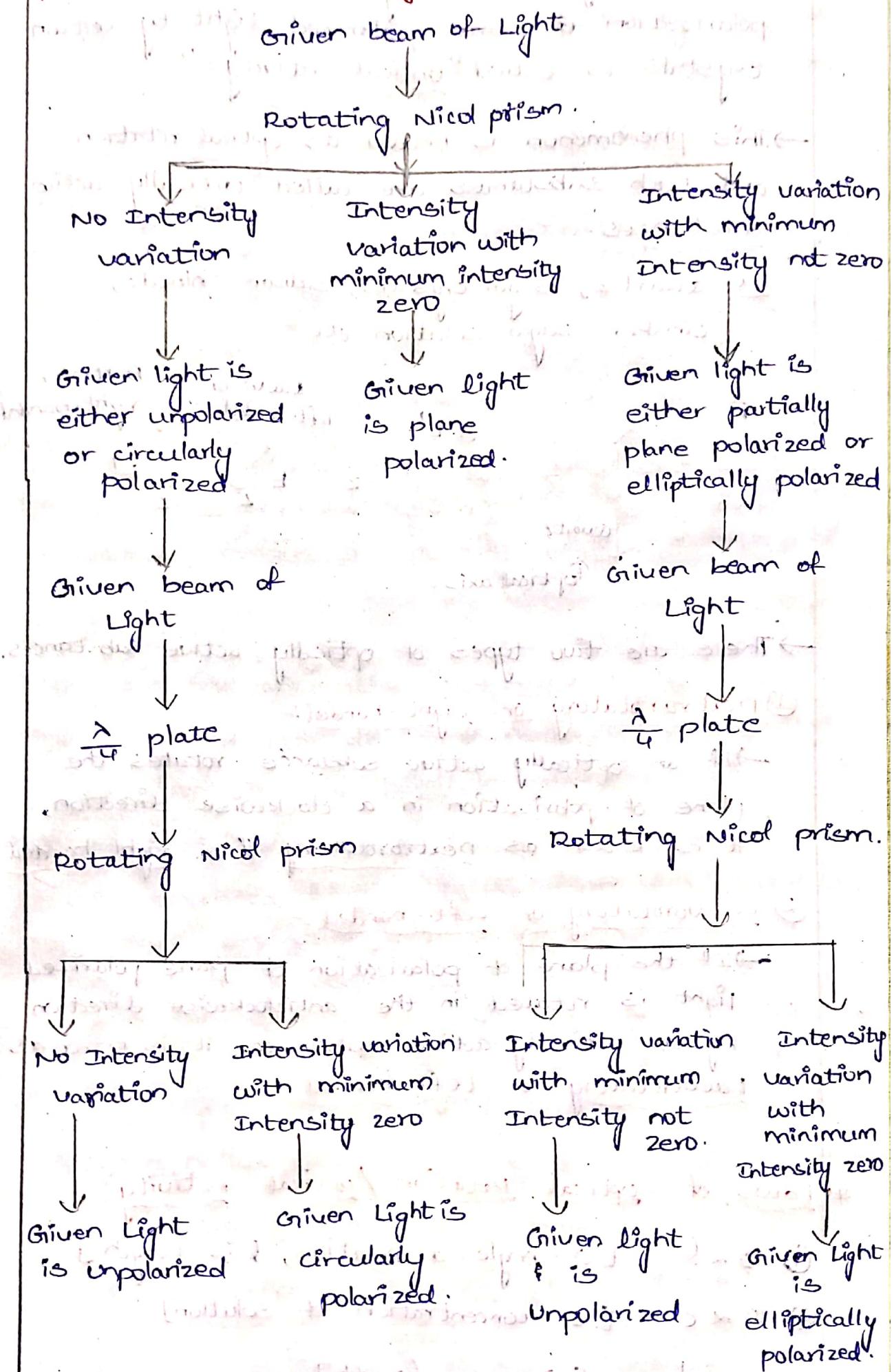
→ When the plane polarized light emergent from a Nicol prism is allowed to fall on a quarter-wave plate such that its vibrations make an angle of α with optic axis of quarter-wave plate.

→ ① For $\alpha = 0^\circ$, and 90° , the emergent light remains plane polarized.

② For $\alpha = 45^\circ$ - circularly polarized.

③ For α value other than $0^\circ, 45^\circ, 90^\circ$ - Elliptically polarized.

* Detection of unpolarized, polarized, circularly polarized & Elliptically polarized Light

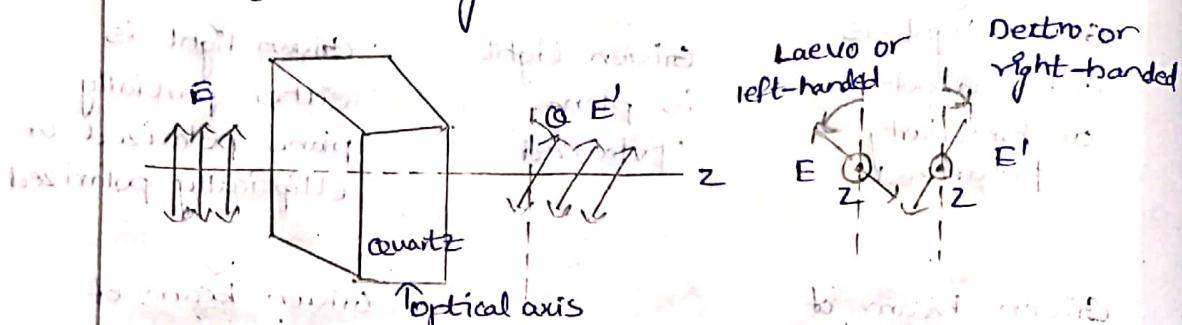


* Optical activity

→ The property of rotating the plane of polarization of plane polarized light by certain crystals is called "optical activity".

→ This phenomenon is known as optical rotation and such substances are called "optically active substances".

Ex:- quartz, sugar crystals, sodium chloride, cinnabar sugar solution etc.



→ There are two types of optically active substances.

(1) Dextrorotatory or right-handed :-

→ If an optically active substance rotates the plane of polarization in a clockwise direction, it is known as dextrorotatory or right-handed.

(2) Laevorotatory or left-handed :-

→ If the plane of polarization of plane polarized light is rotated in the anticlockwise direction by an optically active substance, it is known as Laevorotatory or left-handed.

* Laws of optical rotation / optical activity :-

$$① \theta \propto l \quad [\theta = \text{angle of rotation}, l \text{ is length}]$$

$$② \theta \propto c \lambda \quad [c = \text{concentration of solution}]$$

$$③ \theta \propto \frac{1}{\lambda^2} \quad [\lambda = \text{wavelength}]$$

$$④ \theta = \theta_1 \pm \theta_2 \pm \theta_3 \pm \dots$$

* Specific Rotation:

→ It is defined as the optical rotation 'θ' produced by one decimeter of solution containing one gram of optically active substance per cc of solution.

$$\theta = \frac{\alpha}{l c}, \text{ degree (dm)}^{-1} \left(\frac{\text{gm}}{\text{cc}} \right)^{-1}$$

If length of liquid is in centimeter:

$$\theta = \frac{10\alpha}{l c}$$

* Laurent's Half-shade Polarimeter:

→ It is an optical device used for measuring the optical rotation of optically active substances.

Construction:

O → a monochromatic light source,

S → a slit to obtain monochromatic light emitted from 'O' in a particular direction.

L → a convex lens to convert monochromatic light emitted from 'O' in the form of a parallel beam.

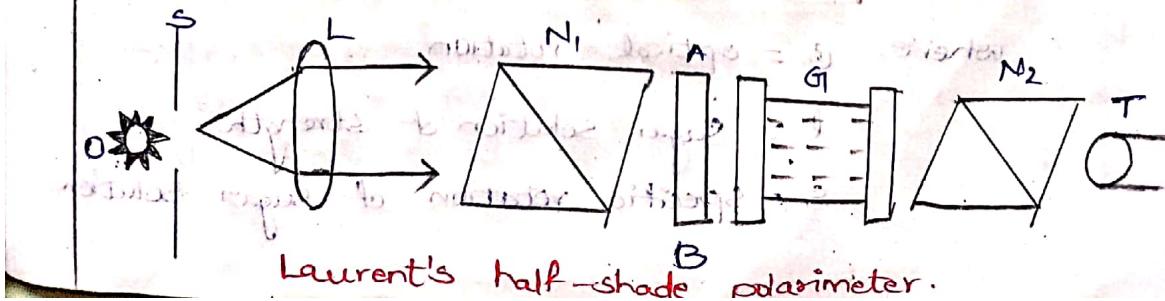
N → a Nicol prism, acts as polarizer.

AB → a circular plate [Half-shade device / Laurent's plate].
Its left-half part is made of glass & right-half part is of quartz.

G → a hollow tube for filling optically active substance.

N₂ → a Nicol prism, acts as Analyzer.

T → a telescope to observe optical rotation.

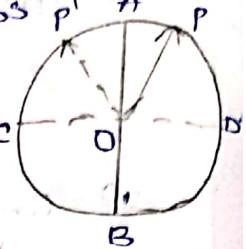


Laurent's half-shade polarimeter.

Working :-

→ The light passing through 'N₁' is incident on 'AB' with its vibration along OP.

→ on passing through its semicircle glass plate half part 'ACB', its vibration remain along OP & on passing through 'APB', Light ray splits into 'O-ray' & 'E-ray'.



→ vibrations of 'O-ray' & 'E-ray' are along OP & OA.

→ Semicircle quartz-half part acts as $\frac{\lambda}{2}$ plate & gives a phase difference of π .

→ on emergence from plate AB, vibrations of O-ray occur along OC instead of OD. $\angle POA = \angle P'OA$.

→ Observations when we analyze the light coming out of analyzer N₂ are :-

- ① If principal plane of N₂ || to OP, glass-half part appears brighter.
- ② If principal plane of N₂ || to OP', quartz-half part appears brighter.
- ③ If principal plane of N₂ || to AOB, Both quartz and glass-half-parts appear equally bright.
- ④ If principal plane of N₂ || is normal to AOB, Both appear equally less brighter than case ③.

Determination of strength of sugar solution :-

$$\theta = \frac{S}{l \times c}$$

where, θ = optical rotation

l = sugar solution of strength

S = specific rotation of sugar solution

LASERS

* LASER [Einstein, 1917]

→ LASER = Light amplification by stimulated Emission of Radiation.

→ Laser is a monochromatic, collimated, unidirectional 'intense' & highly coherent beam of light with small divergence.

Characteristics :-

- ① The Laser beam is completely coherent.
- ② The Laser beam is perfectly monochromatic.
- ③ It emits radiation only in one direction [unidirectional]
- ④ Laser beam is highly intense due to concentrated energy in a very small region.

$$I = \frac{P}{\pi r^2} \quad P - \text{Power}$$

r - distance

- ⑤ Light from laser is brighter than ordinary source.

$$\text{Brightness} = \frac{\text{Power of source}}{\text{Area} \times \text{solid angle}}$$

* Concept of coherence :-

→ If the phase difference b/w two light beams is constant with time, then beams are said to be coherent.

→ There are two types of coherency.

① Temporal coherence :-

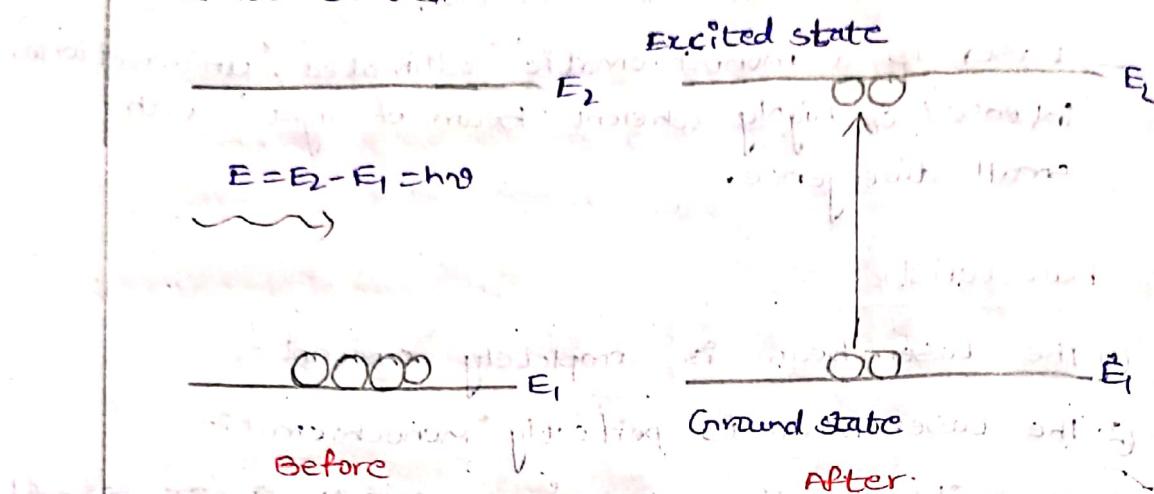
→ Here phase difference b/w two points along the direction of wave propagation remains constant.

② Spatial or Lateral coherence :-

→ If the phase difference b/w two points on a plane perpendicular to direction of propagation is constant, then it is called spatial / lateral coherence.

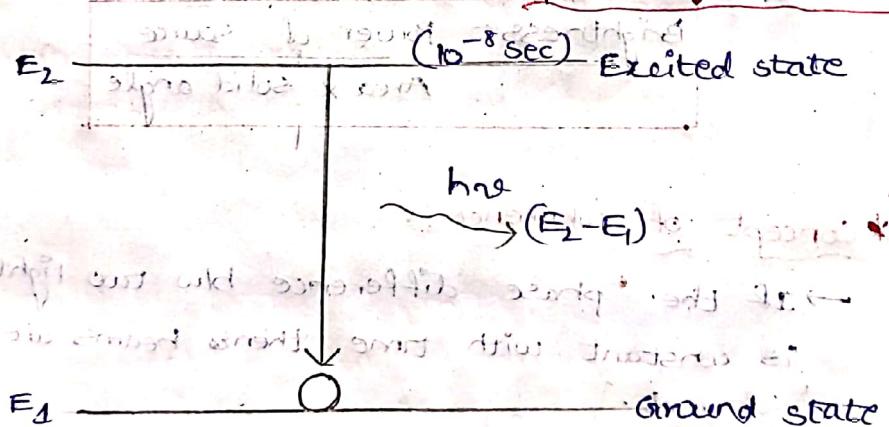
* Absorption of Radiation:

→ It is the process in which a photon is absorbed by the atom & increasing the no. of atoms to its excited state.



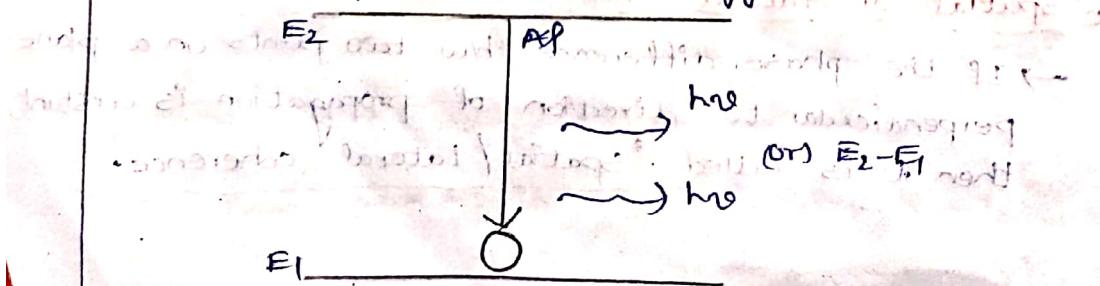
* Spontaneous Emission of Radiation:

→ When an atom in its excited state E_2 makes a transition to its ground state by emitting a photon of energy $(E_2 - E_1)$ without any outside influence, then it is called spontaneous Emission.



* Stimulated Emission of Radiation:

→ It is the process by which an atom is induced with a photon, to make transition from higher energy level to lower energy level by emitting an additional photon of same energy.



Note : [Einstein coefficient].

→ The probability of absorption transition is proportional to energy density of radiation of frequency.

$$P \propto u(v) \Rightarrow P_{12} = B_{12} u(v)$$

Einstein coefficient

① For spontaneous emission,

$$P_{21} = A_{21}$$

② Total probability for transition $2 \rightarrow 1$ is

$$P_{21} = A_{21} + B_{21} u(v).$$

* Differences between spontaneous & stimulated emission

Spontaneous emission	stimulated emission.
① Transition from higher to lower energy without outside influence.	① Transition from higher to lower energy by emitting photon's energy due to induced atom.
② It is Incoherent	② It is coherent.
③ It is Less intense	③ It is Highly Intense.
④ It has a broad spectrum.	④ It has single wavelength.

* Population Inversion

→ It is necessary phenomenon for working of laser.

→ It is to increase the probability of stimulated emission, the no. of atoms in higher energy state (N_2) must be greater than no. of atoms in lower state (N_1).

$$\frac{N_2}{N_1} = e^{-(E_2 - E_1)/kT}$$

where k = Boltzmann constant

T = Temperature

→ The system where population inversion is achieved is active system.

* Pumping:

→ The process by which we can raise atoms from 'lower to higher energy' state is called Pumping.

① Optical pumping:

→ It is the process in which population inversion can be achieved by providing optical energy to ground state atoms.

② Electrical pumping:

→ It is used for population inversion in 'gas lasers' such as He-Ne laser.

③ Direct electric pumping:

→ Here electric current directly creates enough mobile charges at interphase of two different types of semiconductors. Ex: GaAs laser.

④ chemical pumping:

→ The exothermic chemical reactions generate enough heat energy to utilize for pumping the atoms to higher energy levels. Ex: CO₂ laser.

* optical cavity or optical Resonator:

→ An arrangement of pair of mirrors in which the active material is placed in between is known as optical Resonator.

→ Advantages:-

① It increases monochromaticity.

② It improves coherence.

③ It reduces pumping power requirements.

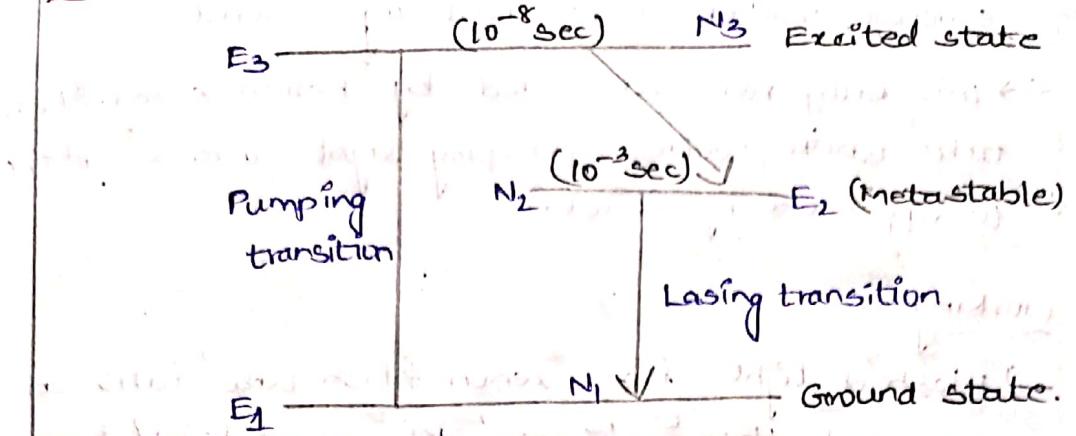
④ It controls reflection rate & beam quality.

⑤ It improves gain of laser medium.

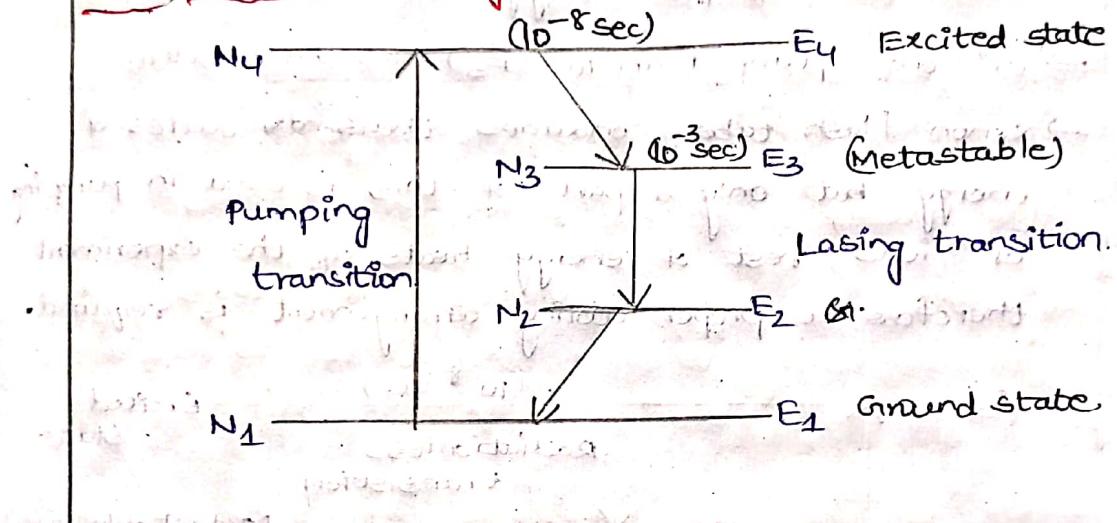
$$\text{Laser gain} = \frac{P_{\text{out}}}{P_{\text{in}}} \quad [\text{Power of outgoing beam}]$$

$$P_{\text{in}} \quad [\text{Power of incoming beam}]$$

* Three Level Laser system



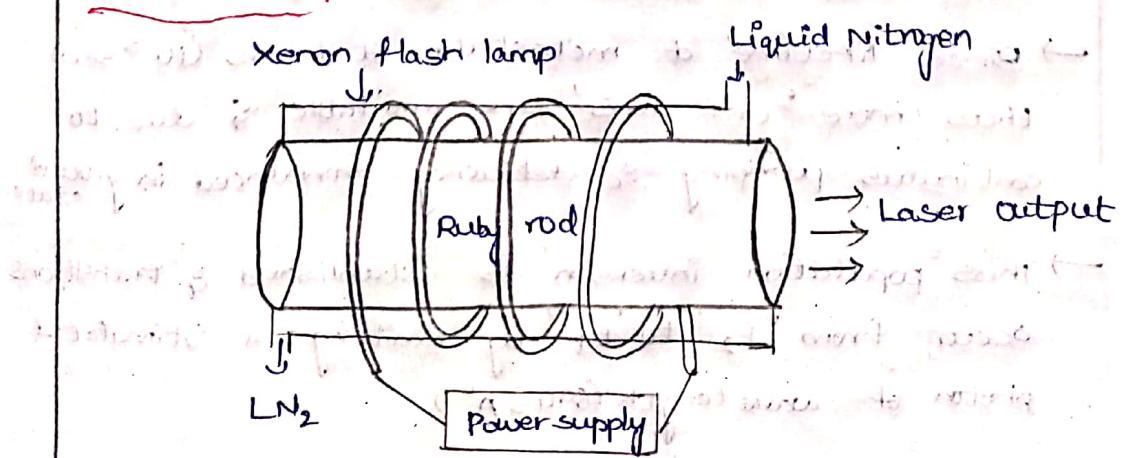
* Four Level Laser system



* Ruby Laser: [solid state Laser].

- It was first laser developed by Maiman, in 1960, based on 3-energy level system.
- Ruby is a crystal of Al_2O_3 doped with Cr_2O_3 .
- Ruby laser operates in a 'pulse mode laser beam' of wavelength 6943 \AA .

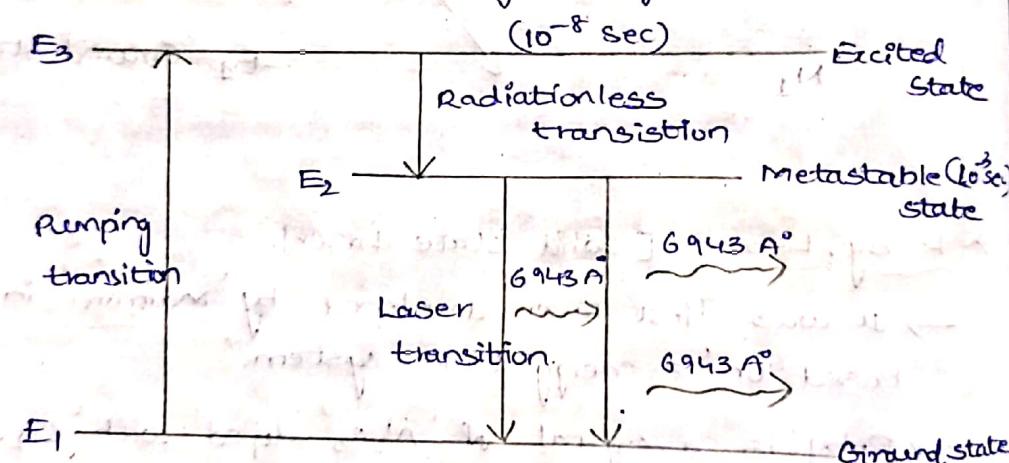
Construction:



- Ruby rod - cylindrical - one end is optically 'coupled' silvered, another end is partially silvered.
- This Ruby rod surrounded by helical xenon flash tube which provides pumping light to misc. Cr^{+3} ions to upper energy level.

Working:

- Flash of light from xenon flash tube falls on ruby rod, then Cr^{+3} ions in ground level/state absorb light of wavelength [$5000\text{-}6000\text{\AA}$] 5500\AA & excited to upper energy state.
- Cr^{+3} ions pumped in to (E_3) . as shown below
- xenon flash tube consumes thousands joules of energy but only a part of this is used in pumping Cr^{+3} ions, rest of energy heats up the experiment therefore a proper cooling arrangement is required.



- Due to small mean lifetime of atoms (10^{-8} sec) some atoms jump back to 'ground state' & some jump to 'metastable state' (E_2).
- Since lifetime of metastable state is (10^{-3} sec) thus more ' Cr^{+3} ions' are available & due to continuous pumping & deficiency pronounced in ground state.
- Thus 'population inversion' is established & transitions occur from ' E_2 ' to ' E_1 ' by emitting a stimulated photon of wavelength (6943\AA°)

Draw Backs:

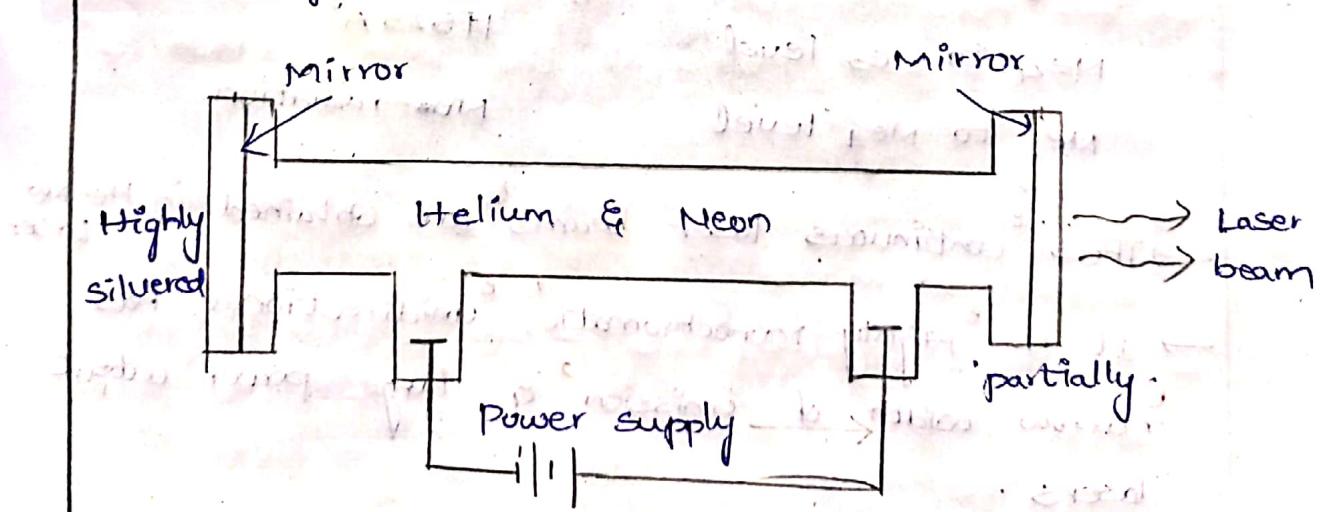
- ① Due to '3-level system', high power pumping system is required for population inversion.
- ② The output beam occurs in the form of micro-second's duration of 'pulses'.
- ③ Efficiency is very low because it uses only green part of pumping light.

* Helium-Neon (He-Ne) Laser [gas laser]

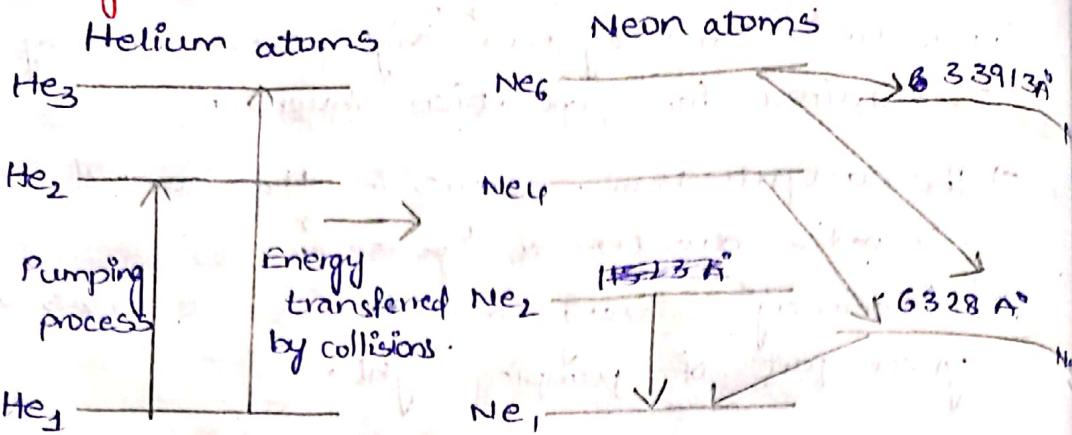
- It is based on 4-level laser system.
- It uses a mixture of 'He' & 'Ne' in ratio 10:1 or 7:1 at low pressure.
- It is superior to Ruby Laser because it gives continuous laser beams of wavelength 6328 Å , 33913 Å and 11523 Å .

construction

- It consists of glass tube of length 10-100 cm & narrow diameter of 2-10 mm.
- one end is highly silvered & other is partially silvered.
- Two electrodes are inserted in tube to get high power to achieve population inversion by electric discharge method.



Working:



Energy level diagram of He-Ne Laser.

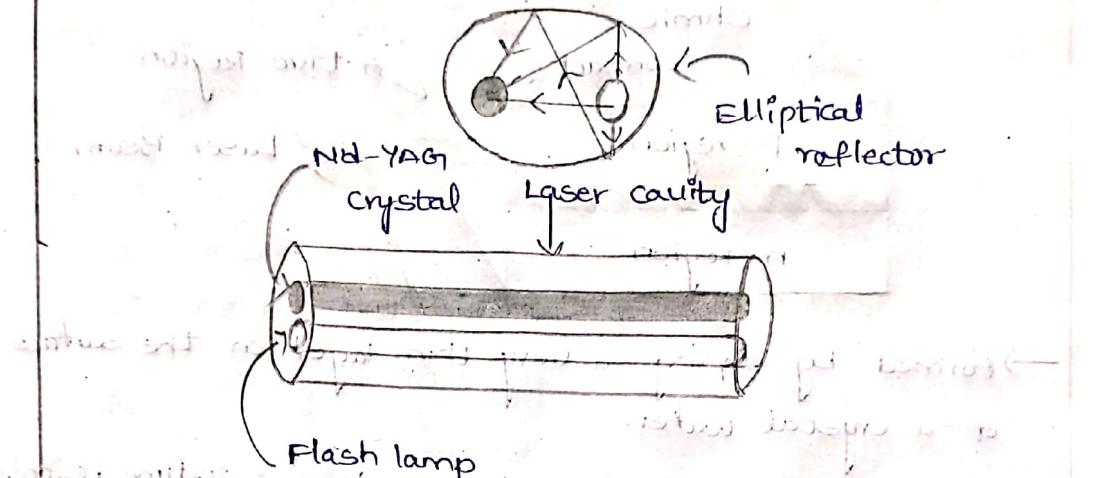
- A 'High voltage' is applied across electrodes to ionize the gas.
- The 'probability of collision' of electrons & ions with 'He' atoms is higher than 'Ne' atoms.
- He atoms reach the higher energy states.
- Some of 'He' atoms collide with 'Ne' atoms and transfer energy to them which excite to Ne₄, Ne₅, Ne₆ levels to achieve population inversion.
- Ne₁, Ne₂, Ne₃ are metastable states for Ne atoms.

Transitions : Radiation [Wavelengths]

Ne ₆ to Ne ₅ level	33913 Å
Ne ₆ to Ne ₃ level	6328 Å
Ne ₄ to Ne ₃ level	11523 Å
Ne ₂ to Ne ₁ level	No radiation.

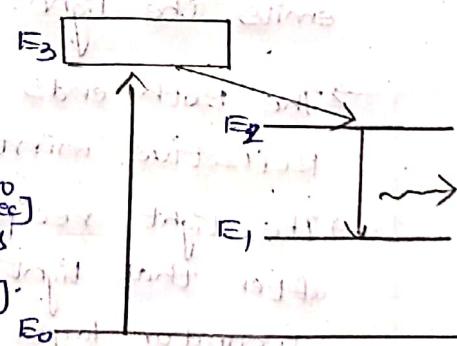
- Thus 'continuous laser beams' are obtained in He-Ne Laser.
- It is 'highly monochromatic', 'unidirectional', has 'narrow width of emission' & 'large power output' lasers.
- In it, atomic inelastic collisions are used as pumping for population inversion.

- * Nd:YAG [Neodymium-doped Yttrium Aluminium garnet] Nd:Y₃Al₅O₁₂] Laser:
- It is optically pumped solid-state laser & 4-level system
 - It is given by Grenier et al. in 1964 at Bell Laboratories
 - construction:
 - It consists of a cylindrical crystal which forms 'laser cavity' & has reflective ends.
 - One end is '100% reflective' other is partial.



Working:

- Population inversion results from shining light on this crystal.
- Light transition from ground state into absorption bands by ~~with~~ a flash lamp.
- Atoms transition efficiently from the E_3 level to upper energy levels.
- The radiative decays to ground state E_0 from these bands have long lifetimes [Micro Sec] as compared to fast transitions to upper energy levels [Nano-sec].

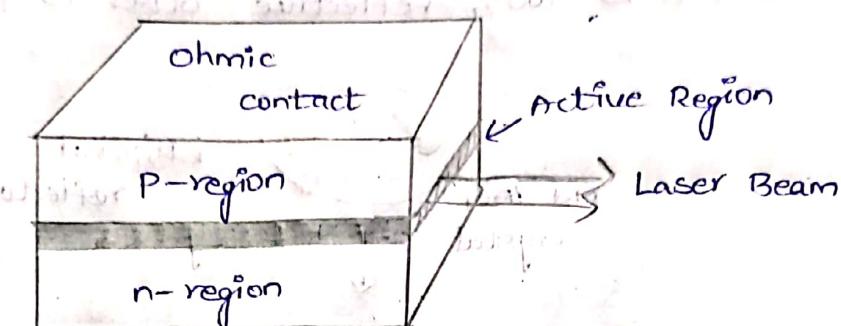


- Approximately 99% of ions are excited to absorption band transfer to the upper energy levels.
- Due to long lifetime [milli seconds], these levels de-excite solely due to spontaneous emission.

* Semiconductor Laser:

- It is a laser diode in which the active medium is a semiconductor similar to that found in a light-emitting diode.
- It is formed from a p-n junction & powered by injected electrical current.

construction:



- Formed by doping a very thin layer on the surface of a crystal wafer.
- Crystal is doped to produce n-type & p-type regions and results a p-n junction diode.
- The junction surface of diode lasers is polished at two sides.

Working:

- When forward voltage is applied, electrons combine with holes at the p-n junction & emits the light.
- The both ends of active layer acts as a reflective mirror.
- The light reciprocates in the active layer. after that light is amplified and the semiconductor layer oscillation is generated.

Advantages:

- small in size and low cost
- Having high efficiency
- construction is very simple.

Disadvantages :-

- It depends on temperature.
- Due to lower power consumption it is not suitable for many laser applications.

Applications :-

- Used in telecommunications.
- Used for Barcode readers.
- Used in measuring instruments like Range-finders.
- Infrared & red laser diodes are common in CD players, CD-ROMs and DVD technology.

* Applications of Lasers:-

- ① In communications.
- ② In welding & cutting.
- ③ In surgery. [Medical].
- ④ In computer industry.
- ⑤ In Holography.
- ⑥ In spectroscopy.
- ⑦ In scientific and industrial Research.