Isotropic smoothing of image via Heat equation

import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.colors as colors
from skimage import color
from skimage import io
```

load input image

filename for the input image is 'barbara_color.jpeg'

check the size of the input image

convert the color image into a grey image

```
print('number of rows of I = ', num_row)
print('number of columns of I = ', num_column)

number of rows of I = 512
number of columns of I = 512
```

normalize the converted image

 normalize the converted grey scale image so that its maximum value is 1 and its minimum value is 0

define a function to compute the derivative of input matrix in x(row)-direction

• forward difference : I[x+1,y]-I[x,y]

• backward difference : I[x,y] - I[x-1,y]

```
In [ ]: def compute_derivative_x_backward(I):
```

define a function to compute the derivative of input matrix in y(column)-direction

• forward difference : I[x,y+1]-I[x,y]

• backward difference : I[x,y]-I[x,y-1]

define a function to compute the laplacian of input matrix

```
• \Delta I = 
abla^2 I = rac{\partial^2 I}{\partial x^2} + rac{\partial^2 I}{\partial y^2}
```

- $\Delta I = I[x+1,y] + I[x-1,y] + I[x,y+1] + I[x,y-1] 4*I[x,y]$
- ΔI = derivative_x_forward derivative_x_backward + derivative_y_forward derivative_y_backward

define a function to compute the heat equation of data ${\cal I}$ with a time step

```
• I = I + \delta t * \Delta I
```

```
In [ ]: def heat_equation(I, time_step):
```

run the heat equation over iterations

functions for presenting the results

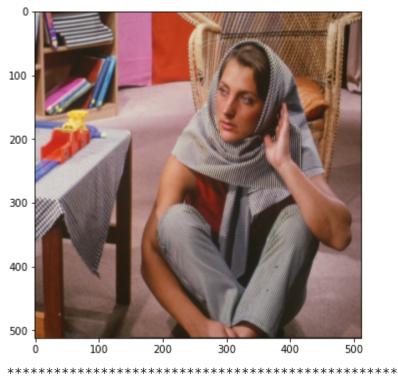
```
In [ ]: def function_result_01():
    plt.figure(figsize=(8,6))
    plt.imshow(I0)
    plt.show()

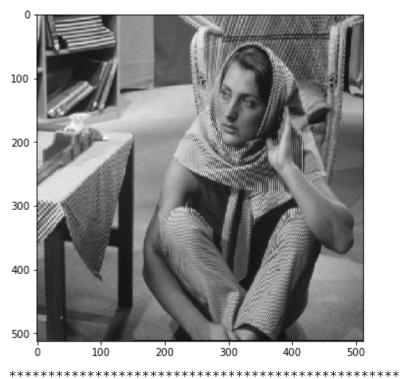
In [ ]: def function_result_02():
    plt.figure(figsize=(8,6))
    plt.imshow(I, cmap='gray', vmin=0, vmax=1, interpolation='none')
    plt.show()
```

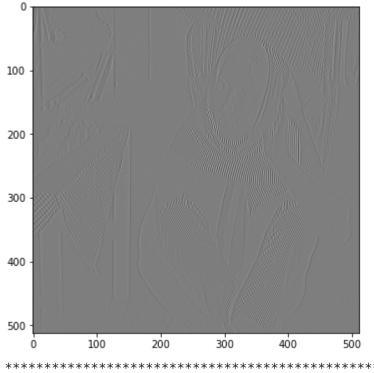
```
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                                                     assignment 04
             def function_result_03():
    In [ ]:
                  L = compute_laplace(I)
                  plt.figure(figsize=(8,6))
                  plt.imshow(L, cmap='gray')
                  plt.show()
    In [ ]:
             def function_result_04():
                  time step
                              = 0.25
                  I update
                              = heat_equation(I, time_step)
                  plt.figure(figsize=(8,6))
                  plt.imshow(I update, vmin=0, vmax=1, cmap='gray')
                  plt.show()
    In [ ]:
             def function_result_05():
                  time_step
                                      = 0.25
                  number_iteration
                                      = 128
                  I_update = run_heat_equation(I, time_step, number_iteration)
                  plt.figure(figsize=(8,6))
                  plt.imshow(I update, vmin=0, vmax=1, cmap='gray')
                  plt.show()
    In [ ]:
             def function result 06():
                  time_step
                                      = 0.25
                  number_iteration
                                      = 512
                  I update = run heat equation(I, time step, number iteration)
                  plt.figure(figsize=(8,6))
                  plt.imshow(I_update, vmin=0, vmax=1, cmap='gray')
                  plt.show()
    In [ ]:
             def function_result_07():
                  L = compute_laplace(I)
                  value1 = L[0, 0]
                  value2 = L[-1, -1]
                  value3 = L[100, 100]
                  value4 = L[200, 200]
                  print('value1 = ', value1)
                  print('value2 = ', value2)
                  print('value3 = ', value3)
                  print('value4 = ', value4)
    In [ ]:
```

```
def function result 08():
              time step
                            = 0.25
              I_update
                           = heat_equation(I, time_step)
              value1 = I_update[0, 0]
              value2 = I update[-1, -1]
              value3 = I_update[100, 100]
              value4 = I_update[200, 200]
              print('value1 = ', value1)
print('value2 = ', value2)
print('value3 = ', value3)
              print('value4 = ', value4)
In [ ]:
          def function result 09():
              time step
                                    = 0.25
              number iteration
                                    = 128
              I update = run heat equation(I, time step, number iteration)
              value1 = I update[0, 0]
              value2 = I update[-1, -1]
              value3 = I_update[100, 100]
              value4 = I update[200, 200]
              print('value1 = ', value1)
              print('value2 = ', value2)
              print('value3 = ', value3)
              print('value4 = ', value4)
In [ ]:
          def function result 10():
                                    = 0.25
              time step
              number iteration
                                    = 512
              I update = run heat equation(I, time step, number iteration)
              value1 = I_update[0, 0]
              value2 = I_update[-1, -1]
              value3 = I update[100, 100]
              value4 = I_update[200, 200]
              print('value1 = ', value1)
              print('value2 = ', value2)
print('value3 = ', value3)
              print('value4 = ', value4)
```

results







[RESULT 04]

