Linear regression

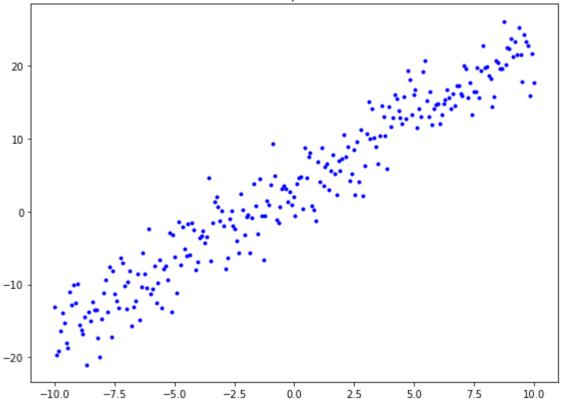
import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load data points

• $\{(x_i, y_i)\}_{i=1}^n$





compute the residual

compute the loss

• useful functions: np.inner

compute the gradient with respect to $heta_0$

• useful functions: np.inner

compute the gradient with respect to $heta_1$

useful functions: np.inner

gradient descent for the optimization

```
theta1
                = 0
list_theta0
                = np.zeros(number iteration)
list thetal
                = np.zeros(number iteration)
list loss
                = np.zeros(number iteration)
for i in range(number iteration):
   # complete the blanks
   theta0 = theta0-(learning_rate*compute_gradient_theta0(x, y, theta0, theta1
   thetal = thetal-(learning_rate*compute_gradient_thetal(x, y, theta0, theta1
         = compute_loss(x, y, theta0, theta1)
   list theta0[i] = theta0
   list_thetal[i] = thetal
   list loss[i]
               = loss
```

functions for presenting the results

```
In [ ]:
         def function_result_01():
             plt.figure(figsize=(8,6))
             plt.plot(x, y, '.', color='blue')
             plt.title('data points')
             plt.show()
In [ ]:
         def function_result_02():
             plt.figure(figsize=(8,6))
             ax = plt.gca()
             plt.plot(list theta0, '-', color='blue', label=r'$\theta 0$')
             plt.plot(list theta1, '-', color='red', label=r'$\theta 1$')
             plt.title('model parameters')
             ax.legend()
             plt.show()
In [ ]:
         def function_result_03():
             plt.figure(figsize=(8,6))
             plt.plot(list_loss, '-', color='blue')
             plt.title('loss curve')
             plt.show()
In [ ]:
         def function_result_04():
```

```
f = theta0 + theta1 * x

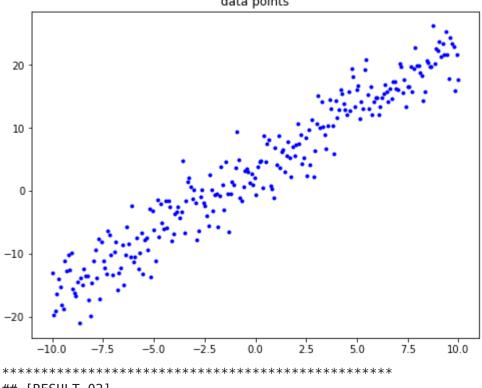
plt.figure(figsize=(8,6))
ax = plt.gca()
plt.plot(x, y, '.', color='blue', label='data point')
plt.plot(x, f, '-', color='red', label='regression')
plt.title('regression')
ax.legend()
plt.show()
```

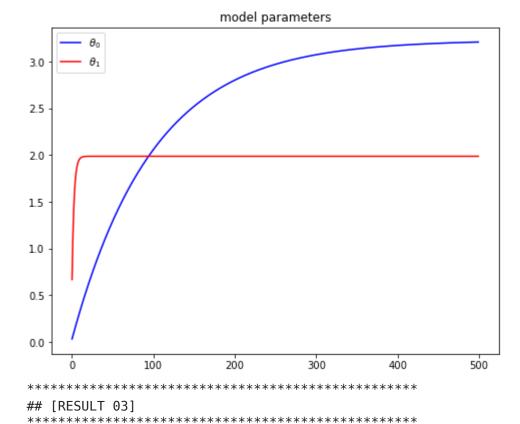
```
In [ ]:
         def function result 05():
             X0 = np.arange(-10, 10, 0.1)
             X1 = np.arange(-10, 10, 0.1)
             grid theta0, grid theta1 = np.meshgrid(X0, X1)
             grid loss
                         = np.zeros(grid_theta0.shape)
             for i, t0 in enumerate(X0):
                 for j, t1 in enumerate(X1):
                     grid_loss[j, i] = compute_loss(x, y, t0, t1)
             fig = plt.figure(figsize=(8,6))
             ax = fig.add_subplot(111, projection='3d')
             plt.title('loss surface')
             ax = plt.axes(projection='3d')
             ax.set_xlabel(r'$\theta_0$')
             ax.set ylabel(r'$\theta 1$')
             ax.set zlabel('loss')
             ax.plot_surface(grid_theta0, grid_theta1, grid_loss, rstride=1, cstride=1, 
             plt.tight layout()
             plt.show()
```

results

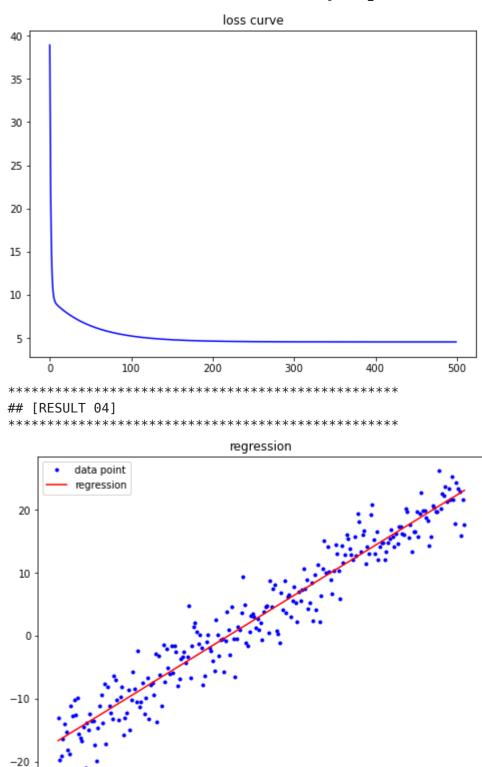
```
print(title)
print('***********************************
eval(name_function)
```







file:///home/kangjunekoo/MachineLearning/MachineLearning/06/assignment_06.html



-2.5

0.0

2.5

5.0

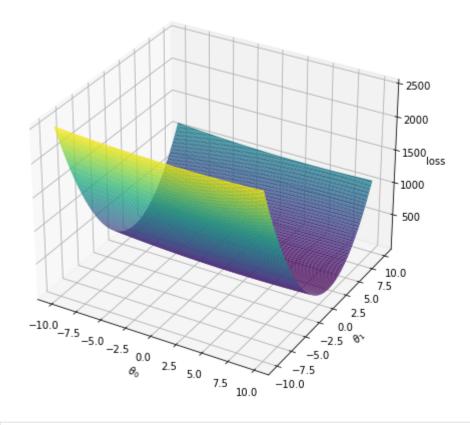
-5.0

-10.0

-7.5

10.0

7.5



In []: