Linear Regression

import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load point data for training and testing

```
In [ ]:
         filename_data
                        = 'assignment_07_data.csv'
                         = np.genfromtxt(filename data, delimiter=',')
         data
         number data
                         = data.shape[0]
         x = data[:, 0]
         y = data[:, 1]
         z = data[:, 2]
         print('number of data = ', number data)
         print('data type of x =', x.dtype)
         print('data type of y =', y.dtype)
         print('data type of z =', z.dtype)
        number of data = 2500
        data type of x = float64
        data type of y = float64
        data type of z = float64
```

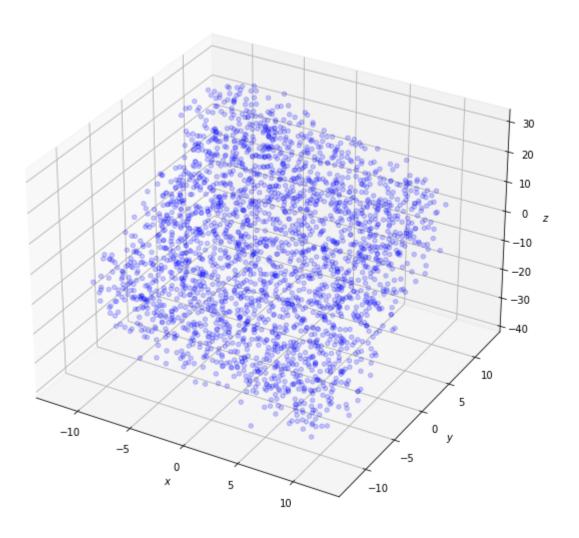
plot the data in the three dimensional space

```
fig = plt.figure(figsize=(12, 8))
ax1 = plt.subplot(111, projection='3d')

ax1.set_xlabel('$x$')
ax1.set_ylabel('$y$')
ax1.set_zlabel('$z$')
ax1.scatter(x, y, z, marker='o', color='blue', alpha=0.2)

plt.title('data points')
plt.tight_layout()
plt.show()
```

data points



compute the prediction function

- $heta=(heta_0, heta_1, heta_2)\in\mathbb{R}^3$
- $x,y\in\mathbb{R}$

compute the loss function

• $heta=(heta_0, heta_1, heta_2)\in\mathbb{R}^3$

• $x,y,z\in\mathbb{R}$

• useful functions: np.inner

compute the gradient for the model parameters heta

• useful functions: np.matmul

```
In [ ]:
      def compute gradient(theta, x, y, z):
         # complete the blanks
         number data = data.shape[0]
                 = compute residual(theta, x, y, z)
          residual
         x=x.tolist()
         y=y.tolist()
         A=[]
          for i in range(len(x)):
            A.append([1,x[i],y[i]])
         A=np.array(A)
         gradient
                   = (1/number_data)*np.matmul(A.T,residual.T)
         return gradient
```

gradient descent for the optimization

```
In [ ]:
       number_iteration
                      = 1000
       learning rate
                       = 0.01
       theta
                   = np.array((0, 0, 0))
       theta iteration = np.zeros((number iteration, len(theta)))
       loss iteration = np.zeros(number iteration)
       for i in range(number_iteration):
          # complete the blanks
          theta
                = theta -learning rate*compute gradient(theta, x, y, z)
                = compute loss(theta, x, y, z)
          loss
          theta iteration[i, :] = theta
          loss iteration[i]
                            = loss
```

functions for presenting the results

```
In [ ]:
    def function_result_01():
        plt.figure(figsize=(8,6))
        plt.title('loss')

        plt.plot(loss_iteration, '-', color='red')
        plt.xlabel('iteration')
        plt.ylabel('loss')

        plt.tight_layout()
        plt.show()
```

```
def function_result_02():
    plt.figure(figsize=(8,6))
    plt.title('model parameters')

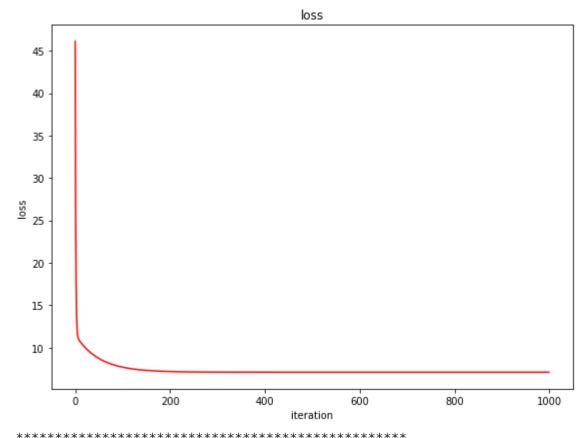
plt.plot(theta_iteration[:, 0], '-', color='red', label=r'$\theta_0$')
    plt.plot(theta_iteration[:, 1], '-', color='green', label=r'$\theta_1$')
    plt.plot(theta_iteration[:, 2], '-', color='blue', label=r'$\theta_2$')

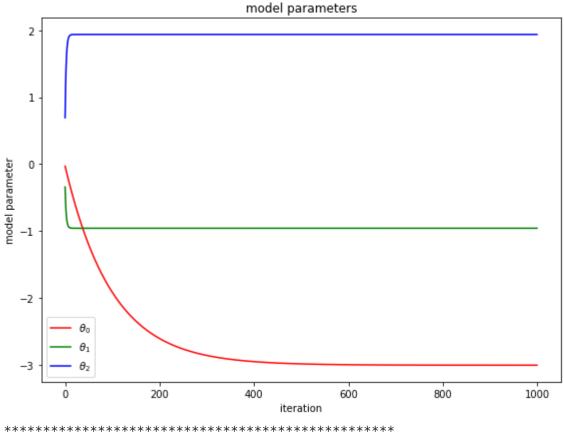
plt.xlabel('iteration')
    plt.ylabel('model parameter')
    plt.legend()
```

```
plt.tight_layout()
plt.show()
```

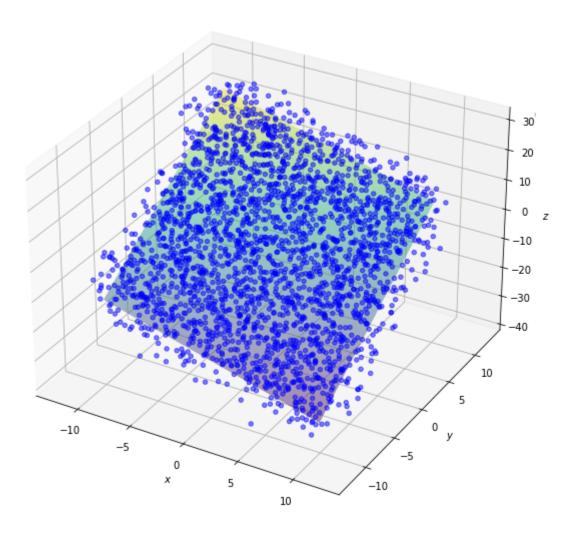
```
In [ ]:
         def function_result_03():
             xx = np.arange(-10, 10, 0.1)
             yy = np.arange(-10, 10, 0.1)
             (grid_x, grid_y) = np.meshgrid(xx,yy)
             zz = theta[0] + theta[1] * grid x + theta[2] * grid y
             fig = plt.figure(figsize=(8,8))
             ax = fig.add subplot(111, projection='3d')
             plt.title('regression surface')
             ax = plt.axes(projection='3d')
             ax.set_xlabel(r'$x$')
             ax.set ylabel(r'$y$')
             ax.set zlabel(r'$z$')
             ax.plot_surface(grid_x, grid_y, zz, rstride=1, cstride=1, cmap='viridis', ec
             ax.scatter(x, y, z, marker='o', color='blue', alpha=0.5)
             plt.tight_layout()
             plt.show()
```

results





regression surface



In []:		