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ECE523 - HWK2

Problem 1:

Determine the symmetrical components for the following currents and sketch a phasor diagram, based on

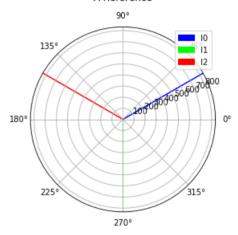
- a) Phase "a" referenced components
- b) Phase "b" referenced components
- c) Phase "c" referenced components

```
In [8]:
                # Define and Display Currents
                currents = [[0,0],
            3
                             [0, -120],
                             [2500,30]]
            4
               phs = ep.phasorlist(currents)
            5
               ep.cprint(phs,label=["IA","IB","IC"])
               # a) "A"-Reference
            8
            9
               symA = ep.abc_to_seq(phs)
          10 ep.phasorplot(symA,legend=["I0","I1","I2"],title="A-Reference",
11 colors=["#0000FF","#00FF00","#FF0000"])
12 ep.cprint(symA,label=["I0","I1","I2"])
           13
                print()
           14
              # b) "B"-Reference
           15
                symB = ep.abc_to_seq(phs, "B")
                ep.phasorplot(symB,legend=["I0","I1","I2"],title="B-Reference",
           17
           colors=["#0000FF","#00FF00","#FF0000"])

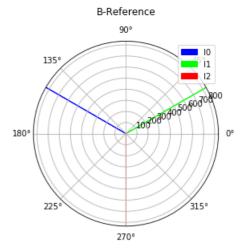
ep.cprint(symB,label=["I0","I1","I2"])
           20 print()
           21
           22 # c) "C"-Reference
           23 symC = ep.abc_to_seq(phs,"C")
           24 ep.phasorplot(symC,legend=["I0","I1","I2"],title="C-Reference", colors=["#0000FF","#00FF00","#FF0000"])
           26 ep.cprint(symC, label=["I0", "I1", "I2"])
           27 print()
```

```
[['IA 0.0 ∠ 0.0°']
['IB 0.0 ∠ -180.0°']
['IC 2500.0 ∠ 30.0°']]
```

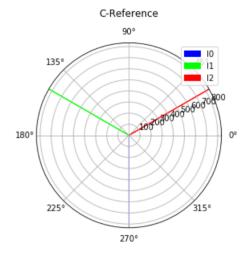
A-Reference



```
[['I0 833.333 \(\neq 30.0\)\"]
['I1 833.333 \(\neq -90.0\)\"]
['I2 833.333 \(\neq 150.0\)\"]
```



```
[['I0 833.333 \(\neq \) 150.0°']
['I1 833.333 \(\neq \) 30.0°']
['I2 833.333 \(\neq \) -90.0°']]
```



[['I0 833.333 ∠ -90.0°'] ['I1 833.333 ∠ 150.0°'] ['I2 833.333 ∠ 30.0°']]

Problem 2:

Repeat problem 1. with the following currents:

```
In [9]:
            # Define and Display Currents
            currents = [[4500, -25.84],
          3
                        [8503,-229.5],
                        [4500,94.16]]
          4
            phs = ep.phasorlist(currents)
          5
            ep.cprint(phs,label=["IA","IB","IC"])
            # a) "A"-Reference
         8
         9
            symA = ep.abc_to_seq(phs)
         ep.cprint(symA,label=["I0","I1","I2"])
         12
         13
            print()
         14
            # b) "B"-Reference
         15
            symB = ep.abc_to_seq(phs, "B")
            ep.phasorplot(symB,legend=["I0","I1","I2"],title="B-Reference",
         17
        colors=["#0000FF","#00FF00","#FF0000"])

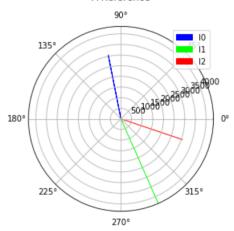
ep.cprint(symB,label=["I0","I1","I2"])
         20 print()
         21
         22 # c) "C"-Reference
         23 symC = ep.abc_to_seq(phs,"C")
         24 ep.phasorplot(symC,legend=["I0","I1","I2"],title="C-Reference", colors=["#0000FF","#00FF00","#FF0000"])
         26 ep.cprint(symC, label=["I0", "I1", "I2"])
         27 print()
```

```
[['IA 4500.0 ∠ -25.84°']

['IB 8503.0 ∠ 130.5°']

['IC 4500.0 ∠ 94.16°']]
```

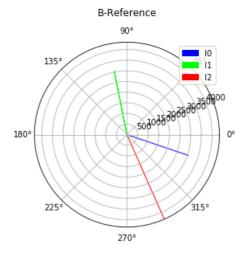
A-Reference



```
[['I0 3056.873 ∠ 101.311°']

['I1 4348.723 ∠ -66.214°']

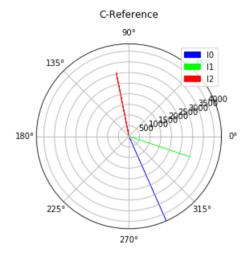
['I2 3056.873 ∠ -18.689°']]
```



```
[['I0 3056.873 ∠ -18.689°']

['I1 3056.873 ∠ 101.311°']

['I2 4348.723 ∠ -66.214°']]
```



[['I0 4348.723 ∠ -66.214°'] ['I1 3056.873 ∠ -18.689°'] ['I2 3056.873 ∠ 101.311°']]

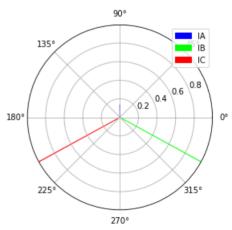
Problem 3:

Determine the phase voltage given the following phase "a" referenced symmetrical components. Repeat assuming they are instead phase "b" and then phase "c" referenced symmetrical components.

```
In [10]:
             # Define Symmetrical Voltages
             volt = [[0.274, -90],
          3
                     [0.709,90],
                     [0.299,-90]]
          4
             seq = ep.phasorlist(volt)
          5
            ep.cprint(seq,label=["I0","I1","I2"])
            # a) "A"-Reference
          8
          9
            phsA = ep.seq_to_abc(seq)
            10
         11
             ep.cprint(phsA,label=["IA","IB","IC"])
         12
         13
             print()
         14
            # b) "B"-Reference
         15
             phsB = ep.seq_to_abc(seq, "B")
         17 ep.phasorplot(phsB,legend=["IA","IB","IC"],title="B-Reference",
                          colors=["#0000FF","#00FF00","#FF0000"])
         18
         19 ep.cprint(phsB,label=["IA","IB","IC"])
         20 print()
         21
         22 # c) "C"-Reference
         phsC = ep.seq_to_abc(seq,"C")
         24 ep.phasorplot(phsC,legend=["IA","IB","IC"],title="C-Reference", colors=["#0000FF","#00FF00","#FF0000"])
         26 ep.cprint(phsC,label=["IA","IB","IC"])
         27 print()
```

```
[['I0 0.274 \(\neq \) -90.0°']
['I1 0.709 \(\neq \) 90.0°']
['I2 0.299 \(\neq \) -90.0°']]
```

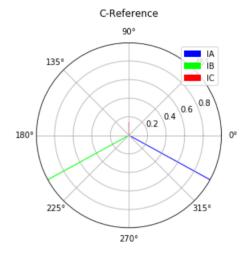
A-Reference



```
[['IA 0.136 ∠ 90.0°']
['IB 0.996 ∠ -28.754°']
['IC 0.996 ∠ -151.246°']]
```

B-Reference 90° 135° 180° 225° 180° 270°

```
[['IA 0.996 \angle -151.246^{\circ}']
['IB 0.136 \angle 90.0^{\circ}']
['IC 0.996 \angle -28.754^{\circ}']]
```



[['IA 0.996 ∠ -28.754°'] ['IB 0.996 ∠ -151.246°'] ['IC 0.136 ∠ 90.0°']]

Problem 4: (text 2.10)

```
In [5]:
          1 # Create Arbitrary Impedance (Load)
          2 Zaa = 0.5+0.1i
          3 \mid Zbb = 0.74+0.15j
          4 | Zcc = 0.89 + 0.11j
          5 \mid Zab = 0.1 + 0.6j
          6 Zbc = 0.11+0.58j
            Zca = 0.12+0.56i
            Zabc = np.array([[Zaa,Zab,Zca],
          9
                              [Zab, Zbb, Zbc],
         10
                               [Zca,Zbc,Zcc]])
         11
         12 # Evaluate Sequence Impedance
         13 Z012 = ep.sequencez(Zabc)
         14 print("Sequence Impedance:\n",Z012)
         15
         16
            # Create Balanced Voltage Source
         17 Vsrc = ep.phasorlist([[1,0],
         18
                                    [1, -120],
         19
                                    [1,120]])
         20 V012 = ep.abc_to_seq(Vsrc)
         21 print("\nSequence Voltages of Balanced Voltage Source:")
         22 ep.cprint(V012,label=["V0","V1","V2"])
         23
         24 # Evaluate Sequence Currents
         25 | I012 = np.linalg.inv(Z012).dot(V012)
         26 print("\nSequence Currents:")
         27 ep.cprint(I012,label=["I0","I1","I2"])
         28
         29 # Evaluate Phase Currents
         31 print("\nPhase Currents:")
         32 | ep.cprint(Iabc,label=["IA","IB","IC"])
         33
         34 # Determine Neutral Current
         35 In = np.sum(Iabc)
         36 print("\nNeutral Current:")
         37 ep.cprint(In,label="In:")
         38
         39 # Determine 3*Io
         40 \quad I0_3 = 3*I012[0]
         41 print("\nZero-Sequence Current:")
         42 ep.cprint(I0_3,label="3*I0:")
         43
         44 # Demonstrate that Currents are Equal
         45 | ion = r"$$I_{0}-I_{n}="+ep.clatex(I0_3-In,double=True,predollar=False)
        Sequence Impedance:
         [[ 0.930+1.28j -0.082+0.039j -0.128-0.059j]
         [-0.128-0.059j 0.600-0.46j -0.117+0.022j]
         [-0.082+0.039j -0.093-0.042j 0.600-0.46j]]
        Sequence Voltages of Balanced Voltage Source:
        [['V0 0.0 \( \text{ 0.0°'}]
         ['V1 1.0 \(\neq -0.0°']
         ['V2 0.0 \(\neq \) 90.0°']]
        Sequence Currents:
        [['I0 0.073 ∠ -29.092°']
         ['I1 1.338 \(\neg 38.622°')]
         ['I2 0.177 \(\neq \) 97.877°']]
        Phase Currents:
        [['IA 1.458 ∠ 41.934°']
         ['IB 1.472 ∠ -85.131°']
         ['IC 1.089 \(\neg \) 159.259°']]
        Neutral Current:
        In: 0.219 ∠ -29.092°
        Zero-Sequence Current:
        3*I0: 0.219 ∠ -29.092°
```

This demonstrates that $I_n=I_0$ as shown below by their subtracted total:

$$I_0 - I_n = 0.0 \angle - 17.103^\circ$$

Problem 5: (text 2.13)

```
In [6]:
        1 # Define Givens
          2 Vab = ep.phasor(1,30)
          3 Vac = ep.phasor(1,-30)
          4 Vbc = ep.phasor(1,-90)
          5 Vca = Vac * 1j**2
         7 # Determine Line-to-Neutral Voltages
         8 Van = ep.phaseline(VLL=Vab,complex=True)
         9 Vbn = ep.phaseline(VLL=Vbc,complex=True)
         10 Vcn = ep.phaseline(VLL=Vca,complex=True)
         11
         12 # Generate Sequence Voltages
         13 V012 = ep.abc_to_seq([Van,Vbn,Vcn])
         14 ep.cprint(V012,label=["V0","V1","V2"])
         15
         16 # Create LaTeX String
         17 Vtex = r'$$V_{012}='+ep.clatex(V012,predollar=False,double=True)
        [['V0 0.0 \(\neq\) -104.036°']
```

Line-to-Neutral Voltages:

$$V_{012} = \begin{bmatrix} 0.0\angle - 104.036^{\circ} \\ 0.577\angle - 0.0^{\circ} \\ 0.0\angle 15.945^{\circ} \end{bmatrix}$$

Problem 6:

```
In [7]:
          1 # Define Givens
          2 CTR H = 500
          3 | CTR_L = 5
          4 CTR = CTR_H/CTR_L
          5 PHS_L = [[12, -87],
          6
                     [4,-120],
                     [4,120]]
          8
            PHS L = ep.phasorlist(PHS L)
          9
         10 # a) Primary Currents
         11 print("a) Primary Currents:")
         12 PHS_H = ep.primary(PHS_L,CTR)
         13 ep.cprint(PHS_H)
         14
         15 # b) Secondary Sequence Currents
         16 print("\nb) Sequence Components:")
         17 PHS_L_012 = ep.abc_to_seq(PHS_L)
         18 | ep.cprint(PHS_L_012,label=["I0","I1","I2"])
         19
         20 # c) Residual Current
         21 print("\nc) Neutral Current:")
         I_r = np.sum(PHS_L)
         23 ep.cprint(I_r,label="Residual:")
         24 ep.cprint(3*PHS_L_012[0],label="3*I0:\t ")
         25
         26 | # d) Delta Currents
         27 PHS_L_D = ep.phaseline(Iline=ep.secondary(PHS_L,CTR),complex=True)
         28 PHS_L_D_012 = ep.abc_to_seq(PHS_L_D)
         29 PHS_L_D_012[0] = 0 # Force Zero-Sequence to Zero
         30 print("\nd) Sequence Currents:")
         31 ep.cprint(PHS_L_D_012,label=["I0","I1","I2"])
        a) Primary Currents:
        [['1200.0 ∠ -87.0°']
         ['400.0 \(\neq\) -120.0°']
         ['400.0 \(\neq\) 120.0°']]
        b) Sequence Components:
        [['I0 4.15 ∠ -105.716°']
         ['I1 4.922 ∠ -54.247°']
         ['I2 4.15 \(\neq\) -105.716°']]
        c) Neutral Current:
        Residual: 12.449 ∠ -105.716°
        3*I0:
                  12.449 ∠ -105.716°
        d) Sequence Currents:
        [['I0 0.0 \(\neq 0.0\)\cdot\']
         ['I1 0.028 \(\neg \cdot -24.247\)']
         ['I2 0.024 \(\neq\) -75.716°']]
```