



# Public-Key Cryptography and RSA

Data Encryption & Security (CEN-451)

**Spring 2025 (BSE-8A&B)** 



#### Overview



- Public-key cryptography is **asymmetric**, i.e. involving use of *two separate keys*.
- There is nothing about **symmetric** or **asymmetric** encryption that makes one superior to another w.r.t. *cryptanalysis*.
- Computational overhead of public-key encryption exists w.r.t.
   key management and signature applications.
- Some form of protocol is needed for key distribution, generally involving a **central agent**.

# Public

## Terminologies

- Asymmetric Keys: two "related" keys, a public and private key, used to perform complementary operations, such as encryption and decryption or signature generation and verification.
- Public Key Infrastructure (PKI): set of policies, processes, server platforms, software and workstations used for administering certificates and public-private key pairs.

## Public-Key Cryptosystems



• The concept of **public-key cryptography** evolved from an attempt to solve two of the most difficult problems in symmetric encryption:

#### **Key distribution**

• How to have secure communications in general without having to trust a Key Distribution Center with your key

#### Digital signatures

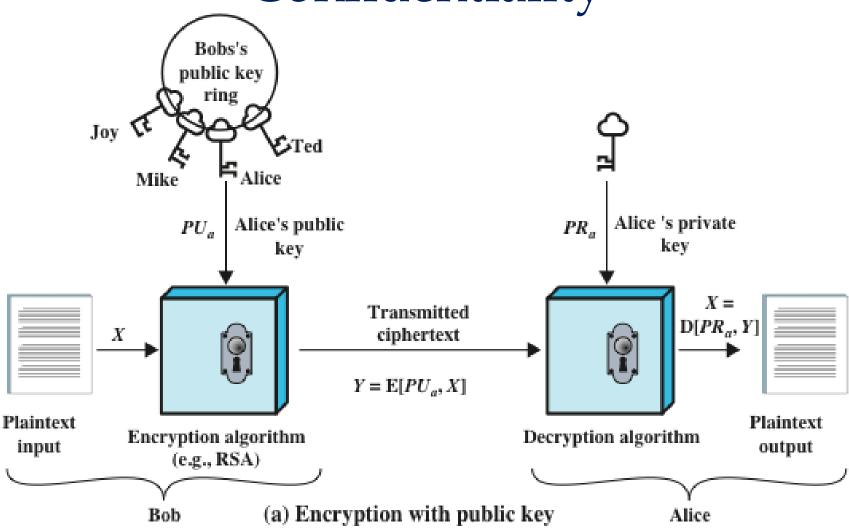
 How to verify that a message comes from the claimed sender

# Public-Key Cryptosystems (Cont.)



- Asymmetric algorithms rely on one key for encryption and a *different but related* key for decryption.
- These algorithms have the following general characteristic:
  - a. It is computationally infeasible to determine decryption key given only cryptographic algorithm and encryption key.
  - b. Either of the two related keys can be used for encryption, with the other used for decryption (as is the case in **RSA**).









#### **Example:**

- If **Bob** wishes to send a confidential message to **Alice**, **Bob** encrypts the message using **Alice's** public key.
- When Alice receives the message, she decrypts it using her private key, where no other recipient can decrypt the message because only Alice knows Alice's private key.



#### Mechanism in public-key cryptosystem:

- Each user generates a **pair of keys** to be used for encryption and decryption of messages.
- Each user places one of the two keys in a public register (*this is the public key*), while the companion key is kept private.
- All participants have access to public keys; hence each user has a collection of public keys obtained from others.



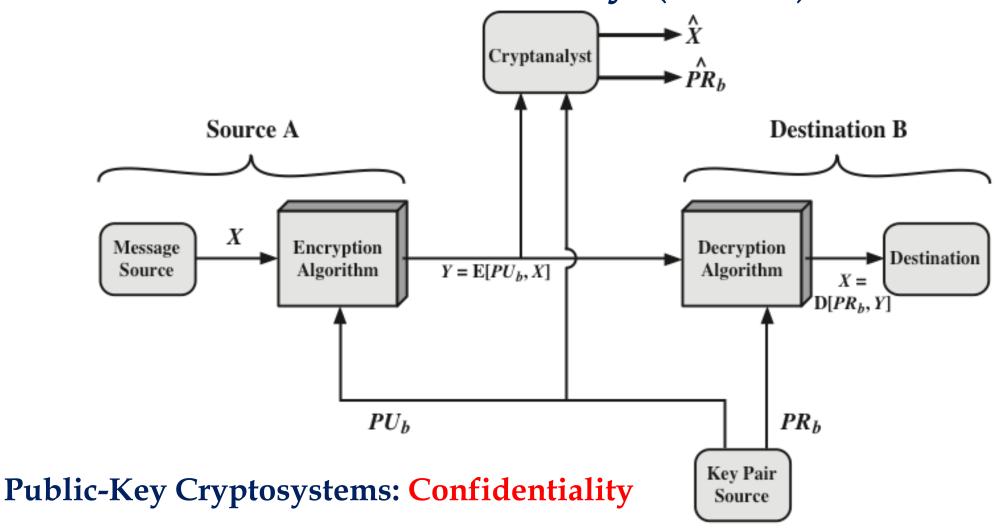


#### Mechanism in public-key cryptosystem (Cont.):

- Private keys are generated locally by each participant and therefore *need never to be distributed*.
- At any time, a system can change its private key and publish the companion public key to replace its old public key.









### Conventional Encryption

#### Public-Key Encryption

# Public Private

#### **Needed to Work:**

- The same algorithm with same key is used for encryption and decryption.
- The sender and receiver must share the algorithm and key.

#### **Needed to Work:**

- One algorithm is used for encryption and a related algorithm for decryption, with a pair of keys where one for encryption and one for decryption.
- Sender and receiver must each have one of the matched pair of keys (not the same one).

#### **Needed for Security:**

- The key must be kept secret.
- It must be impossible or at least impractical to decipher a message if key is kept secret.
- Knowledge of the algorithm plus samples of ciphertext must be insufficient to determine key.

#### **Needed for Security:**

- One of the two keys must be kept secret.
- It must be impossible or at least impractical to decipher a message if one of the keys is kept secret.
- Knowledge of the algorithm plus one of the keys plus samples of ciphertext must be insufficient to determine the other key.



### Public-Key Cryptosystems: Authentication



• Since either of the two related keys can be used for encryption with the other used for decryption, the public-key encryption can also be used to provide authentication.

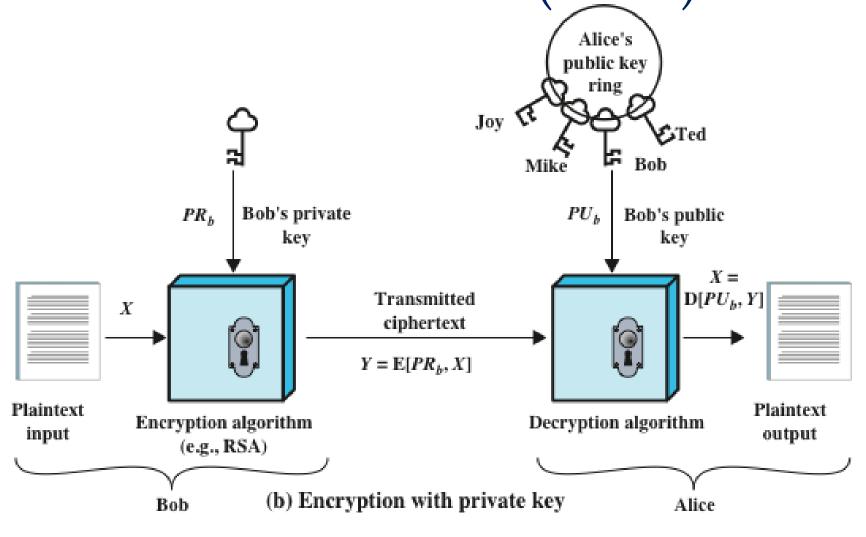
#### **Example:**

- A prepares a message to  $\mathbf{B}$  and encrypts it using  $\mathbf{A's}$  private key.
- B can decrypt the message using A's public key.
- Because the message was encrypted using A's private key, only A could have prepared the message not anyone else.
- Hence, entire encrypted message serves as a digital signature.



Public-Key Cryptosystems: Authentication (Cont.)

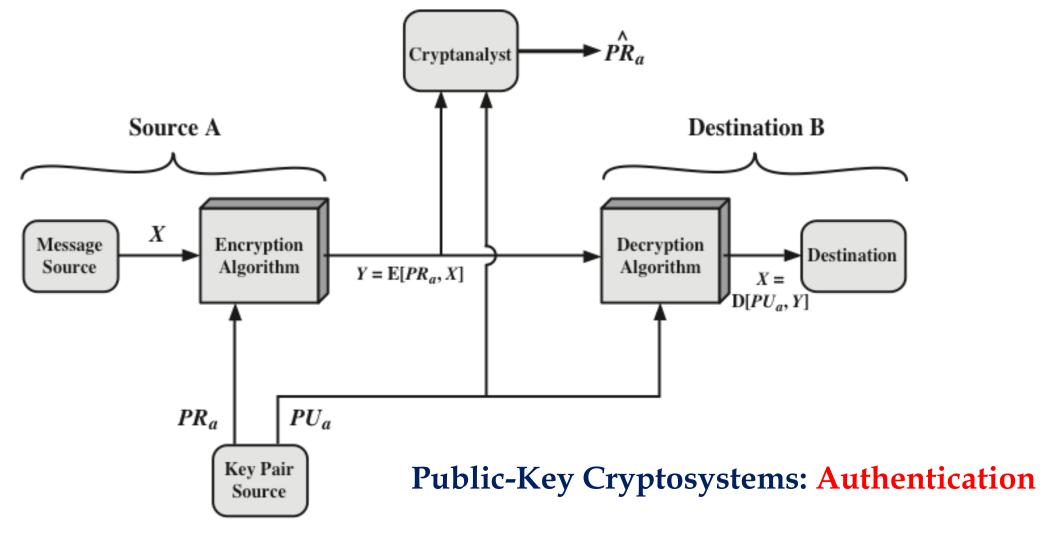






### Public-Key Cryptosystems: Authentication (Cont.)





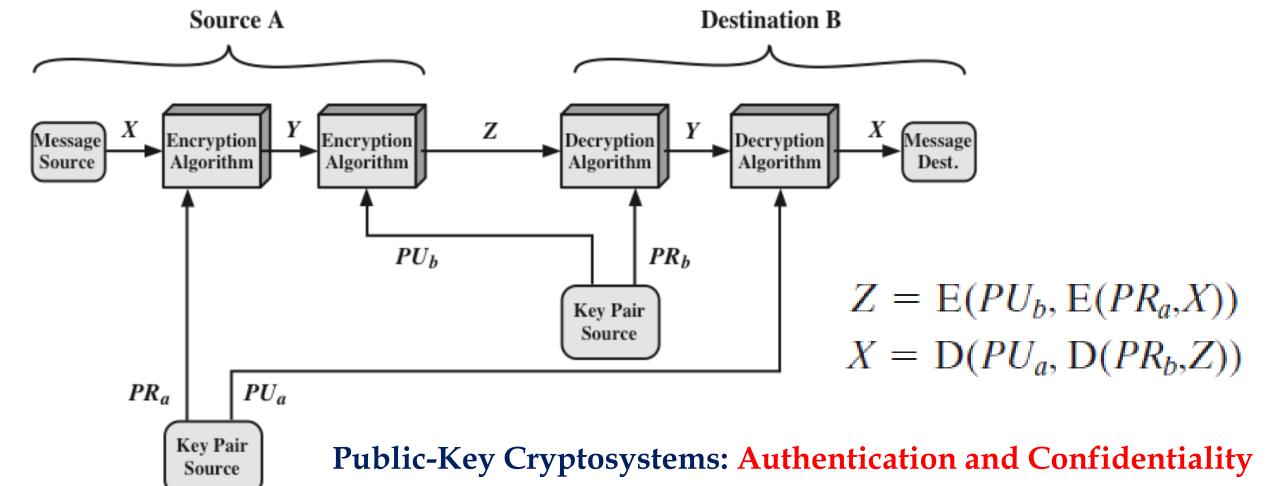
# Public-Key Cryptosystems: Confidentiality and Authentication



- The encryption process, using the private key for encryption, does not provide confidentiality.
- The message being sent is safe from **authentication** issues but not from **eavesdropping**.
- There is no protection of **confidentiality** because any observer can decrypt the message by using the sender's public key.
- It is possible to provide both **authentication** and **confidentiality** by a **double use of the public-key scheme**.



# Public-Key Cryptosystems: Confidentiality and Authentication (Cont.)





# Public-Key Cryptosystems: Confidentiality and Authentication (Cont.)

#### **Working mechanism:**

- We begin by encrypting a message using sender's private key. Hence, providing digital signature.
- Next, we encrypt again using the receiver's public key. Hence, generating the final ciphertext. This final ciphertext can be decrypted only by the receiver who has the matching private key. Thus, confidentiality is achieved.
- The receiver decrypts the received **ciphertext** first by its **own private key**. Followed by decrypting the result with the **sender's public key**. By that, the **plaintext** is obtained.



## Application of Public-Key Cryptosystems



- Depending on the application, sender uses either the sender's private key or receiver's public key or both.
- Broadly, we can classify the use of public-key cryptosystems into three categories:

**Encryption / Decryption** 

 The sender encrypts a message with the recipient's public key

Digital signature

 The sender "signs" a message with its private key

Key exchange

 Two sides cooperate to exchange a session key, which is a secret key for symmetric encryption



# Application of Public-Key Cryptosystems (Cont.)



- Some algorithms are suitable for all three applications, whereas others can be used only for one or two of these applications.
- Table below indicates the applications supported by the algorithms.

Algorithm	Encryption/Decryption	Digital Signature	Key Exchange				
RSA	Yes	Yes	Yes				
Elliptic Curve	Yes	Yes	Yes				
Diffie-Hellman	No	No	Yes				
DSS	No	Yes	No				

# (Rivest-Shamir-Adleman) RSA

# RSA Overview



- RSA scheme is the most widely accepted and implemented "general-purpose" approach to public-key encryption.
- RSA is a cipher in which plaintext and ciphertext are integers between 0 and n-1 for some n.
- A typical size for *n* is **1024 bits** or **309 decimal digits**.
- So, *n* is less than 2<sup>1024</sup>.

## RSA Algorithm



- RSA makes use of exponential expressions.
- For some plaintext block *M* and ciphertext block *C*, encryption and decryption are of the following form:

$$C = M^e \mod n$$

$$M = C^d \mod n$$

- Sender knows value of e and "only" receiver knows value of d.
- However, both sender and receiver must know the value of n.
- **RSA** is a public key encryption algorithm with the following:
  - *Public key of PU* = {*e, n*}

Private key of 
$$PR = \{d, n\}$$



## RSA Algorithm (Cont.)



- For this algorithm to be satisfactory for public-key encryption, the following requirements must be met:
  - 1. It is possible to find values of **e**, **d** and **n** such that  $M^{ed}$  mod n = M, for all M < n.
  - 2. It is relatively easy to calculate  $M^e \mod n$  and  $C^d \mod n$ , for all M < n.
  - 3. It is infeasible to determine d given e and n.



## RSA Algorithm (Cont.)

- The relationship  $M^{ed}$  mod n = M holds if e and d are multiplicative inverses modulo  $\Phi(\mathbf{n})$ , where  $\Phi(\mathbf{n})$  is the Euler totient function.
- The relationship between **e** and **d** can be expressed as:

$$ed \mod \Phi(n) = 1$$
  
 $ed \equiv 1 \mod \Phi(n)$ 

• According to rules of modular arithmetic, this is true only if d (and therefore e) is relatively prime to  $\Phi(n)$ . Equivalently,  $gcd(\Phi(n), d) = 1$ .



## RSA Algorithm (Cont.)

• RSA algorithm is based on a fact that finding factors of large composite numbers is difficult *when the integers are prime numbers*.

#### Following are required in RSA algorithm:

• p, q are two prime numbers

(private, chosen)

n = pq

(public, calculated)

 $\Phi(n) = \Phi(pq) = (p-1)(q-1).$ 

• e, such that  $gcd(\Phi(n), e) = 1$ ,

(public, chosen)

where  $1 \le e \le \Phi(n)$ •  $d \equiv e^{-1} \mod \Phi(n)$ 

(private, calculated)



#### Key Generation by Alice

Select p, q p and q both prime,  $p \neq q$ 

Calculate  $n = p \times q$ 

Calculate  $\phi(n) = (p-1)(q-1)$ 

Select integer e

 $gcd(\phi(n), e) = 1; 1 < e < \phi(n)$ 

Calculate d

 $d = e^{-1} \pmod{\phi(n)}$ 

Public key

 $PU = \{e, n\}$ 

Private key

 $PR = \{d, n\}$ 

# Encryption by Bob with Alice's Public Key Plaintext: M < n

 $C = M^e \mod n$ 

#### Decryption by Alice with Alice's Private Key

Ciphertext:

C

Plaintext:

 $M = C^d \mod n$ 

Ciphertext:



## RSA Example

#### **Example of RSA algorithm:**

- Select two prime numbers, p = 17 and q = 11
- Calculate  $n = pq = 17 \times 11 = 187$
- Calculate  $\Phi(n) = (p-1)(q-1) = 16 \times 10 = 160$
- Select e such that e is relatively prime to  $\Phi(n) = 160$  and  $1 < e < \Phi(n)$ . We choose e = 7
- Determine *d* such that  $de \equiv 1 \pmod{160}$  and d < 160
- Value of d = 23 (calculated using extended Euclid's algorithm)
- Resulting keys are  $PU = \{7, 187\}$  and  $PR = \{23, 187\}$



## RSA Example (Cont.)

#### **Example of RSA algorithm (Cont.):**

- Use the generated keys for a plaintext input of M = 88
- For encryption, we calculate  $C = 88^7 \mod 187$
- By exploiting properties of modular arithmetic, we have:
  - $88^7 \mod 187 = [(88^4 \mod 187) \times (88^2 \mod 187) \times (88^1 \mod 187)] \mod 187$
  - $88^1 \mod 187 = 88$
  - $88^2 \mod 187 = 7744 \mod 187 = 77$
  - 88<sup>4</sup> mod 187 = 59,969,536 mod 187 = 132
  - So,  $88^7 \mod 187 = (88 \times 77 \times 132) \mod 187 = 894,432 \mod 187 = 11$
  - So, C = 11

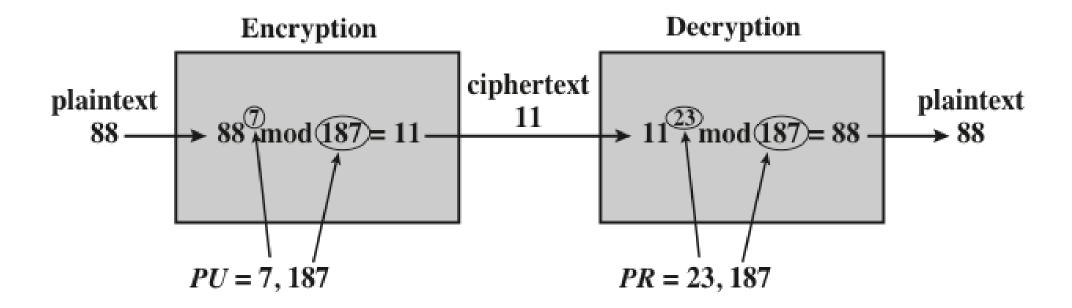
## RSA Example (Cont.)

#### **Example of RSA algorithm (Cont.):**

- For decryption, we calculate  $M = 11^{23} \mod 187$ :
  - 11<sup>23</sup> mod 187 = [(11<sup>1</sup> mod 187) × (11<sup>2</sup> mod 187) × (11<sup>4</sup> mod 187) × (11<sup>8</sup> mod 187) × (11<sup>8</sup> mod 187) × (11<sup>8</sup> mod 187)] mod 187
  - $11^1 \mod 187 = 11$
  - $\blacksquare$  11<sup>2</sup> mod 187 = 121
  - $11^4 \mod 187 = 14,641 \mod 187 = 55$
  - 11<sup>8</sup> mod 187 = 214,358,881 mod 187 = 33
  - 11<sup>23</sup> mod 187 = (11 \* 121 \* 55 \* 33 \* 33) mod 187 = 79,720,245 mod 187 = 88
  - So, M = 88



## RSA Example (Cont.)





#### RSA Practice

• Example: while using the RSA algorithm, show the process to encrypt and decrypt a letter with ASCII value of 32 (i.e. space character). Given that: p = 3, q = 11 and e = 17

Dec	H	Oct	Cha	r	Dec	Нх	Oct	Html	Chr	Dec	Нх	Oct	Html	Chr	Dec	: Hx	Oct	Html CI	hr
0	0	000	NUL	(null)	32	20	040	@#32;	Space	64	40	100	a#64;	0	96	60	140	a#96;	8
1	1	001	SOH	(start of heading)	33	21	041	@#33;	!	65	41	101	A	A	97	61	141	a#97;	a
2	2	002	STX	(start of text)	34	22	042	@#3 <b>4</b> ;	**	66	42	102	B	В	98	62	142	a#98;	b
3	3	003	ETX	(end of text)	35	23	043	@#35;	#	67	43	103	C	C	99	63	143	a#99;	C
4	4	004	EOT	(end of transmission)	36	24	044	@#36;	ş	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ	(enquiry)				@#37;					E					e	
6	6	006	ACK	(acknowledge)	38	26	046	<b>@#38;</b>	6				F		102	66	146	f	f
7	7	007	BEL	(bell)	39	27	047	<b>@#39;</b>	1	71	47	107	G	G		-		@#103;	
8	8	010	BS	(backspace)				<u>@#40;</u>					H					a#104;	
9	9	011	TAB	(horizontal tab)				)					I					a#105;	
10	A	012	LF	(NL line feed, new line)				&# <b>4</b> 2;					@#74;		-			j	
11	В	013	VT	(vertical tab)				&#<b>4</b>3;</td><td></td><td>75</td><td>4B</td><td>113</td><td>K</td><td></td><td></td><td></td><td></td><td>k</td><td></td></tr><tr><td>12</td><td>С</td><td>014</td><td>FF</td><td>(NP form feed, new page)</td><td></td><td></td><td></td><td>@#44;</td><td></td><td></td><td></td><td></td><td>L</td><td></td><td></td><td></td><td></td><td>l</td><td></td></tr><tr><td>13</td><td>D</td><td>015</td><td>CR</td><td>(carriage return)</td><td>45</td><td>2D</td><td>055</td><td>a#45;</td><td>F 11</td><td>77</td><td>4D</td><td>115</td><td>M</td><td>M</td><td></td><td></td><td></td><td>m</td><td></td></tr><tr><td>14</td><td>E</td><td>016</td><td>so</td><td>(shift out)</td><td>46</td><td>2E</td><td>056</td><td>@#<b>4</b>6;</td><td>+\\\\</td><td>78</td><td>4E</td><td>116</td><td>N</td><td>N</td><td>110</td><td>6E</td><td>156</td><td>n</td><td><math>\mathbf{n}</math></td></tr><tr><td>15</td><td></td><td>017</td><td></td><td>(shift 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# Diffie-Hellman Key Exchange



### Diffie-Hellman Overview

- The main purpose of Diffie-Hellman algorithm is to enable two users to *securely exchange a "key"*.
- The shared "key" can then be used for subsequent *symmetric* encryption.
- Diffie-Hellman algorithm is limited to the exchange of *secret values* (*i.e. keys*).
- For its effectiveness, the algorithm depends on the difficulty of computing discrete logarithms.

#### Primitive Root

- A **primitive root** of a prime number p is one whose powers modulo p generate all the integers from (1 to p 1).
- If a is a **primitive root** of the prime number p, then the numbers below are *distinct* and consist of integers from 1 to p-1 in some permutation.

 $a \mod p$ ,  $a^2 \mod p$ , ...,  $a^{p-1} \mod p$ 



## Key Exchange Algorithm

- There are two publicly known numbers, i.e. a prime number q and an integer  $\alpha$  that is a primitive root of q.
- To create a shared "secret key" between Alice and Bob, the following are adopted:
  - a. Alice independently selects a random integer  $X_A < q$
  - b. Bob independently selects a random integer  $X_B < q$
  - c. Alice computes  $Y_A = \alpha^{X_A} \mod q$
  - d. Bob computes  $Y_B = \alpha^{X_B} \mod q$



# Key Exchange Algorithm (Cont.)

- Each side keeps the X value "private" and makes the Y value available "publicly" to the other side.
- Hence,  $X_A$  is Alice's private key and  $Y_A$  is Alice's corresponding public key  $\rightarrow$  Alice  $(X_A, Y_A)$ .
- Whereas,  $X_B$  is Bob's private key and  $Y_B$  is Bob's corresponding public key  $\rightarrow$  Alice  $(X_B, Y_B)$ .



# Key Exchange Algorithm (Cont.)

- Finally, the "secret key" is computed at each side as follows:
  - 1. Alice computes the key as  $K = (Y_B)^{X_A} \mod q$
  - 2. Bob computes the key as  $K = (Y_A)^{X_B} \mod q$
- The above two calculations would produce identical results!



## Key Exchange Algorithm (Cont.)

#### Alice

**Bob** 

Alice and Bob share a prime number q and an integer  $\alpha$ , such that  $\alpha < q$  and  $\alpha$  is a primitive root of q

Alice and Bob share a prime number q and an integer  $\alpha$ , such that  $\alpha < q$  and  $\alpha$  is a primitive root of q

Alice generates a private key  $X_A$  such that  $X_A < q$ 

Bob generates a private key  $X_B$  such that  $X_B < q$ 

Alice calculates a public key  $Y_A = \alpha^{X_A} \mod q$ 

Bob calculates a public key  $Y_B = \alpha^{X_B} \mod q$ 

Alice receives Bob's public key *Y<sub>B</sub>* in plaintext

Bob receives Alice's public key  $Y_A$  in plaintext

Alice calculates shared secret key  $K = (Y_R)^{X_A} \mod q$ 

Bob calculates shared secret key  $K = (Y_A)^{X_B} \mod q$ 







## Diffie-Hellman Example

- Q) Given the prime number q = 353 and a primitive root a = 3. Calculate the secret key if Alice and Bob select private keys  $X_A$  = 97 and  $X_B$  = 233, respectively.
- A) Alice computes  $Y_A = \alpha^{X_A} \mod q$ 
  - $Y_A = 3^{97} \mod 353 \rightarrow In Book (397 \mod 353 = 40)!$
  - $\mathbf{Y_A} = [(3^{20} \mod 353) \times (3^{20} \mod 353) \times (3^{20} \mod 353) \times (3^{20} \mod 353) \times (3^{17} \mod 353)] \mod 353$
  - $\mathbf{Y}_{A} = [73 \times 73 \times 73 \times 73 \times 55] \mod 353$
  - $Y_A = 40$

## Diffie-Hellman Example (Cont.)

- Bob computes  $Y_B = \alpha^{X_B} \mod q$ 
  - $Y_B = 3^{233} \mod 353 \rightarrow In Book (3233 \mod 353 = 248)!$
  - $Arr Y_B = [(3^{20} \mod 353) \times (3^{20} \mod 35) \times$

  - $\mathbf{Y}_{B} = [2,073,071,593 \times 2,073,071,593 \times 12775] \mod 353$



## Diffie-Hellman Example (Cont.)

- Bob computes  $Y_B = \alpha^{X_B} \mod q$  (Cont.)
  - $\mathbf{Y}_{\mathbf{B}} = [(2,073,071,593 \mod 353) \times (2,073,071,593 \mod 353) \times (12775 \mod 353)] \mod 353$
  - $\mathbf{Y}_{B} = [21 \times 21 \times 67] \mod 353$
  - $\mathbf{Y}_{B} = [29547] \mod 353$
  - $Y_B = 248$



## Diffie-Hellman Example (Cont.)

- After Alice and Bob exchange **public keys**, each can compute the common **"secret key"**:
- Alice computes  $K = (Y_B)^{X_A} \mod q$

$$= 248^{97} \mod 353 = 24897 \mod 353 = 160.$$

• Bob computes  $K = (Y_A)^{X_B} \mod q$ 

$$= 40^{233} \mod 353 = 40233 \mod 353 = 160.$$

• Hence, the common secret key = 160.



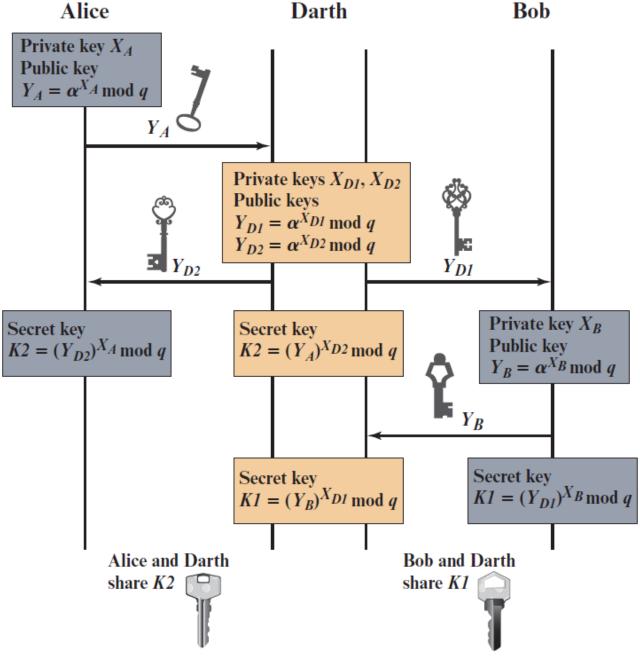
### Diffie-Hellman: Brute Force Attack

- For small values, e.g. for prime number q and primitive root a, it would be possible to determine the secret key by brute force.
- E.g., an attacker can determine the secret key by discovering a solution to  $3^a \mod 353 = 40 \ OR \ 3^b \mod 353 = 248$ , through brute-force.
- For the case of " $3^a \mod 353 = 40$ ", the attacker would stop the search process when a = 97, which provides  $3^{97} \mod 353 = 40$ .
- However, **brute force** would becomes **impractical** when considering larger numbers.



### Diffie-Hellman: MiTM Attack

- The protocol behind Diffie-Hellman Key Exchange is insecure against a man-in-the-middle (MiTM) attack.
- The key exchange protocol is vulnerable to such an attack because it does not authenticate the participants.
- This vulnerability can be overcome with the use of digital signatures and public-key certificates.



# Thank You!