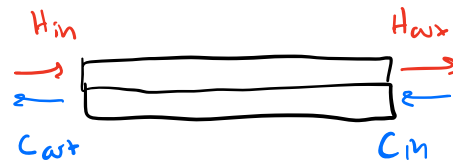


Counter flow

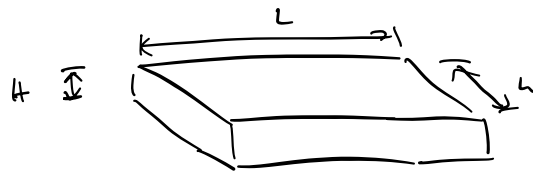


a) Find convective heat transfer coefficient on hot & cold sides

$$\overline{Nu} = \frac{\overline{h} D_h}{k}$$

$$D_h = \frac{4A_c}{\text{per}}$$

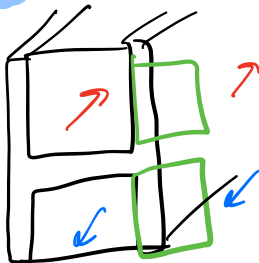
Duct flow:



$$\text{Aspect} = H/w$$

→ KEY VAR IN EES

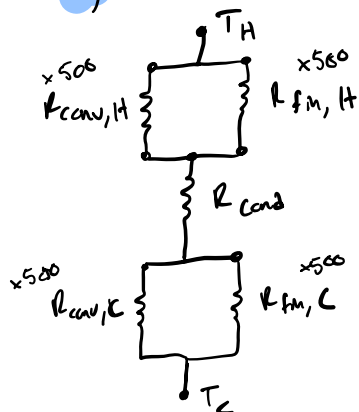
b) Fin resistance of hot & cold



→ KEY VAR IN EES

c) Conductance (UA)

$$UA = \frac{1}{R_{tot}}$$



→ KEY VAR

d) NTU

$$NTU = \frac{UA}{\dot{C}_{min}} \rightarrow \text{KEY VAR}$$

$$\dot{C}_{min} = \min(\dot{m}_C C_C, \dot{m}_H C_H)$$

e) effectiveness

$$\epsilon = \frac{1 - \exp(-NTU(1 - C_R))}{1 - C_R \exp(-NTU(1 - C_R))}$$

$$C_R = \dot{C}_{min} / \dot{C}_{max} \rightarrow \epsilon \text{ KEY VAR}$$

f)

$$T_{Cout}, T_{Hout} \text{ KEY VARS}$$

\$unitsystem SI J Pa

"Geometry"

W = 5 [mm]*convert(mm,m)
th_f = 1 [mm]*convert(mm,m)
H = 10 [mm]*convert(mm,m)
th_b = 2 [mm]*convert(mm,m)

N_c = 500 [-]

\$ifnot parametrictable

L = 5 [m]

\$endif

T_H_in = 90 [C]

T_C_in = 20 [C]

m_dot_H_tot = 2 [kg/s]
m_dot_C_tot = .5 [kg/s]
m_dot_H = m_dot_H_tot / N_c
m_dot_C = m_dot_C_tot / N_c
T_prop = (T_H_in + T_C_in)/2

k_m=20 [W/m-K]

"Property lookups for hot and cold side"

cp_H=cp(Air,T=T_prop)
cp_C =specheat(Water, T=T_prop, P=Po#)

rho_H = density(Air, T=T_prop, P=Po#)
rho_C = density(Water, T=T_prop, P=Po#)

mu_H = viscosity(Air, T=T_prop)
mu_C = viscosity(Water, T=T_prop, P=Po#)

k_C = conductivity(Water, T=T_prop, P=Po#)
k_H = conductivity(Air, T=T_prop)

"part a convective HTC"

"both"

D_h = 4*A_c/per
per = 2*H+2*W
LowerD_h = L/D_h
Aspect = W/H
RelRough = 0
A_c = W*H

"cold water"

Call ductflow_nd(Re_C,Pr_C,LowerD_h, Aspect,RelRough: Nusselt_T_C, Nusselt_H_C, f_C)
u_C = m_dot_C/rho_C / A_c
Re_C = rho_C*u_C*D_h/mu_C
Pr_C = mu_C*cp_C/k_C
Nusselt_H_C = h_bar_C*D_h/k_C

"hot air"

"Channel width"

"Fin width"

"Fin/Channel height"

"Channel separator thickness"

"Number of fins"

"Overall length of the heat exchanger"

"Hot stream inlet temperature"

"Cold stream inlet temperature"

"Total hot side mass flow"

"Total cold side mass flow"

"Single channel hot side mass flow"

"Single channel cold side mass flow"

"Temperature used for property evaluations"

"Metal conductivity"

Call ductflow_nd(Re_H,Pr_H,LowerD_h, Aspect,RelRough: Nusselt_T_H, Nusselt_H_H, f_H)
 $u_H = \dot{m}_H / \rho_H / A_c$
 $Re_H = \rho_H u_H D_h / \mu_H$
 $Pr_H = \mu_H c_{p,H} / k_H$
 $Nusselt_{H,H} = \bar{h}_H D_h / k_H$

"part b fin resistance"

$per_f = 2H + th_f$
 $per_f = 2L$
 $A_f = th_f L$
 $A_s = 2H L$

"TA says perimeter from top down"
"top down area"

"cold fin"

$m_C = \sqrt{per_f \bar{h}_C / (k_m A_f)}$
 $\eta_{fin,C} = \tanh(m_C H) / (m_C H)$
 $finres_C = 1 / (\eta_{fin,C} \bar{h}_C A_s)$

"hot fin"

$m_H = \sqrt{per_f \bar{h}_H / (k_m A_f)}$
 $\eta_{fin,H} = \tanh(m_H H) / (m_H H)$
 $finres_H = 1 / (\eta_{fin,H} \bar{h}_H A_s)$

"part c conductance"

$A_{unf} = W L$
 $R_{conv,H} = 1 / (\bar{h}_H A_{unf})$
 $R_{conv,C} = 1 / (\bar{h}_C A_{unf})$
 $R_{cond} = th_b / (k_m A_{unf})$

$R_{tot} = R_{cond} / N_c + 1 / (N_c / R_{conv,C} + N_c / finres_C) + 1 / (N_c / R_{conv,H} + N_c / finres_H)$
 $UA = 1 / R_{tot}$

"part d NTU"

$c_{dot,C} = \dot{m}_{tot,C} c_{p,C}$
 $c_{dot,H} = \dot{m}_{tot,H} c_{p,H}$
 $c_{dot,min} = \min(c_{dot,C}, c_{dot,H})$

$NTU = UA / c_{dot,min}$

"part e effectiveness"

$C_R = \min(c_{dot,C}, c_{dot,H}) / \max(c_{dot,C}, c_{dot,H})$
 $\epsilon = (1 - \exp(-NTU(1 - C_R))) / (1 - C_R \exp(-NTU(1 - C_R)))$

"part f outlet temps"

$$T_{C_out} = T_{C_in} + \epsilon \cdot c_{dot_min} \cdot (T_{H_in} - T_{C_in}) / c_{dot_C}$$

$$T_{H_out} = T_{H_in} - \epsilon \cdot c_{dot_min} \cdot (T_{H_in} - T_{C_in}) / c_{dot_H}$$

SOLUTION

Unit Settings: SI C Pa J mass deg

Aspect = 0.5 [-]	$A_c = 0.00005 \text{ [m}^2\text{]}$	$A_f = 0.005 \text{ [m}^2\text{]}$	$A_s = 0.1 \text{ [m}^2\text{]}$
$A_{unf} = 0.025 \text{ [m}^2\text{]}$	$cp_c = 4183 \text{ [J/kg-K]}$	$cp_H = 1006 \text{ [J/kg-K]}$	$\dot{c}_C = 2091 \text{ [J/K-s]}$
$\dot{c}_H = 2013 \text{ [J/K-s]}$	$\dot{c}_{min} = 2013 \text{ [W/C]}$	$CR = 0.9624 \text{ [-]}$	$D_h = 0.006667 \text{ [m]}$
$\epsilon = 0.7634 \text{ [-]}$	$\eta_{fin,C} = 0.4679 \text{ [-]}$	$\eta_{fin,H} = 0.5623$	$finres_C = 0.04986 \text{ [C/W]}$
$finres_H = 0.06512 \text{ [C/W]}$	$f_C = 0.2367 \text{ [-]}$	$f_H = 0.02434 \text{ [-]}$	$H = 0.01 \text{ [m]}$
$\bar{h}_C = 428.7 \text{ [W/m}^2\text{-K]}$	$\bar{h}_H = 273.1 \text{ [W/m}^2\text{-K]}$	$k_C = 0.646 \text{ [W/m-K]}$	$k_H = 0.02772 \text{ [W/m-K]}$
$k_m = 20 \text{ [W/m-K]}$	$L = 5 \text{ [m]}$	$LowerD_h = 750 \text{ [-]}$	$\mu_C = 0.0005036 \text{ [Pa-s]}$
$\mu_H = 0.00001986 \text{ [Pa-s]}$	$\dot{m}_C = 207 \text{ [1/m]}$	$\dot{m}_C = 0.001 \text{ [kg/s]}$	$\dot{m}_{C,tot} = 0.5 \text{ [kg/s]}$
$\dot{m}_H = 0.004 \text{ [kg/s]}$	$\dot{m}_{H,tot} = 2 \text{ [kg/s]}$	$\dot{m}_H = 165.3 \text{ [1/m]}$	$NTU = 3.045 \text{ [-]}$
$Nusselt_{H,C} = 4.424 \text{ [-]}$	$Nusselt_{H,H} = 65.68 \text{ [-]}$	$Nusselt_{T,C} = 3.539 \text{ [-]}$	$Nusselt_{T,H} = 65.68 \text{ [-]}$
$N_c = 500 \text{ [-]}$	$per = 0.03 \text{ [m]}$	$per_f = 10 \text{ [m]}$	$Prc = 3.261 \text{ [-]}$
$Pr_H = 0.721 \text{ [-]}$	$RelRough = 0 \text{ [-]}$	$Rec = 264.7 \text{ [-]}$	$Re_H = 26856 \text{ [-]}$
$\rho_C = 985.7 \text{ [kg/m}^3\text{]}$	$\rho_H = 1.076 \text{ [kg/m}^3\text{]}$	$R_{cond} = 0.004 \text{ [C/W]}$	$R_{conv,C} = 0.09331 \text{ [C/W]}$
$R_{conv,H} = 0.1465 \text{ [C/W]}$	$R_{tot} = 0.0001632 \text{ [C/W]}$	$th_b = 0.002 \text{ [m]}$	$th_f = 0.001 \text{ [m]}$
$T_{C,in} = 20 \text{ [C]}$	$T_{C,out} = 71.43 \text{ [C]}$	$T_{H,in} = 90 \text{ [C]}$	$T_{H,out} = 36.56 \text{ [C]}$
$T_{prop} = 55 \text{ [C]}$	$UA = 6129 \text{ [W/C]}$	$uc = 0.02029 \text{ [m/s]}$	$u_H = 74.37 \text{ [m/s]}$
$W = 0.005 \text{ [m]}$			

No unit problems were detected.

KEY VARIABLES

$\bar{h}_H = 273.1 \text{ [W/m}^2\text{-K]}$	<i>a) HTC for hot air side</i>
$\bar{h}_C = 428.7 \text{ [W/m}^2\text{-K]}$	<i>a) HTC for cold water side</i>
$finres_C = 0.04986 \text{ [C/W]}$	<i>b) fin resistance for cold</i>
$finres_H = 0.06512 \text{ [C/W]}$	<i>b) fin resistance for hot</i>
$UA = 6129 \text{ [W/C]}$	<i>c) total conductance</i>
$NTU = 3.045 \text{ [-]}$	<i>d) NTU</i>
$\epsilon = 0.7634 \text{ [-]}$	<i>e) heat exchanger effectiveness</i>
$T_{C,out} = 71.43 \text{ [C]}$	<i>f) cold outlet temp</i>
$T_{H,out} = 36.56 \text{ [C]}$	<i>f) hot outlet temp</i>

