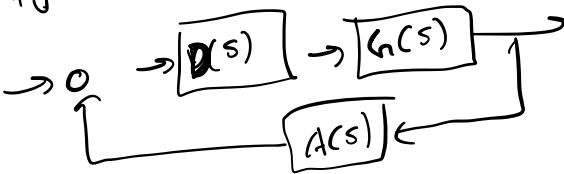


$+j\omega \leftarrow$ F.R. OL system



\rightarrow # poles @ origin

\rightarrow # unstable OL poles (P)

$$Z = N + P$$



stability margins $G(s) = M e^{j\phi}$

- increasing gain moves everything away from origin
- \rightarrow can cause encirclements
- \rightarrow leads to instability

Gain stability condition:

$$|KG(j\omega)| < 1$$

$$\text{when } \angle G(j\omega) = -180^\circ$$

stable system: $G_M > 1$, $G_M > 0 \text{ dB}$

phase stability condition

$$\angle G(j\omega) > (-180^\circ)$$

$$\text{when } |KG(j\omega)| = 1$$

$$\frac{1}{G_M} = |KG(j\omega)|_{\phi = -180^\circ}$$

$$P_M = \angle G(j\omega)_{|K|=1} + 180^\circ$$

exceptions

$$\frac{\sim}{\sim} (s-s) \quad \text{zeros in LHP}$$

$$\frac{\sim}{\sim (s-u)} \quad \text{unstable or poles}$$

→ need to check nyquist in rhp plane

System bandwidth (describes speed of response)

- Range of forcing frequencies where system is most responsive
- Output power > half of peak output power

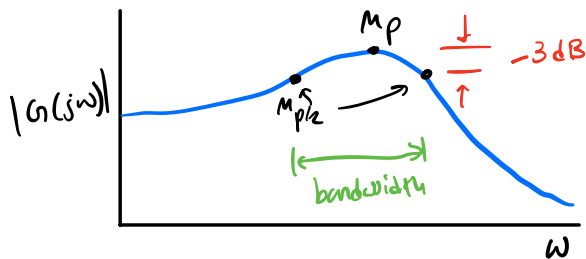
Output power: $P = a M^2$

e.g. $P = IV = I^2 R = \frac{V^2}{R}$

$$\rightarrow \frac{1}{2} P_{\text{peak}} = a M_{p/2}^2$$

Peak power: $P_{\text{peak}} = a M_p^2$

$$\frac{M_{p/2}}{M_p} = \frac{\sqrt{2}}{2} \approx -3 \text{ dB}$$



Alternative definition:

