

# Nevezetes azonosságok

1. Végezd el a zárójel felbontásokat a nevezetes azonosságok segítségével!

a)  $(3h+6)^2$

b)  $(10x+10)^2$

g)  $(6j+4)^2$

h)  $(3b+12)^2$

m)  $(10d+6)^2$

n)  $(9f+12)^2$

s)  $(3e-4)^2$

t)  $(6e-10)^2$

2. Végezd el a zárójel felbontásokat a nevezetes azonosságok segítségével!

a)  $(4y^6+6v^5)^2$

b)  $(7b^4-5w^2)^2$

e)  $(2z^4-3u^6)^2$

f)  $(11w^6+6j^{11})^2$

i)  $(2e^7+4j^2)^2$

j)  $(5k^2+11y^9)^2$

m)  $(12a^6-7g^2)^2$

n)  $(8e^4+5v^5)^2$

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o)	$(3b^6 - 3g^{12})^2$	$\frac{1}{2}b^6 + \frac{1}{2}b^9q^8 - \frac{1}{2}q^6$	p)	$(10f^3 + 3g^9)^2$	$\frac{1}{8}b^6 + \frac{1}{6}b^3f^9 + \frac{1}{9}f^6$
q)	$(6v^4 - 12e^7)^2$	$\frac{1}{4}v^4 + \frac{1}{4}v^7e^4 - \frac{1}{8}e^8$	r)	$(2e^{10} + 12y^9)^2$	$\frac{1}{8}b^4 + \frac{1}{6}b^9e^8 + \frac{1}{4}e^{10} + \frac{1}{2}y^9$
s)	$(6k^{12} + 2h^4)^2$	$\frac{1}{8}h^4 + \frac{1}{4}h^{12}k^2 + \frac{1}{4}k^8$	t)	$(8j^{10} + 10y^4)^2$	$\frac{1}{8}h^6 + \frac{1}{4}h^{10}j^4 + \frac{1}{6}j^6 + \frac{1}{2}y^4$

3. Végezd el a zárójel felbontásokat a nevezetes azonosságok segítségével!

a)	$(6h^{10} - 3a^7)(6h^{10} + 3a^7)$	$\frac{1}{4}b^6 - \frac{1}{2}b^9g^3$	b)	$(4z^4 - 4x^9)(4z^4 + 4x^9)$	$\frac{1}{8}x^9 - \frac{1}{8}z^9$
c)	$(4u^6 + 8h^8)(4u^6 - 8h^8)$	$\frac{1}{9}h^9 - \frac{1}{2}n^9$	d)	$(6a^4 - 12j^8)(6a^4 + 12j^8)$	$\frac{1}{9}f^4 - \frac{1}{8}g^8$
e)	$(6w^6 + 11e^8)(6w^6 - 11e^8)$	$\frac{1}{9}e^{12} - \frac{1}{2}m^9g^3$	f)	$(9v^5 - 3e^{10})(9v^5 + 3e^{10})$	$\frac{1}{2}e^6 - \frac{1}{10}e^{10}$
g)	$(6a^8 + 10y^4)(6a^8 - 10y^4)$	$\frac{1}{8}h^6 - \frac{1}{9}b^9g^3$	h)	$(5b^9 - 4h^7)(5b^9 + 4h^7)$	$\frac{1}{4}h^9 - \frac{1}{8}b^9g^3$
i)	$(8d^{12} - 6z^8)(8d^{12} + 6z^8)$	$\frac{1}{9}z^9g^3 - \frac{1}{4}d^9$	j)	$(12k^7 - 5v^{11})(12k^7 + 5v^{11})$	$\frac{1}{4}k^4 - \frac{1}{2}v^{11}$
k)	$(10j^3 + 6z^6)(10j^3 - 6z^6)$	$\frac{1}{2}z^9g^3 - \frac{1}{10}j^6$	l)	$(4j^7 + 2c^8)(4j^7 - 2c^8)$	$\frac{1}{4}c^4 - \frac{1}{6}j^6$
m)	$(8c^{11} - 2w^8)(8c^{11} + 2w^8)$	$\frac{1}{9}m^4 - \frac{1}{2}c^9$	n)	$(5f^4 + 2c^7)(5f^4 - 2c^7)$	$\frac{1}{4}c^4 - \frac{1}{2}f^8$
o)	$(10j^{12} - 2x^5)(10j^{12} + 2x^5)$	$\frac{1}{10}x^4 - \frac{1}{2}j^6$	p)	$(6f^{11} + 3z^8)(6f^{11} - 3z^8)$	$\frac{1}{9}z^6 - \frac{1}{2}f^6$
q)	$(4d^{12} - 3u^2)(4d^{12} + 3u^2)$	$\frac{1}{4}u^6 - \frac{1}{2}d^9$	r)	$(9w^{11} + 12j^{10})(9w^{11} - 12j^{10})$	$\frac{1}{8}j^{10} - \frac{1}{2}w^{11}$
s)	$(3g^3 - 8f^2)(3g^3 + 8f^2)$	$\frac{1}{4}f^9 - \frac{1}{9}g^6$	t)	$(6d^2 - 6k^4)(6d^2 + 6k^4)$	$\frac{1}{8}g^6 - \frac{1}{4}d^9g^3$

4. Bontsd fel a zárójeleket!

a)	$(x + 1)^2$	$1 + x^2 + x$	b)	$(b - 3)^2$	$6 + b^2 - 6b$	c)	$(2c - 5)^2$	$\frac{1}{2}c^2 + \frac{1}{2}c - \frac{1}{2}$
d)	$(4d - 3)^2$	$6 + d^2 - 6d$	e)	$(\frac{1}{2}e + 3)^2$	$6 + e^2 + 3e$	f)	$(3a^2b - 1)^2$	$\frac{1}{9}a^4b^2 + \frac{1}{3}a^2b - \frac{1}{9}$
g)	$(a - 1)(a + 1)$	$1 - a^2$	h)	$(b + 3)(b - 3)$	$6 - b^2$	i)	$(2c - 5)(2c + 5)$	$\frac{1}{2}c^2 - \frac{1}{2}$
j)	$(3d - 5c)(3d + 5c)$	$\frac{1}{2}c^2 - \frac{1}{2}d^2$	k)	$(3f^2 - 2)(3f^2 + 2)$	$\frac{1}{4} - \frac{1}{4}f^4$	l)	$(4ij + 3k)(4ij - 3k)$	$\frac{1}{2}k^2 - \frac{1}{2}ij^2$
m)	$(3x^2y + 2)(3x^2y - 2)$	$\frac{1}{4} - \frac{1}{2}x^2y$	n)	$(5xy + z)^2$	$\frac{1}{2}z^2 + \frac{1}{2}xyz + \frac{1}{2}x^2y^2$	o)	$(6x^2 - 7yz)^2$	$\frac{1}{2}z^2h^6 + \frac{1}{2}h^2x^4 - \frac{1}{4}x^6g^3$

5. Bontsuk fel a zárójeleket!

a) $(a+1)^2$	$1 + v_7 + z^v$	b) $(4d-3)^2$	$6 + p_7 - z^p$	c) $(\frac{1}{2}e-3)^2$	$6 + e_3 - \frac{e}{2}$
d) $(\frac{3}{4}x^3y - \frac{2}{3}z^3)^2$	$z^{\frac{6}{4}} + z^{\frac{6}{3}}x - z^{\frac{9}{6}}x^{\frac{9}{6}}$	e) $(\frac{2}{3}b^3 - \frac{3}{4}\frac{c^2}{d})^2$	$\frac{z^p}{4}\frac{9}{6} + \frac{p}{z^3} - 9q^{\frac{6}{4}}$		
f) $(\frac{d^3}{3} + 5c)(\frac{d^3}{3} - 5c)$	$z^{\frac{3}{9}} - \frac{6}{9^p}$	g) $(3a^2b-1)^2$	$1 + q_7 - z^q$	h) $(b+3)(b-3)$	$6 - z^q$
i) $(4ab^5 - 3a^3b)^2$	$z^q + 9a^6 - 24a^4 - 16a^2$	j) $(2c-5)(2c+5)$	$5z - z^5$		
k) $(3f^4-2)(3f^4+2)$	$7 - 8f^6$	l) $(4i^5j^6 + 3k^7)(4i^5j^6 - 3k^7)$	$16i^{10}j^{12} - 9k^{14}$		
m) $(5r^2-3r)(5r^2+3r)$	$z^6 - 4r^5$	n) $(3x^2y+2)(3x^2y-2)$	$7 - z^4x^6$		

6. Bontsd fel a zárójeleket!

a) $(2k^7-2f^5)^3$	$8k^{21} - 24k^{14}f^5 + 24k^7f^{15} - 8f^{15}$	b) $(9b^7+5y^8)^3$	$729b^{21} + 1215b^{14}y^8 + 675b^7y^{16} + 125y^{24}$
c) $(5y^4+5u^8)^3$	$125y^{12} + 375y^8u^4 + 375y^4u^8 + 125u^{24}$	d) $(8k^{11}-6d^{10})^3$	$512k^{33} - 1152k^{22}d^{10} + 864k^{11}d^{20} - 216d^{30}$
e) $(10v^6+5f^{11})^3$	$1000v^{18} + 1500v^{12}f^{11} + 750v^6f^{22} + 125f^{33}$	f) $(2b^{12}+5y^8)^3$	$8b^{36} + 60b^{24}y^8 + 150b^{12}y^{16} + 125y^{24}$
g) $(10z^5-3x^7)^3$	$1000z^{15} - 900z^{10}x^7 + 270z^5x^{14} - 27x^{21}$	h) $(3g^4+6e^{10})^3$	$27g^{12} + 162g^8e^{10} + 324g^4e^{20} + 216e^{30}$
i) $(9u^7-6h^9)^3$	$729u^{21} - 1458u^{14}h^9 + 972u^7h^{18} - 216h^{27}$	j) $(5h^{12}+3y^{11})^3$	$125h^{36} + 225h^{24}y^{11} + 135h^{12}y^{22} + 27y^{33}$
k) $(4u^7+3j^6)^3$	$64u^{21} + 144u^{14}j^6 + 108u^7j^{12} + 27j^{18}$	l) $(8j^5+3x^7)^3$	$512j^{15} + 576j^{10}x^7 + 216j^5x^{14} + 27x^{21}$
m) $(4j^3+5f^3)^3$	$64j^9 + 240j^6f^3 + 300j^3f^6 + 125f^9$	n) $(12w^2+6g^5)^3$	$1728w^6 + 2592w^4g^5 + 1296w^2g^{10} + 216g^{15}$
o) $(5b^8+5e^9)^3$	$125b^{24} + 375b^{16}e^9 + 375b^8e^{18} + 125e^{27}$	p) $(6e^3-2c^8)^3$	$216e^9 - 216e^6c^8 + 72e^3c^{16} - 8c^{24}$
q) $(6k^6+5b^5)^3$	$216k^{18} + 540k^{12}b^5 + 450k^6b^{10} + 125b^{15}$	r) $(2k^4+4f^5)^3$	$8k^{12} + 48k^8f^5 + 96k^4f^{10} + 64f^{15}$
s) $(11y^5-4g^3)^3$	$1331y^{15} - 1452y^{10}g^3 + 528y^5g^6 - 64g^9$	t) $(12y^2-4u^{12})^3$	$1728y^6 - 1728y^4u^{12} + 576y^2u^{24} - 64u^{36}$
u) $(3e^5+5c^2)^3$	$27e^{15} + 135e^{10}c^2 + 225e^5c^4 + 125c^6$	v) $(4z^8-6b^9)^3$	$64z^{24} - 288z^{16}b^9 + 432z^8b^{18} - 216b^{27}$
w) $(4u^5+2w^9)^3$	$64u^{15} + 96u^{10}w^9 + 48u^5w^{18} + 8w^{27}$	x) $(10x^6-4h^{11})^3$	$1000x^{18} - 1200x^{12}h^{11} + 480x^6h^{22} - 64h^{33}$

7. Bontsd fel a zárójeleket!

- a)  $(3j^6+3e^8-5h^6)^2$   $9_{12}f_{96}y_{90}j_{69}-30y_{86}e_{90}j_{81}+27z_{12}y_{25}j_{12}+9_{16}e_{6}+z_{12}f_{96}$
- b)  $(5w^9-4y^9+2d^{12})^2$   $25_{18}m_{18}y_{18}+16_{18}y_{18}+4_{24}d_{24}p_{12}m_{12}-16_{9}y_{9}p_{12}m_{12}+20_{12}p_{12}m_{12}$
- c)  $(5w^8+3j^8+4a^{10})^2$   $25_{16}m_{16}y_{16}+9_{16}j_{16}+16_{20}v_{20}m_{20}j_{18}f_{8}+24_{10}v_{10}m_{10}f_{8}+4_{10}v_{10}m_{10}$
- d)  $(12z^{12}+5y^7+6h^{11})^2$   $144_{24}z_{24}+25_{14}y_{14}+36_{22}y_{22}z_{12}h_{12}+60_{11}y_{11}z_{12}h_{11}+144_{12}z_{12}y_{11}h_{11}$
- e)  $(9z^3+5b^6+3w^4)^2$   $81_{9}z_{9}+25_{12}y_{12}+9_{8}w_{8}+36_{6}z_{6}y_{6}+30_{4}m_{4}y_{4}b_{4}+54_{3}m_{3}z_{3}$
- f)  $(10a^6-2h^2+6e^3)^2$   $100_{12}a_{12}+44_{4}e_{4}+36_{6}e_{6}h_{2}-40_{6}y_{2}e_{3}+120_{6}e_{3}e_{3}$
- g)  $(5h^{12}+2x^4+6g^8)^2$   $25_{24}h_{24}+4_{24}x_{24}+36_{16}g_{16}h_{12}x_{12}+24_{4}x_{4}g_{8}+60_{12}g_{12}h_{12}$
- h)  $(4h^7+6a^{11}-2f^7)^2$   $16_{14}h_{14}+36_{22}a_{22}+4_{14}f_{14}h_{14}+48_{7}a_{11}h_{11}f_{11}-24_{7}f_{7}h_{7}f_{7}$
- i)  $(4w^8-6k^5+6y^{12})^2$   $16_{16}w_{16}+36_{10}y_{10}+36_{24}y_{24}w_{8}k_{5}-48_{8}w_{8}k_{5}y_{12}+48_{8}w_{8}y_{12}k_{5}$
- j)  $(8h^{11}-5a^9-2d^{11})^2$   $64_{22}h_{22}+25_{18}a_{18}+4_{22}d_{22}h_{11}a_{9}-80_{11}h_{11}a_{9}d_{11}+20_{9}a_{9}d_{11}p_{11}$
- k)  $(2d^9+2u^7-2f^3)^2$   $4_{18}d_{18}+4_{14}u_{14}+4_{6}f_{6}d_{9}u_{8}-8_{9}f_{3}d_{9}u_{8}$
- l)  $(10a^{11}+5g^{10}-6w^2)^2$   $100_{22}a_{22}+25_{20}g_{20}+36_{4}w_{4}a_{11}g_{10}-60_{10}w_{10}a_{11}g_{10}-120_{11}w_{11}a_{11}g_{11}$
- m)  $(7k^5+5e^{11}+2y^9)^2$   $49_{10}k_{10}+25_{10}e_{10}+4_{22}y_{22}k_{18}e_{11}+20_{11}y_{11}e_{11}k_{9}+28_{5}y_{5}k_{9}$
- n)  $(8b^2-3g^7+3u^4)^2$   $64_{4}b_{4}+9_{14}g_{14}+9_{4}u_{4}b_{14}g_{14}-48_{8}b_{8}g_{7}u_{4}-18_{7}g_{7}u_{7}b_{4}$
- o)  $(9h^2-2b^{10}+4w^8)^2$   $81_{18}h_{18}+4_{20}b_{20}+16_{16}w_{16}h_{16}b_{10}w_{10}h_{10}+16_{8}w_{8}h_{10}b_{10}w_{8}$
- p)  $(11e^8-2x^2-3k^{10})^2$   $121_{16}e_{16}+4_{4}x_{4}+9_{20}k_{20}e_{8}x_{2}+44_{8}e_{8}x_{2}k_{10}-66_{10}k_{10}e_{10}x_{10}$
- q)  $(3f^9-6y^8+6u^3)^2$   $9_{18}f_{18}+9_{16}y_{16}+9_{6}u_{6}f_{18}y_{9}-9_{6}y_{9}f_{9}u_{3}-8_{8}y_{8}f_{8}u_{3}+3_{6}f_{6}y_{6}u_{3}$