







Laplacian Smoothing

We usually compute the probability of a word given a class as follows:

$$P\left(\mathbf{w_i} \mid ext{ class} \;
ight) = rac{\operatorname{freq}\left(\mathbf{w_i}, \operatorname{class} \;
ight)}{N_{\operatorname{class}}} \quad \operatorname{class} \; \in \left\{ \; \operatorname{Positive}, \operatorname{Negative} \;
ight\}$$

However, if a word does not appear in the training, then it automatically gets a probability of 0, to fix this we add smoothing as follows

$$P\left(\mathbf{w_i} \mid \mathbf{class}
ight) = rac{\mathrm{freq}(\mathbf{w_i}, \, \mathrm{class} \,) + 1}{(\mathrm{N_{class}} + \mathrm{V})}$$

Note that we added a 1 in the numerator, and since there are V words to normalize, we add V in the denominator.

 N_{class} : frequency of all words in class

V: number of unique words in vocabulary