Logistic Regression Cross Entropy

Objective

How Cross-Entropy using random initialization influence the accuracy of the model.

Table of Contents

In this lab, you will review how to make a prediction in several different ways by using PyTorch.

- 1. Get Some Data
- 2. Create the Model and Total Loss Function
- 3. Train the Model via Batch Gradient Descent

Estimated Time Needed: 15 min

Preparation

We'll need the following libraries:

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
import torch
from torch.utils.data import Dataset, DataLoader
import torch.nn as nn
```

The class plot_error_surfaces is just to help you visualize the data space and the parameter space during training and has nothing to do with Pytorch.

```
In [2]: # Create class for plotting and the function for plotting

class plot_error_surfaces(object):

# Constructor

def __init__(self, w_range, b_range, X, Y, n_samples = 30, go = True):
    W = np.linspace(-w_range, w_range, n_samples)
    B = np.linspace(-b_range, b_range, n_samples)
    w, b = np.meshgrid(W, B)
    Z = np.zeros((30, 30))
    count1 = 0
    self.y = Y.numpy()
    self.x = X.numpy()
    for w1, b1 in zip(w, b):
        count2 = 0
        for w2, b2 in zip(w1, b1):
```

```
yhat= 1 / (1 + np.exp(-1*(w2*self.x+b2)))
            Z[count1, count2] = -1*np.mean(self.y*np.log(yhat+1e-16) + (1-self.y)*np.log(1)
            count2 += 1
        count1 += 1
    self.Z = Z
    self.w = w
    self.b = b
    self.W = []
    self.B = []
    self.LOSS = []
    self.n = 0
    if go == True:
        plt.figure()
        plt.figure(figsize=(7.5, 5))
        plt.axes(projection='3d').plot_surface(self.w, self.b, self.Z, rstride=1, cstr
        plt.title('Loss Surface')
        plt.xlabel('w')
        plt.ylabel('b')
        plt.show()
        plt.figure()
        plt.title('Loss Surface Contour')
        plt.xlabel('w')
        plt.ylabel('b')
        plt.contour(self.w, self.b, self.Z)
        plt.show()
# Setter
def set_para_loss(self, model, loss):
    self.n = self.n + 1
    self.W.append(list(model.parameters())[0].item())
    self.B.append(list(model.parameters())[1].item())
    self.LOSS.append(loss)
# Plot diagram
def final_plot(self):
    ax = plt.axes(projection='3d')
    ax.plot_wireframe(self.w, self.b, self.Z)
    ax.scatter(self.W, self.B, self.LOSS, c='r', marker='x', s=200, alpha=1)
    plt.figure()
    plt.contour(self.w, self.b, self.Z)
    plt.scatter(self.W, self.B, c='r', marker='x')
    plt.xlabel('w')
    plt.ylabel('b')
    plt.show()
# Plot diagram
def plot_ps(self):
    plt.subplot(121)
    plt.ylim
    plt.plot(self.x, self.y, 'ro', label="training points")
    plt.plot(self.x, self.W[-1] * self.x + self.B[-1], label="estimated line")
    plt.plot(self.x, 1 / (1 + np.exp(-1 * (self.W[-1] * self.x + self.B[-1]))), label=
    plt.xlabel('x')
    plt.ylabel('y')
    plt.ylim((-0.1, 2))
    plt.title('Data Space Iteration: ' + str(self.n))
    plt.show()
    plt.subplot(122)
    plt.contour(self.w, self.b, self.Z)
    plt.scatter(self.W, self.B, c='r', marker='x')
    plt.title('Loss Surface Contour Iteration' + str(self.n))
    plt.xlabel('w')
```

```
plt.ylabel('b')

# Plot the diagram

def PlotStuff(X, Y, model, epoch, leg=True):
    plt.plot(X.numpy(), model(X).detach().numpy(), label=('epoch ' + str(epoch)))
    plt.plot(X.numpy(), Y.numpy(), 'r')
    if leg == True:
        plt.legend()
    else:
        pass
```

Set the random seed:

```
In [3]: # Set random seed
torch.manual_seed(0)
```

Out[3]: <torch._C.Generator at 0x1ac4d012410>

Get Some Data

```
In [4]: # Create the data class

class Data(Dataset):

    # Constructor
    def __init__(self):
        self.x = torch.arange(-1, 1, 0.1).view(-1, 1)
        self.y = torch.zeros(self.x.shape[0], 1)
        self.y[self.x[:, 0] > 0.2] = 1
        self.len = self.x.shape[0]

# Getter

def __getitem__(self, index):
    return self.x[index], self.y[index]

# Get Length

def __len__(self):
    return self.len
```

Make Data object

```
In [5]: # Create Data object
data_set = Data()
```

Create the Model and Total Loss Function

Create a custom module for logistic regression:

```
In [6]: # Create Logistic_regression class
    class logistic_regression(nn.Module):
```

```
# Constructor
def __init__(self, n_inputs):
    super(logistic_regression, self).__init__()
    self.linear = nn.Linear(n_inputs, 1)

# Prediction
def forward(self, x):
    yhat = torch.sigmoid(self.linear(x))
    return yhat
```

Create a logistic regression object or model:

```
In [7]: # Create the logistic_regression result
model = logistic_regression(1)
```

Replace the random initialized variable values. Theses random initialized variable values did convergence for the RMS Loss but will converge for the Cross-Entropy Loss.

```
In [8]: # Set the weight and bias

model.state_dict() ['linear.weight'].data[0] = torch.tensor([[-5]])
model.state_dict() ['linear.bias'].data[0] = torch.tensor([[-10]])
print("The parameters: ", model.state_dict())
```

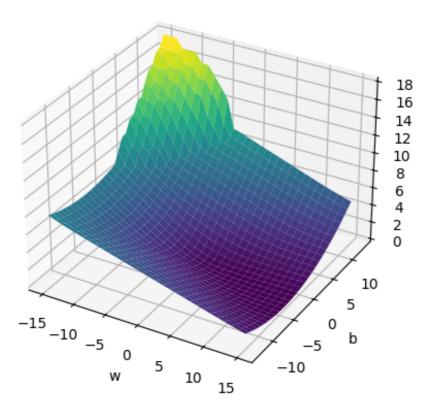
The parameters: OrderedDict({'linear.weight': tensor([[-5.]]), 'linear.bias': tensor([-1 0.])})

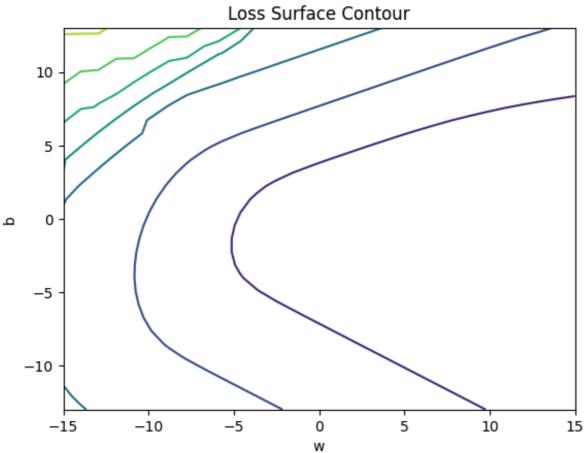
Create a plot_error_surfaces object to visualize the data space and the parameter space during training:

```
In [9]: # Create the plot_error_surfaces object
get_surface = plot_error_surfaces(15, 13, data_set[:][0], data_set[:][1], 30)
```

<Figure size 640x480 with 0 Axes>

Loss Surface





Define the cost or criterion function:

```
In [10]: # Create dataloader, criterion function and optimizer

def criterion(yhat,y):
    out = -1 * torch.mean(y * torch.log(yhat) + (1 - y) * torch.log(1 - yhat))
    return out
```

```
# Build in criterion
# criterion = nn.BCELoss()

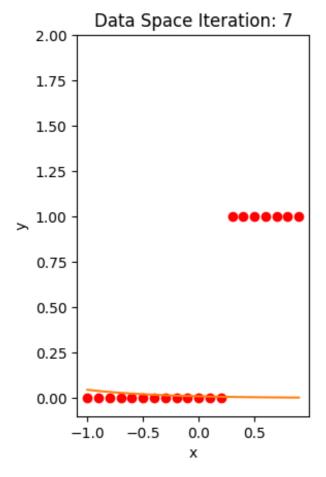
trainloader = DataLoader(dataset = data_set, batch_size = 3)
learning_rate = 2
optimizer = torch.optim.SGD(model.parameters(), lr = learning_rate)
```

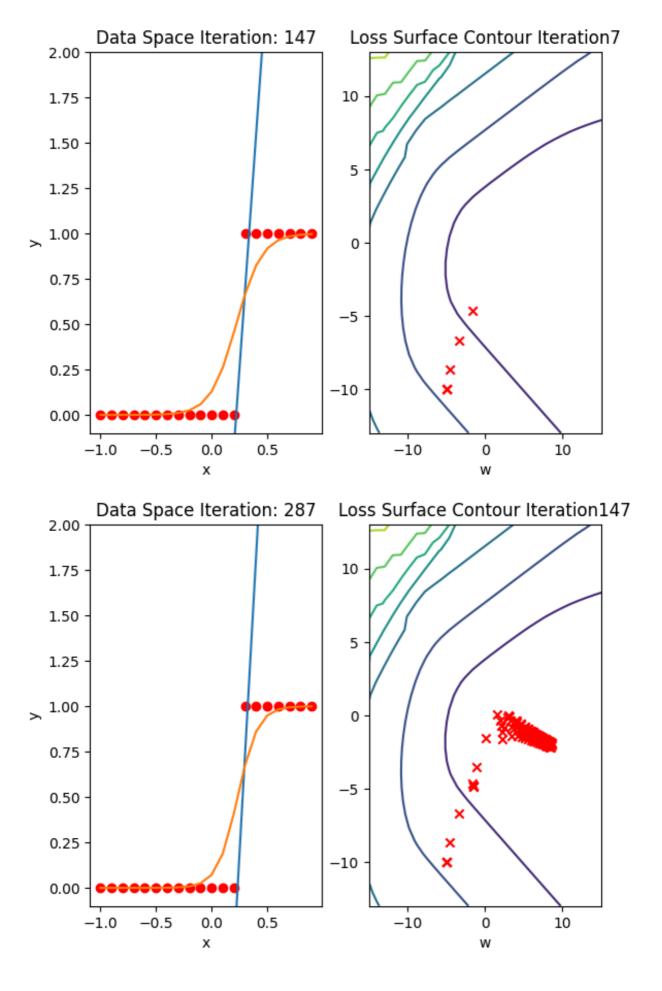
Train the Model via Batch Gradient Descent

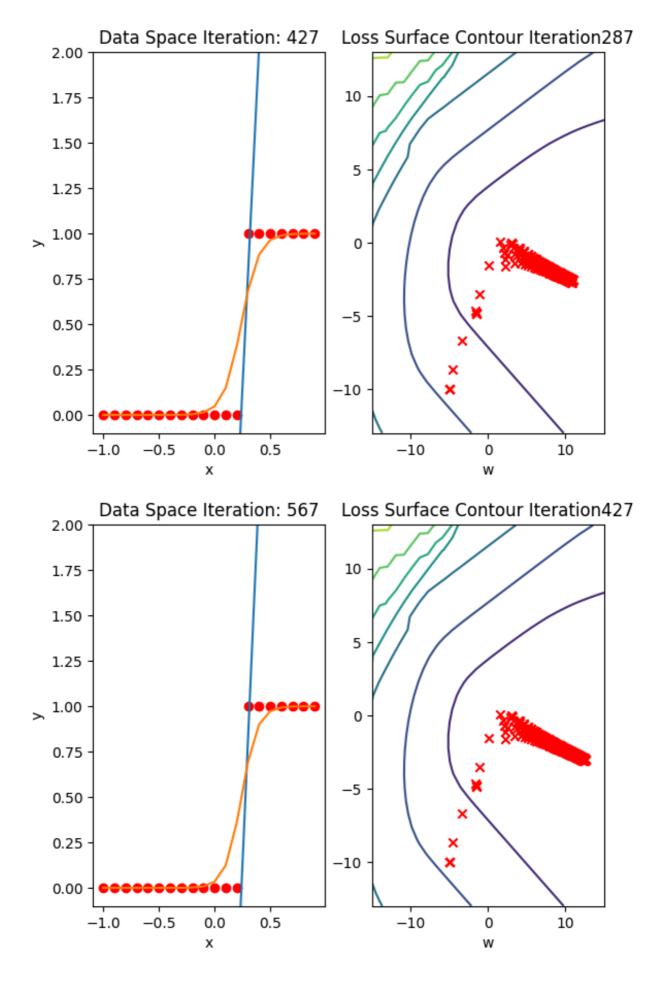
Train the model

```
In [11]: # Train the Model

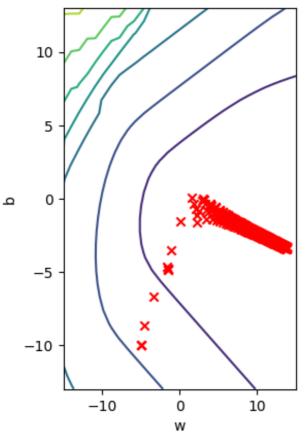
def train_model(epochs):
    for epoch in range(epochs):
        for x, y in trainloader:
            yhat = model(x)
            loss = criterion(yhat, y)
            optimizer.zero_grad()
            loss.backward()
            optimizer.step()
            get_surface.set_para_loss(model, loss.tolist())
        if epoch % 20 == 0:
            get_surface.plot_ps()
```







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Get the actual class of each sample and calculate the accuracy on the test data:

```
In [12]: # Make the Prediction

yhat = model(data_set.x)
    label = yhat > 0.5
    print("The accuracy: ", torch.mean((label == data_set.y.type(torch.ByteTensor)).type(torch
    The accuracy: tensor(1.)
```

The accuracy is perfect.