



# VISION-BASED EQUATION SOLVER VISION-BASED EQUATION SOLVER OLIGINATION SOLVER OLIGIN

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# PROBLEM

Recognizing mathematical equations from images: process, segment and recognize the digits to compute the final result.

#### Input

Images containing handwritten mathematical equations.

#### **Ouput**

Result of the equation.

#### Challenges

Variability in handwriting, symbol complexity, and image quality.

# IMAGE CLEANING

To accurately segment and predict symbols with a CNN, clear number display in images is crucial. **Noise Reduction** 

**Brightness Adjustment** 

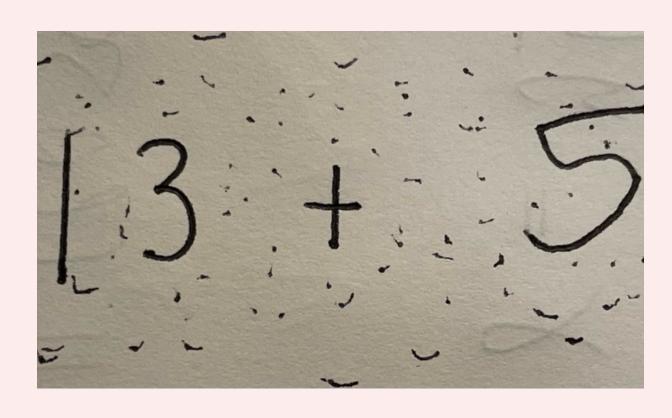
**Histogram Equalization** 

62 - 40

 $\longrightarrow 62 - 40$ 

# **NOISE REDUCTION**

Removing noise from photos



### **VERSION 1**

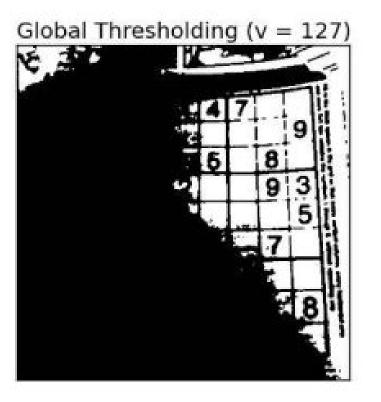
- Thresholding
- Blurring

### **VERSION 2**

- Shadow removal
- Erosion
- Adaptive thresholding

# **ADAPTIVE THRESHOLDING**









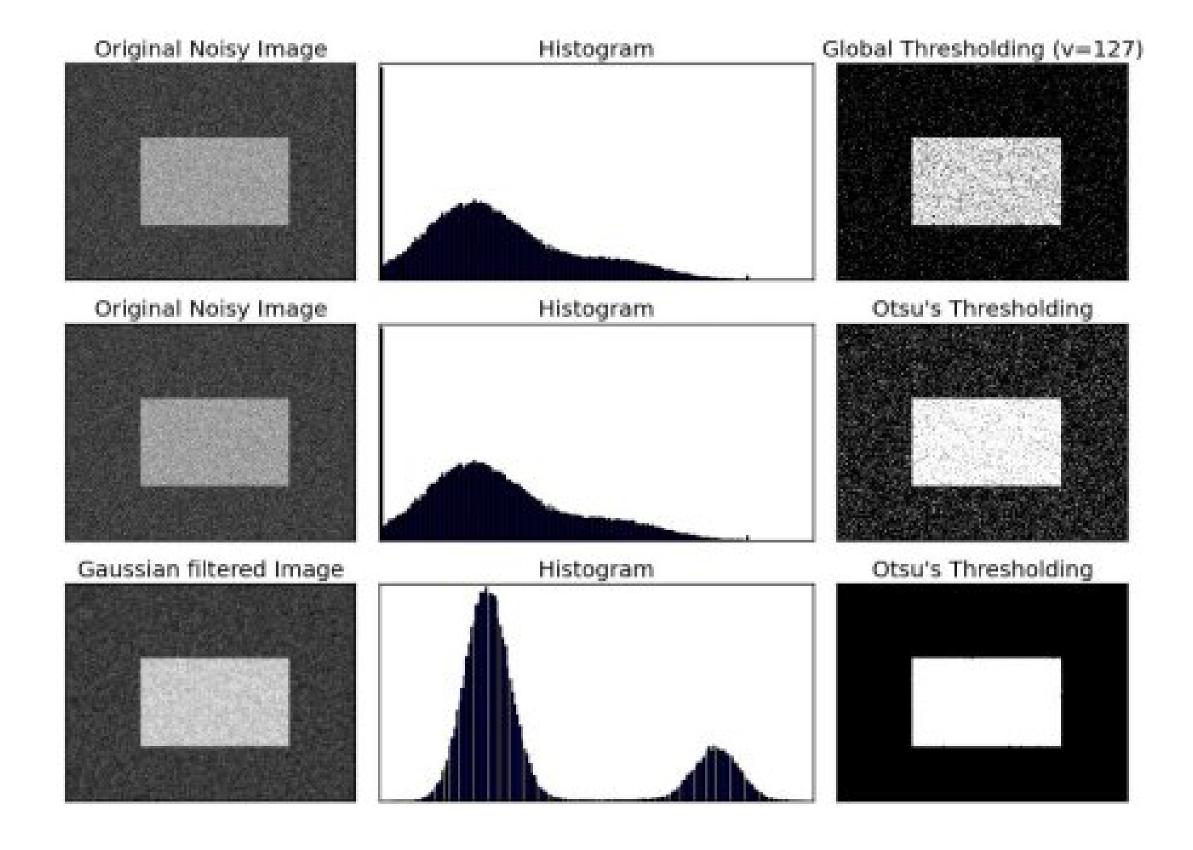
### **ADAPTIVE MEAN**

Thresholds areas based on the mean intensity of the neighborhood area

### **ADAPTIVE GAUSSIAN**

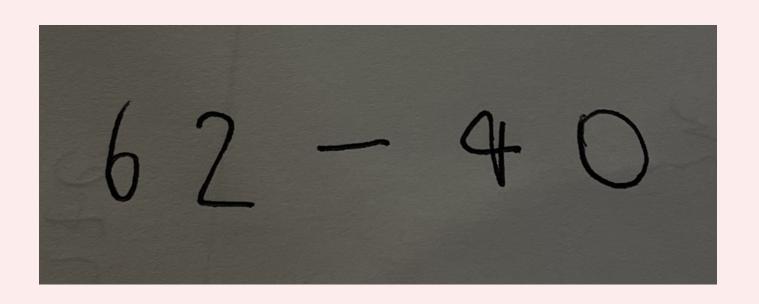
Thresholds areas based on the Gaussian weighted sum of the neighborhood area. Weight each intensity by a Gaussian kernel, then take the sum of all elements.

# OTSU'S BINARIZATION



# BRIGHTNESS ADJUSTMENT

Adjusting the brightness in order to improve photo with low brightness to be recognized

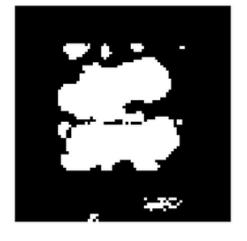


### **ISSUES**

- Makes the background more prominent than the text
- Complicates textbackground contrast







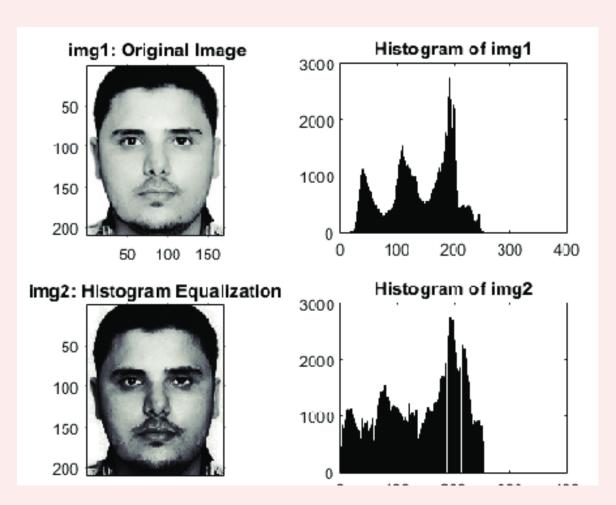
Threshold, Bright



Threshold, Original

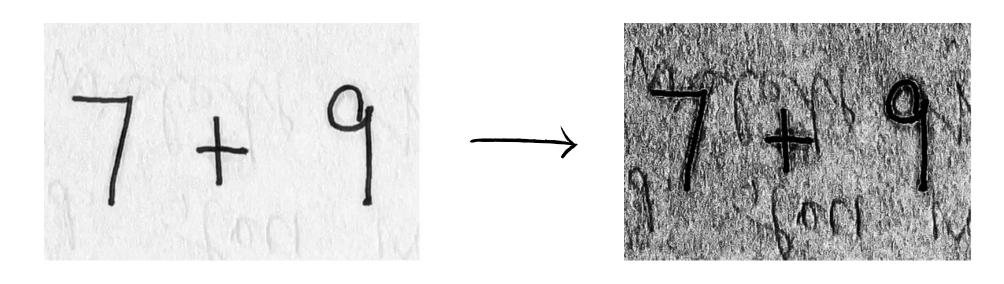
# HISTOGRAM EQUALIZATION

For adjusting image contrasts. To enhance low-contrast images, especially where symbols are faint or background lighting is poor.



### **ISSUES**

- Amplification of background features.
- Unwanted enhancement of noise



# IMAGE SEGMENTATION

Photos of equations need to be separated into their constituent symbols so that each symbol can be fed as input to the neural network.





# CONTOURING

Segmenting the images by contouring

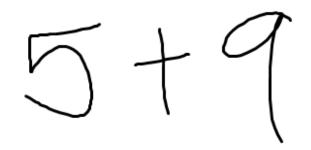




**Bounding Rectangles** 

# CONTOUR DETECTION

Identify the outlines of objects and shapes in an image



- cv2.findContours function used for detecting contours in an image.
- Analyzes a binary image and returns a list of contours found.

# CONTOUR PROCESSING

Processing the contours identified in an image

Sorting contours based on their x-coordinate

• Ignoring child contours



# BOUNDING RECTANGLES

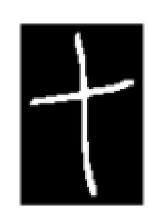
Encloses a contour and isolates individual symbols from the rest of the image.

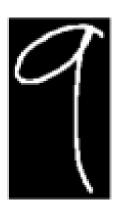
5+9

Original Image

- Isolates individual symbols from the rest of the image.
- The area within this rectangle is then cut out from the original binary image



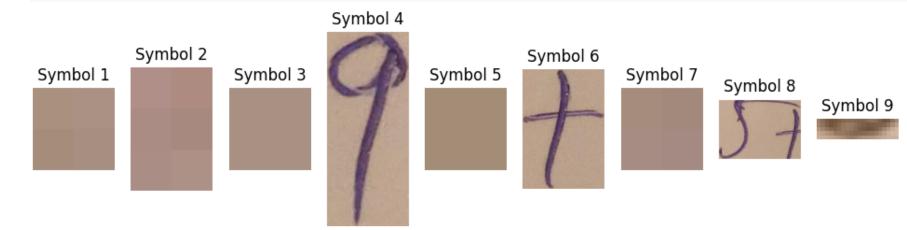


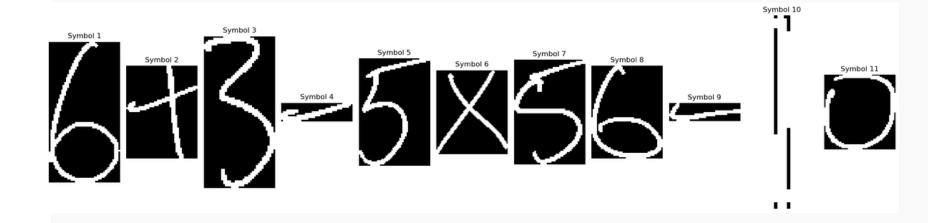


# ISSUES

There are examples of what we needed to fix.

These issues usually revolve around the shape and nature of the symbol.





### **EXAMPLES**

- Division symbol
- Equals sign

These numbers have a common theme





# FIXING THE ISSUE

- We examine two separate contours.
- The edges are compared.
- Merging based on threshold.

#### A visual example:



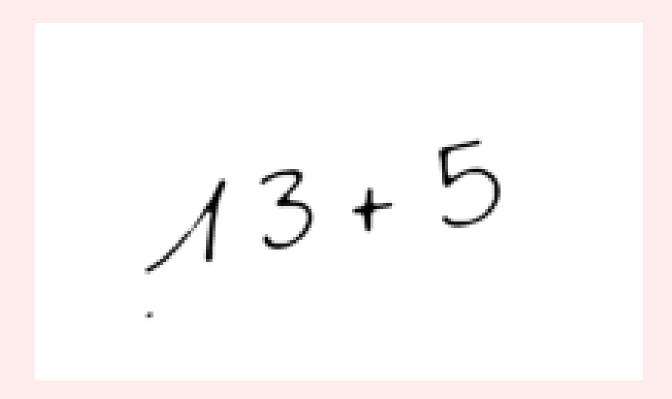
Contours with no merging



After merging contours to display a symbol

# MEAN SHIFT FILTERING

Decomposes an image into its constituent symbols based on the clustering of feature points.



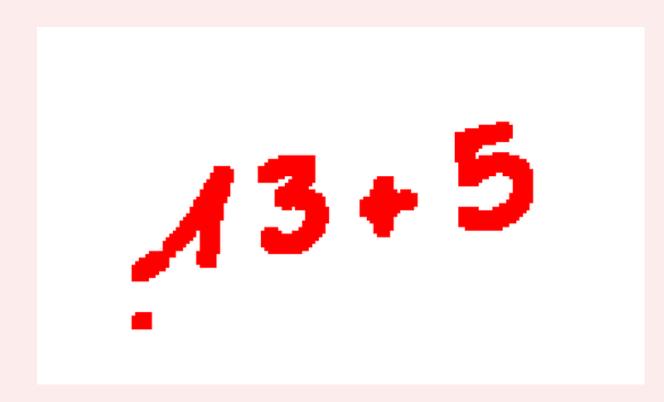
Harris corner detection

 Mean Shift Clustering groups feature points.

 Iterative processing of clusters to extract symbols.

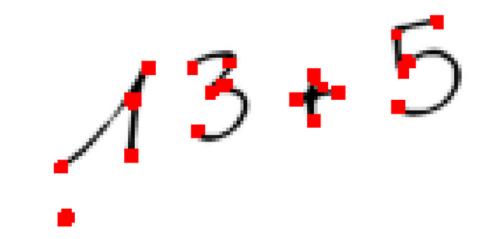
# HARRIS CORNER DETECTION

Find special points in the image



### **ISSUES**

- Noise
- Density



### **SOLUTION**

Hyper-parameters tuning

# **CLUSTERING**

Find the groups of points that are close with **Mean Shift Algorithm** 



### **ISSUES**

- Underfitting
- Overfitting
- Number of clusters



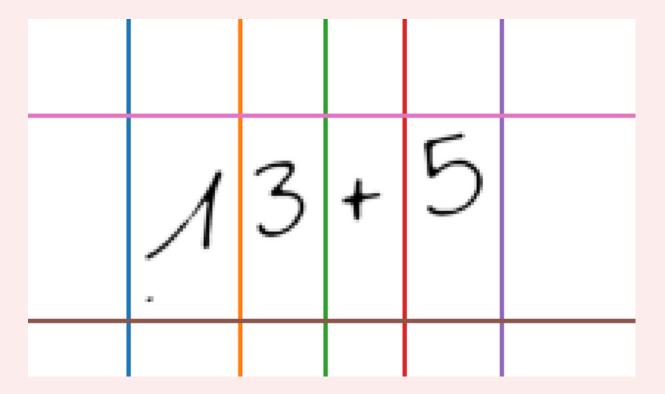


### **SOLUTION**

- Hyper-parameters tuning
- Filtering

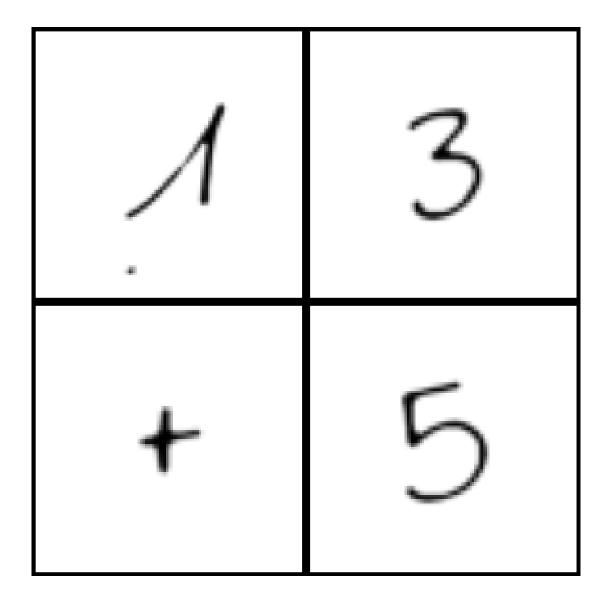
# SYMBOLS EXTRACTING

Decompose the original image in smaller images with one digit each



### **RESULTS & ISSUES**

- This method is scale sensible
- We are able to get good results in general



# IMAGE RECOGNITION

Cleaned up and segmented images are now ready to be recognized.

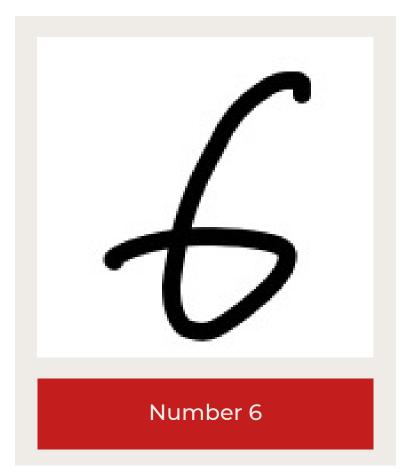


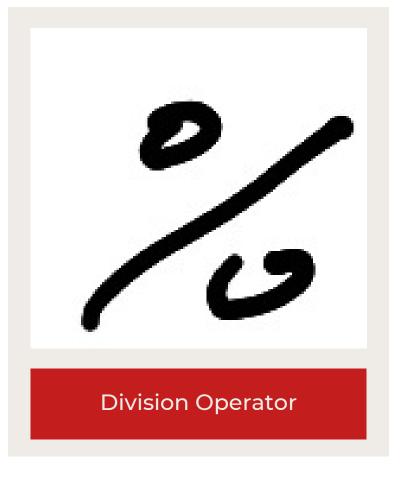




# **DATASET**

- Handwritten
- No noise
- 554 images for each symbol
- Each image 155x135 pixels

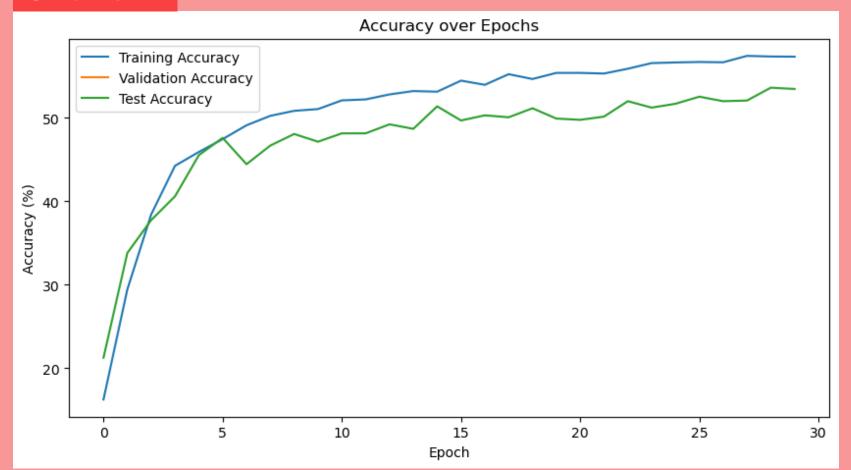




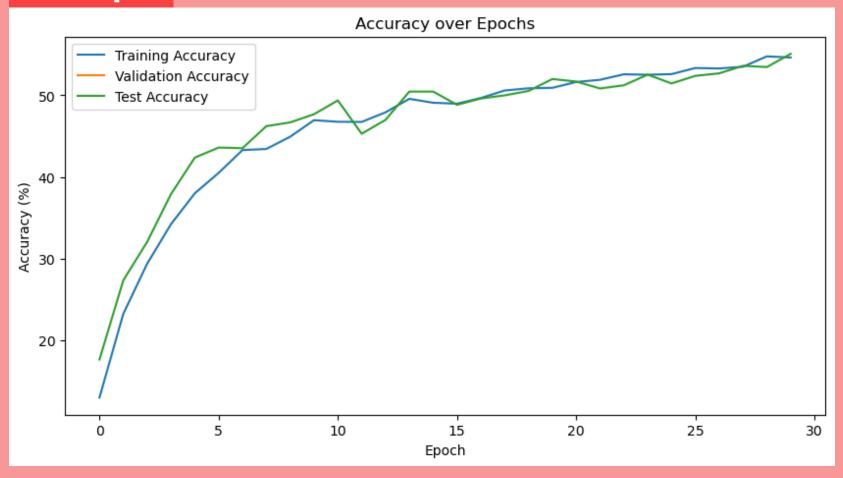
# MLP

- Shallow and Deep MLP have low accuracy
- Not able learn the features

#### **Shallow**

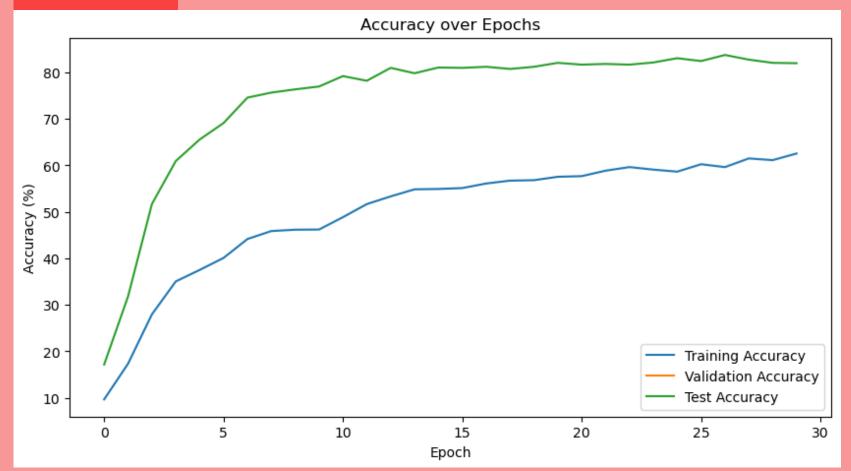


#### Deep

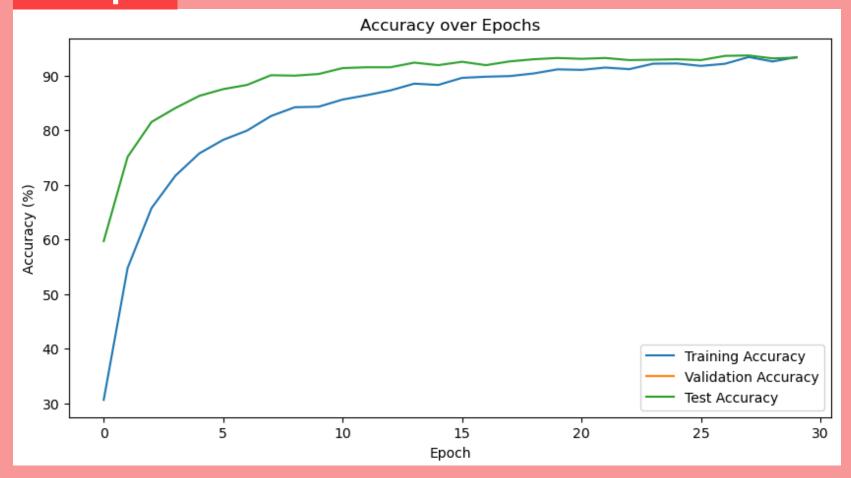


- CNNs perform better
- Shallow CNN is biased
- Deep CNN has very good accuracy and generalization capabilities

#### **Shallow**



#### Deep



# OUR BEST MODEL

2 CONV

32 filters Kernel size of 3

1 MAX-POOL

2 FULLY-CONNECTED

93.4%

Train Accuracy

0.18

Train Loss

93.3%

Test Accuracy

0.27

Test Loss

# FUTURE WORK

Next steps to make a better product.

Scale invariant segmentation

Recognizing symbols at different angle

Larger dataset

# LIVE DEMO

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# THANK YOU

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# CONTRIBUTIONS



Led Image Cleaning



Led Image Recognition



Led Image Segmentation



Led Image Contouring



Led Image Contouring