

QUESTION 1 - SOLUTION:

State 1:	State 2:
P_1	P_2
$T_1 = 25^\circ\text{C} = 298\text{ K}$	$T_2 = 500\text{ K}$
$V_1 = 0,8\text{ m}^3$	$V_1 = V_2 = 0,8\text{ m}^3$

$$m_{\text{air}} = 5,2\text{ kg}$$

$$R_{\text{air}} = 0,287\text{ kJ/kg}\cdot\text{K}$$

A) From the gas perfect law for state 1:

$$P_1 \cdot V_1 = m \cdot R \cdot T_1 \Rightarrow P_1 \cdot 0,8\text{ [m}^3\text{]} = 5,2\text{ [kg]} \cdot 0,287\text{ [}\frac{\text{kJ}}{\text{kg}\cdot\text{K}}\text{]} \cdot 298\text{ [K]}$$

$$\Rightarrow P_1 = \frac{5,2 \cdot 0,287 \cdot 298\text{ [kJ]}}{0,8\text{ [m}^3\text{]}} = 555,92 \cdot \frac{\text{kJ}}{\text{m}^3} =$$

$$= 555,92 \cdot 10^3 \frac{\text{N}\cdot\text{m}}{\text{m}^3} \cdot \frac{\text{m}^3}{\text{N}} \cdot P_0 \Rightarrow \boxed{P_1 = 5,56\text{ bar}}$$

B) The ideal gas equation for states 1 & 2 are written below

$$\left. \begin{array}{l} \text{State 1: } P_1 \cdot V_1 = m R T_1 \\ \text{State 2: } P_2 \cdot V_2 = m R T_2 \end{array} \right\} \begin{array}{l} \text{①} \\ \text{②} \end{array} \Rightarrow \frac{P_1 \cdot V_1 = m R T_1}{P_2 \cdot V_2 = m R T_2} \Rightarrow \frac{P_1}{P_2} = \frac{T_1}{T_2} \Rightarrow$$

$$P_2 = \frac{P_1 \cdot T_2}{T_1} = 5,56\text{ [bar]} \cdot \frac{500}{298} = \boxed{9,33\text{ bar}}$$

C) The work done in the process $W = \int_{V_1}^{V_2} P \cdot dV = P [V_2 - V_1]$

$$\Rightarrow \boxed{W = 0}$$

Question 2 - Solution:

The work during a polytropic process is given by:

$$W = \frac{P_2 \cdot V_2 - P_1 \cdot V_1}{1 - n} \quad (1)$$

From the ideal gas law for state 1:

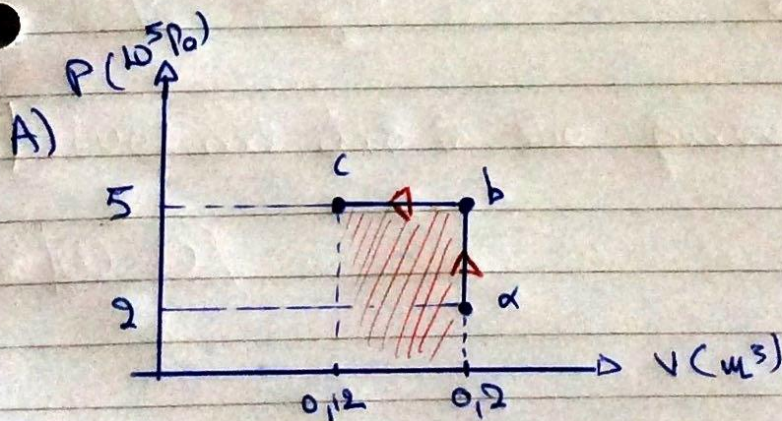
$$P_1 \cdot V_1 = n R T_1 \Rightarrow n \cdot R = \frac{P_1 \cdot V_1}{T_1} = \frac{400 \cdot 10^3 \text{ Pa} \cdot 0,3 \text{ m}^3}{383 \text{ K}} \Rightarrow$$

$$n \cdot R = \frac{120 \cdot 10^3 [\text{Pa} \cdot \text{m}^3]}{383 \text{ K}} = \frac{120 \text{ kJ}}{383 \text{ K}} = \boxed{0,313 \frac{[\text{kJ}]}{[\text{K}]}}$$

From equation (1) $W = \frac{P_2 \cdot V_2 - P_1 \cdot V_1}{1 - n} \Rightarrow W = \frac{n R T_2 - n R T_1}{1 - n} \Rightarrow$

$$W = \frac{n \cdot R [T_2 - T_1]}{1 - 1,2} = \frac{0,313 \left[\frac{\text{kJ}}{\text{K}} \right] \cdot [673 - 383] \cdot \cancel{[\text{K}]}}{-0,2} = 0$$

$$W = -453,85 \text{ kJ}$$

Question 3 - Solution:

B) The work done during process ab: $W_{ab} = 0$ [isochoric Process]

The work done during process bc: $W_{bc} = \int P \cdot dV = P \cdot [V_c - V_b] \Rightarrow$

$$\Rightarrow W_{bc} = 5 \cdot 10^5 [\text{Pa}] \cdot [-0,08] \text{ m}^3 \Rightarrow \boxed{W_{bc} = -4 \cdot 10^4 \text{ J}}$$

$$\text{Total Work: } W_{ab} + W_{bc} = \boxed{-4 \cdot 10^4 \text{ J}}$$