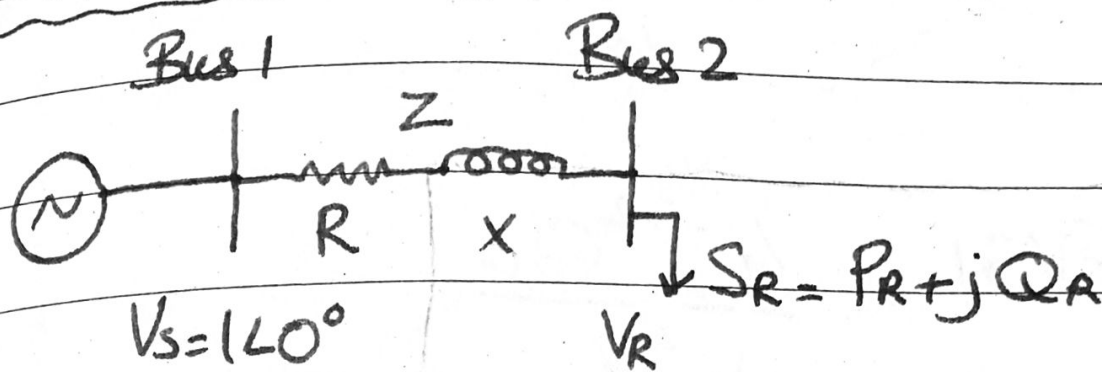


VSI Evaluations:



Note: Base values: $V_B = 20\text{KV}$; $S_B = 10\text{MVA}$

$$Z = R + jX = 2 + j1$$

#	LL1	LL2	LL3
S_R	$5 + j2.5$	$20 + j10$	$40 + j25$

$$I_B = S_B / V_B = 10 \times 10^6 / 20 \times 10^3 = 500\text{A}$$

$$Z_B = V_B^2 / S_B = (20 \times 10^3)^2 / 10 \times 10^6 = 40\Omega$$

$$Z_{pu} = \frac{Z}{Z_B} = \frac{2 + j1}{40} = 0.05 + j0.025\text{ pu}$$

$\begin{matrix} P(pu) & X(pu) \\ = 10.0559/pu \end{matrix}$

$$\text{LL1: } S_R(pu) = \frac{5 + j2.5}{10} = 0.5 + j0.25\text{ pu}$$

$= 10.559/pu$

$$\text{LL2: } S_R(pu) = \frac{20 + j10}{10} = 2 + j1\text{ pu}$$

$= 12.23607/pu$

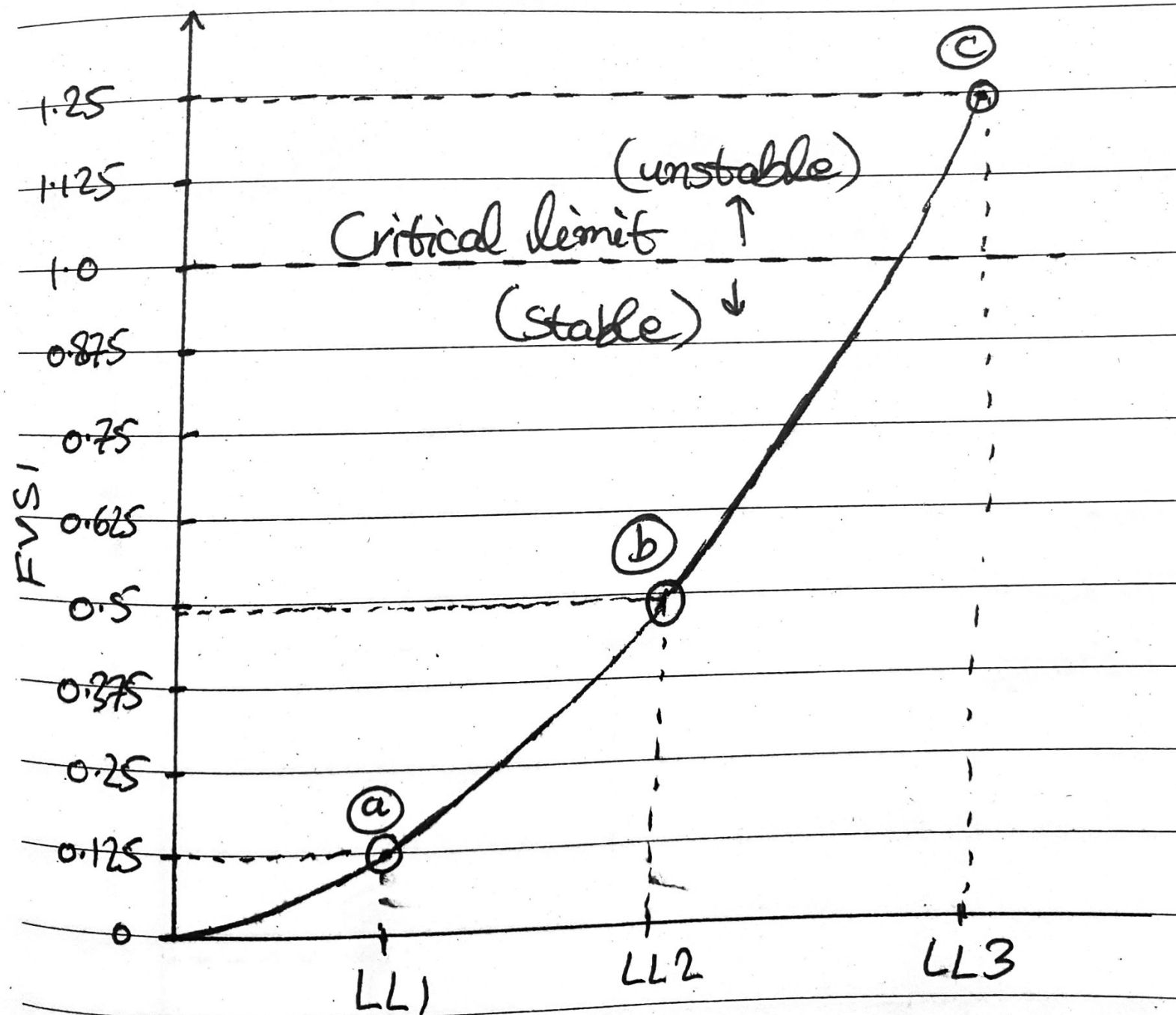
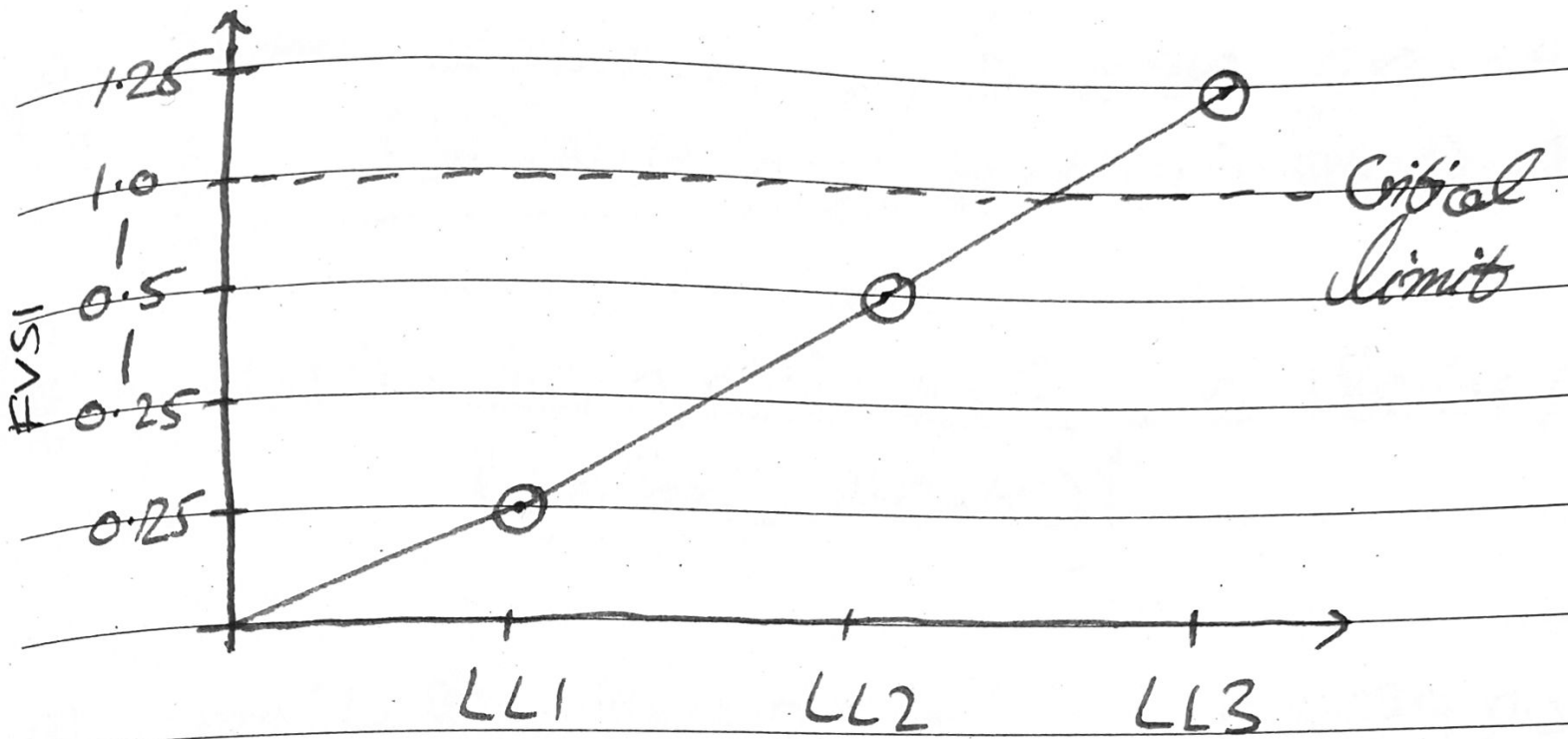
$$LL3: SR(pu) = \frac{40+j25}{10} = 4+j2.5 = 4.717 \angle 31^\circ$$

$$\textcircled{1} \quad FVSI = \frac{4Z^2 Q_r}{V_s^2 X}$$

$$\textcircled{a} \quad LL1: FVSI_{LL1} = \frac{4(0.0559)^2 \times 0.25}{(1)^2 \times 0.025} = 0.125 \text{ pu (stable)}$$

$$\textcircled{b} \quad LL2: FVSI_{LL2} = \frac{4 \times (0.0559)^2 \times 1}{(1)^2 \times 0.025} = 0.49997 \text{ pu (stable)}$$

$$\textcircled{c} \quad LL3: FVSI_{LL3} = \frac{4 \times (0.0559)^2 \times 2.5}{(1)^2 \times 0.025} = 1.25 \text{ pu (unstable)}$$



②

$$L_{mn} = \frac{4 \times Q_r}{(V_s \sin(\theta - \delta))^2}$$

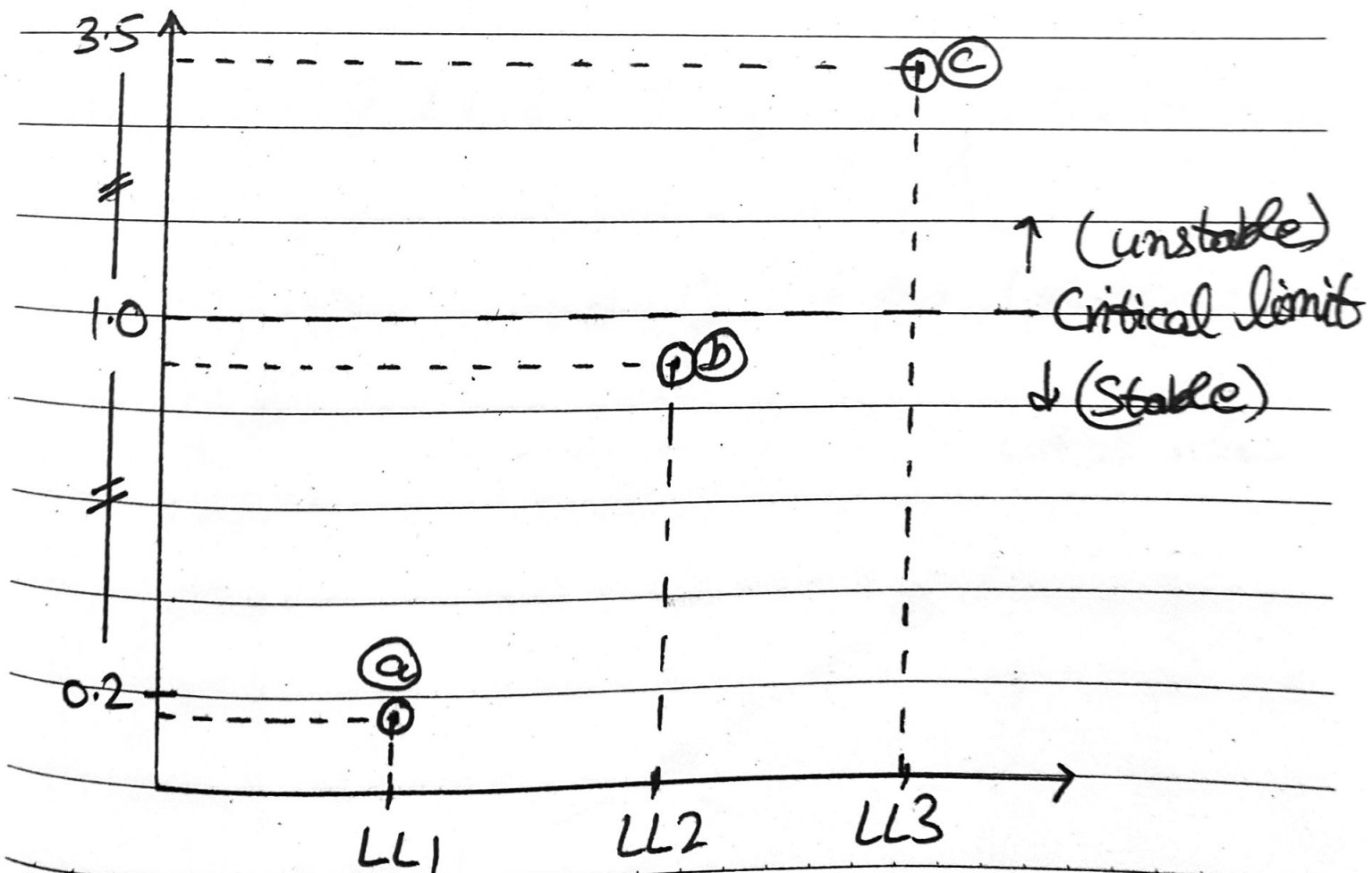
$$\theta = 25.84^\circ; \cos \theta = 0.9$$

$$\delta = 4^\circ (LL1); 7^\circ (LL2); 10^\circ (LL3)$$

$$a) L_{mn}(LL1) = \frac{4 \times 0.025 \times 0.25}{(1.0 \sin(25.84^\circ - 4^\circ))^2} = 0.18064 \text{ pu}$$

$$b) L_{mn}(LL2) = \frac{4 \times 0.025 \times 1}{(1 \sin(25.84^\circ - 7^\circ))^2} = 0.9589 \text{ pu}$$

$$c) L_{mn}(LL3) = \frac{4 \times 0.025 \times 2.5}{(1 \sin(25.84^\circ - 10^\circ))^2} = 3.356 \text{ pu}$$



$$(P_s = P_R)$$

$$\textcircled{3} \quad LQP = 4 \left(\frac{X}{V_s^2} \right) \left(Q_R + \frac{P_s^2 X}{V_s^2} \right)$$

$$\textcircled{a} \quad LQP_{LL1} = 4 \left(\frac{0.025}{1.0^2} \right) \left(0.25 + \frac{0.5^2 \times 0.025}{1.0^2} \right)$$

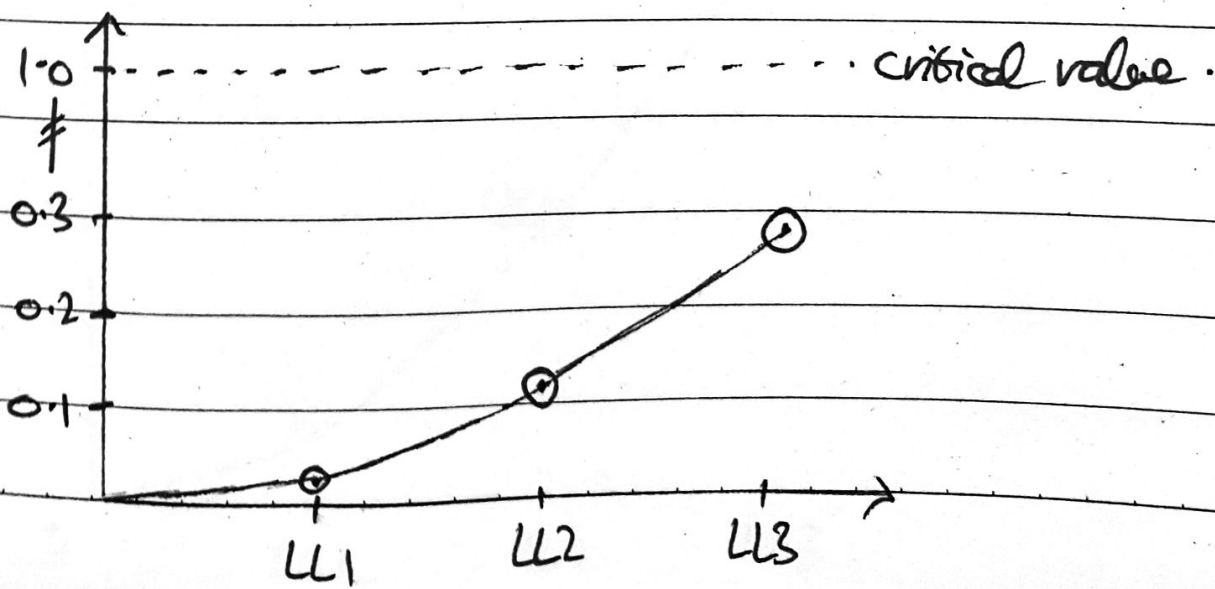
$$= 0.02625 \text{ pu (stable)}$$

$$\textcircled{b} \quad LQP_{LL2} = 4 \left(\frac{0.025}{1^2} \right) \left(1 + \frac{2^2 \times 0.025}{1^2} \right)$$

$$= 0.11 \text{ pu (stable)}$$

$$\textcircled{c} \quad LQP_{LL3} = 4 \left(\frac{0.025}{1^2} \right) \left(2.5 + \frac{4^2 \times 0.025}{1} \right)$$

$$= 0.29 \text{ pu (stable)}$$



$$\textcircled{4} \text{ NLSI} = \frac{P_r R + Q_r X}{0.25 V_s^2}$$

$$\textcircled{a} \text{ NLSI-LL1} = \frac{(0.5 \times 0.05) + (0.25 \times 0.025)}{0.25 \times 1^2}$$

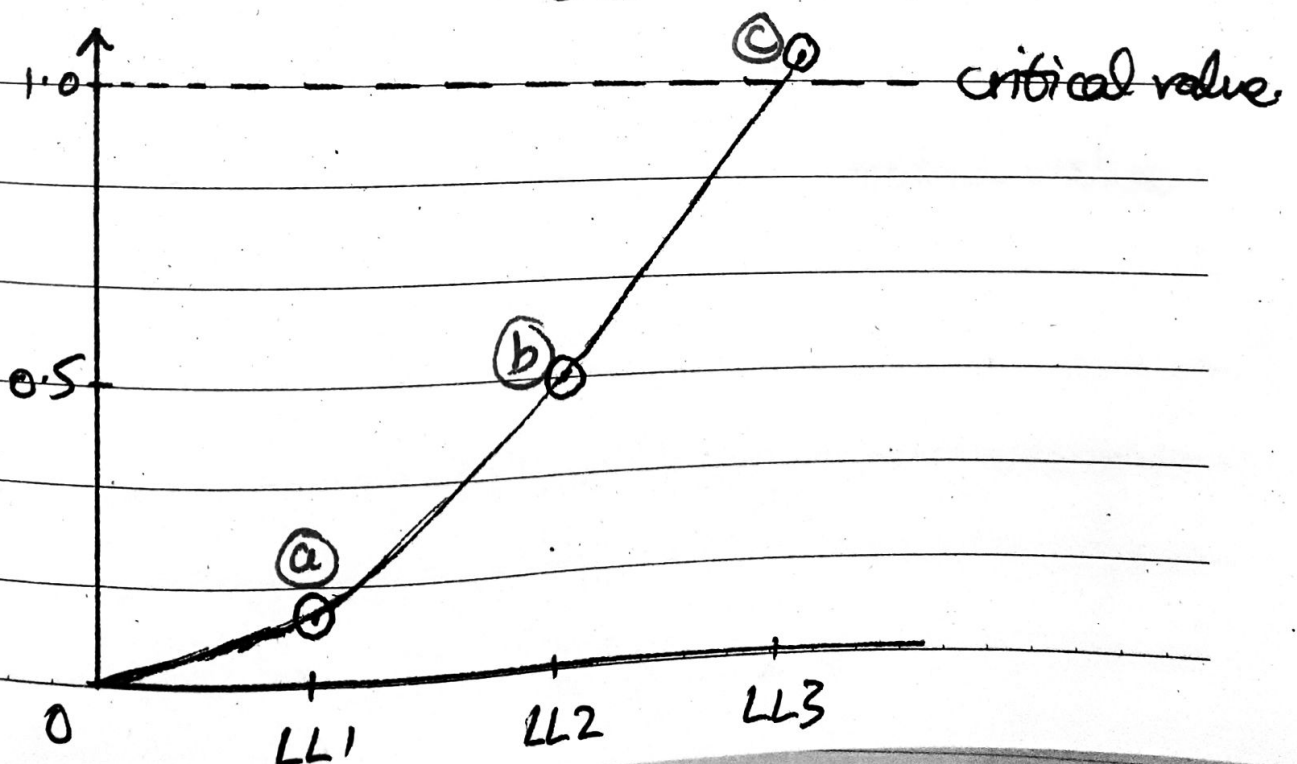
$$= 0.125$$

$$\textcircled{b} \text{ NLSI-LL2} = \frac{(2 \times 0.05) + (1 \times 0.025)}{0.25 \times 1^2}$$

$$= 0.5$$

$$\textcircled{c} \text{ NLSI-LL3} = \frac{(4 \times 0.05) + (2.5 \times 0.025)}{0.25 \times 1^2}$$

$$= 1.05$$



$$\textcircled{c} \quad VSI-2 = \frac{4Q_r(R+x)^2}{X(V_s^2 + 8RQ_r)}$$

$$\textcircled{a} \quad VSI-2(LL1) = \frac{4 \times 0.25 \times (0.05 + 0.025)^2}{0.025(1^2 + 8 \times 0.05 \times 0.25)} \\ = 0.2045$$

$$\textcircled{b} \quad VSI-2(LL2) = \frac{4 \times 1 \times (0.05 + 0.025)^2}{0.025(1^2 + 8 \times 0.05 \times 1)} \\ = 0.6429$$

$$\textcircled{c} \quad VSI-2(LL3) = \frac{4 \times (2.5) \times (0.05 + 0.025)^2}{0.025(1^2 + 8 \times 0.05 \times 2.5)} \\ = 1.125$$

