Modeling Titanic Survival

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ARTICLE HISTORY

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ABSTRACT

This short analysis showcases the development of a binary logistic model with spline transformations on predictors, to predict the possibility of survival in the loss of Titanic. I demonstrate the overall modeling process, including preprocessing, exploratory analysis, model fitting, adjustment, bootstrap validation and interpretation as well as other relevant techniques such as multiple imputation for missing data. The motivation and justification behind critical statistial decision are explained. This analysis is also made fully reproducible with all R code and text provided.

KEYWORDS

logistic regression; multiple imputation; model validation

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http://www.crema-research.ch/papers/2009-03.pdf
https://www.insider.com/titanic-secrets-facts-2018-4#
at-the-memorial-of-frederick-fleet-one-of-the-lookouts-a-prankster-left-a-pair-of-bino http://rpubs.com/edwardcooper/titanic1
https://www.kaggle.com/mrisdal/exploring-survival-on-the-titanic/
report
https://www.kaggle.com/startupsci/titanic-data-science-solutions/
comments
https://www.newscientist.com/article/dn22119-sinking-the-titanic-women-and-children-facetory.
```

1. Introduction

The sinking of RMS Titanic brought to various machine learning competitions a quintessential dataset among others, in which one major interest is to predict possibility of survival given sex, age, class, etc. There are several variants of this data existed on the web, the one I will be using is accessed on Encyclopedia Titanica, namely titanic3, courtesy of Philip Hind, with the following variables (table 1)

This data frame recorded the survival status 1309 Titanic passengers¹ alongside his/her gender, age, family relations on board, ticket fare, etc. There were 809 victims and 500 survivors in total.

Inspired by Dr. Frank Harrell's similar case study on the same topic in his *Regression Modeling Strategies* (2015) book, here I attempt to propose my own idea and interpretation of model development that is as original as possible. To ensure repro-

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¹The data does not involve the crew, and the total number of passengers is said to be 1317

Table 1. Data with 1309 passengers and 14 columns

	Variable	Definition	Note
<u>·</u>	pclass	Ticket class	1 = 1st, $2 = 2$ nd, $3 = 3$ rd
2	survival	Survival Status	0 = No, 1 = Yes
_			0 = No, 1 = Tes
3	name	Name	
4	sex	Sex	
5	age	Age	In years, some infants had fractional values
6	$_{ m sibsp}$	Number of Siblings/Spouses Aboard	
7	parch	Number of Parents/Children Aboard	
8	ticket	Ticket Number	
9	fare	Passenger Fare	in Pre-1970 British Pounds
10	cabin	Cabin	
11	embarked	Port of Embarkation	Cherbourg, Queenstown or Southampton
12	boat	Lifeboat	
13	body	Body Identification Number	
14	home.dest	Home/Destination	

ducibility, all the analysis is done in R (R Core Team 2020) and RStudio with code and text made public in this repo.

- Quantify predictive ability of each predictors, i.e. which predictor is most dominant in determining whether a passenger will survive
- Find Interactions between predictors
- Whether the Women and children first policy is respected. After the collision, The captain explicitly issued an order for women and children to be saved first.

Here is a brief summary of the following sections

• Exploration, data preprocessing based on descriptive statistics and visualization, finish with a redundancy analysis

2. Exploration

2.1. Exploratory analysis on survival patterns

Before any analysis, we'll start by some data munging. First exclude those variables that bring little insight to prediction: name, ticket, embarked, body, cabin² and home.dest. The boat column is left out for another reason, because an non-missing entry in boat basically means survival and missing means death³.

Next, for purposes of interpretation we will transform fare into today's US dollars with correction for inflation. According to discussion here, we make the transformation

 $^{^2\}mathrm{Because}$ this was primarily an identification for class and most were missing

³More precisely, there were 9 recorded passengers who got on the lifeboat yet died before reaching Carpathia, another RMS which spearheaded the rescue of Titanic survivors. There were also 13 passengers who survived with no boat information documented, and this is most likely due to data quality issues after looking up on Encyclopedia Titanica. Even with these exceptions, whether a passenger got on a lifeboat yields perfect prediction on his/her survival. If one fits a logistic regression model on survival based on whether boat is missing, the apparent accuracy will be nearly 1

$$\frac{\text{today's US dollar}}{\text{fare in 1914}} = \underbrace{5}_{\text{exchange rate then}} \times \underbrace{26}_{\text{inflation index from 1914 to 2020}}$$

There were 17 passengers whose fare is zero, all of whom males boarding in Southampton, the start of the voyage. It is suspected that some of them may be crew members, or this could be an error in data collection. I will treat these anomalies as missing entries for simplicity. Moreover, one passenger in the 3rd class had missing value in fare. Given the small amount of missingness, single imputation with median fare conditional on class is used.

Finally, a nice summary of all existing variables in the data is given by the Hmisc::describle function.

```
# print a summary for the data
titanic %>%
  mutate(survived = factor(survived)) %>%
  describe() %>%
  latex(file = "", size = "small", center = "none")
```

7 Variables 1309 Observations

```
pclass
               missing 0
      1309
Value 1st 2nd 3rd
Frequency 323 277 709
Proportion 0.247 0.212 0.542
survived
               missing
                           distinct
      ^{
m n}_{1309}
Frequency 809 500
Proportion 0.618 0.382
               missing 0
                           distinct
     1309
Frequency
Proportion
               0.356
                                                                                                       age
               missing
263
                           distinct
98
                                        Info
0.999
                                                   Mean
29.88
                                                                                                            \frac{.90}{50}
                                                              Gmd
     1046
lowest: 0.1667 0.3333 0.4167 0.6667 0.7500, highest: 70.5000 71.0000 74.0000 76.0000 80.0000
                                                                                               1 . . . . .
sibsp
               \underset{0}{\operatorname{missing}}
                                         Info
                                                  Mean
                                                             Gmd
                           distinct
      1309
lowest : 0 1 2 3 4, highest: 2 3 4 5 8
Frequency 891 319 42 20 22 6 9
Proportion 0.681 0.244 0.032 0.015 0.017 0.005 0.007
                    0
```

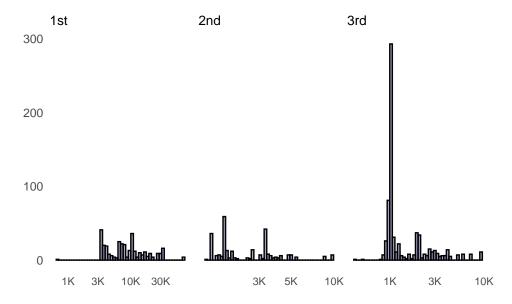
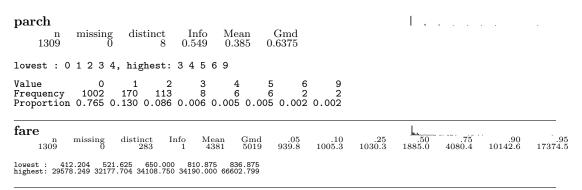


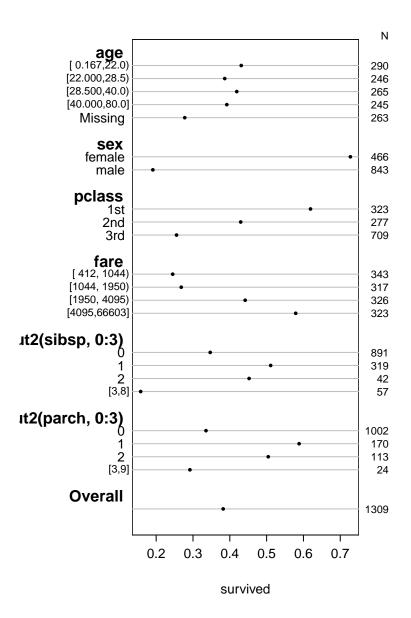
Figure 1. More than 75% of the third class passengers (700-plus in total) purchased tickets with price lower than \$2000, while the median fare for second and first class is \$3861. X axis is on log 10 scale



There are several interesting patterns to notice ⁴

- age has a nice distribution with 80% observations falling between 14 and 50. Yet it is the only variable suffering from missing values after excluding irrelevant columns.
- Both sibsp and parch
- The distribution of fare is heavily right skewed, caused by the large amount of third class passengers who make do with cheap cabins, as shown in figure 1. This may suggest a log transformation in the model.
- \bullet Approximately 20% age is missing. This calls for a necessary imputation method as we will see later, that survival can exhibit

 $^{^4}$ Though this is not very relevant to the model, it is still an surprising discovery that it wasn't until the late 19th century that the idea of women traveling alone gained ground. As a result, there were nearly twice as many males passengers as females on Titanic. In fact, only 40% female passengers have no family accompanies on the ship



Finally, redundant analysis

Redundancy Analysis

Number of NAs: 263

Frequencies of Missing Values Due to Each Variable

pclass	sex	age	<pre>cut2(sibsp, 0:3)</pre>
0	0	263	0
<pre>cut2(parch, 0:3)</pre>	fare		
0	0		

Transformation of target variables forced to be linear

Minimum category frequency required for retention of a binary or categorical variable: 40

R-squared cutoff: 0.9 Type: ordinary

 R^2 with which each variable can be predicted from all other variables:

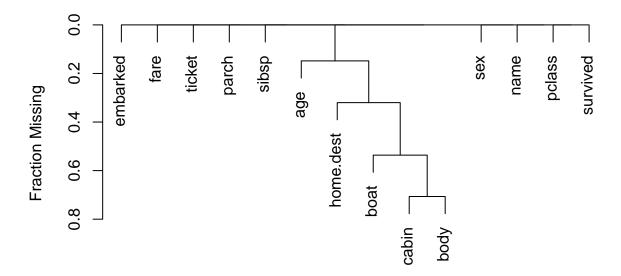
pclass	sex	age	<pre>cut2(sibsp, 0:3)</pre>
0.797	0.102	0.304	0.414
<pre>cut2(parch, 0:3)</pre>	fare		
0.439	0.451		

No redundant variables

2.2. Data missing patterns

Here we use the data before exluding irrelevant columns

plot(naclus(titanic_raw))



There are some simple workarounds

- complete-case analysis: That is, we delete all incomplete observations. Needless to say this will translate into a major harm on sample size since over 60% of boat are missing, not to mention other columns. Even if we remove boat and then delete rows with missing age we still lose over 1/5 of data. Moreover, figures in 2.1 have shed light on the relatively strong influence of age on survival. Also, the deletion of incomplete observations assumes date are missing completely at random (MCAR). When it's not the case, this could severly bias estimates of coefficients (Van Buuren 2018)
- single imputation:
- multiple imputation

For demonstration purposes I will fit two decision trees to predict

3. Modeling

3.1. Initial model

First and foremost,

3.2. Multiple imputatiin

3.3. Validation

In the award-winning solution to this legendary dataset presented by IBM Watson, they used a holdout sample to validate their model. https://www.fharrell.com/post/split-val/

3.4. The final model

4. Discussion

A more detailed explanation of some of these measures is presented in the appendix.

5. Conclusion

Appendix A. Assessment of binary logistic model

This will be Appendix A.

References

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