

Methods for Distance Calculation

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Manhattan Distance

2

Euclidean Distance

3

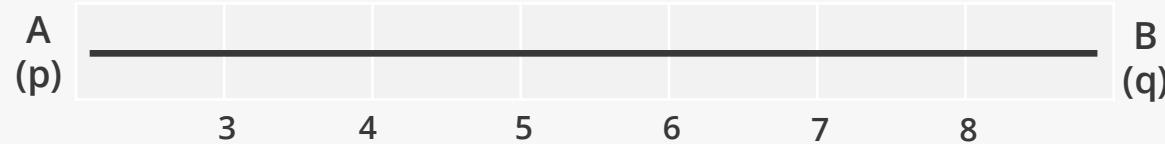
Hamming Distance



Manhattan Distance

$$d = |p_1 - q_1| + |p_2 - q_2| + \dots + |p_n - q_n|$$

Manhattan Distance



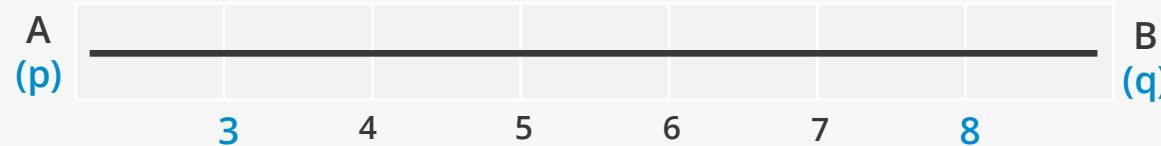
Manhattan Distance



Manhattan Distance

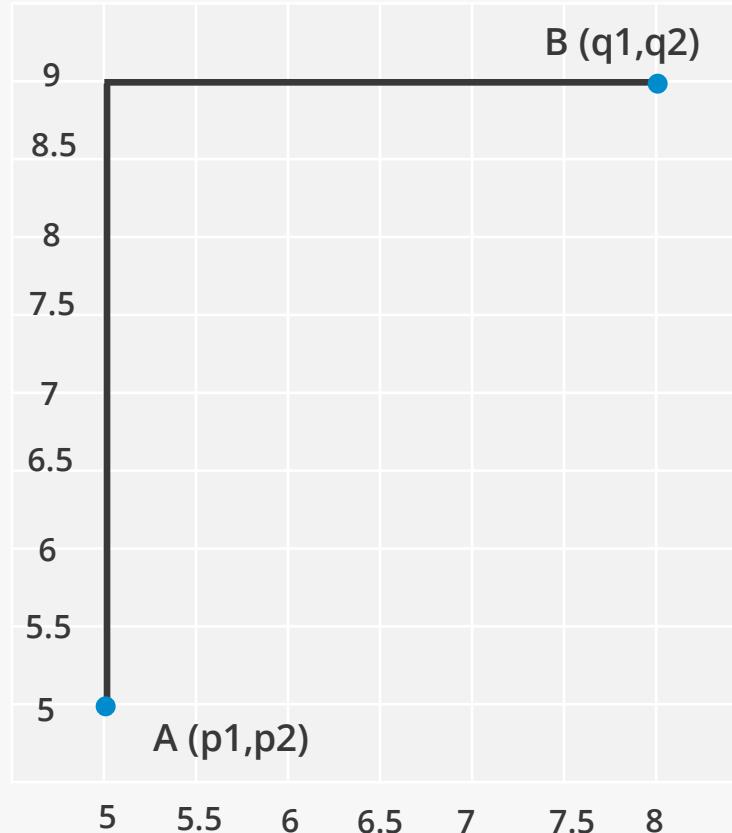


Manhattan Distance

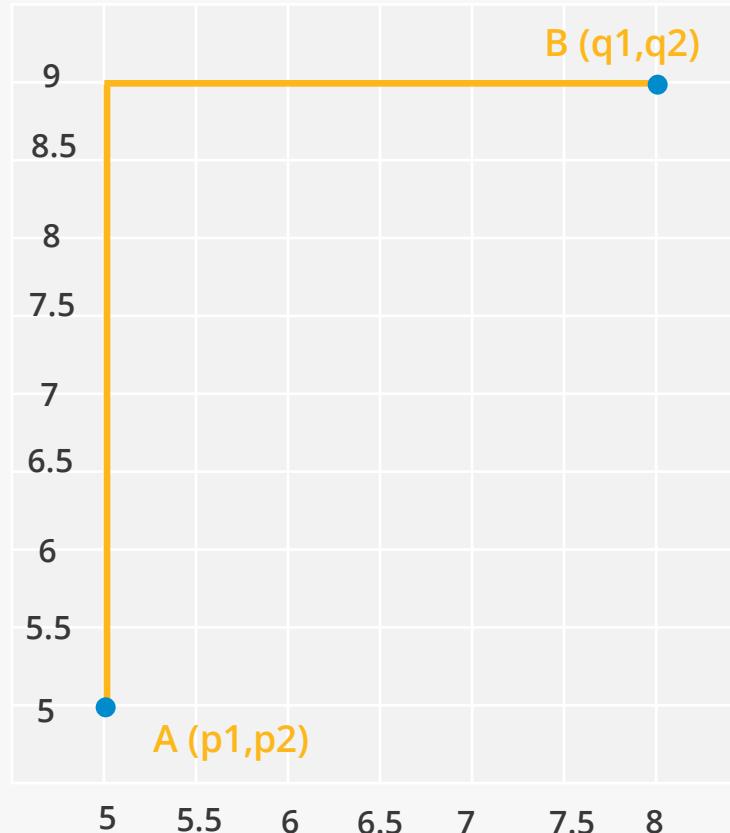


$$\begin{aligned}\text{Distance} &= |p - q| \\ &= |3 - 8| = \text{5 units}\end{aligned}$$

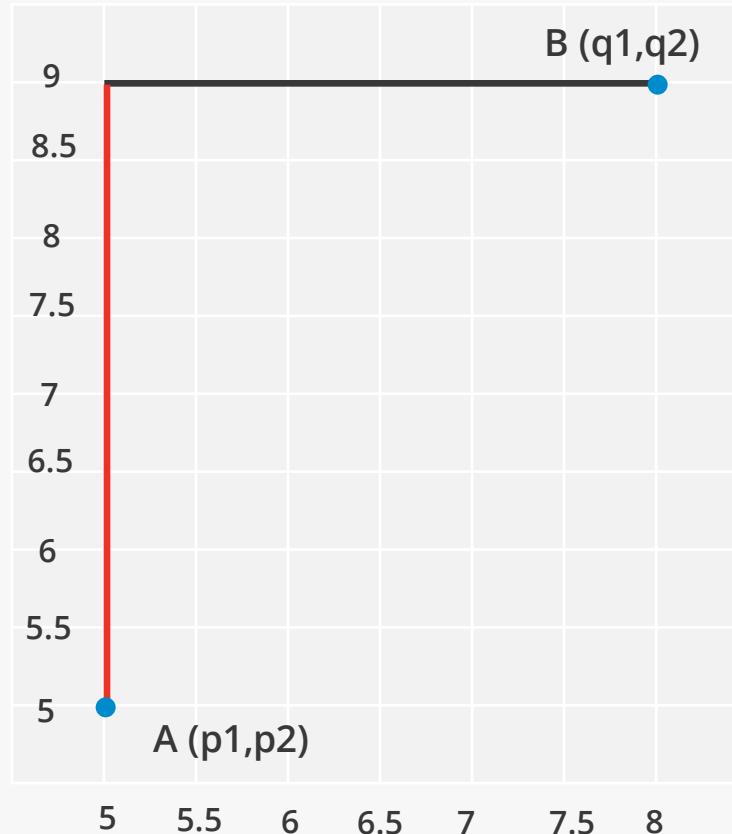
Manhattan Distance



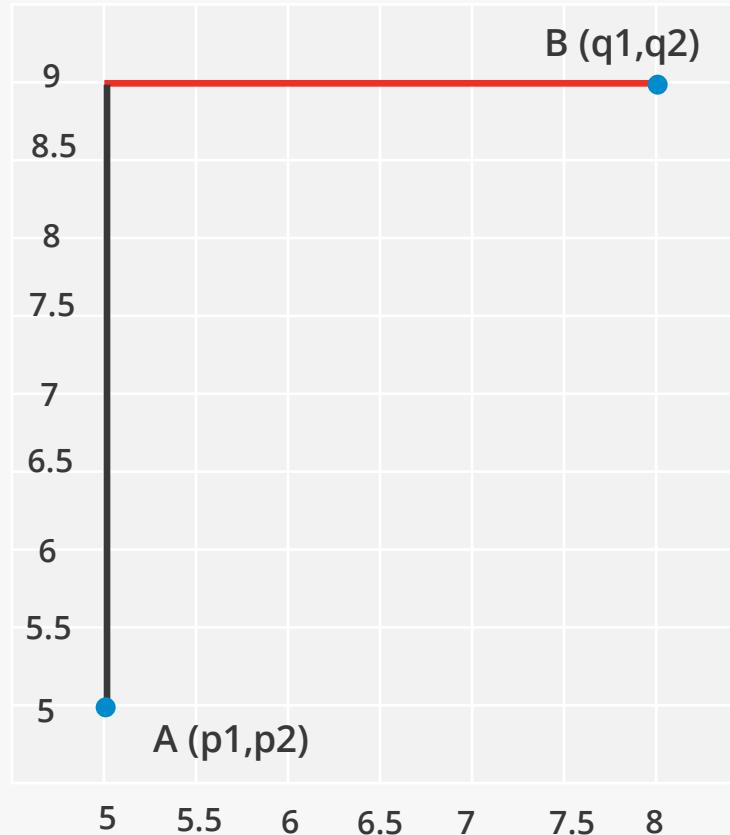
Manhattan Distance



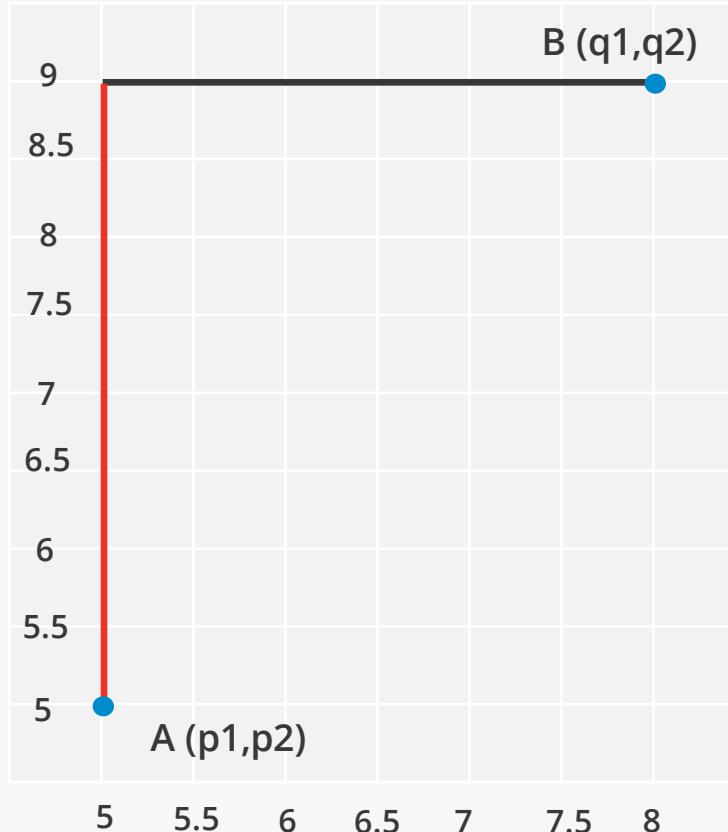
Manhattan Distance



Manhattan Distance

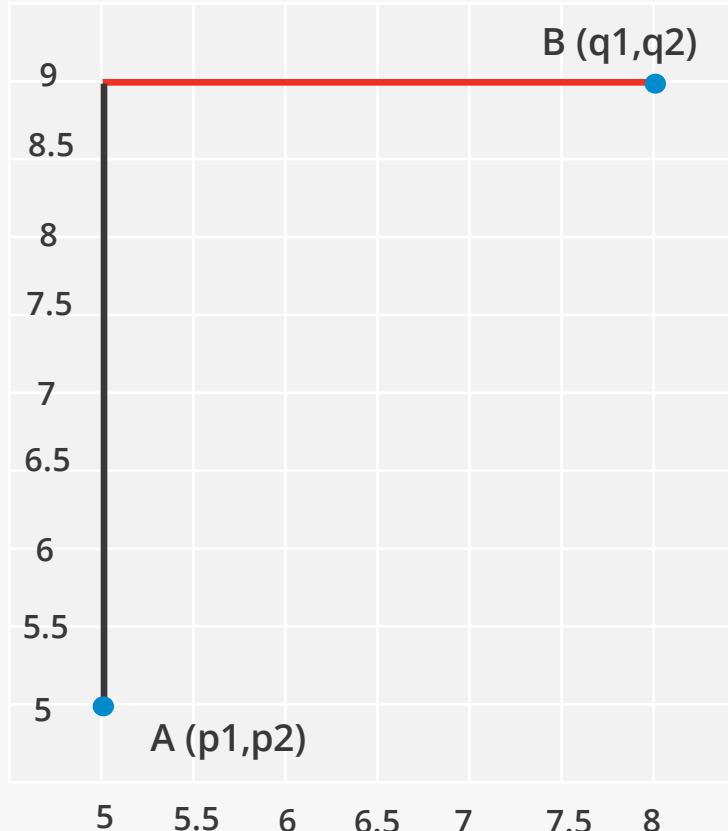


Manhattan Distance



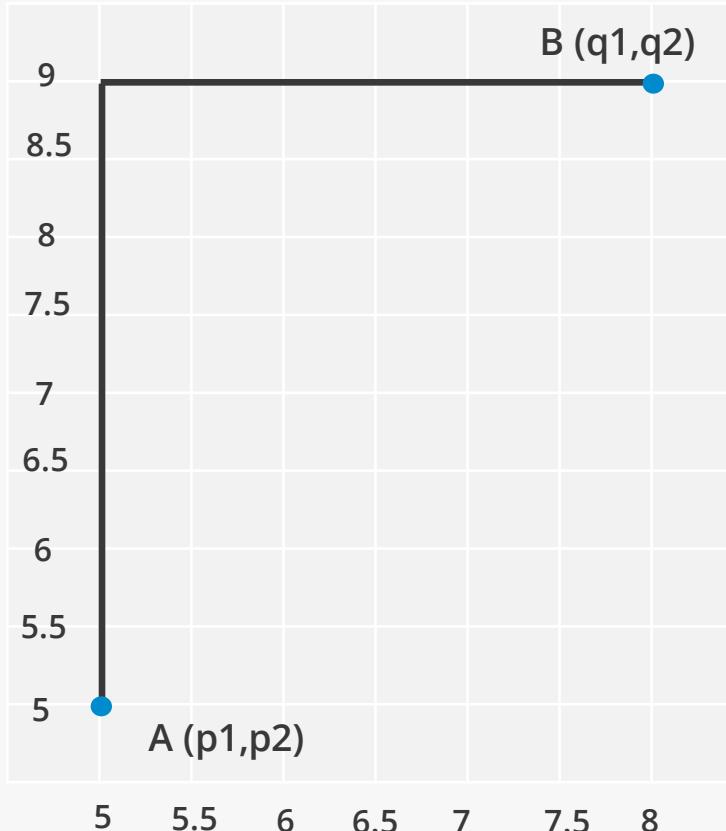
Distance = $|p_1 - q_1| +$

Manhattan Distance



$$\text{Distance} = |p_1 - q_1| + |p_2 - q_2| \\ =$$

Manhattan Distance



$$\begin{aligned}\text{Distance} &= |p_1 - q_1| + |p_2 - q_2| \\ &= |5 - 8| + |5 - 9| \\ &= 3 + 4 = \mathbf{7 \text{ Units}}\end{aligned}$$

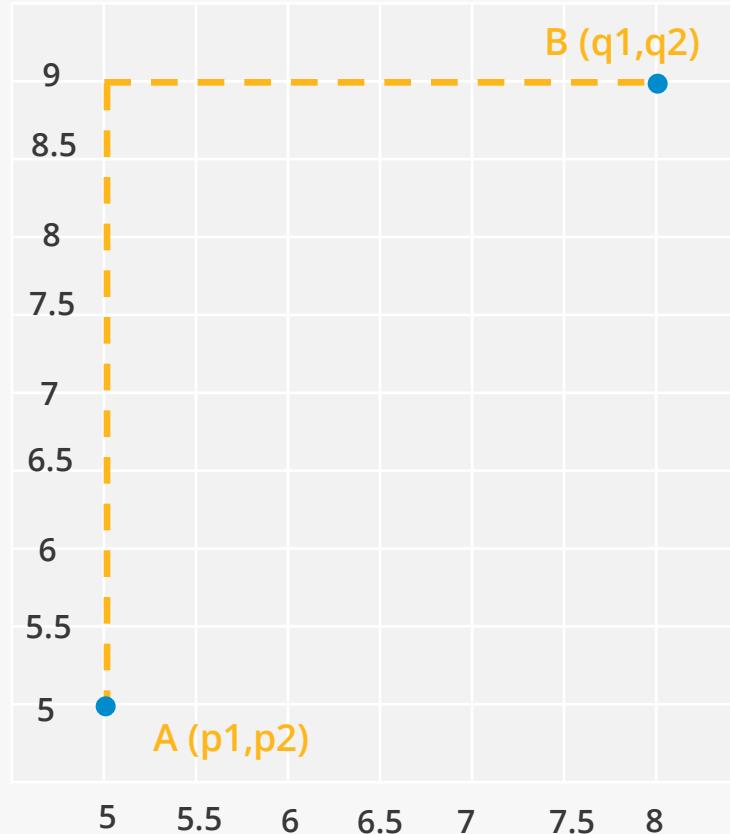
Manhattan Distance

Distance for n dimensions:

$$d = |p_1 - q_1| + |p_2 - q_2| + \dots + |p_n - q_n|$$



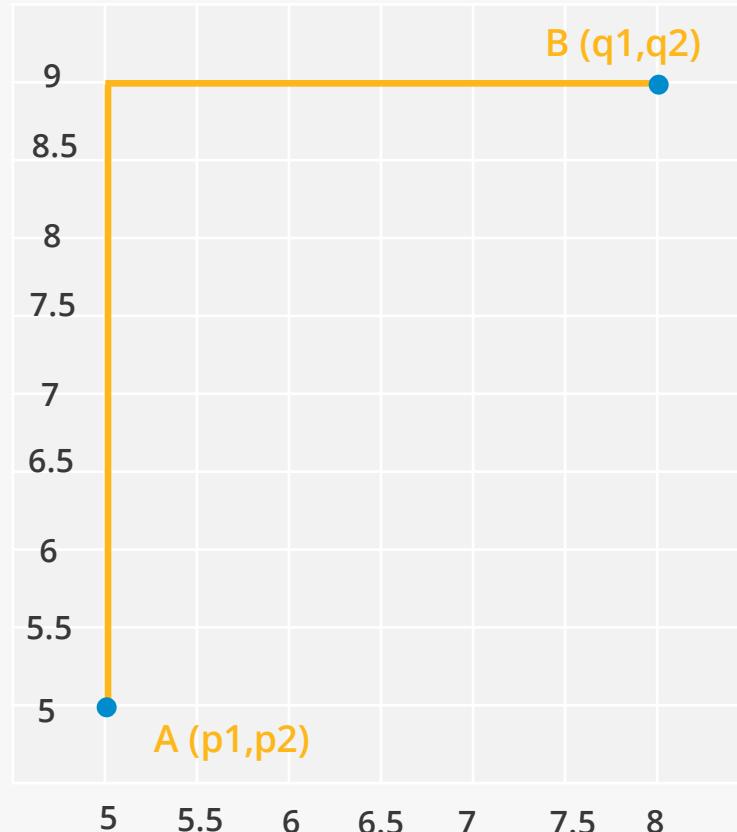
Manhattan Distance





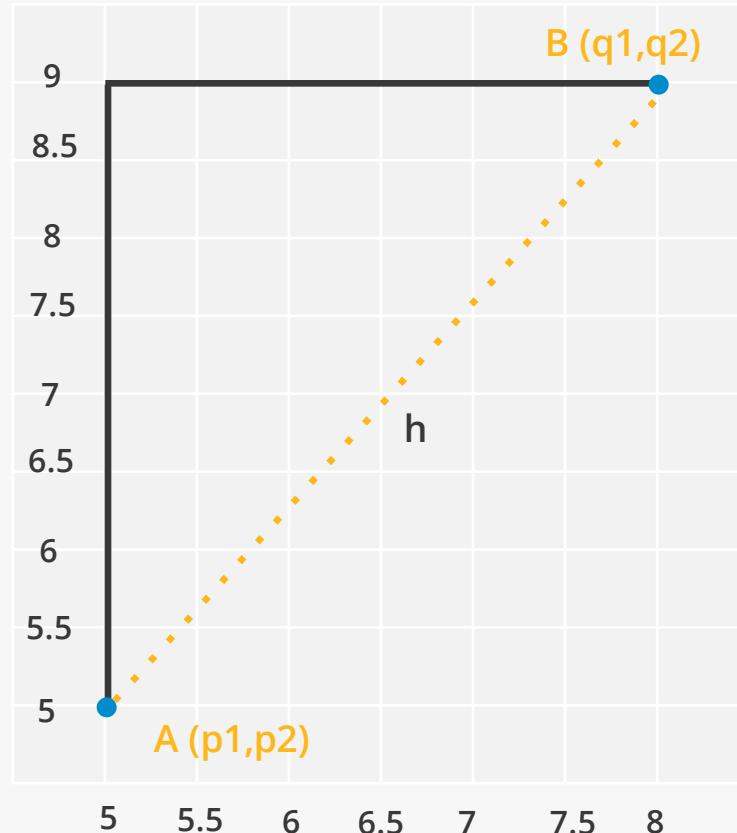
Euclidean Distance

Euclidean Distance



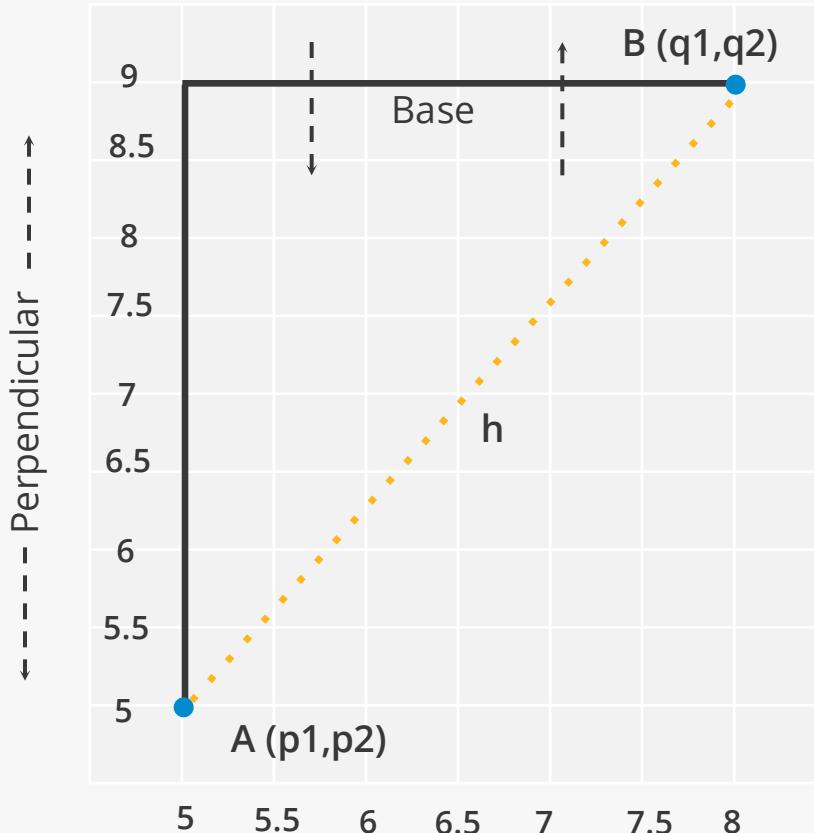
Distance between A and B
= **7 Units**

Euclidean Distance



Distance between A and B
= **7 Units**

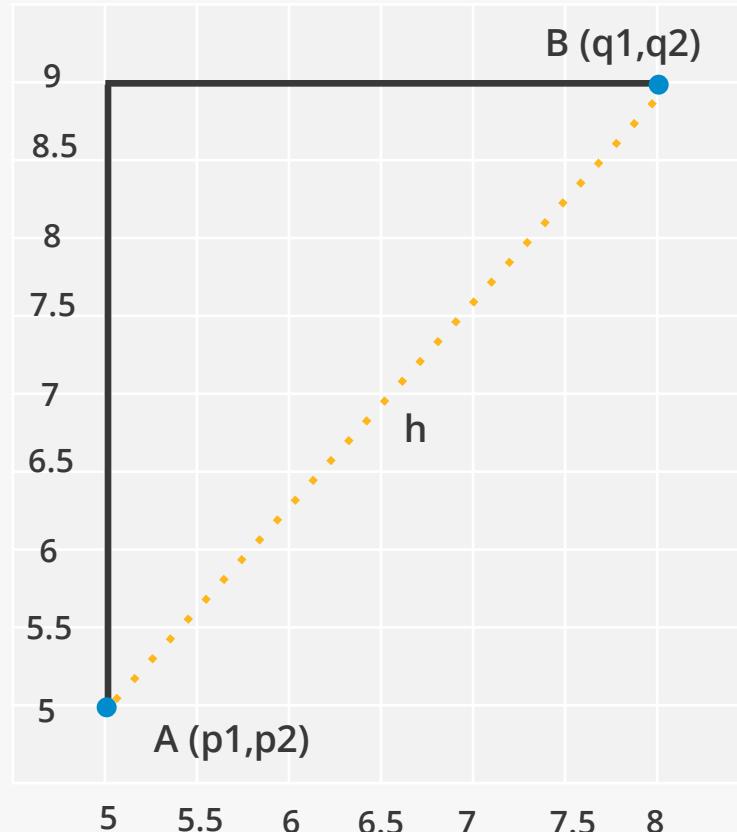
Euclidean Distance



Pythagoras Theorem

$$\sqrt{\text{base}^2 + \text{perpendicular}^2} = c$$

Euclidean Distance



$$\sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2}$$

$$= \sqrt{(5 - 9)^2 + (5 - 8)^2}$$

$$= \sqrt{4^2 + 3^2}$$

= **5 Units**

Euclidean Distance

Shortest distance between 2 points for n dimensions:

$$d = \sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2 + \dots + (p_n - q_n)^2}$$



Euclidean Distance

Shortest distance between 2 points for n dimensions:

$$\left[\sum_{i=1}^n (p_i - q_i)^2 \right]^{1/2}$$





Distance between 2 categorical variables



Hamming Distance

Hamming Distance

The Hamming Distance is the total number of differences between two strings of identical length. **Identical length** implies that the number of characters in both strings should be the same.



Hamming Distance: Example

ID	Gender	Strings
A	Male	'0'
B	Female	'1'
C	Male	'0'

Hamming Distance: Example

ID	Gender	Strings	
A	Male	'0'	
B	Female	'1'	1
C	Male	'0'	

Hamming Distance: Example

ID	Gender	Strings	
A	Male	'0'	
B	Female	'1'	
C	Male	'0'	



Hamming Distance: Example

ID	Gender	Strings	
A	Male	'0'	
B	Female	'1'	
C	Male	'0'	

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status
A	Male	Married	Self Employed
B	Female	Married	Salaried
C	Male	Unmarried	Unemployed

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status
A	'0'	'0'	'1'
B	'1'	'0'	'2'
C	'0'	'1'	'3'

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings
A	'0'	'0'	'1'	'001'
B	'1'	'0'	'2'	'102'
C	'0'	'1'	'3'	'013'

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings
A	'0'	'0'	'1'	'01'
B	'1'	'0'	'2'	'102'
C	'0'	'1'	'3'	'013'

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings
A	'0'	'0'	'1'	'0 0 1'
B	'1'	'0'	'2'	'1 0 2'
C	'0'	'1'	'3'	'01 3 '

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings
A	'0'	'0'	'1'	'00 1 '
B	'1'	'0'	'2'	'10 2 '
C	'0'	'1'	'3'	'01 3 '

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings	
A	'0'	'0'	'1'	'001'	---
B	'1'	'0'	'2'	'102'	---
C	'0'	'1'	'3'	'013'	2

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings	
A	'0'	'0'	'1'	'001'	---
B	'1'	'0'	'2'	'102'	---
C	'0'	'1'	'3'	'013'	2

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings	
A	'0'	'0'	'1'	'0 0 1'	---
B	'1'	'0'	'2'	'10 2 '	---
C	'0'	'1'	'3'	'0 1 3'	

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings	
A	'0'	'0'	'1'	'00 1 '	---
B	'1'	'0'	'2'	'102'	---
C	'0'	'1'	'3'	'01 3 '	2

Hamming Distance: Example

ID	Gender	Marital Status	Employment Status	Strings	
A	'0'	'0'	'1'	'001'	2
B	'1'	'0'	'2'	'102'	2
C	'0'	'1'	'3'	'013'	