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CIS 17A Problem #6 Scratch Work

given A.) 3.75 B.) 0.7 C.) 89.9

#1 Convert to binary, octal, and hex

A.) $3.75_{10} \rightarrow \underline{3} . \underline{C}_{16}$ hex

$$\begin{array}{r} 16 \overline{) 3.75} \\ \underline{32} \\ 50 \\ \underline{48} \\ 20 \\ \underline{16} \\ 4 \end{array} \quad \begin{array}{l} \vdots \\ \vdots \\ \vdots \end{array} \quad \begin{array}{l} 0.75 \times 16 = 12 \\ \vdots \end{array}$$

$3.C_{16} \rightarrow \underline{11} . \underline{1100}_2$ binary

$11.1100_2 \rightarrow \underline{3} . \underline{6}_8$ octal

B.) $0.7_{10} \rightarrow \underline{0} . \underline{B\bar{3}}_{16}$ hex

$0.7_{10} \times 16 = 11.2 \Rightarrow B_{16}$

$0.2_{10} \times 16 = 3.2 \Rightarrow 3_{16}$

$0.2_{10} \times 16 = 3.2 \Rightarrow 3_{16}$

$0.B\bar{3}_{16} \rightarrow \underline{0} . \underline{10110011}_2$ binary

$0.101100110011001100110011_2 \rightarrow 0.54631_8$ octal

C.) $89.9_{10} \rightarrow \underline{59} . \underline{E6}_{16}$ hex

$$\begin{array}{r} 16 \overline{) 89.9} \\ \underline{80} \\ 90 \\ \underline{80} \\ 100 \\ \underline{96} \\ 40 \\ \underline{32} \\ 8 \end{array}$$

$0.9_{10} \times 16 = 14.4 \Rightarrow E_{16}$

$0.4_{10} \times 16 = 6.4 \Rightarrow 6_{16}$

$0.4_{10} \times 16 = 6.4 \Rightarrow 6_{16}$

$59.E6_{16} \rightarrow \underline{1011001} . \underline{11101110}_2$ binary

$1011001.111011100110011001100110_2 \rightarrow 131.714631463_8$

$\Rightarrow 131.71463_8$ octal

#2. Convert to NASA Hex Float w/ first 24 bits representing the signed fraction and the last bits representing the signed exponent.

scaled as $0. \text{Fraction} \times 2^{\text{Exponent}}$

A.) 3.75_{10}

$$\rightarrow 11.1100_2 \times 2^0$$

$$0.111100_2 \times 2^2$$

$$0.11110000|00000000|00000000|00000010$$

$$= 78000002$$

B.) 0.7_{10}

$$\rightarrow 0.10110011_2 \times 2^0$$

$$0.10110011|10011001|10011001|00000000$$

$$= 5999900$$

C.) 89.9_{10}

$$\rightarrow 1011001.11100110_2 \times 2^0$$

$$0.101100111100110_2 \times 2^7$$

$$0.10110011|11100110|01100110|00000111$$

$$= 59E66607$$

#5) Convert to IEEE 754 format

A) $3.75_{10} \rightarrow 0.1111_2 \times 2^2$

$\rightarrow \overset{\text{ignore}}{1}.1111_2 \times 2^1$

power = $1 + 127 = 128$

$\frac{0}{\uparrow \text{sign}} (100 | 0000 | 0) 1110000 | 00000000 | 00000000$

$\Rightarrow 40700000$

B) $0.7_{10} \rightarrow 0.10110011_2 \times 2^0$
 $\rightarrow \cancel{1}.0110011_2 \times 2^{-1}$

power = $-1 + 127 = 126$

$\frac{0}{\uparrow \text{sign}} (011 | 1101 | 0) 0110011 | 00110011 | 00110011$

$\Rightarrow 3F333333$

C) $89.9_{10} \rightarrow 1011001.11100110_2 \times 2^6$
 $\rightarrow \cancel{1}.01100111100110_2 \times 2^6$

power = $6 + 127 = 133$

$\frac{0}{\uparrow \text{sign}} (100 | 0010 | 1) 0110011 | 11001100 | 11001101$

$\Rightarrow 42B3CCCC$

11001
roundup