

Solve in integers: $3x + 5y + 7z = 11$.

$$(3, 5, 7) \mid 11$$

$$1 \mid 11$$

$$z = \frac{11 - 3x - 5y}{7}$$

$$11 - 3x - 5y \equiv 0 \pmod{7}$$

$$3x + 5y \equiv 4 \pmod{7}$$

$$3x + 5y \equiv 4 + 7w \quad (w \in \mathbb{Z})$$

$$y = \frac{4 + 7w - 3x}{5}$$

$$4 + 7w - 3x \equiv 0 \pmod{5}$$

$$3x \equiv 4 + 2w \pmod{5}$$

$$3x \equiv 9 + 12w \pmod{5}$$

$$\therefore x_n = 3 + 4w$$

$$y = \frac{4 + 7w - 9 - 12w}{5}$$

$$= -1 - w$$

$$f_n = -1 - w$$

$$z = \frac{11 - 9 - 12w + 5 + 5w}{7}$$

$$= 1 - w$$

$$\boxed{(3 + 4n, -1 - n, 1 - n)}$$

$$\begin{aligned} 9 - 5 + 7 &= 11 \\ 2(-10) + 10 &= 11 \end{aligned}$$