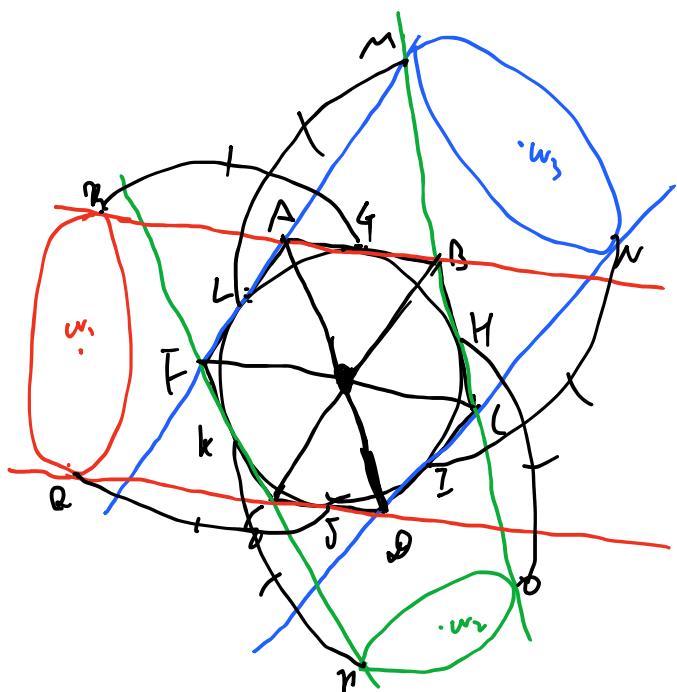


## Branchon's Theorem

The diagonals of a hexagon (6 points) that inscribes a circle concur.  
Proof



$W1W3$ ,  $GR = LM$

$AL = AG$

$\therefore RA = RM \Leftrightarrow A \in \text{rad}(W1, W3)$

$JD = DI$

$\therefore QD = DW \Leftrightarrow D \in \text{rad}(W1, W3)$

$\therefore AD = \text{rad}(W1, W3)$

$$\text{rad}(W1, W2) = EB$$

$$\text{rad}(W2, W3) = FL$$

$$\text{rad}(W3, W1) = AD$$

By Monge's Theorem,  
 $EB$ ,  $FL$ , and  $AD$  concur.