

Branchon's Theorem

The diagonals of a hexagon (6 points) that inscribes a circle concur.
 1st proof

$$W_1W_2, GR = LM$$

$$AL = AG$$

$$\therefore RA = RM \Leftrightarrow A \in \text{rad}(W_1, W_3)$$

$$JD = DI$$

$$\therefore QD = DW \Leftrightarrow D \in \text{rad}(W_1, W_3)$$

$$\therefore AD = \text{rad}(W_1, W_3)$$

$$\begin{aligned} \text{rad}(W_1, W_2) &= EB \\ \text{rad}(W_2, W_3) &= FL \\ \text{rad}(W_3, W_1) &= AD \end{aligned}$$

By Monge's Theorem,
 EB, FL , and AD concur.

