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€\ ($\epsilon \big| \bi
   Aquamacs File Edit Options Tools QuickCheck Erlang Window
                                                    simonthompson — xterm — beam.smp
% erl
Erlang/OTP 17 [erts-6.3] [source-f9282c6] [64-bit] [smp:8:8] [a
sync-threads:10] [hipe] [kernel-poll:false]
                                                                                                                                                                                       "scratch"
Eshell V6.3 (abort with ^G)
1> c(interactive).
                                                                                                                                                                         % interactively play against a strategy, provided as argument.
{ok,interactive}
2> [scissors,paper,rock].
[scissors,paper,rock]
                                                                                                                                                                         play(Strategy) ->
3> interactive:play(fun(Plays) -> rock end).
                                                                                                                                                                                   io:format("Rock - paper - scissors~n"),
Rock - paper - scissors
                                                                                                                                                                                   io:format("Play one of rock, paper, scissors, ...~n"),
Play one of rock, paper, scissors, ...
                                                                                                                                                                                   io:format("...r, p, s, stop, followed by '.'~n"),
... r, p, s, stop, followed by '.'
                                                                                                                                                                                   play(Strategy,[]).
Play: r.
Result: draw
                                                                                                                                                                         % tail recursive loop for play/1
Play: p.
Result: win
                                                                                                                                                                         play(Strategy, Moves) ->
Play: s.
                                                                                                                                                                                   {ok,P} = io:read("Play: "),
Result: lose
                                                                                                                                                                                   Play = expand(P),
Play: p.
                                                                                                                                                                                   case Play of
Result: win
Play: .
                                                                                                                                                                                              stop ->
                                                                                                                                                                                                         io:format("Stopped~n");
** exception error: no match of right hand side value
                                                    {error, {1,erl_parse,
                                                                          ["syntax error before: ","'.'"]}}
                                                                                                                                                                                                         Result = result(Play, Strategy(Moves)),
            in function interactive:play/2 (interactive.erl, line 16)
                                                                                                                                                                                                         io:format("Result: ~p~n", [Result]),
                                                                                                                                                                                                        play(Strategy, [Play | Moves])
4>
                                                                                                                                                                                   end.
                                                                                                                                                                         % auxiliary functions
                                                                                                                                                                          -: **- interactive.erl 33% (61,0) [(Erlang EXT Flymake)]
```

```
€ (a) 88% (a) 13:34
 Aquamacs File Edit Options Tools QuickCheck Erlang Window
                    simonthompson — xterm — beam.smp
Rock - paper - scissors
Play one of rock, paper, scissors, ...
... r, p, s, stop, followed by '.'
                                                                         "scratch"
Play: r.
Result: draw
Play: p.
                                                                   % interactively play against a strategy, provided as argument.
Result: win
Play: s.
Result: lose
                                                                   play(Strategy) ->
Play: p.
                                                                        io:format("Rock - paper - scissors~n"),
Result: win
                                                                       io:format("Play one of rock, paper, scissors, ...~n"),
Play: .
                                                                       io:format("...r, p, s, stop, followed by '.'~n"),
** exception error: no match of right hand side value
                                                                       play(Strategy,[]).
                     {error, {1,erl parse,
                             ["syntax error before: ","'.'"]}}
                                                                   % tail recursive loop for play/1
     in function interactive:play/2 (interactive.erl, line 16)
                                                                   play(Strategy, Moves) ->
4> interactive:play(fun(Plays) -> rock end).
                                                                       {ok,P} = io:read("Play: "),
Rock - paper - scissors
                                                                       Play = expand(P),
Play one of rock, paper, scissors, ...
                                                                       case Play of
... r, p, s, stop, followed by '.'
                                                                            stop ->
Play: p.
                                                                                io:format("Stopped~n");
Result: win
Play: p.
Result: win
                                                                                Result = result(Play, Strategy(Moves)),
Play: p.
                                                                                io:format("Result: ~p~n", [Result]),
Result: win
                                                                               play(Strategy, [Play | Moves])
Play: p.
                                                                       end.
Result: win
Play: p.
Result: win
                                                                   % auxiliary functions
Play: stop.
Stopped
ok
                                                                    -: **- interactive.erl 33% (54,25) [(Erlang EXT Flymake)]
5> interactive:play(fun interactive:echo/
```

Functions as results





```
Functions as arguments ...
```

```
... e.g. map, filter, zipwith, foldr ...
```





Writing down functions in Erlang

Find the area of all ... using area

```
all_areas(Xs) -> lists:map(fun area/1,Xs).
```

If area is in the module shape

```
all areas(Xs) -> lists:map(fun shape:area/1,Xs).
```

In the shell, with the variable Area bound to the area function

```
... > lists:map(Area, Xs).
```

As well as being able to use fun expressions directly.





"Partially applied" functions

The + operator applies to two numbers, to give a number.

What if we "applied it to a single argument" ...

```
add(X) -> fun(Y) -> X+Y end.
```

 \dots we get a *function*, that adds \mathbf{x} to its argument.

```
addOneToAll(Xs) ->
   lists:map(add(1),Xs).

addToAll(N,Xs) ->
   lists:map(add(N),Xs).
```





Composing functions

We often use function composition to define functions ...

... first do this (F) and then do this (G).

compose
$$(F,G) \rightarrow$$

fun $(X) \rightarrow G(F(X))$ end.

The result of compose is a function, that "composes" its arguments.





```
Functions as arguments ...
... e.g. map, filter, zipwith, foldr ...
Functions as results ...
... e.g. "curried" functions

Functions as arguments and results ...
... e.g. compose, iterate, etc.
```





Rock-paper-scissors and HoFs





```
Functions as arguments ...
... e.g. map, filter, zipwith, foldr ...
Functions as results ...
... e.g. "curried" functions

Functions as arguments and results ...
... e.g. compose, iterate, etc.
```





Strategy vs Strategy

```
play_two(StrategyL,StrategyR,N) ->
    play_two(StrategyL,StrategyR,[],[],N).
play_two(_,_,PlaysL,PlaysR,0) ->
    io:format("Overall result ... ");
play_two(StrategyL,StrategyR,PlaysL,PlaysR,N) ->
    PlayL = StrategyL(PlaysR),
    PlayR = StrategyR(PlaysL),
    Result = result(PlayL, PlayR),
    io:format("Result: ~p~n", [Result]),
    play_two(StrategyL,StrategyR,[PlayL|PlaysL],[PlayR|PlaysR],N-1).
```





Strategy vs Strategy

```
play_two(StrategyL,StrategyR,N) ->
    play_two(StrategyL,StrategyR,[],[],N).
play_two(_,_,PlaysL,PlaysR,0) ->
    io:format("Overall result ... ");
play_two(StrategyL,StrategyR,PlaysL,PlaysR,N) ->
    PlayL = StrategyL(PlaysR),
    PlayR = StrategyR(PlaysL),
    Result = result(PlayL, PlayR),
    io:format("Result: ~p~n", [Result]),
    play_two(StrategyL,StrategyR,[PlayL|PlaysL],[PlayR|PlaysR],N-1).
```





Iteration

Apply the function F, N times

```
iterate(0) ->
    fun(_F) ->
    fun id/1 end;

iterate(N) ->
    fun(F) ->
    compose(F, (iterate(N-1))(F)) end.
```

How would you define it using lists:map, lists:foldr and compose?





```
Functions as arguments ...
... e.g. map, filter, zipwith, foldr ...
Functions as results ...
... e.g. "curried" functions

Functions as arguments and results ...
... e.g. compose, iterate, etc.
```

