

Functional patterns



Lists

Every list is either empty `[]` ... or non-empty.

In the non-empty case it matches the pattern `[X|Xs]`,

... `X` matches the first element, and

... `Xs` matches the rest of the list.



Lists

Take the example of `[2,3,4,5] ...`

It matches the pattern `[X|Xs] ...`

... `X` matches the first element, `2`, and

... `Xs` matches the rest of the list, `[3,4,5]`.



Template for recursion over lists

To define a function `foo` by recursion over lists, try this template ...

```
foo([])      -> ... ;  
foo([X|Xs]) -> ... foo(Xs) ...
```



Sum a list of numbers

Give the sum of the elements in a list of numbers.

```
sum([])      -> 0 ;  
sum([X|Xs]) -> X + sum(Xs) .
```



Find the area of all shapes in a list

Find the area of each shape in a list of shapes.

```
all_areas([])      -> [] ;  
all_areas([X|Xs]) -> [ area(X) | all_areas(Xs) ] .
```



Find the circles in a list of shapes

Extract the circles from a list of shapes.

```
circles([])      -> [] ;
```

```
circles( [{circle,{X,Y},R} | Xs] ) ->  
  [ {circle,{X,Y},R} | circles(Xs) ] ;
```

```
circles( [{rectangle,{_,_},_,_} | Xs] ) ->  
  circles(Xs) .
```



Patterns ...

Combine all the elements of a list into one ...

... e.g. using **+** to give the sum of list.

Transform all the elements of a list ...

... e.g. using **area** to give the area of each of the shapes.

Select the elements of a list with a particular property ...

... e.g. select the circles from a list of the shapes.



Patterns ...

Reduce (or **fold**) all the elements of a list into one ...

... e.g. using **+** to give the sum of list.

Map all the elements of a list ...

... e.g. using **area** to give the area of each of the shapes.

Filter all the elements of a list with a particular property ...

... e.g. select the circles from a list of the shapes.



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From specific to generic



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Transform all the elements of a list ...

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... e.g. select the circles from a list of the shapes.



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... e.g. using **area** to give the area of each of the shapes.

Filter all the elements of a list with a particular property ...

... e.g. select the circles from a list of the shapes.



Apply **F** to every element of a list

Find the area of all ... the only specific thing is applying **area**

```
all_areas([])      -> [] ;  
all_areas([X|Xs]) -> [ area(X) | all_areas(Xs) ] .
```



Apply **F** to every element of a list

Find the area of all ... the only specific thing is applying **area**

```
all_areas([])      -> [] ;  
all_areas([X|Xs]) -> [ area(X) | all_areas(Xs) ] .
```

Apply **F** instead of **area** ... and add **F** as an argument:

```
map(F, [])      -> [] ;  
map(F, [X|Xs]) -> [ F(X) | map(F, Xs) ] .
```

Here's the final definition:

```
all_areas(Shapes) -> map(fun area/1, Shapes) .
```



Patterns ... why?

Map all the elements of a list ...

... e.g. using **area** to give the area of each of the shapes.

We get **reuse** ... define **map** once and reuse forever.

We get **comprehensibility** ... when we see **map** we know what's going on – no need to understand a recursive definition.



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Find the circles in a list of shapes

Extract the circles from a list of shapes.

```
circles([])      -> [] ;
```

```
circles( [{circle,{X,Y},R} | Xs] ) ->  
  [ {circle,{X,Y},R} | circles(Xs) ] ;
```

```
circles( [{rectangle,{_,_},_,_} | Xs] ) ->  
  circles(Xs) .
```



Find the circles in a list of shapes

What is specific here is the **test** of whether to add or not ...
... which is done here by **pattern matching**.

```
circles([])      -> [] ;
```

```
circles( [{circle,{X,Y},R} | Xs] ) ->  
  [ {circle,{X,Y},R} | circles(Xs) ] ;
```

```
circles( [{rectangle,{_,_},_,_} | Xs] ) ->  
  circles(Xs) .
```



Filter all the elements with property P

Include X in the list if it has the property P ... i.e. $P(X)$ is **true**.

```
filter(P, []) -> [];  
  
filter(P, [X|Xs]) ->  
  case P(X) of  
    true  -> [X|filter(P,Xs)];  
    false -> filter(P,Xs)  
  end.
```



Is this a circle?

We used **pattern matching** in our original definition ...

```
circles([])      -> [] ;
```

```
circles( [{circle,{X,Y},R} | Xs] ) ->  
  [ {circle,{X,Y},R} | circles(Xs) ];
```

```
circles( [{rectangle,{_,_},_,_} | Xs] ) ->  
  circles(Xs) .
```

... "factor this out" as a test like this:

```
is_circle( {circle,{_,_},_} ) ->  
  true;
```

```
is_circle( {rectangle,{_,_},_,_} ) ->  
  false.
```



Find the circles in a list of shapes

So finally we can define `circles` using `filter` ...

```
circles(Shapes) ->  
  filter(fun is_circle/1, Shapes) .
```

... using this property (= function that returns a boolean):

```
is_circle( {circle,{_,_},R} ) ->  
  true;
```

```
is_circle( {rectangle,{_,_},_,_} ) ->  
  false.
```



The sum of a list of numbers

What's specific in the definition of `sum`?

```
sum([])      -> 0;  
sum([X|Xs]) -> X + sum(Xs)
```

... the **starting value** of **0**, and
... the combining function **+**.

```
reduce(Combine, Start, []) ->  
    Start;  
reduce(Combine, Start, [X|Xs]) ->  
    Combine(X, reduce(Combine, Start, Xs)).
```

```
sum(Xs) -> reduce(fun plus/2, 0, Xs).
```

```
plus(X,Y) -> X+Y.
```



The sum of a list of numbers

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sum([])      -> 0;  
sum([X|Xs]) -> X + sum(Xs)
```

... the **starting value** of **0**, and
... the combining function **+**.

```
reduce(Combine, Start, []) ->  
    Start;  
reduce(Combine, Start, [X|Xs]) ->  
    Combine(X, reduce(Combine, Start, Xs)).  
  
sum(Xs) -> reduce(fun (X,Y) -> X+Y end,  
                  0, Xs).
```



Using these higher-order functions

Process a collection of web pages ... using **map**.

For each word on the page generate value ... using **map** again.

Select all values for a particular word ... using **filter** (or **map**).

Combine that set of values to a single value ... using **reduce**.

Available in a map-reduce framework like Hadoop.



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Terminal Shell Edit View Window Help
simonthompson — xterm — beam.smp

```
% erl
Erlang/OTP 17 [erts-6.3] [source-f9282c6] [64-bit] [smp:8:8] [a
sync-threads:10] [hipe] [kernel-poll:false]

Eshell V6.3 (abort with ^G)
1> c(z).
{ok,z}
2> zip_with(fun (X,Y) -> max(X,Y) end, [1,3,2,4], [0,5,4,3]).
** exception error: undefined shell command zip_with/3
3> z:zip_with(fun (X,Y) -> max(X,Y) end, [1,3,2,4], [0,5,4,3]).

[1,5,4,4]
4> z:zip_with(fun max/2, [1,3,2,4], [0,5,4,3]).
** exception error: undefined function erl_eval:max/2
5> z:zip_with(fun erlang:max/2, [1,3,2,4], [0,5,4,3]).
[1,5,4,4]
6> z:zip_with(fun (X,Y) -> {\X,Y} end, [1,3,2,4], [0,5,4,3]).
* 1: syntax error before: '\\'
6> z:zip_with(fun (X,Y) -> {X,Y} end, [1,3,2,4], [0,5,4,3]).
[{1,0},{3,5},{2,4},{4,3}]
7>
```

z.erl

```
-module(z).
-export([zip_with/3]).

zip_with(_F,_,[]) ->
    [];
zip_with(_F,[],_) ->
    [];
zip_with(F,[X|Xs],[Y|Ys]) ->
    [ F(X,Y) | zip_with(F,Xs,Ys) ].
```

U:---- z.erl All (2,19) (Erlang EXT Flymake)



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