COMPUTATIONAL FLUID DYNAMICS SIMULATIONS OF OVERFLOW PATTERNS IN UTILITY-CHAMBER AND HYDRODYNAMIC STRESSES IN VEGETATION ZONE

A THESIS SUBMITTED TO THE GRADUATE DIVISION OF THE UNIVERSITY OF HAWAI'I AT MĀNOA IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF

(MASTER OF SCIENCE)

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(DEGREE-AWARDEDMONTH) (DEGREE-AWARDED YEAR)

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Keywords: (keyword-1, keyword-2, keyword-3, ...)

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To my	,

ACKNOWLEDGMENTS

Firstly, I want to express my appreciation and respect to my

ABSTRACT

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TABLE OF CONTENTS

A	cknov	wledgments	\mathbf{v}
Al	ostra	ct	ii
Li	st of	Tables	x
Li	st of	Figures	κi
1	Sew	ver Chamber Design under Critical Conditions using Computational Fluid	
	Dyn	namics (CFD)	1
	1.1	Introduction	1
	1.2	Simulations	1
		1.2.1 Governing equations	1
		1.2.2 Manhole structure and meshing	2
	1.3	Results and Discussions	2
		1.3.1 Result section title	2
		1.3.2 Tantalizing phenomena	3
		1.3.2.1 3D investigation	3
		1.3.2.2 2D investigation	3
		1.3.3 Result verification and convergence test	3
	1.4	Conclusion	3
\mathbf{A}	\mathbf{App}	pendix	8
	A.1	Hollow and Filled Unit Stem Generation Using C++ and GNU Make Utility	8
	A.2	MATLAB Script to calculate alphaU	0
	A.3	Symmetry Boundary Condition Shear Calculations	2
	A.4	Alternative Canopy Orientations	2
\mathbf{Bi}	bliog	graphy	4

LIST OF TABLES

1.1	Chamber and pipe dimensions. CFD simulations were conducted for three outlet	
	diameters: $18, 20, \text{ and } 24 \text{ inches } (0.457, 0.508, \text{ and } 0.610 \text{ meters, respectively}).$	4
1.2	Properties of water and air used for interFoam simulations. In addition, the surface	
	tension between water and air was set as 0.072 N/m and the gravitational acceleration (9.81m/s^2) was used	5
A.1	Calculations of shear rate [1/s] using the fine mesh at time = 3.00s with front and back faces (cyclic)	12



LIST OF FIGURES

1.1	Section view of a real manhole	6
1.2	Generated mesh structures: (a) 2D and (b) 3D views. The lower purple and upper	
	brown regions represent water and air phases, respectively. The vertical line in the	
	y-direction near the chamber outlet indicates a line through which sewage levels are	
	calculated using OpenFOAM simulation results. In addition, x -direction is along the	
	left inlet pipe, and z-direction is out of the $x-y$ plane	7
A 1		10
A.1	0-0-0-0-0 stem orientation (a)2D and (3) 3D plot	13

CHAPTER 1 SEWER CHAMBER DESIGN UNDER CRITICAL CONDITIONS USING COMPUTATIONAL FLUID DYNAMICS (CFD)

This chapter of the dissertation is a manuscript published in Desalination and Water Treatment, 108 (2018) 1-14, doi: 10.5004/dwt.2018.22019.

Transient sewage flow patterns inside a utility chamber are ...

Keywords: Computational fluid dynamics (CFD); OpenFOAM; Sewer design; manhole flow; urban runoff

1.1 Introduction

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1.2 Simulations

1.2.1 Governing equations

A brief summary of governing equations is as follows. As noted above, interFoam is a solver for two incompessible, isothermal, immiscible fluid, which uses the volume of fluid (VOD) phase fraction. The continuity and phase-fraction transport equations are

$$\nabla \cdot \boldsymbol{U} = 0 \tag{1.1}$$

and

$$\frac{\partial \alpha_1}{\partial t} + \nabla \cdot (\boldsymbol{U}\alpha_1) = 0 \tag{1.2}$$

respectively, and the momentum equation is

$$\frac{\partial (\rho \mathbf{U})}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) = -\nabla p + \nabla \cdot \mathbf{T} + \rho \mathbf{f}_b$$
(1.3)

where α_1 is the phase-fraction of water, ranging from 0.0 to 1.0. In Eq. (1.3), T in is the stress tensor and f_b is a body force term including gravity and surface tension, and the fluid density ρ and viscosity μ are estimated as

$$\rho = \alpha_1 \rho_1 + (1 - \alpha_1) \rho_0 \tag{1.4}$$

$$\mu = \alpha_1 \mu_1 + (1 - \alpha_1) \mu_0 \tag{1.5}$$

where the subscript 1 and 0 indicate water and air phases, respectively. More details of the solver can be found elsewhere [8, 9].

1.2.2 Manhole structure and meshing

Fig. 1.1 shows ...

•

This is summarized in Table 1.1.

Fig. 1.2 shows ..

1.3 Results and Discussions

1.3.1 Result section title

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1.3.2 Tantalizing phenomena

1.3.2.1 3D investigation

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1.3.2.2 2D investigation

1.3.3 Result verification and convergence test

In this section, we provide ...

1.4 Conclusion

In order to maintain ...

Acknowledgment This research used the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National Science Foundation grant number ACI-1053575, and was financially supported by R. M. Towill Corporation, Honolulu, Hawaii, USA. The authors appreciate Mr. Jonathan Imai for his Solid Works drawing for the mesh generation.

	D	L	W	Н
inlet pipe	16.0 in. (0.406 m)	16.0 ft (4.9 m)	_	_
outlet pipe	18.0 in. (0.457 m)	22.0 ft (6.7 m)	_	_
chamber	_	10.0 ft (3.0 m)	4.0 ft (1.2 m)	6.0 ft (1.8 m)

Table 1.1: Chamber and pipe dimensions. CFD simulations were conducted for three outlet diameters: 18, 20, and 24 inches (0.457, 0.508, and 0.610 meters, respectively).

	water	air	unit
fluid type	Newtonian	Newtonian	-
density, ρ	998.0	1.21	${\rm kg/m^3}$
kinematic viscosity, ν	1.0×10^{-6}	1.51×10^{-5}	m^2/s

Table 1.2: Properties of water and air used for interFoam simulations. In addition, the surface tension between water and air was set as $0.072~\mathrm{N/m}$ and the gravitational acceleration $(9.81\mathrm{m/s^2})$ was used.

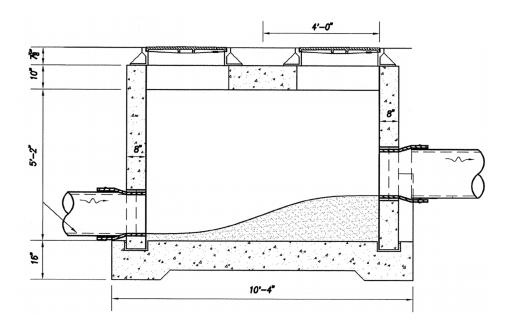


Figure 1.1: Section view of a real manhole.

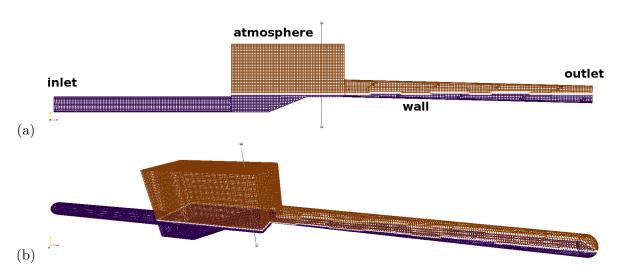


Figure 1.2: Generated mesh structures: (a) 2D and (b) 3D views. The lower purple and upper brown regions represent water and air phases, respectively. The vertical line in the y-direction near the chamber outlet indicates a line through which sewage levels are calculated using OpenFOAM simulation results. In addition, x-direction is along the left inlet pipe, and z-direction is out of the x-y plane.

APPENDIX A APPENDIX

A.1 Hollow and Filled Unit Stem Generation Using C++ and GNU Make Utility

Source code: gen_blockMeshToFile-v8.tex

```
1 #include <iostream>
2 #include <fstream>
3 #include <ctype.h>
4 #include <stdio.h>
5 #include <stdlib.h>
6 #include <unistd.h>
7 using namespace std;
8
9 int main (int argc, char **argv){
10
                        cylinderType, comma ;
      char
11
                        // hollow (h or H) or filled (f or F)
12
      double
                       Rinr = 0.5;
13
      double
                       HLCx = 2.0;
14
      double
                       HLCy = 2.0;
15
      int
                       nGrZ = 5;
                       Ninr = 8;
16
      int
17
      char
                        idSp,idX, idY;
18
19
      std::ifstream infile("blockMesh.param");
      cylinderType= 'F';
20
      infile
21
                  >> Rinr
                                            // >> comma
                  >> HLSq
                                            // >> comma
22
23
                  >> FLCz
                                            // >> comma
24
      std::cout << "infile_{\sqcup\sqcup}=_{\sqcup}" << "blockMesh.param" << endl;
25
      std::cout << "Rinr_{\sqcup\sqcup\sqcup\sqcup}=_{\sqcup}" << Rinr << endl;
26
      \mathtt{std}::\mathtt{cout} << \ "\mathtt{HLSq}_{\sqcup\sqcup\sqcup\sqcup}=_{\sqcup}" << \ \mathtt{HLSq} << \ \mathtt{endl};
27
28
```

```
29
    /* omitted */
30
31
    /* MERGEPATCHPAIRS */
    outfile <<"mergePatchPairs" <<endl;</pre>
32
    outfile <<"("<<endl;</pre>
33
    outfile <<");"<<endl<<endl;</pre>
34
    35
36
37
    outfile.close();
    return 0;}
38
  Makefile
1 # Makefile
2 version=v8
3 srcroot=gen_blockMeshToFile-$(version)
4 cxx=g++
5 # CXX = c++ compiler
6 # cxx = icpc
7 #
8 gbm:
           $(cxx) $(srcroot).cpp -o $(srcroot).x
9
10
11 hollow:
12
          cp -f blockMesh.param.default blockMesh.param
           sed -i 's/cylinderType/H/' blockMesh.param $(srcroot).x
13
          cp blockMeshDict_hollow \
14
15
                   ./stem_hollow/stem_hollow/system/blockMeshDict
          cd ./stem_hollow/stem_hollow && blockMesh
16
17
18
  filled:
19
           cp -f blockMesh.param.default blockMesh.param
20
           sed -i 's/cylinderType/F/' blockMesh.param $(srcroot).x
21
           cp blockMeshDict_filled \
22
                   ./stem_filled/stem_filled/system/blockMeshDict
23
          cd ./stem_filled/stem_filled && blockMesh
```

A.2 MATLAB Script to calculate alphaU

The following script and associated text files were used to produce AlphaU datasets for each simulation time step. This MATLAB script was initially used until modifications were made directly in the OpenFOAM script to automatically calculate alphaU. As seen in the README.txt section, there are variables within the matlab script that will need to be changed depending on the OpenFOAM case and mesh size.

AlphaU.m

```
1 \% Create Alpha - U Data Set
 2 \% Date \Box Created: \Box September \Box 7, \Box 2019
 3 \% Last \cup Updated : USeptember \cup 12, \cup 2019
 4 \quad \text{$\%_{\sqcup}$ Created$$$_{\sqcup}$ by:$$_{\sqcup}$ Tyler$$_{\sqcup}$ Tsuchida$$_{\sqcup}$ \%$$_{\sqcup}$ Document$$_{\sqcup}$ Name:$_{\sqcup}$ CreateAlphaU.m.}
 5 \quad \% \sqcup \textit{Location:} \sqcup /\textit{home/student/Documents/TylerTsuchida/}
           TylerTsuchidaThesis/
 6\ \%_{\sqcup} Description:_{\sqcup} This_{\sqcup} script_{\sqcup} is_{\sqcup} to_{\sqcup} create_{\sqcup} a_{\sqcup} new_{\sqcup} dataset, _{\sqcup} alphaU, _{\sqcup} for_{\sqcup}
           every_{\sqcup}timestep_{\sqcup}in_{\sqcup}an_{\sqcup}openFOAM_{\sqcup}simulation
 7 \%_{\square}Read_{\square}alpha.water_{\square}and_{\square}U_{\square}values_{\square}from_{\square}time-step_{\square}file
 8 \%Some_{\sqcup}lines_{\sqcup}beyond_{\sqcup}this_{\sqcup}point_{\sqcup}may_{\sqcup}need_{\sqcup}revision
 after_{\sqcup}U_{\sqcup}or_{\sqcup}alphawater_{\sqcup}header
10 num_boundary_rows=10500; \square%number\squareof\squaredata\squarepoints\squareat\squareboundaries\square--\square
          given_{\sqcup} after_{\sqcup} boundary_{\sqcup} conditions_{\sqcup} are_{\sqcup} stated_{\sqcup} at_{\sqcup} end_{\sqcup} of_{\sqcup} U_{\sqcup} or_{\sqcup}
           alphawater
before \_mes \_data \_is \_written
    \verb|num_boundarylines=5340528; \verb||| % number || of || lines || from || line || 1 || of || code || to ||
           line_{\sqcup}before_{\sqcup}boundary_{\sqcup}data_{\sqcup}is_{\sqcup}written
    \texttt{folder=3:} \; \sqcup \; \textit{\%the} \; \_ \; next \; \_ \; line \; \_ \; of \; \_ \; code \; \_ \; lists \; \_ \; all \; \_ \; folders \; \_ \; in \; \_ \; your \; \_ \;
13
          simulation_{\sqcup}directory, _{\sqcup}to_{\sqcup}skip_{\sqcup}invisible_{\sqcup}folders,
14 folder=1st_{\sqcup}time_{\sqcup}step_{\sqcup}folder_{\sqcup}on_{\sqcup}list
15 timestep=dir('/media/student/Elements/2019-10-25-Coarse/
          \verb|cavity_cFE_coarse0/cavity_cFE_coarse0'|; \verb||%insert_{||} & directory_{||} \\ with_{||} \\
          all_{\sqcup}timesteps_{\sqcup}here
16 %Do_{\square}not_{\square}need_{\square}to_{\square}edit_{\square}the_{\square}code_{\square}beyond_{\square}this_{\square}point
17 \ \% \ \dots
18 %<sub>U</sub>...
```

```
19 end
   alphaU sections
   alphaU\_Header2.txt
1 object alphaU;
2 }
3 //************************//
4 dimensions [0 1 -1 0 0 0 0];
5 internalField nonuniform List<vector>
6 5340000
7 (
   alphaU_Footer1.txt
2 boundaryField
3 {
   DOWN_btm_F00 { type noSlip; }
4
   DOWN_btm_H10 { type noSlip; }
5
6
7
   DOWN_inn_F36 { type noSlip; }
    DOWN_inn_F46 { type noSlip; }
8
    merged_LEFT_inn_F40 { type flowRateInletVelocity; volumetricFlowRate
9
       constant 0.0075; extrapolateProfile false; value uniform (0.3197619
        -0 -0; }
    merged_RGHT_btm_F90 { type pressureInletOutletVelocity; value
10
       nonuniform List<vector> 10500 (
   alphaU_Footer 2.txt
1 ) ; }
2 merged_FRNT_inn_F10 { type noSlip; }
3 merged_FRNT_btm_F00 { type noSlip; }
4 merged_BACK_inn_F16 { type noSlip; }
5 merged_BACK_btm_F06 { type noSlip; }
6 merged_ATOP_inn_F46 { type zeroGradient; }
7 merged_ATOP_btm_F96 { type zeroGradient; }
8 }
```

9 10 // ************//

README.txt

- 1 Sources for data files:
- 2 alphaU_generator.zip
- 3 alphaU_generator:
- $4 \quad alphaU_Footer1.txt \quad alphaU_Footer2.txt \quad alphaU_Header2.txt \quad calc_alphaU.m \\ README.txt$
- 5 All files listed above must be in the directory of all timestep folders for calc_alphaU.m to run properly.
- 6 Enter directory and other information in calc_alphaU.m as needed to match information of the desired run.

A.3 Symmetry Boundary Condition Shear Calculations

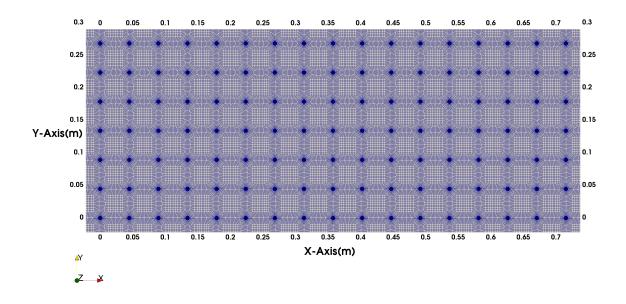
Along with the shear rate calculations presented in the paper, calculations were also performed on the fine, medium, and coarse meshes using cyclic boundary conditions. Also, shear rates of the checkerboard were also calculated as supplementary information.

Face Name	$\frac{\partial(\alpha U_x)}{\partial x}$	$\frac{\partial(\alpha U_x)}{\partial y}$	$\frac{\partial(\alpha U_x)}{\partial z}$	$\frac{\partial(\alpha U_y)}{\partial x}$	$\frac{\partial(\alpha U_y)}{\partial y}$	$\frac{\partial(\alpha U_y)}{\partial z}$
DOWN_Eab_merged	2.64E-02	6.91E-09	3.90E+00	_	_	_
HOLE_Eab	-1.49E-02	1.12E-07	-6.66E-11	_	_	_
HOLE_Eab	_	_	_	-1.01E-07	1.81E-02	8.54E-11
inlet	1.07E-03	0.00E+00	0.00E+00	_	_	_
outlet	1.07E-03	1.13E-09	-2.57E-04	_	_	_

Table A.1: Calculations of shear rate [1/s] using the fine mesh at time = 3.00s with front and back faces (cyclic).

A.4 Alternative Canopy Orientations

The following figures shows alternative configurations of 24 stems embedded on the bed surface.



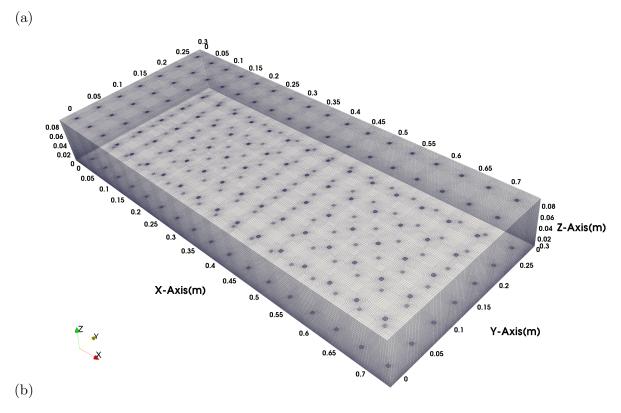


Figure A.1: 0-0-0-0-0-0 stem orientation (a)2D and (3) 3D plot.

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