

# Enrico Facca

## Academic Curriculum

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## Current Position

2019/Now **Postdoc research fellowship**, *Centro di Ricerca Matematica Ennio De Giorgi - Scuola Normale Superiore, Pisa (Italy)*, Advisor: Michele Benzi.

## Positions Held

2018/2019 **Postdoc research fellowship**, *Padova University (Italy)*, Advisor: Mario Putti.

2018 **Scholarship researcher**, *Padova University (Italy)*, Advisor: Mario Putti.

## Education

2018 **PhD in Mathematics**, *Padova University (Italy)*, Supervisor: Mario Putti, Co-advisor Franco Cardin Thesis: *Biologically inspired formulation of Optimal Transport Problems*.

2014 **Master in Mathematics**, *Padova University (Italy)*, Supervisor: Mario Putti, Co-advisor Franco Cardin. Thesis: *A biology-inspired model for the Optimal Transport Problem*.

2011 **Bachelor in Mathematics**, *Padova University (Italy)*, Supervisor: Francesco Fassò. Thesis: *Reduction of vector fields invariant under Lie group action*.

## Teaching and Tutoring experiences

2018/2019 **Numerical calculus, Matlab laboratory assistant**, *Aerospace Engineering Bachelor, University of Padova*, 24 hours lectures.

2016 **Pre-course for Physical-Mathematics Models**, *Mathematical Engineering Master, University of Padova*, six hours lectures.

2013/2014 **Tutor for Calculus and Linear Algebra**, *Engineering Bachelor, University of Padova*, 24+24 exercise hours.

## Research interests

- Numerical solution of Optimal Transport Problems: Monge-Kantorovich Problem, Congested and Branched Transport Problems
- Biological and complex networks
- Sparse Optimization, Basis Pursuit Problem

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## Research activities summary

In my PhD thesis, I introduced a dynamical formulation, called Dynamical Monge-Kantorovich (DMK), of the Optimal Transport Problem (OTP). The OTP is a type of optimization problem where the goal is to determine the optimal reallocation of resources from one configuration to another. The definition of the DMK model equations and the develop of methods for the numerical solution of the OTP have been summarized in [A5, A2, A4]. Recent advances in the theoretical consolidation of the DMK model are described in [P4], where we introduced a Gradient Flow reinterpretation of the model. In [P5] we introduced an extension of DMK model addressing those problems where concentration along the transport is either penalized or favored is described. More recently, I started exploring some adaptation of the DMK model in finite dimensional frameworks, starting from the ideas presented in [P6]. Together with Caterina De Bacco and her PhD students at Max Plank Institute in Tübingen, in [A1, P3] we worked on the application of a discrete version of the DMK model on graphs. In collaboration with the research group of Prof. Kurt Mehlhorn from Max Plank Institute in Saarbrücken, in [A3] we studied a reformulation of the discrete DMK model addressing the solution of Linear Programming problem. In [P1] we addressed the solution of the multi-commodity Optimal Transport Problem i.e., the extension of the OTP where different resources needs to be reallocated. In [P2], together with Prof. Michele Benzi from Scuola Normale Superiore Pisa, we worked on the efficient numerical solution of the OTP on graphs, combining backward Euler time-stepping of the dynamical equations of the DMK model with inexact Newton Method.

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## List of Publications

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### PhD Thesis

Facca Enrico. *Biologically inspired formulation of Optimal Transport Problems* . 2018.

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### Peer-Reviewed Journal Articles

- [A1] Diego Baptista, Daniela Leite, Enrico Facca, Mario Putti, and Caterina De Bacco. “Network extraction by routing optimization”. In: *Sci. Rep.* 10 (2020).
- [A2] Enrico Facca, Sara Daneri, Franco Cardin, and Mario Putti. “Numerical solution of Monge–Kantorovich Equations via a Dynamic Formulation”. In: *J. Scient. Comput.* 82.3 (2020), pp. 1–26.
- [A3] Enrico Facca, Andreas Karrenbauer, Pavel Kolev, and Kurt Mehlhorn. “Convergence of the non-uniform directed Physarum model”. In: *Theor. Comput. Sci.* 816 (2020), pp. 184–194.
- [A4] Luca Bergamaschi, Enrico Facca, Ángeles Martínez Calomardo, and Mario Putti. “Spectral preconditioners for the efficient numerical solution of a continuous branched transport model”. In: *J. Comput. Appl. Math.* 354 (2018), pp. 259–270.
- [A5] Enrico Facca, Franco Cardin, and Mario Putti. “Towards a Stationary Monge–Kantorovich Dynamics: The Physarum Polycephalum Experience”. In: *SIAM J. Appl. Math.* 78.2 (2018), pp. 651–676.

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### Preprints

- [P1] Vincenzo Bonifaci, Enrico Facca, Frederic Folz, Andreas Karrenbauer, Pavel Kolev, Kurt Mehlhorn, Giovanna Morigi, Golnoosh Shahkarami, and Quentin Vermande. “Physarum Multi-Commodity Flow Dynamics”. Under review at Theor. Comput. Sci. (ArXiv preprint available). 2020.
- [P2] Enrico Facca and Michele Benzi. “Fast Iterative Solution of the Optimal Transport Problem on Graphs”. Under review at SIAM J. Sci. Comput. (ArXiv preprint available). 2020.
- [P3] Alessandro Lonardi, Enrico Facca, Mario Putti, and Caterina De Bacco. “Optimal transport for multi-commodity routing on networks”. Under review at Phys. Rev. Res. (ArXiv preprint available). 2020.
- [P4] Enrico Facca and Federico Piazzon. “Transport Energy”. (ArXiv preprint available). 2019.
- [P5] Enrico Facca, Franco Cardin, and Mario Putti. “Branching structures emerging from a continuous optimal transport model”. Under review at J. Comp. Phys. (ArXiv preprint available). 2018.
- [P6] Enrico Facca, Franco Cardin, and Mario Putti. “Physarum Dynamics and Optimal Transport for Basis Pursuit”. (ArXiv preprint available). 2018.

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## List of Scientific Presentations

- 10-14-2020 **Invited Research Seminary**, *Presentation to the Vittorio Di Federico research group, “Emergence of branching structures via Optimal Transport and P-Laplacians”*, Bologna (Italy).
- 10-02-2019 **Contributed Talk**, *European Numerical Mathematics and Advanced Applications Conference 2019, “Optimal Transport Tools on Surface”*, Egmond aan Zee (Netherland).
- 06-26-2019 **Contributed Talk**, *People in Optimal Transportation and Applications - Incontri Indam 2019*, “A nature inspired optimization tool”, Cortona (Italy).
- 04-14-2019 **Contributed Talk**, *SIAM Conference on Mathematical Computational Issues in the Geosciences, “Plant Root Modeling via Optimal Transport”*, Houston - Texas, USA .
- 04-12-2019 **Contributed Talk**, *SIAM Conference on Mathematical Computational Issues in the Geosciences, “Numerical Solution of  $L^1$ -Optimal Transport Problem”*, Houston - Texas, USA .
- 11-15-2018 **Invited Presentation**, *Optimal Transportation and Applications*, “Biologically inspired deduction of Optimal Transport Problems”, Pisa, Italy.
- 09-06-2018 **Research Seminar**, *Presentation to porous media research group, “Biologically inspired formulation of Optimal Transportation Problems”*, Bergen, Norway.
- 07-06-2018 **Contributed Talk**, *SIMAI 2018, “Biologically inspired formulation of Optimal Transportation Problems”*, Roma, Italy.
- 06-04-2018 **Contributed Talk**, *Computational Methods in Water Resources XXIII, “Plant root dynamics via Optimal Transport”*, Saint Malom, France.

- 04-05-2018 **Contributed Talk**, *Terrestrial Systems Research: Monitoring, Prediction and High Performance Computing*, “*Hydrological networks as optimal transport structures*”, Bonn, Germany .
- 09-11-2017 **Contributed Talk**, *SIAM Conference on Mathematical and Computational Issues in the Geo-sciences*, “*Biologically inspired formulation of Optimal Transportation Problems*”, Erlangen, Germany.
- 04-27-2017 **Research Seminar**, *Presentation to the Fabio Nobile research group*, “*Biologically inspired formulation of Optimal Transportation Problems*”, Lausanne, Switzerland.
- 12-18-2014 **Contributed Talk**, *Current Problems in fluid-dynamics and non equilibrium thermodynamics*, “*Biologically inspired formulation of Optimal Transportation Problem*”, Bressanone, Italy.

## Master Thesis Co-supervision

Co-advisor with Mario Putti of the master degree thesis in Mathematics and Mathematical Engineering of Andrea Pinto (2015), Enrico Cortese (2017), Claudia Dario (2017), Riccardo Tosi (2018), Luca Berti (2018), Nicola Segala (2019).

## Visiting periods

- 2019 **Max Planck Institute Saarbrücken, Germany**, One week working on *Polycephalum model for Basis Pursuit Problem* with the research group of Kurt Mehlhorn.
- 2018 **Bergen University, Norway**, One week working on the application of the *Branched Transport Problem* to the study of blood vessel in the brain with the research group of Jan Martin Nordbotten.
- 2016 **Orsay - Paris Sur University, France**, Two weeks working on my doctoral dissertation with with *Filippo Santambrogio*.
- 2015-2016 **Friedrich-Alexander-Universität Erlangen-Nürnberg Germany**, Seven months working on my doctoral dissertation with *Peter Knabner, Aldo Pratelli, and Sara Daneri*.

## Organizing activities

- Organizer of a two-days workshop “*Seminari Padovani di Analisi Numerica 2018*” May 2018, Padova.

## Computer skills

- Advanced knowledge with Unix system
- Expert with Fortran, including Object-Oriented Fortran 2003-2008
- Advanced knowledge with Python, Matlab

## Languages

Italian Mother tongue

|         | Understanding |         | Speaking | Writing |
|---------|---------------|---------|----------|---------|
|         | Listening     | Reading | -        | -       |
| English | B2            | C1      | B2       | B2      |
| Spanish | B2            | C1      | B2       | B2      |

## References

*For a reference letter please contact the following persons.*

- Michele Benzi (Scuola Normale Superiore, Italy)
- Giuseppe Buttazzo (University of Pisa, Italy)
- Franco Cardin (University of Padova, Italy)
- Malgorzata Peszynska (Oregon State University, USA)
- Mario Putti (University of Padova, Italy)