

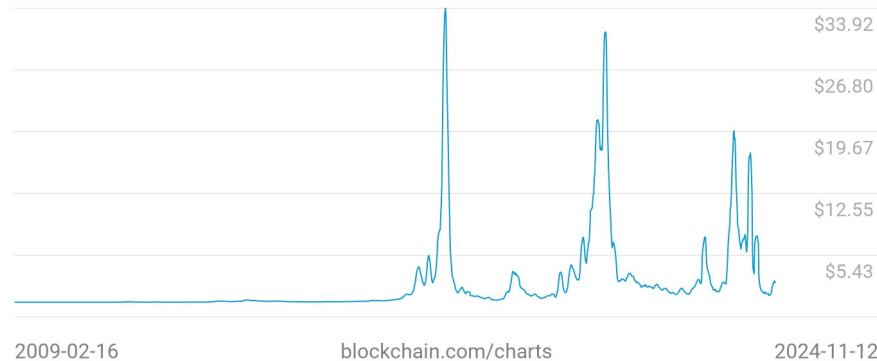
# Decentralized Systems

**Payment Channels**

# Transaction Cost

FEES USD PER TRANSACTION

\$2.27



- When the number of transactions grows, transaction fees go up
- Scalability limit: fixed number of slots per second, demand may go up

# First Ever Answer On Bitcoin

Satoshi Nakamoto wrote:

```
> I've been working on a new electronic cash system that's fully  
> peer-to-peer, with no trusted third party.  
>  
> The paper is available at:  
> http://www.bitcoin.org/bitcoin.pdf
```

We very, very much need such a system, but the way I understand your proposal, it does not seem to scale to the required size.

For transferable proof of work tokens to have value, they must have monetary value. To have monetary value, they must be transferred within a very large network - for example a file trading network akin to bittorrent.

To detect and reject a double spending event in a timely manner, one must have most past transactions of the coins in the transaction, which, naively implemented, requires each peer to have most past transactions, or most past transactions that occurred recently. If hundreds of millions of people are doing transactions, that is a lot of bandwidth - each must know all, or a substantial part thereof.

Source: James A. Donald, archived by the **Satoshi Nakamoto Institute**

# Off-Chain Transactions

- There is an inherent scalability limit on a single blockchain
  - With  $n$  users,  $O(n^2)$  total storage
- Writing on a blockchain is **expensive** and it has **limited throughput**
  - We are writing **too many copies of them**
- We will look at alternatives that allow transacting **without touching the blockchain**

# References

- J. Poon and T. Dryja. **The Bitcoin Lightning Network: Scalable Off-Chain Instant Payments.**
- N. Narula and T. Dryja, **Cryptocurrency Engineering and Design.** MIT OpenCourseWare, lectures 13 and 14.

# The Bitcoin Lightning Network

# One-Way Channels: Idea

- Incremental payment channels for **recurring payments from A to B**
- A sets aside a given amount of money in a transaction
- When they are both done, the channel is closed and each gets their remaining balance
- Key: doing it **without trust involved**

# One-Way Channels: Funding

- A “channel” is just a **multi-signature** output
  - an output for Alice and Bob can only be spent by transactions signed by **both Alice and Bob**
- Alice **funds** the channel to **spend at Bob's**

Funding transaction – on blockchain	
Input	Output
From: Alice's output Alice's signature	To: Alice's and Bob's multi-sig 10 coins



# One-Way Channels: Refund

- Transactions have a **lock time**:
  - output can be spent only after the lock time (block height)
- The refund transaction is signed **before** the funding one
  - Needs segwit to work

Refund transaction – <b>LOCKED UNTIL December 15, held by Alice</b>	
Input	Output
From: funding transaction's id (txid) Bob's signature (Alice's signature not there yet)	To: Alice's address 10 coins

# One-Way Channels: Full Setup

Funding transaction – on blockchain	
Input	Output
From: Alice's output Alice's signature	To: Alice's and Bob's multi-sig 10 coins

Refund transaction – <b>LOCKED UNTIL December 15, held by Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's address 10 coins

- Now, in the worst case, Alice can simply wait until she can get the refund
  - Alice won't lose money

# One-Way Channels: Spending (1)

Funding transaction – on blockchain	
Input	Output
From: Alice's output Alice's signature	To: Alice's and Bob's multi-sig 10 coins

Spending transaction 1 Held by Bob	
Input	Output
From: funding txid Alice's signature (Bob's signature not there yet)	To: Alice's address 9 coins
	To: Bob's address 1 coin

- Bob can post the transaction and **close the channel**
  - He should do before the refund transaction becomes valid

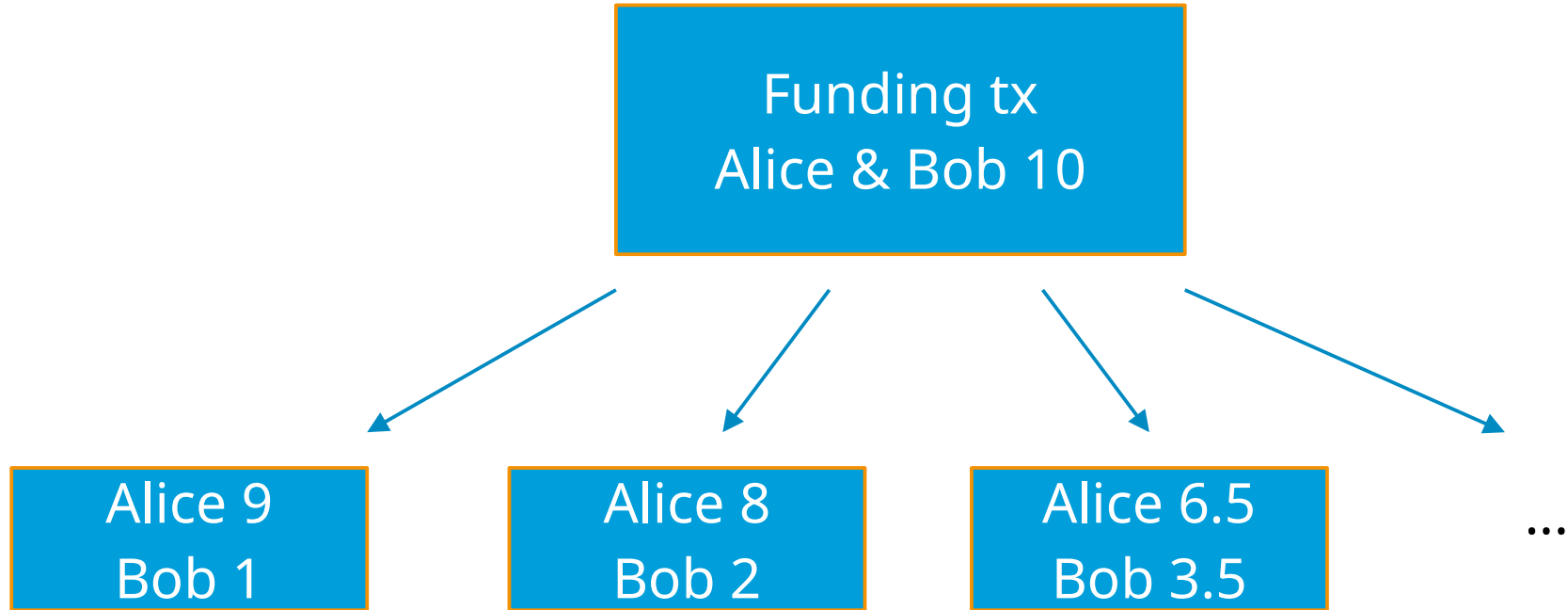
# One-Way Channels: Spending (2)

Spending transaction 1 <b>Held by Bob</b>	
Input	Output
From: funding txid Alice's signature (Bob's signature not there yet)	To: Alice's address 9 coins
	To: Bob's address 1 coin

Spending transaction 2 <b>Held by Bob</b>	
Input	Output
From: funding txid Alice's signature (Bob's signature not there yet)	To: Alice's address 8 coins
	To: Bob's address 2 coins

- Now Bob can forget about the first transaction: the **second is better**
- Spending transactions **aren't posted to the blockchain**
  - Until A and B want to close the channel

# One-Way Channels: Spending (3)



# One-Way Channels: Outcome

- Bob keeps getting half-signed transactions with more money going to him
  - **Fast** (off-chain payments) and with **no fees**
  - He **must** sign and broadcast one before the refund time!
- Currency flows **only one way**
  - From Alice to Bob, **never vice versa**
- Channels are only useful **before they expire**
  - Expiration can't be too far away: if Bob disappears Alice's funds are locked
- Common case: how many transactions on the blockchain?
  - Two: funding and closing (last expense by Alice)

# Bidirectional Payment Channels

- A construct that, like what we have seen until now
  - Avoids paying on-chain most transactions
  - Doesn't require trust between Alice and Bob
- But
  - Is bidirectional (money can flow in either direction)
  - Doesn't expire
- We'll follow the Bitcoin Lightning protocol
  - Raiden is the equivalent solution for Ethereum

# Bitcoin Timing Opcodes

## OP\_CHECKSEQUENCEVERIFY

- Argument: sequence
- Requires that the input has at least  $n$  confirmations
  - i.e., it is  $\geq n$  blocks old
- Otherwise, the transaction fails

## OP\_CHECKLOCKTIMEVERIFY

- Argument: locktime
- Requires that the transactions' output has at least  $n$  confirmations to be spent
- Otherwise, the transaction fails



# Using the New Opcodes

- “This transaction’s output is spendable by *[the private key corresponding to public]* key X after 100 blocks”
- “or by this other *[private key corresponding to public]* key Y”
- “or by [...] keys W and Z in conjunction”

# Revokable Transactions

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's key after 100 blocks OR To Bob and AliceR keys 2 coins
	To: Bob's address 8 coins

Held by <b>Bob</b>	
Input	Output
From: funding txid Alice's signature (Bob's signature not there yet)	To: Alice's address 2 coins
	To: Bob's key after 100 blocks OR To Alice and BobR keys 8 coins

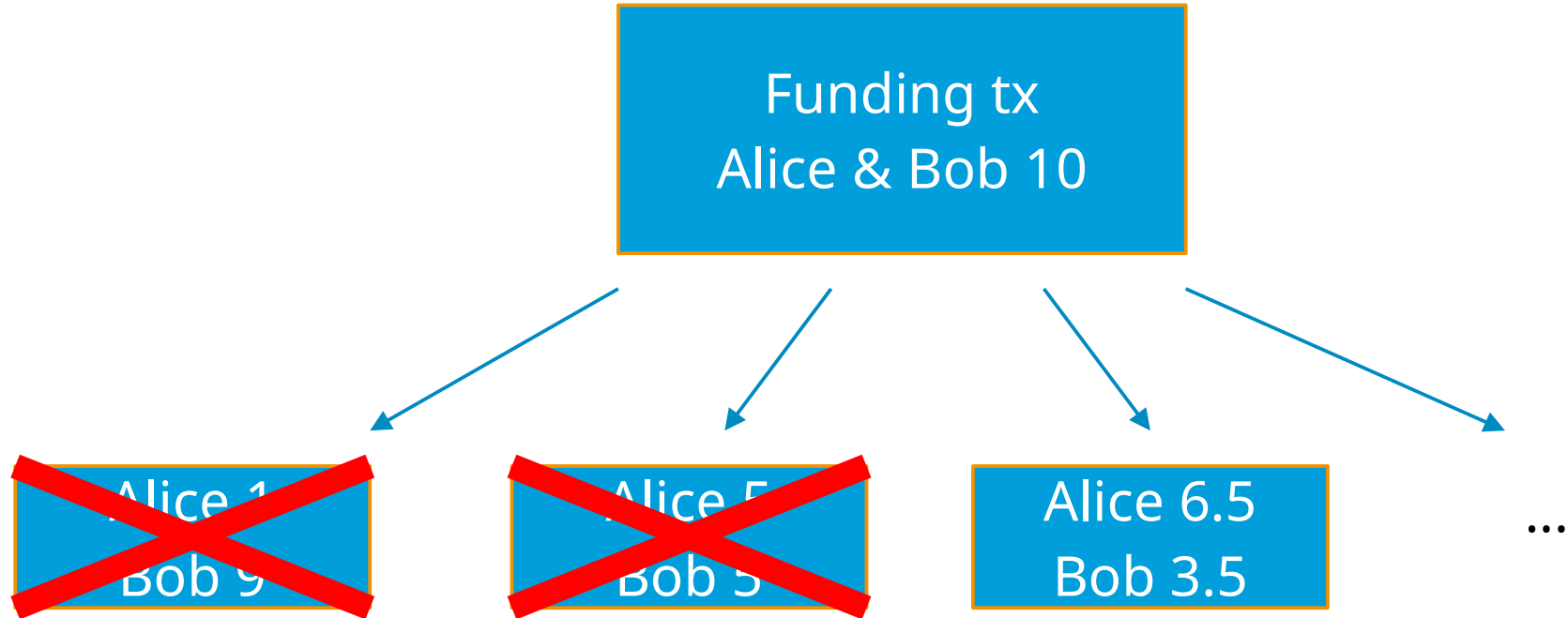
- Both Alice and Bob build new AliceR/BobR key pairs

# Reveal to Revoke

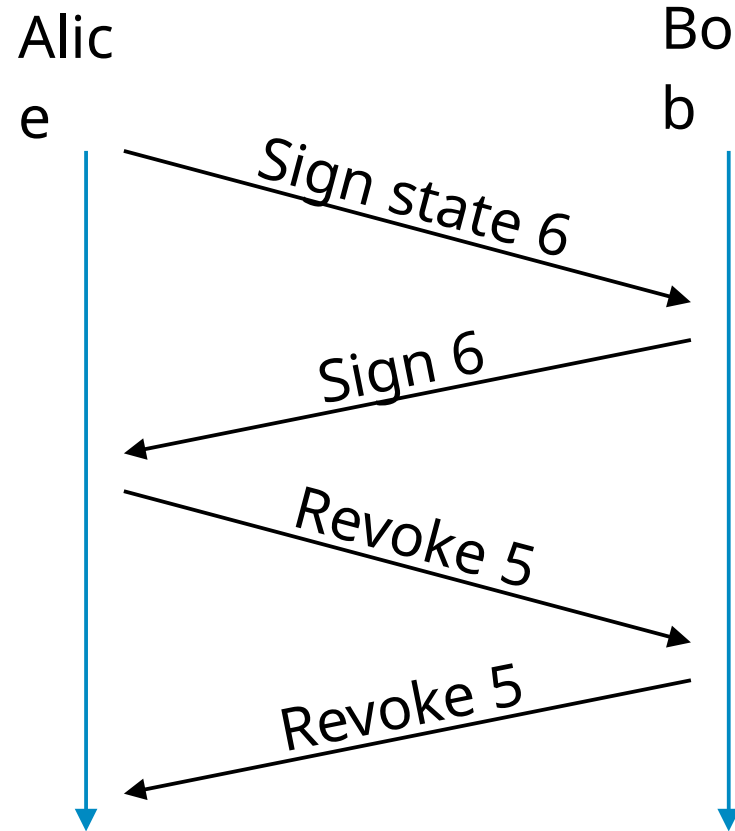
- Bob can **revoke** this transaction by sending Alice the BobR private key
- If he ever tries to broadcast this transaction, Alice can use BobR to recover **all** the funds in the channel
- Key assumption: **Alice has to remain online!**

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's key after 100 blocks OR To Bob and AliceR keys 2 coins
	To: Bob's address 8 coins

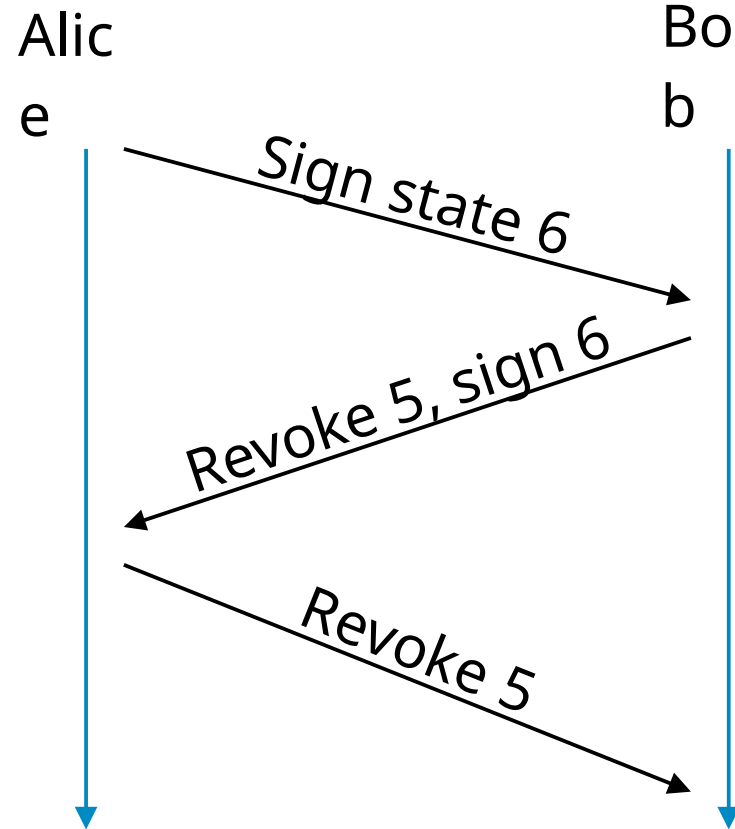
# Updating States



# Message Order



# Optimized Message Order



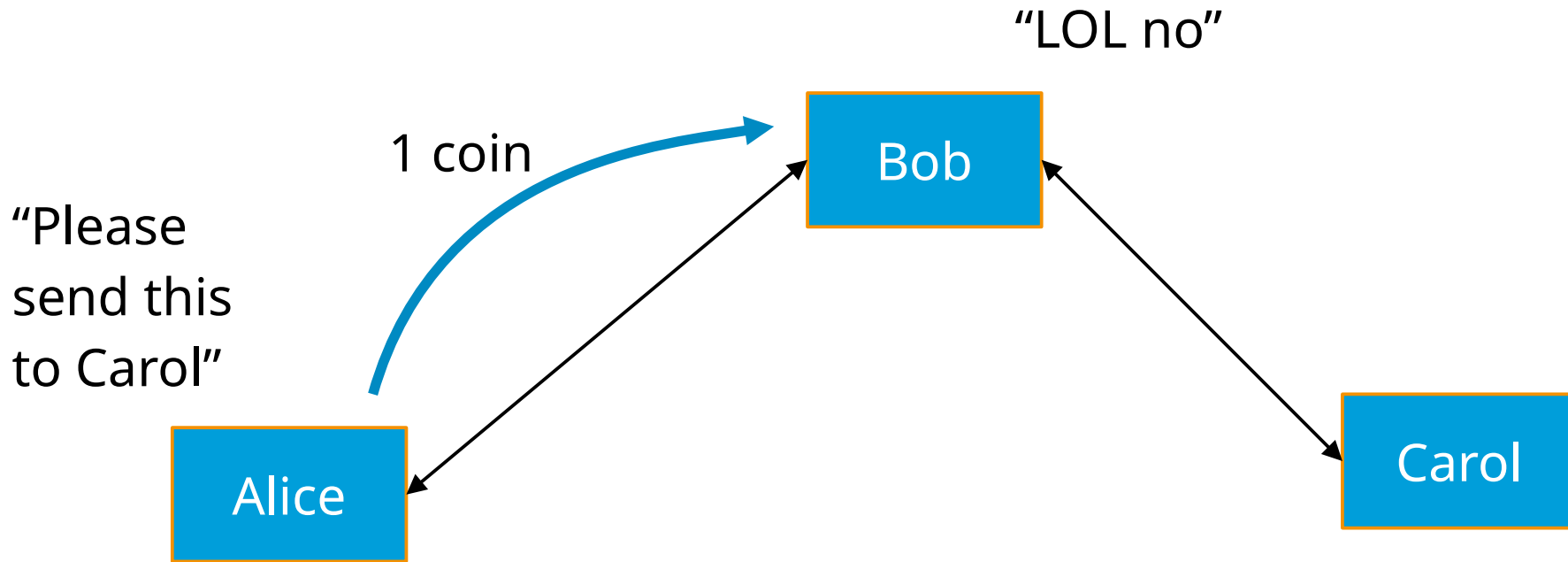
# Storing Revocation Secrets

- How many revocation secrets should one store?
  - (Almost) all those in the history of the channel!
  - 32 bytes per state
- A clever optimization: **Elkrem tree**
- With  $n$  transactions
  - You just need to store  $O(\log n)$  secrets
  - You need to perform  $O(\log n)$  hashes to get to the secret

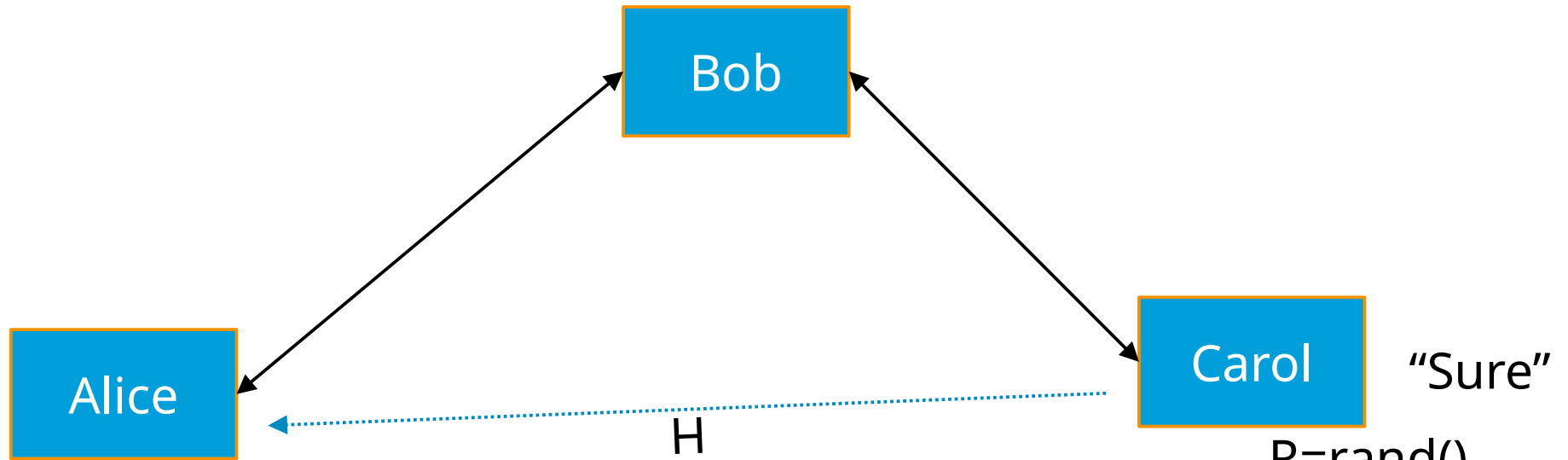
# Multi-Hop Transfers



# Trust Issues



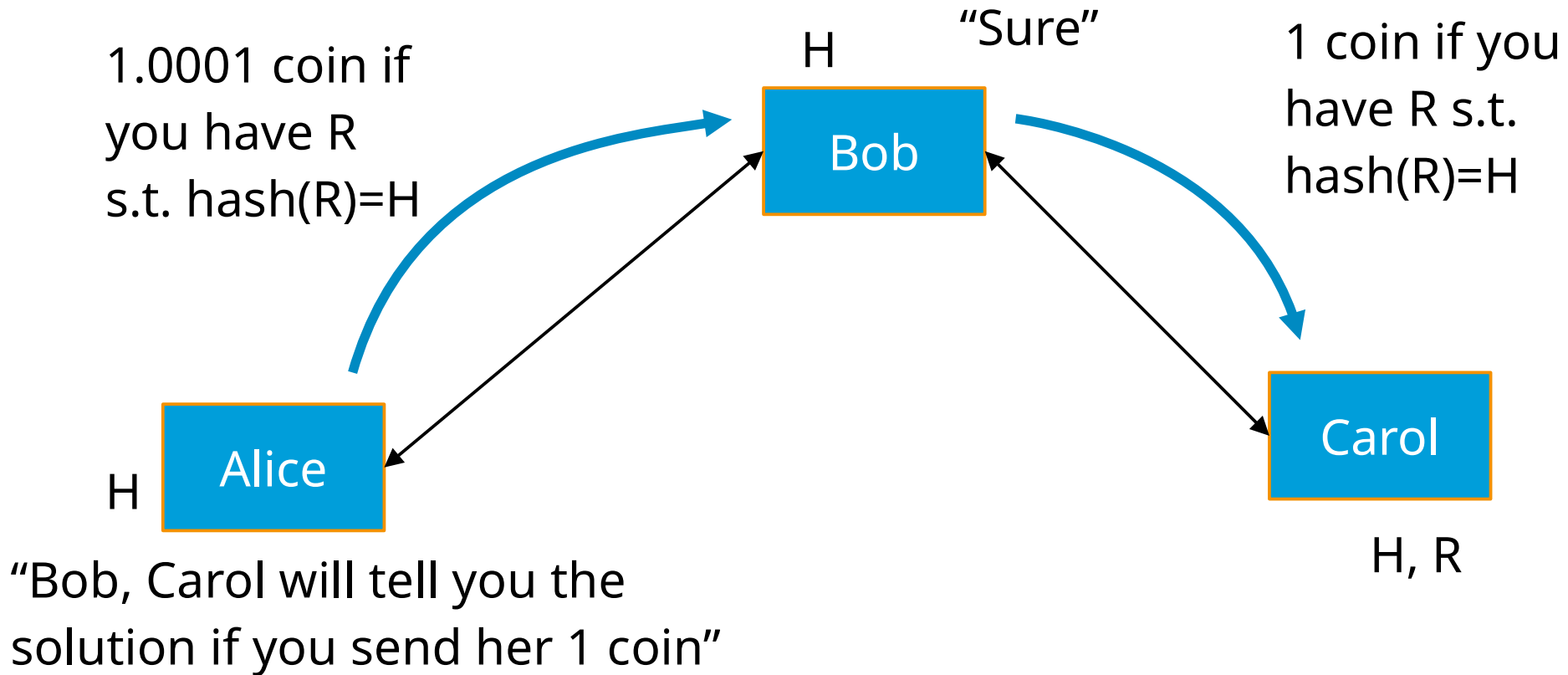
# The Method (1)



“Carol, pick a random number and send me its hash”

“Sure”  
 $R = \text{rand}()$   
 $H = \text{hash}(R)$

# The Method (2)



# Hash/Time Locked Contract (HTLC)

Held by <b>Bob</b>	
Input	Output
From: funding txid Alice's signature (Bob's signature not there yet)	To: Alice's address 0.9999 coin
	To Bob's key after 100 blocks OR To Alice and BobR keys 8 coins
	<b>To Bob if he knows the preimage to H</b> <b>OR</b> <b>To Alice at 17:00 (uses block height)</b> <b>1.0001 coin</b>

# How It's Implemented (1)

HTLC:

Bob with preimage of H

OR

Alice at 17:00

H

Alice

H

Bob

HTLC:

Carol with

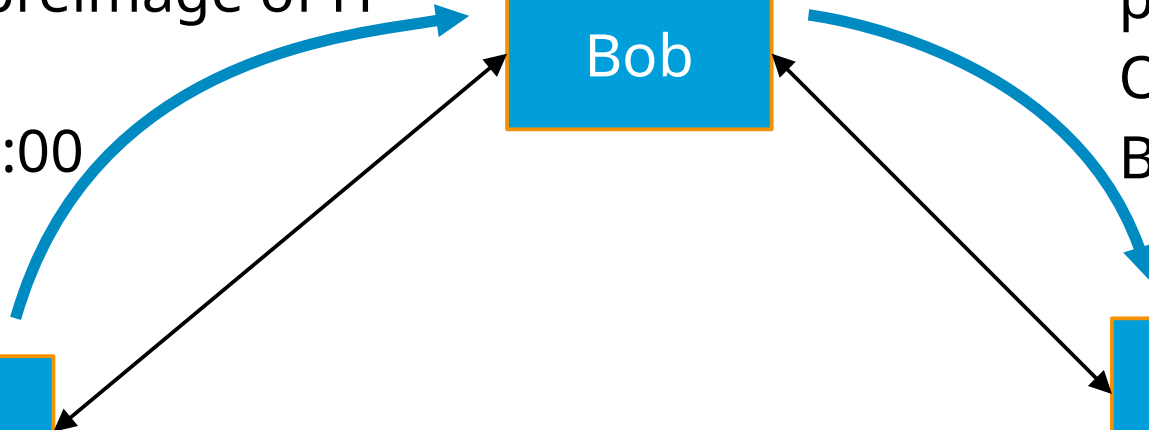
preimage of H

OR

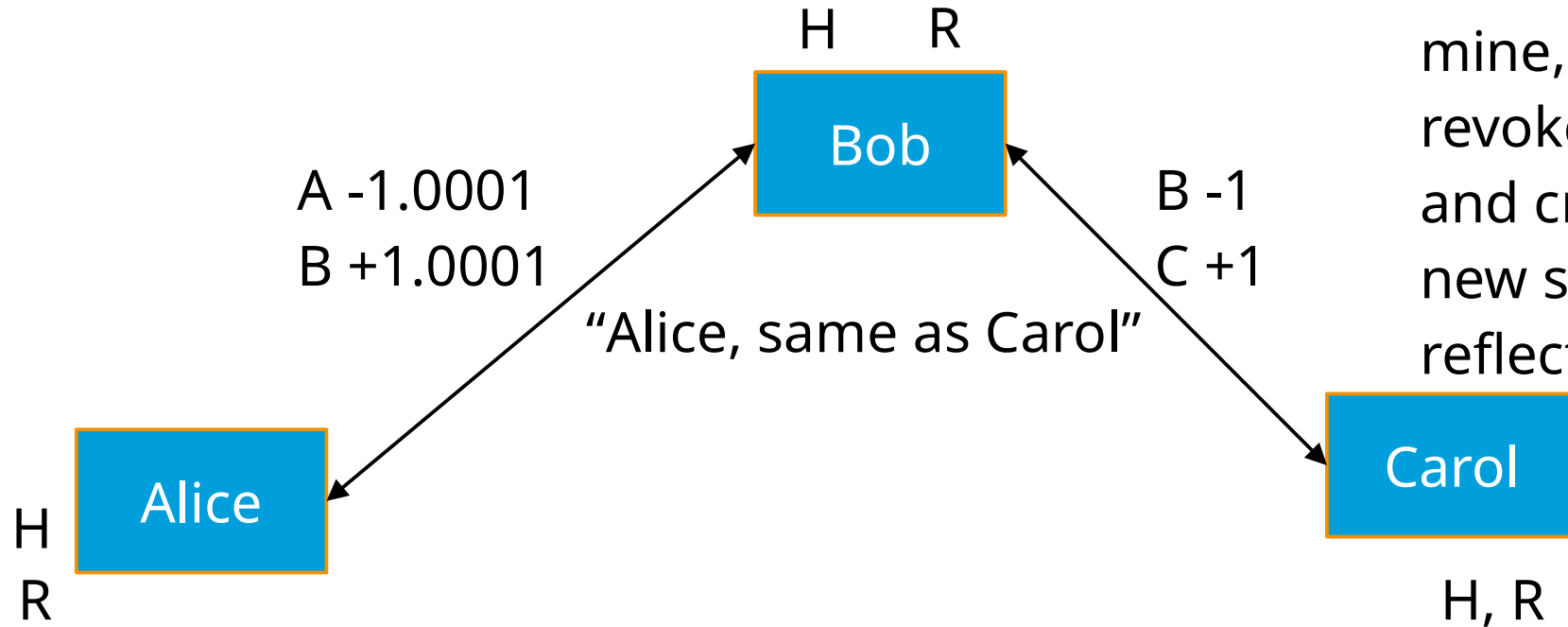
Bob at 16:00

Carol

H, R



# How It's Implemented (2)



"Bob, here's R, the money is mine, let's revoke the HTLC and create a new state that reflects that"

# Implementation

# Revocation Keys as Hash Preimages

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's key after 100 blocks OR To Bob and AliceR keys 2 coins
	To: Bob's address 8 coins

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's key after 100 blocks OR To Bob <b>if he knows P s.t. <math>H(P)=\text{AliceR}</math></b> 2 coins
	To: Bob's address 8 coins

- Less storage on blockchain (~20B vs ~80B), same concept



# An Elliptic Curve-Based Trick

- Remember the slides on elliptic curves? Say we have two private/public key pairs  $(b, B)$  and  $(c, C)$
- $(b+c, B+C)$  is a working key pair because
  - $bG=B, cG=C \rightarrow (b+c)G = B+C$

ECC: scalar multiplication 

- Given a known **base point G**, it can be multiplied by a private key **Sk** to find the corresponding public key **Pk**

# Even Better: Just Sum Keys

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To: Alice's key after 100 blocks OR To Bob and AliceR keys 2 coins
	To: Bob's address 8 coins

Held by <b>Alice</b>	
Input	Output
From: funding txid Bob's signature (Alice's signature not there yet)	To Alice's key after 100 blocks OR To <b>KeyR=Bob+AliceR</b> 2 coins
	To: Bob's address 8 coins

- Even shorter script
- Compactness matters this much on the blockchain!

# The Reduced Script

OP\_IF KeyR

OP\_ELSE

<delay>

OP\_CHECKSEQUENCEVERIFY

OP\_DROP

KeyA

OP\_ENDIF

OP\_CHECKSIG

- Stack-based language
- Working inputs on stack:
  - 1 SigR
  - 0 SigA (after the delay is passed)
- OP\_CSV doesn't consume the stack for the soft fork backwards compatibility

# The Lightning P2P Network

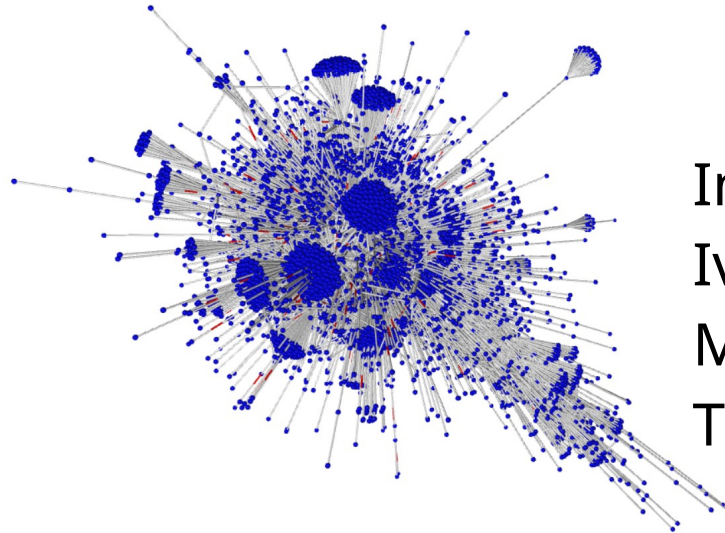


Image from  
Ivan Gallo's  
Master  
Thesis

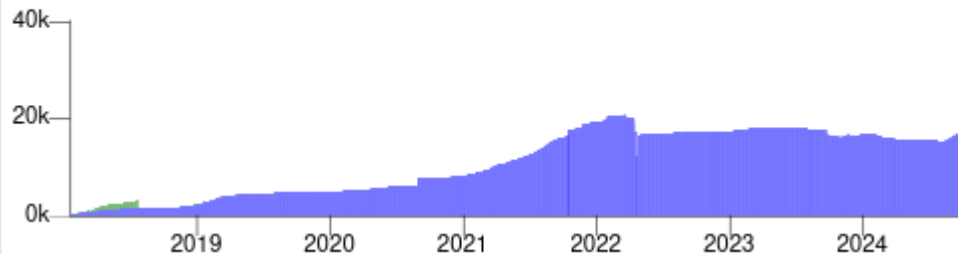
# The Network

- Nodes use **gossiping** to exchange information about the available channels
- Finding a way to send money from A to B is a graph problem: find paths from A to B
  - Easy if you have all the network
  - Some research on doing it with **privacy about existing channels**
- Not very big, but appears to have grown fast
  - +1212% in 2021-2023 (source: **river.com**)

# Some Stats

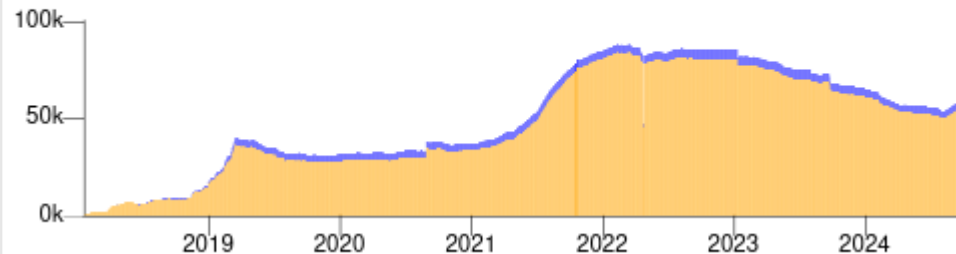
## Nodes

Number of nodes with and without channels.



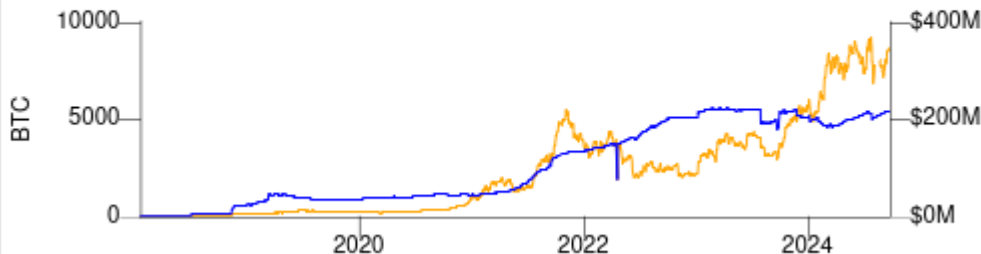
## Channels

Unique = channels connecting nodes directly for the first time. Duplicate = channels between nodes that are already connected.



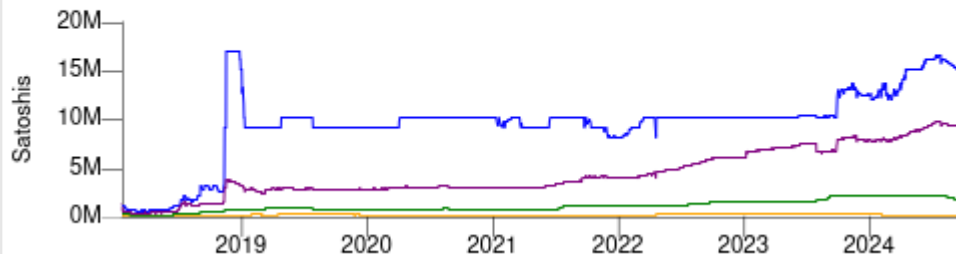
## Network Capacity

Cumulative bitcoin capacity across all channels.



## Capacity Per Channel

Channel capacity statistics.



Source: **Bitcoin Visuals**

# Cross-Chain Swaps

# The Tragedy of Centralized Exchanges

Mt. Gox

🌐 11 languages ▾

Article Talk

From Wikipedia:

**Mt. Gox** was a Bitcoin exchange handling over 70% of all Bitcoin transactions. It ceased operations in early 2011, resulting in the loss of thousands of Bitcoins. In February 2014, it was filed for bankruptcy proceedings.<sup>[1]</sup> The disappearance of the exchange was a major event in the history of cryptocurrency. New evidence has emerged that "most or all of the missing Bitcoins were cryptocurrency".

## FTX

Article Talk

From Wikipedia, the free encyclopedia

*For other uses, see [FTX \(disambiguation\)](#).*

**FTX Trading Ltd.**, commonly known as **FTX** (short for "Futures Exchange"), is a company that formerly operated a fraud-ridden [cryptocurrency exchange](#) fund.<sup>[6][7]</sup> The exchange was founded in 2019 by [Sam Bankman-Fried](#). At its peak in July 2021, the company had over one million users and was the largest cryptocurrency exchange by volume.<sup>[8][9]</sup> FTX is incorporated in [Antigua and Barbuda](#) and headquartered in [the Bahamas](#).<sup>[10]</sup> FTX is closely associated with [Fidelity Investments](#) and is not available to US residents.<sup>[11]</sup>

Since November 11, 2022, FTX has been in [Chapter 11 bankruptcy](#) protection system.<sup>[12][13][14][15]</sup> Public concern began with rumors of unethical company transfers of client funds. In November 2022 [CoinDesk](#) also reported that FTX's partner firm [Alameda Research](#) held a significant portion

🌐 20 languages ▾

## Crypto giant Binance admits to money laundering and agrees to pay \$4.3bn

**CEO Changpeng Zhao will resign and pay a \$50m individual fine as part of a plea deal with the US Justice Department**





# Trustless Cross-Chain Trading

- Requirement:
  - A sends X COIN1 to B
  - B sends Y COIN2 to A
- A and B agree on the exchange rate
  - But don't trust each other!
- Idea: use payment channels for this!

# Back to HTLCs

HTLC:

Bob with preimage of H

OR

Alice at 17:00

H

Alice

H

Bob

HTLC:

Carol with

preimage of H

OR

Bob at 16:00

Carol

H, R

This works even if the two channels are on **different blockchains**!

# Cross-Chain Swaps

HTLC sending 3 COIN1:  
Bob with preimage of H  
OR  
Alice at 17:00

Alice

H,R

H

Bob

HTLC sending 2 COIN2:  
Carol with  
preimage of H  
OR  
Bob at 16:00

Alice

H, R

Here, Alice is exchanging 3 COIN1 for 2 COIN2 with Bob

