

Exercises. Lesson 3

Effects of noise in analog communications

Problem 3.1

A transmitter can perform either DSB or AM modulations. The post-detection signal-to-noise ratio has to be at least $20dB$ in order to meet the required quality specifications.

When DSB modulation is used, we get a maximum range of $15km$ with a transmission power of $1W$. The link attenuation (in dB) is proportional to the distance between transmitter and receiver.

Answer:

- Calculate the power of the signal at the output on the transmitter when DSB modulation is used, and the desired range is $20km$.
- Repeat a. when AM at 80% is used.
- Calculate the envelope peak power values at the output of the transmitter under the conditions mentioned in a. and b., respectively.

DATA:

- $\frac{N_0}{2} = 2 \cdot 10^{-9} W/Hz$
- $W_x = 2\pi \cdot 5krad/s$
- $|x(t)|_{max} = 1V$
- $S_x = 0.5W$
- $\alpha_t[dB] = A \cdot d[km]$, with A a constant.

RESULT:

- $S_{T_{DBL}} = 7.96W$
- $S_{T_{AM}} = 32.69W$
- $PEP_{DBL} = 15.92W$, $PEP_{AM} = 80.25W$

Problem 3.2

A normalized signal with $5kHz$ bandwidth and average power $0.5W$ is transmitted by an AM system. The transmitter power is $660W$. At the receiver side, located $40km$ away, we get a post-detection signal-to-noise ratio of $33dB$.

We know that the noise power spectral density is $N_0/2 = 5 \cdot 10^{-13} W/Hz$, and that the propagation attenuation is given by $A[dB] = 40 + 20 \cdot \log(d[km])$. Answer:

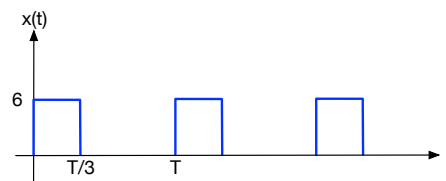
- Calculate the modulation index m .
- Calculate the amount of power needed to transmit the carrier, and the amount of power devoted to the transmission of each sideband.

RESULT:

1. $m = 0.8$
2. $P_p = 500W$, $P_{BL} = 80W$

Problem 3.3

The signal $x(t)$ in the figure goes through a lowpass filter with bandwidth $10kHz$. We assume that the signal power is not affected, and that the DC component is removed.



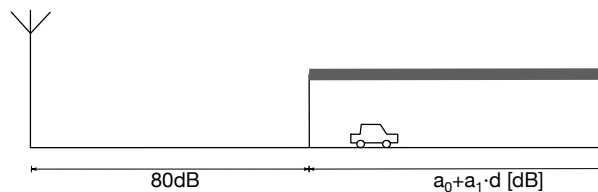
The resulting signal AM modulates a $125V$ carrier, with a modulation index of 0.7484 . This signal is transmitted by a radio station. The transmission channel introduces 80 dB attenuation, and Gaussian white noise whose power spectral density is $N_0/2 = 10^{-11}W/Hz$.

A vehicle is tuned to this radio station, and it enters a tunnel where the propagation attenuation is no longer constant and varies according to:

$$A[dB] = a_0 + a_1 \cdot d$$

where:

- $a_0 = 10dB$
- $a_1 = \frac{1}{3}dB/m$
- d : Distance (m)



- a. Calculate the average power of the modulated signal.
- b. Calculate the demodulation signal-to-noise ratio at the tunnel entrance.
- c. Calculate the distance where the signal will no longer be audible, if the demodulation threshold is $10dB$.
- d. Repeat c. when the demodulator employed is an envelope detector, assuming that the pre-detection threshold is $13dB$.

RESULT:

1. $S_T = 10kW$
2. $\left(\frac{S}{N}\right)_D = 20.38dB$
3. $d = 11.94m$
4. $d' = 2.94m$

Problem 3.4

A communication system is such that the signal arriving at the receiver side has a power $100dB$ below the emitted power at the transmitter side, and that the noise power spectral density is $N_0/2 = 5 \cdot 10^{-15}W/Hz$. A post-detection signal-to-noise ratio of $40dB$ is required for a correct reception.

The maximum voltage value of the message is $2V$, its mean power is $1W$, and its bandwidth, $10kHz$. A pre-detection threshold signal-to-noise ratio of $10dB$ is required. Calculate the minimum transmitted power when using each one of the following modulation systems:

- a. DSB modulation.
- b. AM modulation with $m = 0.5$ and envelope detection.
- c. FM modulation without de-emphasis ($f_d = 10^5 Hz/V$).

RESULT:

1. $S_T = 10kW$
2. $\gamma > \gamma_{th} \Rightarrow S_T = 170kW$
3. $\gamma < \gamma_{th} \Rightarrow S_T = S_{T_{th}} = 420W$

Problem 3.5

We want to transmit a signal with bandwidth $10kHz$ and normalized average power 0.5 , by using an FM communication system. The post-detection signal-to-noise ratio has to be greater than $40dB$, but ensuring a minimum amount of output power consumption. The channel has $120kHz$ bandwidth and introduces white noise with power spectral density $N_0/2 = 0.5 \cdot 10^{-8}W/Hz$. This channel is characterized by an attenuation of $40dB$. Indicate the amount of power needed to transmit the signal.

RESULT:

- $S_T = 416.66W$

Problem 3.6

A radio transmission system uses a frequency modulator (FM) with modulator constant $f_d = 20kHz/V$, and carrier signal $c(t) = 5 \cdot \cos(2\pi \cdot 5 \cdot 10^7 t)$. Answer:

- a. Calculate the modulation index D and the approximate bandwidth when the modulating signal is $x_1(t) = \cos(2\pi \cdot 500t)$.
- b. Repeat a. when the modulating signal is $x_2(t) = \cos(2\pi \cdot 10^4 t)$.

In order to improve the demodulation signal-to-noise ratio, a pre-emphasis and de-emphasis filters are introduced, with cut-off frequency 1430Hz . The system is tested with the modulating signal $x(t) = x_1(t) + x_2(t)$.

- c. Determine the improvement in demodulation signal-to-noise ratio.

RESULT:

1. $D_1 = 40$, $B_T = 41\text{kHz}$
2. $D_2 = 2$, $B_T = 80\text{kHz}$
3. $\Delta \left(\frac{S}{N} \right)_D = 12.14\text{dB}$

Problem 3.7

A signal with bandwidth 5kHz , whose maximum voltage value is $2V$ and with average power $0.5W$ is transmitted using FM through an AWGN channel. The channel has a noise power spectral density of $N_0/2 = 3 \cdot 10^{-14}W/\text{Hz}$. The receiver power is 50nW . The maximum deviation of frequency is 20kHz . Calculate the post-detection signal-to-noise ratio.

RESULT:

- $\left(\frac{S}{N} \right)_D = 30\text{dB}$

Problem 3.8

A signal with bandwidth 10kHz and normalized average power 0.5 is transmitted using FM through an AWGN channel. The channel has a noise power spectral density of $N_0/2 = 5 \cdot 10^{-10}W/\text{Hz}$ and attenuates the signal 40dB . In order to meet the required quality specifications, a threshold γ_{th} of 100 is required for a pre-detection threshold signal-to-noise ratio of 10dB .

- a. Calculate the minimum possible power transmitted to the channel (S_T).
- b. Find the demodulation (post-detection) signal-to-noise ratio.

In order to improve the demodulation signal-to-noise ratio, pre-emphasis and de-emphasis filters are introduced. The 3dB cutoff frequency of the de-emphasis filter, $B_{de} = 1\text{kHz}$.

- c. Determine the improvement in dB of the demodulation (post-detection) signal-to-noise ratio.

RESULT:

1. $S_{T_{min}} = 10\text{dBW}$
2. $\left(\frac{S}{N} \right)_D = 31.3\text{dB}$
3. $\Delta \left(\frac{S}{N} \right)_D = 15.23\text{dB}$