

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones

Year 2021/2022

Exercises. Lesson 6 Bandpass digital transmission

Problem 6.1

Calculate the expected value of the number of error bits during a day for the coherent BPSK receiver described below, under continuous operation. The data rate is 5000bits/s. The input digital signals are $s_1(t) = A \cdot cos(\omega_p t)$ and $s_2(t) = -A \cdot cos(\omega_p t)$, where A = 1mV, and the unilateral noise power spectral density is $N_0 = 10^{-11}W/Hz$.

Problem 6.2

A coherent BPSK system operating continuously produces errors at an average rate of 100 errors per day. The data rate is 1000bits/s. The unilateral noise power spectral density is $N_0 = 10^{-10}W/Hz$. a) b)

Un sistema BPSK coherente que opera continuamente comete errores a razón de 100 errores al día como promedio. La velocidad de los datos es de 1000bits/s. La densidad espectral unilateral de potencia de ruido es $N_0=10^{-10}W/Hz$.

- a. If the system is ergodic, which is the average error probability?
- b. If the average received power is adjusted to 10^{-6} W, would this value be enough to keep the error probability calculated in a)?

x.20220119



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones

Year 2021/2022

Problem 6.3

The signal component of a coherent PSK system is defined by the expression

$$s(t) = A_c k sen(\omega_p t) \pm A_c \sqrt{1 - k^2} cos(\omega_p t)$$

where $0 \le t < T_b$, and the plus sign corresponds to the 1 symbol, and the minus sign corresponds to the 0 one. The first term on the right hand side of the equation represents a carrier component, included to improve the synchronization between transmitter and receiver. Solve this:

- a. Plot the constellation of the signals described; what can be said about this diagram?
- b. Show that, in presence of zero-mean additive white Gaussian noise with power spectral density $N_0/2$, the average error probability is

$$P_e = Q\left(\sqrt{\frac{2E_b}{N_0}(1-k^2)}\right)$$

with
$$E_b = \frac{1}{2}A_c^2T_b$$

- c. Assume that 10% of the transmitted power is located in the carrier component. Determine the value of E_b/N_0 required to obtain an error probability of 10^{-4} .
- d. Compare this E_b/N_0 value with the one required in a conventional PSK system with the same error probability.

Problem 6.4

We want to compare two data transmission bandpass systems. One of them employs 16-PSK, the other, 16-QAM. Both systems have to provide an average symbol error probability of 10^{-3} . Compare the signal-to-noise requirements of said systems.



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

Problem 6.5

If the performance criterion of a system is the bit error probability, which one of the following modulation schemes would be chosen to operate in an AWGN channel? Show the calculations.

- a. Coherent binary orthogonal FSK with $E_b/N_0=13dB. \label{eq:bolden}$
- b. Coherent binary PSK with $E_b/N_0=8dB. \label{eq:bound}$



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

RESULTS FOR PROBLEM 5
2338 bits



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

RESULTS FOR PROBLEM 6

- 1. $1.16 \cdot 10^{-6}$
- 2. No

v.20220119



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

RESULTS FOR PROBLEM 7

- 1. PSK constellation
- 2. Demonstration
- 3. $\frac{E_b}{N_0} = 8.02$
- 4. $\frac{E_b}{N_0} = 7.22$



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

RESULTS FOR PROBLEM 8

$$\Delta\left(\frac{E_s}{N_0}\right) = 3.68dB$$

v.20220119



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2021/2022

RESULTS FOR PROBLEM 9

Coherent binary orthogonal FSK

v.20220119