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Dpto. de Teoría de la Señal y Comunicaciones Year 2020/2021

# Exercises. Lesson 2 Analog modulations

### Problem 2.1

A zero-mean periodic signal x(t), with bandwidth 5kHz, amplitude 4V and normalized average power 0.5, DSB modulates a 1MHz carrier. The result is a signal with average power 400W. Determine:

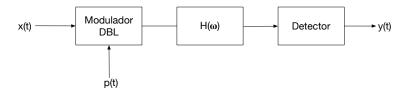
- a. Carrier amplitude.
- b. Average power of the lower sideband.
- c. Outline of the detector needed to recover the signal x(t), and the value of its main parameters

### RESULT:

- 1.  $A_c = 10V$
- 2.  $P_{LSB} = 200W$
- 3. Synchronous detector  $f_{LO} = 1MHz$ ,  $A_{LO} = \frac{2}{A_c}$  and  $f_{lp} = 5kHz$ .

# Problem 2.2

The signal  $x(t) = cos(2\pi \cdot 10 \cdot 10^3 t) + 4 \cdot cos(2\pi \cdot 15 \cdot 10^3 t) + cos(2\pi \cdot 20 \cdot 10^3 t)$  DSB modulates the carrier  $p(t) = 2 \cdot cos(2\pi \cdot 10^5 t)$  and passes through a filter with frequency response  $H(\omega)$  before reaching the detector, as it can be observed in the figure



with

$$H(\omega) = \left\{ \begin{array}{ll} 0 & |\omega| < 200\pi krad/s \\ 1 & |\omega| \geq 200\pi krad/s \end{array} \right.$$

- a. Find the signal obtained at the output of the detector, when using an envelope detector of  $K_D = 1$  with DC suppression.
- b. b) Determine the detector needed to obtain a detected signal equal to the modulating signal. Please specify all necessary parameters.

### RESULT:

- 1.  $y(t) = 2 \cdot \cos(2\pi \cdot 5 \cdot 10^3 t)$
- 2. Synchronous detector with  $f_{LO} = 2 \cdot cos(\omega_c \cdot t)$  and a low pass filter with cut-off frequency of at least 20kHz.

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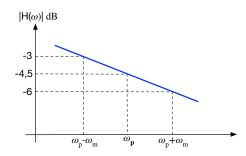
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# Problem 2.3

A transmitter has an average nominal power of 30W and a peak envelope power of 60W. Determine:

- a. The power in a sideband when the signal  $x(t) = cos(\omega_m t)$  modulates the carrier given by  $p(t) = A_p$ .  $cos(\omega_p t)$ , and the value of  $A_p$  in the following cases:
  - (a) AM modulation when the modulation index is 80%.
  - (b) DSB modulation
- b. Considering the first case for a), and knowing that the channel presents a non-uniform attenuation as depicted in the figure: Obtain the signal detected in the following cases:



- (a) Envelope detector
- (b) Synchornous detector

Note: Assume in both cases that a DC suppressor is present.

RESULT:

1. (a) 
$$A_p = 6.08V, P_{BL} = 2.96W$$

(b) 
$$A_p = 10.95V, P_{BL} = 15W$$

2. (a) 
$$y_D(t) = k_D \cdot [A(t) - \langle A(t) \rangle]$$
, con:

• 
$$A(t) = x_i(t) \cdot \left[ 1 + 0.5 \cdot \left( \frac{x_q(t)}{x_i(t)} \right)^2 \right]$$
  
•  $x_i(t) = 0.6 \cdot A_p + 0.48 \cdot A_p \cdot \cos(\omega_m t)$ 

• 
$$x_i(t) = 0.6 \cdot A_p + 0.48 \cdot A_p \cdot \cos(\omega_m t)$$

• 
$$x_q(t) = -0.08 \cdot A_p \cdot sen(\omega_m t)$$

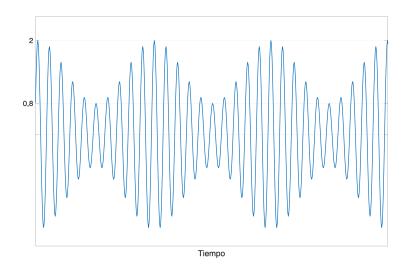
(b) 
$$y_D(t) = \frac{A_{OL}}{2} \cdot A_p \cdot 0.48 \cdot \cos(\omega_m t)$$

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# Problem 2.4

A 10kHz signal x(t) modulates a 100kHz carrier and the result, as observed using an oscilloscope, is presented in the figure. Determine:



- a. Modulation used.
- b. Modulation index.
- c. Carrier's power and Modulating signal's normalized power. Recovered signal when using a synchronous detector tuned to 100kHz and with an amplitude of 1V.
- d. Recovered signal when using an envelope detector.

Note: It can be assumed that  $K_D = 1$ .

Result:

- 1. AM
- $2. m \approx 0.43$
- 3.  $P_p = 0.98W, S_{xn} = 0.5$
- 4.  $y_D(t) = 0.3 \cdot \cos(2\pi \cdot 10^4 t)$
- 5.  $y_D(t) = 0.6 \cdot \cos(2\pi \cdot 10^4 t)$

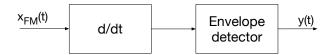
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## Problem 2.5

Considering that  $x_{FM}(t)$  is the signal obtained when FM modulating a signal x(t) with the carrier  $p(t) = A_p \cdot cos(\omega_p t)$ . Determine the condition needed to recover the signal x(t) if the system outlined in the figure is used.



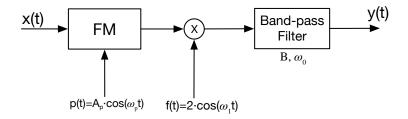
RESULT:

$$\omega_p - \omega_\Delta \cdot |x(t)|_{max} > 0$$

# Problem 2.6

The outline presented in the figure shows a FM modulator followed by a frequency converter and a band-pass filter (used to adapt the modulated signal to a suitable transmission frequency band). In order to set the system's parameters, a test tone x(t) is used. Determine:

- a. Modulation index D, and modulated signal's bandwidth.
- b. Value of the filter's bandwidth, B, and the filter's central frequency,  $\omega_0$ , considering that a frequency band that is above  $\omega_1$  has been assigned for our transmission.
- c. Average power of the output y(t) as a function of  $A_p$  considering that the filter attenuates the signal a 10%.



DATA:

• 
$$x(t) = cos(\omega_m t) [V]$$

• 
$$\omega_m = 2\pi \cdot 4krad/s$$

• 
$$\omega_p = 2\pi \cdot 400 krad/s$$

• 
$$\omega_1 = 2\pi \cdot 2Mrad/s$$

• 
$$\omega_d = 2\pi \cdot 16krad/s \cdot V$$

RESULT:

1. 
$$D = 4$$
,  $B_T = 2\pi \cdot 48krad/s$ 

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