

Dpto. de Teoría de la Señal y Comunicaciones

Lesson 3 Effects of noise in analog communications

1 Key concepts

Before doing these exercises it is important to review and understand the following concepts:

- General diagram of an analog communication system with noise.
- Concept of signal to noise ratio. Difference between pre-detection and post-detection.
- Concept of threshold effect, and when it is necessary to take it into account.

2 Basic problems

This first part includes problems mostly extracted from the bibliography aimed at practicing basic calculations needed for the rest of the lesson.

Problem 3.1

[Carlson2010] A DSB signal plus noise is demodulated by synchronous detection. Find $(S/N)_D$ in dB given that the received power is 20nW, the message has a bandwidth of 5MHz and the channel introduces a noise with $N_0 = 4 \cdot 10^{-20}$ W/Hz.

RESULTS FOR PROBLEM

 $\left(\frac{S}{N}\right)_D = 50 \text{ dB}$

Problem 3.2

[Carlson2010] A DSB signal plus noise is demodulated by a product detector with phase error ϕ . Take the local oscillator signal to be $2\cos(\omega_c t + \phi)$ and show that $(S/N)_D = \gamma \cos^2(\phi)$.

RESULTS FOR PROBLEM

Problem 3.3

[Carlson2010] An AM system with envelope detection is operating at the threshold point. Find the power gain in dB needed at the transmitter to get up the $(S/N)_D$ to 40dB with full-load tone modulation.

RESULTS FOR PROBLEM

G = 32dB

Problem 3.4

[Carlson2010] An FM signal plus noise has a received power of 1nW, $S_x=0.1$, $|x(t)|_{max}=4$ V, $\omega_d=500$ kHz/V and $N_0=4\cdot10^{-20}$. Find $(S/N)_D$ in dB for FM detection and for deemphasized FM detection with $B_{de}=5$ kHz.

RESULTS FOR PROBLEM

x20230118 **1**



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2022/2023

- FM: $(S/N)_D = 53.8dB$
- deemphasized FM: $(S/N)_D = 89dB$

Problem 3.5

[Carlson2010] An analog communication system has $S_x = 1/2$, $W_x = 10 \text{kHz}$, $N_0 = 10^{-15} \text{W/Hz}$, and transmission loss 100dB. Calculate the transmitted power needed to get $(S/N)_D = 40 \text{dB}$ when the modulation is:

- a) AM with m=1
- b) AM with M = 0.5
- c) FM with D=1
- d) FM with D=5
- e) FM with D = 10

RESULTS FOR PROBLEM

- a) $P_T = 3kW$
- b) $P_T = 9kW$
- c) $P_T = 667 \text{W}$
- d) $P_T = 26.7W$
- e) $P_T = 24W$

v.20230118 **2**

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones

3 Aditional problems

These problems are slightly more ellaborated than the previous ones, in many cases extracted from old exams.

Problem 3.6

A transmitter can perform either DSB or AM modulations. The post-detection signal-to-noise ratio has to be at least 20dB in order to meet the required quality specifications.

When DSB modulation is used, we get a maximum range of 15km with a transmission power of 1W. The link attenuation (in dB) is proportional to the distance between transmitter and receiver. Answer:

- a) Calculate the power of the signal at the output on the transmitter when DSB modulation is used, and the desired range is 20km.
- b) Repeat a. when AM at 80% is used.
- c) Calculate the envelope peak power values at the output of the transmitter under the conditions mentioned in a. and b., respectively.

DATA:

•
$$\frac{N_0}{2} = 2 \cdot 10^{-9} W/Hz$$

•
$$W_x = 2\pi \cdot 5krad/s$$

•
$$|x(t)|_{max} = 1V$$

•
$$S_x = 0.5W$$

• $\alpha_t[dB] = A \cdot d[km]$, with A a constant.

RESULTS FOR PROBLEM

a)
$$S_{T_{DBL}} = 7.96W$$

b)
$$S_{T_{AM}} = 32.69W$$

c) $PEP_{DBL} = 15.92W$, $PEP_{AM} = 80.25W$

v.20230118



Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2022/2023

Problem 3.7

A normalized signal with 5kHz bandwidth and average power 0.5W is transmitted by an AM system. The transmitter power is 660W. At the receiver side, located 40km away, we get a post-detection signal-to-noise ratio of 33dB.

We know that the noise power spectral density is $N_0/2 = 5 \cdot 10^{-13} W/Hz$, and that the propagation attenation is given by $A[dB] = 40 + 20 \cdot log(d[km])$. Answer:

- a) Calculate the modulation index m.
- b) Calculate the amount of power needed to transmit the carrier, and the amount of power devoted to the transmission of each sideband.

RESULTS FOR PROBLEM

- a) m = 0.8
- b) $P_p = 500W, P_{BL} = 80W$

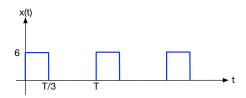
v.20230118 4

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2022/2023

Problem 3.8

The signal x(t) in the figure goes through a lowpass filter with bandwidth 10kHz. We assume that the signal power is not affected, and that the DC component is removed.



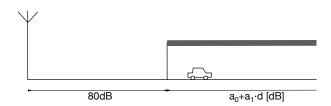
The resulting signal AM modulates a 125V carrier, with a modulation index of 0.7484. This signal is transmitted by a radio station. The transmission channel introduces 80 dB attenuation, and Gaussian white noise whose power spectral density is $N_0/2 = 10^{-11}W/Hz$.

A vehicle is tuned to this radio station, and it enters a tunnel where the propagation attenuation is no longer constant and varies according to:

$$A[dB] = a_0 + a_1 \cdot d$$

where:

- $a_0 = 10dB$
- $a_1 = \frac{1}{3}dB/m$
- d: Distance (m)



- a) Calculate the average power of the modulated signal.
- b) Calculate the demodulation signal-to-noise ratio at the tunnel entrance.
- c) Calculate the distance where the signal will no longer be audible, if the demodulation threshold is 10dB.
- d) Repeat c. when the demodulator employed is an envelope detector, assuming that the pre-detection threshold is 13dB.

RESULTS FOR PROBLEM

a)
$$S_T = 10kW$$

b)
$$\left(\frac{S}{N}\right)_D = 20.38dB$$

c) d = 11.94m

d) d' = 2.94m

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2022/2023

Problem 3.9

A communication system is such that the signal arriving at the receiver side has a power 100dB below the emitted power at the transmitter side, and that the noise power spectral density is $N_0/2 = 5 \cdot 10^{-15} W/Hz$. A post-detection signal-to-noise ratio of 40dB is required for a correct reception.

The maximum voltage value of the message is 2V, its mean power is 1W, and its bandwidth, 10kHz. A predetection threshold signal-to-noise ratio of 10dB is required. Calculate the minimum transmitted power when using each one of the following modulation systems:

- a) DSB modulation.
- b) AM modulation with m = 0.5 and envelope detection.
- c) FM modulation without de-emphasis ($f_d = 10^5 Hz/V$).

RESULTS FOR PROBLEM

- a) $S_T = 10kW$
- b) $\gamma > \gamma_{th} \Rightarrow S_T = 170kW$
- c) $\gamma < \gamma_{th} \Rightarrow S_T = S_{T_{th}} = 420W$

Problem 3.10

We want to transmit a signal with bandwidth 10kHz and normalized average power 0.5, by using an FM communication system. The post-detection signal-to-noise ratio has to be greater than 40dB, but ensuring a minimum amount of output power consumption. The channel has 120kHz bandwidth and introduces white noise with power spectral density $N_0/2 = 0.5 \cdot 10^{-8}W/Hz$. This channel is characterized by an attenuation of 40dB. Indicate the amount of power needed to trasmit the signal.

RESULTS FOR PROBLEM

• $S_T = 416.66W$

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones Year 2022/2023

Problem 3.11

A radio transmission system uses a frequency modulator (FM) with modulator constant $f_d = 20kHz/V$, and carrier signal $c(t) = 5 \cdot cos(2\pi \cdot 5 \cdot 10^7 t)$. Answer:

- a) Calculate the modulation index D and the approximate bandwidth when the modulating signal is $x_1(t) = cos(2\pi \cdot 500t)$.
- b) Repeat a. when the modulating signal is $x_2(t) = cos(2\pi \cdot 10^4 t)$.

In order to improve the demodulation signal-to-noise ratio, a pre-emphasis and de-emphasis filters are introduced, with cut-off frequency 1430Hz. The system is tested with the modulating signal $x(t) = x_1(t) + x_2(t)$.

c) Determine the improvement in demodulation signal-to-noise ratio.

RESULTS FOR PROBLEM

- a) $D_1 = 40, B_T = 41kHz$
- b) $D_2 = 2$, $B_T = 80kHz$
- c) $\Delta \left(\frac{S}{N}\right)_D = 12.14dB$

Problem 3.12

A signal with bandwidth 5kHz, whose maximum voltage value is 2V and with average power 0.5W is transmitted using FM through an AWGN channel. The channel has a noise power spectral density of $N_0/2 = 3 \cdot 10^{-14} W/Hz$. The receiver power is 50nW. The maximum deviation of frequency is 20kHz. Calculate the post-detection signal-to-noise ratio.

RESULTS FOR PROBLEM

•
$$\left(\frac{S}{N}\right)_D = 30dB$$

v.20230118

Grados TIC

Dpto. de Teoría de la Señal y Comunicaciones

Problem 3.13

A signal with bandwidth 10kHz and normalized average power 0.5 is transmitted using FM through an AWGN channel. The channel has a noise power spectral density of $N_0/2 = 5 \cdot 10^{-10} W/Hz$ and attenuates the signal 40dB. In order to meet the required quality specifications, a threshold γ_{th} of 100 is required for a pre-detection threshold signal-to-noise ratio of 10dB.

- a) Calculate the minimum possible power transmitted to the channel (S_T) .
- b) Find the demodulation (post-detection) signal-to-noise ratio.

In order to improve the demodulation signal-to-noise ratio, pre-emphasis and de-emphasis filters are introduced. The 3dB cutoff frequency of the de-emphasis filter, $B_{de} = 1kHz$.

c) Determine the improvement in dB of the demodulation (post-detection) signal-to-noise ratio.

RESULTS FOR PROBLEM

- a) $S_{T_{min}} = 10dBW$
- b) $\left(\frac{S}{N}\right)_D = 31.3dB$
- c) $\Delta \left(\frac{S}{N}\right)_D = 15.23dB$

References

[Carlson2010] A. Bruce Carlson and Paul B. Crilly. Communication Systems: An Introduction to Signals and Noise in Electrical Communication, 5th Ed. McGraw-Hill, 2010.

v.20230118