

Tarea 07 - El Lenguaje LETREC

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Especificación del Lenguaje.

Sintáxis Concreta

```
Program      := Expression

Expression   := Number
                | -(Expression Expression)
                | zero? (Expression)
                | if Expression then Expression else Expression
                | Identifier
                | let Identifier = Expression in Expression
                | proc (Identifier) Expression
                  (Expression Expression)
                | letrec Identifier(Identifier) = Expression in Expression

Digit        := 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

Number       := Digit
                | DigitNumber
                | Digit.Digit{Digit}*

Alphabetic   = [a-zA-Z]

Identifier    := AlphabeticIdentifier
                | Identifier{Digit}*
```

Sintaxis Abstracta (Notación de Racket)

Program:

- (a-program exp_1)

Expression:

- (const-exp num)
- (diff-exp exp_1 exp_2)
- (zero?-exp exp_1)
- (if-exp exp_1 exp_2 exp_3)
- (var-exp var)
- (let-exp var exp_1 body)
- (proc-exp var body)
- (call-exp rator rand)
- (letrec-exp p-name b-var p-body letrec-body)

Number: Real

Identifier: Versión limitada de Symbol

Semántica

$\text{value-of } (\text{const-exp } n) \ \rho = (\text{num-val } n)$

$(\text{value-of } (\text{var-exp } var) \ \rho) = \rho(var)$

$(\text{value-of } (\text{diff-exp } exp_1 \ exp_2) \ \rho) =$
 $(\text{num-val } (- (\text{expval} \rightarrow \text{num } (\text{value-of } exp_1 \ \rho))$
 $\quad (\text{expval} \rightarrow \text{num } (\text{value-of } exp_2 \ \rho))))$

$(\text{value-of } (\text{zero?-exp } exp_1) \ \rho) =$
 $(\text{let } ([val_1 (\text{value-of } exp_1 \ \rho)])$
 $\quad (\text{bool-val } (= 0 (\text{expval} \rightarrow \text{num } val_1))))$

$(\text{value-of } (\text{if-exp } exp_1 \ exp_2 \ exp_3) \ \rho) =$
 $(\text{if } (\text{expval} \rightarrow \text{bool } (\text{value-of } exp_1 \ \rho))$
 $\quad (\text{value-of } exp_2 \ \rho)$
 $\quad (\text{value-of } exp_3 \ \rho))$

$(\text{value-of } (\text{let-exp } var \ exp_1 \ body) \ \rho) =$
 $(\text{let } ([val_1 (\text{value-of } exp_1 \ \rho)])$
 $\quad (\text{value-of } body \ [var = val_1] \rho))$

$(\text{value-of } (\text{proc-exp } var \ body) \ \rho) =$
 $(\text{proc-val } (\text{procedure } var \ body \ \rho))$

$$\begin{aligned}
&(\text{value-of } (\text{call-exp op-exp arg-exp}) \rho) = \\
&(\text{let } ([\text{proc } (\text{expval} \rightarrow \text{proc } (\text{value-of op-exp } \rho))] \\
&\quad [\text{arg } (\text{value-of arg-exp } \rho)]]) \\
&\quad (\text{apply-procedure proc arg}))
\end{aligned}$$

donde:

$$\begin{aligned}
&(\text{apply-procedure } (\text{procedure } \text{var } \text{body } \rho) \text{ val}) = \\
&(\text{value-of } \text{body } [\text{var} = \text{val}] \rho)
\end{aligned}$$

$$\begin{aligned}
&(\text{value-of } (\text{letrec-exp p-name b-var p-body letrec-body}) \rho) = \\
&(\text{value-of } \text{letrec-body } [\text{p-name} = \text{b-var} \mapsto \text{p-body}] \rho)
\end{aligned}$$

donde:

Si $\rho_1 = [\text{p-name} = \text{b-var} \mapsto \text{p-body}] \rho$, entonces:

si $\text{var} = \text{p-name}$

$$(\text{apply-env } \rho_1 \text{ var}) =$$

$$(\text{proc-val } (\text{procedure } \text{b-var } \text{p-body } \rho_1))$$

si $\text{var} \neq \text{p-name}$.

$$(\text{apply-env } \rho_1 \text{ var}) = (\text{apply-env } \rho \text{ var})$$