Modelling Handedness as a Function of Cooperation and Competition Or: How I Learned to Bow Down to My Left-Handed Overlords

Meridith Bartley John Ensley

Department of Statistics The Pennsylvania State University

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Outline

Introduction
History of Handedness

Building the Model

Comparing Model to Baseball Data



History of Handedness

- ▶ 10% of population is left-handed.
- Why hasn't this percentage reached equilibrium in populations at either:
 - ► 50%-50% between left and right-handedness
 - ▶ 100% either left or right handed
 - Some other handedness ratio
- This paper proposes that hand preference may be influenced by costs and benefits of cooperation and competition during human evolution.



Building the Model

▶ We want to model *I*, the proportion of lefties, over time.

$$\frac{dI}{dt} = (1 - I)P_{RL}(I) - IP_{LR}(I)$$

Assume P_{RL} and P_{LR} are symmetric.

$$\frac{dI}{dt} = (1 - I)P_{RL}(I) - IP_{RL}(1 - I) \tag{1}$$

▶ Break $P_{RL}(I)$ into increasing and decreasing components.

$$P_{RL}(I) = cP_{RL}^{\text{coop}}(I) + (1 - c)P_{RL}^{\text{comp}}(I)$$
 (2)



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Video



Using Athletics Data

Ideally

Want to compare predicted equilibria of eq (1) to animal population data where cooperation is present.

 Quantification of cooperation and available data very depending on task

Proxy Situation

Within atheletics, data on handedness and cooperation are readily available.

Baseball Rank Equation

$$I_r = \frac{1}{2} \frac{I_{bg} N \operatorname{erfc}(\hat{s}_r - \Delta \hat{s})}{r}$$

Visualizations

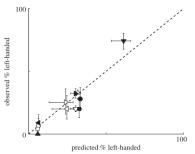
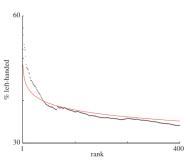


Figure: Lefty proportion as a function of rank in baseball, predicted and observed

Figure: Predicted vs observed lefty proportions for various sports





Summary

- Sports data may not be analogous to natural world data; further quantitative analysis with social animal groups vital for future research.
- Analysis of athletics provides new insights into evolutionary origins of handedness.
- ► This model may be applied to any species of animal and may also be used in understanding other physical and/or behavioral lateralized adaptations.



— Appendix

For Further Reading

For Further Reading I



Abrams, Daniel M. and Panaggio, Mark J.

A model balancing cooperation and competition can explain our right-handed world and the dominance of left-handed athletes

Journal of The Royal Society Interface, 2012.

