

# Priority Note – Extended ICP Version

*Canister Field Mathematics – Foundational Definition, Priority Claim, and ICP Substrate*

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Title: Canister Field Mathematics – Foundational Definition, Priority Claim, and ICP Substrate

Context

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Abstract:

This document establishes the foundational definition, authorship priority, and computational substrate context of the concept known as Canister Field Mathematics. This formalism defines distributed computation as a field of interacting canisters, each acting as a discrete computational cell with deterministic or probabilistic state transitions. The Internet Computer Protocol (ICP) provides the first globally available execution environment capable of hosting large-scale, stateful, autonomous canister fields with deterministic message passing, unbounded horizontal scaling, and cryptographic timestamping.

## 1. Definition of a Canister Field

A Canister Field is defined as a tuple  $F = (C, N, S, f)$ , where:

- $C$  is a countable set of canisters deployed on a distributed substrate such as ICP.
- $N: C \rightarrow P(C)$  defines a neighborhood function assigning to each canister a finite interaction set based on topology or routing rules.
- $S$  is the state space for individual canisters, stored persistently within ICP's replicated state machine.
- $f: S \times S^{|N(c)|} \rightarrow S$  is a transition function executed as canister update calls or heartbeat cycles.

## 2. ICP as the Native Substrate

The Internet Computer Protocol is uniquely suited to implement Canister Field Mathematics because:

- Canisters maintain persistent state independent of servers.
- Deterministic message execution ensures reproducible field evolution.
- Subnet scaling expands computational surface area linearly or superlinearly.

- The ICP consensus layer provides global cryptographic time-ordering of field updates.
- Canisters can autonomously trigger state transitions via timers, forming continuous-time fields.

### 3. Fundamental Axiom

Each canister  $c \in C$  updates its state  $s(t+1)$  via:

$$s_c(t+1) = f(s_c(t), \{ s_n(t) \mid n \in N(c) \})$$

implemented via deterministic ICP update calls or certified query patterns.

### 4. Priority Claim

This document establishes Enter Yourname as the originator of the following concepts:

- Canister Field Mathematics
- Canister Field Processor (CFP) Architecture
- Distributed quasi-neural activation models built on ICP canister meshes
- Field-theoretic compute substrates using ICP subnets as computational manifolds

### 5. Hash Placeholder:

(To be replaced with SHA-256 after deposition)

This note is intended for archival on decentralized ledgers (ICP, ETH, etc.) and for upload to public research repositories as permanent prior art.