



Supervised vs Unsupervised

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Unsupervised Learning

Data: x
Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

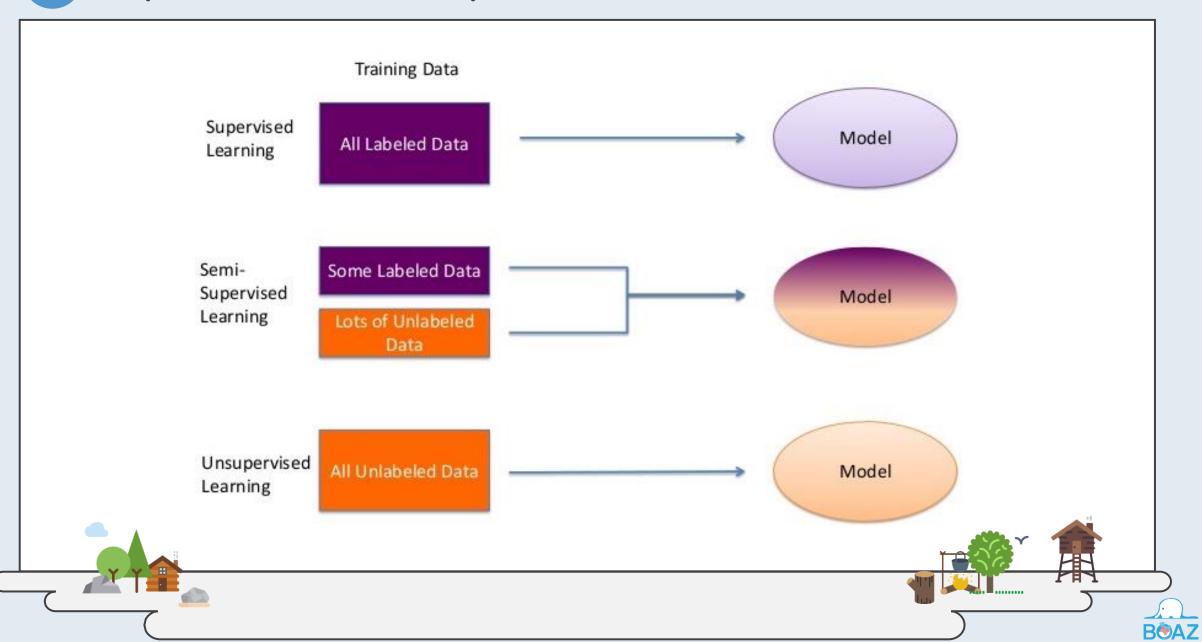
Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.







Supervised vs Unsupervised

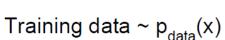


Generative Models

Generative Models

Given training data, generate new samples from same distribution







Generated samples $\sim p_{\text{model}}(x)$

Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

Addresses density estimation, a core problem in unsupervised learning **Several flavors**:

- Explicit density estimation: explicitly define and solve for p_{model}(x)
- Implicit density estimation: learn model that can sample from $p_{model}(x)$ w/o explicitly defining it







Generative Models

Why Generative Models?

Realistic samples for artwork, super-resolution, colorization, etc.







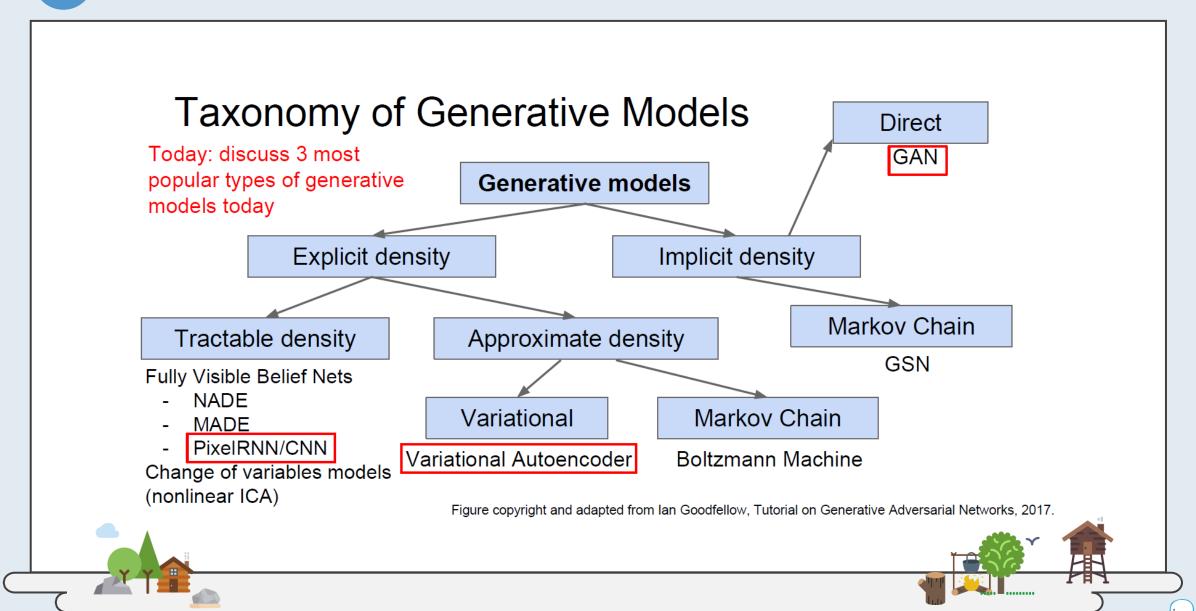
- Generative models of time-series data can be used for simulation and planning (reinforcement learning applications!)
- Training generative models can also enable inference of latent representations that can be useful as general features







Generative Models



Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i|x_1,...,x_{i-1})$$
 \tag{Will need to define ordering of "previous pixels} \text{pixels"}

Then maximize likelihood of training data

Complex distribution over pixel values => Express using a neural network!



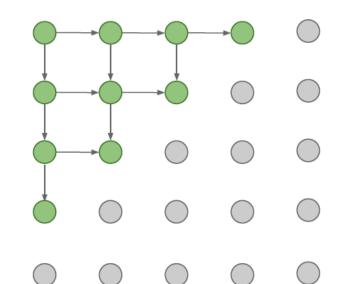


PixeIRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

Drawback: sequential generation is slow!







PixelCNN [van der Oord et al. 2016]

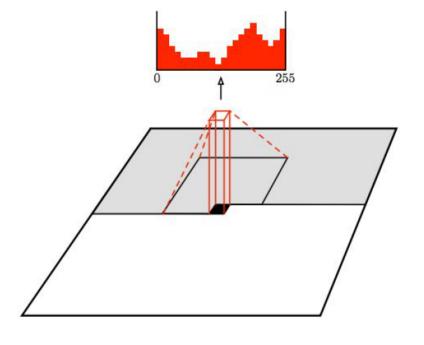
Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^{n} p(x_i|x_1, ..., x_{i-1})$$

Softmax loss at each pixel







PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood p(x)
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

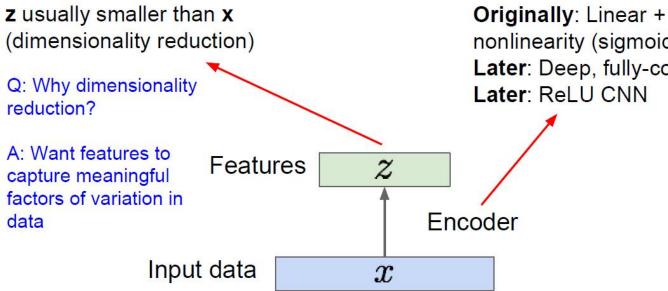
- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

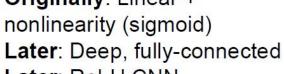




Some background first: Autoencoders

Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data







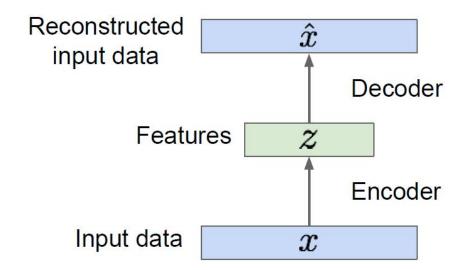


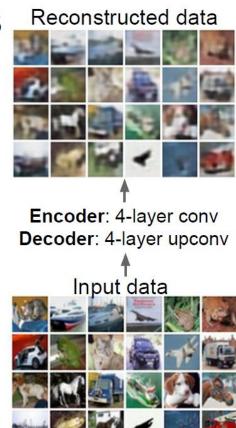


Some background first: Autoencoders

How to learn this feature representation?

Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself

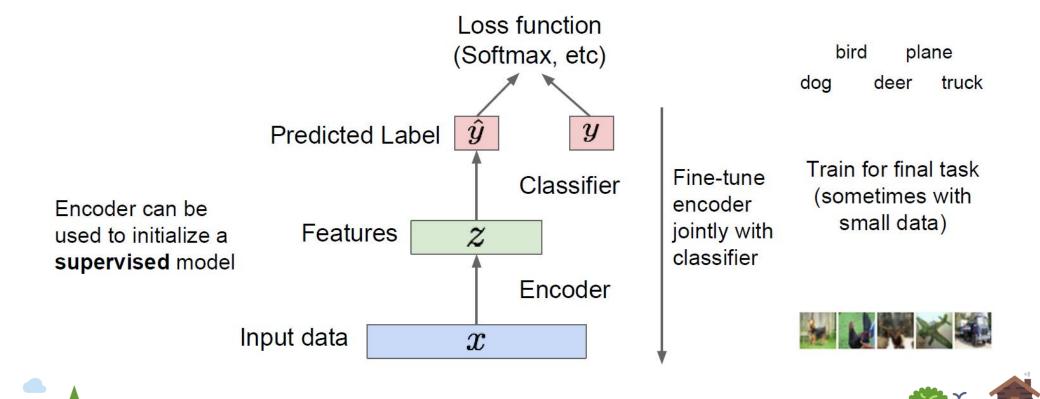








Some background first: Autoencoders



Variational Autoencoders

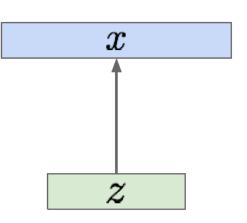
Probabilistic spin on autoencoders - will let us sample from the model to generate data!

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from underlying unobserved (latent) representation **z**

Sample from true conditional

$$p_{\theta^*}(x \mid z^{(i)})$$

Sample from true prior $p_{\theta^*}(z)$



Intuition (remember from autoencoders!):

x is an image, **z** is latent factors used to generate **x**: attributes, orientation, etc.



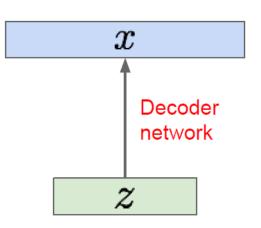


Variational Autoencoders

Sample from true conditional

 $p_{\theta^*}(x \mid z^{(i)})$

Sample from true prior $p_{\theta^*}(z)$



We want to estimate the true parameters θ^* of this generative model.

How should we represent this model?

Choose prior p(z) to be simple, e.g. Gaussian.

Conditional p(x|z) is complex (generates image) => represent with neural network





Variational Autoencoders: Intractability

Data likelihood: $p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$

Posterior density also intractable: $p_{ heta}(z|x) = p_{ heta}(x|z)p_{ heta}(z)/p_{ heta}(x)$

Solution: In addition to decoder network modeling $p_{\theta}(x|z)$, define additional encoder network $q_{\phi}(z|x)$ that approximates $p_{\theta}(z|x)$

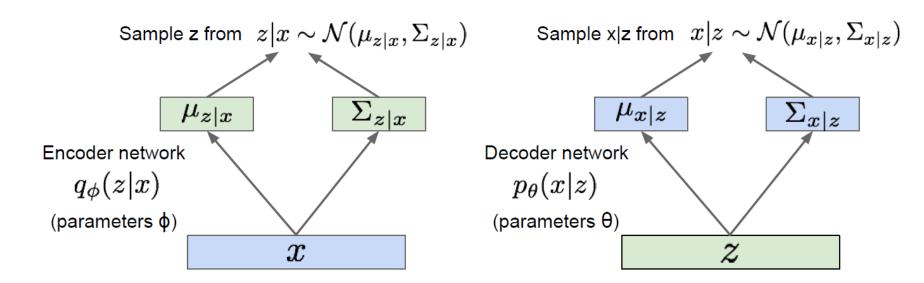
Will see that this allows us to derive a lower bound on the data likelihood that is tractable, which we can optimize





Variational Autoencoders

Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic



Encoder and decoder networks also called "recognition"/"inference" and "generation" networks Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014



Variational Autoencoders

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Bayes' Rule)}$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad \text{(Multiply by constant)}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad \text{(Logarithms)}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))$$

Decoder network gives $p_{\theta}(x|z)$, can compute estimate of this term through sampling. (Sampling differentiable through reparam. trick. see paper.)

This KL term (between Gaussians for encoder and z prior) has nice closed-form solution!

p_θ(z|x) intractable (saw earlier), can't compute this KL term :(But we know KL divergence always >= 0.



Variational Autoencoders

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Bayes' Rule}) \qquad \text{Make approximate}$$

$$\text{Reconstruct}$$

$$\text{the input data} = \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})}\right] \quad (\text{Multiply by constant}) \quad \text{close to prior}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))$$

$$\geq 0$$

$$\log p_{\theta}(x^{(i)}) \geq \mathcal{L}(x^{(i)}, \theta, \phi)$$

$$\theta^{*}, \phi^{*} = \arg \max_{\theta, \phi} \sum_{i=1}^{N} \mathcal{L}(x^{(i)}, \theta, \phi)$$

$$\log p_{\theta}(x^{(i)}) \ge \mathcal{L}(x^{(i)}, \theta, \phi)$$

Variational lower bound ("ELBO")

$$\theta^*, \phi^* = \arg\max_{\theta, \phi} \sum_{i=1}^N \mathcal{L}(x^{(i)}, \theta, \phi)$$

Training: Maximize lower bound



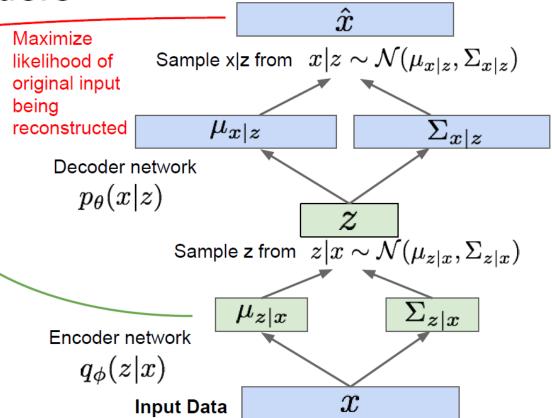
Variational Autoencoders

Putting it all together: maximizing the likelihood lower bound

$$\underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

Make approximate posterior distribution close to prior

For every minibatch of input data: compute this forward pass, and then backprop!





Variational Autoencoders

Probabilistic spin to traditional autoencoders => allows generating data

Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Allows inference of q(z|x), can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

- More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian
- Incorporating structure in latent variables



So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

VAEs define intractable density function with latent **z**:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

What if we give up on explicitly modeling density, and just want ability to sample?

GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game





Generative Adversarial Networks

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

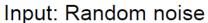
Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

Q: What can we use to represent this complex transformation?

A: A neural network!

Output: Sample from training distribution

> Generator Network



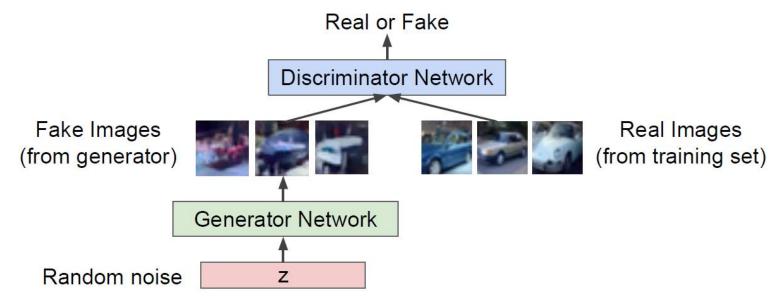




Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images







Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in minimax game

Discriminator outputs likelihood in (0,1) of real image

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
Discriminator output for for real data x
$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

- Discriminator (θ_d) wants to maximize objective such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator (θ_g) wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)



Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

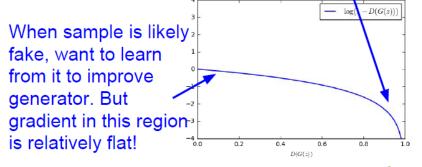
$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

In practice, optimizing this generator objective does not work well!

Gradient signal dominated by region where sample is already good







Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

• Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_q(z)$.

• Sample minibatch of m examples $\{x^{(1)}, \dots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.

• Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

Recent work (e.g. Wasserstein GAN) alleviates this problem, better stability!

Some find k=1

others use k > 1.

more stable,

no best rule.

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for



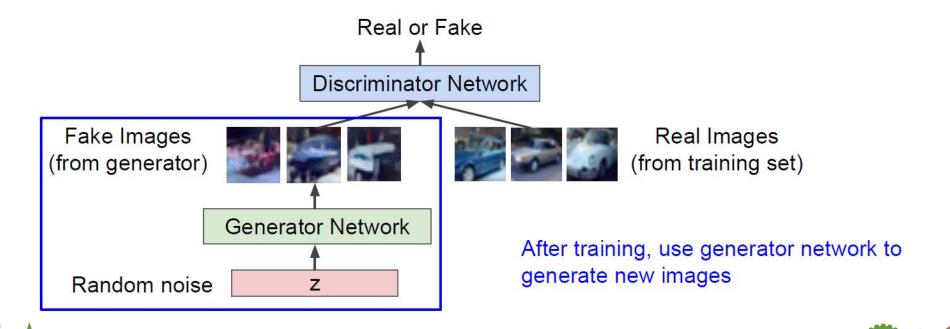




Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

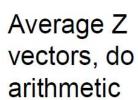




Generative Adversarial Nets: Interpretable Vector Math

rativo / tavorcariai rioto: iritorprotablo voctor iviatir

Samples from the model





Smiling woman





Neutral woman





Neutral man





Radford et al, ICLR 2016







GANs

Don't work with an explicit density function

Take game-theoretic approach: learn to generate from training distribution through 2-player
game

Pros:

Beautiful, state-of-the-art samples!

Cons:

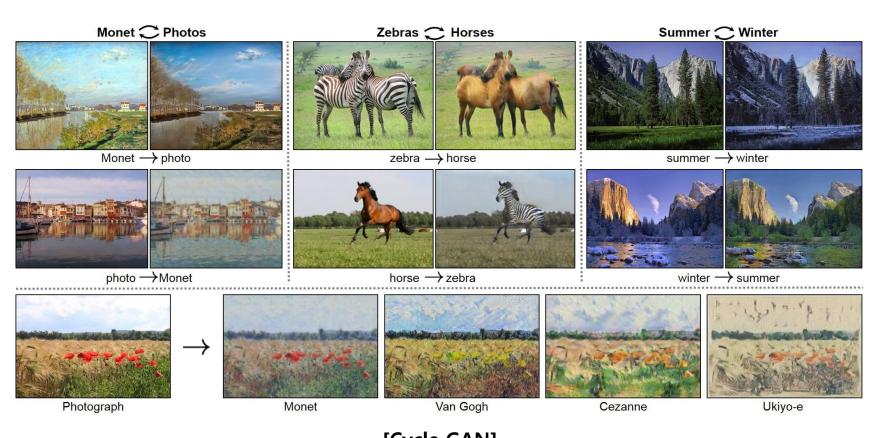
- Trickier / more unstable to train
- Can't solve inference queries such as p(x), p(z|x)

Active areas of research:

- Better loss functions, more stable training (Wasserstein GAN, LSGAN, many others)
- Conditional GANs, GANs for all kinds of applications

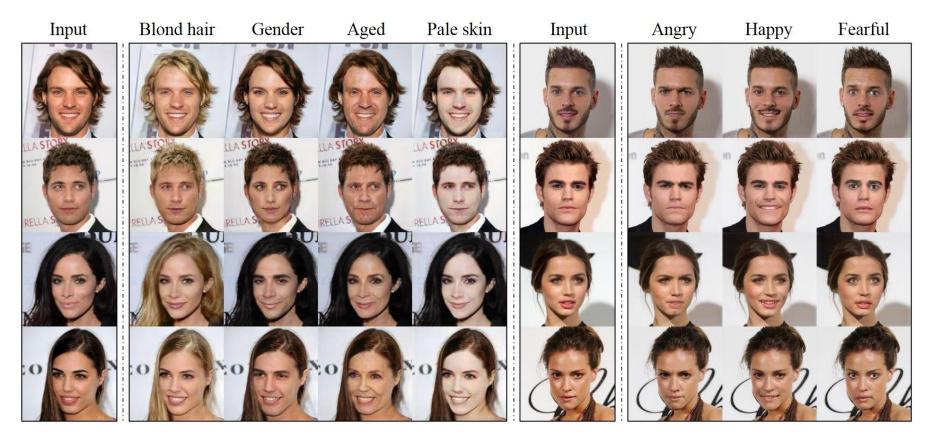












[Star GAN]









[Style GAN]



BOAZ

Recap

Generative Models

- PixeIRNN and PixeICNN Explicit density model, optimizes exact likelihood, good samples. But inefficient sequential generation.
- Variational Autoencoders (VAE) Optimize variational lower bound on likelihood. Useful latent representation, inference queries. But current sample quality not the best.
- Generative Adversarial Networks (GANs) Game-theoretic approach, best samples!

 But can be tricky and unstable to train,
 no inference queries.

Also recent work in combinations of these types of models! E.g. Adversarial Autoencoders (Makhanzi 2015) and PixelVAE (Gulrajani 2016)

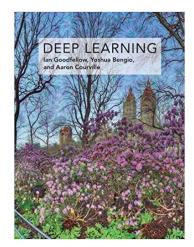


앞으로 공부할 방향

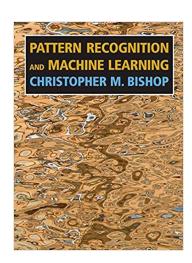
Stanford: 자연어 처리 cs224n (http://cs224n.stanford.edu/)

PR12 : 논문 읽기 모임

(https://www.youtube.com/playlist?list=PLIMkM4tgfjnJhhd4wn5aj8fVTYJwIpWkS)











CS231n: http://cs231n.stanford.edu/syllabus.html



