Exoskeletal microstructure and tensile behavior of the acorn weevil rostrum

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INTRODUCTION

The exoskeleton of Coleoptera (beetles) is a hierarchically-structured fibrous composite characterized or less in revisions, 12 nanofibrils embedded in a heterogeneous protein matrix. Although α-chitin is brittle and strongly anisotropic, argu-ment/near beetle cuticle is simultaneously rigid and tough due to its uniquely layered microstructure. Beetle cuticle is divided into two structurally and mechanically distinct regions, the (outer) exocuticle and (inner) endocuticle. exocuticle is characterized by a transversely-isotropic helicoidal structure that is comparatively rigid (though brittle) and has been the subject of numerous prior studies. By contrast, the endocuticle of beetles is comprised of large, aligned bundles (macrofibers) of chitin that are strongly anisotropic. Arranged in unidirectional laminae, the macrofibers improve cuticle toughness by inhibiting crack formation and propagation between 30 successive plies [11–13].

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In general, impact-prone areas and exaggerated struc-31 tures, such as horns and legs exhibit cuticle organization that resists deformation and fracture. Acorn weevils in the genus *Curculio* are typified by an elongate structure of the head, called the rostrum (snout), which 36 instead exhibits unusual distal flexibility. The rostrum ₃₇ is a hollow, strongly curved (over 90° in some species), 38 cylindrical, exoskeletal extension of the otherwise nearly-39 spherical head, which bears at its apex the terminal chew-40 ing mouthparts. Despite being composed of the same material as other rigid body parts, the snout can be repeat-42 edly bent without evident damage. This structure is used 43 by the female to feed and excavate sites for egg-laying 44 (oviposition); the latter process causes significant, appar-45 ently elastic, deformation of the rostrum. By maintaining constant tension on the snout and rotating around the bore-hole, females are able to flex the rostrum into 49 a near-perfectly straight configuration and thereby pro-

50 duce a linear channel into the fruit; a single female may 51 prepare hundreds of such sites during the adult stage.

While this behavior has been observed in many species of Curculio, it was unclear how the rostrum of female 54 acorn weevils can withstand the repeated, often extreme 55 bending incurred during the process of egg-chamber ex-56 cavation. In this study we characterize the composite 57 profile of the rostral cuticle to account for the observed 58 flexibility of the snout. We show that the relative layer thicknesses and fiber orientation angles of the exocuticle 60 and endocuticle of the rostrum are strongly differenti-61 ated from the head capsule and other body parts, and 62 we estimate the effect of these differences using Classical 63 Laminate Plate Theory (CLPT).

Because recent studies have shown that the yield 65 strength of the weevil rostrum exoskeleton is lower in ten-66 sion than compression, we perform a comparative analy-67 sis of the ultimate tensile strength of the rostrum across 68 species and snout morphotypes; we also report the re-69 sults of displacement-controlled load cycling of the snout 70 in a species with strongly curved morphology. We relate 71 an observed increase in the volume fraction of endocuti-72 cle in the rostrum to higher tensile strength at the ros-73 tral apex in all tested species, and find that a strongly 74 curved rostrum can be flexed repeatedly without harm 75 to the structure.

We additionally describe the fracture mechanics of the 77 snout, as pertains to both cuticle composite structure 78 and tensile behavior, and consider how modification of 79 the cuticle may reduce the risk of rostral fracture dur-80 ing oviposition. Based on our findings we posit that the composite profile of the rostral apex enables the snout to be flexed until straight while remaining within the elas-83 tic limits of the material, mitigating the risk of structural 84 damage, and without evident alteration of the mechani-85 cal properties of the individual components of the cuti-86 cle across the structure and between species. Thus, the 87 flexibility and tensile strength of the rostrum appear to 88 be derived exclusively from modification of the composite 89 architecture of the exoskeleton. To our knowledge, this is 90 the first time that a modified composite profile has been 91 reported as a means of enhancing structural elasticity in

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92 the insect exoskeleton.

MICROSTRUCTURE OF THE CURCULIO ROSTRUM

In arthropods (including beetles), the exocuticle is 158 material for the exoskeleton.

macrofibers are orthotropic (axial: $E_1=8.5\,\mathrm{GPa}$, trans- 171 ($E_m=1.36\,\mathrm{GPa}$, $E_f=2.44\,\mathrm{GPa}$). verse: $E_2 = E_3 = 0.52 \,\mathrm{GPa} \,[1]$) and arranged in $_{172}$ INSERTA (i.e., angled approx. 90° to each other, see Figs.), with 175 eled, each with only one of the modifications, namely: REFS-118 a constant stacking angle between pairs, although other configurations have been observed [11, 12]. This geowhat kind of 19 metric sequence of the macrofiber laminae yields an ap- 176 lami-nate is 120 proximately transversely isotropic composite, similar to 177 the Bouligand structure. Notably, the resulting lami- 178 122 nate is less rigid than the exocuticle, but exhibits greater 179 123 toughness because the pseudo-orthogonal plies effectively 180 124 inhibit crack formation and propagation between succes-125 sive layers [11–13].

Serial thin sectioning and scanning electron microscopy 181 of fractured Curculio specimens has revealed that endo-128 cuticle in the head capsule fits this general profile, with 183 ¹²⁹ an angle of approximately 30° between successive pairs of ¹⁸⁴ pseudo-orthogonal plies. Additionally, in the head cap- 185 131 sule, the thickness of the exocuticle in cross section is 186 thickness nearly equal to that of the endocuticle. However, we have also found that the cuticle composite lay-up of the here 135 rostral apex differs from that of the head capsule (see INSER Fig.) in two key characteristics:

> The exocuticle is reduced to a thin shell, with the endocuticle thickened to offset this reduction to maintain a constant cuticle thickness in the head.

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2. The endocuticular macrofibers exhibit no rotation between successive pseudo-orthogonal plies, which are all oriented at approximately $\pm 45^{\circ}$ to the lon- $[\pm 45^{\circ}]$ angle-ply laminate).

the composite structure of the cuticle within a single 202 The available evidence therefore suggests that the rel-150 species, C. longinasus Chittenden, 1927 [1?]. This com- 203 ative flexibility of the snout is primarily derived from the 151 posite profile has now been uncovered in the rostral apex 204 composite profile of its cuticle.

152 of six additional, phylogenetically disparate, species (de-153 tailed in methods), indicating that this is likely a genus-154 wide trait. In all examined species, the portion of the 155 snout between the head capsule and apex of the scrobe 156 exhibits a gradual transition in composite profile along 157 an anterior-posterior gradient.

To investigate the effect of these cuticle modifications, comprised of numerous unidirectional laminae of chitin 159 we estimated uni-axial membrane and transverse flexfibers; each layer is the thickness of a single fiber (2- 160 ural Young's moduli of the cuticle in both the rostral 99 4 nm) embedded in a proteinaceous matrix. These layers 161 apex and head capsule using Classical Laminate Plate 100 are stacked at a more or less constant angle to each other, 162 Theory (CLPT), as detailed in our methods. We previthus forming a quasi-isotropic laminate referred to as the 163 ously derived the effective elastic constants of the cu-Bouligand structure [7–9]. This layout effectively pro- 164 ticle regions of C. longinasus, which we used here to 103 duces a transversely isotropic composite, mitigating the 165 construct constitutive equations for the entire cuticle of $_{104}$ strong anisotropy of α -chitin to yield a versatile building $_{166}$ that species. The cuticle was estimated to have membrane and flexural moduli of $E_m = 4.77 \,\mathrm{GPa}$ and Beetle endocuticle, however, is unique among arthro- 168 $E_f=6.04\,\mathrm{GPa}$, respectively, in the head capsule; howpods and is comprised of large (1-5 µm diameter) uni- 169 ever, in the rostral apex we found that these values were 108 directional bundles of chitin, called macrofibers. Chitin 170 reduced by approximately 72% and 60%, respectively

To assess the individual contributions of layer thickness INSERT unidirectional plies, seen in Figs. [12, 13]. Typically, adjacent macrofiber plies are paired and pseudo-orthogonal jacent macrofiber plies are paired and pseudo-ortho

- 1. A hybrid cuticle with the angle stacking sequence of regular cuticle (the head capsule) but possessing the layer thicknesses of the rostral apex. $E_m = 3.73 \,\mathrm{GPa}, E_f = 4.31 \,\mathrm{GPa}, \mathrm{representing}$ 22% and 29% decreases, respectively.
- 2. A hybrid cuticle with the layer thicknesses regular cuticle but possessing the ansequence of the rostral apex gle stacking $\pm 45^{\circ}$ angle-ply in the endocuticle). $E_m = 3.77 \,\mathrm{GPa}, E_f = 5.76 \,\mathrm{GPa}, \,\mathrm{representing}$ 21% and 4.7% decreases, respectively.

Each of the cuticle modifications noted in the rostral apex individually decreased the elastic moduli of the cuti-189 cle; however, they appear to have a synergistic combined 190 effect on cuticle elasticity, rather than a simple additive effect. This result suggests that both modifications are 192 necessary in order for the snout to function properly in 193 the living animal, where the combined effect allows the 194 rostrum to bend until completely straight without frac-

Below we demonstrate that the endocuticle does not gitudinal axis of the snout (i.e., an antisymmetric 198 vary in tensile strength across the rostrum or between 199 species, making it unlikely that differences in scleroti-200 zation or chitin composition within the cuticle are re-In previous work we identified these modifications to 201 sponsible for the mechanical behavior of the rostrum.

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FORCE-CONTROLLED LOADING TO FRACTURE

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To better characterize the mechanical behavior of the 207 ing on the snouts of six species in the genus Curculio, 264 young's modulus for such species representing a mixture of closely and distantly related taxa. Although the heads were rehydrated by immersion in de-ionized water for 24 hours, we observed comparatively brittle fracture (but see below), in contrast to GIVE EXAMPLES HERE. The tensile behavior for the 265 III. LOAD CYCLING OF CURCULIO CARYAE cuticle of these weevils is a result of its microstructure, which lacks pores, etc (give reasons). THIS IS ALSO A GOOD SPOT TO SIGNPOST WHAT I FOUND IN GENERAL.

We observed that the maximum force sustained at the 220 site of the break was strongly correlated with the crosssectional area of the endocuticle, and not the exocuticle. Consequently, there was a negative correlation between utlimate tensile strenth of the specimen and the ratio of 272 230 species membership, rostrum length, and location on the 279 initially believed that this indicated damage to the spec-

These data have three important implications:

- behavior of the cuticle across the genus, in agreement with our current understanding of cuticle mechanobiology. (singh 2016, jansen 2016)
- 2. The endocuticle contributes more to the tensile strength of the rostrum than the exocuticle, possibly because the endocuticle is organized in large bundles of aligned, anisotropic fibers.
- 3. Thus, in addition to making the cuticle more flex- 292 ible, the altered apical composite profile makes it less likely to break, suggesting a possible means by breakage, maybe say this in conclusions).

246 247 in specimens with a longer snout. This observation was 299 these chains as the hydrogen bonds break and reform in 257 however Young's modulus of the rostrum would be com- 300 configuration, dissipating the accumulated strain without 258 paratively higher in these species because of the greater 310 any damage to the specimen.

259 volume fraction of exocuticle. [OR SAY MORE CON-260 CISELY THAT: based on prelim CLSM data we believe 261 that the snout is reinforced against bucking with thicker 262 exocuticle in the base of these species; as a result, the $_{208}$ snout as an integrated whole, we performed tensile test- $_{263}$ higher volume fraction of exocuticle in the snout increases

The shearing motion and accommodation of strain led us to question how the cuticle might accommodate re-268 peated strain, as is seen in the living organism. We therefore performed fatigue testing on a female curculio 270 longinasus, which exhibits the most extreme degree of bending in the sis species examined.

400K cycles, complete elongation, rehydrated, coated exocuticle to endocuticle cross-sectional area at the site of 273 in grease to prevent loss of moisture and stiffening of fracture, indicating that as the proportion of exocuticle 274 the specimen. We observed viscoelastic behavior in the increased, tensile strength decreased. In other words, 275 specimen, as indicated by histeresis in the stress-strain UTS is strongly correlated with the cross-sectional area 276 relationship during each cycle. Fmax decreased logarithof the endocuticle across species. These associations were 277 mically with cycle number, etc., and the specimen apfound to be statistically significant and independent of 278 peared to have deformed plastically during the test. We 280 imen; however, after cleaning the specimen in a 24 hour 281 wash with ethanol and water, we observed that the spec-282 imen returned to its original shape. The specimen did 1. There is very little variation in the gross elastic 283 not show any evidence of fractures or shear cusps any-²⁸⁴ where in the surface of the exocuticle, and, furthermore, 285 the tensile strength of the specimen was consistent with 286 other members of its species. Given this surprising result, 287 it appears that the specimen was undamaged by the test-288 ing. We therefore believe that under normal conditions 289 in life, repeated bending of the snout does exceed the 290 yield/plastic limit of the cuticle, and the bending strain 291 is purely elastic/viscoelastic.

We cannot fully account for these results, but we spec-293 ulate that the microstructure of the endocuticle is re-294 sponsible for what we observed. The endocuticle is made which the system evolved (via negative selection of 295 of aligned α -chitin nanofibrils whose crystalline structure 296 is enforced by hydrogen bonds between individual chitin 297 chains along their length. The viscoelasticity of the cu-Finally, we observed that the elastic modulus is higher 298 ticle is thought, in part, to come from slippage between initially quite puzzling, as we had expected that a longer 300 response to shearing between the chitin molecules. We (and typically more strongly curved [insert ecomorph pa- 301 believe that repeated strain may have caused such slipper ref here]) would need to be more flexible to avoid 302 page in the endocuticle of the rostral apex during the fracture during oviposition. Based on preliminary confo- 303 fatigue test, but without sufficient time for the matecal microscopy data, we speculate that this phenomenon 304 rial to completely relax after deformation, the specimen may be the result of a longer scrobe/transition/gradient 305 would slowly accumulate strain and consequently deform from the basal profile to the apical profile in longer rostra. 306 viscoelastically/viscoplastically. After 24 hours soaking A decrease in exocuticle thickness along a longer portion 307 in ethanol and water, the hydrogen bonds would relax of the base might reinforce the snout against buckling; 308 sufficiently to allow the specimen to return to its original

FRACTOGRAPHY OF TEST SPECIMENS

Examination of the fracture surfaces and adjacent cu-312 313 ticle of tensile testing specimens revealed that although fracture was comparatively brittle, the fracture mechanics of the exocuticle and endocuticle differed according to their microstructure, in agreement with previous studies

In cross-section, the exocuticle consistently presented 318 a smooth, nearly continuous fracture surface, indicative of relatively brittle fracture, likely due to the microarchitecture and resultant transverse isotropy of the Bouligand structure (explain this). Endocuticle, on the other hand exhibited severe delamination, ply-splitting, and 324 fiber pulling, consistent with viscoelastic/plastic behav-325 ior shown in previous studies and congruent with theoretical consideration of the microstructure of this material (name something here). These patterns indicate that the endocuticle is probably less brittle than the exocuticle, most likely due to the alignment of the α -chitin fibers in each macrofiber.

In addition, the exocuticle typically appears to fracture before the endocuticle, with shear-cusp formation evident over unbroken endocuticle. We note, however, that the exocuticle of weevils/beetles is anchored to the endocuticle by cross-linking fibers in a transition zone described by Kamp et al. (see refs.). The presence of shear-cusps 337 therefore indicates that the fibers of the endocuticle are 338 shearing past each other within each ply along the ra-339 dial/normal plane (type II shearing???, extension shear-341 between plies, the layers of endocuticle are likely shearing 369 able in the online version of this paper.

342 past each other (type III shearing) along the transverse 343 plane. We therefore infer that, under tension, the en-344 docuticle tends to deform viscoelastically and plastically 345 along the longitudinal axes of the macrofibers, while the 346 overlying exocuticle exhibits brittle fracture due to shear-347 ing between the stretching endocuticle fibers to which it $_{348}$ is anchored.

Additionally, the fracture surfaces show a characteris-350 tic failure mode, based on the pattern of fiber dislocation 351 in the plies of the endocuticle. (copy description from 352 DATA PRESENTATION, for figure 5B).

From this pattern we hypothesize that the exocuticle-354 rich gular sutures are the most likely site for the initiation 355 of void nucleation and failure of the integrated rostral cu- $_{356}$ ticle in cross section. Structural failure would take place 357 as cracks propagate through the endocuticle from these sutures, which penetrate the entire thickness of the lami-359 nate. We speculate that this could be the reason why the ₃₆₀ cross-sectional profile of *C. caryae* is flattened ventrally. 361 Flattening this region may reduce tensile-strain across 362 the gular sutures when the snout is bent dorsally, thus 363 reducing the risk of fracture in the elongate, stronglycurved rostrum in this species.

CONCLUSIONS

METHODS VI.

Methods, including statements of data availability and 340 coupling). Furthermore, given the delamination observed 368 any associated accession codes and references, are avail-

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ACKNOWLEDGMENTS

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AUTHOR CONTRIBUTIONS

415 **Andrew Jansen:** Conducted sectioning and staining, 436
416 microscopy and imaging, tensile and fatigue
417 testing, statistical analysis, and participated in 437
418 manuscript preparation.

Jason Williams: Conducted tensile and fatigue testing, participated in manuscript preparation.

Nikhilesh Chawla: Facilitated microscopy, tensile and fatigue testing, and participated in manuscript preparation.

Nico Franz: Facilitated specimen acquisition and imaging, participated in manuscript preparation.

ADDITIONAL INFORMATION

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints.
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COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

METHODS

Histological sectioning

Tensile and fatigue testing

Specimen imaging and microscopy

Constitutive modeling of the cuticle

General Approach

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Cuticle profile of model The cuticle of C. longinasus is 50 microns thick; we use C. longinasus because we have constitutive models for the cuticle regions of this species. We assumed equal layer thicknesses in the endocuticle of the basal cuticle, and equal thicknesses of exocuticle and endocuticle. In the apical cuticle we assumed the exocuticle and upper 8 layers of the endocuticle were each incrons thick, with 4 thinner layers of endocuticle, each 1.25 µm thick. The angles of the endocuticle layers for both types of cuticle are as described above.

450 Permutations We additionally calculated models for
 451 two hypothetical hybrid cuticles: one model has the layer
 452 thicknesses of the apex, but fiber orientations of the base,
 453 while the second has the fiber orientations of the apex,
 454 but the layer thicknesses of the base.

Classical Laminate Plate Theory We begin by calculating the 2D reduced stiffness matrix for each part of the tuticle. For orthotropic materials with the principal axes parallel to the ply edges, the reduced stiffness matrix is defined as follows:

$$[Q] = \begin{bmatrix} Q_{11} & Q_{12} & 0 \\ Q_{21} & Q_{22} & 0 \\ 0 & 0 & Q_{66} \end{bmatrix} , \tag{1}$$

and where:

$$Q_{11} = \frac{E_1}{1 - \nu_{12}\nu_{21}},$$

$$Q_{12} = \frac{E_1\nu_{21}}{1 - \nu_{12}\nu_{21}} = Q_{21},$$

$$Q_{21} = \frac{E_2\nu_{12}}{1 - \nu_{12}\nu_{21}} = Q_{12},$$

$$Q_{22} = \frac{E_2}{1 - \nu_{12}\nu_{21}},$$

$$Q_{66} = G_{12}.$$
(2)

For each layer k, the reduced stiffness matrix is transformed to account for the layer orientation angle θ within the laminate coordinate system, yielding a reduced transformed stiffness matrix according to:

$$[\bar{Q}] = [T]^{-1}[Q][T]^{-T},$$
 (3)

where the transformation matrix [T] is defined as:

$$[T] = \begin{bmatrix} \cos^2 \theta & \sin^2 \theta & 2\cos\theta\sin\theta\\ \sin^2 \theta & \cos^2 \theta & -2\cos\theta\sin\theta\\ -\cos\theta\sin\theta & \cos\theta\sin\theta & \cos^2 \theta - \sin^2 \theta \end{bmatrix}. \quad (4)$$

Using the lay-ups specified for the cuticle permutations, we calculate the extensional stiffness matrix [A], bending stiffness matrix [D], and bending-extension cou- $_{469}$ pling matrix B for each laminate consisting of n layers at 470 a distance z from the laminate mid-plane. The elements 471 of these matrices can be found according to:

$$A_{ij} = \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k - z_{k-1}),$$

$$B_{ij} = \frac{1}{2} \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k^2 - z_{k-1}^2),$$

$$D_{ij} = \frac{1}{3} \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k^3 - z_{k-1}^3).$$

These stiffness matrices relate vectors of resultant $_{473}$ forces $\{N\}$ and bending moments $\{M\}$ to mid-surface $_{496}$ laminate, we first specify the moment-curvature relation 474 strains and curvatures $\{\epsilon^{\circ}\}$ and $\{\kappa\}$, respectively, in the 497 of an Euler-Bernoulli beam: 475 laminate according to the following relationship:

$$\begin{cases} \{N\} \\ \{M\} \end{cases} = \begin{bmatrix} [A] & [B] \\ [B] & [D] \end{bmatrix} \begin{cases} \{\epsilon^{\circ}\} \\ \{\kappa\} \end{cases} .$$
 (6)

For symmetric laminates, [B] = 0, and therefore: 476

$$\{N\} = [A]\{\epsilon^{\circ}\}, \{M\} = [D]\{\kappa\}.$$
 (7)

or, in expanded form:

$$\begin{cases}
N_{xx} \\
N_{yy} \\
N_{xy}
\end{cases} = \begin{bmatrix}
A_{11} & A_{12} & A_{16} \\
A_{21} & A_{22} & A_{26} \\
A_{61} & A_{62} & A_{66}
\end{bmatrix} \begin{Bmatrix}
\epsilon_{xx}^{\circ} \\
\epsilon_{yy}^{\circ} \\
\gamma_{xy}
\end{Bmatrix},$$

$$\begin{cases}
M_{xx} \\
M_{yy} \\
M_{xy}
\end{Bmatrix} = \begin{bmatrix}
D_{11} & D_{12} & D_{16} \\
D_{21} & D_{22} & D_{26} \\
D_{61} & D_{62} & D_{66}
\end{bmatrix} \begin{Bmatrix}
\kappa_{xx} \\
\kappa_{yy} \\
\kappa_{xy}
\end{Bmatrix}.$$
(8)

If we make the simplifying assumptions (see ref.) that and and all oading and (1) the laminate experiences pure axial loading and (1) transverse bending (i.e., $N_{vv} = N_{vv} = 0$ and $M_{vv} = 1$ transverse bending (i.e., $N_{yy} = N_{xy} = 0$ and $M_{yy} = M_{xy} = 0$, respectively) and (2) the laminate is a beam 483 of sufficiently high aspect ratio to minimize the Poisson 484 effect and anisotropic shear coupling (i.e., below we ef-485 fectively let $A_{12}^*=A_{16}^*=0$ and $D_{12}^*=D_{16}^*=0$), then 486 we can calculate the in-plane effective flexural and axial 487 Young's moduli of the laminate along the x-axis.

For axial Young's modulus of the laminate, we first 489 define the average membrane stresses in the laminate as:

$$\{\bar{\sigma}^m\} = \frac{\{N\}}{z_1 - z_n}.$$
 (9)

By substitution in Eq. 7, we find:

$$\begin{cases}
\bar{\sigma}_{xx}^{m} \\
\bar{\sigma}_{yy}^{m} \\
\bar{\tau}_{xy}^{m}
\end{cases} = \frac{1}{(z_{1} - z_{n})} \begin{bmatrix} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ A_{61} & A_{62} & A_{66} \end{bmatrix} \begin{cases} \epsilon_{xx}^{m} \\ \epsilon_{yy}^{m} \\ \gamma_{xy}^{m} \end{cases},$$
(10)

and, by inverting this equation (let $A^* = A^{-1}$) and 492 substituting based on the assumptions above, we infer:

$$\epsilon_{xx}^m = (z_1 - z_n) A_{11}^* \bar{\sigma}_{xx}^m \,.$$
 (11)

We therefore define Young's modulus for effective axial (5) 493 We therefore elasticity as:

$$E_{xx}^{m} = \frac{\bar{\sigma}_{xx}^{m}}{\epsilon_{xx}^{m}} = \frac{1}{(z_{1} - z_{k})A_{11}^{*}}$$
(12)

To find the transverse flexural Young's modulus of the

$$M = EI\kappa. (13)$$

Along the x-axis, the second moment of area for a rect-499 angular cross-section is:

$$I_{yy} = \frac{b(z_1 - z_n)^3}{12} \,, \tag{14}$$

Given the assumption that $M_{yy} = M_{xy} = 0$, the mo-501 ment along the x-axis is related to the moment of the 502 beam by:

$$M = M_{xx}b. (15)$$

Thus, given the assumption that $D_{12} = D_{16} = 0$, ⁵⁰⁴ Young's modulus for the effective transverse flexural elas-505 ticity of the laminate can be found by making Eq. 13 spe-506 cific to transverse flexure of the x-axis and rearranging 507 the terms:

$$E_{xx}^f = \frac{12M_{xx}}{(z_1 - z_n)^3 \kappa_{xx}} \tag{16}$$

From inversion of Eq. 7 (let $D^* = D^{-1}$) this reduces

$$E_{xx}^f = \frac{12}{(z_1 - z_n)^3 D_{11}^*} \tag{17}$$

Statistical analysis

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General approach To explore the relationships be-511 tween the composite structure and mechanical properties of the cuticle, we fit phylogenetic linear mixed-effects models to the data using maximum likelihood estimation. In order to control for phylogenetic non-independence in the data, we included the species of each specimen as a random effect in all models. We also allowed for correlation in the error term of the models, as specified by a variance-covariance matrix generated from a Brownian motion model of trait evolution along the phylogeny. Response variables and covariates were natural-log transformed, as needed, to ensure model residuals were normally distributed and homoscedastic. In all models, we 524 tested whether the inclusion of phylogenetic correlation $_{525}$ in the model error produced significantly better model $_{549}$ 526 fit, using a likelihood-ratio test and R_{σ}^2 -difference test 550 between the fully-specified model and a model lacking 551 the phylogenetic effect.

Hypothesis testing The following three hypotheses were tested using PGLMMs fitted using ML estimation: $_{552}$

1. The maximum sustained tensile force is proportional to the cross-sectional area of the endocuticle, and *not* that of the exocuticle.

- 2. The ultimate tensile strength of the samples is inversely proportional to the ratio of exocuticle to endocuticle at the location of fracture.
- 3. Young's modulus of the samples is proportional to the length of the snout.

We fitted a fully-specified model with the cross-540 sectional area of endocuticle and exocuticle at the site of fracture as fixed effects, including an interaction term, 542 and with maximum tensile force sustained prior to frac-543 ture as a response variable. This model was then com-544 pared to models with only cross-sectional area of either 545 endocuticle or exocuticle as the sole fixed effect in the 546 model. We then tested the first hypothesis by using 547 likelihood-ratio tests and $R_{\beta*}^2$ -difference tests between 548 each of the three models.

The hypothesis that Model selection and fitting Estimating phylogenetic signal

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Code availability

Data availability

REFERENCES

[1] Leslie Lamport, Lambert, a document preparation system, Addison Wesley, Massachusetts, 2nd edition, 1994.