Exoskeletal microstructure and tensile behavior of the acorn weevil rostrum

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The acorn weevil snout exhibits remarkable flexibility and toughness that are derived from from the microarchitecture of its exoskeleton. Here we characterize modifications to the composite profile of the rostral cuticle that simultaneously enhance the flexibility and fracture toughness of the distal portion of the snout. Using Classical Laminate Plate Theory (CLPT) we estimate the effect of these modifications on the elastic behavior of the exoskeleton. Additionally, changes in the relative layer thicknesses and orientation angles of layers in the exoskeleton are related to the tensile behavior of the snout in six species of diverse morphology, and we demonstrate that a highly curved rostrum can be completely straightened without structural damage. We demonstrate that increased endocuticle thickness is strongly correlated with increased tensile strength in the snout. Consequently, snout stiffness is shown to be inversely correlated with fracture toughness. Finally, we identify exocuticle rich invaginations of the occipital sutures both as a likely site of crack initiation in tensile failure and as a source of morphological constraint on the evolution of the snout.

8 hierarchically-structured fibrous composite characterized 37 trum of female acorn weevils can withstand the repeated, 9 by variously arranged α-chitin (N-acetylglucosamine) 38 often extreme bending incurred during the process of 10 nanofibrils embedded in a heterogeneous protein ma- 39 egg-chamber excavation. In this study we characterize detail below [4–6]. Impact-prone areas and exaggerated structures in arthropods generally exhibit cuticle organization that resists deformation and fracture (e.g. [7–11]); however, acorn weevils in the genus Curculio Linnaeus, 1758¹ instead exhibit unusual distal flexibility in an elongate extension of the head called the rostrum (snout) [1, 12–14]. The rostrum is a hollow, strongly curved (over 90° in some species), cylindrical, exoskeletal extension of the otherwise nearly-spherical head, which bears at its apex the terminal chewing mouthparts ₂₅ [14–18]. This structure is used by the female to feed 26 and to excavate sites for egg-laying (oviposition, see Fig. 1c), and can be repeatedly bent without evident damage despite being composed of the same material as other rigid body parts [1, 12–14]. By maintaining constant pressure on the snout and rotating around the bore-hole, females are able to flex the rostrum into a straightened configuration and produce a linear channel into the fruit; a single female may prepare hundreds of such sites as an adult [13, 19, 20].

While this behavior has been observed in many species

The exoskeleton of Coleoptera (beetles) is a 36 of Curculio [13, 14, 19, 20], it was unclear how the rostrix [1-3]. Although α-chitin is brittle and strongly 40 the composite profile of the rostral cuticle to account anisotropic, beetle cuticle is simultaneously rigid and 41 for the observed flexibility of the snout. We show that tough due to its unique laminate microstructure (see 42 the relative layer thicknesses and fiber orientation ankamp, vincent for review), which we characterize in 43 gles of the exocuticle and endocuticle of the rostrum are 44 strongly differentiated from the head capsule and other 45 body parts, and we estimate the effect of these differ-46 ences on the elasticity of the cuticle using Classical Lam-47 inate Plate Theory (CLPT). Because recent studies have 48 shown that the yield strength of the beetle exoskeleton 49 is lower in tension than compression [22], we perform 50 a comparative analysis of the ultimate tensile strength 51 of the rostrum across species and snout morphotypes; we 52 also report the results of displacement-controlled load cy-53 cling of the snout in a species with strongly curved mor-54 phology. We relate an observed increase in the volume 55 fraction of endocuticle in the rostrum to higher tensile 56 strength at the rostral apex in all tested species, and find 57 that a strongly curved rostrum can be flexed repeatedly 58 without harm to the structure.

> We additionally describe the fracture mechanics of the 60 snout and consider how modification of the cuticle may 61 prevent crack formation during oviposition. Based on 62 our findings, we posit that the composite profile of the 63 rostral apex enables the snout to undergo repeated distal flexion while remaining within the elastic limits of the 65 material, mitigating the risk of structural damage, and 66 without evident alteration of the mechanical properties 67 of the individual components of the cuticle across the 68 structure and between species. Thus, the flexibility and 69 tensile strength of the rostrum appear to be derived ex-70 clusively from modification of the composite architecture 71 of the exoskeleton. To our knowledge, this is the first 72 time that a modified composite profile has been reported 73 as a means of enhancing structural elasticity in the insect

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Pursuant to the International Code of Zoological Nomenclature, the first mention of any specific epithet will include the full genus and species names as a binomen (two part name) followed by the author and date of publication of the name. This is not an in-line reference; it is a part of the name itself and refers to a particular species-concept as indicated in the description of the species by that author [21].

74 exoskeleton (but see [23]).

MICROSTRUCTURE OF THE CURCULIO ROSTRUM

In arthropods (including beetles), the exocuticle is comprised of numerous unidirectional laminae of chitin nanofibrils; each layer is the thickness of a single fiber (2-4 nm) embedded in a proteinaceous matrix [24, 25]. These layers are stacked at a more or less constant angle to each other, forming a quasi-isotropic laminate known as the Bouligand structure [6, 26, 27]. This layout effec-84 tively mitigates the strong anisotropy of α -chitin to yield a versatile building material for the exoskeleton [2, 24, 25, 28]. Beetle endocuticle, however, is unique among arthropods and is comprised of large (1-5 µm diame-88 ter in Curculio) unidirectional bundles of chitin, called 89 macrofibers. Chitin macrofibers are orthotropic (axial: 90 $E_1 = 8.5 \,\mathrm{GPa}$, transverse: $E_2 = E_3 = 0.52 \,\mathrm{GPa} \,[1]$) 91 and arranged in unidirectional plies, seen in Figs. REF 92 [4, 5]. Typically, adjacent macrofiber laminae are paired 93 and pseudo-orthogonal (i.e., angled approx. 90° to each 94 other [29], see Figs. REF), with a constant stacking an-95 gle between pairs, although other configurations have been observed [3–5, 30]. This geometric sequence of the macrofiber laminae yields an approximately transversely isotropic composite, similar to the Bouligand structure [5, 25]. Notably, the resulting laminate is less rigid than the exocuticle, but exhibits greater toughness because the pseudo-orthogonal plies effectively inhibit crack formation and propagation between successive layers [3–5]. Serial thin sectioning and scanning electron microscopy of fractured Curculio specimens revealed that endocuticle in the head capsule fits this general profile, with an angle of approximately 30° between successive pairs of pseudoorthogonal plies. Additionally, in the head capsule, the thickness of the exocuticle and endocuticle in cross section are nearly equal (typically between 20-30 µm). However, we found that the cuticle composite lay-up of the 111 rostral apex is strongly differentiated from the head capsule (see Fig. REF). Distally the exocuticle is reduced to a thin shell (ca. 5 µm), with the endocuticle thickened to offset this reduction and maintain a constant 169 117 tation between successive pseudo-orthogonal plies, and 172 and distantly related taxa (see Methods) [33–36]. Each $_{118}$ are oriented at approximately $\pm 45^{\circ}$ to the longitudinal $_{173}$ specimen was immersed in di-H₂O for 24 hours, to sim-119 axis of the snout (i.e., an antisymmetric [±45°] angle-ply 174 ulate the living tissue (see [37]), then subjected to force-

129 along an anterior-posterior gradient.

We estimated the effect of differential cuticle organization on uni-axial membrane and transverse-flexural Young's moduli of the cuticle in the rostral apex and head capsule using Classical Laminate Plate Theory 134 (CLPT), as detailed in our methods [31, 32]. The ef-135 fective elastic constants of the cuticle regions of C. longinasus (estimated previously, see [1]) were used to construct constitutive equations for the entire cuticle of that species. The cuticle of the head capsule was 139 estimated to have membrane and flexural moduli of $E_m = 4.77 \,\text{GPa}$ and $E_f = 6.04 \,\text{GPa}$, respectively; 141 however, in the rostral apex we found that these values 142 were reduced by approximately 72% and 60%, respec-143 tively $(E_m = 1.36 \, \text{GPa}, E_f = 2.44 \, \text{GPa})$. Two hypo-144 thetical cuticle lay-ups were also modeled to individually 145 assess the contributions of either modified layer thickness 146 or stacking angle sequence to cuticle flexibility. The ef-147 fective moduli of a configuration with the angle stacking 148 sequence of typical cuticle (i.e., in the head capsule) but 149 possessing the layer thicknesses of the rostral apex were 150 calculated as $E_m = 3.73 \,\mathrm{GPa}, E_f = 4.31 \,\mathrm{GPa}, \,\mathrm{repre}$ 151 senting 22% and 29% decreases from unmodified cuticle, 152 respectively. Similarly, a hypothetical cuticle with the 153 layer thicknesses of ordinary cuticle but possessing the angle stacking sequence of the rostral apex (i.e., $\pm 45^{\circ}$ angle-ply in the endocuticle) had effective elastic moduli of $E_m = 3.77 \,\mathrm{GPa}, E_f = 5.76 \,\mathrm{GPa}, \mathrm{representing} \,21\%$ and 4.7% decreases from unmodified cuticle, respectively. 158 Each of the cuticle modifications noted in the rostral apex 159 individually decreased the elastic moduli of the cuticle; 160 however, they appear to have a synergistic combined ef-161 fect on cuticle elasticity, rather than a simple additive 162 effect. This result suggests that both modifications are 163 necessary in order for the snout to function properly in 164 the living animal, where the combined effect allows the 165 rostrum to bend until completely straight without frac-166 ture.

FORCE-CONTROLLED LOADING TO **FRACTURE**

To better characterize the failure behavior of the roscuticle thickness (ca. 50 µm total) throughout its length. 170 trum, we performed tensile testing on the snouts of six Moreover, the endocuticular macrofibers exhibit no ro- 171 Curculio species that representing a mixture of closely laminate). We previously identified these modifications 175 controlled, uniaxial loading to fracture at a constant to the composite structure of the cuticle within a sin- 176 stress rate of 1.0 gf · s⁻¹ (detailed in Methods). In gen-122 gle species, C. longinasus Chittenden, 1927 [1, 12]; how- 177 eral, the specimens exhibited a non-linear viscoelastic re-123 ever this composite profile has now been uncovered in 178 sponse curve characterized by a sharp increase in stress the rostrum of six additional, phylogenetically disparate, 179 at higher strains, terminating in brittle fracture [38]. We 125 species (detailed in methods), indicating that this is likely 180 postulate that strain hardening occurs as the longitudi-126 a genus-wide trait. In all examined species, the portion 181 nal axis of the macrofibers becomes more closely aligned 127 of the snout between the head capsule and apex of the 182 to the cylindrical axis of the rostrum, thereby resisting 128 scrobe exhibits a gradual transition in composite profile 183 tension more directly with increasing strain [39].

We examined the correspondence between composite 239 The specimen was aligned so that uniaxial tension would cle regions vary across the length of the head along an 256 returned to its original shape. 202 anterior-posterior gradient, it is not possible to correlate 257 of the entire snout.

Instead, we found that the uniaxial elastic modulus 260 coelasticity. 205 be comparatively higher in these species because of the 274 dissipating the accumulated strain. higher volume fraction of exocuticle. From these tests, 275 bundles of aligned, anisotropic fibers, leading to a trade- 283 yield strength of the cuticle. off between rigidity and toughness. Consequently, the altered composite profile of the cuticle in the rostral apex makes the rostrum simultaneously more flexible and fracture resistant.

III. LOAD CYCLING OF CURCULIO CARYAE

we performed displacement-controlled fatigue testing on 291 describe here (see [44] for general approach). 237 a typical female specimen of Curculio caryae, a species 292 In transverse view, the exocuticle consistently pre-₂₃₈ that exhibits extreme (80-90°) rostral curvature [14, 19]. ₂₉₃ sented a nearly continuous fracture surface, character-

structure and mechanical behavior of the snout using 240 induce elongation of the distal portion of the rostrum phylogenetic linear mixed effects models (PGLMM) to 241 with minimal off-axis deflection of the un-curved section. account for phylogenetic non-independence in residual 242 The strain per cycle was fixed at an amplitude sufficient variance, with species membership included as a random 243 to completely elongate the snout and generate a tensile effect [40, 41]. Our models show that the maximum force 244 load of 1.0 N in the straightened configuration (ca. 20% sustained at the site of failure was strongly correlated 245 ultimate strength) at a frequency of 0.33 Hz. The test with the cross-sectional area of the endocuticle, and not 246 was terminated after a period of two weeks (ca. 400K the exocuticle, at that site. Accordingly, there was a neg- 247 cycles) when the stress amplitude appeared to reach an ative correlation between ultimate tensile strength of the 248 asymptotic minimum. The rostrum behaved viscoelasspecimen and the ratio of exocuticle to endocuticle cross- 249 tically, indicated by histeresis in the stress-strain relasectional area at the site of fracture. Although CLPT 250 tionship during each cycle. Strain amplitude decreased predicts a positive association between the proportion of 251 logarithmically with cycle number, and the specimen iniexocuticle and stiffness of a generalized cuticle, we found 252 tially appeared to have deformed plastically during the no correspondence between the cross-sectional properties 253 test. We believed that this indicated damage to the specof the fracture site and the gross behavior of the entire 254 imen; however, after cleaning the specimen in a 24 hour rostrum. Because the cross-sectional areas of the cuti- 255 wash with ethanol and water, we observed that rostrum

We cannot fully account for the stress relaxation of measurements from the fracture surface to the properties 258 the rostrum after testing, but we speculate that it arose 259 from the general mechanism associated with cuticle vis-The endocuticle is made of aligned α -(low strain: E_{low}) and secant modulus at failure (E_{sec}) 261 chitin nanofibrils whose crystalline structure is enforced were inversely correlated with ultimate strain and frac- 262 by hydrogen bonds between individual chitin chains ture toughness, implying that stiffer specimens, and by 263 and with the protein matrix along their length; macroextension, stiffer cuticle profiles, are generally more brit- 264 scopic viscoelastic behavior results from slippage between tle. We also observed a moderate, stiffening size-effect 265 these chains in response to shearing between the chitin with respect to rostral length, contrary to our expecta- 266 molecules [2, 42, 43]. We posit that repeated strain may tion that a longer, more strongly curved (see [35, 36]) 267 have caused such slippage in the endocuticle of the rostral snout would require increased flexibility to avoid frac- 268 apex during the fatigue test; however, without sufficient ture during oviposition. One possible explanation for 269 time for the material to completely relax after deformathis trend is that longer snouts may have a longer transi- 270 tion, the specimen would slowly accumulate strain and tion gradient from basal to apical profile to reinforce the 271 deform viscoelastically [39]. After immersion in ethanol junction between the rostrum and head capsule against 272 and water, the cuticle would be sufficiently plasticized to buckling. Thus, Young's modulus of the rostrum would 273 allow the specimen to return to its original configuration,

The specimen did not show any evidence of fractures, we infer that the gross elastic behavior of the cuticle is 276 micro-tears, or shear cusps anywhere in the surface of consistent across the genus, and that a single mechanism 277 the exocuticle, and, furthermore, the tensile strength of (i.e. the modified composite profile) confers increased 278 the specimen was consistent with other members of its flexibility and tensile strength to the rostral apex in the 279 species ($F_m ax = 5.02 \,\mathrm{N}$). Given this surprising result, genus Curculio. In addition, the endocuticle demonstra- 280 it appears that the specimen was undamaged by the testbly contributes more to rostral tensile strength than the 281 ing. We therefore expect that under normal conditions exocuticle, likely because of its organization into large 282 in life, repeated bending of the snout does not exceed the

IV. FRACTOGRAPHY OF TEST SPECIMENS

Although it was not always possible to identify void 286 nucleation and crack initiation sites given the complex 287 failure modes evident in the fractured specimens, we ob-288 served several patterns characteristic of both the micro-To confirm that repeated, proscribed straightening of 299 scale behavior of the cuticle and the meso-scale behavior the rostrum does not result in damage to the cuticle, 290 of the rostrum during uniaxial tensile failure, which we

294 istic of comparatively brittle failure, presumably due to 352 and ply-splitting followed by broom-like tensile failure; cle typically appeared to fracture at lower strains than 355 a large dorsal section of cuticle. 302 tion, off-axis ply-splitting, and fiber-pulling away from 360 trated in Fig REF. According to this model, structural vidual endocuticle laminae, implying that ply-splitting 367 tension only along the ventral surface of the rostrum. occurred via mode II fracture between macrofibers at high strain [31, 32]. We hypothesize that intra-laminar 312 extension-shear coupling also yielded off-axis, in-plane re-313 sultant forces as a function of lamina orientation angle; 314 mode III shearing then occurred between laminae with 315 opposing in-plane resultant forces, causing the observed 316 inter-ply delamination. Tensile failure of the macrofiber 317 laminae would ultimately occur via mixed-mode I/II (transverse tension/intra-laminar shear) fracture due to an increase in applied stress caused by ply-splitting in adjacent laminae [44].

At the meso-scale, most specimens fractured along a 322 single plane across and between the occipital sulci, which are cuticle invaginations that traverse the entire length of the rostrum [15, 45]. These sulci increase the volume fraction of exocuticle in the ventral part of the snout and contain large interfaces ideal for void nucleation. The exocuticle of the occipital sulci usually displayed shear cusps oriented outward from the center of the invagination, continuing dorsolaterally and ventromedially. Ventrally the cusps converged toward a prominent scarp where the crack fronts joined, although in specimens with large cross-sectional areas of endocuticle, this was often obscured by delaminated endocuticular macrofibers.

surfaces often exhibited extensive inter-ply delamination 402 resulting in present day diversity of the genus. and fiber de-bonding in scarp-like prominences, likely due 403 Based on fractographic analysis of the test-specimens, 350 the dorsally-radiating crack front. Dorsally, the coa- 405 a comparatively low strain, due to shearing between the

the relatively homogeneous arrangement of α-chitin lam- 353 in some specimens, the contralateral crack fronts were inae in the Bouligand structure [24, 25]. The exocuti- 354 out of plane and coalesced via transverse shear through

the endocuticle, with shear-cusp formation evident both 356 From these patterns we hypothesize that the at the fracture surface and across exocuticle (but with 357 exocuticle-rich occipital sulci are the most likely site for endocuticle intact) adjacent to the plane of fracture. 358 the initiation of void nucleation and catastrophic failure Conversely, the endocuticle exhibited severe delamina- 359 of the integrated rostral cuticle in cross section, as illusthe fracture surface, indicating the relatively high tough- 361 failure would take place as cracks propagate through the ness of the unidirectional α-chitin organization within 362 endocuticle from these sutures, which penetrate the enthe macrofibers [4, 5]. Because the exocuticle of wee- 363 tire thickness of the laminate [45]. Although other, more vils is anchored to the endocuticle by cross-linking fibers 364 complex failure modes have been observed, we posit that (see [5, 22]), exocuticular shear-cusp formation in uniax- 365 in live specimens this is the most likely mechanism of ial tension suggests extension-shear coupling within indi- 366 tensile failure because typical bending behavior generates

CONCLUSIONS

The rostrum of Curculio is characterized by a discon-370 tinuous composite profile, wherein the cuticle is strongly 371 differentiated in terms of relative layer thicknesses and 372 orientation angles along an anterior-posterior gradient. 373 These modifications are sufficient to achieve marked re-374 duction in the effective membrane and flexural moduli 375 of the cuticle (72% and 60%, respectively) in constitu-376 tive models based on CLPT, thereby accounting for the 377 observed flexibility of the rostral apex in live specimens. $_{378}$ However, these reductions can only be realized with both 379 modifications to the cuticle, which have a non-additive 380 effect on cuticle elasticity, implying that these weevils 381 require both modifications to function properly during 382 oviposition. Likewise, tensile and fatigue testing have 383 revealed a trade-off between stiffness and fracture resis-384 tance (as measured by ultimate strain and toughness), 385 mediated by the relative proportion of endocuticle in the 386 laminate. The altered composite profile of the cuticle in 387 the rostral apex makes the rostrum simultaneously more 388 flexible and fracture resistant, permitting the structure The first layer of endocuticle usually fractured along 389 to be flexed without exceeding the elastic limits of the the same plane as the exocuticle, and ventrally the en- 390 cuticle. To our knowledge, this is the first time that docuticle laminae typically converged toward a scarp-like 391 the composite profile of the cuticle has been related to region characterized by severe delamination and numer- 392 a gradient in elasticity and tensile performance across a ous de-bonded macrofibers. Additionally, macrofibers 393 cuticular structure in arthropods. Because these associaligned with the direction of crack propagation exhib- 394 ations were independent of species membership, we posit 340 ited extensive ply-splitting with intermittent transverse 395 that the behavior of the cuticle is consistent across the shearing, while macrofibers oriented against the direc- 396 genus, and that rostral flexibility is achieved exclusively tion of crack propagation primarily displayed fracture 397 through a modified cuticle lay-up in all Curculio species. by transverse shear along the plane of ply-splitting in 398 This conclusion raises the intriguing possibility that a adjacent laminae. Because the laminae form a cylin- 399 single ancestral shift in cuticle organization at the rosder, contralateral fibers in the same lamina display op- 400 tral apex - yielding higher flexibility and tensile strength posing fracture modes. In addition, the ventrolateral 401 – opened a large region of morphospace for exploration,

to a combination of tensile failure and shearing along 404 we infer that the exocuticle exhibits brittle fracture at 351 lescent crack fronts often caused significant de-bonding 406 endocuticle macrofibers to which it is anchored; these 412 extension shear-coupling $(A_{16}, A_{26} \neq 0)$ for individual 431 well as the minimization of exocuticle thickness in the 413 off-axis macrofiber laminae [31, 32]. These results im- 432 rostral apex, and the increased toughness derived from a 414 ply that fracture initiation occurs in the comparatively 433 thickened endocuticle, lead us to consider the avoidance 415 brittle exocuticle, and that the reduction in exocuticle 434 of catastrophic structural failure as a driving selective 416 thickness in the snout apex might serve to mitigate crack 435 pressure in the evolution of the rostrum. formation in rostral bending. Based on this pattern of fracture behavior, we identified the exocuticle-rich occipi-419 tal suture as a common point of void nucleation and crack initiation. From a biological perspective, these findings 421 reveal an unexpected morphological source of evolution-422 ary constraint on rostral flexibility, raising the intriguing 423 possibility that this system evolved primarily via nega-437 424 tive selection of fracture, rather than positive selection 438 any associated accession codes and references, are avail-425 of flexibility. In particular, the cuticle is invaginated in 439 able in the online version of this paper.

407 macrofibers fail at higher strain as a result of mixed-mode 426 precisely the portion of the snout that experiences the shearing and tensile fracture within and between laminae. 427 greatest degree of tension during antero-dorsal flexion; This outcome is consistent with behavior shown in pre- 428 the doubly-thick exocuticle in the invagination thus crevious studies and is congruent with theoretical consider- 429 ates an unavoidable, brittle weak-point in the otherwise ation of cuticle microstructure in CLPT, which predicts 430 endocuticle-dominated rostral apex. This constraint, as

METHODS

Methods, including statements of data availability and

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AUTHOR CONTRIBUTIONS

M.A.J. conducted sectioning and staining, microscopy 592 and imaging, tensile and fatigue testing, statistical 593 analysis, and participated in manuscript preparation. J.W. conducted tensile and fatigue testing and partic-595 ipated in manuscript preparation. N.C. facilitated mi-596 croscopy, tensile and fatigue testing, and participated 597 in manuscript preparation. N.M.F. facilitated specimen 598 acquisition and imaging and participated in manuscript 599 preparation.

ADDITIONAL INFORMATION

Supplementary information is available in the online 602 version of the paper. Reprints and permissions infor-603 mation is available online at www.nature.com/reprints. 604 Correspondence and requests for materials should be ad-605 dressed to M.A.J.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

METHODS

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Specimen acquisition and taxon sampling

Specimens for use in tensile and fatigue testing came 611 from the Hasbrouck Insect Collection at Arizona State University [ASUC]. This set of specimens was supple-613 mented with material housed in the following collections, using the codens of Arnett et al. [46]:

616 Ontario, Canada

617 D.C., USA 618

624 radiations and sister taxa with a variety of rostral mor- 676 head capsule, using the same procedure. The segmented 625 photypes, according to the phylogenetic hypotheses of 677 specimens were then placed into individual glass vials to 626 Hughes et al. [33, 35] and Bonal et al. [34]. The six 678 protect the fracture surfaces from contamination prior to 627 species of Curculio used herein are C. caryae (Horn, 679 microscopy. 628 1873), C. humeralis (Casey, 1897), C. proboscideus Fabricius, 1775, C. sulcatulus (Casey, 1897), C. uniformis 630 (LeConte, 1857), and C. victoriensis (Chittenden, 1904). 680

Histological sectioning

634 ducted on exemplary female specimens of C. humeralis 686 brittle specimens when gripping the ends of each head, 635 and C. longinasus Chittenden 1927. Live specimens of 687 a method was devised to create solid handles that could vation. A female specimen was selected and the rostrum 689 the cuticle. was separated from the head capsule with a fine-edged 690 For each head, four 1 cm² strips of gaffer tape were cut; in EMbed812, as follows.

644 and then transferred to a 2:1 mixture of acetone to epoxy 696 trum was aligned perpendicular to the edge of the strip. 645 resin. Samples remained at 21°C for 12 hours on a shaker 697 Hardening of the cyanoacrylate effectively embedded the 646 table to prevent hardening. These were then transferred 698 curved portion of the snout in a solid mass, isolating a 647 into a 1:1 mixture of acetone to resin, following by a 699 straight section of the snout (from the base to a point 648 1:2 mixture (each for 12 hours and at 21°C on a shaker 700 distad of the apex of the scrobe) for testing. A second 649 table), before finally being placed into a silicone mold 701 strip of tape was fixed over this mass with an additional 650 with pure resin. The mold was placed into an oven heated 702 layer of cyanoacrylate to provide a dorsal gripping sur-₆₅₁ to 38°C, and the resin was allowed to cure for 24 hours. ₇₀₃ face for the mass, and a small mark was made to indicate The resulting blocks were machined to prepare the apical 704 the extent of the head inside the mass. This embedding surface of each sample for microtomy.

655 used to expose a cross-section (transverse plane) of the 707 handles for testing. 656 apical and basal portions of the rostrum and to remove 708 Prior to testing, each specimen was placed in de-657 excess material. Semi-thin sections (0.5 µm thick) were 709 ionized water for 24 hours to allow full saturation of the

658 kept and stained with toluidine-blue-borax for light mi-659 croscopy and imaging.

Cold-fracture of specimens

Two pinned female specimens of each species were se-662 lected at random and retained for cold-fracturing of the 663 rostrum. The heads of the specimens were removed and 664 cleaned using a 95% ethanol solution and a thin paint-CMNC: Canadian Museum of Nature Collection, Ottawa, 665 brush. Any muscles protruding from the occipital fora-666 men were removed with a fine-edged razor blade. The antennae were removed directly using forceps to pull the USNM: National Museum of Natural History, Washington, 668 scape (basal section of antenna) from the antennal in-₆₆₉ sertion. Cleaned specimens were stored at -80° C for 24 670 hours, then fractured using forceps over a chilled alu-Cold fracture, semi-thin sectioning, and tensile testing 671 minum block. To fracture each specimen, the head capwere conducted on randomly chosen female specimens 672 sule and rostrum were each gripped firmly in a pair of belonging to six species obtainable through field work in 673 forceps; the forceps were then sharply rotated to fracture the southwestern USA and northwestern Mexico. Taxon 674 the base of the snout via dorsal flexion. The rostrum sampling was targeted to represent a mixture of disparate 675 was fractured a second time, after separation from the

Tensile and fatigue testing

Force-controlled loading to failure Five female spec-682 imens of each species were randomly allocated for use 683 in tensile testing. The head of each specimen was re-To illustrate the relative proportions of the cuticle re- 684 moved, cleaned, and prepared as described above in the gions in cross-section, serial semi-thin sectioning was con- 685 cold-fracture protocol. To avoid destroying the delicate, both species were collected into 95% ethanol for preser- 688 be clamped tightly into grips without risk of damage to

razor blade. The apical 1/4th of the rostrum was also 691 these were used as gripping and mounting points for the removed and then discarded. The remaining portion of 692 specimen. A strip of tape would be laid flat, with a large the rostrum and the head capsule were then embedded 693 drop of cyanoacrylate glue placed upon the upturned sur-694 face. The curved portion of the snout was then placed The cuticle was first immersed in acetone for 24 hours, 695 into the drop such that the straight portion of the ros-705 procedure was likewise repeated for the head capsule, re-A Leica Ultracut R Microtome and diamond knife were 706 sulting in a finished specimen with anterior and posterior

710 cuticle, simulating the condition of live tissue (see [37]). 765 assessed using both light microscopy and SEM to im-715 section of the snout was coated in petroleum jelly using a 770 croscope and attached computer running the software Le-716 cotton swab to prevent loss of moisture and stiffening of 771 ica Application Suite (LAS), as well as a Visionary Dig-₇₁₈ a Tryton 250 Microforce Testing System equipped with ₇₇₃ camera outfitted with interchangeable microptic lenses. 719 a 5N load cell and mechanical clamp grip. All specimens 774 Specimen length, layer thicknesses, macrofiber orienta-720 were subjected to force-controlled uniaxial tension at a 775 tion angles, and cross-sectional areas were assessed in the ₇₂₁ rate of 1.0 gf·s⁻¹ until failure, with a sampling interval ₇₇₆ Leica Application Suite and in Adobe Illustrator using 722 of 0.1s. Engineering stresses ($\sigma_0 = F/A_0$) and strains 777 pixel-wise measurements multiplied by a scaling factor $(\epsilon_0 = \Delta l/l_0)$ were reported only for specimens that did 778 for the image. not fracture due to strain accumulation at the interface between the rostrum and the cyanoacrylate handles.

Displacement-controlled cyclic loading To confirm 779 727 that repeated, complete extension of a strongly curved rostrum would not result in fracture of the cuticle, a rep-729 resentative female specimen of C. carvae was allocated for fatigue testing. The head capsule of the specimen was fixed to a push-pin using cyanoacrylate glue; this served as a pedestal and gripping location for the posterior portion of the specimen. The apex of the rostrum was fixed to a strip of ripstop nylon fabric equal in length to the head using cyanoacrylate glue. As with tensile testing, the specimen was placed in de-ionized water for 24 hours, then coated in petroleum jelly using a cotton swab immediately prior to load cycling.

The end of the fabric was gripped and used to elongate the snout in tension by pulling; in this way, the rostrum would return to its original configuration in a spring-like manner, as in living specimens, rather than being forced to return to the initial position. The snout was aligned such that complete elongation of the curved section would take place in tension with minimal off-axis deflection of the un-curved section. The specimen was subjected to displacement-controlled loading sufficient to fully extend the snout and generate a load stress of 1 N, or approximately 20% of the tensile strength of the species aver-₇₅₀ age. Load cycling took place at a rate of 0.33Hz, and was continued for 14 days (ca. 400K cycles), until the tensile stress in the sample approached an asymptotic minimum. Once the test was concluded, the specimen was placed

754 in a 50% ethanol solution for 24 hours to clean the petroleum jelly from the rostrum. The specimen was 756 examined for surface fractures and micro-tears, then sub-757 jected to tensile testing via the same protocol as the other 758 specimens to assess whether the cuticle had begun to fa-759 tigue.

Specimen imaging and microscopy

760

Once removed for testing, the specimen was gripped us- 766 age the fracture surfaces of the specimens in transverse ing the cyanoacrylate handles at the marked locations 767 view. Electron microscopy was conducted using a JEOL immediately beyond the anterior margin of the rostrum 768 JSM6300 scanning electron microscope, while light miand the posterior margin of the head capsule The exposed 769 croscopy was conducted using a Leica M205 C stereomithe specimen during the test. Specimens were loaded in 772 ital Passport II system using a Canon EOS Mark 5D II

Constitutive modeling of the cuticle

General Approach The effective uni-axial membrane 781 and transverse flexural elastic moduli of idealized cuti-782 cle organizations representing both the rostral apex and 783 head capsule were estimated using Classical Laminate 784 Plate Theory (CLPT); for general approach see [31, 32]). 785 The composite profiles of both types of cuticle were ide-786 alized using the layer thicknesses and stacking sequences observed in C. longinasus. This particular species was chosen because we derived the effective elastic constants 789 of the individual components of the cuticle in previous 790 work [1, 12]. In addition, C. longinasus exhibits a profile 791 that is typical and representative for the genus Curculio, 792 based on examination of the six species used for tensile 793 testing, as described previously.

For C. longinasus the total thickness of the cuticle 795 in the head and rostrum is roughly 50 µm, as in most 796 specimens of the other examined species. In the head 797 capsule, the exocuticle occupies between 30-50% of 798 the through-thickness of the laminate, with the re-799 maining thickness nearly evenly divided between 12 800 layers of endocuticle. We use the maximum (50%)801 of through-thickness, or 25 μm) for the model, since 802 the cuticle appears to deviate from this value only 803 in sulci (grooves), pores, and other scattered features 804 of surface sculpture. The macrofiber laminae of the 805 endocuticle were assigned a stacking sequence sequence of $806\ 0^{\circ}, 90^{\circ}, 30^{\circ}, -60^{\circ}, 60^{\circ}, -30^{\circ}, 90^{\circ}, 0^{\circ}, -60^{\circ}, 30^{\circ}, -30^{\circ}, 60^{\circ}$ 807 thereby representing pairs of orthogonal plies stacked at 808 a constant rotation angle of 30°, in approximation of the living tissue.

In the rostral apex, the exocuticle is reduced to a thin shell approximately 5 µm in thickness, or 10% of the total 812 cuticle thickness. The endocuticle displays a more com-813 plex pattern of layer thicknesses in the rostral apex than 814 in the head capsule. Each of the eight outermost layers are of nearly equal thickness to the exocuticle (5 µm), The fracture surfaces of cold-fractured specimens were 816 while the four innermost layers have a combined thickexamined using scanning electron microscopy to charac- 817 ness equal to that of the exocuticle or a single layer of terize the composite profile and microstructure of the ros- $_{818}$ outer endocuticle ($h_{outer} = 5 \,\mu\mathrm{m}, h_{inner} = 1.25 \,\mu\mathrm{m}$). The trum. Fracture behavior of tensile testing specimens was 819 stacking sequence with respect to the longitudinal axis $_{220}$ of the rostrum forms an antisymmetric [±45°] angle-ply $_{221}$ laminate.

To assess the individual contributions of layer thickness and stacking angle sequence to cuticle flexibility in the rostral apex, two hypothetical cuticle lay-ups were also modeled, each with only one of the modifications present in the cuticle of the rostral apex. The first of these models has the layer thicknesses of the rostral apex, but fiber orientations of the head capsule, while the second has the fiber orientations of the rostral apex, but the layer thicknesses of the head capsule.

Because these laminates are not symmetric, there exists for each a bending-extension coupling matrix [B]ists for each a bending-extension coupling matrix [B]populated with non-zero terms, thus complicating the calculation of effective in-plane elastic moduli. To cirists cumvent this difficulty and enable meaningful comparison between each laminate, all of the layups are reflected about their inner surface. This effectively doubles their thickness while producing a balanced, symmetric laminate with no coupling between bending and extension (i.e., $[B] = 0_{3,3}$). Estimation of in-plane elastic constants from the extension([A]) and bending ([D]) matrices is described in detail below; Matlab R2018b was used to numerically evaluate the final values of the effective elastic merically evaluate the final values of the effective elastic sequences.

Classical Laminate Plate Theory We begin by calculating the 2D reduced stiffness matrix for each part of the cuticle. For orthotropic materials with the principal axes parallel to the ply edges, the reduced stiffness matrix is defined as follows:

$$[Q] = \begin{bmatrix} Q_{11} & Q_{12} & 0 \\ Q_{21} & Q_{22} & 0 \\ 0 & 0 & Q_{66} \end{bmatrix} , \tag{1}$$

and where:

$$\begin{split} Q_{11} &= \frac{E_1}{1 - \nu_{12}\nu_{21}} \,, \\ Q_{12} &= \frac{E_1\nu_{21}}{1 - \nu_{12}\nu_{21}} = Q_{21} \,, \\ Q_{21} &= \frac{E_2\nu_{12}}{1 - \nu_{12}\nu_{21}} = Q_{12} \,, \\ Q_{22} &= \frac{E_2}{1 - \nu_{12}\nu_{21}} \,, \\ Q_{66} &= G_{12} \,. \end{split} \tag{2}$$

For each layer k, the reduced stiffness matrix is transformed to account for the layer orientation angle θ within the laminate coordinate system, yielding a reduced transformed stiffness matrix according to:

$$[\bar{Q}] = [T]^{-1}[Q][T]^{-T},$$
 (3)

where the transformation matrix [T] is defined as:

$$[T] = \begin{bmatrix} \cos^2 \theta & \sin^2 \theta & 2\cos\theta\sin\theta \\ \sin^2 \theta & \cos^2 \theta & -2\cos\theta\sin\theta \\ -\cos\theta\sin\theta & \cos\theta\sin\theta & \cos^2 \theta - \sin^2 \theta \end{bmatrix} . \quad (4)$$

Using the lay-ups specified for each type of cuticle described above, we calculate the extensional stiffness matrix [A], bending stiffness matrix [D], and bending-extension coupling matrix [B] for each laminate consisting of n layers at a distance z from the laminate mid-plane. The elements of these matrices can be found according to:

$$A_{ij} = \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k - z_{k-1}),$$

$$B_{ij} = \frac{1}{2} \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k^2 - z_{k-1}^2),$$

$$D_{ij} = \frac{1}{3} \sum_{k=1}^{n} (\bar{Q}_{ij})_k (z_k^3 - z_{k-1}^3).$$
(5)

These stiffness matrices relate vectors of resultant forces $\{N\}$ and bending moments $\{M\}$ to mid-surface strains and curvatures $\{\epsilon^{\circ}\}$ and $\{\kappa\}$, respectively, in the laminate according to the following relationship:

$${\{N\} \atop \{M\}} = \begin{bmatrix} [A] & [B] \\ [B] & [D] \end{bmatrix} {\{\epsilon^{\circ}\} \atop \{\kappa\}} .$$
 (6)

For symmetric laminates, $[B] = 0_{3,3}$, and therefore:

$$\{N\} = [A]\{\epsilon^{\circ}\}, \{M\} = [D]\{\kappa\},$$

$$(7)$$

or, in expanded form:

$$\begin{cases}
N_{xx} \\
N_{yy} \\
N_{xy}
\end{cases} = \begin{bmatrix}
A_{11} & A_{12} & A_{16} \\
A_{21} & A_{22} & A_{26} \\
A_{61} & A_{62} & A_{66}
\end{bmatrix} \begin{Bmatrix}
\epsilon_{xx}^{\circ} \\
\epsilon_{yy}^{\circ} \\
\gamma_{xy}^{\circ}
\end{Bmatrix},$$

$$\begin{cases}
M_{xx} \\
M_{yy} \\
M_{xy}
\end{Bmatrix} = \begin{bmatrix}
D_{11} & D_{12} & D_{16} \\
D_{21} & D_{22} & D_{26} \\
D_{61} & D_{62} & D_{66}
\end{bmatrix} \begin{Bmatrix}
\kappa_{xx} \\
\kappa_{yy} \\
\kappa_{xy}
\end{Bmatrix}.$$
(8)

If we make the simplifying assumptions (see [31, 32]) that (1) the laminate experiences pure axial loading and that (1) the laminate experiences pure axial loading and that transverse bending (i.e., $N_{yy} = N_{xy} = 0$ and $M_{yy} = 0$ that $M_{xy} = 0$, respectively) and (2) the laminate is a beam that $M_{xy} = 0$, respectively) and (2) the laminate is a beam that $M_{xy} = 0$, of sufficiently high aspect ratio to minimize the Poisson effect and anisotropic shear coupling (i.e., below we effectively let $M_{12} = M_{16}^* = 0$ and $M_{12} = M_{16}^* = 0$), then we can calculate the in-plane effective flexural and axial (3) s77 Young's moduli of the laminate along the x-axis.

For axial Young's modulus of the laminate, we first define the average membrane stresses in the laminate as:

$$\{\bar{\sigma}^m\} = \frac{\{N\}}{z_1 - z_n} \,.$$
 (9)

 $_{10}$ By substitution in Eq. 7, we find:

$$\begin{cases}
\bar{\sigma}_{xx}^{m} \\
\bar{\sigma}_{yy}^{m} \\
\bar{\tau}_{xy}^{m}
\end{cases} = \frac{1}{(z_{1} - z_{n})} \begin{bmatrix} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ A_{61} & A_{62} & A_{66} \end{bmatrix} \begin{Bmatrix} \epsilon_{xx}^{m} \\ \epsilon_{yy}^{m} \\ \gamma_{xy}^{m} \end{Bmatrix},$$
(10)

and, by inverting this equation (let $A^*=A^{-1}$) and substituting $A_{12}^*=A_{16}^*=0$ based on the assumptions above, we infer:

$$\epsilon_{xx}^{m} = (z_1 - z_n) A_{11}^* \bar{\sigma}_{xx}^{m} \,. \tag{11}$$

 884 We therefore define Young's modulus for effective axial 885 elasticity as:

$$E_{xx}^{m} = \frac{\bar{\sigma}_{xx}^{m}}{\epsilon_{xx}^{m}} = \frac{1}{(z_{1} - z_{k})A_{11}^{*}}$$
(12)

To find the transverse flexural Young's modulus of the laminate, we first specify the moment-curvature relation of an Euler-Bernoulli beam:

$$M = EI\kappa. (13)$$

 889 Along the x-axis, the second moment of area for a rect- 890 angular cross-section is:

$$I_{yy} = \frac{b(z_1 - z_n)^3}{12} \,, \tag{14}$$

Given the assumption that $M_{yy}=M_{xy}=0$, the moment along the x-axis is related to the moment of the beam by:

$$M = M_{xx}b. (15)$$

Thus, given the assumption that $D_{12}^* = D_{16}^* = 0$, so Young's modulus for the effective transverse flexural elasticity of the laminate can be found by making Eq. 13 specific to transverse flexure of the x-axis and rearranging the terms:

$$E_{xx}^f = \frac{12M_{xx}}{(z_1 - z_n)^3 \kappa_{xx}} \tag{16}$$

From inversion of Eq. 7 (let $D^* = D^{-1}$) this reduces 900 to:

$$E_{xx}^f = \frac{12}{(z_1 - z_n)^3 D_{11}^*} \tag{17}$$

Model selection and fitting In order to explore the 903 relationships between the composite structure and me-904 chanical properties of the cuticle, we fit phylogenetic linear mixed-effects models (PGLMM) to the tensile 906 testing data using maximum likelihood estimation [48– 907 51]. Raw data was processed using a custom script in Python version 3.5.2 [52]. Model exploration and fitting was conducted in R version 3.5.1 (2018-07-02) --"Feather Spray" using the 'nlme' and 'ape' pack-911 ages [53–55]. Response variables and covariates were 912 natural-log transformed, as needed, to ensure that the 913 normalized model residuals were normally distributed 914 [R:shapiro.test] and homoscedastic [R:levene.test], 915 using numerical and graphical analysis (see Supplemen-916 tary Data). In order to control for phylogenetic non- $_{917}$ independence in the data, we included the species of each 918 specimen as a random effect in all models. We also al-919 lowed for correlation in the error term of the models, 920 as specified by a variance-covariance matrix generated 921 from a Brownian motion [R: 'ape':corBrownian] model 922 of trait evolution along a phylogeny [54, 56].

The preferred phylogeny for North American Curculio is that of Bonal et al. [34]; this phylogeny was generated using Maximum-Likelihood methods and is untrametric, but has uniform internal branch lengths. The preferred tree was pruned to include only those species used in tenses sile testing, with a polytomy at each species to represent the individual specimens examined for that species; because the branch lengths of the tree were not specified, all branch lengths were set equal to 1. In general, phylogenetic regression is very robust with respect to missing or incomplete branch length data; underestimation of branch length causes overestimation of phylogenetic signal, which was not found to be statistically significant for any of our models, and we therefore believe that this procedure does not affect the findings of this study [56–58]

Other models of trait evolution were considered dur-940 ing model exploration, including Ornstein-Uhlenbeck (15) 941 [R:'ape':corMartins] and variable rate (AC/DC) 942 [R: 'ape':corBlomberg] models [54, 56]. However, nei-943 ther of these produced a significantly better fit to the 944 data than the Brownian motion model for any compar-945 ison, as measured by likelihood score and residual vari-946 ance, viz. R_{σ}^2 , and $R_{\beta*}^2$ [R:'r2glmm':r2beta] (see Sup-947 plementary Data). R_{σ}^2 is the proportion of generalized 948 variance explained by fixed effects, and is generally used 949 to compare between covariance structures [59–61]. $R_{\beta*}^2$ (16) 950 measures the multivariate association between the out-951 come and the fixed effects within a given correlation 952 structure, and is generally used to compare between fixed 953 effects [59–61]. We additionally estimated the phyloge-954 netic signal in the residual variance of each model using 955 two measures of spatial autocorrelation (Abouheif's C $_{956}$ and Moran's I) and two measures of phylogenetic sig-₉₅₇ nal (Pagel's λ and Blomberg's κ) using the R package 'phytools' [56, 62].

In all models, we tested whether the inclusion 999 960 of phylogenetic correlation in the model error pro- 1000 tween specimen stiffness and resistance to fracture. Specduced significantly better model fit, using a likelihood- 1001 imen stiffness was characterized using a low strain elasratio test [R:'lmtest':lrtest] and R_{σ}^2 -difference 1002 tic modulus (averaged across the first 33% of the stresstest [R:'r2glmm':r2beta(method='sgv')] between the 1003 strain curve) and the secant modulus at failure. Refully-specified model and a model lacking the phyloge- 1004 sistance to fracture was quantified in terms of ultimate netic effect [61, 63]. Models that incorporated covariance 1005 strain and fracture toughness (measured as area under 966 due to Brownian motion consistently produced a higher 1006 the stress-strain curve). Four models were fitted, two of 967 likelihood score and fit to the data; however, no model ex- 1007 which had ultimate strain as the response variable and hibited statistically significant phylogenetic signal in any 1008 two with fracture toughness as response variable. Each of the variables. Once models were fitted to the data, 1009 model then used one of the different measures of speci-T and F-statistics were calculated to determine whether 1010 men stiffness as a fixed effect. each cofactor was significantly different from zero.

men stiffness and resistance to fracture; and (3) examine 1017 as the fixed effect in both. whether snout length and flexibility are correlated.

To test the relationship between relative layer thicknesses and tensile strength, we fitted a fully-specified $_{1018}$ model with the cross-sectional area of exocuticle and endocuticle at the site of fracture as fixed effects, including an interaction term, and with maximum tensile force sustained prior to fracture as a response variable. This model was then compared to models with only crosssectional area of either endocuticle or exocuticle, but not both, as the sole fixed effect in the model. We then tested the whether one or both regions was significantly correlated to the maximum force sustained in tension by 1023 using likelihood-ratio tests and $R_{\beta*}^2$ -difference tests between each of the three models. We found that only the 1024 995 more parsimonious. The final model generated for our 1028 a PDF (Supplement 3). Raw and processed data will be 996 first aim featured the ratio of exocuticle to endocuticle 1029 provided by the corresponding author upon reasonable in cross-section as a fixed effect, with ultimate tensile 1030 request.

998 strength as the response variable.

For our second aim we examined the relationship be-

1011 Finally, in the third aim we explored whether a size-Hypothesis testing Our objectives for hypothesis test- 1012 effect might exist in the Curculio rostrum, particularly ing using the PGLMM's were threefold: (1) assess 1013 if longer (and typically more curved) rostra were more whether the altered ratio of exocuticle to endocuticle in 1014 flexible than shorter, straighter rostra. We generated two the rostral apex has an effect on the tensile strength of the 1015 models: the low strain and secant elastic moduli individsnout; (2) test whether a trade-off exists between speci- 1016 ually served as response variables, with specimen length

Code availability

R, Python, and Matlab scripts used to manipulate and 1020 analyze the raw data (as well as their outputs), produce 1021 figures, and estimate effective elastic constants is avail-1022 able from the corresponding author upon request.

Data availability

Stress-strain curves for all tensile and fatigue-tested cross-sectional area of endocuticle was a significant fixed 1025 specimens are provided as PDFs (Supplement 1). Diageffect, and therefore we elected to remove cross-sectional 1026 nostic plots for all PGLMMs are provided as PDFs (Suparea of exocuticle as a fixed effect to make the model 1027 plement 2). PGLMM terms and output are provided in

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