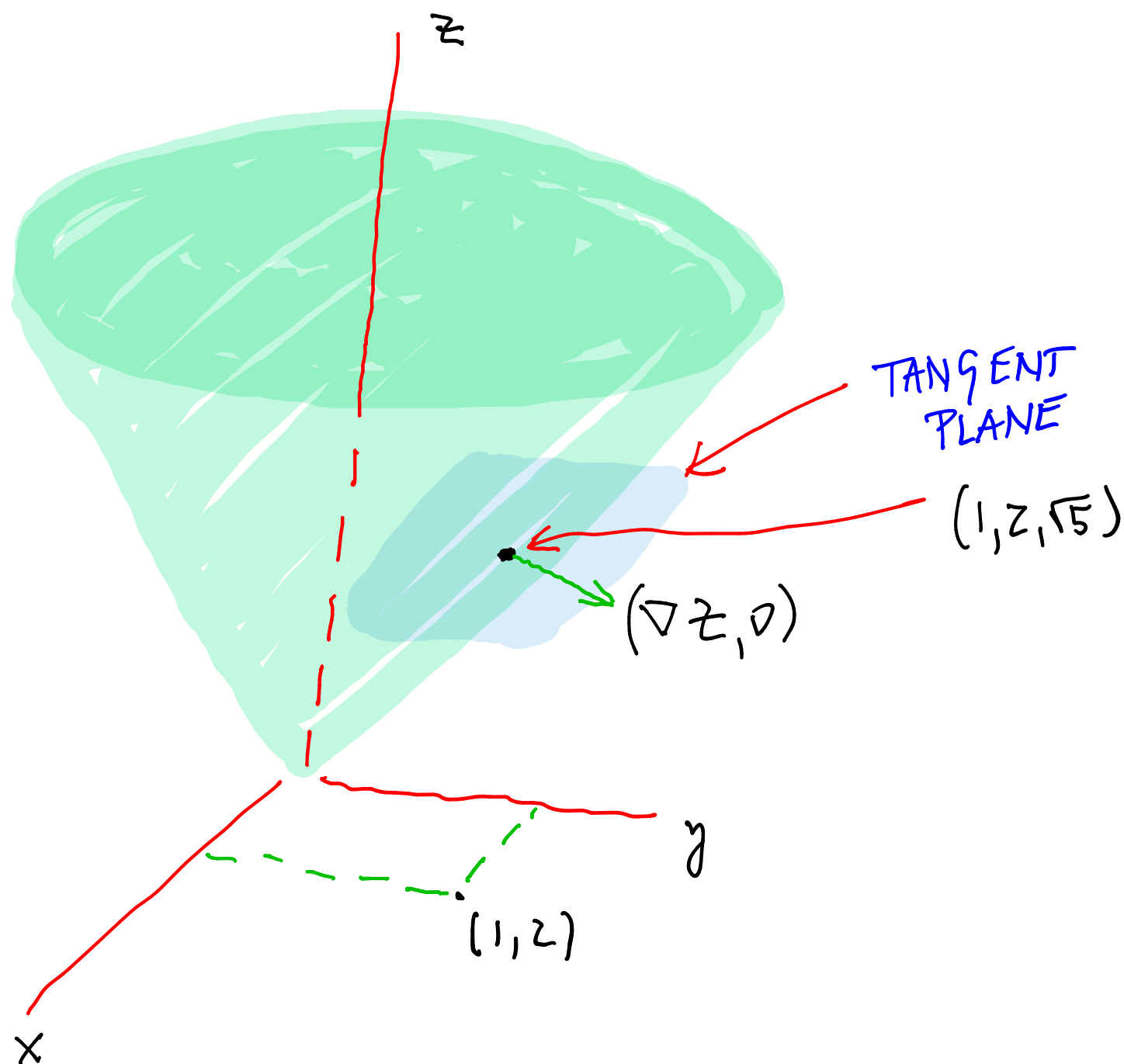


$$1.) \quad z = \sqrt{x^2 + y^2}$$



$$z_x = \frac{x}{\sqrt{x^2 + y^2}}$$

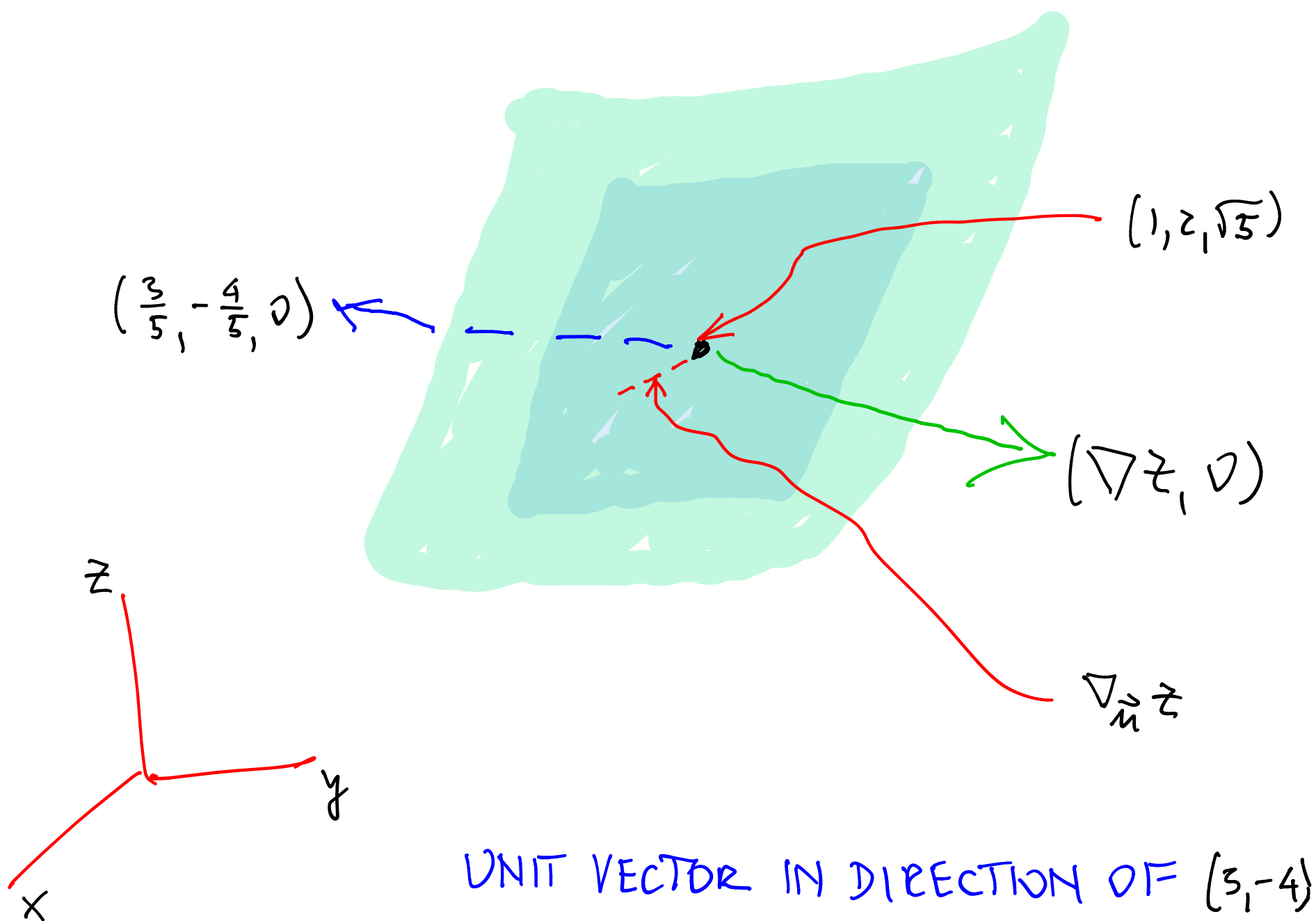
$$z_y = \frac{y}{\sqrt{x^2 + y^2}}$$

$$P = (1, 2) : z = \sqrt{5}, \quad z_x = \frac{1}{\sqrt{5}}, \quad z_y = \frac{2}{\sqrt{5}}$$

$$\text{TANGENT PLANE: } z = \sqrt{5} + \frac{1}{\sqrt{5}}(x-1) + \frac{2}{\sqrt{5}}(y-2)$$

$$x - 1 + 2y - 4 + 5 = \sqrt{5} z$$

$$x + 2y - \sqrt{5} z = 0$$



$$\vec{n} = \left( \frac{3}{5}, -\frac{4}{5} \right)$$

$$\begin{aligned} D_{\vec{n}} z(1, 2) &= \vec{n} \cdot \nabla z(1, 2) = \left( \frac{3}{5}, -\frac{4}{5} \right) \cdot \left( \frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}} \right) = \\ &= \frac{1}{5\sqrt{5}} (3 - 8) = -\frac{1}{\sqrt{5}} \end{aligned}$$

NONE OF THESE OBJECTS EXIST AT  $(0, 0)$  B/C

$z$  HAS A CORNER THERE.

$$2.) \quad z = f(x, y), \quad x = r \cos \theta, \quad y = r \sin \theta$$

$$z_r = z_x \cos \theta + z_y \sin \theta$$

$$z_\theta = -z_x r \sin \theta + z_y r \cos \theta$$

$$r z_r \cos \theta - z_\theta \sin \theta = r z_x$$

$$r z_r \sin \theta + z_\theta \cos \theta = r z_y$$

$$z_x = z_r \cos \theta - z_\theta \frac{\sin \theta}{r}$$

$$z_y = z_r \sin \theta + z_\theta \frac{\cos \theta}{r}$$

$$x z_x + y z_y = r \cos \theta \left( z_r \cos \theta - z_\theta \frac{\sin \theta}{r} \right) +$$

$$+ r \sin \theta \left( z_r \sin \theta + z_\theta \frac{\cos \theta}{r} \right) =$$

$$= r z_r$$