

Type Systems for Programming Languages

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Working draft of January 15, 2000

This is preliminary draft of a book in progress. Comments, suggestions, and corrections are welcome.

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