

Custom-Ebook

Team 13

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Operating_System_200_202

OPTIMIZATION OF DFA-BASED PATTERN MATCHERS 175 position of the leaf and also as a position of its symbol. Note that a symbol can have several positions; for instance, a has positions 1 and 3 in Fig. 3.56. The positions in the syntax tree correspond to the important states of the constructed NFA. Example 3.32 : Figure 3.57 shows the NFA for the same regular expression as Fig. 3.56, with the important states numbered and other states represented by letters. The numbered states in the NFA and the positions in the syntax tree correspond in a way we shall soon see. 2A B1 C2 DE 3 4 5 6 a b a b # ### ##### start # F Figure 3.57: NFA constructed by Algorithm 3.23 for (ajb)abb# 3.9.2 Functions Computed From the Syntax Tree To construct a DFA directly from a regular expression, we construct its syntax tree and then compute four functions: nullable, rstpos, lastpos, and followpos, defined as follows. Each definition refers to the syntax tree for a particular augmented regular expression (r)#. 1. nullable(n) is true for a syntax-tree node n if and only if the subexpression represented by n has in its language. That is, the subexpression can be "made null" or the empty string, even though there may be other strings it can represent as well. 2. rstpos(n) is the set of positions in the subtree rooted at n that correspond to the first symbol of at least one string in the language of the subexpression rooted at n. 3. lastpos(n) is the set of positions in the subtree rooted at n that correspond to the last symbol of at least one string in the language of the subexpression rooted at n. 176 CHAPTER 3. LEXICAL ANALYSIS 4. followpos(p), for a position p, is the set of positions q in the entire syntax tree such that there is some string $x = a_1 a_2 \dots a_n$ in $L(r)^\#$ such that for some i, there is a way to explain the membership of x in $L(r)^\#$ by matching a_i to position p of the syntax tree and a_{i+1} to position q. Example 3.33 : Consider the cat-node n in Fig. 3.56 that corresponds to the expression (ajb)a. We claim nullable(n) is false, since this node generates all strings of a's and b's ending in an a; it does not generate ϵ . On the other hand, the star-node below it is nullable; it generates along with all other strings of a's and b's. $\text{rstpos}(n) = \{1, 2, 3\}$. In a typical generated string like aa, the first position of the string corresponds to position 1 of the tree, and in a string like ba, the first position of the string comes from position 2 of the tree. However, when the string generated by the expression of node n is just a, then this a comes from position 3. $\text{lastpos}(n) = \{3\}$. That is, no matter what string is generated from the expression of node n, the last position is the a from position 3 of the tree. followpos is trickier to compute, but we shall see the rules for doing so shortly. Here is an example of the reasoning: $\text{followpos}(1) = \{1, 2, 3\}$. Consider a string ac, where the c is either a or b, and the a comes from position 1. That is, this a is one of those generated by the a in expression (ajb). This a could be followed by another a or b coming from the same subexpression, in which case c comes from position 1 or 2. It is also possible that this a is the last in the string generated by (ajb), in which case the symbol c must be the a that comes from position 3. Thus, 1, 2, and 3 are exactly the positions that can follow position 1. 23.9.3 Computing nullable, rstpos, and lastpos We can compute nullable, rstpos, and lastpos by a straightforward recursion on the height of the tree. The basis and inductive rules for nullable and rstpos are summarized in Fig. 3.58. The rules for lastpos are essentially the same as for rstpos, but the roles of children c1 and c2 must be swapped in the rule for a cat-node. Example 3.34 : Of all the nodes in Fig. 3.56 only the star-node is nullable. We note from the table of Fig. 3.58 that none of the leaves are nullable, because they each correspond to non- operands. The or-node is not nullable, because neither of its children is. The star-node is nullable, because every star-node is nullable. Finally, each of the cat-nodes, having at least one nonnullable child, is not nullable. The computation of rstpos and lastpos for each of the nodes is shown in Fig. 3.59, with rstpos(n) to the left of node n, and lastpos(n) to its right. Each of the leaves has only itself for rstpos and lastpos, as required by the rule for non- leaves in Fig. 3.58. For the or-node, we take the union of rstpos at the OPTIMIZATION OF DFA-BASED PATTERN MATCHERS 177

NODE n	nullable(n)	rstpos(n)	lastpos(n)
A leaf labeled true	true		
A leaf with position i	false	{i}	{i}
An or-node $n = c_1 \vee c_2$	$\text{nullable}(c_1) \vee \text{nullable}(c_2)$	$\text{rstpos}(c_1) \cup \text{rstpos}(c_2)$	$\text{lastpos}(c_1) \cup \text{lastpos}(c_2)$
A cat-node $n = c_1 c_2$	$\text{nullable}(c_1) \wedge \text{nullable}(c_2)$	$\text{rstpos}(c_1)$	$\text{lastpos}(c_2)$
A star-node $n = c^*$	true	$\text{rstpos}(c)$	$\text{lastpos}(c)$

$c1 \text{ true rstpos}(c1)$ Figure 3.58: Rules for computing nullable and rstposchildren and do the same for lastpos. The rule for the star-node says that we take the value of rstpos or lastpos at the one child of that node. Now, consider the lowest cat-node, which we shall call n . To compute $\text{rstpos}(n)$, we first consider whether the left operand is nullable, which it is in this case. Therefore, rstpos for n is the union of rstpos for each of its children, that is $f1; 2g \cup f3g = f1; 2; 3g$. The rule for lastpos does not appear explicitly in Fig. 3.58, but as we mentioned, the rules are the same as for rstpos , with the children interchanged. That is, to compute $\text{lastpos}(n)$ we must ask whether its right child (the leaf with position 3) is nullable, which it is not. Therefore, $\text{lastpos}(n)$ is the same as lastpos of the right child, or $f3g$.

23.9.4 Computing followpos

Finally, we need to see how to compute followpos. There are only two ways that a position of a regular expression can be made to follow another.

1. If n is a cat-node with left child $c1$ and right child $c2$, then for every position i in $\text{lastpos}(c1)$, all positions in $\text{rstpos}(c2)$ are in $\text{followpos}(i)$.
2. If n is a star-node, and i is a position in $\text{lastpos}(n)$, then all positions in $\text{rstpos}(n)$ are in $\text{followpos}(i)$.

Example 3.35 : Let us continue with our running example; recall that rstpos and lastpos were computed in Fig. 3.59. Rule 1 for followpos requires that we look at each cat-node, and put each position in rstpos of its right child in followpos for each position in lastpos of its left child. For the lowest cat-node in Fig. 3.59, that rule says position 3 is in $\text{followpos}(1)$ and $\text{followpos}(2)$. The next cat-node above says that 4 is in $\text{followpos}(3)$, and the remaining two cat-nodes give us 5 in $\text{followpos}(4)$ and 6 in $\text{followpos}(5)$.

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4.7. MORE POWERFUL LR PARSERS

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INIT PASS 1 PASS 2 PASS 3
 10: $S0! S \$ \$ \$ I1: S0! S \$ \$ \$ I2: S! L = R \$ \$ \$ R! L \$ \$ \$ I3: S! R \$ \$ \$ I4: L! R = =/\$ =/\$ =/\$ =/\$ =/\$ =/\$ =/\$ I5: L! id = =/\$ =/\$ =/\$ I6: S! L = R \$ I7: L! R = =/\$ =/\$ I8: R! L = =/\$ =/\$ I9: S! L = R \$$

Figure 4.47: Computation of lookahead

4.7.6 Compaction of LR Parsing Tables

A typical programming language grammar with 50 to 100 terminals and 100 productions may have an LALR parsing table with several hundred states. The action function may easily have 20,000 entries, each requiring at least 8 bits to encode. On small devices, a more efficient encoding than a two-dimensional array may be important. We shall mention briefly a few techniques that have been used to compress the ACTION and GOTO fields of an LR parsing table. One useful technique for compacting the action field is to recognize that usually many rows of the action table are identical. For example, in Fig. 4.42, states 0 and 3 have identical action entries, and so do 2 and 6. We can therefore save considerable space, at little cost in time, if we create a pointer for each state into a one-dimensional array. Pointers for states with the same actions point to the same location. To access information from this array, we assign each terminal a number from zero to one less than the number of terminals, and we use this integer as an offset from the pointer value for each state. In a given state, the parsing action for the i th terminal will be found i locations past the pointer value for that state. Further space efficiency can be achieved at the expense of a somewhat slower parser by creating a list for the actions of each state. The list consists of (terminal-symbol, action) pairs. The most frequent action for a state can be placed at the end of the list, and in place of a terminal we may use the notation $\backslash \text{any,}$ meaning that if the current input symbol has not been found so far on the list, we should do that action no matter what the input is. Moreover, error entries can safely be replaced by reduce actions, for further uniformity along a row. The errors will be detected later, before a shift move.

Example 4.65 : Consider the parsing table of Fig. 4.37. First, note that the actions for states 0, 4, 6, and 7 agree. We can represent them all by the list $\text{SYMBOL ACTION id } s5(s4 \text{ any error}$. State 1 has a similar list: $+ s6 \$ \text{acc any error}$. In state 2, we can replace the error entries by $r2$, so reduction by production 2 will occur on any input but $*$. Thus the list for state 2 is $s7 \text{any } r2$. State 3 has only error and $r4$ entries. We can replace the former by the latter, so the list for state 3 consists of only the pair (any, $r4$). States 5, 10, and 11 can be treated similarly. The list for state 8 is $+ s6) s11 \text{any error}$ and for state 9 $s7 \text{any } r12$. We can also encode the GOTO table by a list, but here it appears more efficient to make a list of pairs for each nonterminal A . Each pair on the list for A is of the form (currentState; nextState), indicating $\text{GOTO}[\text{currentState}; A] = \text{nextState}$.

MORE POWERFUL LR PARSERS 277 This technique is useful because there tend to be rather few states in any one column of the GOTO table. The reason is that the GOTO on nonterminal A can only be a state derivable from a set of items in which some items have A immediately to the left of a dot. No set has items with X and Y immediately to the left of a dot if $X \neq Y$. Thus, each state appears in at most one GOTO column. For more space reduction, we note that the error entries in the goto table are never consulted. We can therefore replace each error entry by the most common non-error entry in its column. This entry becomes the default; it is represented in the list for each column by one pair with any in place of current state. Example 4.66 : Consider Fig. 4.37 again. The column for F has entry 10 for state 7, and all other entries are either 3 or error. We may replace error by 3 and create for column F the list `CURRENTSTATE NEXTSTATE 7 10 any 3`. Similarly, a suitable list for column T is `any 2`. For column E we may choose either 1 or 8 to be the default; two entries are necessary in either case. For example, we might create for column E the list `4 8 any 12`. This space savings in these small examples may be misleading, because the total number of entries in the lists created in this example and the previous one together with the pointers from states to action lists and from nonterminals to next-state lists, result in unimpressive space savings over the matrix implementation of Fig. 4.37. For practical grammars, the space needed for the list representation is typically less than ten percent of that needed for the matrix representation. The table-compression methods for finite automata that were discussed in Section 3.9.8 can also be used to represent LR parsing tables.

4.7.7 Exercises for Section 4.7
Exercise 4.7.1 : Construct the a) canonical LR, and b) LALR sets of items for the grammar $S \rightarrow SS + j SS j a$ of Exercise 4.2.1.
Exercise 4.7.2 : Repeat Exercise 4.7.1 for each of the (augmented) grammars of Exercise 4.2.2(a)–(g).
Exercise 4.7.3 : For the grammar of Exercise 4.7.1, use Algorithm 4.63 to compute the collection of LALR sets of items from the kernels of the LR(0) sets of items.
Exercise 4.7.4 : Show that the following grammar $S \rightarrow A a j b A c j d c j b d a A$ is LALR(1) but not SLR(1).
Exercise 4.7.5 : Show that the following grammar $S \rightarrow A a j b A c j B c j b B a A$ is LR(1) but not LALR(1).

4.8 Using Ambiguous Grammars
It is a fact that every ambiguous grammar fails to be LR and thus is not in any of the classes of grammars discussed in the previous two sections. However, certain types of ambiguous grammars are quite useful in the specification and implementation of languages. For language constructs like expressions, an ambiguous grammar provides a shorter, more natural specification than any equivalent unambiguous grammar. Another use of ambiguous grammars is in isolating commonly occurring syntactic constructs for special-case optimization. With an ambiguous grammar, we can specify the special-case constructs by carefully adding new productions to the grammar. Although the grammars we use are ambiguous, in all cases we specify disambiguating rules that allow only one parse tree for each sentence. In this way, the overall language specification becomes unambiguous, and sometimes it becomes possible to design an LR parser that follows the same ambiguity-resolving choices. We stress that ambiguous constructs should be used sparingly and in a strictly controlled fashion; otherwise, there can be no guarantee as to what language is recognized by a parser.

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2.5. A TRANSLATOR FOR SIMPLE EXPRESSIONS 75

```
import java.io.*;
class Parser
{
    static int lookahead;
    public Parser() throws IOException { lookahead = System.in.read(); }
    void expr() throws IOException {
        term();
        while(true) {
            if( lookahead == '+' ) { match('+'); term(); }
            System.out.write('+');
        }
        else if( lookahead == '-' ) { match('-'); term(); System.out.write('-'); }
        else return;
    }
    void term() throws IOException {
        if( Character.isDigit((char)lookahead) )
            { System.out.write((char)lookahead); match(lookahead); }
        else throw new Error("syntax error");
    }
    void match(int t) throws IOException {
        if( lookahead == t ) lookahead = System.in.read();
        else throw new Error("syntax error");
    }
    public class Postfix {
        public static void main(String[] args) throws IOException {
            Parser parse = new Parser();
            parse.expr();
            System.out.write("\n");
        }
    }
}
```

Figure 2.27: Java program to translate infix expressions into postfix form

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DIRECTED TRANSLATOR A Few Salient Features of Java Those unfamiliar with Java may find the following notes on Java helpful in reading the code in Fig. 2.27: A class in Java consists of a sequence of variable and function definitions. Parentheses enclosing function parameter lists are needed even if there are no parameters; hence we write `expr()` and `term()`. These functions are actually procedures, because they do not return values, signified by the keyword `void` before the function name. Functions communicate either by passing parameters "by value" or by accessing shared data. For example, the functions `expr()` and `term()` examine the lookahead symbol using the class variable `lookahead` that they can all access since they all belong to the same class `Parser`. Like C, Java uses `=` for assignment, `==` for equality, and `!=` for inequality. The clause `"throws IOException"` in the definition of `term()` declares that an exception called `IOException` can occur. Such an exception occurs if there is no input to be read when the function `match` uses the routine `read`. Any function that calls `match` must also declare that an `IOException` can occur during its own execution.

2.6 Lexical Analysis

A lexical analyzer reads characters from the input and groups them into "token objects." Along with a terminal symbol that is used for parsing decisions, a token object carries additional information in the form of attribute values. So far, there has been no need to distinguish between the terms "token" and "terminal," since the parser ignores the attribute values that are carried by a token. In this section, a token is a terminal along with additional information. A sequence of input characters that comprises a single token is called a *lexeme*. Thus, we can say that the lexical analyzer insulates a parser from the lexeme representation of tokens. The lexical analyzer in this section allows numbers, identifiers, and "whitespace" (blanks, tabs, and newlines) to appear within expressions. It can be used to extend the expression translator of the previous section. Since the expression grammar of Fig. 2.21 must be extended to allow numbers and identifiers, we

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77 shall take this opportunity to allow multiplication and division as well. The extended translation scheme appears in Fig. 2.28.

```

expr ! expr + term f print(0+0) g
j expr - term f print(0-0) g
j term
term ! term * factor f print(0*0) g
j term / factor f print(0/0) g
j factor
factor ! ( expr ) j num f print(num:value) g
j id f print(id:lexeme) g

```

Figure 2.28: Actions for translating into postfix notation

In Fig. 2.28, the terminal `num` is assumed to have an attribute `num.value`, which gives the integer value corresponding to this occurrence of `num`. Terminal `id` has a string-valued attribute written as `id.lexeme`; we assume this string is the actual lexeme comprising this instance of the token `id`. The pseudocode fragments used to illustrate the workings of a lexical analyzer will be assembled into Java code at the end of this section. The approach in this section is suitable for hand-written lexical analyzers. Section 3.5 describes a tool called `Lex` that generates a lexical analyzer from a specification. Symbol tables or data structures for holding information about identifiers are considered in Section 2.7.

2.6.1 Removal of White Space and Comments

The expression translator in Section 2.5 sees every character in the input, so extraneous characters, such as blanks, will cause it to fail. Most languages allow arbitrary amounts of white space to appear between tokens. Comments are likewise ignored during parsing, so they may also be treated as white space. If white space is eliminated by the lexical analyzer, the parser will never have to consider it. The alternative of modifying the grammar to incorporate white space into the syntax is not nearly as easy to implement. The pseudocode in Fig. 2.29 skips white space by reading input characters as long as it sees a blank, a tab, or a newline. Variable `peek` holds the next input character. Line numbers and context are useful within error messages to help pinpoint errors; the code uses variable `line` to count newline characters in the input.

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```

for ( ; ; peek = next input character )
if ( peek is a blank or a tab ) do nothing;
else if ( peek is a newline ) line = line+1;
else break;

```

Figure 2.29: Skipping white space

2.6.2 Reading Ahead

A lexical analyzer may need to read ahead some characters before it can decide on the token to be returned to the parser. For example, a lexical analyzer for C or Java must read ahead after it sees the character `>`. If the next character is `=`, then `>` is part of the character sequence `>=`, the lexeme for the token for the "greater than or equal to" operator. Otherwise `>` itself forms the "greater than" operator, and the lexical analyzer has read one character too many. A general approach to reading ahead on the input, is to maintain an input buffer from which the lexical analyzer can read and push back characters. Input buffers can be justified on efficiency

grounds alone, since fetching a block of characters is usually more efficient than fetching one character at a time. A pointer keeps track of the portion of the input that has been analyzed; pushing back a character is implemented by moving back the pointer. Techniques for input buffering are discussed in Section 3.2. One-character read-ahead usually succeeds, so a simple solution is to use a variable, say `peek`, to hold the next input character. The lexical analyzer in this section reads ahead one character while it collects digits for numbers or characters for identifiers; e.g., it reads past 1 to distinguish between 1 and 10, and it reads past t to distinguish between t and true. The lexical analyzer reads ahead only when it must. An operator like * can be identified without reading ahead. In such cases, `peek` is set to a blank, which will be skipped when the lexical analyzer is called to find the next token. The invariant assertion in this section is that when the lexical analyzer returns a token, variable `peek` either holds the character beyond the lexeme for the current token, or it holds a blank.

2.6.3 Constants

Anytime a single digit appears in a grammar for expressions, it seems reasonable to allow an arbitrary integer constant in its place. Integer constants can be allowed either by creating a terminal symbol, say `num`, for such constants or by incorporating the syntax of integer constants into the grammar. The job of collecting characters into integers and computing their collective numerical value is generally given to a lexical analyzer, so numbers can be treated as single units during parsing and translation.