COL106: Data Structures. I semester, 2015-16. Minor I

2:30 PM to 3:30 PM, 1st September 2015.

Question	1	2	3	4	Total
	(4 marks)	(6 marks)	(6 marks)	(4 marks)	(20 marks)
Marks	4	CIT	0	4	13.5

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Write your answers on the printed question paper in the space provided. ROUGH SHEETS WILL NOT BE COLLECTED.

Q1. (Time Complexity and O-notation. Total marks = 4). Marks: $\[\]$ Suppose we have some already defined functions g(n) and h(n), consider the following function definition of the function f(n).

```
void f (int n)
{
    c = 1;
    for i = 1 to n
    {
        print g(i);
        if (i = c)
            then
        {
            print h(i);
            c = 2*c;
        }
    }
}
```

In the following we will assume that each assignment statement (e.g. c = 1) takes 1 unit of time, each time the for statement is run it takes 2 units of time, each a print statement is executed it takes 1 unit of time, and each multiplication takes 1 unit of time.

In each of the following questions you have to calculate the <u>exact</u> number of time units it takes for f(n) to run, and <u>also</u> write the time complexity in simplified big-Oh notation, e.g., if the number of time units turns out to be $3n^3 + 2\log n$, you must give the final answer as $O(n^3)$. Q1.1. (1.5 marks) Calculate the number of time units and time complexity of f(n), if g(i) takes i units of time and h(i) takes 1 unit of time.

time units

of $f(n) = \frac{1 + (i+4)n + 3log n}{1 + 4n + n(n+1) + 3log_2 n} = \frac{1}{2}n^2 + \frac{9}{2}n + 3log_2 n$ exity $0 (n^2)$

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Q1.2. (2.5 marks) Calculate the number of time units and time complexity of f(n), if g(i) [.] - g.i.

= 1 + 4m + log(n1) + 2log2n + 0 (rod (wi)) Time complexity

Q2. (Linked Lists. Total marks = 6).

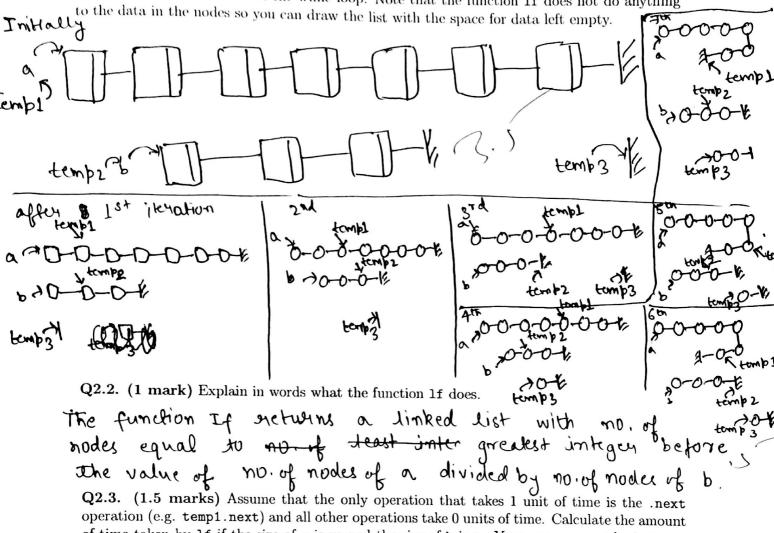
{

Consider the following function that takes two linked lists as input:

```
list lf (list a, list b)
   temp1 = a;
   if b = null
     then
       throw exception Ex;
     else
       temp2 = b;
  temp3 = null;
  while (temp1 not equal to null)
       if (temp2 = null)
          then
            x = new node;
            x.next = temp3;
            temp3 = x;
            temp2 = b;
       temp2 = temp2.next;
       temp1 = temp1.next;
  }
  return temp3;
```

}

Q2.1. (3.5 marks) Suppose we call 1f with the list a having 7 nodes and b having 3 nodes, show the state of the three lists (a, b, temp3) and the positions of the pointers temp1, temp2 at the end of each iteration of the while loop. Note that the function 1f does not do anything to the data in the nodes so you can draw the list with the second of the list with the



operation (e.g. temp1.next) and all other operations take 0 units of time. Calculate the amount of time taken by 1f if the size of a is m and the size of b is n. Your answer must be in terms of m and n. Calculate the exact number of steps and also give the answer in terms of big-oh notation.

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Q3. (Queues. 6 marks).

Marks: ()

A queue contains three types of characters R (red), W (white) and B (blue) in a jumbled up (assorted) fashion. The total number of characters is say n and n is known to you. Write an algorithm to arrange these characters in the queue such that all the R's come first, the W's come next, and B's come last in the queue. You may use one additional queue and one or two constant space variables if required. Your algorithm is not allowed to create or destroy any character of the input, it can only rearrange them. Please write your algorithm in plain English giving exact steps. No code or pseudocode. If you write code or pseudocode you automatically get 0.

Q4. (Trees. Total marks = 5)

Marks: 4

Suppose we are given a java implementation which has a Tree class and a Node class. The Tree class has the following methods available:

- public Node root(): This returns the root of the tree.
- public Boolean is Empty(): This returns 1 if the tree is empty, 0 otherwise.

The Node class has the following methods available:

- public int data(): This returns the integer data value stored in the node.
- public int no_children(): This returns the number of children of the node.
- public Node child(int i): This returns the Node of the *i*th child, returning null if there are less than *i* children.
- public Tree subtree(int i): This returns the Tree rooted at the *i*th child, returning an empty tree if there are less than *i* children.

Consider the following functions:

```
public int f1 (Tree T) {
     if (T.isEmpty()) {
        return 0;
     }
     else {
        Node curr = T.root();
        int temp = curr.data();
        if (temp < 0) \{ temp = 0; \}
        int i = 0;
        while (i < curr.no_children()) {
           temp = temp + f1(curr.subtree(i));
           i++;
        return temp;
    }
}
public int f2 (Tree T) {
     if (T.isEmpty()) {
        return 1;
     }
     else {
        Node curr = T.root();
        if (curr.no_children() > 2) {
```

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```
return 0;
}
else {
   int temp = 1;
   int i = 0;
   while (i < curr.no_children()) {</pre>
       if (temp > f2(curr.subtree(i)) {
          temp = 0;
       }
       else
          i++;
   }
   return temp;
}
```

Q4.1. (1.5 marks): Given a tree T explain in words what the function f1(T) outputs?

ILCT) gives the sum of all the non-revalues stores in that tree. (as each and every model is considered and the value is added to a counter if it is non-reg finally the wunter is returned)

Q4.2. (2.5 marks): Given a tree T explain in words what the function f2(T) outputs?

returns zero if not a binney so tree/subtree
For binney tree/subtree returns I