Major

Time: 120 min

$$R = 8.314 \text{J K}^{-1} \text{ mol}^{-1}$$
, $k = 1.381 \times 10^{-23} \,\text{m}^2 \,\text{kg} \,\text{s}^{-2} \,\text{K}^{-1}$, $1 \,\text{amu} = 1.661 \times 10^{-27} \,\text{kg}$

Consider the reaction $2A \xrightarrow{k} P$ at constant temperature and volume. Let the concentration of A, [A], be given in terms of a measurable property Z by $Z = B \exp(b[A]t)$ where B and b are constants depending only on temperature and t denotes the time.

- 1. (4 points) Express the rate of the reaction in terms of rate of variation of Z.
- **2.** (*4 points*) If the reaction is second order, obtain an expression for the specific rate constant *k* in terms of known quantities.

The steps of a proposed mechanism for the reaction $H_2 + Cl_2 \longrightarrow 2HCl$ is given below in arbitrary order. For your information, the bond dissociation energies of H_2 , HBr, HCl, Br₂, and Cl₂ are 432 kJ mol⁻¹, 363 kJ mol⁻¹, 428 kJ mol⁻¹, 190 kJ mol⁻¹, and 239 kJ mol⁻¹, respectively.

$$Cl' + Cl' + M \xrightarrow{k_1} Cl_2 + M \tag{1}$$

$$Cl' + H_2 \xrightarrow{k_2} H' + HCl$$
 (2)

$$Cl_2 + M \xrightarrow{k_3} Cl' + Cl' + M$$
 (3)

$$H' + Cl_2 \xrightarrow{k_4} Cl' + HCl \tag{4}$$

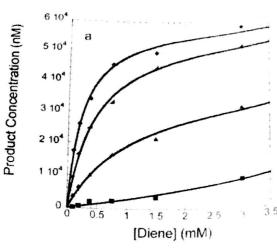
- 3. (4 points) Identify the initiation, propagation, and termination steps in this mechanism. In what way is this mechanism different from that of the $H_2 + Br_2$ reaction discussed in class?
- **4.** (3 points) The steady state approximation (SSA) is not applicable in this case. With the help of a figure for a model case, illustrate why the SSA might not be applicable here.
- **5.** (3 points) Under identical conditions do you expect this reaction to be faster or slower than the $H_2 + Br_2$ reaction? Why?
- **6.** (4 points) SSA is applicable when this reaction is conducted in the presence of around $1\% O_2$ or greater. Under these conditions the following termination steps dominate:

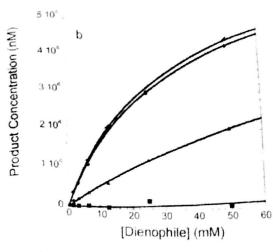
$$H' + O_2 + M \xrightarrow{k_5} HO_2 + M \tag{5}$$

$$Cl' + O_2 + M \xrightarrow{k_6} ClO_2 + M \tag{6}$$

Set up, but do not solve, the steady state approximation for all the relevant species when H_2 and Cl_2 react in the presence of O_2 .

In a recent paper Baker and coworkers computationally designed four enzymes to catalyze the reaction of a diene with a dienophile, the Diels-Alder reaction. The product concentration in 3.0 hour when the enzyme concentration is $10\,\mu\text{mol}$ is given below. In the figure on the left the dienophile concentration is fixed at $50\,\text{mmol}$, while on the right the diene concentration is fixed at $3\,\text{mmol}$. The different curves in the figure give the data for the four enzymes, denoted by different symbols.





- 7. (2 points) Identify (with the symbol) the most efficient enzyme in the figure on the left. Justify your answer.
- **8.** (3 points) List the steps involved to determine the kinetic parameters from data of the type given in the figure.

For the elementary reaction $CH_3 + H_2 \longrightarrow CH_4 + H$ at $T = 300 \,\text{K}$, the measured Arrhenius pre-exponential factor is $6.7 \times 10^{12} \, \text{cm}^3 \, \text{mol}^{-1} \, \text{s}^{-1}$ and activation energy is $40.7 \, \text{kJ} \, \text{mol}^{-1}$.

- **9.** (4 points) Calculate the steric or orientation factor, P, according to collision theory for this reaction at $T=300\,\mathrm{K}$. The cross sectional areas are $4.0\times10^{-19}\,\mathrm{m}^2$ for CH_3 and $2.7\times10^{-19}\,\mathrm{m}^2$ for $\mathrm{H_2}$. The average velocity is $\langle v \rangle = \sqrt{\frac{8kT}{\pi m}}$.
- 10. (4 points) What are the activation enthalpy and entropy for this reaction?
- 11. (5 points) Consider a surface-catalyzed bimolecular reaction between molecules A and B that has a rate law of the form $v = k_{\text{obs}}\theta_A\theta_B$ where θ_A is the fraction of surface sites occupied by reactant A and θ_B is the fraction of surface sites occupied by reactant B. A mechanism consistent with this reaction is as follows:

$$A(g) + S(s) \xrightarrow{k_d^A} A - S(s)$$
 fast equilibrium (7)

$$B(g) + S(s) \xrightarrow{k\frac{B}{q}} B - S(s) \qquad \text{fast equilibrium}$$
 (8)

$$A-S(s) + B-S(s) \xrightarrow{k_3} products$$
 (9)

Take K_A and K_B to be the equilibrium constants for equations 7 and 8, respectively. Derive an expression for θ_A in terms of p_A , p_B , K_A , and K_B .