NTJ UDESC

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1 Strings

1.1 Automato de Aho Corasick

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// Faz coisarada
 const int N = 3e5 + 5;
 struct AC {
     int N, P;
     const int A = 26;
     vector < vector < int >> next;
     vector < int > link, out_link;
     vector < int >> out;
     AC() : N(0), P(0) { node(); }
     int node() {
         next.emplace_back(A, 0);
         link.emplace_back(0);
         out_link.emplace_back(0);
         out.emplace_back(0);
         return N++;
     }
     inline int get(char c) { return c - 'a'; }
     int add_pattern(const string T) {
         int u = 0;
         for (auto c : T) {
             if (!next[u][get(c)]) next[u][get(c)] = node();
             u = next[u][get(c)];
         out[u].push_back(P);
         return P++;
     void compute() {
         queue < int > q;
         for (q.push(0); !q.empty();) {
             int u = q.front();
             q.pop();
             for (int c = 0; c < A; ++c) {</pre>
                  int v = next[u][c];
                  if (!v)
                      next[u][c] = next[link[u]][c];
                  else {
                      link[v] = u ? next[link[u]][c] : 0;
                      out_link[v] = out[link[v]].empty() ? out_link[link[v]] :
                         link[v];
                      q.push(v);
                 }
             }
         }
     }
     int advance(int u, char c) {
         while (u && !next[u][get(c)]) u = link[u];
         u = next[u][get(c)];
         return u;
 };
 /*
```

```
int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    auto st = clock();
    int t, cs = 0;
    cin >> t;
    while (t--) {
        int n;
        cin >> n;
        vector<string> v;
        for (int i = 0; i < n; i++) {
            string s;
            cin >> s;
            v.push_back(s);
        }
        sort(v.begin(), v.end());
        v.erase(unique(v.begin(), v.end()), v.end());
        AC aho;
        vector < int > len(n + 3, 0);
        for (auto s : v) {
            len[aho.add_pattern(s)] = s.size();
        aho.compute();
        string s;
        cin >> s;
        n = s.size();
        vector < int > dp(n, n + 10);
        int u = 0;
        for (int i = 0; i < n; i++) {
            char c = s[i];
            u = aho.advance(u, c);
            for (int v = u; v; v = aho.out_link[v]) {
                 for (auto p : aho.out[v]) {
                     dp[i] = min(dp[i], (i - len[p] >= 0 ? dp[i - len[p]] : 0)
                        + 1);
                 }
            }
        }
        cout << "Case " << ++cs << ": ";
        if (dp[n - 1] == n + 10) {
             cout << "impossible\n";</pre>
        } else {
            cout << dp[n - 1] << '\n';
    }
    cout << 1.0 * (clock() - st) / 1000 << '\n';</pre>
    return 0;
}
*/
```

1.2 Hashing

```
// Hashing estatico
// Tambem funciona com vector
//
// Build: O(n)
// Query (operator): O(1)
```

const int mods = 1;

```
typedef array<ll, mods> Hash; // array<T, mods>
template <typename obj = string, typename T = 11, typename U = __int128_t>
   struct Hashing {
    int N;
    bool inverse = 0;
    U p = 1001003;
    Hash mod{(T)1e18 + 9};
    array < vector < T > , mods > pw , hsh;
    void build(obj s, bool _inverse = 0) {
        inverse = _inverse;
        if (inverse) reverse(begin(s), end(s));
        N = size(s);
        for (int j = 0; j < mods; j++) {
            pw[j].resize(N), hsh[j].resize(N);
            pw[j][0] = 1;
            hsh[j][0] = s[0] \% mod[j];
            for (int i = 1; i < N; i++) {</pre>
                pw[j][i] = (U)pw[j][i - 1] * p % mod[j];
                hsh[j][i] = ((U)hsh[j][i - 1] * p + s[i]) % mod[j];
            }
        }
    }
    Hash operator()(int 1, int r) {
        if (inverse) {
            1 = N - 1 - 1, r = N - 1 - r;
            swap(1, r);
        Hash ans;
        for (int j = 0; j < mods; j++) {
            ans[j] = hsh[j][r];
            if (1 > 0) {
                ans[j] = (ans[j] - ((U)hsh[j][l - 1] * pw[j][r - l + 1] %
                    mod[j]) + mod[j]) % mod[j];
        return ans;
    }
};
// Hashing dinamico
// Hash que usa uma Fenwick pra updatar
//
// Build: O(n)
// Query (operator): O(log(n))
// Update: O(log(n))
const int mods = 1;
typedef array<11, mods> Hash; // array<T, mods>
template <typename obj = string, typename T = 11, typename U = __int128_t>
   struct Hashing {
    int N;
    bool inverse = 0;
    U p = 1001003;
    Hash mod{(11)1e18 + 9};
    array < vector < 11 > , mods > pw , hsh , inv;
    void build(obj s, bool _inverse = 0) {
        inverse = _inverse;
        if (inverse) reverse(begin(s), end(s));
```

```
N = size(s);
    for (int j = 0; j < mods; j++) {
        pw[j].resize(N + 1), hsh[j].resize(N + 1), inv[j].resize(N + 1);
        pw[j][1] = p;
        pw[j][0] = inv[j][0] = inv[j][1] = 1;
        U b = p;
        for (U e = mod[j] - 2; e > 0; e >>= 1, b = b * b % mod[j]) {
            if (e & 1) inv[j][1] = (U)inv[j][1] * b % mod[j];
        for (int i = 2; i <= N; i++) {</pre>
            inv[j][i] = (U)inv[j][i - 1] * inv[j][1] % mod[j];
            pw[j][i] = (U)pw[j][i - 1] * pw[j][1] % mod[j];
        hsh[j][1] = s[0] * pw[j][1] % mod[j];
        for (int i = 2; i <= N; i++) {</pre>
            hsh[j][i] = (U)s[i - 1] * pw[j][i] % mod[j];
        }
        for (int i = 1; i <= N; i++) {</pre>
            int u = i + (i & -i);
            if (u <= N) hsh[j][u] = (hsh[j][u] + hsh[j][i]) % mod[j];</pre>
        }
    }
}
Hash operator()(int 1, int r) {
    assert(1 <= r);</pre>
    if (inverse) {
        l = N - 1 - 1, r = N - 1 - r;
        swap(1, r);
    Hash ans;
    1 += 1, r += 1;
    for (int j = 0; j < mods; j++) {</pre>
        ans[j] = 0;
        for (int i = r; i > 0; i -= (i & -i)) {
            ans[j] = (ans[j] + hsh[j][i]) % mod[j];
        for (int i = 1 - 1; i > 0; i -= (i & -i)) {
            ans[j] = (ans[j] - hsh[j][i] + mod[j]) % mod[j];
        ans[j] = (U)ans[j] * inv[j][l - 1] % mod[j];
    }
    return ans;
void update(int idx, T val) {
    if (inverse) idx = N - 1 - idx;
    idx += 1;
    for (int j = 0; j < mods; j++) {
        T u = 0;
        for (int i = idx; i > 0; i -= (i & -i)) {
            u = (u + hsh[j][i]) \% mod[j];
        for (int i = idx - 1; i > 0; i -= (i & -i)) {
            u = (u - hsh[j][i] + mod[j]) \% mod[j];
        for (int i = idx; i <= N; i += (i & -i)) {</pre>
            hsh[j][i] = (hsh[j][i] - u + mod[j]) % mod[j];
        for (int i = idx; i <= N; i += (i & -i)) {</pre>
            hsh[j][i] = (hsh[j][i] + (U)val * pw[j][idx] % mod[j]) %
               mod[j];
        }
```

```
}
};
```

1.3 KMP

```
// Fonte: https://github.com/shahjalalshohag/code-library
// String matching
 const int N = 3e5 + 9;
 // returns the longest proper prefix array of pattern p
 // where lps[i]=longest proper prefix which is also suffix of p[0...i]
 vector<int> build_lps(string p) {
     int sz = p.size();
     vector < int > lps;
     lps.assign(sz + 1, 0);
     int j = 0;
     lps[0] = 0;
     for (int i = 1; i < sz; i++) {
         while (j \ge 0 \&\& p[i] != p[j]) {
             if (j >= 1)
                 j = lps[j - 1];
             else
                  j = -1;
         }
         j++;
         lps[i] = j;
     return lps;
 vector < int > ans;
 // returns matches in vector ans in 0-indexed
 void kmp(vector<int> lps, string s, string p) {
     int psz = p.size(), sz = s.size();
     int j = 0;
     for (int i = 0; i < sz; i++) {</pre>
         while (j \ge 0 \&\& p[j] != s[i])
             if (j >= 1)
                 j = lps[j - 1];
             else
                 j = -1;
         j++;
         if (j == psz) {
             j = lps[j - 1];
             // pattern found in string s at position i-psz+1
             ans.push_back(i - psz + 1);
         // after each loop we have j=longest common suffix of s[0..i] which is
         // also prefix of p
     }
 }
 /*
 int main() {
     int i, j, k, n, m, t;
     cin >> t;
     while (t--) {
```

```
string s, p;
         cin >> s >> p;
         vector < int > lps = build_lps(p);
         kmp(lps, s, p);
         if (ans.empty())
              cout << "Not Found\n";</pre>
         else {
             cout << ans.size() << endl;</pre>
              for (auto x : ans) cout << x << ', ';
              cout << endl;</pre>
         ans.clear();
         cout << endl;</pre>
    }
    return 0;
}
*/
```

1.4 Suffix Automaton

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// Faz coisarada
 const int N = 3e5 + 9;
 // len -> largest string length of the corresponding endpos-equivalent class
 // link -> longest suffix that is another endpos-equivalent class.
 // firstpos -> 1 indexed end position of the first occurrence of the largest
 // string of that node minlen(v) -> smallest string of node v = len(link(v))
 // terminal nodes -> store the suffixes
 struct SuffixAutomaton {
     struct node {
         int len, link, firstpos;
         map < char , int > nxt;
     };
     int sz, last;
     vector < node > t;
     vector < int > terminal;
     vector < long long > dp;
     vector < vector < int >> g;
     SuffixAutomaton() {}
     SuffixAutomaton(int n) {
         t.resize(2 * n);
         terminal.resize(2 * n, 0);
         dp.resize(2 * n, -1);
         sz = 1;
         last = 0;
         g.resize(2 * n);
         t[0].len = 0;
         t[0].link = -1;
         t[0].firstpos = 0;
     void extend(char c) {
         int p = last;
         if (t[p].nxt.count(c)) {
             int q = t[p].nxt[c];
             if (t[q].len == t[p].len + 1) {
```

```
return;
            }
            int clone = sz++;
            t[clone] = t[q];
            t[clone].len = t[p].len + 1;
            t[q].link = clone;
            last = clone;
            while (p != -1 && t[p].nxt[c] == q) {
                t[p].nxt[c] = clone;
                p = t[p].link;
            }
            return;
        }
        int cur = sz++;
        t[cur].len = t[last].len + 1;
        t[cur].firstpos = t[cur].len;
        p = last;
        while (p != -1 && !t[p].nxt.count(c)) {
            t[p].nxt[c] = cur;
            p = t[p].link;
        if (p == -1)
            t[cur].link = 0;
        else {
            int q = t[p].nxt[c];
            if (t[p].len + 1 == t[q].len)
                t[cur].link = q;
            else {
                int clone = sz++;
                t[clone] = t[q];
                t[clone].len = t[p].len + 1;
                while (p != -1 && t[p].nxt[c] == q) {
                    t[p].nxt[c] = clone;
                    p = t[p].link;
                t[q].link = t[cur].link = clone;
            }
        }
        last = cur;
    void build_tree() {
        for (int i = 1; i < sz; i++) g[t[i].link].push_back(i);</pre>
    void build(string &s) {
        for (auto x : s) {
            extend(x);
            terminal[last] = 1;
        }
        build_tree();
    long long cnt(int i) { // number of times i-th node occurs in the string
        if (dp[i] != -1) return dp[i];
        long long ret = terminal[i];
        for (auto &x : g[i]) ret += cnt(x);
        return dp[i] = ret;
    }
};
/*
int32_t main() {
```

last = q;

```
ios_base::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin >> t;
    while (t--) {
       string s;
        cin >> s;
        int n = s.size();
        SuffixAutomaton sa(n);
        sa.build(s);
        long long ans = 0; // number of unique substrings
        for (int i = 1; i < sa.sz; i++) ans += sa.t[i].len -
           sa.t[sa.t[i].link].len;
        cout << ans << '\n';
    }
    return 0;
}
*/
```

2 Problemas

2.1 Kth digito na string infinita de digitos

```
// Retorna qual o numero e qual o algarismo do Kth digito
// na string infinita dos numeros naturais (12345678910111213...)
// Complexidade: O(log_10(k))
pair<ll, ll> kthdig(ll k) {
     11 qtd = 1, num_alg = 1, base = 1;
     while (1) {
         11 add = (9 * base) * num_alg;
         if (qtd + add < k) {
             qtd += add;
         } else
             break;
         base *= 10, num_alg++;
     }
     ll algarismo = (k - qtd) % num_alg;
     ll numero = (k - qtd) / num_alg + base;
     return {numero, algarismo};
 }
```

3 Estruturas

3.1 Fenwick Tree

void merge(int t) {

```
// Processas queries de operacao com inverso
// Build: O(n)
// Query: 0(log(n))
// Update: O(log(n))
 typedef long long 11;
 struct fenwick {
     vector<ll> bit;
     fenwick(int n) { bit.assign(n + 1, 0); }
     fenwick(vector<ll> &v) {
         int n = v.size();
         bit.assign(n + 1, 0);
         for (int i = 1; i <= n; i++) bit[i] = v[i - 1];</pre>
         for (int i = 1; i <= n; i++) {</pre>
              int j = i + (i & -i);
             if (j <= n) bit[j] += bit[i];</pre>
     }
     11 query(int i) {
         11 res = 0;
         for (; i; i -= (i & -i)) res += bit[i];
         return res;
     11 query(int 1, int r) { return query(r) - query(1 - 1); }
     void update(int i, ll d) {
         for (; i && i < (int)bit.size(); i += (i & -i)) bit[i] += d;</pre>
 };
    Segment Tree Beats
// Faz coisarada
 const int MAXN = 200001; // 1-based
 int N;
 11 A[MAXN];
 struct Node {
     ll sum; // Sum tag
     11 max1; // Max value
     11 max2; // Second Max value
     ll maxc; // Max value count
     ll min1; // Min value
     11 min2; // Second Min value
     11 minc; // Min value count
     ll lazy; // Lazy tag
 } T[MAXN * 4];
```

T[t].sum = T[t << 1].sum + T[t << 1 | 1].sum;

```
// max
    if (T[t << 1].max1 == T[t << 1 | 1].max1) {
        T[t].max1 = T[t << 1].max1;
        T[t].max2 = max(T[t << 1].max2, T[t << 1 | 1].max2);
        T[t].maxc = T[t << 1].maxc + T[t << 1 | 1].maxc;
    } else {
        if (T[t << 1].max1 > T[t << 1 | 1].max1) {</pre>
            T[t].max1 = T[t << 1].max1;
            T[t].max2 = max(T[t << 1].max2, T[t << 1 | 1].max1);
            T[t].maxc = T[t << 1].maxc;</pre>
        } else {
            T[t].max1 = T[t << 1 | 1].max1;
            T[t].max2 = max(T[t << 1].max1, T[t << 1 | 1].max2);
            T[t].maxc = T[t << 1 | 1].maxc;
        }
    }
    // min
    if (T[t << 1].min1 == T[t << 1 | 1].min1) {</pre>
        T[t].min1 = T[t << 1].min1;
        T[t].min2 = min(T[t << 1].min2, T[t << 1 | 1].min2);
        T[t].minc = T[t << 1].minc + T[t << 1 | 1].minc;
    } else {
        if (T[t << 1].min1 < T[t << 1 | 1].min1) {</pre>
            T[t].min1 = T[t << 1].min1;
            T[t].min2 = min(T[t << 1].min2, T[t << 1 | 1].min1);
            T[t].minc = T[t << 1].minc;
        } else {
            T[t].min1 = T[t << 1 | 1].min1;
            T[t].min2 = min(T[t << 1].min1, T[t << 1 | 1].min2);
            T[t].minc = T[t << 1 | 1].minc;
        }
    }
}
void push_add(int t, int tl, int tr, ll v) {
    if (v == 0) {
        return;
    T[t].sum += (tr - tl + 1) * v;
    T[t].max1 += v;
    if (T[t].max2 != -11INF) {
        T[t].max2 += v;
    T[t].min1 += v;
    if (T[t].min2 != 11INF) {
        T[t].min2 += v;
    T[t].lazy += v;
}
// corresponds to a chmin update
void push_max(int t, ll v, bool l) {
    if (v >= T[t].max1) {
        return;
    }
    T[t].sum -= T[t].max1 * T[t].maxc;
    T[t].max1 = v;
    T[t].sum += T[t].max1 * T[t].maxc;
    if (1) {
        T[t].min1 = T[t].max1;
```

```
} else {
         if (v <= T[t].min1) {</pre>
             T[t].min1 = v;
         } else if (v < T[t].min2) {</pre>
             T[t].min2 = v;
         }
    }
}
// corresponds to a chmax update
void push_min(int t, ll v, bool l) {
    if (v <= T[t].min1) {</pre>
         return;
    }
    T[t].sum -= T[t].min1 * T[t].minc;
    T[t].min1 = v;
    T[t].sum += T[t].min1 * T[t].minc;
    if (1) {
        T[t].max1 = T[t].min1;
    } else {
        if (v >= T[t].max1) {
             T[t].max1 = v;
         } else if (v > T[t].max2) {
             T[t].max2 = v;
         }
    }
}
void pushdown(int t, int tl, int tr) {
    if (tl == tr) return;
    // sum
    int tm = (tl + tr) >> 1;
    push_add(t << 1, tl, tm, T[t].lazy);</pre>
    push_add(t << 1 | 1, tm + 1, tr, T[t].lazy);</pre>
    T[t].lazy = 0;
    // max
    push_max(t << 1, T[t].max1, tl == tm);</pre>
    push_max(t << 1 | 1, T[t].max1, tm + 1 == tr);</pre>
    // min
    push_min(t << 1, T[t].min1, tl == tm);</pre>
    push_min(t << 1 | 1, T[t].min1, tm + 1 == tr);</pre>
}
void build(int t = 1, int tl = 0, int tr = N - 1) {
    T[t].lazy = 0;
    if (tl == tr) {
        T[t].sum = T[t].max1 = T[t].min1 = A[t1];
         T[t].maxc = T[t].minc = 1;
         T[t].max2 = -11INF;
        T[t].min2 = 11INF;
         return;
    }
    int tm = (tl + tr) >> 1;
    build(t << 1, tl, tm);
build(t << 1 | 1, tm + 1, tr);</pre>
    merge(t);
}
```

```
void update_add(int 1, int r, ll v, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l) {</pre>
        return;
    }
    if (1 <= t1 && tr <= r) {</pre>
        push_add(t, tl, tr, v);
        return;
    }
    pushdown(t, tl, tr);
    int tm = (tl + tr) >> 1;
    update_add(1, r, v, t << 1, t1, tm);
    update_add(l, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}
void update_chmin(int 1, int r, ll v, int t = 1, int tl = 0, int tr = \mathbb{N} - 1) {
    if (r < tl || tr < l || v >= T[t].max1) {
        return;
    if (1 <= tl && tr <= r && v > T[t].max2) {
        push_max(t, v, tl == tr);
        return;
    pushdown(t, tl, tr);
    int tm = (tl + tr) >> 1;
    update_chmin(1, r, v, t << 1, t1, tm);
    update_chmin(l, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}
void update_chmax(int 1, int r, 11 v, int t = 1, int t1 = 0, int tr = N - 1) {
    if (r < tl || tr < l || v <= T[t].min1) {</pre>
        return;
    if (1 <= tl && tr <= r && v < T[t].min2) {</pre>
        push_min(t, v, tl == tr);
        return;
    pushdown(t, tl, tr);
    int tm = (tl + tr) >> 1;
    update_chmax(1, r, v, t << 1, t1, tm);
    update_chmax(1, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}
ll query_sum(int l, int r, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l) {</pre>
        return 0;
    }
    if (1 <= t1 && tr <= r) {</pre>
        return T[t].sum;
    pushdown(t, tl, tr);
    int tm = (tl + tr) >> 1;
    return query_sum(1, r, t << 1, tl, tm) + query_sum(1, r, t << 1 | 1, tm +
       1, tr);
}
```

```
/*
int main() {
    int Q;
    cin >> N >> Q;
    for (int i = 0; i < N; i++) {
        cin >> A[i];
    build();
    for (int q = 0; q < Q; q++) {
        int t;
        cin >> t;
        if (t == 0) \{
            int 1, r;
            11 x;
            cin >> 1 >> r >> x;
            update_chmin(l, r - 1, x);
        } else if (t == 1) {
            int 1, r;
            11 x;
            cin >> 1 >> r >> x;
            update_chmax(l, r - 1, x);
        } else if (t == 2) {
            int 1, r;
            11 x;
            cin >> 1 >> r >> x;
            update_add(l, r - 1, x);
        } else if (t == 3) {
            int 1, r;
            cin >> 1 >> r;
            cout << query_sum(1, r - 1) << '\n';</pre>
        }
   }
}
*/
```

4 Grafos

4.1 Binary Lifting

```
// Binary Lifting (em nodos)
//
// Computa LCA e tambem resolve queries de operacoes
// associativas e comutativas em caminhos.
//
// Build(): O(n log(n))
// Query(): O(log(n))
// Lca(): O(log(n))
//
// up[u][i] = (2 ^ i)-esimo pai do u
// st[u][i] = query ate (2 ^ i)-esimo pai do u (NAO INCLUI O U)
 const int maxn = 3e5 + 5, LG = 20;
vector < int > adj[maxn];
 struct BinaryLifting {
     int up[maxn][LG], st[maxn][LG], val[maxn], t = 1;
     int tin[maxn], tout[maxn];
     const int neutral = 0;
     int merge(int 1, int r) { return 1 + r; }
     void build(int u, int p = -1) {
         tin[u] = t++;
         for (int i = 0; i < LG - 1; i++) {</pre>
             up[u][i + 1] = up[up[u][i]][i];
             st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
         }
         for (int v : adj[u])
             if (v != p) {
                 up[v][0] = u, st[v][0] = val[u];
                 build(v, u);
         tout[u] = t++;
     void build(int root, vector<int> &v) {
         t = 1;
         int N = size(v);
         for (int i = 0; i < N; i++) val[i] = v[i];</pre>
         up[root][0] = root;
         st[root][0] = val[root];
         build(root);
     }
     bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=
        tout[v]; }
     int query2(int u, int v, bool include_lca) {
         if (ancestor(u, v)) return include_lca ? val[u] : neutral;
         int ans = val[u];
         for (int i = LG - 1; i >= 0; i--) {
             if (!ancestor(up[u][i], v)) {
                 ans = merge(ans, st[u][i]);
                 u = up[u][i];
             }
```

```
return include_lca ? merge(ans, st[u][0]) : ans;
    }
    int query(int u, int v) {
        if (u == v) return val[u];
        return merge(query2(u, v, 1), query2(v, u, 0));
    int lca(int u, int v) {
        if (ancestor(u, v)) return u;
        if (ancestor(v, u)) return v;
        for (int i = LG - 1; i >= 0; i--) {
            if (!ancestor(up[u][i], v)) {
                u = up[u][i];
        }
        return up[u][0];
    }
    int kth(int u, int k) {
        for (int i = 0; i < LG; i++) {</pre>
            if (k & (1 << i)) {</pre>
                u = up[u][i];
        }
        return u;
} b1;
// Binary Lifting (em arestas)
//
// up[u][i] = (2 ^ i)-esimo pai do u
// st[u][i] = query ate (2 ^ i)-esimo pai do u
const int maxn = 3e5 + 5, LG = 20;
vector<pair<int, int>> adj[maxn];
struct BinaryLifting {
    int up[maxn][LG], st[maxn][LG], t = 1;
    int tin[maxn], tout[maxn];
    const int neutral = 0;
    int merge(int 1, int r) { return 1 + r; }
    void build(int u, int p = -1) {
        tin[u] = t++;
        for (int i = 0; i < LG - 1; i++) {</pre>
            up[u][i + 1] = up[up[u][i]][i];
            st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
        for (auto [w, v] : adj[u])
            if (v != p) {
                up[v][0] = u, st[v][0] = w;
                build(v, u);
        tout[u] = t++;
    bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=
```

```
tout[v]; }
    int query2(int u, int v) {
        if (ancestor(u, v)) return neutral;
        int ans = neutral;
        for (int i = LG - 1; i >= 0; i--) {
            if (!ancestor(up[u][i], v)) {
                ans = merge(ans, st[u][i]);
                u = up[u][i];
            }
        }
        return merge(ans, st[u][0]);
    int query(int u, int v) {
        if (u == v) return neutral;
#warning TRATAR ESSE CASO ACIMA
        return merge(query2(u, v), query2(v, u));
    }
} b1;
// Binary Lifting para operacoes nao comutativas (em nodos)
// Levemente diferente do padrao
//
// Esse aqui resolve query de Kadani em arvore
// https://codeforces.com/contest/1843/problem/F2
const int maxn = 3e5 + 5, LG = 20;
vector < int > adj[maxn];
struct node {
    int pref, suff, sum, best;
const node neutral = {0, 0, 0, 0};
node new_node(int x) { return node{x, x, x, x}; }
node merge(node &1, node &r) {
    int pref = max(l.pref, l.sum + r.pref);
    int suff = max(r.suff, r.sum + l.suff);
    int sum = 1.sum + r.sum;
    int best = max(1.suff + r.pref, max(1.best, r.best));
    return node{pref, suff, sum, best};
struct BinaryLifting {
    int up[maxn][LG], val[maxn], t = 1;
    int tin[maxn], tout[maxn];
    node st[maxn][LG], st2[maxn][LG];
    void build(int u, int p = -1) {
        tin[u] = t++;
        for (int i = 0; i < LG - 1; i++) {
            up[u][i + 1] = up[up[u][i]][i];
            st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
            st2[u][i + 1] = merge(st2[up[u][i]][i], st2[u][i]);
        for (int v : adj[u])
            if (v != p) {
                up[v][0] = u;
                st[v][0] = new_node(val[u]);
```

```
st2[v][0] = new_node(val[u]);
                build(v, u);
            }
        tout[u] = t++;
    void build(int root, vector<int> &v) {
        int N = size(v);
        for (int i = 0; i < N; i++) val[i] = v[i];</pre>
        up[root][0] = root;
        st[root][0] = new_node(val[root]);
        st2[root][0] = new_node(val[u]);
        build(root);
    }
    bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=
       tout[v]; }
    node query2(int u, int v, bool include_lca, bool invert) {
        if (ancestor(u, v)) return include_lca ? new_node(val[u]) : neutral;
        node ans = new_node(val[u]);
        for (int i = LG - 1; i >= 0; i--) {
            if (!ancestor(up[u][i], v)) {
                if (invert)
                    ans = merge(st2[u][i], ans);
                    ans = merge(ans, st[u][i]);
                u = up[u][i];
            }
        if (!include_lca) return ans;
        return merge(ans, st[u][0]);
    }
    node query(int u, int v) {
        if (u == v) return new_node(val[u]);
        node l = query2(u, v, 1, 0);
        node r = query2(v, u, 0, 1);
        return merge(1, r);
    }
    int lca(int u, int v) {
        if (ancestor(u, v)) return u;
        if (ancestor(v, u)) return v;
        for (int i = LG - 1; i >= 0; i--) {
            if (!ancestor(up[u][i], v)) {
                u = up[u][i];
            }
        }
        return up[u][0];
    }
} bl, bl2;
```

4.2 Bridges e Edge Biconnected Components

```
// Acha todas as pontes em O(n) // Tambem constroi a arvore condensada, mantendo
```

```
// so as pontes como arestas e o resto comprimindo
// em nodos
//
// Salva no vetor bridges os pares {u, v} cujas arestas sao pontes
 typedef pair<int, int> ii;
 const int maxn = 2e5 + 5;
 int n, m;
 bool vis[maxn];
 int dp[maxn], dep[maxn];
 vector < int > adj[maxn];
 vector<ii> bridges;
 void dfs_dp(int u, int p = -1, int d = 0) {
     dp[u] = 0, dep[u] = d, vis[u] = 1;
     for (auto v : adj[u]) {
         if (v != p) {
             if (vis[v]) {
                  if (dep[v] < dep[u]) dp[v]--, dp[u]++;</pre>
             } else {
                  dfs_dp(v, u, d + 1);
                  dp[u] += dp[v];
             }
         }
     }
     if (dp[u] == 0 \&\& p != -1) { // edge {u, p} eh uma ponte}
         bridges.emplace_back(u, p);
     }
 }
 void find_bridges() {
     memset(vis, 0, n);
     for (int i = 0; i < n; i++) {</pre>
         if (!vis[i]) {
             dfs_dp(i);
         }
     }
 }
 // Edge Biconnected Components (requer todo codigo acima)
 int ebcc[maxn], ncc = 0;
 vector < int > adjbcc[maxn];
 void dfs_ebcc(int u, int p, int cc) {
     vis[u] = 1;
     if (dp[u] == 0 && p != -1) {
         cc = ++ncc;
     }
     ebcc[u] = cc;
     for (auto v : adj[u]) {
         if (!vis[v]) {
             dfs_ebcc(v, u, cc);
         }
     }
 }
 void build_ebcc_graph() {
     find_bridges();
     memset(vis, 0, n);
     for (int i = 0; i < n; i++) {</pre>
```

```
if (!vis[i]) {
            dfs_ebcc(i, -1, ncc);
            ++ncc;
        }
    // Opcao 1 - constroi o grafo condensado passando por todas as edges
    for (int u = 0; u < n; u++) {</pre>
        for (auto v : adj[u]) {
            if (ebcc[u] != ebcc[v]) {
                adjbcc[ebcc[u]].emplace_back(ebcc[v]);
            } else {
                // faz algo
            }
        }
    }
    // Opcao 2 - constroi o grafo condensado passando so pelas pontes
    for (auto [u, v] : bridges) {
        adjbcc[ebcc[u]].emplace_back(ebcc[v]);
        adjbcc[ebcc[v]].emplace_back(ebcc[u]);
    }
}
```

4.3 Dinic

```
// Fonte: https://github.com/shahjalalshohag/code-library
// Max Flow em O(V^3) ou O(E * sqrt(V)) em bipartido
 const int N = 5010;
 const long long inf = 1LL << 61;</pre>
 struct Dinic {
     struct edge {
         int to, rev;
         long long flow, w;
         int id;
     };
     int n, s, t, mxid;
     vector < int > d, flow_through;
     vector < int > done;
     vector < vector < edge >> g;
     Dinic() {}
     Dinic(int _n) {
         n = _n + 10;
         mxid = 0;
         g.resize(n);
     void add_edge(int u, int v, long long w, int id = -1) {
         edge a = {v, (int)g[v].size(), 0, w, id};
         edge b = \{u, (int)g[u].size(), 0, 0, -2\}; // for bidirectional edges
             cap(b) = w
         g[u].emplace_back(a);
         g[v].emplace_back(b);
         mxid = max(mxid, id);
     bool bfs() {
         d.assign(n, -1);
         d[s] = 0;
         queue < int > q;
```

```
q.push(s);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (auto &e : g[u]) {
                int v = e.to;
                 if (d[v] == -1 \&\& e.flow < e.w) d[v] = d[u] + 1, q.push(v);
            }
        }
        return d[t] != -1;
    long long dfs(int u, long long flow) {
        if (u == t) return flow;
        for (int &i = done[u]; i < (int)g[u].size(); i++) {</pre>
            edge &e = g[u][i];
            if (e.w <= e.flow) continue;</pre>
            int v = e.to;
            if (d[v] == d[u] + 1) {
                 long long nw = dfs(v, min(flow, e.w - e.flow));
                 if (nw > 0) {
                     e.flow += nw;
                     g[v][e.rev].flow -= nw;
                     return nw;
                 }
            }
        }
        return 0;
    long long max_flow(int _s, int _t) {
        s = _s;
        t = _t;
        long long flow = 0;
        while (bfs()) {
            done.assign(n, 0);
            while (long long nw = dfs(s, inf)) flow += nw;
        flow_through.assign(mxid + 10, 0);
        for (int i = 0; i < n; i++)</pre>
            for (auto e : g[i])
                 if (e.id >= 0) flow_through[e.id] = e.flow;
        return flow;
    }
};
/*
int main() {
    int n, m;
    cin >> n >> m;
    Dinic F(n + 1);
    for (int i = 1; i <= m; i++) {
        int u, v, w;
        cin >> u >> v >> w;
        F.add_edge(u, v, w);
    }
    cout << F.max_flow(1, n) << '\n';</pre>
    return 0;
*/
```

}

4.4 Pontos de articulação

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// O equivalente a pontes, em vertices
//
// Complexidade: O(n)
 const int N = 3e5 + 9;
 int T, low[N], dis[N], art[N];
 vector < int > g[N];
 void dfs(int u, int pre = 0) {
     low[u] = dis[u] = ++T;
     int child = 0;
     for (auto v : g[u]) {
         if (!dis[v]) {
             dfs(v, u);
             low[u] = min(low[u], low[v]);
             if (low[v] >= dis[u] && pre != 0) art[u] = 1;
             ++child;
         } else if (v != pre)
             low[u] = min(low[u], dis[v]);
     }
     if (pre == 0 && child > 1) art[u] = 1;
}
 /*
 int32_t main() {
     ios_base::sync_with_stdio(0);
     cin.tie(0);
     while (1) {
         int n, m;
         cin >> n >> m;
         if (!n) break;
         while (m--) {
             int u, v;
             cin >> u >> v;
             g[u].push_back(v);
             g[v].push_back(u);
         }
         dfs(1);
         int ans = 0;
         for (int i = 1; i <= n; i++) ans += art[i];
         cout << ans << '\n';
         T = 0;
         for (int i = 1; i \le n; i++) low[i] = dis[i] = art[i] = 0,
            g[i].clear();
     return 0;
 }
 */
```

5 Matematica

5.1 Crivo de Eratostenes

```
// Computa numeros primos entre [2, n] em O(n)
// Crivo linear computando spf (smallest prime factor) pra cada numero
// x entre [2, n] e phi(x) (funcao totiente)
// Complexidade: O(n)
 int spf[maxn], phi[maxn];
 vector < int > primes;
 void sieve(int n) {
     phi[1] = 1;
     for (int i = 2; i <= n; i++) {</pre>
         if (spf[i] == 0) {
              spf[i] = i;
              primes.emplace_back(i);
             phi[i] = i - 1;
         }
         for (int j = 0; j < (int)primes.size() && i * primes[j] <= n &&</pre>
             primes[j] <= spf[i]; j++) {</pre>
              spf[i * primes[j]] = primes[j];
              if (primes[j] < spf[i])</pre>
                  phi[i * primes[j]] = phi[i] * phi[primes[j]];
              else
                  phi[i * primes[j]] = phi[i] * primes[j];
         }
     }
 }
```

5.2 Fast Fourier Transform

```
// Fonte: https://github.com/ShahjalalShohag/code-library
//
// Faz convolucao de dois polinomios
// Complexidade: O(n log(n))
//
// Testado e sem erro de precisao para MAXN = 3e5 e A_i = 1e9
 const int N = 3e5 + 9;
 const double PI = acos(-1);
 struct base {
     double a, b;
     base(double a = 0, double b = 0) : a(a), b(b) {}
     const base operator+(const base &c) const { return base(a + c.a, b +
        c.b); }
     const base operator-(const base &c) const { return base(a - c.a, b -
        c.b); }
     const base operator*(const base &c) const { return base(a * c.a - b *
        c.b, a * c.b + b * c.a; }
 };
 void fft(vector < base > &p, bool inv = 0) {
     int n = p.size(), i = 0;
     for (int j = 1; j < n - 1; ++j) {
         for (int k = n >> 1; k > (i ^= k); k >>= 1)
         if (j < i) swap(p[i], p[j]);</pre>
```

```
for (int 1 = 1, m; (m = 1 << 1) <= n; 1 <<= 1) {
        double ang = 2 * PI / m;
        base wn = base(cos(ang), (inv ? 1. : -1.) * sin(ang)), w;
        for (int i = 0, j, k; i < n; i += m) {
            for (w = base(1, 0), j = i, k = i + 1; j < k; ++j, w = w * wn) {
                 base t = w * p[j + 1];
                 p[j + 1] = p[j] - t;
                 p[j] = p[j] + t;
            }
        }
    }
    if (inv)
        for (int i = 0; i < n; ++i) p[i].a /= n, p[i].b /= n;</pre>
}
vector < long long > multiply(vector < int > &a, vector < int > &b) {
    int n = a.size(), m = b.size(), t = n + m - 1, sz = 1;
    while (sz < t) sz <<= 1;</pre>
    vector < base > x(sz), y(sz), z(sz);
    for (int i = 0; i < sz; ++i) {</pre>
        x[i] = i < (int)a.size() ? base(a[i], 0) : base(0, 0);
        y[i] = i < (int)b.size() ? base(b[i], 0) : base(0, 0);
    fft(x), fft(y);
    for (int i = 0; i < sz; ++i) z[i] = x[i] * y[i];</pre>
    fft(z, 1);
    vector < long long > ret(sz);
    for (int i = 0; i < sz; ++i) ret[i] = (long long)round(z[i].a);</pre>
    while ((int)ret.size() > 1 && ret.back() == 0) ret.pop_back();
    return ret;
}
/*
long long ans[N];
int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    int n, x;
    cin >> n >> x;
    vector<int> a(n + 1, 0), b(n + 1, 0), c(n + 1, 0);
    int nw = 0;
    a[0]++;
    b[n]++;
    long long z = 0;
    for (int i = 1; i <= n; i++) {
        int k;
        cin >> k;
        nw += k < x;
        a[nw]++;
        b[-nw + n]++;
        z += c[nw] + !nw;
        c[nw]++;
    }
    auto res = multiply(a, b);
    for (int i = n + 1; i < res.size(); i++) {
        ans[i - n] += res[i];
    ans [0] = z;
    for (int i = 0; i <= n; i++) cout << ans[i] << ', ';
    cout << '\n';
    return 0;
```

} */

5.3 Pollard Rho

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// Fatora numeros ate 8*10^18
// Complexidade: O(n ^ (1/4))
 namespace PollardRho {
     mt19937 rnd(chrono::steady_clock::now().time_since_epoch().count());
     const int P = 1e6 + 9;
     11 seq[P];
     int primes[P], spf[P];
     inline ll add_mod(ll x, ll y, ll m) { return (x += y) < m ? x : x - m; }</pre>
     inline 11 mul_mod(11 x, 11 y, 11 m) {
         ll res = __int128(x) * y % m;
         return res;
         // ll res = x * y - (ll)((long double)x * y / m + 0.5) * m;
         // return res < 0 ? res + m : res;
     inline ll pow_mod(ll x, ll n, ll m) {
         ll res = 1 % m;
         for (; n; n >>= 1) {
             if (n & 1) res = mul_mod(res, x, m);
             x = mul_mod(x, x, m);
         }
         return res;
     // O(it * (logn)^3), it = number of rounds performed
     inline bool miller_rabin(ll n) {
         if (n <= 2 || (n & 1 ^ 1)) return (n == 2);</pre>
         if (n < P) return spf[n] == n;</pre>
         11 c, d, s = 0, r = n - 1;
         for (; !(r & 1); r >>= 1, s++) {
         }
         // each iteration is a round
         for (int i = 0; primes[i] < n && primes[i] < 32; i++) {</pre>
             c = pow_mod(primes[i], r, n);
             for (int j = 0; j < s; j++) {
                 d = mul_mod(c, c, n);
                 if (d == 1 && c != 1 && c != (n - 1)) return false;
                 c = d;
             }
             if (c != 1) return false;
         }
         return true;
     void init() {
         int cnt = 0;
         for (int i = 2; i < P; i++) {</pre>
             if (!spf[i]) primes[cnt++] = spf[i] = i;
             for (int j = 0, k; (k = i * primes[j]) < P; j++) {
                  spf[k] = primes[j];
                  if (spf[i] == spf[k]) break;
             }
         }
     }
```

```
// returns O(n^{(1/4)})
    11 pollard_rho(ll n) {
        while (1) {
            ll x = rnd() % n, y = x, c = rnd() % n, u = 1, v, t = 0;
            11 *px = seq, *py = seq;
            while (1) {
                *py++ = y = add_mod(mul_mod(y, y, n), c, n);
                 *py++ = y = add_mod(mul_mod(y, y, n), c, n);
                if ((x = *px++) == y) break;
                v = u;
                u = mul_mod(u, abs(y - x), n);
                if (!u) return __gcd(v, n);
                if (++t == 32) {
                     t = 0;
                     if ((u = \_gcd(u, n)) > 1 && u < n) return u;
                }
            }
            if (t && (u = __gcd(u, n)) > 1 && u < n) return u;</pre>
        }
    }
    vector<ll> factorize(ll n) {
        if (n == 1) return vector<ll>();
        if (miller_rabin(n)) return vector<ll>{n};
        vector < ll> v, w;
        while (n > 1 \&\& n < P) {
            v.push_back(spf[n]);
            n /= spf[n];
        if (n >= P) {
            11 x = pollard_rho(n);
            v = factorize(x);
            w = factorize(n / x);
            v.insert(v.end(), w.begin(), w.end());
        return v;
    }
} // namespace PollardRho
int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    PollardRho::init();
    int t;
    cin >> t;
    while (t--) {
        11 n;
        cin >> n;
        auto f = PollardRho::factorize(n);
        sort(f.begin(), f.end());
        cout << f.size() << ', ';</pre>
        for (auto x : f) cout << x << '';
        cout << '\n';
    return 0;
*/
```

6 Geometria

6.1 Convex Hull

```
// Algoritmo Graham's Scan
// Complexidade: O(n log(n))
 bool ccw(pt &p, pt &a, pt &b, bool collinear = 0) {
     pt p1 = a - p;
     pt p2 = b - p;
     return collinear ? (p2 ^ p1) <= 0 : (p2 ^ p1) < 0;</pre>
 }
 vector<pt> convex_hull(vector<pt> v, bool collinear = 0) {
     int n = size(v);
     pt p0 = v[0];
     for (int i = 1; i < n; i++) {</pre>
         if (v[i] < p0) p0 = v[i];</pre>
     sort(begin(v), end(v), [\&](pt \&1, pt \&r) { // sorta clockwise}
         pt p1 = 1 - p0;
         pt p2 = r - p0;
         ll c1 = p1 ^
                      p2;
         return c1 < 0 || ((c1 == 0) && p0.dist2(1) < p0.dist2(r));</pre>
     });
     if (collinear) {
         for (int i = n - 2; i \ge 0; i--) { // reverte o ultimo lado do
             poligono
              if (ccw(v[0], v[n - 1], v[i])) {
                  reverse(begin(v) + i + 1, end(v));
                  break;
              }
         }
     }
     vector < pt > ch { p0, v[1] };
     for (int i = 2; i < n; i++) {</pre>
         while (ch.size() > 2 \&\& (ccw(ch.end()[-2], ch.end()[-1], v[i],
             !collinear))) ch.pop_back();
         ch.emplace_back(v[i]);
     }
     return ch;
 }
    Ponto (Inteiro)
6.2
// Ponto com coordenadas inteiras e alguns metodos
 struct pt {
     11 x, y;
     pt() : x(0), y(0) {}
     pt(ll _x, ll _y) : x(_x), y(_y) {}
     pt operator*(const pt &a, const ll &b) { return pt(b * a.x, b * a.y); }
     pt operator-(const pt &a, const pt &b) { return pt(a.x - b.x, a.y - b.y);
        }
```

```
pt operator+(const pt &a, const pt &b) { return pt(a.x + b.x, a.y + b.y);
       }
    11 operator*(const pt &a, const pt &b) { return a.x * b.x + a.y * b.y; }
    11 operator^(const pt &a, const pt &b) { return a.x * b.y - a.y * b.x; }
    bool operator<(const pt &p) {</pre>
        if (x == p.x) return y < p.y;</pre>
        return x < p.x;</pre>
    11 dist2(const pt &p) {
        11 dx = x - p.x;
        11 dy = y - p.y;
        return dx * dx + dy * dy;
    }
    friend ostream &operator << (ostream &out, const pt &a) { return out << "("
      << a.x << "," << a.y << ")"; }
    friend istream &operator>>(istream &in, pt &a) { return in >> a.x >> a.y;
};
```

7 Extra

7.1 Config do Vim

```
// .vimrc

set nu
set ai
set ts=4
set sw=4
filetype plugin indent on
inoremap {} {}<Left><Return><Up><End><Return>

set nohls
set belloff=all
syntax on
set expandtab
set noshiftround
set showmode
set showcmd
```

7.2 Custom Hash

7.3 Gerador aleatorio de inteiros em [l, r]

```
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());

ll uniform(ll l, ll r) {
    uniform_int_distribution<int> uid(l, r);
    return uid(rng);
}
```

7.4 Mint

```
// Inteiro automaticamente modulado
const int mod = 998244353;
```

```
struct Mint {
    int val:
     Mint(int v = 0) { val = v % mod; }
     bool operator == (Mint o) { return val == o.val; }
     int operator*(Mint o) { return (((11)val * o.val) % mod); }
     int operator+(Mint o) { return ((11)val + o.val) % mod; }
     int operator-(Mint o) { return ((11)val - o.val + mod) % mod; }
     int operator^(ll o) { return pwr(val, o); }
     int pwr(Mint b, ll e) {
         Mint res;
         for (res = 1; e; e >>= 1, b = b * b)
             if (e & 1) res = res * res;
         return res.val;
     }
 };
7.5
    Rand C++
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
7.6 Script de stress test
 set -e
 g++-02 code.cpp -o code
 g++ -02 brute.cpp -o brute
 g++ -02 gen.cpp -o gen
 for((i = 1; ; ++i)); do
     ./gen > input_file
     ./code < input_file > myAnswer
     ./brute < input_file > correctAnswer
     diff myAnswer correctAnswer > /dev/null || break
     echo "Passed test: " $i
 done
 echo "WA on the following test:"
 cat input_file
 echo "Your answer is:"
 cat myAnswer
 echo "Correct answer is:"
 cat correctAnswer
7.7
    Script pra rodar C++
// chmod +x run
// ./run A.cpp
 #!/bin/bash
 g++ --std=c++20 -Wall -O2 -DNTJ -fsanitize=address, undefined $1 && ./a.out
     Template C++
7.8
 #include <bits/stdc++.h>
 #define endl '\n'
```

```
using namespace std;
typedef long long ll;

void solve() {}

signed main() {
   ios_base::sync_with_stdio(0);
   cin.tie(0);
   solve();
}
```

7.9 Template de debug simples

```
void _print() {}
template <typename T, typename... U> void _print(T a, U... b) {
    if (sizeof...(b)) {
        cerr << a << ", ";
        _print(b...);
    } else
        cerr << a;
}
#ifdef NTJ
#define debug(x...) cerr << "[" << #x << "] = [", _print(x), cerr << "]" << endl
#else
#define debug(...)
#endif</pre>
```