

NTJ UDESC

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Índice

1	Strings	3
1.1	Automato de Aho Corasick	3
1.2	Hashing	4
1.3	KMP	7
1.4	Suffix Automaton	8
2	Problemas	11
2.1	Kth digito na string infinita de digitos	11
3	Estruturas	12
3.1	Fenwick Tree	12
3.2	Segment Tree Beats	12
4	Grafos	17
4.1	Binary Lifting	17
4.2	Bridges e Edge Biconnected Components	20
4.3	Dinic	22
4.4	Pontos de articulacao	24
5	Matematica	25
5.1	Crivo de Eratostenes	25
5.2	Fast Fourier Transform	25
5.3	Pollard Rho	27
6	Geometria	29
6.1	Convex Hull	29
6.2	Ponto (Inteiro)	29

7	Extra	31
7.1	Config do Vim	31
7.2	Custom Hash	31
7.3	Gerador aleatorio de inteiros em $[l, r]$	31
7.4	Mint	31
7.5	Rand C++	32
7.6	Script de stress test	32
7.7	Script pra rodar C++	32
7.8	Template C++	32
7.9	Template de debug simples	33

1 Strings

1.1 Automato de Aho Corasick

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// Faz coisarada

const int N = 3e5 + 5;

struct AC {
    int N, P;
    const int A = 26;
    vector<vector<int>> next;
    vector<int> link, out_link;
    vector<vector<int>> out;
    AC() : N(0), P(0) { node(); }
    int node() {
        next.emplace_back(A, 0);
        link.emplace_back(0);
        out_link.emplace_back(0);
        out.emplace_back(0);
        return N++;
    }
    inline int get(char c) { return c - 'a'; }
    int add_pattern(const string T) {
        int u = 0;
        for (auto c : T) {
            if (!next[u][get(c)]) next[u][get(c)] = node();
            u = next[u][get(c)];
        }
        out[u].push_back(P);
        return P++;
    }
    void compute() {
        queue<int> q;
        for (q.push(0); !q.empty(); ) {
            int u = q.front();
            q.pop();
            for (int c = 0; c < A; ++c) {
                int v = next[u][c];
                if (!v)
                    next[u][c] = next[link[u]][c];
                else {
                    link[v] = u ? next[link[u]][c] : 0;
                    out_link[v] = out[link[v]].empty() ? out_link[link[v]] :
                        link[v];
                    q.push(v);
                }
            }
        }
    }
    int advance(int u, char c) {
        while (u && !next[u][get(c)]) u = link[u];
        u = next[u][get(c)];
        return u;
    }
};

int32_t main() {
```

```

ios_base::sync_with_stdio(0);
cin.tie(0);
auto st = clock();
int t, cs = 0;
cin >> t;
while (t--) {
    int n;
    cin >> n;
    vector<string> v;
    for (int i = 0; i < n; i++) {
        string s;
        cin >> s;
        v.push_back(s);
    }
    sort(v.begin(), v.end());
    v.erase(unique(v.begin(), v.end()), v.end());
    AC aho;
    vector<int> len(n + 3, 0);
    for (auto s : v) {
        len[aho.add_pattern(s)] = s.size();
    }
    aho.compute();
    string s;
    cin >> s;
    n = s.size();
    vector<int> dp(n, n + 10);
    int u = 0;
    for (int i = 0; i < n; i++) {
        char c = s[i];
        u = aho.advance(u, c);
        for (int v = u; v; v = aho.out_link[v]) {
            for (auto p : aho.out[v]) {
                dp[i] = min(dp[i], (i - len[p] >= 0 ? dp[i - len[p]] : 0)
                    + 1);
            }
        }
    }
    cout << "Case " << ++cs << ": ";
    if (dp[n - 1] == n + 10) {
        cout << "impossible\n";
    } else {
        cout << dp[n - 1] << '\n';
    }
}
cout << 1.0 * (clock() - st) / 1000 << '\n';
return 0;
}

```

1.2 Hashing

```

// Hashing estatico
// Tambem funciona com vector
//
// Build: O(n)
// Query (operator): O(1)

const int mods = 1;
typedef array<ll, mods> Hash; // array<T, mods>

```

```

template <typename obj = string, typename T = ll, typename U = __int128_t>
struct Hashing {
    int N;
    bool inverse = 0;
    U p = 1001003;
    Hash mod{(T)1e18 + 9};
    array<vector<T>, mods> pw, hsh;
    void build(obj s, bool _inverse = 0) {
        inverse = _inverse;
        if (inverse) reverse(begin(s), end(s));
        N = size(s);
        for (int j = 0; j < mods; j++) {
            pw[j].resize(N), hsh[j].resize(N);
            pw[j][0] = 1;
            hsh[j][0] = s[0] % mod[j];
            for (int i = 1; i < N; i++) {
                pw[j][i] = (U)pw[j][i - 1] * p % mod[j];
                hsh[j][i] = ((U)hsh[j][i - 1] * p + s[i]) % mod[j];
            }
        }
    }
    Hash operator()(int l, int r) {
        if (inverse) {
            l = N - 1 - l, r = N - 1 - r;
            swap(l, r);
        }
        Hash ans;
        for (int j = 0; j < mods; j++) {
            ans[j] = hsh[j][r];
            if (l > 0) {
                ans[j] = (ans[j] - ((U)hsh[j][l - 1] * pw[j][r - l + 1] %
                    mod[j]) + mod[j]) % mod[j];
            }
        }
        return ans;
    }
};

// Hashing dinamico
//
// Hash que usa uma Fenwick pra updatar
//
// Build: O(n)
// Query (operator): O(log(n))
// Update: O(log(n))

```

```

const int mods = 1;
typedef array<ll, mods> Hash; // array<T, mods>

```

```

template <typename obj = string, typename T = ll, typename U = __int128_t>
struct Hashing {
    int N;
    bool inverse = 0;
    U p = 1001003;
    Hash mod{(ll)1e18 + 9};
    array<vector<ll>, mods> pw, hsh, inv;
    void build(obj s, bool _inverse = 0) {
        inverse = _inverse;
        if (inverse) reverse(begin(s), end(s));
        N = size(s);
        for (int j = 0; j < mods; j++) {

```

```

        pw[j].resize(N + 1), hsh[j].resize(N + 1), inv[j].resize(N + 1);
        pw[j][1] = p;
        pw[j][0] = inv[j][0] = inv[j][1] = 1;
        U b = p;
        for (U e = mod[j] - 2; e > 0; e >>= 1, b = b * b % mod[j]) {
            if (e & 1) inv[j][1] = (U)inv[j][1] * b % mod[j];
        }
        for (int i = 2; i <= N; i++) {
            inv[j][i] = (U)inv[j][i - 1] * inv[j][1] % mod[j];
            pw[j][i] = (U)pw[j][i - 1] * pw[j][1] % mod[j];
        }
        hsh[j][1] = s[0] * pw[j][1] % mod[j];
        for (int i = 2; i <= N; i++) {
            hsh[j][i] = (U)s[i - 1] * pw[j][i] % mod[j];
        }
        for (int i = 1; i <= N; i++) {
            int u = i + (i & -i);
            if (u <= N) hsh[j][u] = (hsh[j][u] + hsh[j][i]) % mod[j];
        }
    }
}

Hash operator()(int l, int r) {
    assert(l <= r);
    if (inverse) {
        l = N - 1 - l, r = N - 1 - r;
        swap(l, r);
    }
    Hash ans;
    l += 1, r += 1;
    for (int j = 0; j < mods; j++) {
        ans[j] = 0;
        for (int i = r; i > 0; i -= (i & -i)) {
            ans[j] = (ans[j] + hsh[j][i]) % mod[j];
        }
        for (int i = l - 1; i > 0; i -= (i & -i)) {
            ans[j] = (ans[j] - hsh[j][i] + mod[j]) % mod[j];
        }
        ans[j] = (U)ans[j] * inv[j][1 - 1] % mod[j];
    }
    return ans;
}

void update(int idx, T val) {
    if (inverse) idx = N - 1 - idx;
    idx += 1;
    for (int j = 0; j < mods; j++) {
        T u = 0;
        for (int i = idx; i > 0; i -= (i & -i)) {
            u = (u + hsh[j][i]) % mod[j];
        }
        for (int i = idx - 1; i > 0; i -= (i & -i)) {
            u = (u - hsh[j][i] + mod[j]) % mod[j];
        }
        for (int i = idx; i <= N; i += (i & -i)) {
            hsh[j][i] = (hsh[j][i] - u + mod[j]) % mod[j];
        }
        for (int i = idx; i <= N; i += (i & -i)) {
            hsh[j][i] = (hsh[j][i] + (U)val * pw[j][idx] % mod[j]) %
                mod[j];
        }
    }
}
}

```

```
};
```

1.3 KMP

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// String matching

#include <bits/stdc++.h>
using namespace std;

const int N = 3e5 + 9;

// returns the longest proper prefix array of pattern p
// where lps[i]=longest proper prefix which is also suffix of p[0...i]
vector<int> build_lps(string p) {
    int sz = p.size();
    vector<int> lps;
    lps.assign(sz + 1, 0);
    int j = 0;
    lps[0] = 0;
    for (int i = 1; i < sz; i++) {
        while (j >= 0 && p[i] != p[j]) {
            if (j >= 1)
                j = lps[j - 1];
            else
                j = -1;
        }
        j++;
        lps[i] = j;
    }
    return lps;
}

vector<int> ans;
// returns matches in vector ans in 0-indexed
void kmp(vector<int> lps, string s, string p) {
    int psz = p.size(), sz = s.size();
    int j = 0;
    for (int i = 0; i < sz; i++) {
        while (j >= 0 && p[j] != s[i])
            if (j >= 1)
                j = lps[j - 1];
            else
                j = -1;
        j++;
        if (j == psz) {
            j = lps[j - 1];
            // pattern found in string s at position i-psz+1
            ans.push_back(i - psz + 1);
        }
        // after each loop we have j=longest common suffix of s[0..i] which is
        // also prefix of p
    }
}

int main() {
    int i, j, k, n, m, t;
    cin >> t;
    while (t--) {
```

```

    string s, p;
    cin >> s >> p;
    vector<int> lps = build_lps(p);
    kmp(lps, s, p);
    if (ans.empty())
        cout << "Not Found\n";
    else {
        cout << ans.size() << endl;
        for (auto x : ans) cout << x << ' ';
        cout << endl;
    }
    ans.clear();
    cout << endl;
}
return 0;
}

```

1.4 Suffix Automaton

```

// Fonte: https://github.com/shahjalalshohag/code-library
//
// Faz coisarada

#include <bits/stdc++.h>
using namespace std;

const int N = 3e5 + 9;

// len -> largest string length of the corresponding endpos-equivalent class
// link -> longest suffix that is another endpos-equivalent class.
// firstpos -> 1 indexed end position of the first occurrence of the largest
// string of that node minlen(v) -> smallest string of node v = len(link(v))
// + 1
// terminal nodes -> store the suffixes
struct SuffixAutomaton {
    struct node {
        int len, link, firstpos;
        map<char, int> nxt;
    };
    int sz, last;
    vector<node> t;
    vector<int> terminal;
    vector<long long> dp;
    vector<vector<int>> g;
    SuffixAutomaton() {}
    SuffixAutomaton(int n) {
        t.resize(2 * n);
        terminal.resize(2 * n, 0);
        dp.resize(2 * n, -1);
        sz = 1;
        last = 0;
        g.resize(2 * n);
        t[0].len = 0;
        t[0].link = -1;
        t[0].firstpos = 0;
    }
    void extend(char c) {
        int p = last;
        if (t[p].nxt.count(c)) {

```



```

        int q = t[p].nxt[c];
        if (t[q].len == t[p].len + 1) {
            last = q;
            return;
        }
        int clone = sz++;
        t[clone] = t[q];
        t[clone].len = t[p].len + 1;
        t[q].link = clone;
        last = clone;
        while (p != -1 && t[p].nxt[c] == q) {
            t[p].nxt[c] = clone;
            p = t[p].link;
        }
        return;
    }
    int cur = sz++;
    t[cur].len = t[last].len + 1;
    t[cur].firstpos = t[cur].len;
    p = last;
    while (p != -1 && !t[p].nxt.count(c)) {
        t[p].nxt[c] = cur;
        p = t[p].link;
    }
    if (p == -1)
        t[cur].link = 0;
    else {
        int q = t[p].nxt[c];
        if (t[p].len + 1 == t[q].len)
            t[cur].link = q;
        else {
            int clone = sz++;
            t[clone] = t[q];
            t[clone].len = t[p].len + 1;
            while (p != -1 && t[p].nxt[c] == q) {
                t[p].nxt[c] = clone;
                p = t[p].link;
            }
            t[q].link = t[cur].link = clone;
        }
    }
    last = cur;
}

void build_tree() {
    for (int i = 1; i < sz; i++) g[t[i].link].push_back(i);
}

void build(string &s) {
    for (auto x : s) {
        extend(x);
        terminal[last] = 1;
    }
    build_tree();
}

long long cnt(int i) { // number of times i-th node occurs in the string
    if (dp[i] != -1) return dp[i];
    long long ret = terminal[i];
    for (auto &x : g[i]) ret += cnt(x);
    return dp[i] = ret;
}

};

```

```

int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    int t;
    cin >> t;
    while (t--) {
        string s;
        cin >> s;
        int n = s.size();
        SuffixAutomaton sa(n);
        sa.build(s);
        long long ans = 0; // number of unique substrings
        for (int i = 1; i < sa.sz; i++) ans += sa.t[i].len -
            sa.t[sa.t[i].link].len;
        cout << ans << '\n';
    }
    return 0;
}

```

2 Problemas

2.1 Kth digito na string infinita de digitos

```
// Retorna qual o numero e qual o algarismo do Kth digito
// na string infinita dos numeros naturais (12345678910111213...)
// Complexidade:  $O(\log_{10}(k))$ 

pair<ll, ll> kthdig(ll k) {
    ll qtd = 1, num_alg = 1, base = 1;
    while (1) {
        ll add = (9 * base) * num_alg;
        if (qtd + add < k) {
            qtd += add;
        } else
            break;
        base *= 10, num_alg++;
    }
    ll algarismo = (k - qtd) % num_alg;
    ll numero = (k - qtd) / num_alg + base;
    return {numero, algarismo};
}
```

3 Estruturas

3.1 Fenwick Tree

```
// Processas queries de operacao com inverso
//
// Build: O(n)
// Query: O(log(n))
// Update: O(log(n))

typedef long long ll;

struct fenwick {
    vector<ll> bit;
    fenwick(int n) { bit.assign(n + 1, 0); }
    fenwick(vector<ll> &v) {
        int n = v.size();
        bit.assign(n + 1, 0);
        for (int i = 1; i <= n; i++) bit[i] = v[i - 1];
        for (int i = 1; i <= n; i++) {
            int j = i + (i & -i);
            if (j <= n) bit[j] += bit[i];
        }
    }
    ll query(int i) {
        ll res = 0;
        for (; i; i -= (i & -i)) res += bit[i];
        return res;
    }
    ll query(int l, int r) { return query(r) - query(l - 1); }
    void update(int i, ll d) {
        for (; i && i < (int)bit.size(); i += (i & -i)) bit[i] += d;
    }
};
```

3.2 Segment Tree Beats

```
// Faz coisarada

#include <bits/stdc++.h>
using namespace std;
using ll = long long;

const int MAXN = 200001; // 1-based

int N;
ll A[MAXN];

struct Node {
    ll sum; // Sum tag
    ll max1; // Max value
    ll max2; // Second Max value
    ll maxc; // Max value count
    ll min1; // Min value
    ll min2; // Second Min value
    ll minc; // Min value count
    ll lazy; // Lazy tag
} T[MAXN * 4];
```

```

void merge(int t) {
    // sum
    T[t].sum = T[t << 1].sum + T[t << 1 | 1].sum;

    // max
    if (T[t << 1].max1 == T[t << 1 | 1].max1) {
        T[t].max1 = T[t << 1].max1;
        T[t].max2 = max(T[t << 1].max2, T[t << 1 | 1].max2);
        T[t].maxc = T[t << 1].maxc + T[t << 1 | 1].maxc;
    } else {
        if (T[t << 1].max1 > T[t << 1 | 1].max1) {
            T[t].max1 = T[t << 1].max1;
            T[t].max2 = max(T[t << 1].max2, T[t << 1 | 1].max1);
            T[t].maxc = T[t << 1].maxc;
        } else {
            T[t].max1 = T[t << 1 | 1].max1;
            T[t].max2 = max(T[t << 1].max1, T[t << 1 | 1].max2);
            T[t].maxc = T[t << 1 | 1].maxc;
        }
    }

    // min
    if (T[t << 1].min1 == T[t << 1 | 1].min1) {
        T[t].min1 = T[t << 1].min1;
        T[t].min2 = min(T[t << 1].min2, T[t << 1 | 1].min2);
        T[t].minc = T[t << 1].minc + T[t << 1 | 1].minc;
    } else {
        if (T[t << 1].min1 < T[t << 1 | 1].min1) {
            T[t].min1 = T[t << 1].min1;
            T[t].min2 = min(T[t << 1].min2, T[t << 1 | 1].min1);
            T[t].minc = T[t << 1].minc;
        } else {
            T[t].min1 = T[t << 1 | 1].min1;
            T[t].min2 = min(T[t << 1].min1, T[t << 1 | 1].min2);
            T[t].minc = T[t << 1 | 1].minc;
        }
    }
}

void push_add(int t, int tl, int tr, ll v) {
    if (v == 0) {
        return;
    }
    T[t].sum += (tr - tl + 1) * v;
    T[t].max1 += v;
    if (T[t].max2 != -11INF) {
        T[t].max2 += v;
    }
    T[t].min1 += v;
    if (T[t].min2 != 11INF) {
        T[t].min2 += v;
    }
    T[t].lazy += v;
}

// corresponds to a chmin update
void push_max(int t, ll v, bool l) {
    if (v >= T[t].max1) {
        return;
    }
    T[t].sum -= T[t].max1 * T[t].maxc;

```

```

    T[t].max1 = v;
    T[t].sum += T[t].max1 * T[t].maxc;
    if (l) {
        T[t].min1 = T[t].max1;
    } else {
        if (v <= T[t].min1) {
            T[t].min1 = v;
        } else if (v < T[t].min2) {
            T[t].min2 = v;
        }
    }
}

// corresponds to a chmax update
void push_min(int t, ll v, bool l) {
    if (v <= T[t].min1) {
        return;
    }
    T[t].sum -= T[t].min1 * T[t].minc;
    T[t].min1 = v;
    T[t].sum += T[t].min1 * T[t].minc;
    if (l) {
        T[t].max1 = T[t].min1;
    } else {
        if (v >= T[t].max1) {
            T[t].max1 = v;
        } else if (v > T[t].max2) {
            T[t].max2 = v;
        }
    }
}

void pushdown(int t, int tl, int tr) {
    if (tl == tr) return;
    // sum
    int tm = (tl + tr) >> 1;
    push_add(t << 1, tl, tm, T[t].lazy);
    push_add(t << 1 | 1, tm + 1, tr, T[t].lazy);
    T[t].lazy = 0;

    // max
    push_max(t << 1, T[t].max1, tl == tm);
    push_max(t << 1 | 1, T[t].max1, tm + 1 == tr);

    // min
    push_min(t << 1, T[t].min1, tl == tm);
    push_min(t << 1 | 1, T[t].min1, tm + 1 == tr);
}

void build(int t = 1, int tl = 0, int tr = N - 1) {
    T[t].lazy = 0;
    if (tl == tr) {
        T[t].sum = T[t].max1 = T[t].min1 = A[tl];
        T[t].maxc = T[t].minc = 1;
        T[t].max2 = -11INF;
        T[t].min2 = 11INF;
        return;
    }

    int tm = (tl + tr) >> 1;
    build(t << 1, tl, tm);

```

```

        build(t << 1 | 1, tm + 1, tr);
        merge(t);
    }

void update_add(int l, int r, ll v, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l) {
        return;
    }
    if (l <= tl && tr <= r) {
        push_add(t, tl, tr, v);
        return;
    }
    pushdown(t, tl, tr);

    int tm = (tl + tr) >> 1;
    update_add(l, r, v, t << 1, tl, tm);
    update_add(l, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}

void update_chmin(int l, int r, ll v, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l || v >= T[t].max1) {
        return;
    }
    if (l <= tl && tr <= r && v > T[t].max2) {
        push_max(t, v, tl == tr);
        return;
    }
    pushdown(t, tl, tr);

    int tm = (tl + tr) >> 1;
    update_chmin(l, r, v, t << 1, tl, tm);
    update_chmin(l, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}

void update_chmax(int l, int r, ll v, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l || v <= T[t].min1) {
        return;
    }
    if (l <= tl && tr <= r && v < T[t].min2) {
        push_min(t, v, tl == tr);
        return;
    }
    pushdown(t, tl, tr);

    int tm = (tl + tr) >> 1;
    update_chmax(l, r, v, t << 1, tl, tm);
    update_chmax(l, r, v, t << 1 | 1, tm + 1, tr);
    merge(t);
}

ll query_sum(int l, int r, int t = 1, int tl = 0, int tr = N - 1) {
    if (r < tl || tr < l) {
        return 0;
    }
    if (l <= tl && tr <= r) {
        return T[t].sum;
    }
    pushdown(t, tl, tr);

```

```

    int tm = (tl + tr) >> 1;
    return query_sum(l, r, t << 1, tl, tm) + query_sum(l, r, t << 1 | 1, tm +
        1, tr);
}

int main() {
    int Q;

    cin >> N >> Q;
    for (int i = 0; i < N; i++) {
        cin >> A[i];
    }
    build();
    for (int q = 0; q < Q; q++) {
        int t;
        cin >> t;
        if (t == 0) {
            int l, r;
            ll x;
            cin >> l >> r >> x;
            update_chmin(l, r - 1, x);
        } else if (t == 1) {
            int l, r;
            ll x;
            cin >> l >> r >> x;
            update_chmax(l, r - 1, x);
        } else if (t == 2) {
            int l, r;
            ll x;
            cin >> l >> r >> x;
            update_add(l, r - 1, x);
        } else if (t == 3) {
            int l, r;
            cin >> l >> r;
            cout << query_sum(l, r - 1) << '\n';
        }
    }
}

```


4 Grafos

4.1 Binary Lifting

```
// Binary Lifting (em nodos)
//
// Computa LCA e tambem resolve queries de operacoes
// associativas e comutativas em caminhos.
//
// Build(): O(n log(n))
// Query(): O(log(n))
// Lca(): O(log(n))
//
// up[u][i] = (2 ^ i)-esimo pai do u
// st[u][i] = query ate (2 ^ i)-esimo pai do u (NAO INCLUI O U)

const int maxn = 3e5 + 5, LG = 20;
vector<int> adj[maxn];

struct BinaryLifting {
    int up[maxn][LG], st[maxn][LG], val[maxn], t = 1;
    int tin[maxn], tout[maxn];

    const int neutral = 0;
    int merge(int l, int r) { return l + r; }

    void build(int u, int p = -1) {
        tin[u] = t++;
        for (int i = 0; i < LG - 1; i++) {
            up[u][i + 1] = up[up[u][i]][i];
            st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
        }
        for (int v : adj[u])
            if (v != p) {
                up[v][0] = u, st[v][0] = val[u];
                build(v, u);
            }
        tout[u] = t++;
    }

    void build(int root, vector<int> &v) {
        t = 1;
        int N = size(v);
        for (int i = 0; i < N; i++) val[i] = v[i];
        up[root][0] = root;
        st[root][0] = val[root];
        build(root);
    }

    bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=
        tout[v]; }

    int query2(int u, int v, bool include_lca) {
        if (ancestor(u, v)) return include_lca ? val[u] : neutral;
        int ans = val[u];
        for (int i = LG - 1; i >= 0; i--) {
            if (!ancestor(up[u][i], v)) {
                ans = merge(ans, st[u][i]);
                u = up[u][i];
            }
        }
    }
}
```

```

    }
    return include_lca ? merge(ans, st[u][0]) : ans;
}

int query(int u, int v) {
    if (u == v) return val[u];
    return merge(query2(u, v, 1), query2(v, u, 0));
}

int lca(int u, int v) {
    if (ancestor(u, v)) return u;
    if (ancestor(v, u)) return v;
    for (int i = LG - 1; i >= 0; i--) {
        if (!ancestor(up[u][i], v)) {
            u = up[u][i];
        }
    }
    return up[u][0];
}

int kth(int u, int k) {
    for (int i = 0; i < LG; i++) {
        if (k & (1 << i)) {
            u = up[u][i];
        }
    }
    return u;
}

} bl;

// Binary Lifting (em arestas)
//
// up[u][i] = (2 ^ i)-esimo pai do u
// st[u][i] = query ate (2 ^ i)-esimo pai do u

const int maxn = 3e5 + 5, LG = 20;
vector<pair<int, int>> adj[maxn];

struct BinaryLifting {
    int up[maxn][LG], st[maxn][LG], t = 1;
    int tin[maxn], tout[maxn];

    const int neutral = 0;
    int merge(int l, int r) { return l + r; }

    void build(int u, int p = -1) {
        tin[u] = t++;
        for (int i = 0; i < LG - 1; i++) {
            up[u][i + 1] = up[up[u][i]][i];
            st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
        }
        for (auto [w, v] : adj[u])
            if (v != p) {
                up[v][0] = u, st[v][0] = w;
                build(v, u);
            }
        tout[u] = t++;
    }
}

bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=

```

```

        tout[v]; }

int query2(int u, int v) {
    if (ancestor(u, v)) return neutral;
    int ans = neutral;
    for (int i = LG - 1; i >= 0; i--) {
        if (!ancestor(up[u][i], v)) {
            ans = merge(ans, st[u][i]);
            u = up[u][i];
        }
    }
    return merge(ans, st[u][0]);
}

int query(int u, int v) {
    if (u == v) return neutral;
#warning TRATAR ESSE CASO ACIMA
    return merge(query2(u, v), query2(v, u));
}
} bl;

// Binary Lifting para operacoes nao comutativas (em nodos)
//
// Levemente diferente do padrao
//
// Esse aqui resolve query de Kadani em arvore
// https://codeforces.com/contest/1843/problem/F2

const int maxn = 3e5 + 5, LG = 20;
vector<int> adj[maxn];

struct node {
    int pref, suff, sum, best;
};
const node neutral = {0, 0, 0, 0};
node new_node(int x) { return node{x, x, x, x}; }

node merge(node &l, node &r) {
    int pref = max(l.pref, l.sum + r.pref);
    int suff = max(r.suff, r.sum + l.suff);
    int sum = l.sum + r.sum;
    int best = max(l.suff + r.pref, max(l.best, r.best));
    return node{pref, suff, sum, best};
}

struct BinaryLifting {
    int up[maxn][LG], val[maxn], t = 1;
    int tin[maxn], tout[maxn];
    node st[maxn][LG], st2[maxn][LG];

    void build(int u, int p = -1) {
        tin[u] = t++;
        for (int i = 0; i < LG - 1; i++) {
            up[u][i + 1] = up[up[u][i]][i];
            st[u][i + 1] = merge(st[u][i], st[up[u][i]][i]);
            st2[u][i + 1] = merge(st2[up[u][i]][i], st2[u][i]);
        }
        for (int v : adj[u])
            if (v != p) {
                up[v][0] = u;
                st[v][0] = new_node(val[u]);
            }
    }
};

```

```

        st2[v][0] = new_node(val[u]);
        build(v, u);
    }
    tout[u] = t++;
}

void build(int root, vector<int> &v) {
    t = 1;
    int N = size(v);
    for (int i = 0; i < N; i++) val[i] = v[i];
    up[root][0] = root;
    st[root][0] = new_node(val[root]);
    st2[root][0] = new_node(val[u]);
    build(root);
}

bool ancestor(int u, int v) { return tin[u] <= tin[v] && tout[u] >=
    tout[v]; }

node query2(int u, int v, bool include_lca, bool invert) {
    if (ancestor(u, v)) return include_lca ? new_node(val[u]) : neutral;
    node ans = new_node(val[u]);
    for (int i = LG - 1; i >= 0; i--) {
        if (!ancestor(up[u][i], v)) {
            if (invert)
                ans = merge(st2[u][i], ans);
            else
                ans = merge(ans, st[u][i]);
            u = up[u][i];
        }
    }
    if (!include_lca) return ans;
    return merge(ans, st[u][0]);
}

node query(int u, int v) {
    if (u == v) return new_node(val[u]);
    node l = query2(u, v, 1, 0);
    node r = query2(v, u, 0, 1);
    return merge(l, r);
}

int lca(int u, int v) {
    if (ancestor(u, v)) return u;
    if (ancestor(v, u)) return v;
    for (int i = LG - 1; i >= 0; i--) {
        if (!ancestor(up[u][i], v)) {
            u = up[u][i];
        }
    }
    return up[u][0];
}

} b1, b12;

```

4.2 Bridges e Edge Biconnected Components

```

// Acha todas as pontes em O(n)
// Tambem constroi a arvore condensada, mantendo

```

```

// so as pontes como arestas e o resto comprimindo
// em nodos
//
// Salva no vetor bridges os pares {u, v} cujas arestas sao pontes

typedef pair<int, int> ii;
const int maxn = 2e5 + 5;
int n, m;
bool vis[maxn];
int dp[maxn], dep[maxn];
vector<int> adj[maxn];
vector<ii> bridges;

void dfs_dp(int u, int p = -1, int d = 0) {
    dp[u] = 0, dep[u] = d, vis[u] = 1;
    for (auto v : adj[u]) {
        if (v != p) {
            if (vis[v]) {
                if (dep[v] < dep[u]) dp[v]--, dp[u]++;
            } else {
                dfs_dp(v, u, d + 1);
                dp[u] += dp[v];
            }
        }
    }
    if (dp[u] == 0 && p != -1) { // edge {u, p} eh uma ponte
        bridges.emplace_back(u, p);
    }
}

void find_bridges() {
    memset(vis, 0, n);
    for (int i = 0; i < n; i++) {
        if (!vis[i]) {
            dfs_dp(i);
        }
    }
}

// Edge Biconnected Components (requer todo codigo acima)

int ebcc[maxn], ncc = 0;
vector<int> adjbcc[maxn];

void dfs_ebcc(int u, int p, int cc) {
    vis[u] = 1;
    if (dp[u] == 0 && p != -1) {
        cc = ++ncc;
    }
    ebcc[u] = cc;
    for (auto v : adj[u]) {
        if (!vis[v]) {
            dfs_ebcc(v, u, cc);
        }
    }
}

void build_ebcc_graph() {
    find_bridges();
    memset(vis, 0, n);
    for (int i = 0; i < n; i++) {

```

```

        if (!vis[i]) {
            dfs_ebcc(i, -1, ncc);
            ++ncc;
        }
    }
    // Opcao 1 - constroi o grafo condensado passando por todas as edges
    for (int u = 0; u < n; u++) {
        for (auto v : adj[u]) {
            if (ebcc[u] != ebcc[v]) {
                adjbcc[ebcc[u]].emplace_back(ebcc[v]);
            } else {
                // faz algo
            }
        }
    }
    // Opcao 2 - constroi o grafo condensado passando so pelas pontes
    for (auto [u, v] : bridges) {
        adjbcc[ebcc[u]].emplace_back(ebcc[v]);
        adjbcc[ebcc[v]].emplace_back(ebcc[u]);
    }
}

```

4.3 Dinic

```

// Fonte: https://github.com/shahjalalshohag/code-library
//
// Max Flow em  $O(V^3)$  ou  $O(E * \sqrt{V})$  em bipartido

#include <bits/stdc++.h>
using namespace std;

const int N = 5010;

const long long inf = 1LL << 61;
struct Dinic {
    struct edge {
        int to, rev;
        long long flow, w;
        int id;
    };
    int n, s, t, mxid;
    vector<int> d, flow_through;
    vector<int> done;
    vector<vector<edge>> g;
    Dinic() {}
    Dinic(int _n) {
        n = _n + 10;
        mxid = 0;
        g.resize(n);
    }
    void add_edge(int u, int v, long long w, int id = -1) {
        edge a = {v, (int)g[v].size(), 0, w, id};
        edge b = {u, (int)g[u].size(), 0, 0, -2}; // for bidirectional edges
        cap(b) = w
        g[u].emplace_back(a);
        g[v].emplace_back(b);
        mxid = max(mxid, id);
    }
    bool bfs() {

```

```

        d.assign(n, -1);
        d[s] = 0;
        queue<int> q;
        q.push(s);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (auto &e : g[u]) {
                int v = e.to;
                if (d[v] == -1 && e.flow < e.w) d[v] = d[u] + 1, q.push(v);
            }
        }
        return d[t] != -1;
    }

    long long dfs(int u, long long flow) {
        if (u == t) return flow;
        for (int &i = done[u]; i < (int)g[u].size(); i++) {
            edge &e = g[u][i];
            if (e.w <= e.flow) continue;
            int v = e.to;
            if (d[v] == d[u] + 1) {
                long long nw = dfs(v, min(flow, e.w - e.flow));
                if (nw > 0) {
                    e.flow += nw;
                    g[v][e.rev].flow -= nw;
                    return nw;
                }
            }
        }
        return 0;
    }

    long long max_flow(int _s, int _t) {
        s = _s;
        t = _t;
        long long flow = 0;
        while (bfs()) {
            done.assign(n, 0);
            while (long long nw = dfs(s, inf)) flow += nw;
        }
        flow_through.assign(mxid + 10, 0);
        for (int i = 0; i < n; i++)
            for (auto e : g[i])
                if (e.id >= 0) flow_through[e.id] = e.flow;
        return flow;
    }
};

int main() {
    int n, m;
    cin >> n >> m;
    Dinic F(n + 1);
    for (int i = 1; i <= m; i++) {
        int u, v, w;
        cin >> u >> v >> w;
        F.add_edge(u, v, w);
    }
    cout << F.max_flow(1, n) << '\n';
    return 0;
}

```

4.4 Pontos de articulacao

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// 0 equivalente a pontes, em vertices
//
// Complexidade: O(n)

#include <bits/stdc++.h>
using namespace std;

const int N = 3e5 + 9;

int T, low[N], dis[N], art[N];
vector<int> g[N];
void dfs(int u, int pre = 0) {
    low[u] = dis[u] = ++T;
    int child = 0;
    for (auto v : g[u]) {
        if (!dis[v]) {
            dfs(v, u);
            low[u] = min(low[u], low[v]);
            if (low[v] >= dis[u] && pre != 0) art[u] = 1;
            ++child;
        } else if (v != pre)
            low[u] = min(low[u], dis[v]);
    }
    if (pre == 0 && child > 1) art[u] = 1;
}

int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    while (1) {
        int n, m;
        cin >> n >> m;
        if (!n) break;
        while (m--) {
            int u, v;
            cin >> u >> v;
            g[u].push_back(v);
            g[v].push_back(u);
        }
        dfs(1);
        int ans = 0;
        for (int i = 1; i <= n; i++) ans += art[i];
        cout << ans << '\n';
        T = 0;
        for (int i = 1; i <= n; i++) low[i] = dis[i] = art[i] = 0,
            g[i].clear();
    }
    return 0;
}
```


5 Matematica

5.1 Crivo de Eratostenes

```
// Computa numeros primos entre [2, n] em O(n)
//
// Crivo linear computando spf (smallest prime factor) pra cada numero
// x entre [2, n] e phi(x) (funcao totiente)
// Complexidade: O(n)

int spf[maxn], phi[maxn];
vector<int> primes;
void sieve(int n) {
    phi[1] = 1;
    for (int i = 2; i <= n; i++) {
        if (spf[i] == 0) {
            spf[i] = i;
            primes.emplace_back(i);
            phi[i] = i - 1;
        }
        for (int j = 0; j < (int)primes.size() && i * primes[j] <= n &&
            primes[j] <= spf[i]; j++) {
            spf[i * primes[j]] = primes[j];
            if (primes[j] < spf[i])
                phi[i * primes[j]] = phi[i] * phi[primes[j]];
            else
                phi[i * primes[j]] = phi[i] * primes[j];
        }
    }
}
```

5.2 Fast Fourier Transform

```
// Fonte: https://github.com/ShahjalalShohag/code-library
//
// Faz convolucao de dois polinomios
// Complexidade: O(n log(n))
//
// Testado e sem erro de precisao para MAXN = 3e5 e A_i = 1e9

const int N = 3e5 + 9;

const double PI = acos(-1);
struct base {
    double a, b;
    base(double a = 0, double b = 0) : a(a), b(b) {}
    const base operator+(const base &c) const { return base(a + c.a, b +
        c.b); }
    const base operator-(const base &c) const { return base(a - c.a, b -
        c.b); }
    const base operator*(const base &c) const { return base(a * c.a - b *
        c.b, a * c.b + b * c.a); }
};

void fft(vector<base> &p, bool inv = 0) {
    int n = p.size(), i = 0;
    for (int j = 1; j < n - 1; ++j) {
        for (int k = n >> 1; k > (i ^= k); k >>= 1)
            ;
        if (j < i) swap(p[i], p[j]);
    }
}
```

```

    }
    for (int l = 1, m; (m = l << 1) <= n; l <= 1) {
        double ang = 2 * PI / m;
        base wn = base(cos(ang), (inv ? 1. : -1.) * sin(ang)), w;
        for (int i = 0, j, k; i < n; i += m) {
            for (w = base(1, 0), j = i, k = i + 1; j < k; ++j, w = w * wn) {
                base t = w * p[j + 1];
                p[j + 1] = p[j] - t;
                p[j] = p[j] + t;
            }
        }
    }
    if (inv)
        for (int i = 0; i < n; ++i) p[i].a /= n, p[i].b /= n;
}

vector<long long> multiply(vector<int> &a, vector<int> &b) {
    int n = a.size(), m = b.size(), t = n + m - 1, sz = 1;
    while (sz < t) sz <= 1;
    vector<base> x(sz), y(sz), z(sz);
    for (int i = 0; i < sz; ++i) {
        x[i] = i < (int)a.size() ? base(a[i], 0) : base(0, 0);
        y[i] = i < (int)b.size() ? base(b[i], 0) : base(0, 0);
    }
    fft(x), fft(y);
    for (int i = 0; i < sz; ++i) z[i] = x[i] * y[i];
    fft(z, 1);
    vector<long long> ret(sz);
    for (int i = 0; i < sz; ++i) ret[i] = (long long)round(z[i].a);
    while ((int)ret.size() > 1 && ret.back() == 0) ret.pop_back();
    return ret;
}

long long ans[N];
int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    int n, x;
    cin >> n >> x;
    vector<int> a(n + 1, 0), b(n + 1, 0), c(n + 1, 0);
    int nw = 0;
    a[0]++;
    b[n]++;
    long long z = 0;
    for (int i = 1; i <= n; i++) {
        int k;
        cin >> k;
        nw += k < x;
        a[nw]++;
        b[-nw + n]++;
        z += c[nw] + !nw;
        c[nw]++;
    }
    auto res = multiply(a, b);
    for (int i = n + 1; i < res.size(); i++) {
        ans[i - n] += res[i];
    }
    ans[0] = z;
    for (int i = 0; i <= n; i++) cout << ans[i] << ' ';
    cout << '\n';
    return 0;
}

```

5.3 Pollard Rho

```
// Fonte: https://github.com/shahjalalshohag/code-library
//
// Fatora numeros ate  $8 \cdot 10^{18}$ 
// Complexidade:  $O(n^{1/4})$ 

using ll = long long;
namespace PollardRho {
mt19937 rnd(chrono::steady_clock::now().time_since_epoch().count());
const int P = 1e6 + 9;
ll seq[P];
int primes[P], spf[P];
inline ll add_mod(ll x, ll y, ll m) { return (x += y) < m ? x : x - m; }
inline ll mul_mod(ll x, ll y, ll m) {
    ll res = __int128(x) * y % m;
    return res;
    // ll res = x * y - (ll)((long double)x * y / m + 0.5) * m;
    // return res < 0 ? res + m : res;
}
inline ll pow_mod(ll x, ll n, ll m) {
    ll res = 1 % m;
    for (; n; n >>= 1) {
        if (n & 1) res = mul_mod(res, x, m);
        x = mul_mod(x, x, m);
    }
    return res;
}
//  $O(it * (\log n)^3)$ , it = number of rounds performed
inline bool miller_rabin(ll n) {
    if (n <= 2 || (n & 1 ^ 1)) return (n == 2);
    if (n < P) return spf[n] == n;
    ll c, d, s = 0, r = n - 1;
    for (; !(r & 1); r >>= 1, s++) {
    }
    // each iteration is a round
    for (int i = 0; primes[i] < n && primes[i] < 32; i++) {
        c = pow_mod(primes[i], r, n);
        for (int j = 0; j < s; j++) {
            d = mul_mod(c, c, n);
            if (d == 1 && c != 1 && c != (n - 1)) return false;
            c = d;
        }
        if (c != 1) return false;
    }
    return true;
}
void init() {
    int cnt = 0;
    for (int i = 2; i < P; i++) {
        if (!spf[i]) primes[cnt++] = spf[i] = i;
        for (int j = 0, k; (k = i * primes[j]) < P; j++) {
            spf[k] = primes[j];
            if (spf[i] == spf[k]) break;
        }
    }
}
// returns  $O(n^{1/4})$ 
ll pollard_rho(ll n) {
    while (1) {
        ll x = rnd() % n, y = x, c = rnd() % n, u = 1, v, t = 0;
```

```

    ll *px = seq, *py = seq;
    while (1) {
        *py++ = y = add_mod(mul_mod(y, y, n), c, n);
        *py++ = y = add_mod(mul_mod(y, y, n), c, n);
        if ((x = *px++) == y) break;
        v = u;
        u = mul_mod(u, abs(y - x), n);
        if (!u) return __gcd(v, n);
        if (++t == 32) {
            t = 0;
            if ((u = __gcd(u, n)) > 1 && u < n) return u;
        }
    }
    if (t && (u = __gcd(u, n)) > 1 && u < n) return u;
}

vector<ll> factorize(ll n) {
    if (n == 1) return vector<ll>();
    if (miller_rabin(n)) return vector<ll>{n};
    vector<ll> v, w;
    while (n > 1 && n < P) {
        v.push_back(spf[n]);
        n /= spf[n];
    }
    if (n >= P) {
        ll x = pollard_rho(n);
        v = factorize(x);
        w = factorize(n / x);
        v.insert(v.end(), w.begin(), w.end());
    }
    return v;
}

} // namespace PollardRho
int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    PollardRho::init();
    int t;
    cin >> t;
    while (t--) {
        ll n;
        cin >> n;
        auto f = PollardRho::factorize(n);
        sort(f.begin(), f.end());
        cout << f.size() << ' ';
        for (auto x : f) cout << x << ' ';
        cout << '\n';
    }
    return 0;
}

```

6 Geometria

6.1 Convex Hull

```
// Algoritmo Graham's Scan
// Complexidade:  $O(n \log(n))$ 

bool ccw(pt &p, pt &a, pt &b, bool collinear = 0) {
    pt p1 = a - p;
    pt p2 = b - p;
    return collinear ? (p2 ^ p1) <= 0 : (p2 ^ p1) < 0;
}

vector<pt> convex_hull(vector<pt> v, bool collinear = 0) {
    int n = size(v);
    pt p0 = v[0];
    for (int i = 1; i < n; i++) {
        if (v[i] < p0) p0 = v[i];
    }

    sort(begin(v), end(v), [&](pt &l, pt &r) { // sorta clockwise
        pt p1 = l - p0;
        pt p2 = r - p0;
        ll c1 = p1 ^ p2;
        return c1 < 0 || ((c1 == 0) && p0.dist2(l) < p0.dist2(r));
    });

    if (collinear) {
        for (int i = n - 2; i >= 0; i--) { // reverte o ultimo lado do
            poligono
            if (ccw(v[0], v[n - 1], v[i])) {
                reverse(begin(v) + i + 1, end(v));
                break;
            }
        }
    }

    vector<pt> ch{p0, v[1]};
    for (int i = 2; i < n; i++) {
        while (ch.size() > 2 && (ccw(ch.end()[-2], ch.end()[-1], v[i],
            !collinear))) ch.pop_back();
        ch.emplace_back(v[i]);
    }

    return ch;
}
```

6.2 Ponto (Inteiro)

```
// Ponto com coordenadas inteiras e alguns metodos

struct pt {
    ll x, y;
    pt() : x(0), y(0) {}
    pt(ll _x, ll _y) : x(_x), y(_y) {}

    pt operator*(const pt &a, const ll &b) { return pt(b * a.x, b * a.y); }
    pt operator-(const pt &a, const pt &b) { return pt(a.x - b.x, a.y - b.y); }
}
```

```

pt operator+(const pt &a, const pt &b) { return pt(a.x + b.x, a.y + b.y);
}
ll operator*(const pt &a, const pt &b) { return a.x * b.x + a.y * b.y; }
ll operator^(const pt &a, const pt &b) { return a.x * b.y - a.y * b.x; }

bool operator<(const pt &p) {
    if (x == p.x) return y < p.y;
    return x < p.x;
}
ll dist2(const pt &p) {
    ll dx = x - p.x;
    ll dy = y - p.y;
    return dx * dx + dy * dy;
}

friend ostream &operator<<(ostream &out, const pt &a) { return out << "("
    << a.x << "," << a.y << ")"; }
friend istream &operator>>(istream &in, pt &a) { return in >> a.x >> a.y;
}

};

```

7 Extra

7.1 Config do Vim

```
// .vimrc

set nu
set ai
set ts=4
set sw=4
filetype plugin indent on
inoremap {} {}<Left><Return><Up><End><Return>

set nohls
set belloff=all
syntax on
set expandtab
set noshiftround
set showmode
set showcmd
```

7.2 Custom Hash

```
// Hash personalizado pra evitar colisao no unordered_map
// Uso: map<int, int, custom_hash> mapa;

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
```

7.3 Gerador aleatorio de inteiros em [l, r]

```
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());

ll uniform(ll l, ll r){
    uniform_int_distribution<int> uid(l, r);
    return uid(rng);
}
```

7.4 Mint

```
// Inteiro automaticamente modulado

const int mod = 998244353;
```

```

struct Mint {
    int val;
    Mint(int v = 0) { val = v % mod; }
    bool operator==(Mint o) { return val == o.val; }
    int operator*(Mint o) { return ((ll)val * o.val) % mod; }
    int operator+(Mint o) { return ((ll)val + o.val) % mod; }
    int operator-(Mint o) { return ((ll)val - o.val + mod) % mod; }
    int operator^(ll o) { return pwr(val, o); }
    int pwr(Mint b, ll e) {
        Mint res;
        for (res = 1; e; e >>= 1, b = b * b)
            if (e & 1) res = res * b;
        return res;
    }
};

```

7.5 Rand C++

```
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
```

7.6 Script de stress test

```

set -e
g++ -O2 code.cpp -o code
g++ -O2 brute.cpp -o brute
g++ -O2 gen.cpp -o gen

for((i = 1; ; ++i)); do
    ./gen > input_file
    ./code < input_file > myAnswer
    ./brute < input_file > correctAnswer
    diff myAnswer correctAnswer > /dev/null || break
    echo "Passed test: " $i
done

echo "WA on the following test:"
cat input_file
echo "Your answer is:"
cat myAnswer
echo "Correct answer is:"
cat correctAnswer

```

7.7 Script pra rodar C++

```

// chmod +x run
// ./run A.cpp

#!/bin/bash
g++ --std=c++20 -Wall -O2 -DNTJ -fsanitize=address,undefined $1 && ./a.out

```

7.8 Template C++

```

#include <bits/stdc++.h>
#define endl '\n'

```



```

using namespace std;
typedef long long ll;

void solve() {}

signed main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    solve();
}

```

7.9 Template de debug simples

```

void _print() {}
template <typename T, typename... U> void _print(T a, U... b) {
    if (sizeof...(b)) {
        cerr << a << ", ";
        _print(b...);
    } else
        cerr << a;
}
#ifdef NTJ
#define debug(x...) cerr << "[" << #x << "]" = [", _print(x), cerr << "]" <<
    endl
#else
#define debug(...)
#endif

```