

# Avaliação de Desempenho da Equação do Calor (Python vs Julia)

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Write abstract

CCS Concepts: • General and reference → Measurement; Empirical studies.

Additional Key Words and Phrases: Equação da Difusão do Calor, Análise de Desempenho, Python, Julia

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## 1 Introdução

Este trabalho tem como objetivo comparar o desempenho das linguagens de programação Python e Julia na resolução de equações do calor em 1, 2 e 3 dimensões. Se atentando ao tempo percorrido na execução dos programas, assim como a memória utilizada pelos mesmos, a fim de determinar qual das duas é a mais eficiente para esta aplicação específica. Este trabalho é feito com o intuito de ser um estudo em cálculo computacional e análise de desempenho.

## 2 Descrições Detalhadas

### 2.1 Ambiente

Os experimentos foram executados em uma única máquina com um processador Intel Core I3 de 12<sup>a</sup> geração, 8GB de memória, isolando o processo em um único núcleo usando `-cpuset-cpus="0"`, utilizando o *Frequency Governor* no modo performance para evitar oscilação do clock, *Turbo Boost* desativado, executando os códigos em um Docker para garantir a reproduzibilidade da pilha de software e dando partida a partir de um *Script Makefile* que orquestra todo o fluxo de testes.

### 2.2 Ferramentas

Foram utilizados códigos nas linguagens *Python*, *Julia*, *R*, *Bash* e *LATEX* no projeto. O projeto também conta com *Makefile*, *Dockerfile* e *Jupyter Notebooks*.

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### 2.3 Métodos

Cada dimensão possuí um código em *Python* e em *Julia* que é executado com 3 tamanhos de carga, nomeadas *low*, *mid* e *high*. Um script *R* sorteia uma ordem para que os códigos de cada dimensão em cada linguagem sejam executados com cada uma das cargas. A saída dessas execuções são arquivos *csv* separados em duas pastas *results* e *performance*. Todos os resultados são tratados por outros script *R*, os primeiros geram os gráficos de tempo de execução, os últimos resultam nos gráficos de uso de memória.

## 3 Resultados Finais

## 4 Discussão

## 5 Figures

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## 7 Acknowledgments

Identification of funding sources and other support, and thanks to individuals and groups that assisted in the research and the preparation of the work should be included in an acknowledgment section, which is placed just before the reference section in your document.

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\appendix
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## Acknowledgments

To Robert, for the bagels and explaining CMYK and color spaces.

## Referências

- [1] Rafal Ablamowicz and Bertfried Fauser. 2007. *CLIFFORD: a Maple 11 Package for Clifford Algebra Computations, version 11*. Retrieved February 28, 2008 from <http://math.tntech.edu/rafal/cliff11/index.html>
- [2] Patricia S. Abril and Robert Plant. 2007. The patent holder’s dilemma: Buy, sell, or troll? *Commun. ACM* 50, 1 (Jan. 2007), 36–44. doi:10.1145/1188913.1188915
- [3] Sten Andler. 1979. Predicate Path expressions. In *Proceedings of the 6th ACM SIGACT-SIGPLAN symposium on Principles of Programming Languages (POPL ’79)*. ACM Press, New York, NY, 226–236. doi:10.1145/567752.567774
- [4] David A. Anisi. 2003. *Optimal Motion Control of a Ground Vehicle*. Master’s thesis. Royal Institute of Technology (KTH), Stockholm, Sweden.
- [5] Sam Anzaroot and Andrew McCallum. 2013. *UMass Citation Field Extraction Dataset*. Retrieved May 27, 2019 from <http://www.iesl.cs.umass.edu/data/data-umasscitationfield>
- [6] Sam Anzaroot, Alexandre Passos, David Belanger, and Andrew McCallum. 2014. *Learning Soft Linear Constraints with Application to Citation Field Extraction*. arXiv:1403.1349 doi:10.48550/arXiv.1403.1349
- [7] R. Baggett, M. Simecek, C. Chambellan, K. Tsui, and M. Fraune. 2025. Fluidity in the Phased Framework of Technology Acceptance: Case Study to Gain a Holistic Understanding of (Older Adult) Participant Advancement Through Acceptance Phases with Mobile Telepresence Robots. *Robotics Aut. Systems*. Manuscript submitted for review.
- [8] Lutz Bornmann, K. Brad Wray, and Robin Haunschild. 2019. *Citation concept analysis (CCA)—A new form of citation analysis revealing the usefulness of concepts for other researchers illustrated by two exemplary case studies including classic books by Thomas S. Kuhn and Karl R. Popper*. arXiv:1905.12410 [cs.DL]
- [9] Kenneth L. Clarkson. 1985. *Algorithms for Closest-Point Problems (Computational Geometry)*. Ph.D. Dissertation. Stanford University, Palo Alto, CA. UMI Order Number: AAT 8506171.
- [10] Jacques Cohen (Ed.). 1996. Special issue: Digital Libraries. *Commun. ACM* 39, 11 (Nov. 1996).
- [11] Sarah Cohen, Werner Nutt, and Yehoshua Sagiv. 2007. Deciding equivalences among conjunctive aggregate queries. *J. ACM* 54, 2, Article 5 (April 2007), 50 pages. doi:10.1145/1219092.1219093
- [12] Bruce P. Douglass, David Harel, and Mark B. Trakhtenbrot. 1998. Statecharts in use: structured analysis and object-orientation. In *Lectures on Embedded Systems*, Grzegorz Rozenberg and Frits W. Vaandrager (Eds.), Lecture Notes in Computer Science, Vol. 1494. Springer-Verlag, London, 368–394. doi:10.1007/3-540-65193-4\_29
- [13] Ian Editor (Ed.). 2007. *The title of book one* (1st. ed.). The name of the series one, Vol. 9. University of Chicago Press, Chicago, Chapter The title of the chapter, 127–238. doi:10.1007/3-540-09237-4
- [14] Ian Editor (Ed.). 2008. *The title of book two* (2nd. ed.). University of Chicago Press, Chicago, Chapter 100, 25–137. doi:10.1007/3-540-09237-4
- [15] Matthew Van Gundy, Davide Balzarotti, and Giovanni Vigna. 2007. Catch me, if you can: Evading network signatures with web-based polymorphic worms. In *Proceedings of the first USENIX workshop on Offensive Technologies (WOOT ’07)*. USENIX Association, Berkley, CA, Article 7, 9 pages.
- [16] Torben Hagerup, Kurt Mehlhorn, and J. Ian Munro. 1993. Maintaining Discrete Probability Distributions Optimally. In *Proceedings of the 20th International Colloquium on Automata, Languages and Programming (Lecture Notes in Computer Science, Vol. 700)*. Springer-Verlag, Berlin, 253–264.
- [17] David Harel. 1978. *LOGICS of Programs: AXIOMATICs and DESCRIPTIVE POWER*. MIT Research Lab Technical Report TR-200. Massachusetts Institute of Technology, Cambridge, MA.
- [18] David Harel. 1979. *First-Order Dynamic Logic*. Lecture Notes in Computer Science, Vol. 68. Springer-Verlag, New York, NY. doi:10.1007/3-540-09237-4
- [19] Lars Hörmander. 1985. *The analysis of linear partial differential operators. III*. Grundlehren der Mathematischen Wissenschaften [Fundamental Principles of Mathematical Sciences], Vol. 275. Springer-Verlag, Berlin, Germany. viii+525 pages. Pseudodifferential operators.
- [20] Lars Hörmander. 1985. *The analysis of linear partial differential operators. IV*. Grundlehren der Mathematischen Wissenschaften [Fundamental Principles of Mathematical Sciences], Vol. 275. Springer-Verlag, Berlin, Germany. vii+352 pages. Fourier integral operators.

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- [21] Markus Kirschmer and John Voight. 2010. Algorithmic Enumeration of Ideal Classes for Quaternion Orders. *SIAM J. Comput.* 39, 5 (Jan. 2010), 1714–1747. doi:10.1137/080734467
- [22] Donald E. Knuth. 1997. *The Art of Computer Programming, Vol. 1: Fundamental Algorithms* (3rd. ed.). Addison Wesley Longman Publishing Co., Inc., Boston.
- [23] David Kosiur. 2001. *Understanding Policy-Based Networking* (2nd. ed.). Wiley, New York, NY.
- [24] Barack Obama. 2008. A more perfect union. Video. Retrieved March 21, 2008 from <http://video.google.com/videoplay?docid=6528042696351994555>
- [25] Poker-Edge.Com. 2006. Stats and Analysis. Retrieved June 7, 2006 from <http://www.poker-edge.com/stats.php>
- [26] R Core Team. 2019. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria. <https://www.R-project.org/>
- [27] Mehdi Saeedi, Morteza Saheb Zamani, and Mehdi Sedighi. 2010. A library-based synthesis methodology for reversible logic. *Microelectron. J.* 41, 4 (April 2010), 185–194.
- [28] Mehdi Saeedi, Morteza Saheb Zamani, Mehdi Sedighi, and Zahra Sasanian. 2010. Synthesis of Reversible Circuit Using Cycle-Based Approach. *J. Emerg. Technol. Comput. Syst.* 6, 4 (Dec. 2010), 12 pages.
- [29] Joseph Scientist. 2009. The fountain of youth. Patent No. 12345, Filed July 1st., 2008, Issued Aug. 9th., 2009.
- [30] Stan W. Smith. 2010. An experiment in bibliographic mark-up: Parsing metadata for XML export. In *Proceedings of the 3rd. annual workshop on Librarians and Computers (LAC '10, Vol. 3)*, Reginald N. Smythe and Alexander Noble (Eds.). Paparazzi Press, Milan Italy, 422–431.
- [31] Asad Z. Spector. 1990. Achieving application requirements. In *Distributed Systems* (2nd. ed.), Sape Mullender (Ed.). ACM Press, New York, NY, 19–33. doi:10.1145/90417.90738
- [32] Harry Thorngburg. 2001. *Introduction to Bayesian Statistics*. Retrieved March 2, 2005 from <http://ccrma.stanford.edu/~jos/bayes/bayes.html>, archived at <https://web.archive.org/web/20240505055615/https://ccrma.stanford.edu/~jos/bayes/bayes.html>
- [33] TUG 2017. *Institutional members of the TeX Users Group*. Retrieved May 27, 2017 from <http://wwtug.org/instmem.html>
- [34] Boris Veytsman. 2017. *acmart—Class for typesetting publications of ACM*. Retrieved May 27, 2017 from <http://www.ctan.org/pkg/acmart>

## A Research Methods

### A.1 Part One

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### A.2 Part Two

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## B Online Resources

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