

	Arrays	D.Arrays	LL	Stacks	Queues	Hash tables
Insert	X	$O(1)^*$	$O(1)^{**}$	$O(1)$	$O(n)$	$O(1)$
Delete	X	$O(n)$	$O(1)^{**}$	$O(1)$	$O(n)$	$O(1)$
Lookup	$O(1)$	$O(1)$	$O(n)$	$O(1)$	$O(n)$	$O(1)$

\* At the end, amortized  
\*\* At head or tail

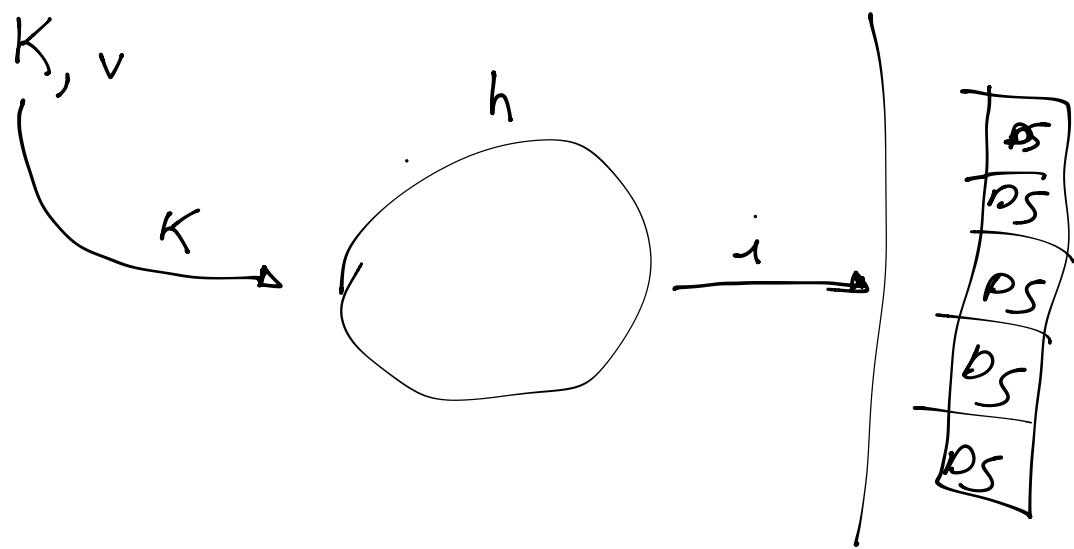
LIFO      FIFO

```
data = 
  {
    k →
    {
      k ←
      "nombre": "P."
      "name": valor
    }
  }
```

$\text{data.set}(k, v)$   
 $\text{data.remove}(k)$   
 $\text{data.get}(k)$   
 $\text{data}[k]$

$\text{map} < T_1, T_2 >$   
 $\text{int} \rightarrow$   
 $\leftarrow \text{strings}$

```
{ 1, 2, 3 }
```

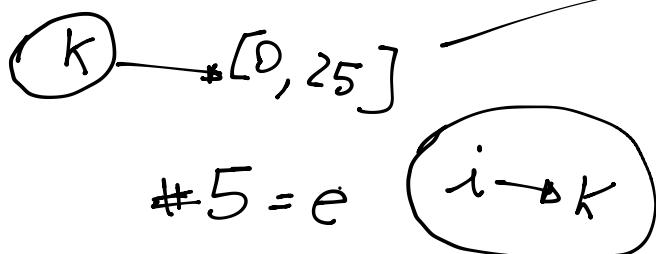


$\cup = \{ \text{ todos } \text{ as } \text{ substrings } \text{ de } "...." \}$   
 $\cup = \{ \text{ todos } \text{ has } \text{ letters } \text{ del } \text{ alfabeto } \Sigma \}$

$$k \xrightarrow{h} i$$

$$h: k \rightarrow N$$

$U = \{a, b, c, \dots, z\}, |U| = 2^6$



K	v
$K_1$	$k_1$
$K_2$	$k_2$
⋮	⋮

$i = 5$   
 $|en| = 26$

## Direct Addressing Table

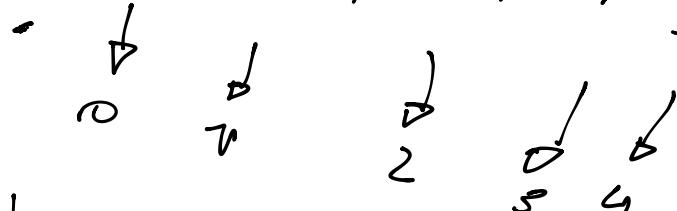
$$U = \{a, b, c, \dots, z\}$$

$$\begin{array}{l} A \rightarrow 0 \\ B \rightarrow 1 \\ \vdots \end{array}$$

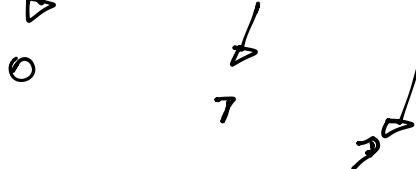
:

$i$  (new memory address)

$$U = \{200, 210, 300, 400, 500\}$$



$$U = \{U_{set(1)}, U_{set(2)}, U_{set(3)}\}$$



Para universos suf. pequeños,

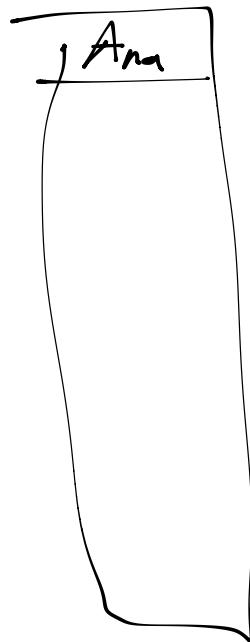
$$\log_m(T) = |\cup|$$

$$h: \cup \rightarrow \{0, 1, \dots m-1\}$$

$\cup$  no es pequeño

- Libros →
- $[1, 10^9]$
- $\mathbb{N} \rightarrow \infty$
- Nombres de personas
- Productos del sup
- Usuarios
- Ciudades

$$T =$$



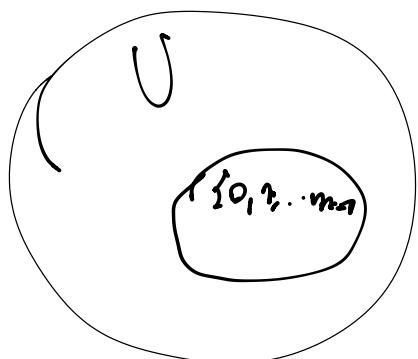
$|U|$        $m$   
 ↴  
 tamano      ↴  
 U            T

$h: U \rightarrow \{0, 1, \dots, m-1\}$   
 $|U| > m$

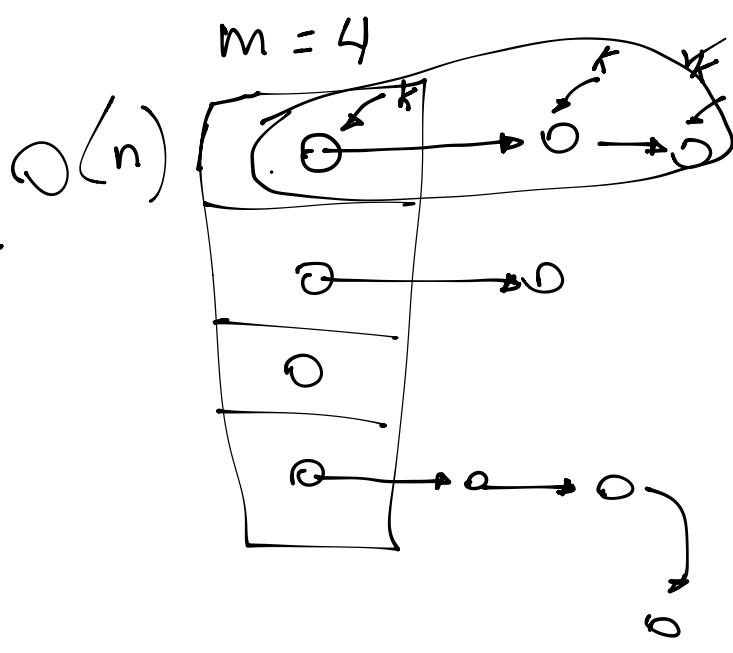
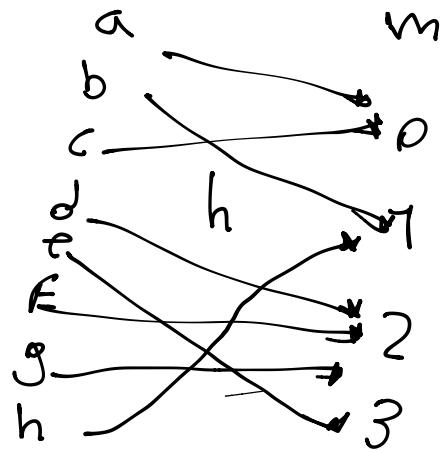
$$|U| = 8$$

$$m = 4$$

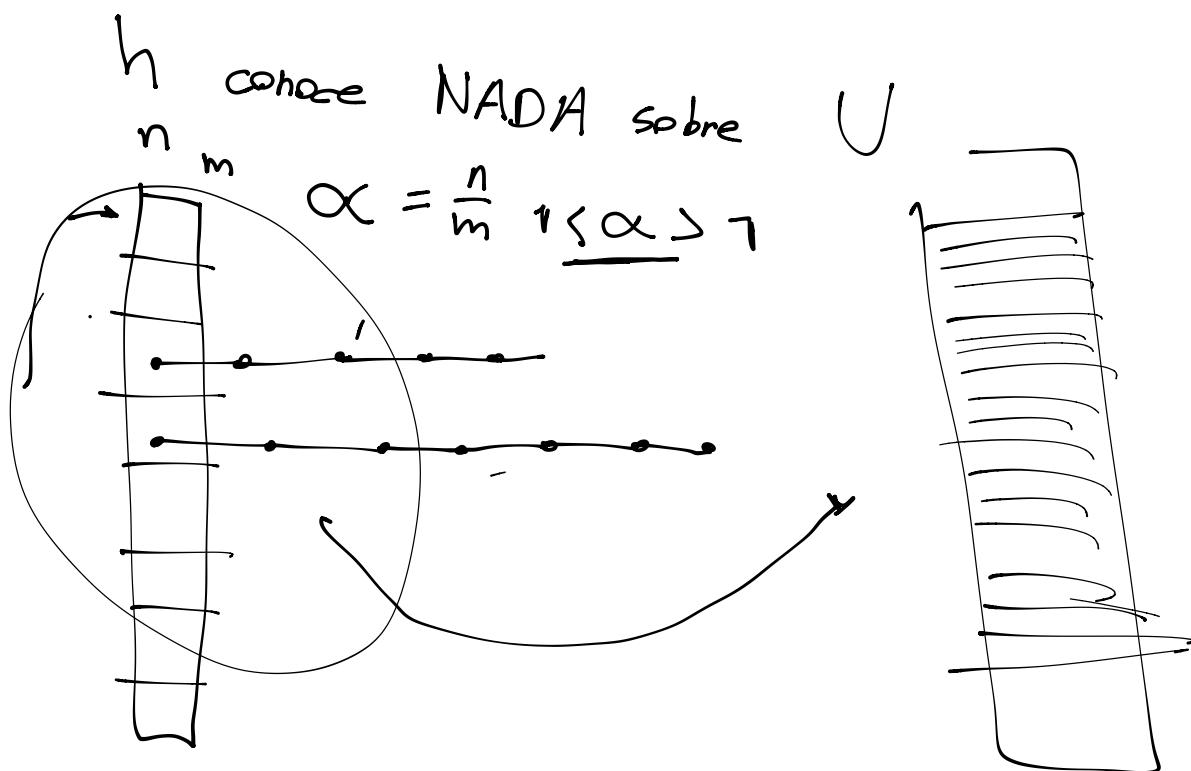
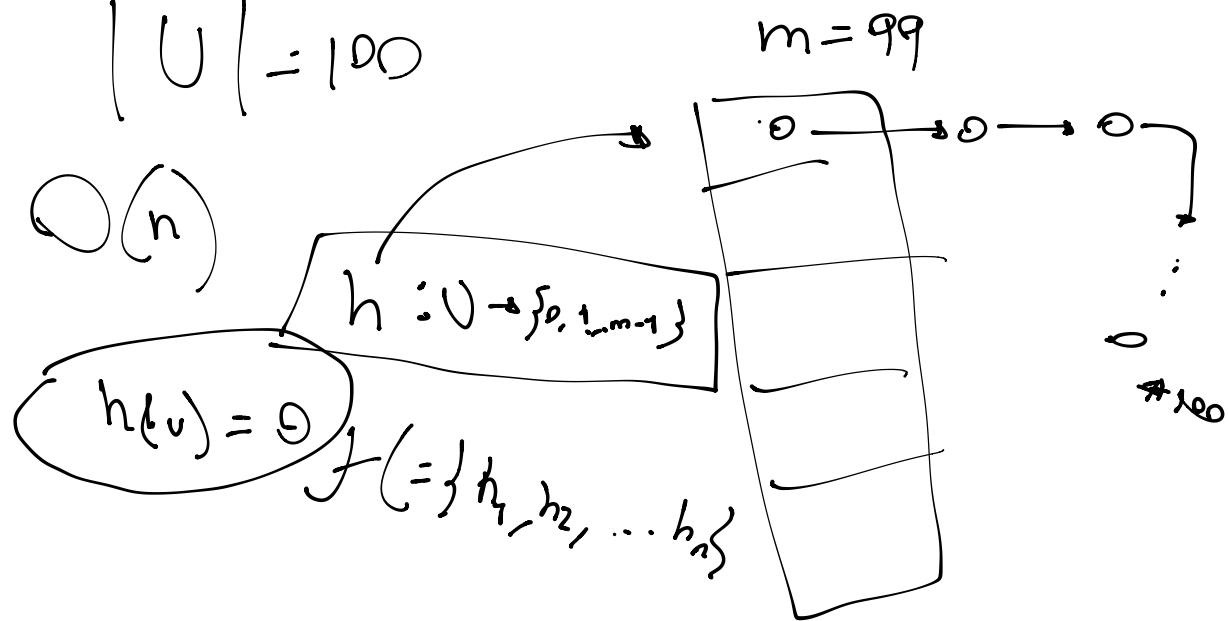
Collision



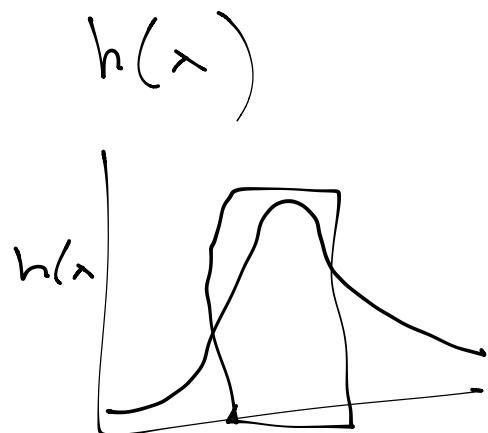
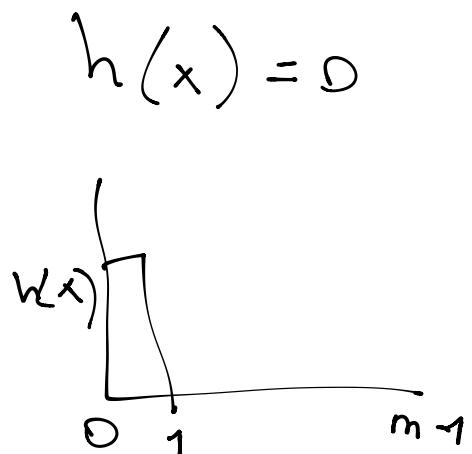
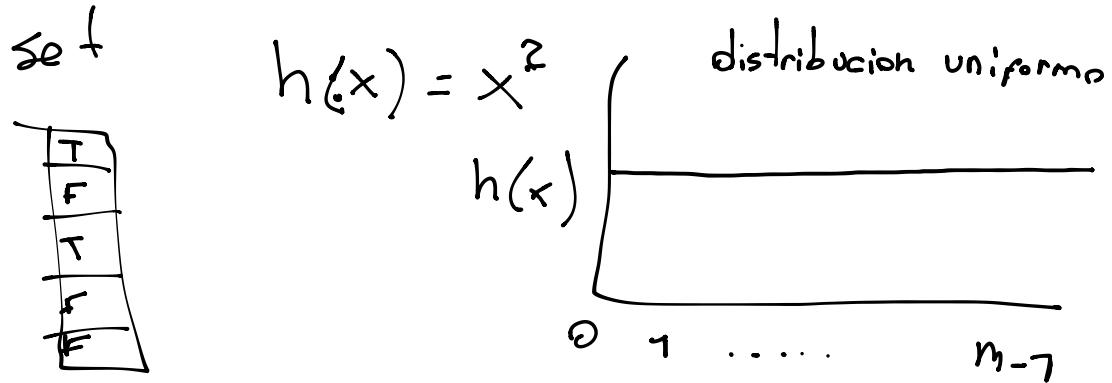
$|U| = 8$   
 "pablo"  
 "edward"  
 "nico"

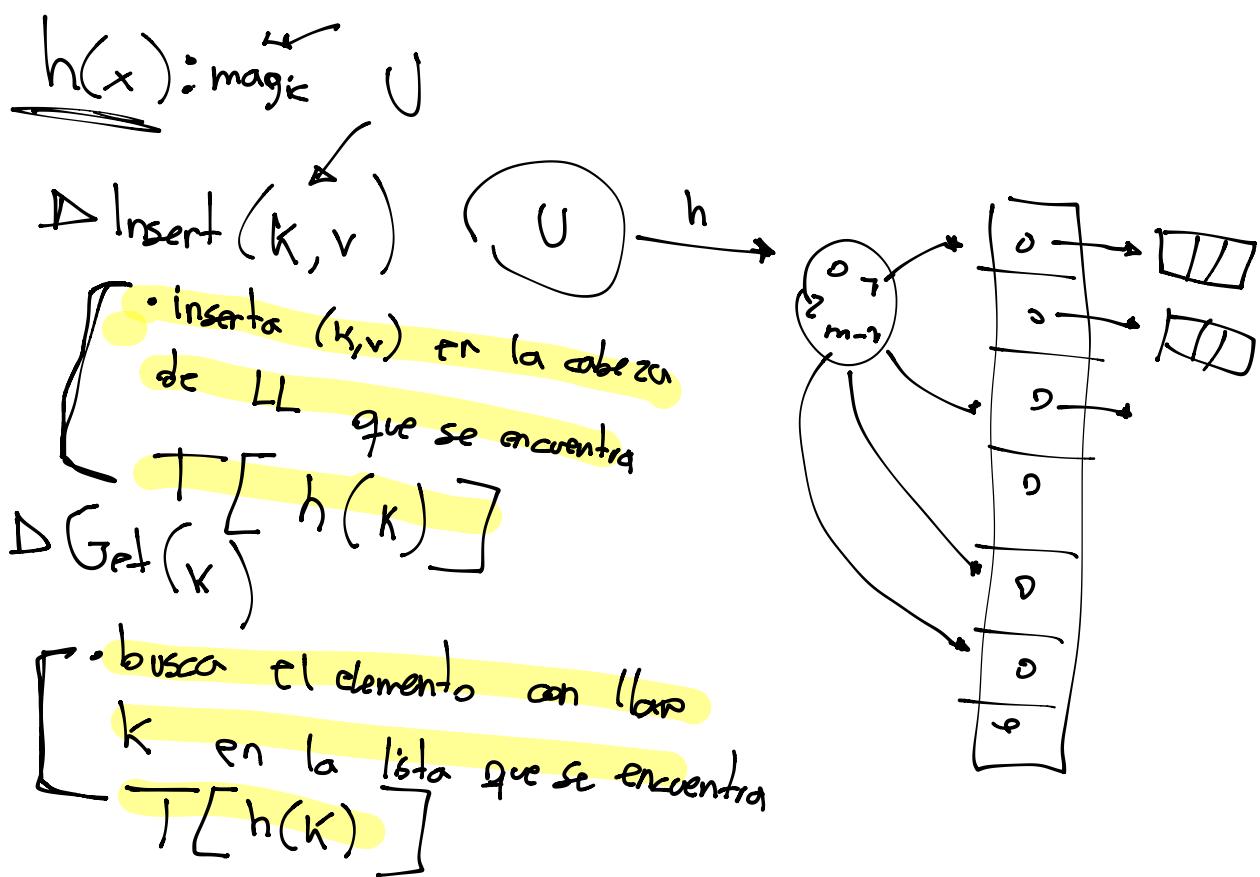


$$|U|=100$$



$$h: U \rightarrow \{0, 1, \dots, m-1\}$$





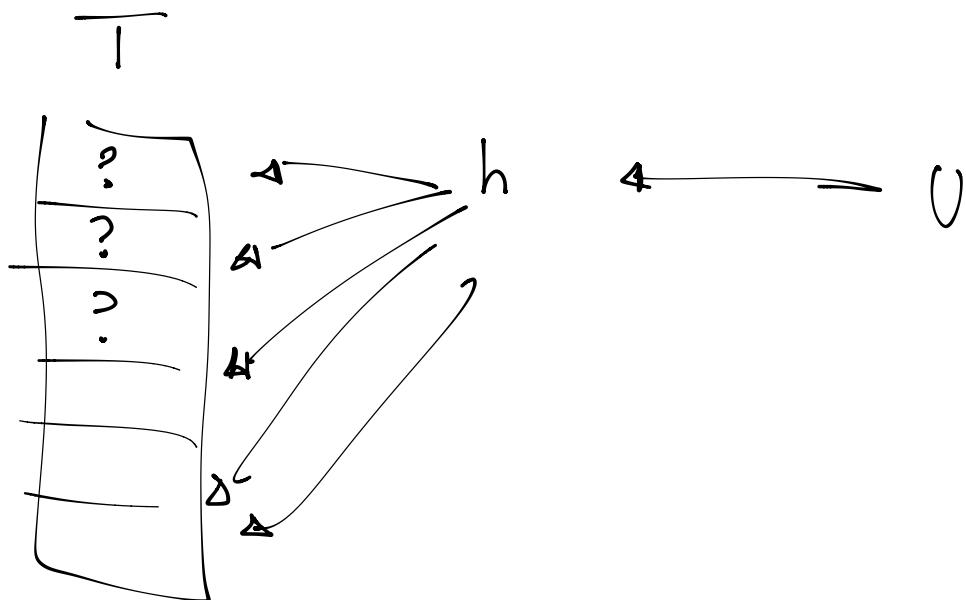
$$\Theta(1 + \alpha) \longrightarrow O(1)$$

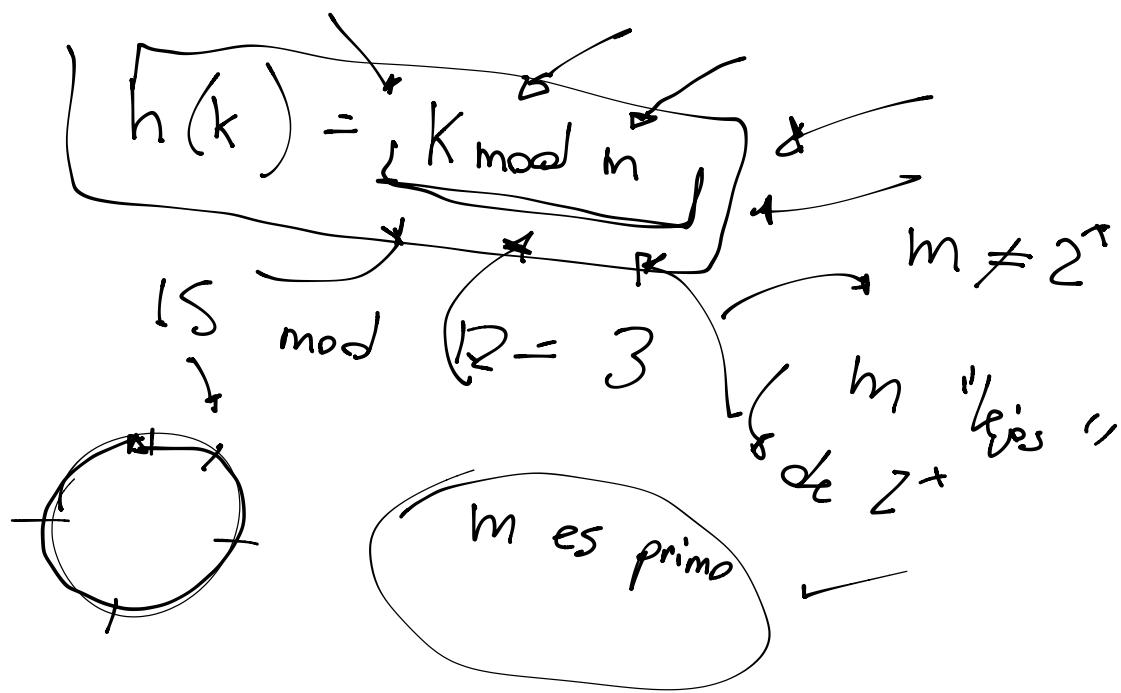
$\alpha = \frac{n}{m}$  total de elementos

total de slots en T

*Insertion, Deletion, Lookups*

- ↗ 1. Convertir  $k$  a un índice  $h$  ←  
 ↗ 2. Agregar, leer, modificar, eliminar el elemento  
 en el índice
- Depende DS dentro de s/o +





1. multiplica  $k$  por una constante  $A \in (0, 1)$
2. obtenemos la parte fraccional de  $ka$ .
3. multiplicamos por  $m$ .
4. Tomamos el suelo de

$$h(k) = \lfloor m(k \bmod 1) \rfloor$$

$$\rightarrow A \approx (\sqrt{5} - 1)/2 \approx 0.6180339887$$

Knuth ↗

$$h(k) = k \bmod m$$

$k \% m$

$m = 105$

$$h(90) = 90$$

$$h(105) = 0$$

$$h(108) = 3$$

$$h(k) = \lfloor m(kA \bmod 1) \rfloor$$

$m = 100$

$A = 0.5$

$$h(90) = \lfloor 100 \left( \frac{90}{2} \bmod 1 \right) \rfloor$$

$$h(90) = \lfloor 100 (45 \bmod 1) \rfloor$$

$$h(90) = \lfloor 100 (0) \rfloor = 0$$

