

YOUR TITLE

— Project Report —

Advanced Bayesian Data Analysis

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1 Introduction

notes to ourselves about things that should go in each section can be in red like this so we dont forget to delete them :)

Background

The association between a voters demographics (gender, age, education etc.) and their propensity to vote for either a democratic or republican candidates is a topic of extensive study. The large political polling organization such as Gallup and Pew Research tend to analyze their polls by breaking respondents into smaller demographic groups [cite](#). However, less is known about the relationship between voting outcomes and the voter's environment. Our modeling would like to investigate the conventional wisdom that says cities tend to be more progressive. To put it more concretely we want to investigate the question; "How does urbanization of a particular US House district affect the resulting party that is elected?".

To answer our question about the nature of the relationship between urbanization and partisan voting outcomes, we choose to investigate the 2022 House Election. Every two years the United States elects 435 officials to the House of Representatives. Each state is allocated one of the the 435 House seats with the rest being allocated roughly proportional to the share of total population living in each state [cite](#). We then use each of the districts as a single replicate.

The 2022 House Election takes places during a non-presidential year, and is the most recent election following the 2020 Census and redistricting, allowing us to use the most recently available district maps, and demographic data. Within this report we combine demographic data and urbanization data into a logistic regression model to predict the district voting outcomes of the 2022 House Election.

comparative literature

Inherent in our analysis is the assumption that republican and democratic voters are not evenly distributed, rather we assume that the distribution of voters is informative for our analysis. Much of the current research related to the relationship between urbanization and partisan voting focuses on the practice of gerrymandering. Gerrymandering is practice of redrawing the voting district boundaries in favor of a particular political party. We ignore the impact of gerrymandering in our analysis, since the method of determining if a district has been gerrymandered is rather unclear and out of the scope of this project.

Since we are using a custom curated dataset, there exists no directly comparable research, however we did find interesting ideas related to urbanization and partisanship. One example of this would be the idea of the inefficient distribution of Democrats in cities, as explored by [CITE](#). In their analysis they discuss the phenomena of spatial inefficiency wherein higher concentrations of democratic voters in urban areas leads to fewer districts voting for democratic candidates that would be expected. Rather than trying to predict

the partisan outcome of a particular district, their analysis focuses on measuring partisan spatial efficiency in order to understand the impact of gerrymandering [CITE](#).

Although the authors in [cite title](#) look at election outcomes through the lense of spatial efficiency and we are trying to look at election results of districts with respect to their urbanization, we can take the following insights from their analysis. First the distribution of Democrats and urbanization are inextricably linked, they found that all over the country Democrats tend to be concentrated in urban areas which indicate that it will likely be a good predictor. We would like to investigate to what extent that is true. They also note that the effect of spatial efficiency is highly dependent on state and the branch of government. When considering that urbanization can be considered a proxy for spatial inefficiency, this further supports our decision to model urbanindex hierarchically.

[why this particular modeling approach? Also what was our modeling approach?](#)

model approach/motivation

Two party system

[why not shift this to the data section? Leonor: here is an explanation for it being two parties, kinda long but yeah](#) Although technically a multiparty system, the U.S. is often called a two party system due to the domination of the major political parties the Democrats and Republicans ([cite](#)). These parties dominate particularly on the federal level because political candidates are required to get a plurality of votes rather than a majority of votes which the two largest parties often reach. This is further reinforced as would be third-party voters, often vote for one of the two major parties so ensure their voice is heard, rather than using their vote on a candidate unlikely to reach a plurality of votes ([cite](#)). Within our dataset, there are no districts represented by a third-party candidate and as such we will refer to the U.S. as being a two party system, which led to using logistic regression as a natural choice for modeling. [i would say led to modeling winner as a binary variable, this doesnt necessarily lead to logistic regression](#)

[this is something like assumptions but im not really sure what to say](#) Since the districts are allocated based on population, they are approximately the same size, which allows us to make the assumption the differences in voting behavior have something to do with people within the districts rather than simply the size of each district. This also allows us to make exchangeability assumptions with respect to state and region.

[maybe put assumptions here? like the exchangeability assumption? i think model assumptions belong in the model section, at least the explanation \(we can just mention the name here is it is important to\)](#)

2 Dataset

Our dataset was made by combining four independent datasets related to the 2022 House election. The first dataset is the publically available urbanization dataset published by fivethirty eight from which we incorporate the variables urbanization index and (urban)

grouping into our final dataset Holly Fuong, 2022. From the description of the dataset: "The urbanization index is calculated as the natural logarithm of the average number of people living within a five-mile radius of every census tract in a given district, based on a weighted average of the population of each census tract. The population of a census tract is according to 2020 census data. This provides a numerical value for how urban or rural a district is." Holly Fuong, 2022. The urbanization dataset was put together by FiveThirtyEight as part of their analysis *The Republican Path To a House Majority Goes Through The Suburbs* which gave election predictions leading up to the 2022 U.S. Congressional Election Skelly, n.d. The other variable we included in our curated dataset was urban grouping, which is a collapsing of the urban index into categories ranging from urban to rural. We however did not end up including this in our model.

The second dataset used in our analysis the Election Results Dataset from FiveThirtyEight Mehta, n.d. It is a continuously updated repository of United States Governor, Congressional and Presidential elections. As this dataset includes all elections going back to 1998, we only used a subset of the data relevant to the 2022 House Election. From this dataset we used the party, state, and winning party variables, it also included the variable incumbent party, which we considered also using, but the data from incumbent party is partially incomplete and would likely have very high correlation with the our target variable winning party, leading to a model that relies most heavily on incumbent party. Since we are more interested in the relationship between our model and our choose covariates we therefore decided not to include it.

The third data used in our analysis is a subset of the 2022 American Community Survey Data. The American Community Survey is a yearly survey collecting information about the occupations, education attainment, income and other demographic information carried out by the United States Census Bureau. The United States Census Bureau provides an online tool to access its extensive survey database, which can then be filtered and refined for further analysis. For our analysis we included the following variables for each House district in our curated dataset; total population, percentage women, median household income, mean household income, percentage retirees, percentage bachelors degree holders above the age of 25 years old and unemployment rate among those above the age of sixteen.

From these covariates we hoped to capture education, income, and, demographic make-up of the districts because we thought they might be influential in determining partisan voting outcomes. However not all of these covariates were included in our final models. As previously explained, the districts are drawn in such a way that the total population of each district should be approximately the same [cite](#), so while this does help support our exchangability assumption, we determined that total population itself would be an unsuitable covariate. Although we initially thought that percentage women may also be a poor predictor-since women should be evenly distributed throughout the United States-however a Pew Research Survey found that women tend to lean more democrat and have higher turnout, which is why we then included it in our largest model. [cite](#). We also initially thought that median and mean income could be combined to as a measure of inequality, but found a study saying that inequality is not a good voting indicator on

its own [cite](#). For that reason we choose to use only the median household income as it would be less skewed. Similarly unemployment is not a good indicator on its own, rather when unemployment is high the incumbent is more likely to loose regardless of party [cite](#). We also decided to use percentage retirees instead of median age, as they were highly correlated and median age also includes a part of the population that cannot vote. [Why is pct retirees included in every single one of our models?](#)

The fourth dataset was the region dataset, which was put together manually by us following the four statistical region designations of United States Census Bureau. [Cite: First link on wiki list of regions of us](#)

Data Cleaning

[how did we code our variables?](#) We then merged these four datasets to created our own curated dataset. We did this by merging the different datasets on shared variables. As previously said, each observation represents a particular house district, so for the first three datasets, we simply merged them based on their state and district number. To include the regions we simply used the state variable for each district.

[maybe talk about the funny shit with alaska and preference voting \(?\)](#) In the election results dataset, we encountered one instance of missing data. For all of the districts in Louisiana, the winning party was not recorded. There was however the incumbant party recorded in the Election Results dataset and by cross referencing this with public record we found for the 2022 House Election only candidates from the incumbant party remained in each of the districts. Therefore as is reflected in our code base we used the data from the incumbant party in place of winning party for the state of Louisiana. For all other states and disticts we did not encounter this problem.

In terms of scaling we wanted all the variables to be on roughly the same scale to aid in convergence times. In order to do that we roughly scaled median income and total population by dividing total population by one million and dividing median income by one hundred thousand. This brought each of these to roughly the same scale as the other variables. Similarly we decided to scale all of the percentage variables to be on the scale zero to one hundred rather than zero to one to make their coefficents more interpretable.

3 Models

The Winning party in each congressional district race ($y_{i,j,k}$ for district i , state j , region k) can be modeled as the outcome of Bernoulli trial, since this is a binary variable:

$$y_{i,j,k} \sim Ber(\pi_{j,k} = \text{logit}^{-1}(\theta_{j,k})) \quad (1)$$

with probability of a Democrat win $\pi_{j,k}$ modeled as the inverse logit transform of $\theta_{j,k}$, a linear combination of our covariates. The inverse logit function converts real numbers into quantities between 0 and 1, and is therefore a standard way to model probabilities [cite](#).

We tested four different models for $\theta_{j,k}$, which include different covariates in addition to our variable of interest (Urban index) and incorporate our data's hierarchical structure in different ways. Therefore, all four are Multilevel Bayesian (Logistic) Models, which require particular assumptions: **CITE** first, that a logistic regression accurately represents the relationship between the log-odds of a Democrat win and the explanatory variables, that is, $\theta_{j,k}$ and our covariates are linearly related; second, interchangeability, meaning that each district is exchangeable within each state and each state is exchangeable within each region; and third, that the value of urban index (and other covariates) in a district has a different effect depending on the state/region it belongs to.

The logistic relationship is common choice for modeling binary outcomes. It allows us to model the probability of a Democrat win by a linear predictor which can take any real value, while still having an interpretation for the coefficient estimates (in terms of change of log-odds). [what do you mean here? that its a suitable choice for binary data? Maybe rewrite to: Modeling a binary as a logistic regression is a common choice in the literature\(?\)](#) (**cite**).

We assume interchangeability because we assume are the districts draw in such a way that they are competitive for both parties. Meaning that although the districts may have different characteristics, certain mechanisms can be best captured when thinking of districts as exchangeable parts of a hierarchical model.

One example would be for complicated historical reasons certain regions of the United States are more similar to each other than others. For example the Southern United states tends to be more religious and religious people tend to vote more conservatively, think about this then as a prior telling us about the mix of democratic and republican districts within a particular state. Although the religiosity may increase the number of potential republican districts in each state, whether one district votes republican does not influence the decision of another since each district outcome is determined by thousands of individual votes. Since each district is part of a state and a region, translate structure the complex geographically determined mechanisms into our model by modeling some of parameters hierarchically.

Model 1 (state level)

Our first model includes only our variable of interest, urban index, plus the percentage of retirees as covariates to explain θ , plus an intercept. [Murthy didn't you find something in initial testing? please write about that](#) Urban index was modeled hierarchically, with the coefficient varying by state, with a prior dependent on common parameters β_{urb} and σ_{urb} , which in turn have (hyper-)priors of their own. The intercept is assumed to be non-variant for all districts, as well as the slope of percentage of retirees.

Equation 2 describes our model conceptually.

$$\theta_j = \beta_0 + \beta_{urb,j}^{uncent} \cdot \text{Urban_Index} + \beta_{ret} \cdot \text{Pct_Retirees} \quad (2)$$

To better understand what happens in the backend when we want to fit this model with BRMS, it is helpful to rewrite the equation 3 in terms of 'global' and 'hierarchical'

effects. The previously considered coefficient is then decomposed into these effects, i.e. $\beta_{urb,j}^{uncent} = \beta_{urb} + \beta_{urb,j}$ with $\beta_{urb,j}$ centered around zero, which does not alter the meaning of the model. [cite brms book](#)

$$\begin{aligned}\theta_j = & \beta_0 + \beta_{urb} \cdot \text{Urban_Index} + \beta_{urb,j} \cdot \text{Urban_Index} \\ & + \beta_{ret} \cdot \text{Pct_Retirees}\end{aligned}\tag{3}$$

Although we assume that there is indeed state-level clustering in the district election outcomes, we have 50 states, and some of them include only one or two districts. This can make the hierarchical estimates unreliable.

Model 2 (region level)

To overcome this problem, we fit another model, with only one difference from the previous one: the hierarchy is at the region level, rather than state. This means the coefficients of urban index vary by region now, with a common mean and variance which are parameters to be estimated themselves. Equation 4 describes this model, in its specification with separate global and hierarchical effects for urban index.

$$\begin{aligned}\theta_k = & \beta_0 + \beta_{urb} \cdot \text{Urban_Index} + \beta_{urb,k} \cdot \text{Urban_Index} \\ & + \beta_{ret} \cdot \text{Pct_Retirees}\end{aligned}\tag{4}$$

Model 3 (nested)

In this model we include the entire geographical hierarchy: a *nested hierarchy* of districts within states within regions. Here the assumption is that the effect of urbanindex ($\beta_{urb,j:k}$) depends on state j and region k through a prior with mean parameter $\beta_{urb,k}$, which in turn varies by region and depends on hyper-mean β_{urb} (which has its own prior, with hyper-hyper-parameters). Equation 5 specifies the model, with the centered around zero formulation.

$$\begin{aligned}\theta_{j,k} = & \beta_0 + \beta_{urb} \cdot \text{Urban_Index} + \beta_{urb,k} \cdot \text{Urban_Index} \\ & + \beta_{urb,j:k} \cdot \text{Urban_Index} + \beta_{ret} \cdot \text{Pct_Retirees}\end{aligned}\tag{5}$$

Model 4 (big model)

This is our most extensive model. Here we used urban index and 4 additional covariates plus an intercept to explain $\theta_{j,k}$. It can be seen as an extension of Model 1, as urban index is modeled hierarchically by state. The region level hierarchy is instead included only in the effect of percentage of bachelors degrees. Median income effect is also considered to vary by state, and the intercept and the slopes of percentage of women and percentage of retirees were modeled non-hierarchically.

Equation 6 describes this model, in the brms adapted specification.

$$\begin{aligned}
 \theta_{j,k} = & \beta_0 + \beta_{women} \cdot \text{Pct_Women} \\
 & + \beta_{urbindex} \cdot \text{Urban_Index} + \beta_{urbindex,j} \cdot \text{Urban_Index} \\
 & + \beta_{bsc} \cdot \text{Pct_Bachelor's} + \beta_{bsc,k} \cdot \text{Pct_Bach.} + \beta_{inc} \cdot \text{Median_Income} \\
 & + \beta_{inc,k} \cdot \text{Median_Income} + \beta_{ret} \cdot \text{Pct_Retirees}
 \end{aligned} \tag{6}$$

4 Priors

Priors represent our initial beliefs about our model parameters' distributions. In each of our models, this means a prior for the intercept, one for the slope of each covariate that is modeled non-hierarchically (e.g., β_{ret} in all four models) and, in the case of covariates with global and hierarchical effects, priors for the hyper-parameters as well.

Table 1 lists our selected priors for each model, by corresponding covariate.

	Model 1	Model 2	Model 3	Model 4
Intercept	$\beta_0 \sim N(0, 10)$	$\beta_0 \sim N(0, 10)$	$\beta_0 \sim N(0, 10)$	$\beta_0 \sim N(0, 10)$
Urban Index	$\beta_{urb} \sim N(0, 1)$	$\beta_{urb} \sim N(0, 1)$	$\beta_{urb} \sim N(0, 1)$	$\beta_{urb} \sim N(0, 1)$
	$\beta_{urb,j} \sim N(0, \sigma_{urb})$,	$\beta_{urb,k} \sim N(0, \sigma_{urb})$,	$\beta_{urb,k} \sim N(0, \sigma_{urb,1})$,	$\beta_{urb,j} \sim N(0, \sigma_{urb})$,
	$\sigma_{urb} \sim \text{Halfcauchy}(10)$	$\sigma_{urb} \sim \text{Halfcauchy}(10)$	$\sigma_{urb,1} \sim \text{Halfcauchy}(10)$	$\sigma_{urb} \sim \text{Halfcauchy}(10)$
			$\beta_{urb,j:k} \sim N(0, \sigma_{urb,2})$,	
			$\sigma_{urb,2} \sim \text{Halfcauchy}(10)$	
Pct.retirees	$\beta_{ret} \sim t(1, -2, 1)$	$\beta_{ret} \sim t(1, -2, 1)$	$\beta_{ret} \sim t(1, -2, 1)$	$\beta_{ret} \sim t(1, -2, 1)$
pct.women				$\beta_{women} \sim N(0, 1)$
pct bsc				$\beta_{bsc} \sim t(1, 0, 1)$
				$\beta_{bsc,k} \sim N(0, \sigma_{bsc})$,
				$\sigma_{bsc} \sim \text{Halfnormal}(0, 1)$
median income				$\beta_{inc} \sim N(0, 1)$
				$\beta_{inc,j} \sim N(0, \sigma_{inc})$,
				$\sigma_{inc} \sim \text{Halfnormal}(0, 1)$

Table 1: Priors defined for each of our four models, for each parameter; parameters and distributions are listed by their corresponding covariate.

We define such distributions before seeing the data, based on existing literature and our own intuition about the effects of our covariates on the probability of a democrat win. We assumed the same priors for the same terms included in different models (intercept, percentage of retirees, urban index for the same levels).

For the intercept β_0 we set a Normal prior centered at zero with a large standard deviation. This represents a weakly informative prior, as we had no strong beliefs about the intercept value, nor does it have any straightforward interpretation in our model: it theoretically represents the (logit of the) probability of a Democrat win in a district with no urbanization at all, a median income of zero dollars, and 0% of women, retirees and citizens with a bachelor's degree in the population; such a district is obviously nonexistent.

For the population-level component of the urbanindex slope we opted for a standard normal prior in all models. We chose not to make assumptions on the sign of the effect of this variable, as it is this variable that we are interested in studying, although we are assuming that its absolute value will be below 1.96 with 95% certainty.

All group-level (zero-centered) priors are Normal, by brms specification **is there a reason???**

For the standard deviation of the hierarchical effects we opted for a relatively weakly informative prior, a *(half)Cauchy*(0, 10). We do not want to place strong constraints on the effect of our variable of interest, hence we 'allow the estimates to fluctuate'.

The Percentage of retirees in each district negatively correlates with the probability of a Democrat winning, but we do not know how strong this effect ought to be. Therefore, for the prior on β_{ret} we chose a distribution centered around a negative number, and with relatively heavy tails, reflecting our uncertainty, for all models.

In Model 4, Pct.Women is not modeled hierarchically. The percentage of women is roughly the same in every district, so we do not expect this covariate to have a strong effect on the probability of either party winning, i.e, we expect β_{women} to be close to zero. So, we set a prior for this slope which is centered around zero and has little variability: a standard normal prior.

The effects of percentage of bachelor degrees and median income are parameterized in 2 hierarchical levels: an average slope across all districts, and a varying slope by group (State or Region), $\beta_{covariate,j}$ or $\beta_{covariate,k}$, which follows a Normal distribution centered at zero with standard deviation modeled at group level (by a hyperprior).

As we expected the population-level effects of both Median Income and Pct Bscs to be positive in some cases and negative in others, we picked symmetric priors for both β_{bsc} and β_{inc} . We are, however, less sure about the on-average-null effect of the Percentage of Bachelor degrees, so for this slope parameter we opted for a prior with 'fatter tails', the standard Cauchy distribution rather than the Normal one, representing a higher degree of uncertainty.

For the hyperparameters, we chose a half standard normal prior for both the standard deviations of $\beta_{bsc,k}$ and $\beta_{inc,j}$. This is a narrow distribution, with most values falling between 0 and 1, as we expect to see weak effects for these covariates, and thus small standard deviations (and positive, as any SD is by definition).

5 Code

6 Results

This section is not on the instructions but is probably the easiest way to talk about the results we got

7 Convergence Diagnostics

One of the fundamentals of Bayesian analysis is its reliance on MCMC sampling. This ensures we have access to both the posterior samples and (in our case) the posterior regression coefficients themselves. All our data analysis was done using BRMS, which

runs on STAN, which itself uses the Hamiltonian Monte Carlo algorithm for the posterior generation.

”Convergence ” in layman’s terms can be described as, ’Do the posterior draws get closer and closer to a specific value?’.

HMC Convergence diagnostics in itself can be a rather extensive topic, so for this project we only consider graphical and summary output based diagnostics, namely: the MCMC trace plots as provided by BRMS, and the Effective Sample Size as provided by the summary output command.

For the first model, we see that all 4 chains are relatively horizontal, and each chain appears to be ’centred’ around a particular value. There are no divergent transitions for any coefficient for this model.

8 Model Comparison

Our four models were built based on somewhat different assumptions about the structure of our data, and all produced slightly different results. We need to know which of these is *better*, that is, which results are more trustworthy and allow us to answer our original research question. To this end, we measured and compared our models’ predictive performance first by looking at absolute in-sample predictive performance, then at relative and finally at the Leave-One-Out statistics to compare out-of-sample Predictive Performance.

Absolute predictive performance metrics directly tell us directly how well the model performs, without looking at other models. To measure absolute predictive performance we used the Root Mean of Squared Error (RMSE). The RMSE for the s -th posterior draw is obtained from the predictive errors, that is, observed outcome y_n minus posterior draw $\hat{y}_n^{(s)}$, squaring those errors and taking the root of their average over all observations, as explained in Equation 7.

$$RMSE^{(s)} = \sqrt{\frac{1}{N} \sum_{n=1}^N (y_n - \hat{y}_n^{(s)})^2} \quad (7)$$

This measure works in a similar way to the R squared statistic that is commonly used to assess the fit of linear models, by evaluating differences between observations and model predictions, but RMSE retains the scale of the response variable, meaning it has a direct interpretation in the context of our problem. Since it is computed for each draw, as opposed to a single point estimate, it takes into account the posterior uncertainty, making it a fully Bayesian measure. [leonora we should talk about this](#) Figure **IT WILL EXIST** shows the histograms of the RMSE with all (4000) draws for each of our models.

[plots of RMSE draws, overlap for comparison]

[interpretation]

Relative predictive performance measures, contrary to absolute ones, do not have any meaning To assess relative predictive performance, we looked at log-likelihood scores, that is, the average of posterior draws’ log-likelihoods for each observation (**FORMULA???**). This is a relative predictive performance measure in the sense that it does not tell us

anything about the model’s predictive performance alone, we need to compare it between different models to establish which is better.

[plot of ll scores or likelihood differences?, overlap]

[interpretation]

Both RMSE and LL scores are in-sample predictive performance metrics. In-sample predictive performance measures evaluate only model predictions for the same observations which were used to fit the model in the first place, therefore they tend to favor more complex models. (In our case, the bigger mmodel (Model 4) was indeed the preferred one using both RMSE and LL scores.?????????????????)

Because we are comparing models with different degrees of complexity, it is essential to check also out-of-sample predictive performance metrics. These metrics are computed by splitting the dataset into training data and test data, fitting the model on the former and assessing the likelihood (ELPD) of the observations in the latter, given the model estimates with the training set.

$$ELPD = \sum_{n=1}^{\tilde{N}} p(\hat{y}_n|y) \quad (8)$$

The way we choose to split the data into training/test sets naturally impacts the ELPD. So, we rely on cross-validation: we do multiple different splits and average over the results. Our chosen method was Leave-One-Out cross-validation, which in theory performs as many splits as observations in the dataset, each time leaving one ”out” as the test data. In practice, a different posterior is not actually computed this many times, but rather an estimate from the full model posterior using importance sampling (PSIS).

[LOO statistics table]

According to the LOO statistics, model 1 is the preferred one.

[pareto k estimates issue and momnet matching?]

9 Prior Sensitivity Analysis

another table with priors here, maybe not all because thats a lot

One of the most important parts of Bayesian Data Analysis is setting the prior distributions. The choice of priors could greatly affect the final results in a model.. (cite prior sensitivity guys) So, we conducted a prior sensitivity analysis, by refitting our model(s) using alternative priors (which also fit our model assumptions) and assessing the impact in our results.

[BRIEFLY explain new priors, graphs comparing them]

10 Limitations and Improvements

11 Changes from Presentation

Please keep track of the changes we make from the presentation

1. stuff probably for exmaple the priors
2. changed the scales for percentages to be on the 100
3. priors: intercept from $N(0,0.5)$ to $N(0,10)$; sd for urban index in bigger model from $\text{Gamma}(2,5)$ to $\text{halfcauchy}(10)$ to match all other models; percentage retirees in bigger model center from -1 to -2, to match other models
4. model order (1-2-3-4 to 3-4-2-1)

12 Conclusion

12.1 Reflection on own learnings

please lets call this subsection something else, this sounds so childish

References

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