

3D Particle-In-Cell study of the Electron Drift Instability in a $E \times B$ discharge

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**ExB Plasmas
Workshop
2022**

Madrid, online event

Motivation

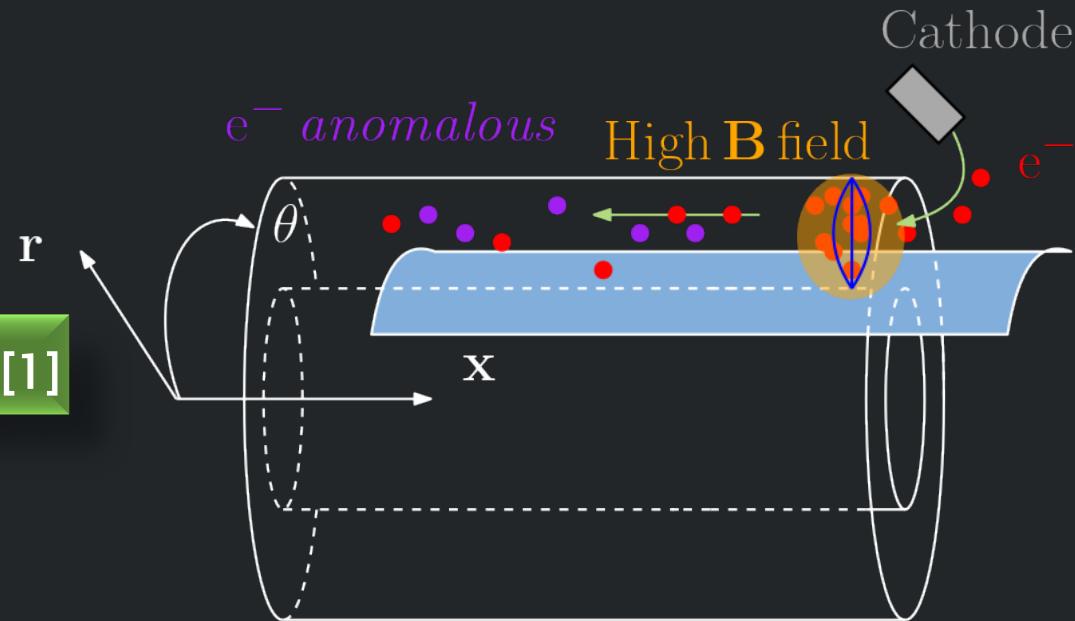
Electron transport classically due to collisions

Actual measurements show a discrepancy with the theory [1]

Anomalous transport likely to be due to EDI [2,3,4]

via additional axial force $\mathbf{R}_{ei} = \langle \delta E_\theta \delta n_e \rangle_\theta \mathbf{x}$

- Numerous studies in
 - 1D θ : [2,5,6],
 - 2D $z - \theta$: [7,8]
 - and 2D $r - \theta$: [9,10]



- [1]: Meezan et al.. (2001). *Physical review. E*. 63:026410
- [2]: Lafleur et al. (2016a) *Physics of Plasmas*, 23(5):053502
- [3]: Lafleur et al.(2016b). *Physics of Plasmas*, 23(5):053503.
- [4]: Charoy, T. (2020). *PhD thesis, Ecole Polytechnique*.
- [5]: Janhunen, S. (2018). *Physics of Plasma*, 25(1):011608
- [6]: Smolyakov, A. et al. (2020). *Plasma Physics Reports*. 46:496-505
- [7]: Adam et al. (2004). *Physics of Plasma*. 11(1):295-305
- [8]: Coche et al. (2014). *Physics of Plasma*. 21(2):023503
- [9]: Héron et al. (2014). *Physics of Plasma*. 20(8):082313
- [10]: Croes et al. (2014). *Plasma Sources Science and Technolgy*. 26(3):034001

Motivation

2D setups artificially prescribed the inherent 3D physics of HTs [1]

3D simulations are required for a more accurate physics.

What can we do ?

- Very scarce attempts of 3D configurations in literature because of computational cost
 - Reduced ion to electron mass ratio m_i/m_e , increase of vacuum permittivity ϵ_0 [2]
 - Miniaturized geometries [3,4]

AVIP PIC: 3D configuration without these assumptions and with an unstructured grid

[1] Tsikata, S. (2010). *Physics of Plasmas*, 17(11):112110

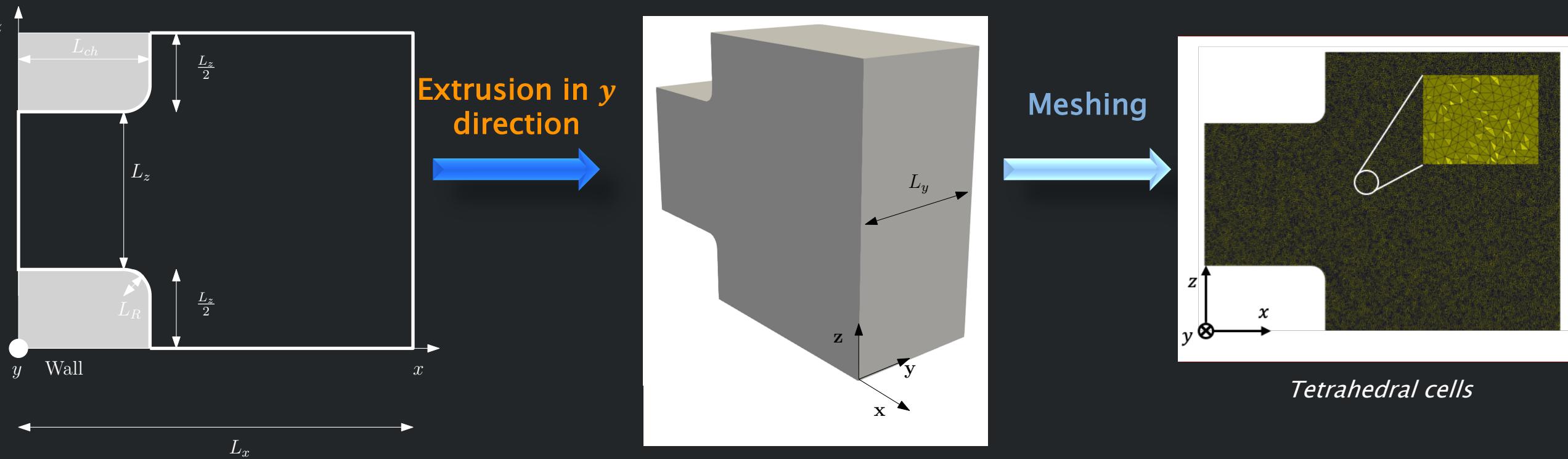
[2] Hirakawa, et al. (1995). In *Proceedings of the 24th International Electric Propulsion Conference*

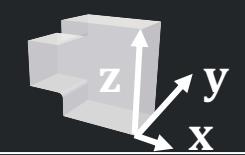
[3] Minelli, P. and Taccogna, F. (2017). *IEEE Transactions on plasma science*, 46(2):219–224

[4] Taccogna, F. and Minelli, P. (2018). *Physics of Plasmas*, 25(6):061208

Numerical setup

- Use CAD to define simulation domain



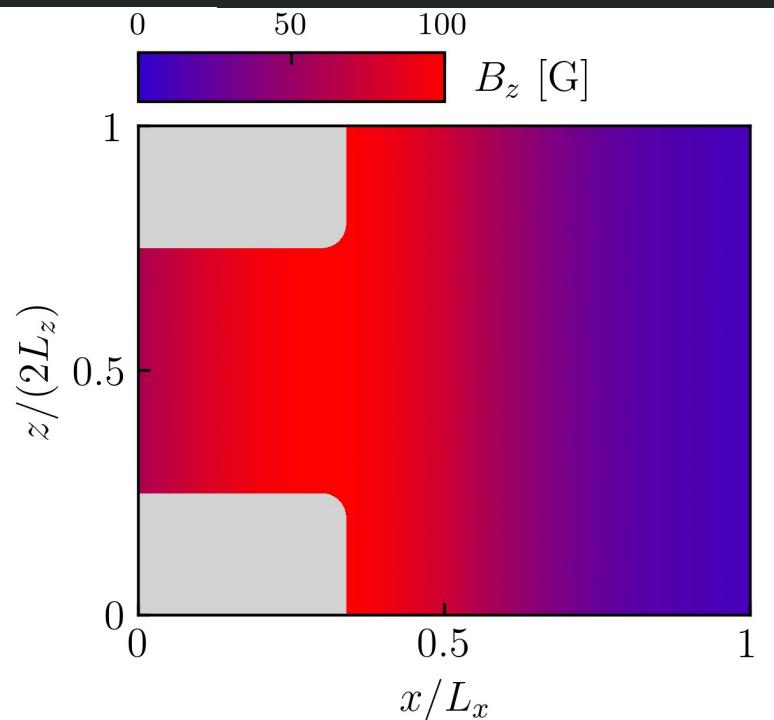
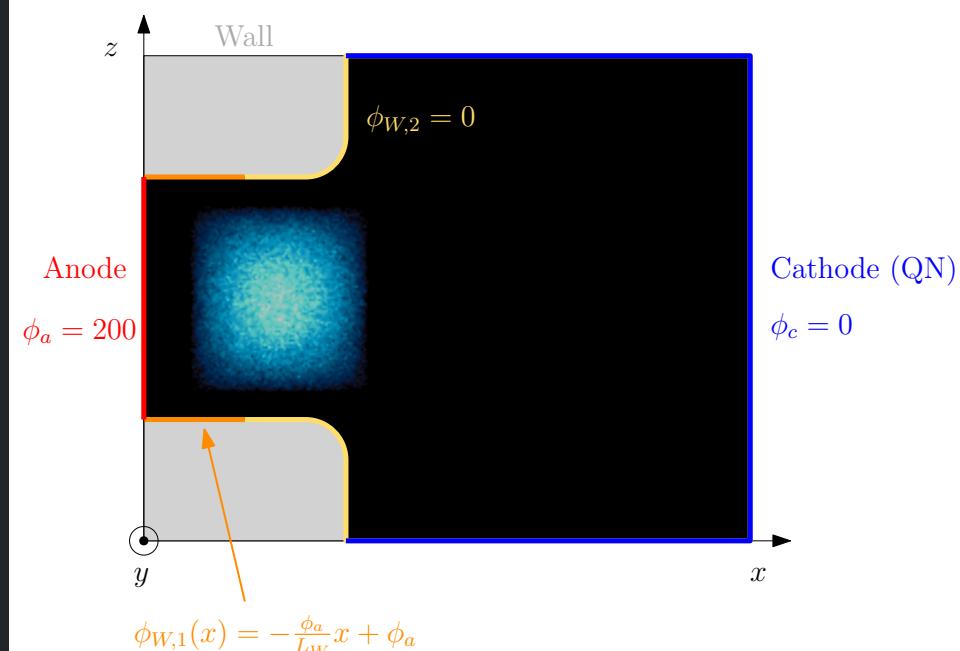


Numerical setup

- Use same framework as in 2D benchmarks[1,2]
 - No curvature effects / Similar BCs
 - Collisionless case
 - Imposed ionization profile $S_i(x, z)$
 - Similar radial magnetic field $\mathbf{B}_z(x)$

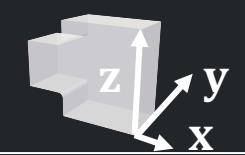
Run parameters

$$13.6 \times 10^6 \text{ cells} \quad L_x \times L_y \times L_z = 2.5 \times 1.28 \times 1 \text{ cm}^3$$
$$\bar{l} = \overline{V_{cell}^{1/3}} = 67 \mu\text{m} \quad n_{X_e^+, 0} = n_{e, 0} = 10^{17} \text{ m}^{-3}$$
$$\Delta t = 5 \text{ ps} \quad t_{total} = 10 \mu\text{s}$$



[1] Charoy, T. et al (2019). PSST, 28(10), 105010
[2] Villafana, W. et al (2021). PSST, 30(7), 075002

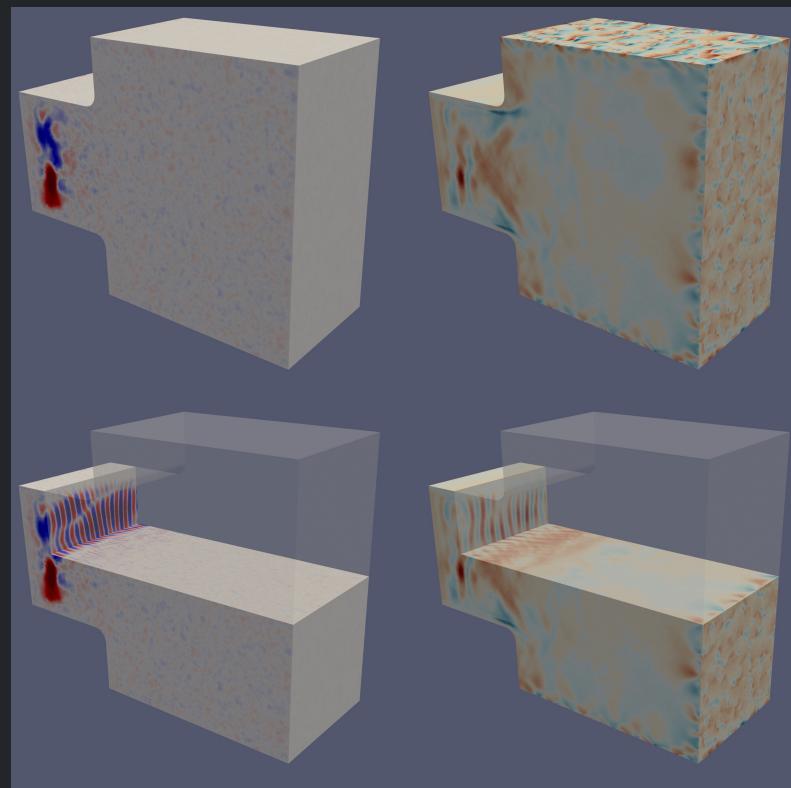
2000 CPUs
40 days of continuous run
3.5 billion particles



Results: timeline

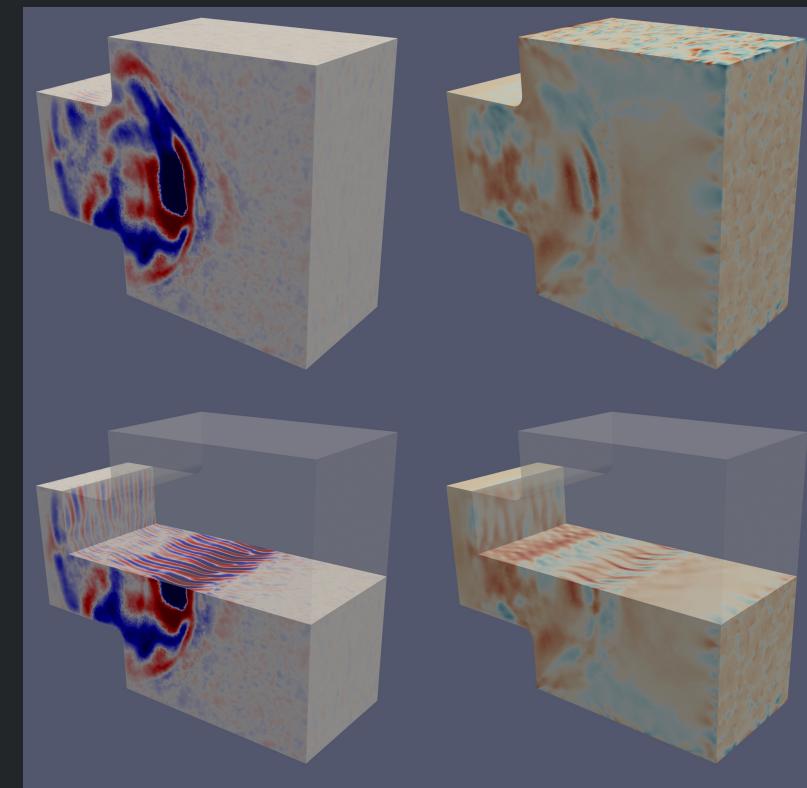
- EDI grows near anode

$t = 0.20\mu s$



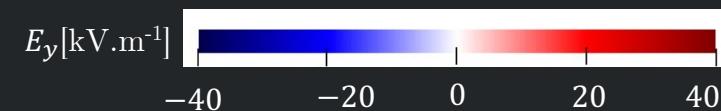
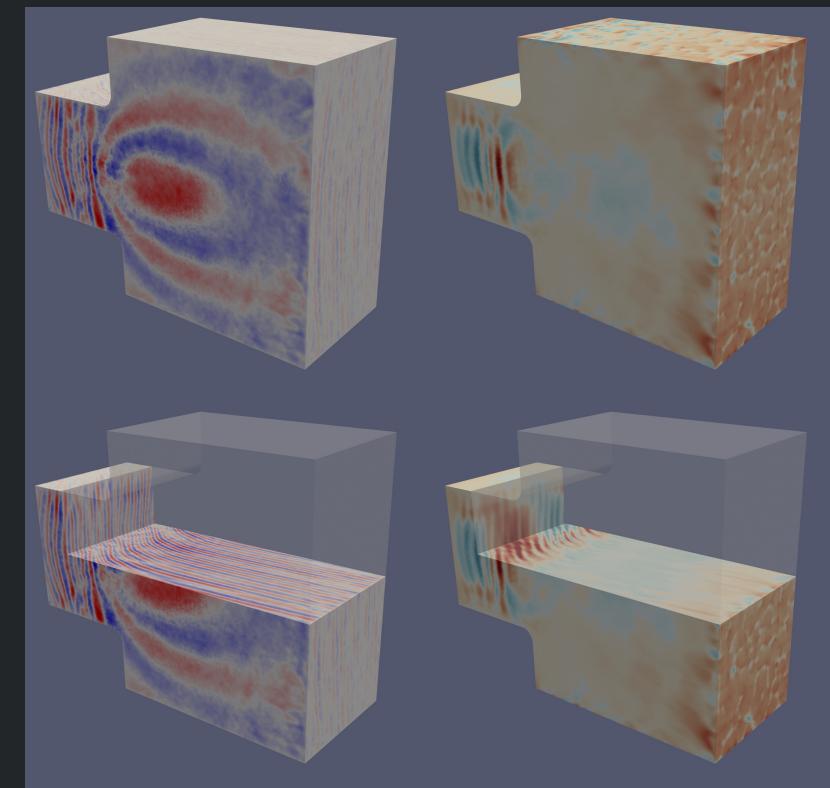
- EDI propagates downstream

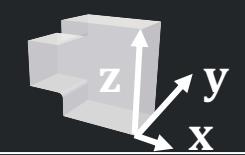
$t = 0.90\mu s$



- EDI in 3D and signature of MTSI?

$t = 5\mu s$

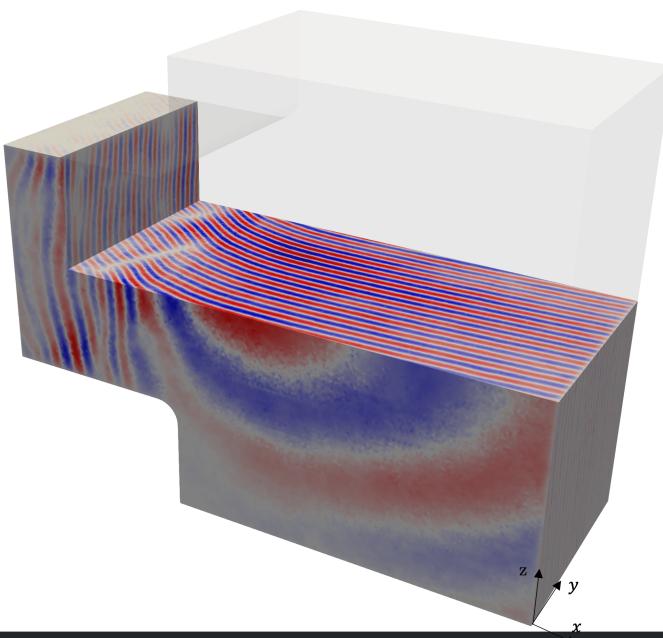




Results: mode reconstruction via DMD

ECDI

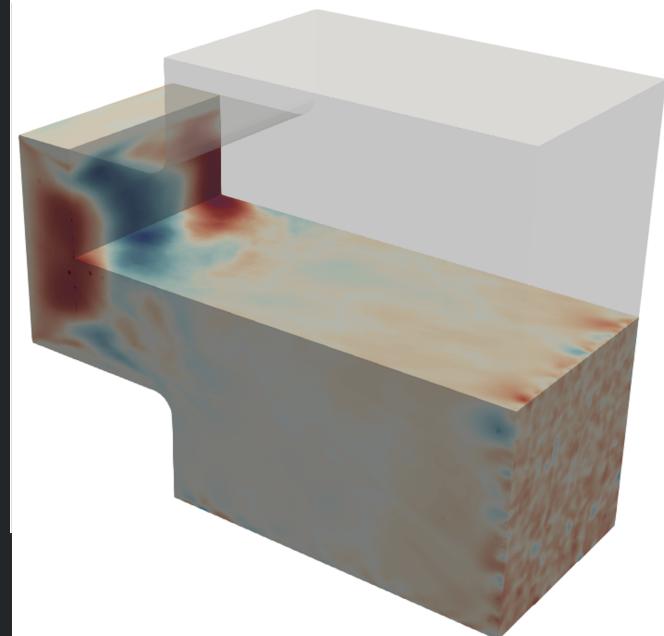
$$E_y [\text{kV.m}^{-1}]$$



- Mainly driven by k_x, k_y in channel
- Mainly driven by k_x, k_z in the plume

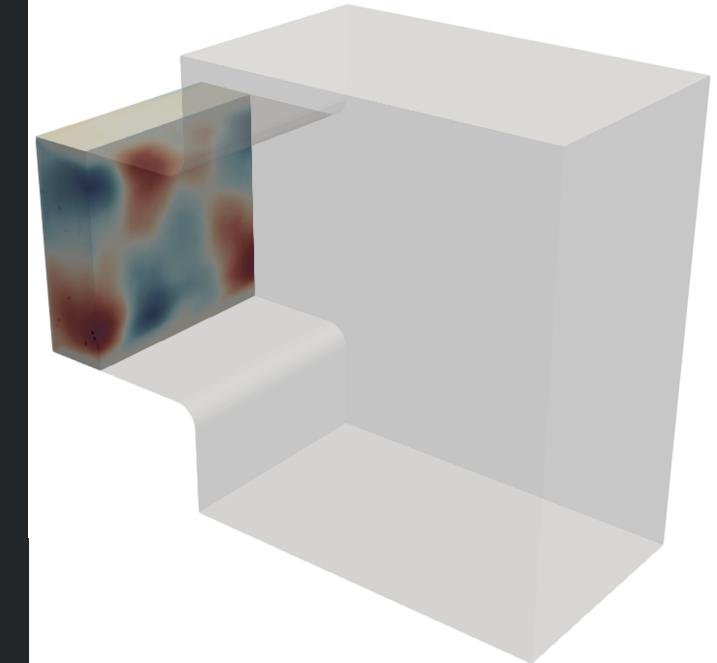
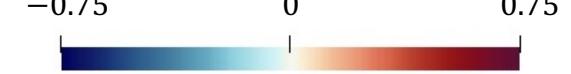
Signature of MTSI?

$$J_{e,x} [\text{kA.m}^{-2}]$$

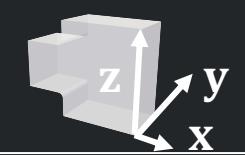


- Long azimuthal wavelength

$$J_{e,z} [\text{kA.m}^{-2}]$$



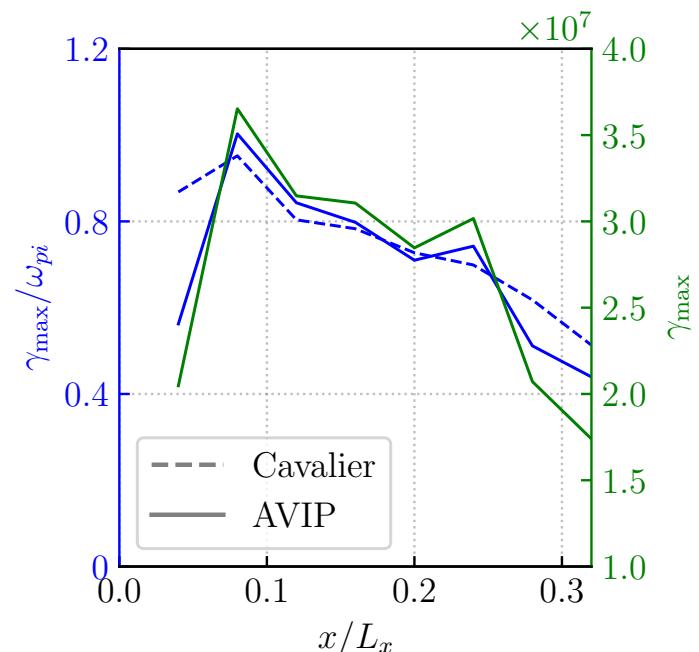
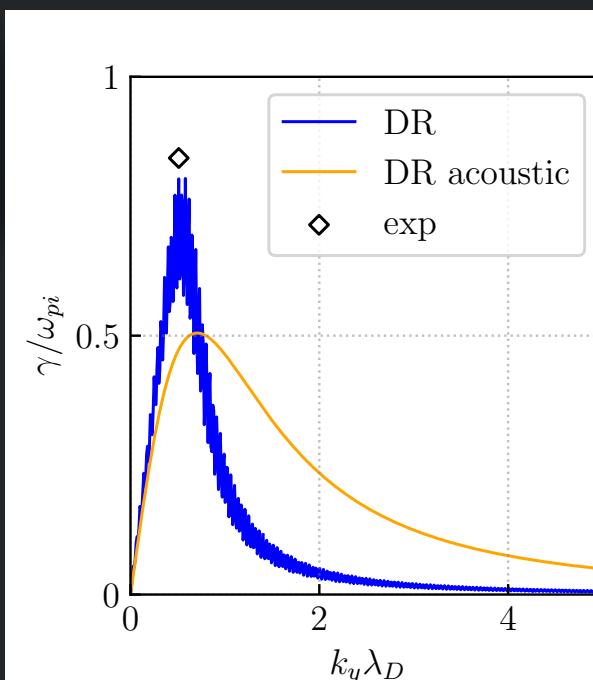
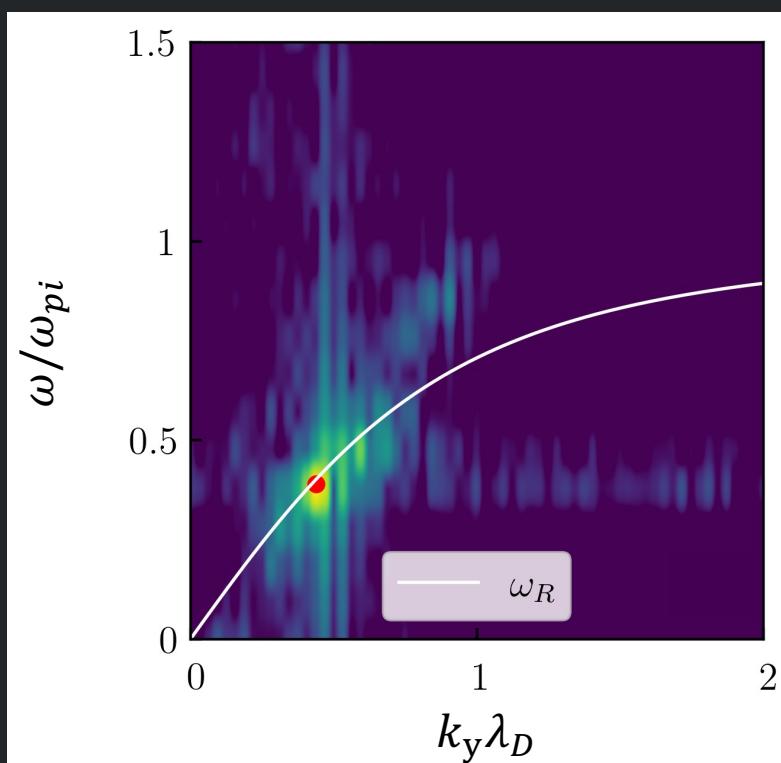
- Also a radial pattern



EDI theoretical analysis

✓ During transient, main E_y mode

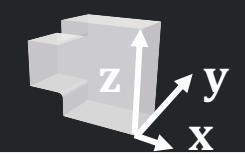
corresponds to ECDI expected growth rate γ [1]



✓ At steady state, the ECDI has transitioned
to an ion acoustic wave[2]

[1] Cavalier, et al., Physics of Plasmas, 20(8):082107. (2013)

[2]: Lafleur et al.(2016b). Physics of Plasmas, 23(5):053503

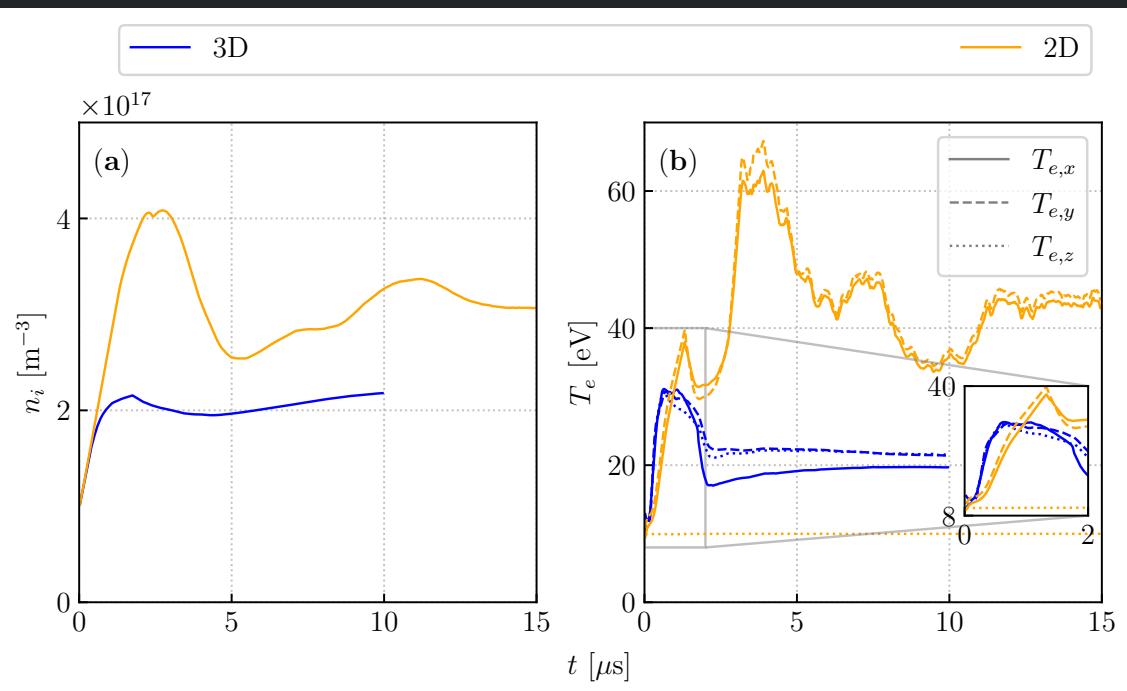


EDI theoretical analysis

- Comparison with pure 2D case axial-azimuthal

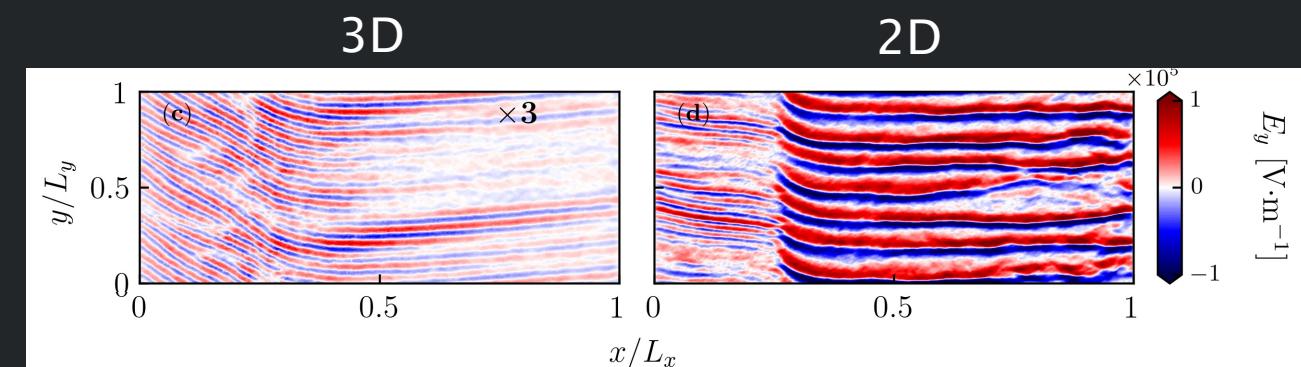
ECDI saturates at a higher energy level in 2D

1. Pure 2D has a hotter and denser plasma

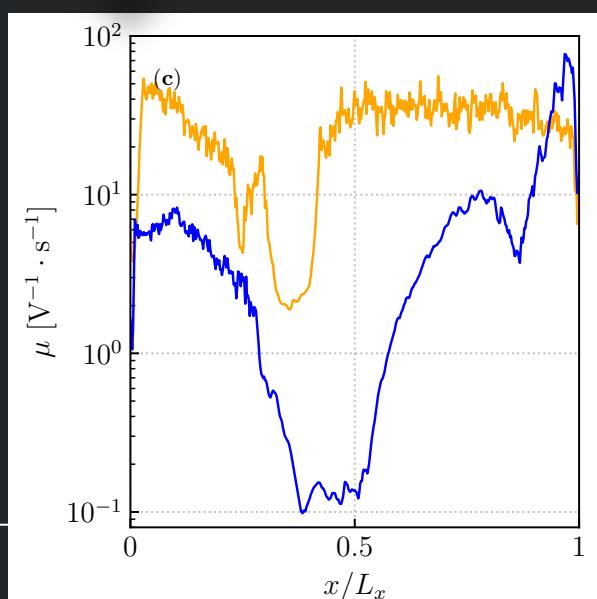


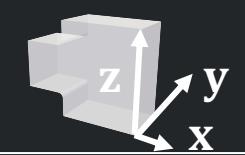
Lower axial mobility in 3D

3D PIC study of the EDI in a ExB discharge



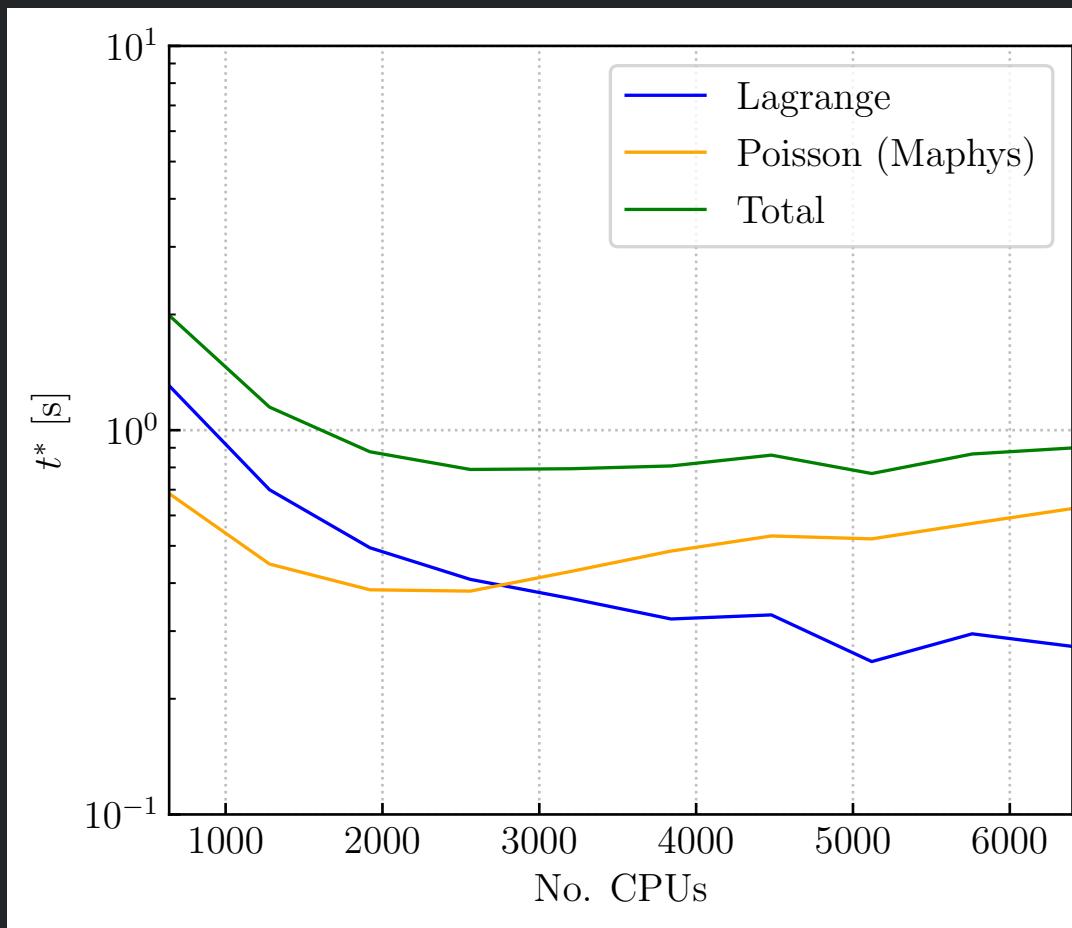
Higher azimuthal amplitudes
 $\langle \delta E_\theta \delta n_e \rangle_\theta$





What's the cost?

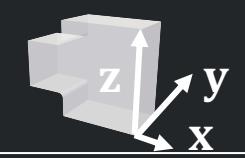
- MPI Domain decomposition over ~2.26 million nodes for 3.5 billion particles



Good strong scalability for
Lagrangian kernel

Poisson solver remains limiting factor

1-1.5 months of simulation for
1.4M CPUh



Conclusion

➤ Summary

- ✓ The 3D structure of the EDI was successfully identified using an unstructured framework based on domain decomposition
 - Poisson solver remains the limiting factor for 3D PIC calculations
- ✓ The anomalous mobility is lower in 3D than in 2D and is affected by the possible signature of the MTSI

➤ Ongoing work

- ⚙️ Ongoing advanced study with LAPLACE laboratory on similar 3D setup

Acknowledgments

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- We acknowledge financial support from a Safran Aircraft Engines within the project POSEIDON (ANR-16-CHIN-003- 01)