
LEMMA (PROOF BY CONTRAPOSITIVE): $\Gamma, \neg B \vdash \neg A \implies \Gamma, A \vdash B$

$$\frac{\frac{\overline{\Gamma, A \vdash B}^{\text{L}\supset} \quad \overline{\Gamma, A, \perp \vdash B}^{\text{id}}}{\Gamma, A, \neg B \vdash B}^{\text{L}\supset} \quad \overline{\Gamma, A, B \vdash B}^{\text{id}}}{\Gamma, A \vdash B}^{\text{EM}}$$